

Part 2: Advanced Learning Algorithms

Week 4+5: Neural Networks

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1. Neural Network Intuition

Overview

Advanced learning algorithms

Neural Networks 

inference (prediction)
training

Practical advice for building machine learning systems



Decision Trees 

Neurons and Brain

Neural networks

Origins: Algorithms that try to mimic the brain.



Used in the 1980's and early 1990's.

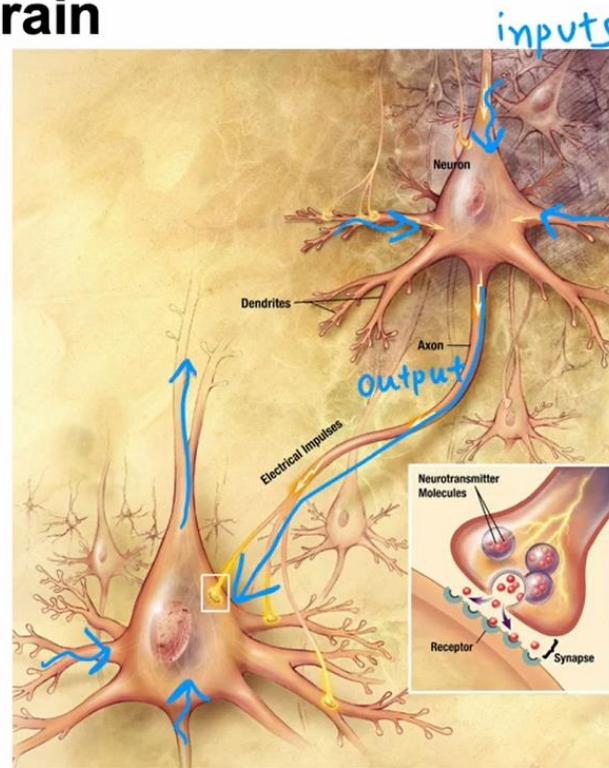
Fell out of favor in the late 1990's.

Resurgence from around 2005.

speech → images → text (NLP) → ...

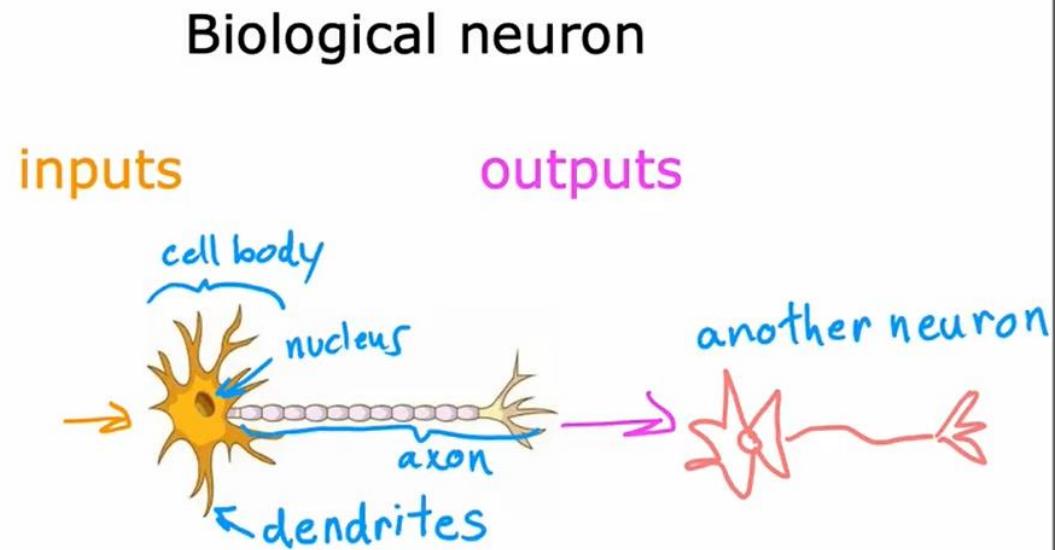
Neurons and Brain

Neurons in the brain



[Credit: US National Institutes of Health, National Institute on Aging]

Neurons and Brain



Simplified mathematical model of a neuron

inputs outputs

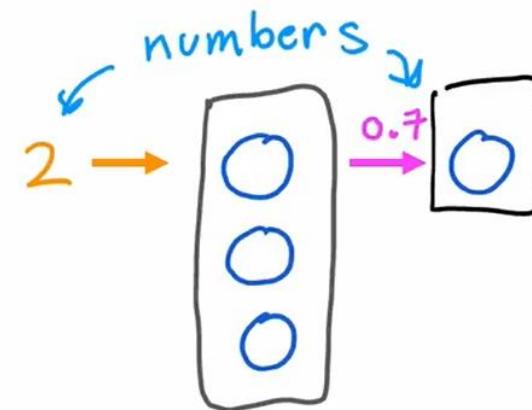
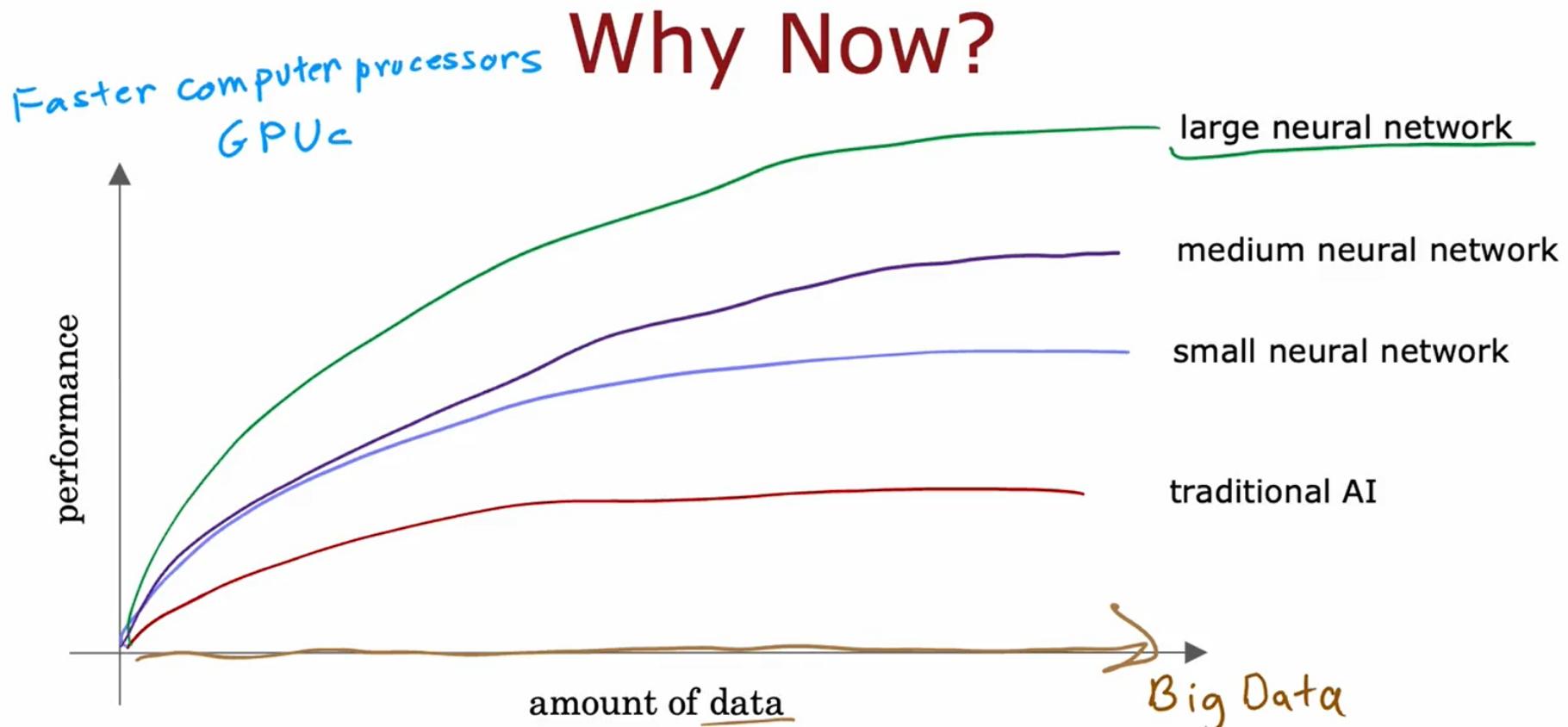
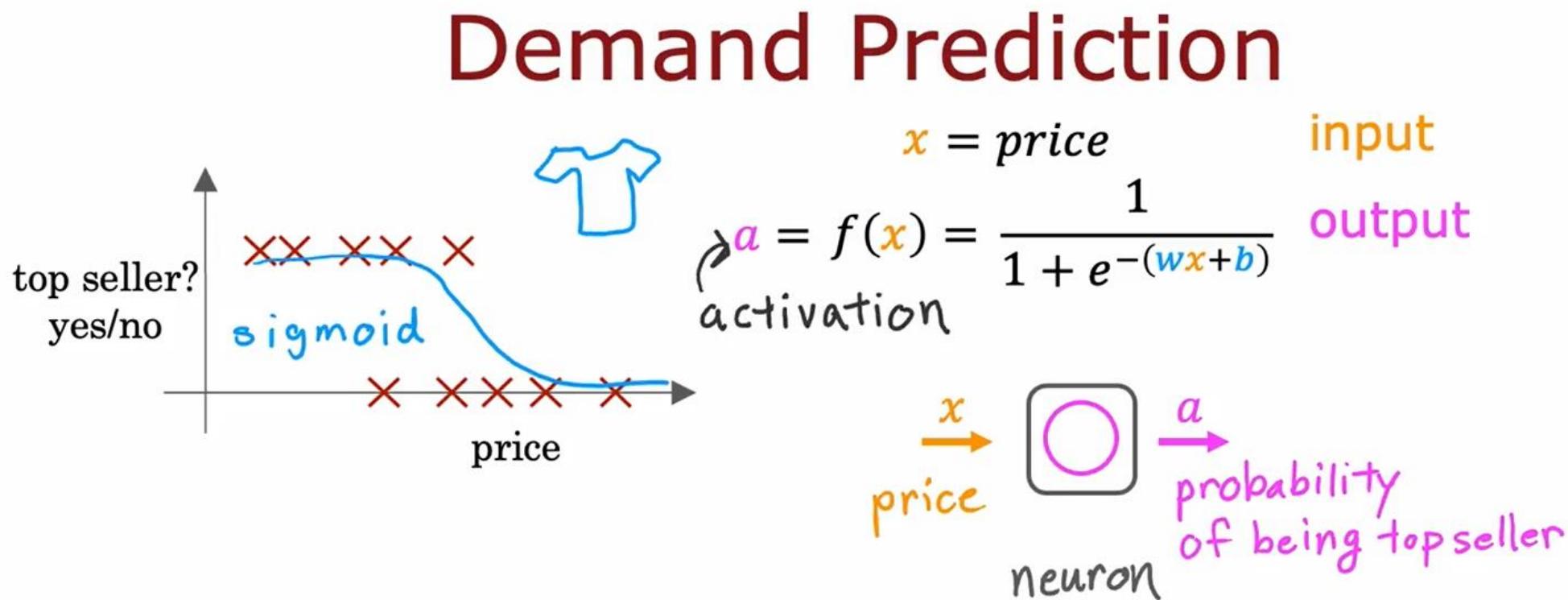


