

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB RECORD

Bio Inspired Systems (23CS5BSBIS)

Submitted by

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in partial fulfillment for the award of the degree of

BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING

(Autonomous Institution under VTU)

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CERTIFICATE

This is to certify that the Lab work entitled “ Bio Inspired Systems (23CS5BSBIS)” carried out by **Hitesh Sharma (1BM23CS114)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

Sowmya T Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
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Github Link:

https://github.com/Hitesh6747/BIS_LAB

Program 1

We have multiple jobs and limited resources and we need to assign them to minimize completion time, cost or maximize efficiency.

ALGORITHM:

LAB → 1: Genetic Algorithm for Optimization Problem:

Date: / / Page:

- Select initial population
- Calculate the fitness
- Selecting the mating pool
- Cross Over
- Mutation

Expected Output = $f(x_i)$

Prob = $\frac{f(x)}{\sum f(x)}$

$= \frac{144}{1155}$

$= 0.1247$

Expected Output = $f(x_i)$

Aug ($\sum f(x_i)$) = 288.75

$= 10.49$

1. $x \rightarrow 0-31$

String No.	Initial Population	Value	$f(x) = x^2$ (Fitness)	Prob	% Prob	Expect	Actual
1	01100	12	144	0.1247	0.47	0.47	1
2	11001	25	625	0.5411	5.11	2.16	2
3	00101	5	25	0.0216	2.16	0.08	0
4	10011	19	361	0.3126	3.126	1.25	1
Sum			1155	1.0	1.00	4	
Average			288.75	0.25	25	1	
Maximum			625	0.5411	54.11	2.16	

3. Selecting Mating Pool

String No.	Mating Pool	Cross Over bit	Offspring (New member)	x-value	$f(x) = x^2$
1	01100	4	01101	13	169
2	11001		11000	24	576
3	11001	2	11011	29	729
4	10011		10001	17	289

Fitness $f(x) = x^2$		Date	Page
Sum	1763		
Average	1740.75		
Maximum	729		
4.	Cross Over (It is chosen Randomly).		
5.	Mutation		
Offspring	Mutation	offspring	
After Crossover	(Genes)	after mutation	
1	01101	10000	29
2	11000	00000	24
3	11011	00000	23
4	10001	00101	20
Sum			2546
Average			636.5
Maximum			841
Output:			
Gen 0: Best $x = 30$		$f(x) = 900$	
Gen 1: Best $x = 30$		$f(x) = 900$	
Gen 2: Best $x = 30$		$f(x) = 900$	
Gen 3: Best $x = 50$		$f(x) = 900$	
Gen 4: Best $x = 31$		$f(x) = 961$	
Gen 5: Best $x = 31$		$f(x) = 961$	
Gen 6: Best $x = 31$		$f(x) = 961$	
Best Solution: $x = 31$		$f(x) = 961$	
Application: $x = 31$		$f(x) = 961$	

```
Code: import numpy as np
```

```
target_position = np.array([10.0, 10.0])
```

```
num_particles = 30
```

```
num_iterations = 50
```

```
w = 0.7
```

```
c1 = 1.5
```

```
c2 = 1.5
```

```
v_max = 1.0
```

```
positions = np.random.uniform(0, 10, (num_particles, 2))
```

```
velocities = np.random.uniform(-1, 1, (num_particles, 2))
```

```
personal_best_positions = positions.copy()
```

```
personal_best_values = np.full(num_particles, np.inf)
```

```
global_best_position = np.zeros(2)
```

```
global_best_value = np.inf
```

```
def fitness(position, velocity):
```

```

distance = np.linalg.norm(position - target_position)
smoothness_penalty = np.linalg.norm(velocity)
return distance + 0.3 * smoothness_penalty

for t in range(num_iterations):
    for i in range(num_particles):
        fit = fitness(positions[i], velocities[i])
        if fit < personal_best_values[i]:
            personal_best_values[i] = fit
            personal_best_positions[i] = positions[i].copy()
        if fit < global_best_value:
            global_best_value = fit
            global_best_position = positions[i].copy()
    for i in range(num_particles):
        r1, r2 = np.random.rand(2)
        velocities[i] = (
            w * velocities[i]
            + c1 * r1 * (personal_best_positions[i] - positions[i])
            + c2 * r2 * (global_best_position - positions[i])
        )
        velocities[i] = np.clip(velocities[i], -v_max, v_max)
        positions[i] += velocities[i]

print("Final optimized position:", global_best_position)
print("Minimum fitness value:", global_best_value)

```

Program 2

The Travelling Salesman Problem (TSP) asks for the shortest possible route that visits a given set of cities exactly once and returns to the starting city. The provided text describes using a Genetic Algorithm to solve this by evolving city sequences (chromosomes) through selection, crossover, and mutation to minimize the total tour distance.

