

* A car company believes that the percentage of residents in city ABC that own a vehicle is 60% or less. A sales manager disagrees with this. He conducts a hypothesis testing surveying 250 residents and found that 170 responded yes to owning a vehicle.

a) state the null & Alternate hypothesis.

b) At 10% significance level, is there enough evidence to support the idea that vehicle ownership in city ABC is 60% or less?

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$$H_0 = P_0 = 60\%$$

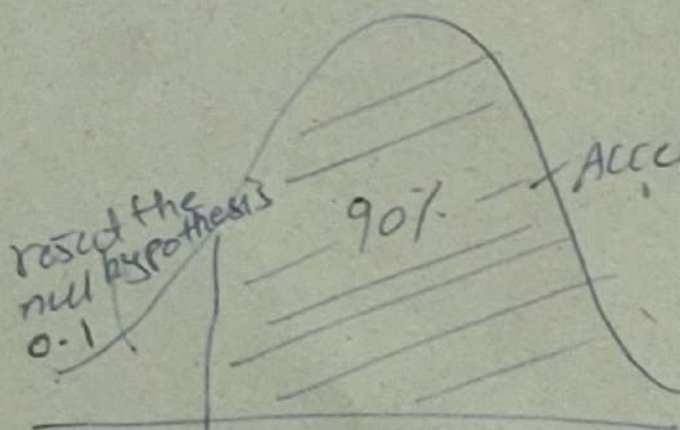
$$H_1 = P_0 \neq 60\%$$

$$n = 250 \quad x = 170$$

$$\hat{p} = \frac{x}{n} = \frac{170}{250} = 0.68$$

$$q_0 = 1 - P_0 = 1 - 0.6 = 0.4$$

$$\alpha = 0.1$$



$$1 - 0.1 = 0.9$$

z test with proportion

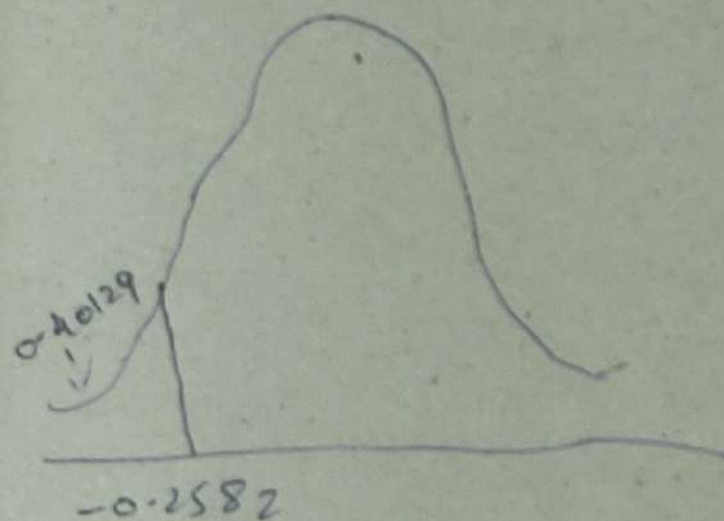
$$\begin{aligned} z_{test} &= \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}} = \frac{0.68 - 0.6}{\sqrt{\frac{0.6 \times 0.4}{250}}} \\ &= \frac{0.08}{\sqrt{\frac{0.24}{250}}} = \frac{0.08}{\sqrt{0.00096}} \\ &= \frac{0.08}{0.0312} = 0.2582 \end{aligned}$$

$$-1.28 < 0.258$$

Accept the null hypothesis

P-value:

$$z_{test} = 0.258$$



$$\begin{aligned} 1 - 0.40129 \\ = 0.59871 \end{aligned}$$

$$\alpha > 0.1$$

$$pvalue = 0.40129$$

$$\alpha < p\text{-value}$$

Accept the null hypothesis.