image source: <https://biologydictionary.net/sensory-neuron/>

Neurons and Brain

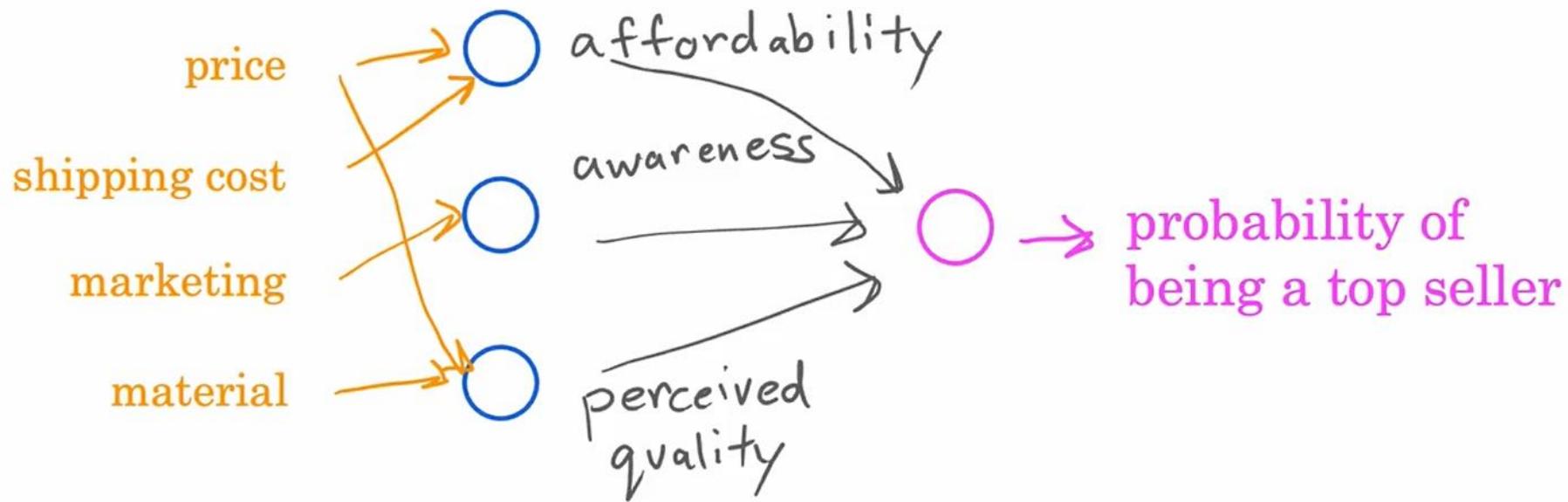


Demand Prediction



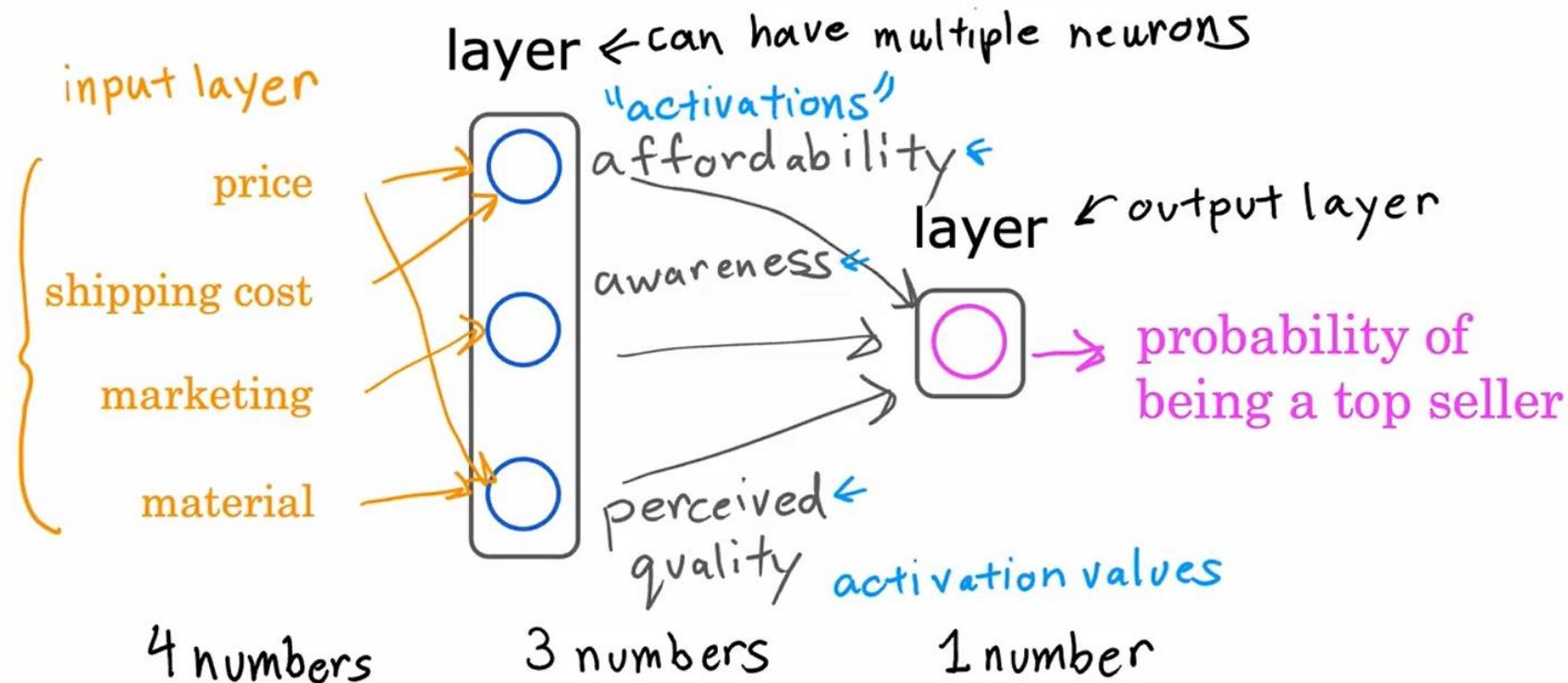
Demand Prediction

Demand Prediction