Algorithm:

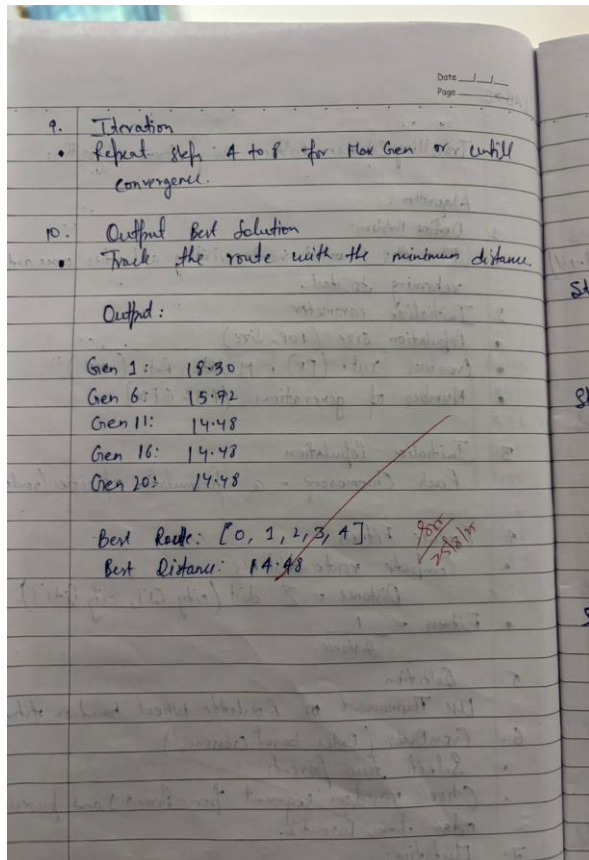
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Travelling Salesman Problem Using Genetic Algorithms

Algorithm:

1. Define Problem:
 - Find the shortest route visiting all cities once and returning to start.
2. Initialize Parameter
 - Population size (POP-size)
 - Crossover Rate (CR), Mutation Rate (MR)
 - Number of generations (MAX GEN)
3. Initialize Population
 - Each Chromosome = a permutation of cities (route)
4. Evaluate Fitness
 - Compute route distance
 - $Distance = \sum dist(city[i], city[i+1])$
 - $Fitness = \frac{1}{Distance}$
5. Selection
 - Use Tournament or Roulette Wheel based on fitness
6. Crossover (Order-based crossover)
 - Select two parents
 - Choose random segment from Parent 1 and preserve order from Parent 2
7. Mutation
 - Swap into cities in the route with a small probability.
8. Gene Expression
 - The Chromosome directly represents a route

841
576
729
400
2546
636.5
841



Code:

```
import random
import math

cities = [(0,0), (1,5), (5,2), (6,6), (8,3)]
num_cities = len(cities)
population_size = 30
generations = 200
crossover_rate = 0.8
mutation_rate = 0.2

def distance(a, b):
    return math.sqrt((a[0]-b[0])**2 + (a[1]-b[1])**2)

def tour_length(chromosome):
    length = 0
```



```

    for i in range(num_cities):
        length += distance(cities[chromosome[i]],
cities[chromosome[(i+1)%num_cities]])
    return length

def fitness(chromosome):
    return 1 / tour_length(chromosome)

def initial_population():
    population = []
    for _ in range(population_size):
        chromosome = list(range(num_cities))
        random.shuffle(chromosome)
        population.append(chromosome)
    return population

def selection(population):
    contenders = random.sample(population, 3)
    contenders.sort(key=lambda c: fitness(c), reverse=True)
    return contenders[0]

def crossover(p1, p2):
    if random.random() < crossover_rate:
        a, b = sorted(random.sample(range(num_cities), 2))
        child = [-1]*num_cities
        child[a:b] = p1[a:b]
        fill = [x for x in p2 if x not in child]
        j = 0
        for i in range(num_cities):
            if child[i] == -1:
                child[i] = fill[j]
                j += 1
        return child
    return p1[:]

def mutate(chromosome):
    if random.random() < mutation_rate:
        a, b = random.sample(range(num_cities), 2)
        chromosome[a], chromosome[b] = chromosome[b], chromosome[a]
    return chromosome

population = initial_population()
best_solution = None
best_distance = float("inf")

```

```
for g in range(generations):
    new_pop = []
    for _ in range(population_size):
        parent1 = selection(population)
        parent2 = selection(population)
        child = crossover(parent1, parent2)
        child = mutate(child)
        new_pop.append(child)
    population = new_pop
    for chromo in population:
        d = tour_length(chromo)
        if d < best_distance:
            best_distance = d
            best_solution = chromo

print("Best Tour (order of cities):", best_solution)
print("Best Tour Distance:", best_distance)
```

Program 3

Particle Swarm Optimization for smooth character movement using position and velocity

Algorithm:

Lab → B

Date: / /
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Particle Swarm Optimization For Smooth Character Movement Using Position and Velocity

Algorithm:

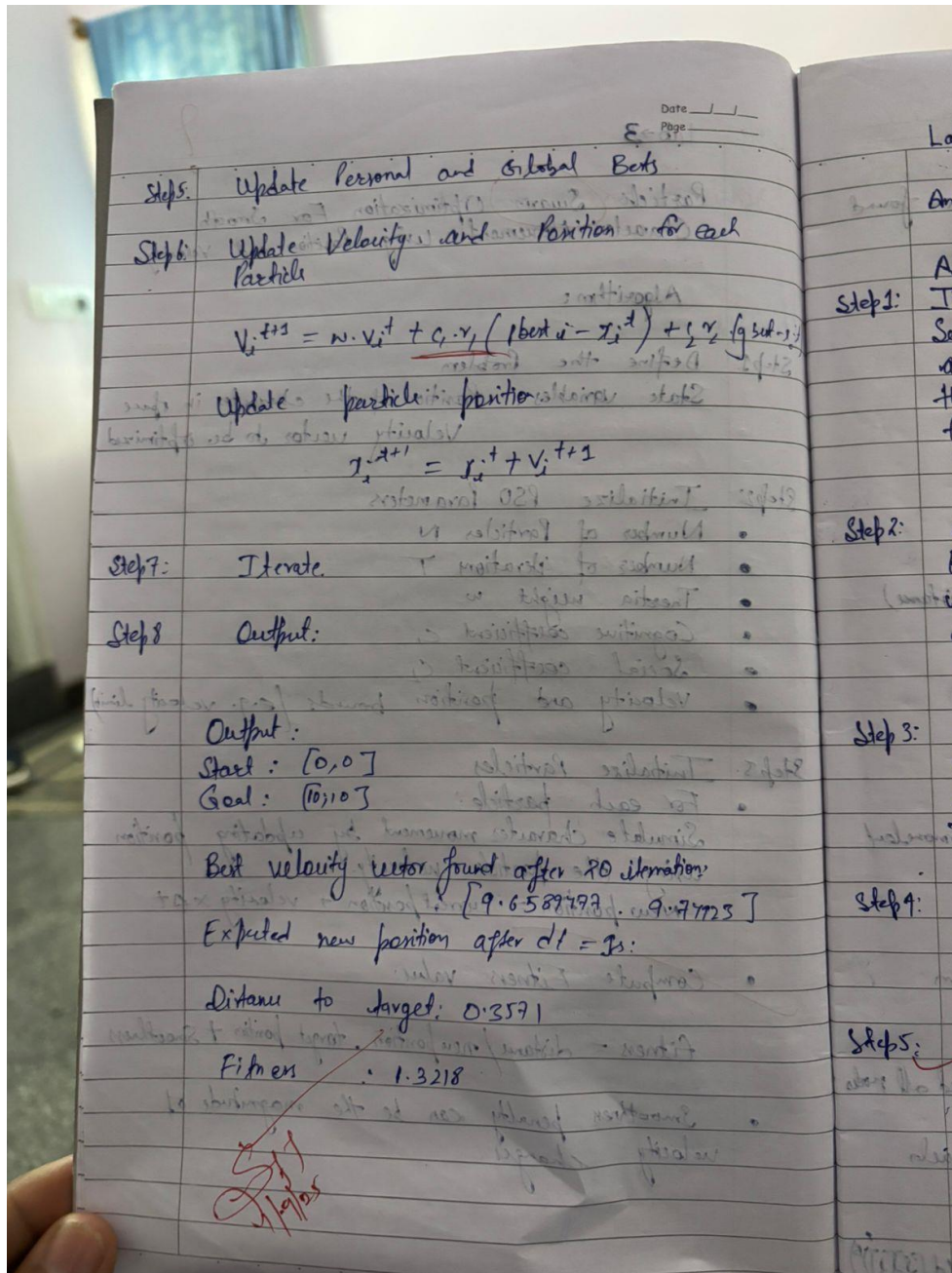
Step 1: Define the Problem
State variables: Position of the character in space
Velocity vector to be optimized

Step 2: Initialize PSO Parameters

- Number of Particles N
- Number of iterations T
- Inertia weight w
- Cognitive coefficient c_1
- Social coefficient c_2
- Velocity and position bounds (e.g. velocity limit)

Step 3: Initialize Particles

- For each particle:
Simulate character movement by updating position using the particle velocity.
new position = current position + velocity $\times \Delta t$
- Compute Fitness value:
fitness = distance / new position, target position + smoothness
- Smoothness penalty can be the magnitude of velocity changes.



Code:

```

import numpy as np

target_position = np.array([10.0, 10.0])
num_particles = 30
num_iterations = 50
w = 0.7
c1 = 1.5
c2 = 1.5
  