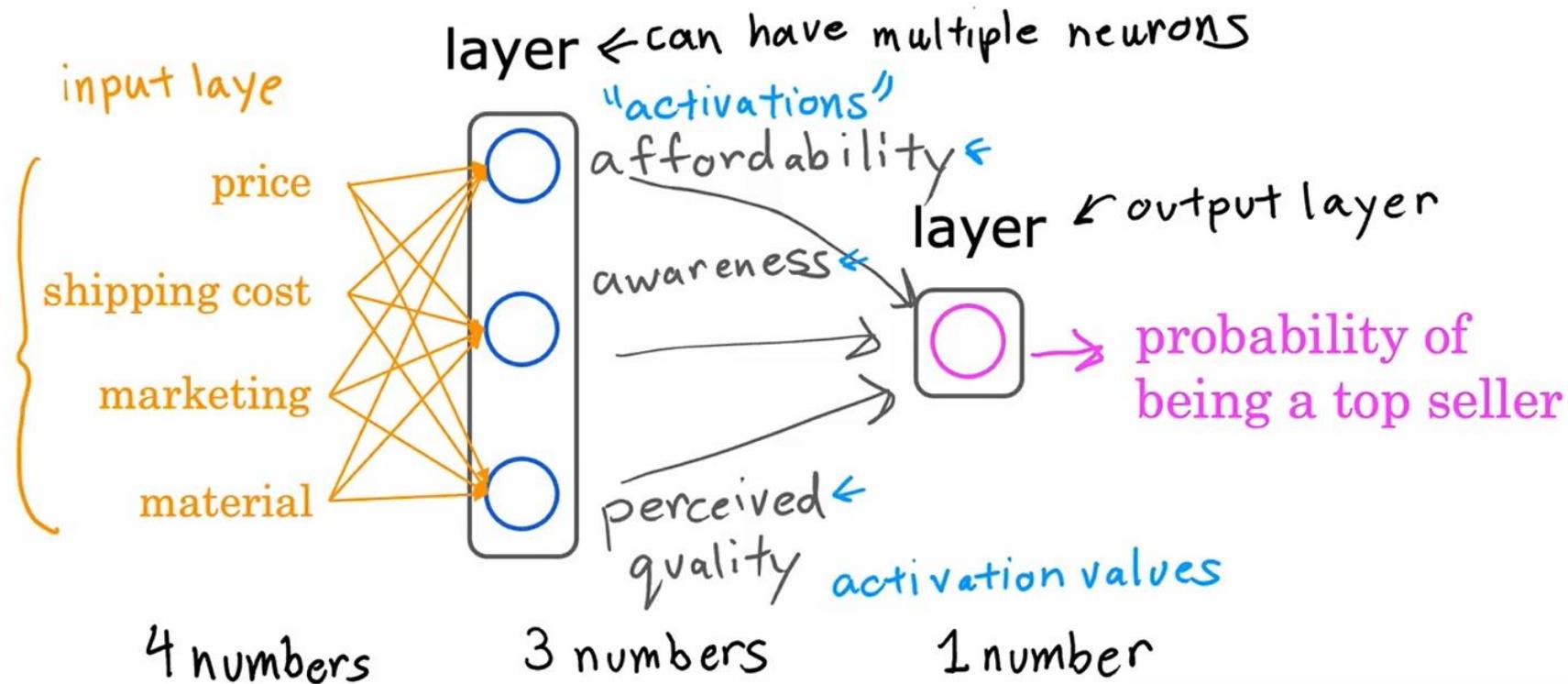
Demand Prediction

Demand Prediction

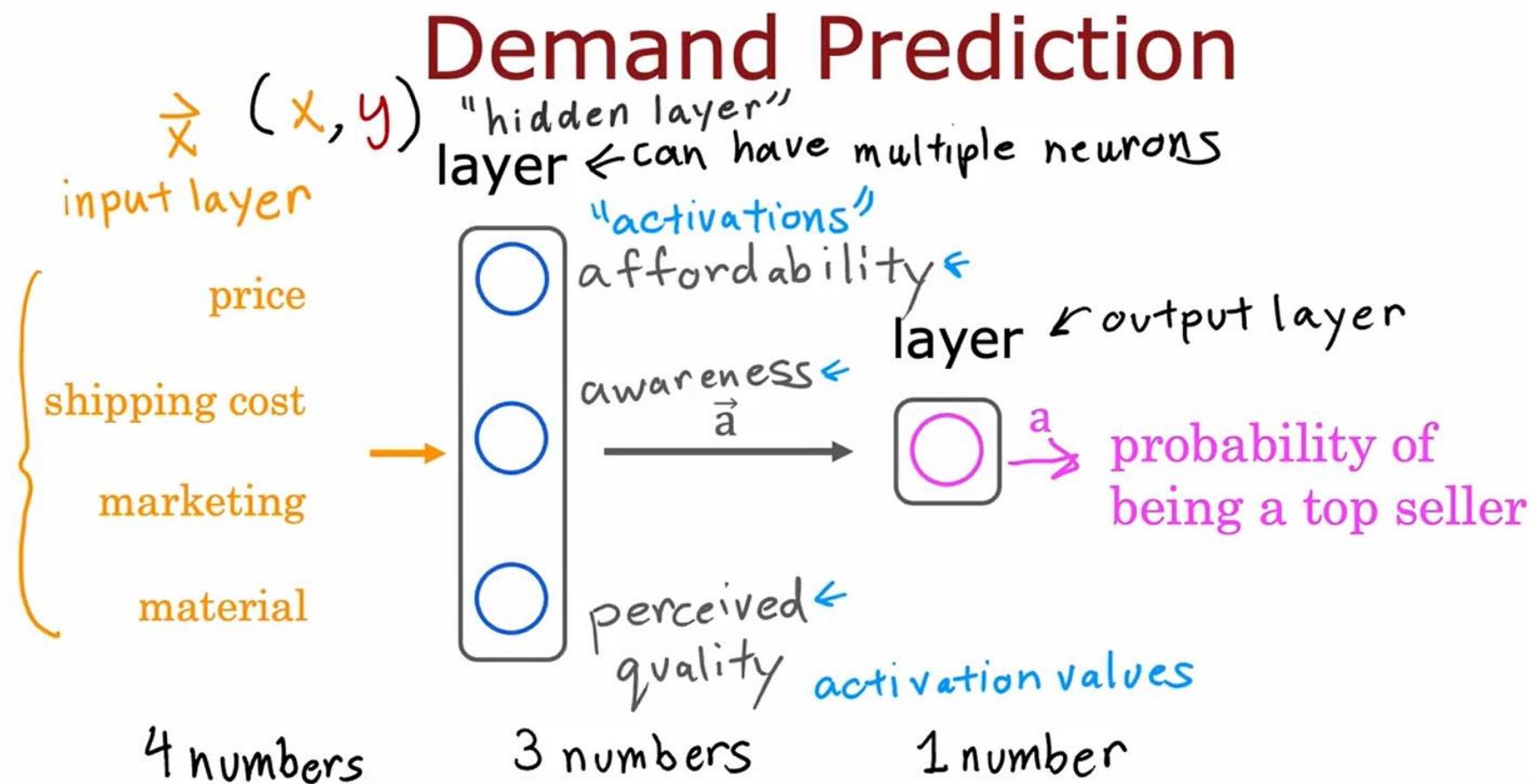


Demand Prediction

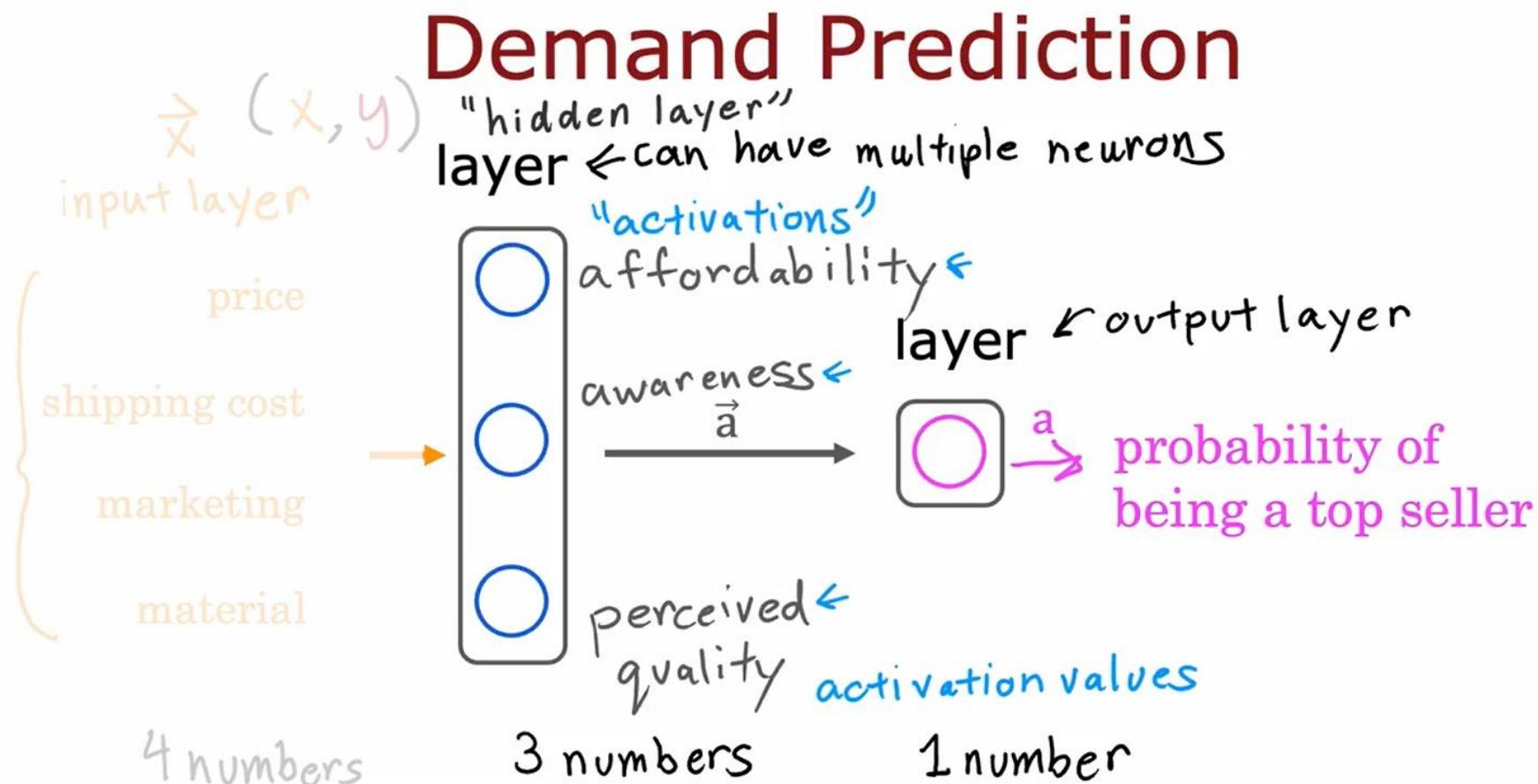
Demand Prediction



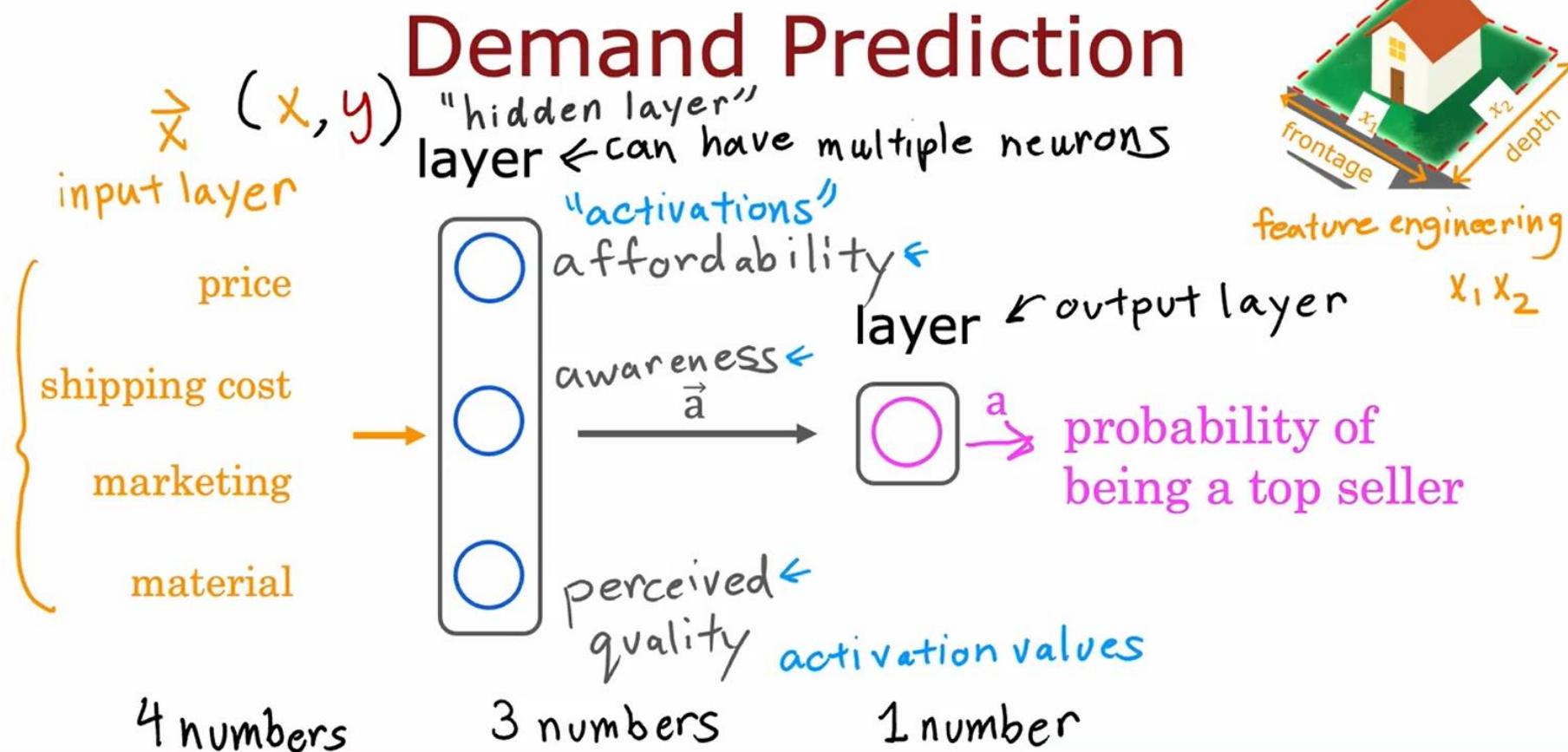
Demand Prediction



Demand Prediction

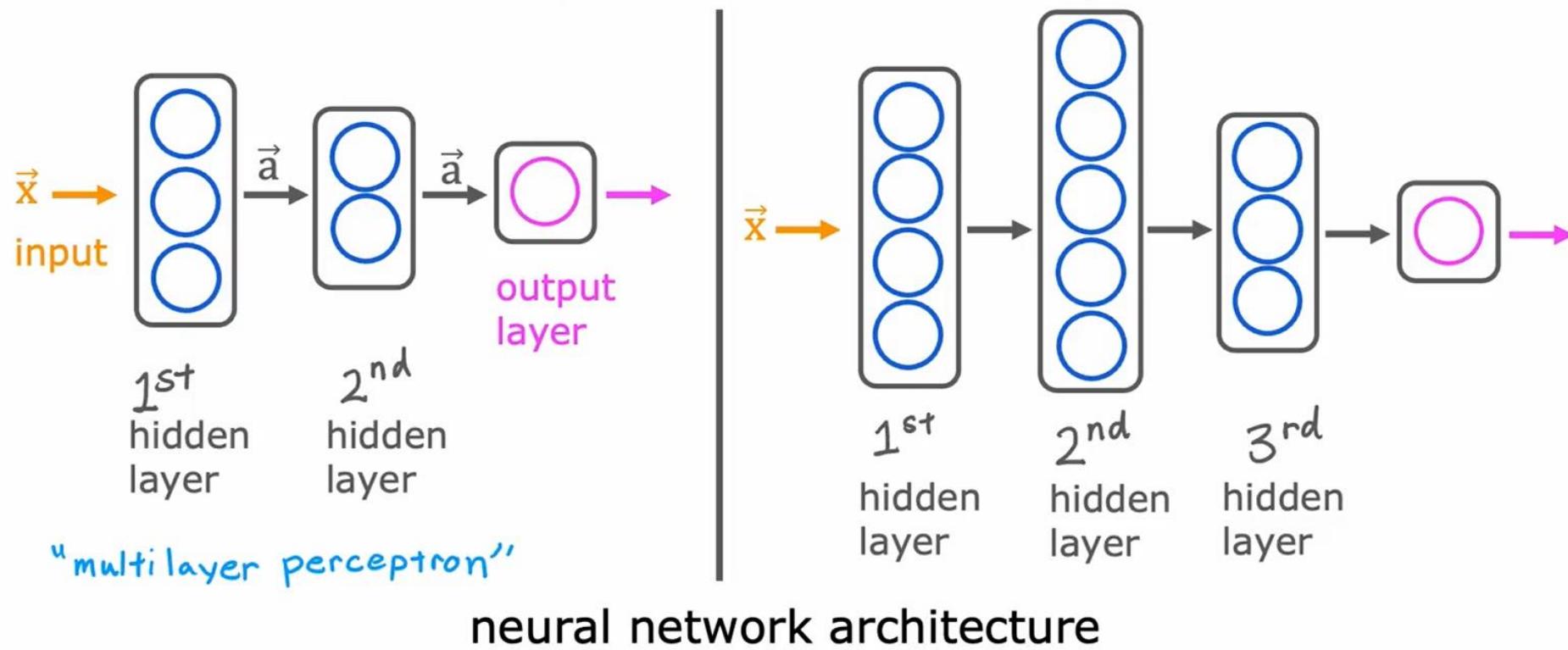


Demand Prediction



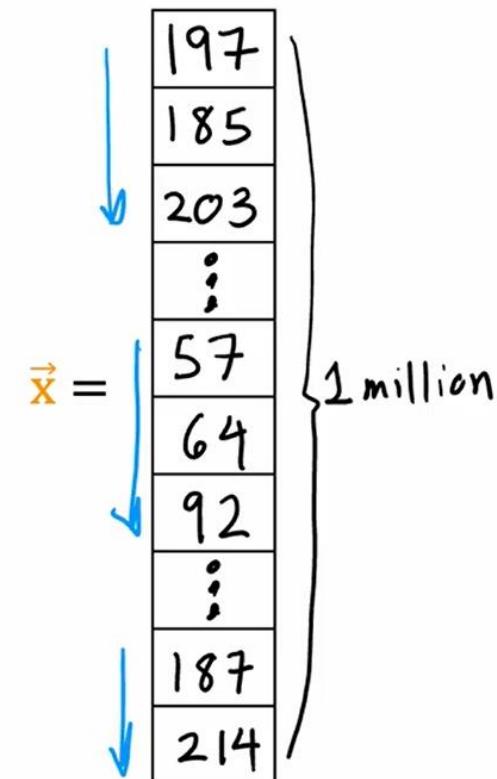
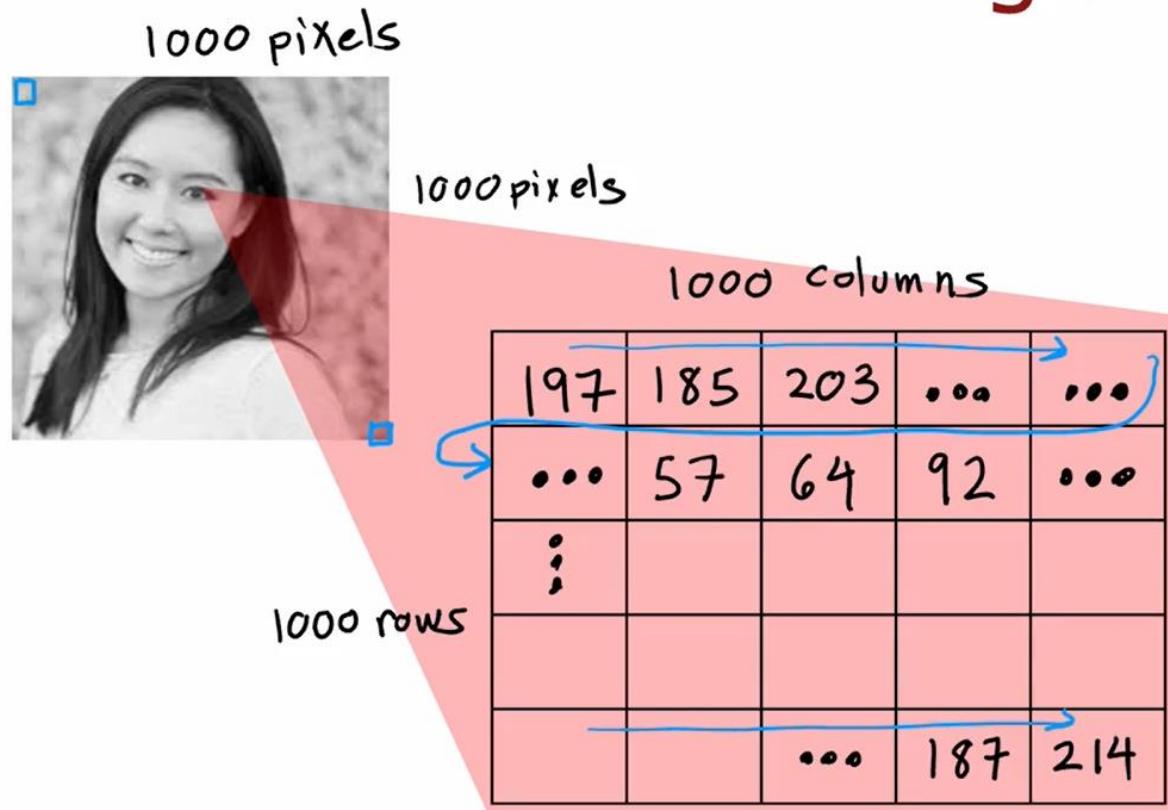
Demand Prediction