```

```

v_max = 1.0

positions = np.random.uniform(0, 10, (num_particles, 2))
velocities = np.random.uniform(-1, 1, (num_particles, 2))
personal_best_positions = positions.copy()
personal_best_values = np.full(num_particles, np.inf)
global_best_position = np.zeros(2)
global_best_value = np.inf

def fitness(position, velocity):
    distance = np.linalg.norm(position - target_position)
    smoothness_penalty = np.linalg.norm(velocity)
    return distance + 0.3 * smoothness_penalty

for t in range(num_iterations):
    for i in range(num_particles):
        fit = fitness(positions[i], velocities[i])
        if fit < personal_best_values[i]:
            personal_best_values[i] = fit
            personal_best_positions[i] = positions[i].copy()
        if fit < global_best_value:
            global_best_value = fit
            global_best_position = positions[i].copy()
    for i in range(num_particles):
        r1, r2 = np.random.rand(2)
        velocities[i] = (
            w * velocities[i]
            + c1 * r1 * (personal_best_positions[i] - positions[i])
            + c2 * r2 * (global_best_position - positions[i])
        )
        velocities[i] = np.clip(velocities[i], -v_max, v_max)
        positions[i] += velocities[i]

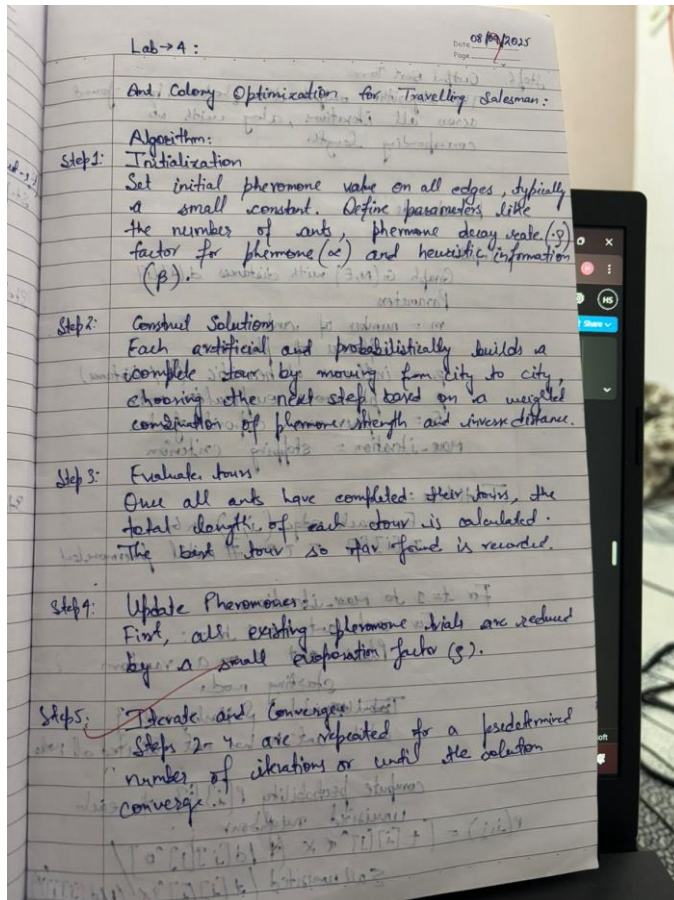
print("Final optimized position:", global_best_position)
print("Minimum fitness value:", global_best_value)

```

Program 4

Ant Colony Optimization (ACO) for the Travelling Salesman :

Algorithm:



Step 6: Output Best Tour
 The algorithm outputs the shortest tour found after all iterations, along with its corresponding length.

Pseudo-code:
 Input: undirected graph $G(N, E)$ with distances $d(i, j)$
 Parameters:
 m = number of ants
 α = influence of pheromone
 β = influence of heuristic $(1/distance)$
 ρ = evaporation rate
 Q = pheromone deposit factor
 Max-iteration = stopping criterion

Initialization:
 For each edge (i, j) in graph
 $\tau(i, j) = \tau_0$ // initial pheromone

For $t = 1$ to max-iterations
 For each ant $k = 1$ to m :
 e.g. start ant k on a random starting node
 While ant k has not visited all nodes
 Compute probability $P(i, j)$ for each unvisited neighbour

$$P(i, j) = \frac{[\tau(i, j)]^\alpha \times [1/d(i, j)]^\beta}{\sum_{j \text{ unvisited}} [\tau(i, j)]^\alpha \times [1/d(i, j)]^\beta}$$

Choose next node j based on probability $P(i, j)$
 Move ant k to node j
 Add j to Tabu k
 Compute tour length L_k for ant k
 Update pheromone:
 For each edge (i, j) :
 $\tau(i, j) = (1 - \rho) \times \tau(i, j)$
 For each ant k :
 If ant k used edge (i, j) in its tour
 $\tau(i, j) + Q/L_k$
 Keep track of the best solution found so far

Output:
 Best tour and its length
 Distance matrix:

0	10	12	11
10	0	9	8
12	9	0	7
11	8	7	0

ants $m = 4$
 $\alpha = 1.0$
 $\beta = 2.0$
 $\rho = 0.5$
 $Q = 100$
 $\tau_0 = 1.0$

heuristic $\eta(i, j) = 1/d(i, j)$

for each edge

(ii) Solution Path:

~~$A \rightarrow B \rightarrow D \rightarrow C \rightarrow A = (10 + 8 + 7 + 12)$~~

~~Tour length: 37~~

~~$\frac{Q}{L_k}$~~

Code:

```
import numpy as np
import random
import math

# City coordinates
cities = [(0,0), (1,5), (5,2), (6,6), (8,3)]
num_cities = len(cities)

# Parameters
num_ants = 20
num_iterations = 100
alpha = 1.0      # pheromone importance
beta = 5.0       # distance importance
rho = 0.5        # pheromone evaporation rate
Q = 100         # pheromone deposit factor

# Distance matrix
dist_matrix = np.zeros((num_cities, num_cities))
for i in range(num_cities):
    for j in range(num_cities):
        if i != j:
            dist_matrix[i][j] = math.sqrt((cities[i][0]-cities[j][0])**2 +
(cities[i][1]-cities[j][1])**2)
        else:
            dist_matrix[i][j] = np.inf

# Initialize pheromone matrix
pheromone = np.ones((num_cities, num_cities))

def probability(i, unvisited, pheromone, dist):
    pher = np.array([pheromone[i][j] ** alpha for j in unvisited])
    vis = np.array([(1.0 / dist[i][j]) ** beta for j in unvisited])
    p = pher * vis
    return p / np.sum(p)

def tour_length(tour):
    return sum(dist_matrix[tour[i]][tour[(i+1)%num_cities]] for i in
range(num_cities))

best_tour = None
best_distance = float("inf")

for _ in range(num_iterations):
    all_tours = []
```



```

all_distances = []
for ant in range(num_ants):
    start = random.randint(0, num_cities - 1)
    tour = [start]
    unvisited = list(range(num_cities))
    unvisited.remove(start)
    while unvisited:
        probs = probability(tour[-1], unvisited, pheromone, dist_matrix)
        next_city = random.choices(unvisited, weights=probs)[0]
        tour.append(next_city)
        unvisited.remove(next_city)
    all_tours.append(tour)
    all_distances.append(tour_length(tour))
    if all_distances[-1] < best_distance:
        best_distance = all_distances[-1]
        best_tour = tour
pheromone *= (1 - rho)
for tour, dist in zip(all_tours, all_distances):
    deposit = Q / dist
    for i in range(num_cities):
        a, b = tour[i], tour[(i+1)%num_cities]
        pheromone[a][b] += deposit
        pheromone[b][a] += deposit

print("Best Tour (order of cities):", best_tour)
print("Best Tour Distance:", best_distance)

```

Program 5

Cuckoo Search Algorithms: For JOB SCHEDULING

Algorithm:

LAB 5

Date: ____/____/____
Page: ____

Cuckoo Search Algorithm for Job Scheduling

Algorithm:

1. Initialize population (nests):
 - Generate an initial population of n solutions (nests).
 - Each solution represents a possible job schedule.
2. Fitness Evaluation:
 - Calculate the fitness of each schedule.
$$\text{fitness} = 1 / \text{makespan}$$
3. Generate new solutions (Levy flights):
 - For each cuckoo (solution), create a new solution by Levy Flight.
4. Evaluate new solution:
 - If the new solution is better than a randomly chosen existing solution, replace it.
5. Abandon fraction of nests (p_a):
 - With probability p_a , some of the worst solutions are abandoned and replaced with new random solutions.
6. Keep Best Solutions:
7. Repeat until stopping condition.
8. Return the best schedule.

Date / /
Page

Output:

1. A: {J1, J2} → 5+7 = 12
B: {J3, J4} → 3+9 = 12
Makespan = 12

2. Another Arrangement
A: {J1, J3} → 5+3 = 8
B: {J2, J4} → 7+9 = 16
Makespan = 16

3. A: {J4, J1} → 9+5 = 14
B: {J2, J3} → 7+3 = 10
Makespan = 14

4. A: {J1, J2, J3} → 5+7+3 = 15
B: {J4} → 9
Makespan = 15

Best solution:

Machine A: J1 (5) + J2 (7) = 12
Machine B: J3 (3) + J4 (9) = 12

San
20/11/19

CODE:

```
import numpy as np
import random

# Number of jobs and machines
num_jobs = 6
num_machines = 3
```

```

# Processing time matrix (rows = jobs, columns = machines)
processing_time = np.array([
    [5, 2, 4],
    [3, 6, 1],
    [4, 3, 5],
    [2, 4, 3],
    [6, 5, 2],
    [7, 3, 4]
])

# Parameters
num_nests = 15
max_iterations = 100
pa = 0.25 # discovery rate of alien eggs

def fitness(schedule):
    machine_loads = [0] * num_machines
    for job, machine in enumerate(schedule):
        machine_loads[machine] += processing_time[job][machine]
    return max(machine_loads)

def levy_flight(Lambda):
    sigma = (np.math.gamma(1 + Lambda) * np.sin(np.pi * Lambda / 2) /
              (np.math.gamma((1 + Lambda) / 2) * Lambda * 2 ** ((Lambda - 1) / 2)))
    ** (1 / Lambda)
    u = np.random.randn() * sigma
    v = np.random.randn()
    step = u / abs(v) ** (1 / Lambda)
    return step

def get_new_nest(nest):
    new_nest = nest.copy()
    step = int(abs(levy_flight(1.5)) * num_jobs) % num_machines
    job_to_change = random.randint(0, num_jobs - 1)
    new_machine = (new_nest[job_to_change] + step) % num_machines
    new_nest[job_to_change] = new_machine
    return new_nest

# Initialize nests (random assignments of jobs to machines)
nests = [np.random.randint(0, num_machines, num_jobs).tolist() for _ in
range(num_nests)]
fitness_values = [fitness(n) for n in nests]
best_nest = nests[np.argmin(fitness_values)]
best_fitness = min(fitness_values)