Multiple hidden layers



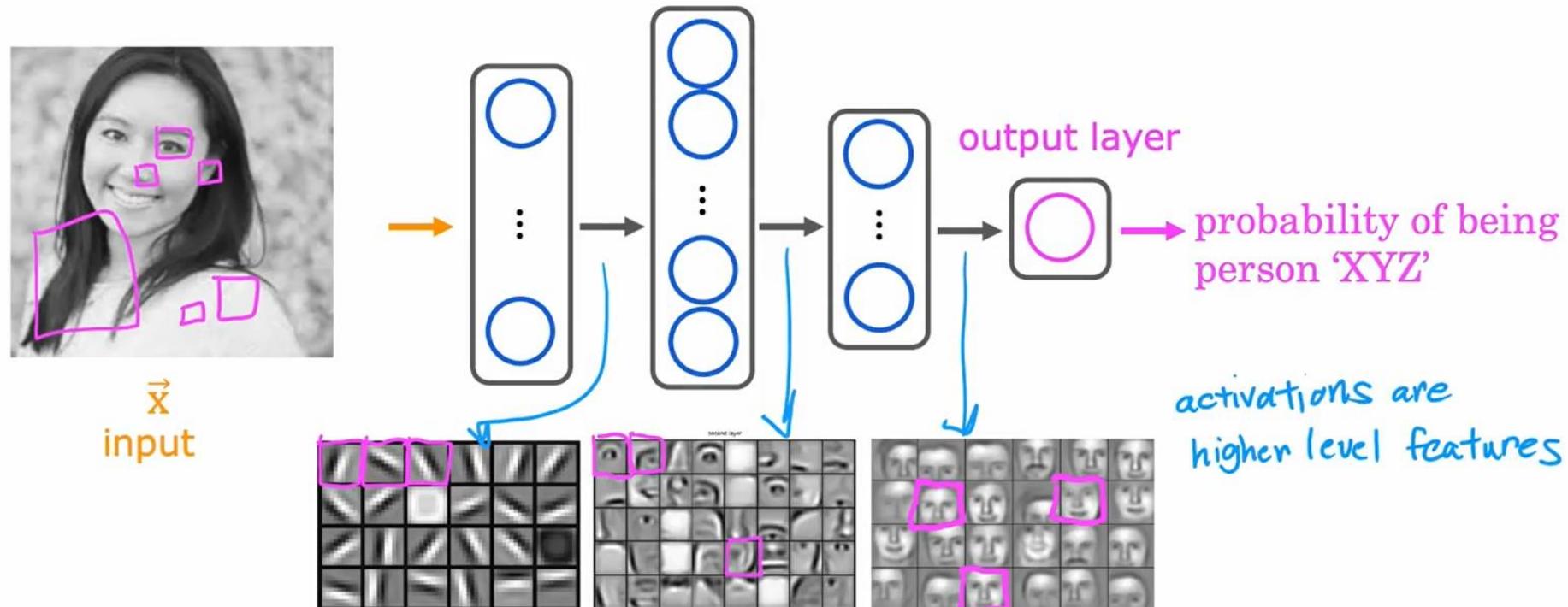
Recognizing Images

Face recognition



Recognizing Images

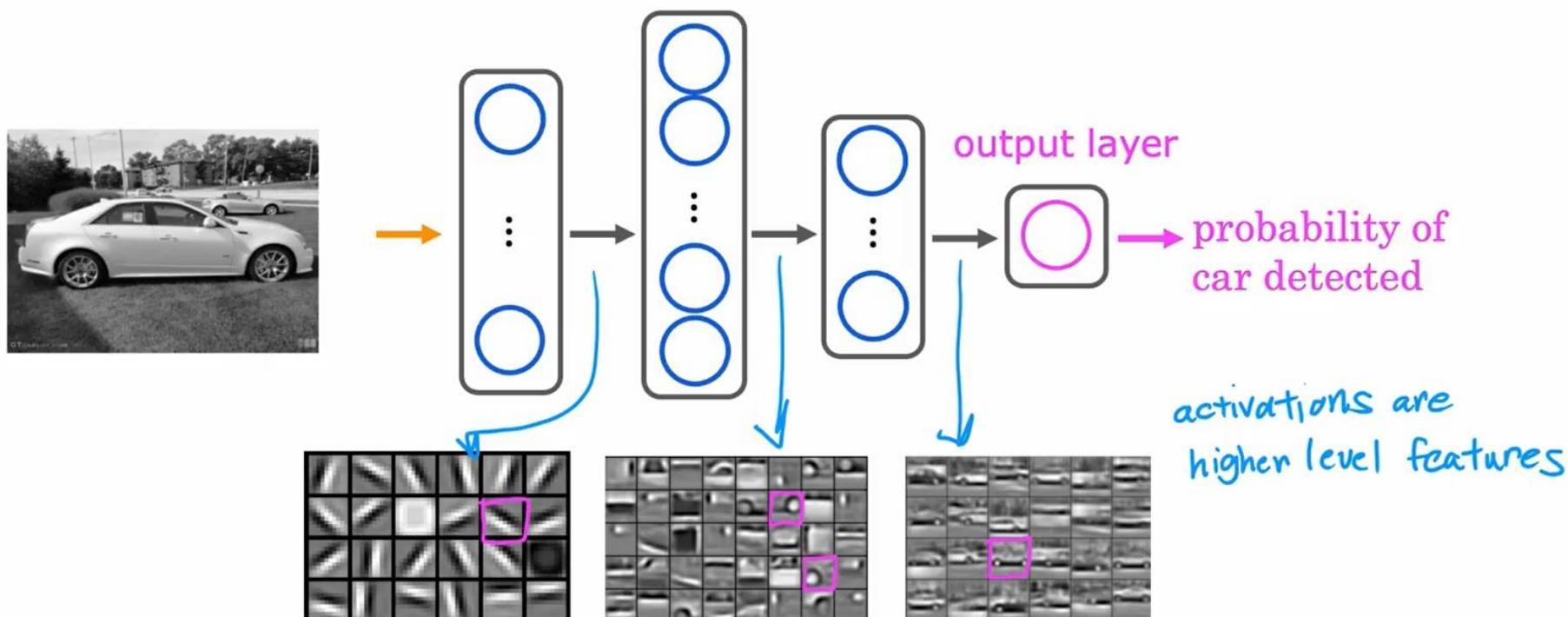
Face recognition



source: Convolutional Deep Belief Networks for Scalable Unsupervised Learning of Hierarchical Representations
by Honglak Lee, Roger Grosse, Ranganath Andrew Y. Ng

Recognizing Images

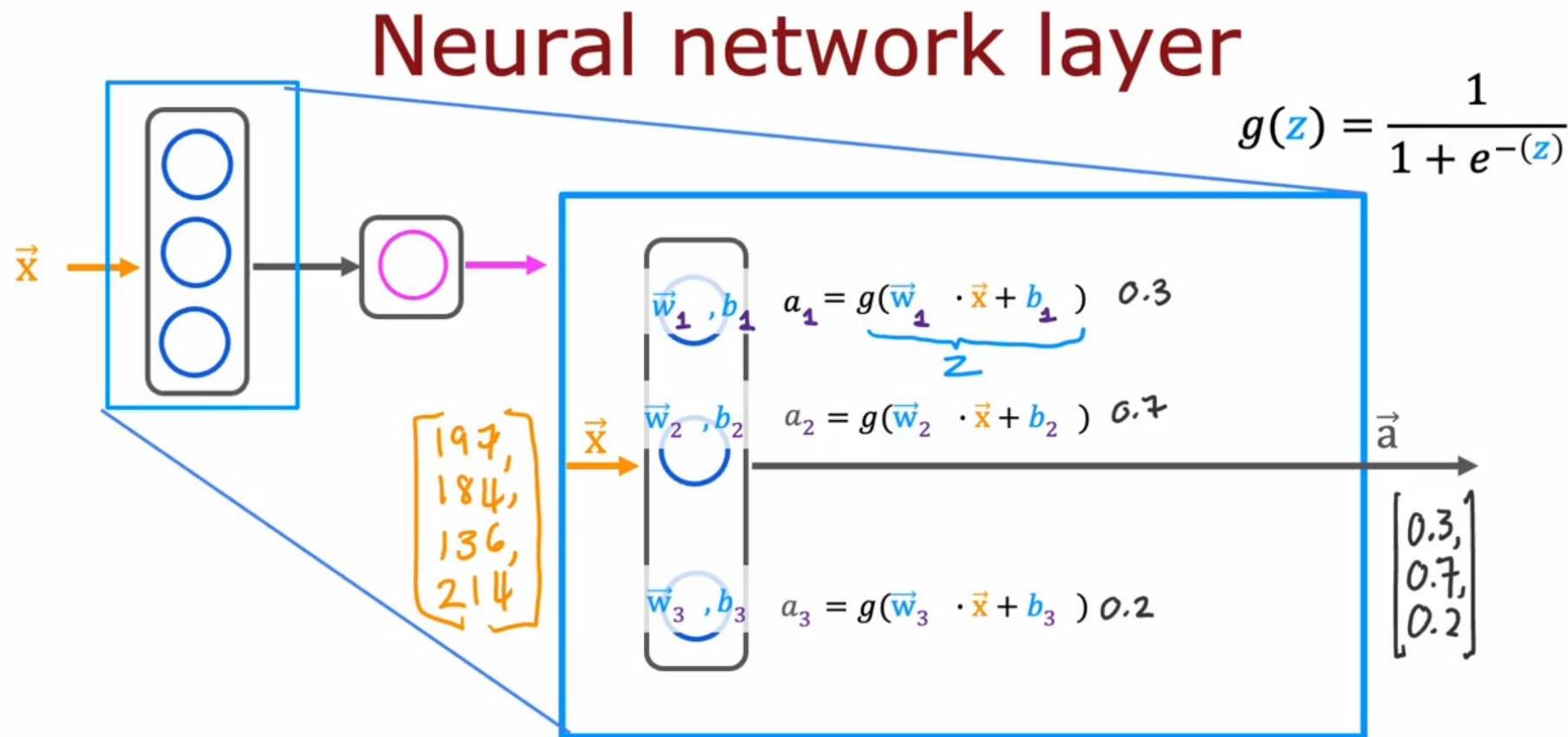
Car classification



source: Convolutional Deep Belief Networks for Scalable Unsupervised Learning of Hierarchical Representations
by Honglak Lee, Roger Grosse, Ranganath Andrew Y. Ng