```

```

for t in range(max_iterations):
    new_nests = []
    for nest in nests:
        new_nest = get_new_nest(nest)
        if fitness(new_nest) < fitness(nest):
            new_nests.append(new_nest)
        else:
            new_nests.append(nest)
    nests = new_nests
    # Discovery and randomization
    for i in range(num_nests):
        if random.random() < pa:
            nests[i] = np.random.randint(0, num_machines, num_jobs).tolist()
    fitness_values = [fitness(n) for n in nests]
    current_best = nests[np.argmin(fitness_values)]
    current_fitness = min(fitness_values)
    if current_fitness < best_fitness:
        best_fitness = current_fitness
        best_nest = current_best

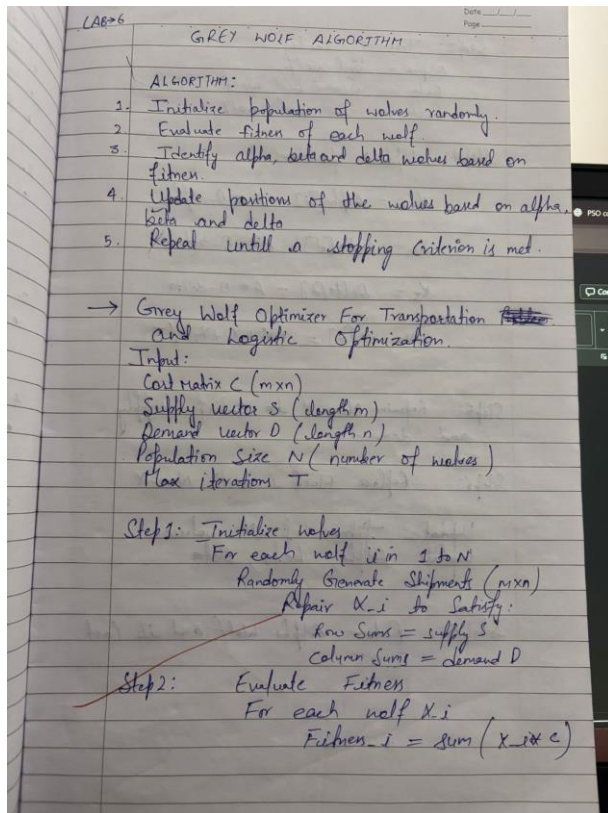
print("Best job-to-machine assignment:", best_nest)
print("Minimum makespan (total completion time):", best_fitness)

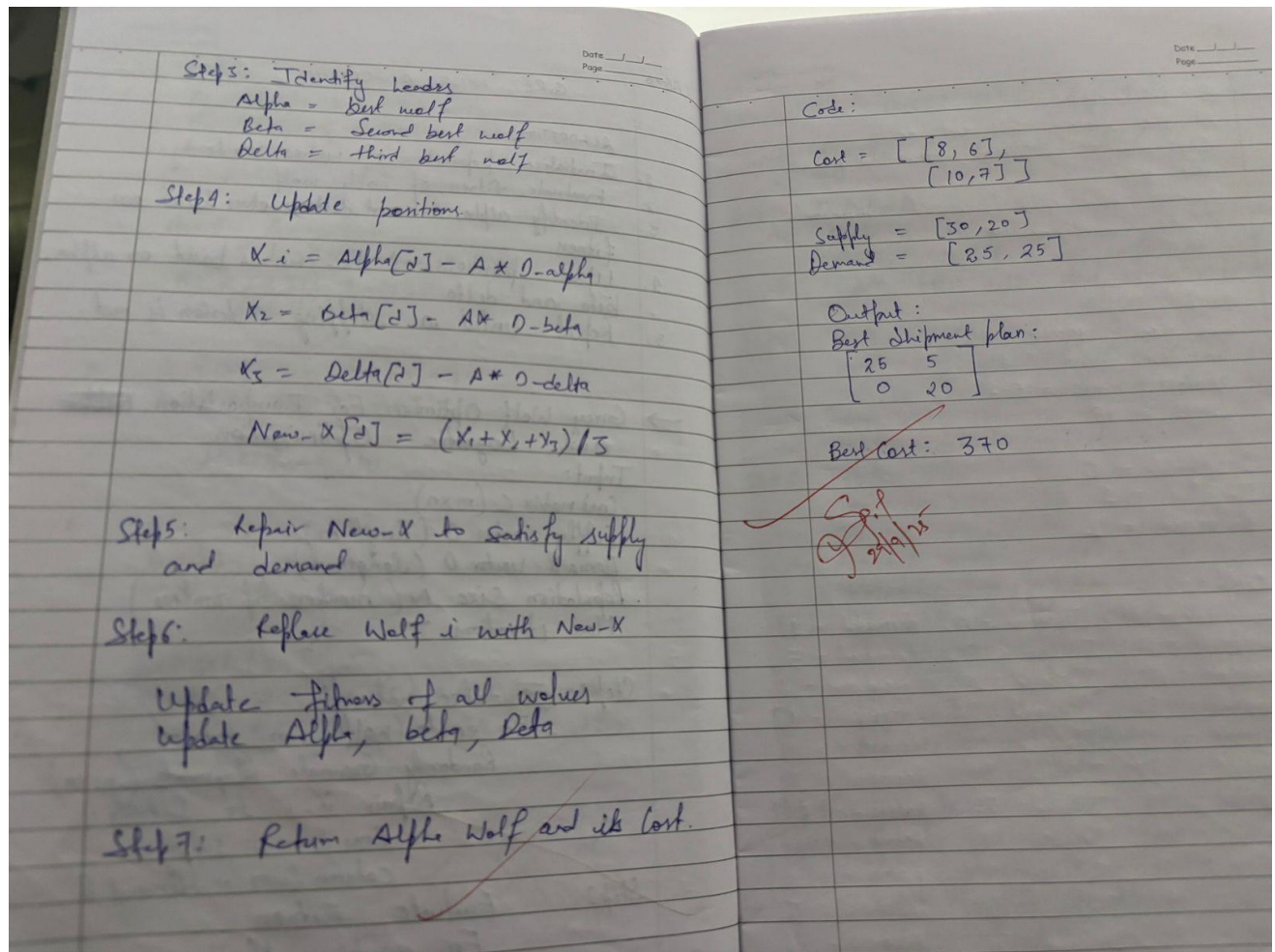
```

Program 6

Using the Grey Wolf Optimizer (GWO), For Transport and Logistics Transportation

Algorithm:





Code

```

import numpy as np
import random

# Example: cost matrix (rows = sources, columns = destinations)
cost = np.array([
    [8, 6, 10, 9],
    [9, 12, 13, 7],
    [14, 9, 16, 5]
])

# Supply and demand
supply = [20, 30, 25]
demand = [10, 15, 25, 25]

num_sources = len(supply)
num_destinations = len(demand)

```

```

num_variables = num_sources * num_destinations

# Grey Wolf Optimizer parameters
num_wolves = 20
max_iter = 100
lb, ub = 0, max(max(supply), max(demand))

# Fitness: total transportation cost + penalty for constraint violation
def fitness(x):
    alloc = x.reshape((num_sources, num_destinations))
    total_cost = np.sum(alloc * cost)
    supply_violation = np.sum(np.abs(np.sum(alloc, axis=1) - supply))
    demand_violation = np.sum(np.abs(np.sum(alloc, axis=0) - demand))
    penalty = 100 * (supply_violation + demand_violation)
    return total_cost + penalty

# Initialize wolves
wolves = np.random.uniform(lb, ub, (num_wolves, num_variables))
fitness_values = np.array([fitness(w) for w in wolves])
alpha, beta, delta = np.argsort(fitness_values)[:3]
alpha_pos, beta_pos, delta_pos = wolves[alpha], wolves[beta], wolves[delta]

for t in range(max_iter):
    a = 2 - t * (2 / max_iter)
    for i in range(num_wolves):
        r1, r2 = np.random.rand(num_variables), np.random.rand(num_variables)
        A1 = 2 * a * r1 - a
        C1 = 2 * r2
        D_alpha = abs(C1 * alpha_pos - wolves[i])
        X1 = alpha_pos - A1 * D_alpha

        r1, r2 = np.random.rand(num_variables), np.random.rand(num_variables)
        A2 = 2 * a * r1 - a
        C2 = 2 * r2
        D_beta = abs(C2 * beta_pos - wolves[i])
        X2 = beta_pos - A2 * D_beta

        r1, r2 = np.random.rand(num_variables), np.random.rand(num_variables)
        A3 = 2 * a * r1 - a
        C3 = 2 * r2
        D_delta = abs(C3 * delta_pos - wolves[i])
        X3 = delta_pos - A3 * D_delta

        wolves[i] = (X1 + X2 + X3) / 3

```



```
wolves[i] = np.clip(wolves[i], lb, ub)

fitness_values = np.array([fitness(w) for w in wolves])
alpha, beta, delta = np.argsort(fitness_values)[:3]
alpha_pos, beta_pos, delta_pos = wolves[alpha], wolves[beta], wolves[delta]

best_alloc = alpha_pos.reshape((num_sources, num_destinations))
best_cost = fitness(alpha_pos)

print("Optimal Transportation Plan (allocation matrix):")
print(np.round(best_alloc, 2))
print("Minimum Transportation Cost:", round(best_cost, 2))
```

Program 7

Parallel Cellular Algorithm for Epidemic Spread

Algorithm:

13/10/25
Date 13/10/25
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LAB-77 Parallel Cellular Algorithm:

→ Algorithm for Epidemic Spread

Step 1: Initialization

- (i) Create a 2D grid.
- (ii) Randomly select a few cells as infected.
- (iii) All other cells start as susceptible.

Step 2: Define Neighbourhood

- (i) Each cell can interact with its neighbours.
- (ii) Infection spreads locally to these neighbouring cells.

Step 3: Define Rules

At every time step

- (i) If a Susceptible cell has at least one infected neighbour it becomes infected with probability β (infection rate).
- (ii) If a cell is infected it recovers after some time with probability γ (recovery rate).
- (iii) Recovered cells remain recovered.