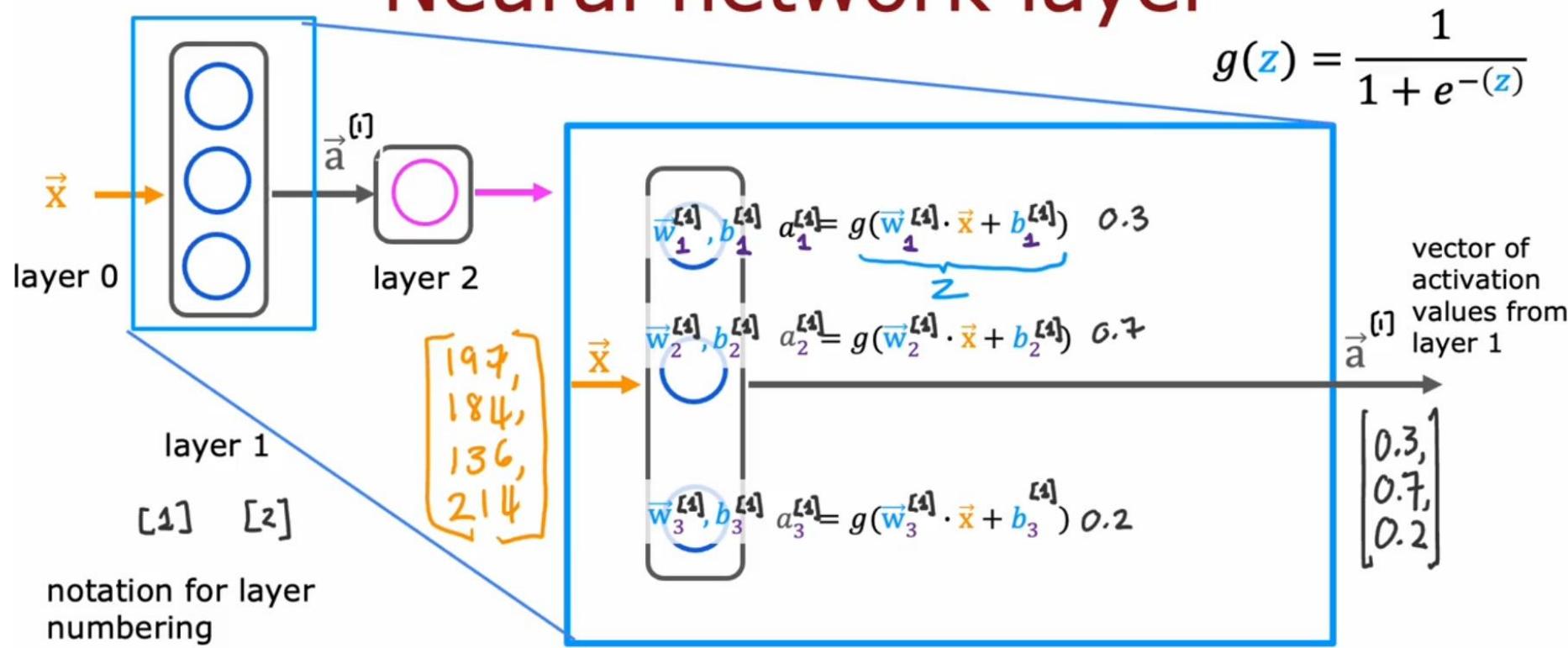
2. Neural Network Model

NN Layer



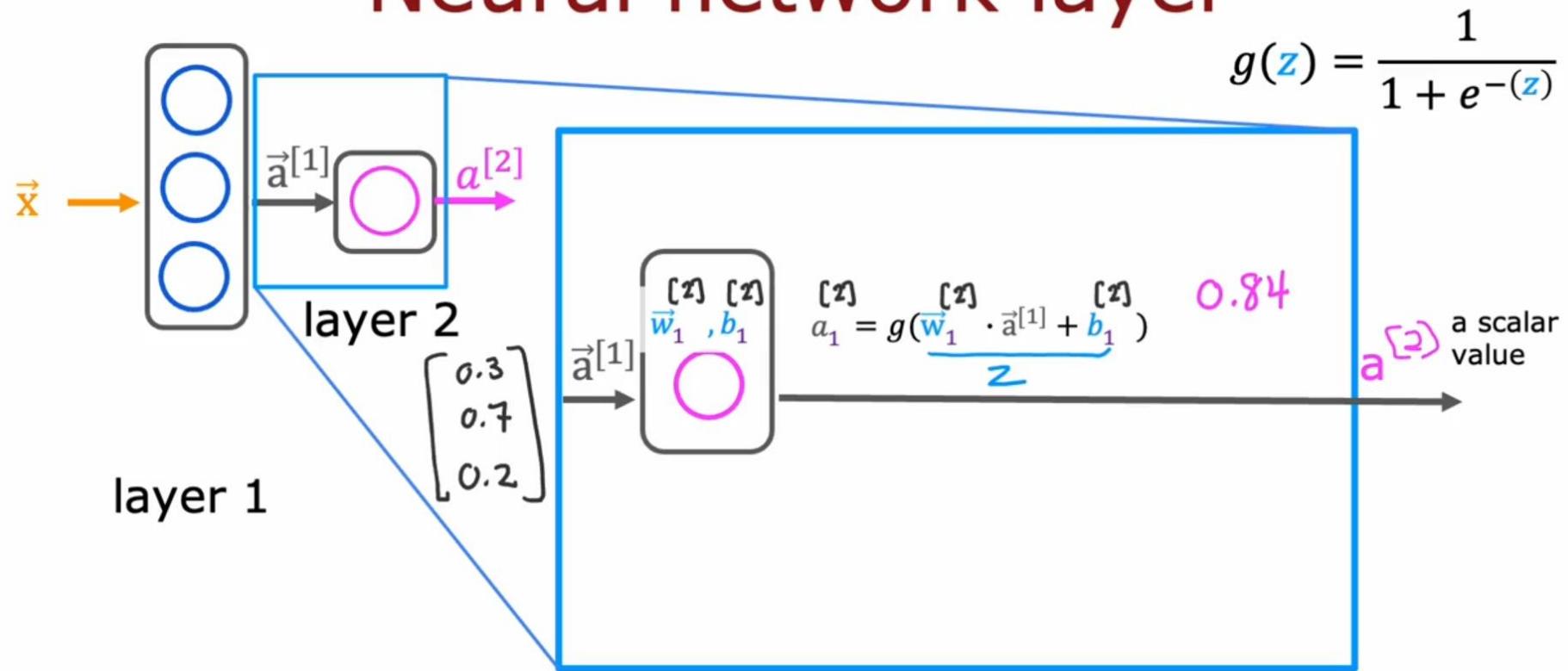
NN Layer

Neural network layer



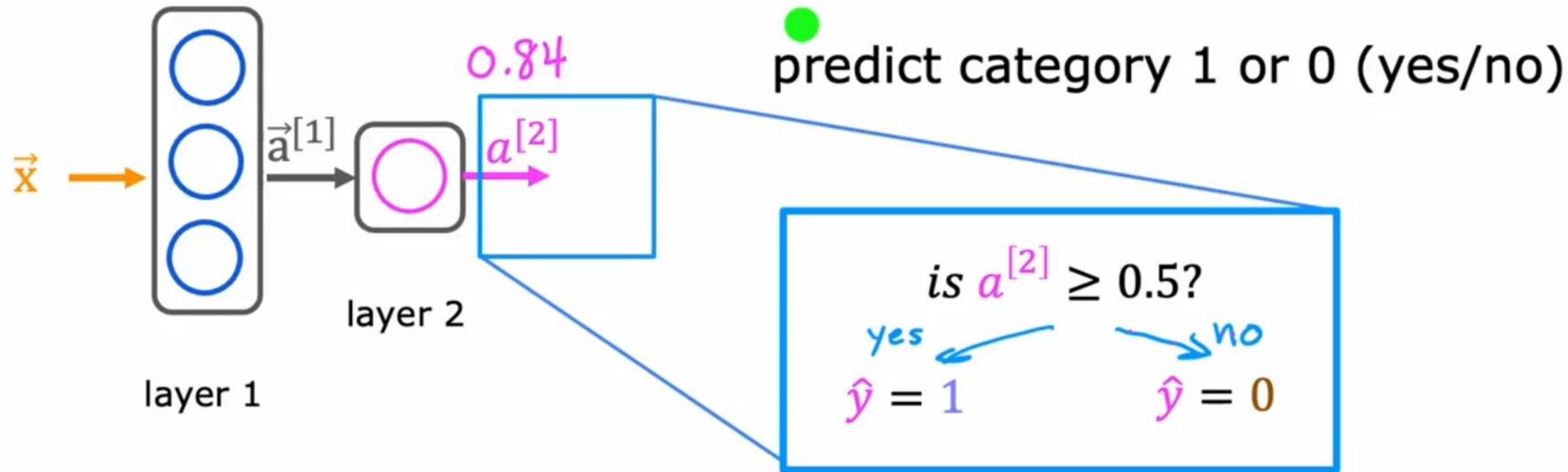
NN Layer

Neural network layer

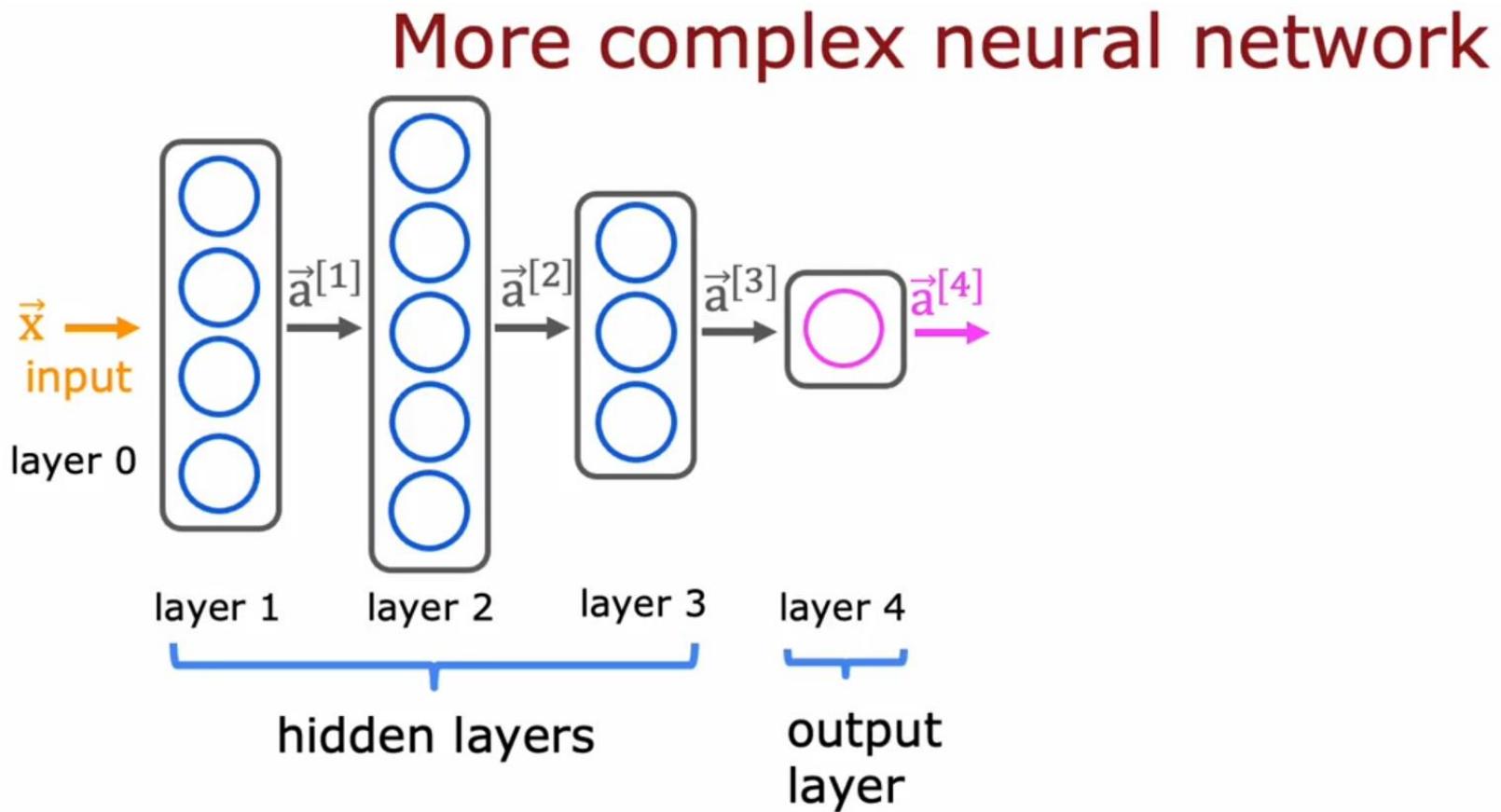


NN Layer