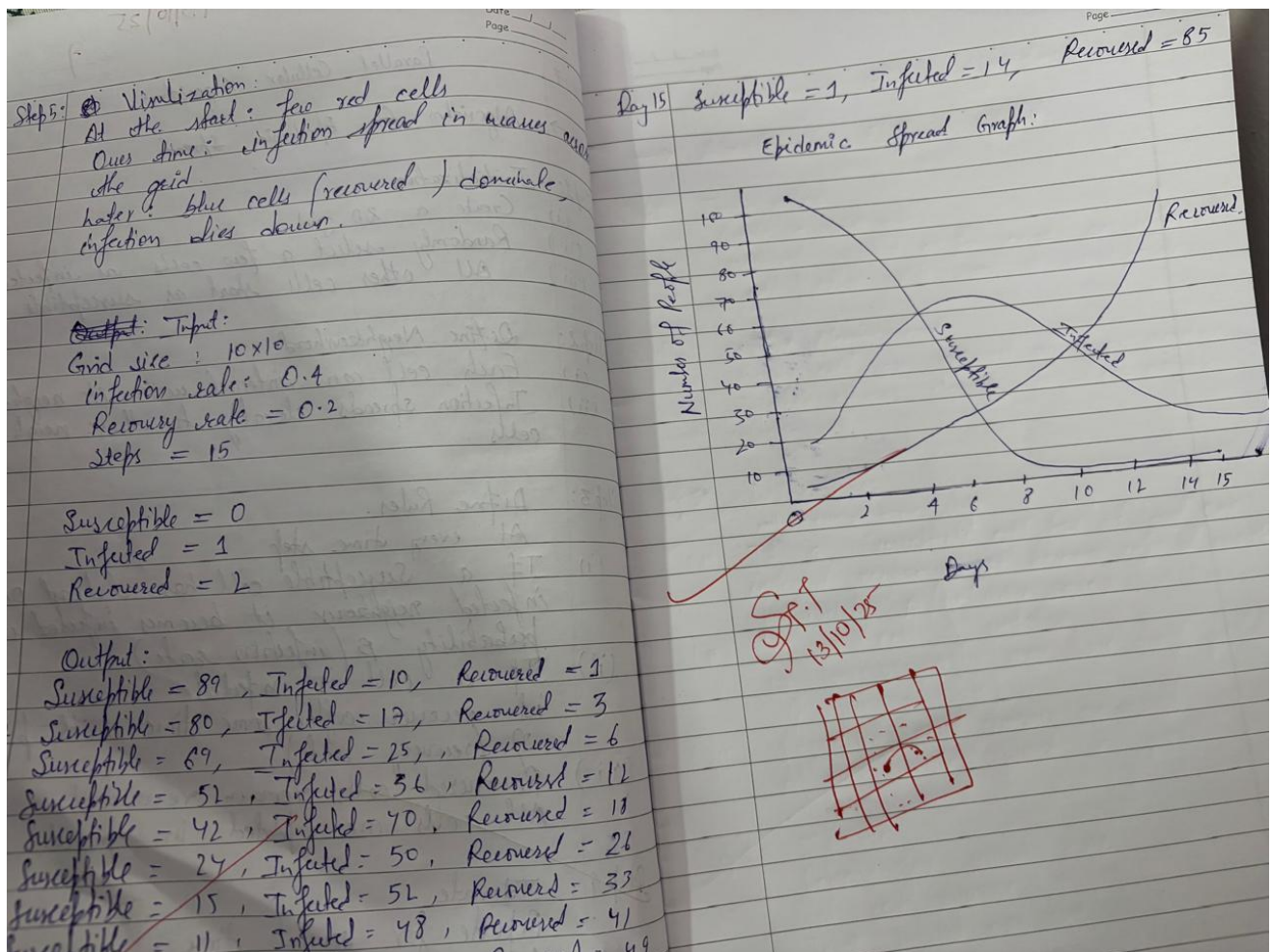
All cells are updated in parallel.

Step 4: Iterate

Repeat for several time.

You can measure:

- Total infected over time
- Infection peaks
- Speed and pattern spread



Code:

```
import numpy as np
import pandas as pd
from sklearn.decomposition import PCA
import matplotlib.pyplot as plt

# Example epidemic data (rows = days, columns = S, I, R)
data = pd.DataFrame({
    'Susceptible': [89, 80, 69, 52, 35, 20, 12],
    'Infected': [10, 17, 25, 36, 42, 35, 22],
    'Recovered': [1, 3, 6, 12, 23, 45, 66]
})

# Standardize the data
data_std = (data - data.mean()) / data.std()
```

```
# Apply PCA
pca = PCA(n_components=2)
principal_components = pca.fit_transform(data_std)
pca_df = pd.DataFrame(principal_components, columns=['PC1', 'PC2'])

# Explained variance ratio
print("Explained variance ratio:", pca.explained_variance_ratio_)

# Combine results
final_df = pd.concat([data, pca_df], axis=1)
print(final_df)

# Plot (optional)
plt.scatter(pca_df['PC1'], pca_df['PC2'], color='blue')
plt.title('PCA of Epidemic Spread')
plt.xlabel('Principal Component 1')
plt.ylabel('Principal Component 2')
plt.grid(True)
plt.show()
```