Neural network layer

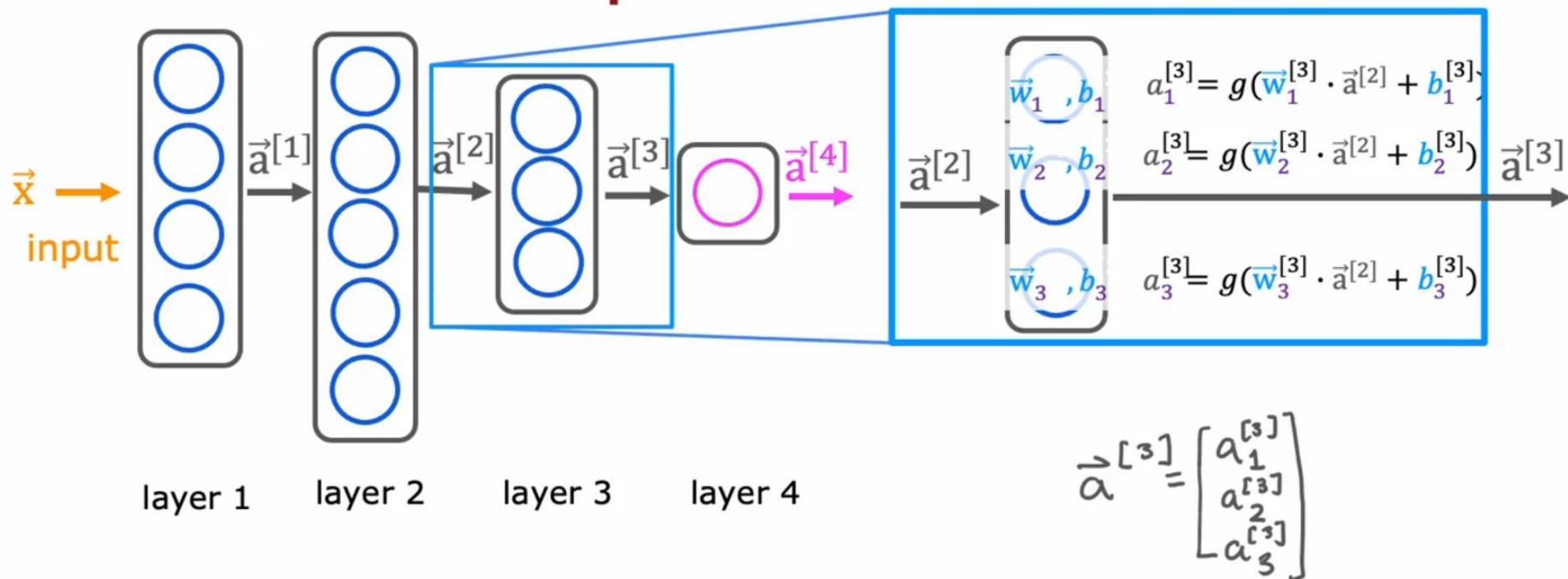


More Complex NN



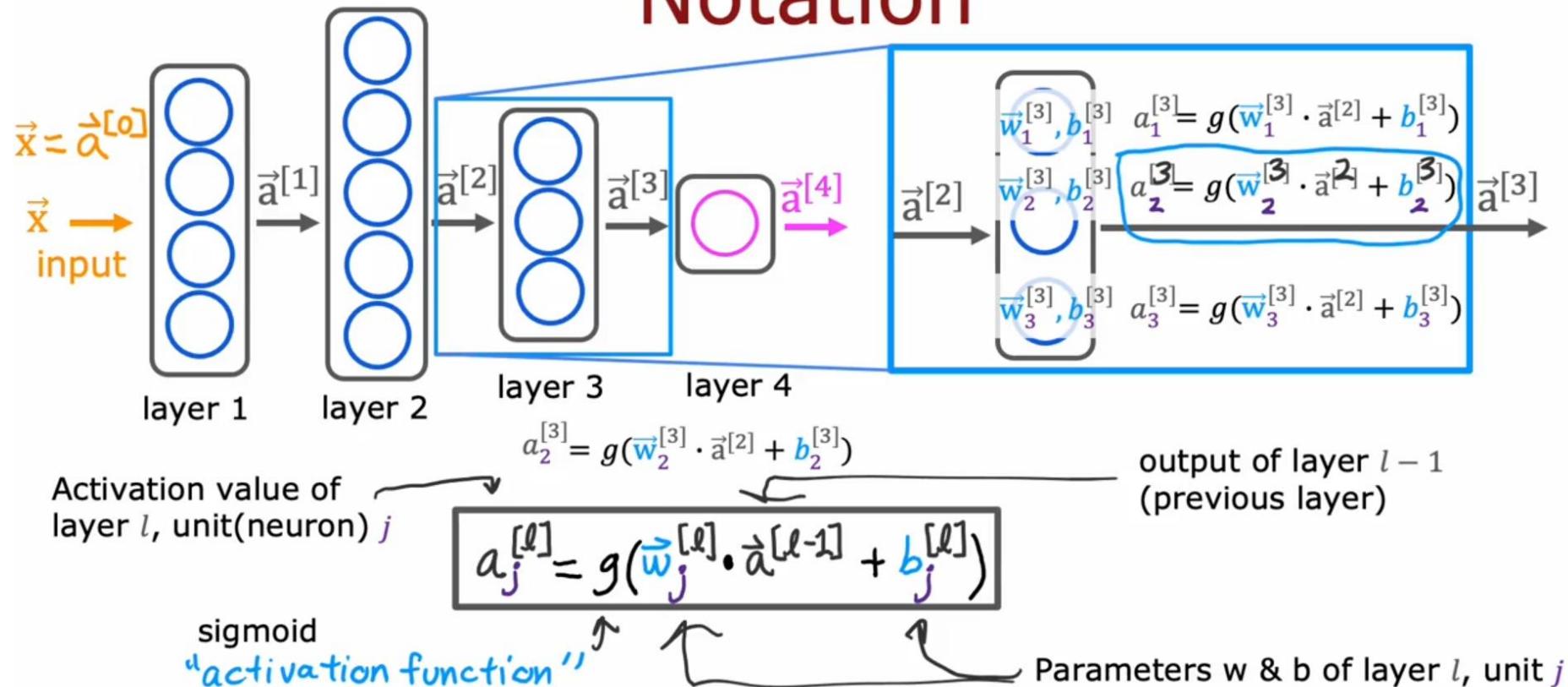
More Complex NN

More complex neural network



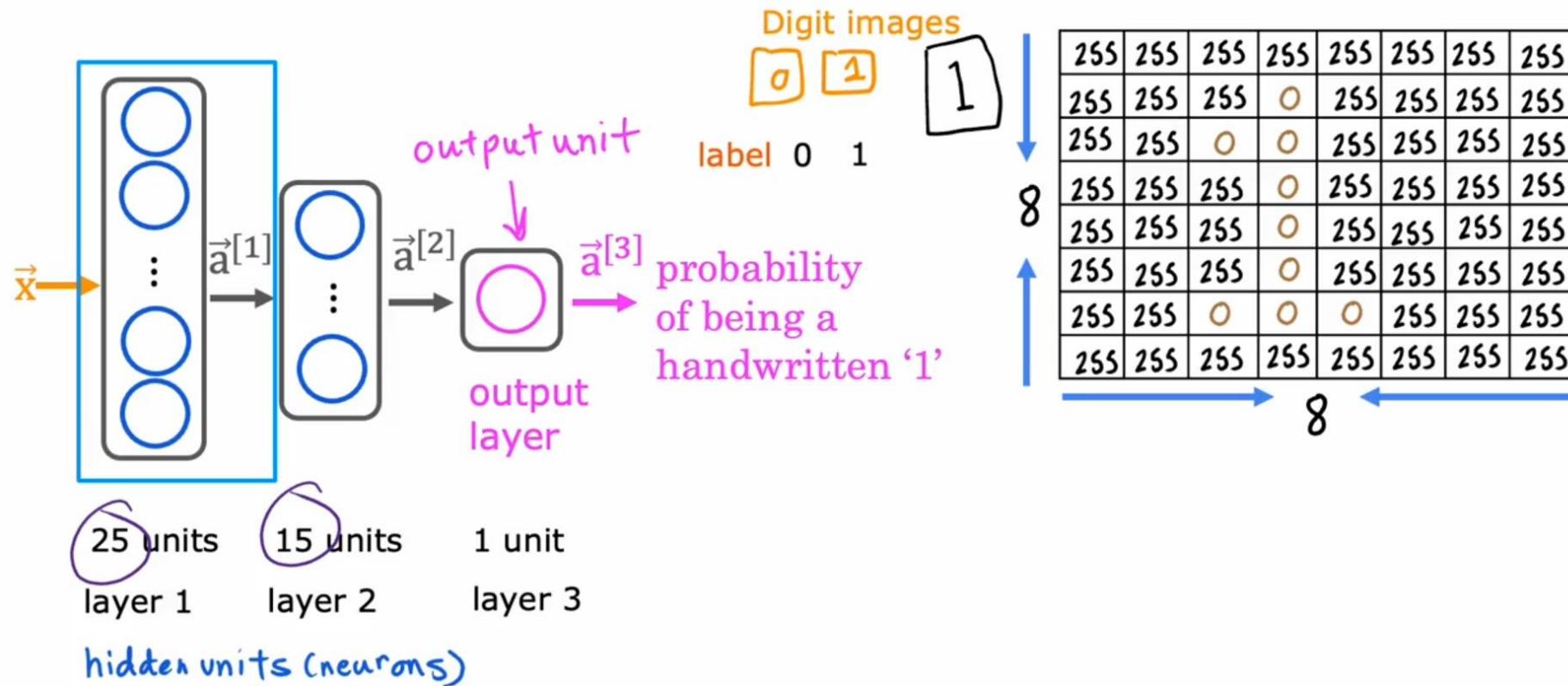
More Complex NN

Notation



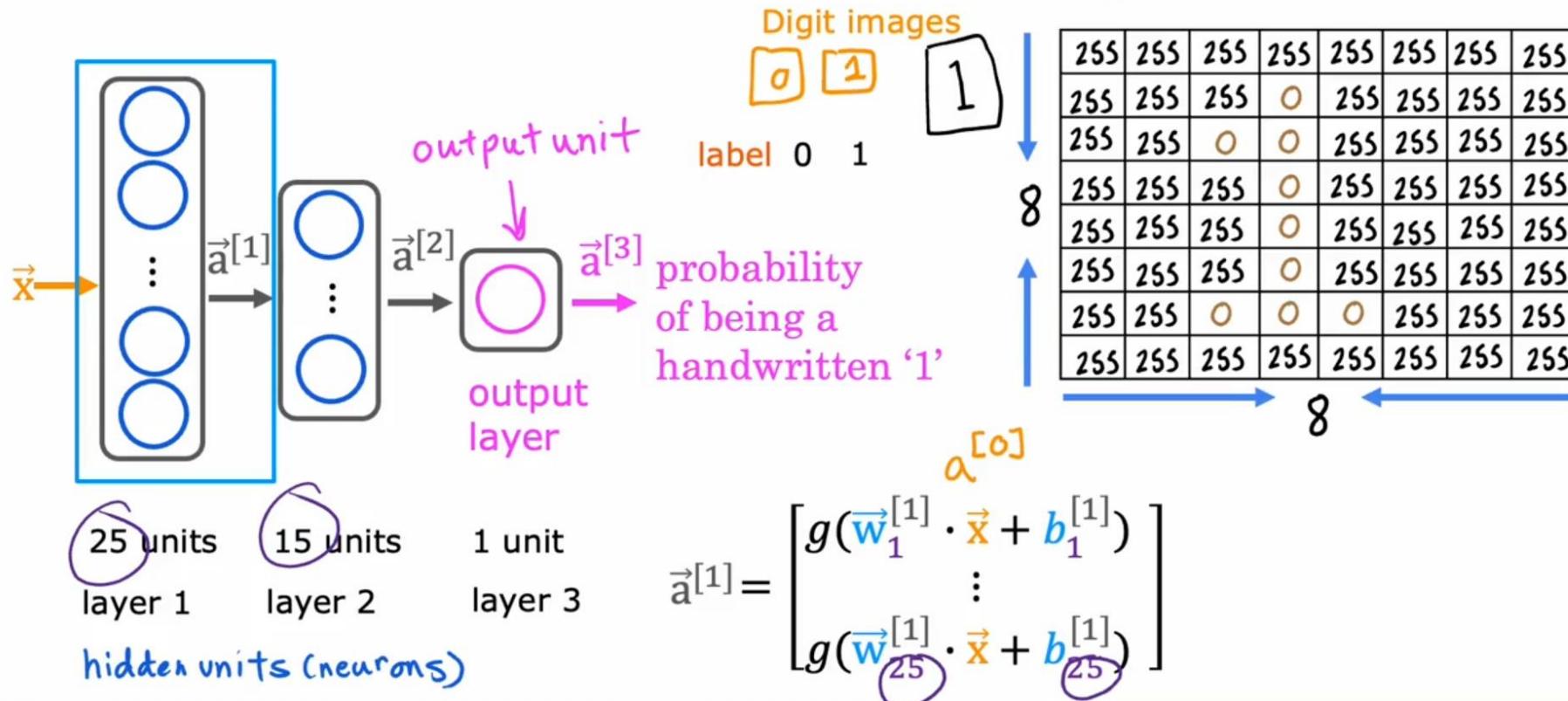
Inference: Making Predictions

Handwritten digit recognition



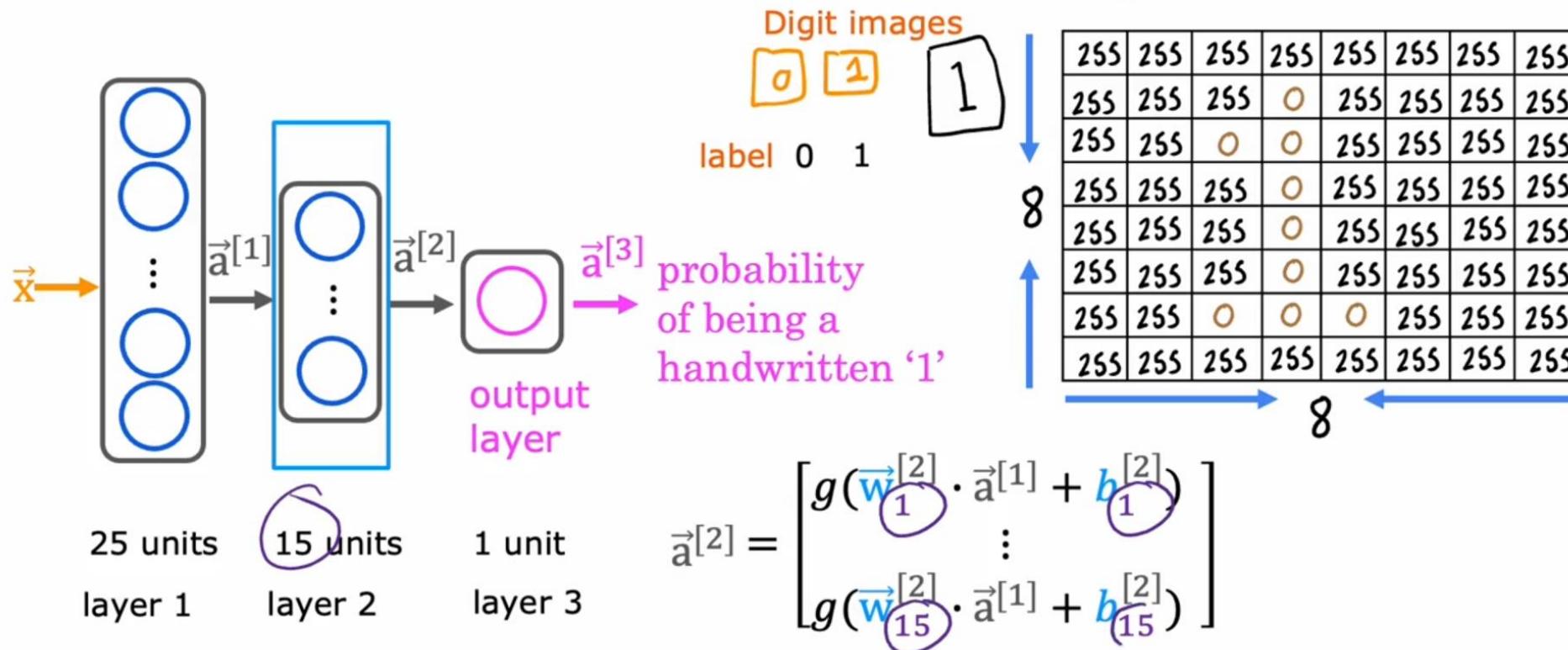
Inference: Making Predictions

Handwritten digit recognition



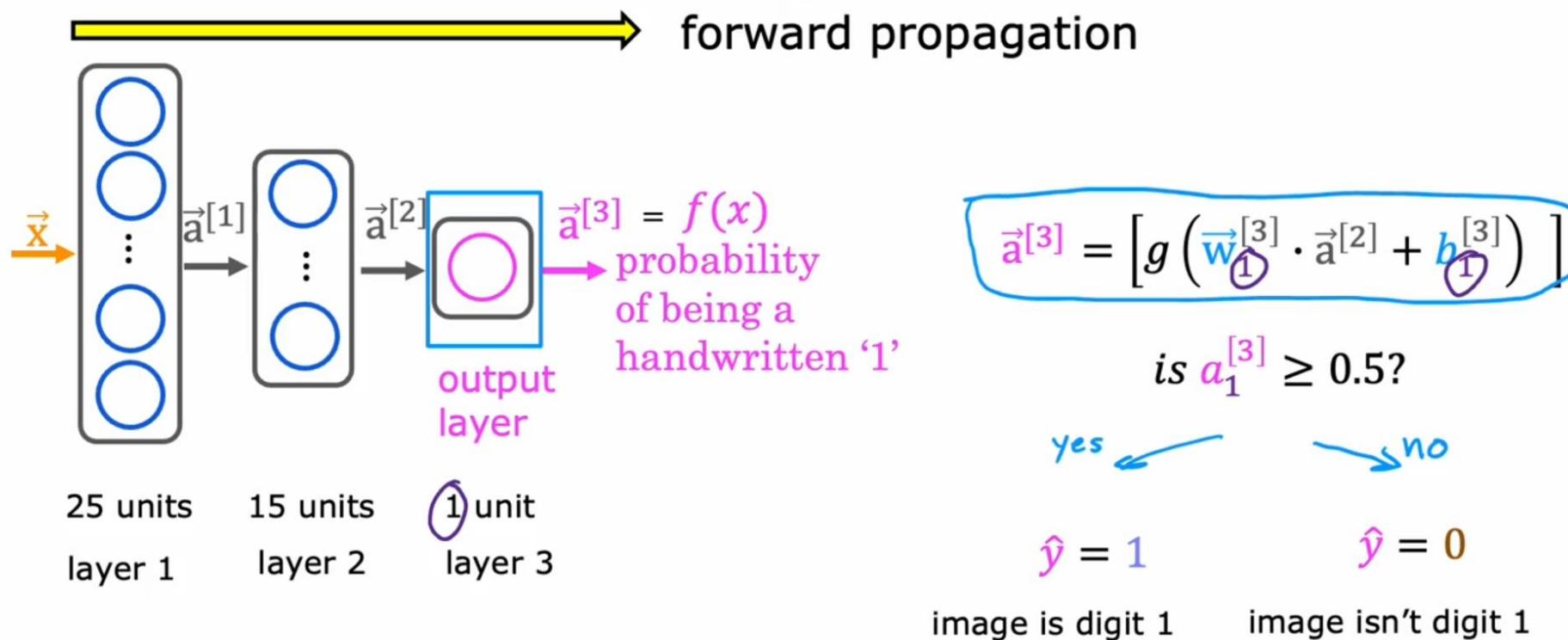
Inference: Making Predictions

Handwritten digit recognition



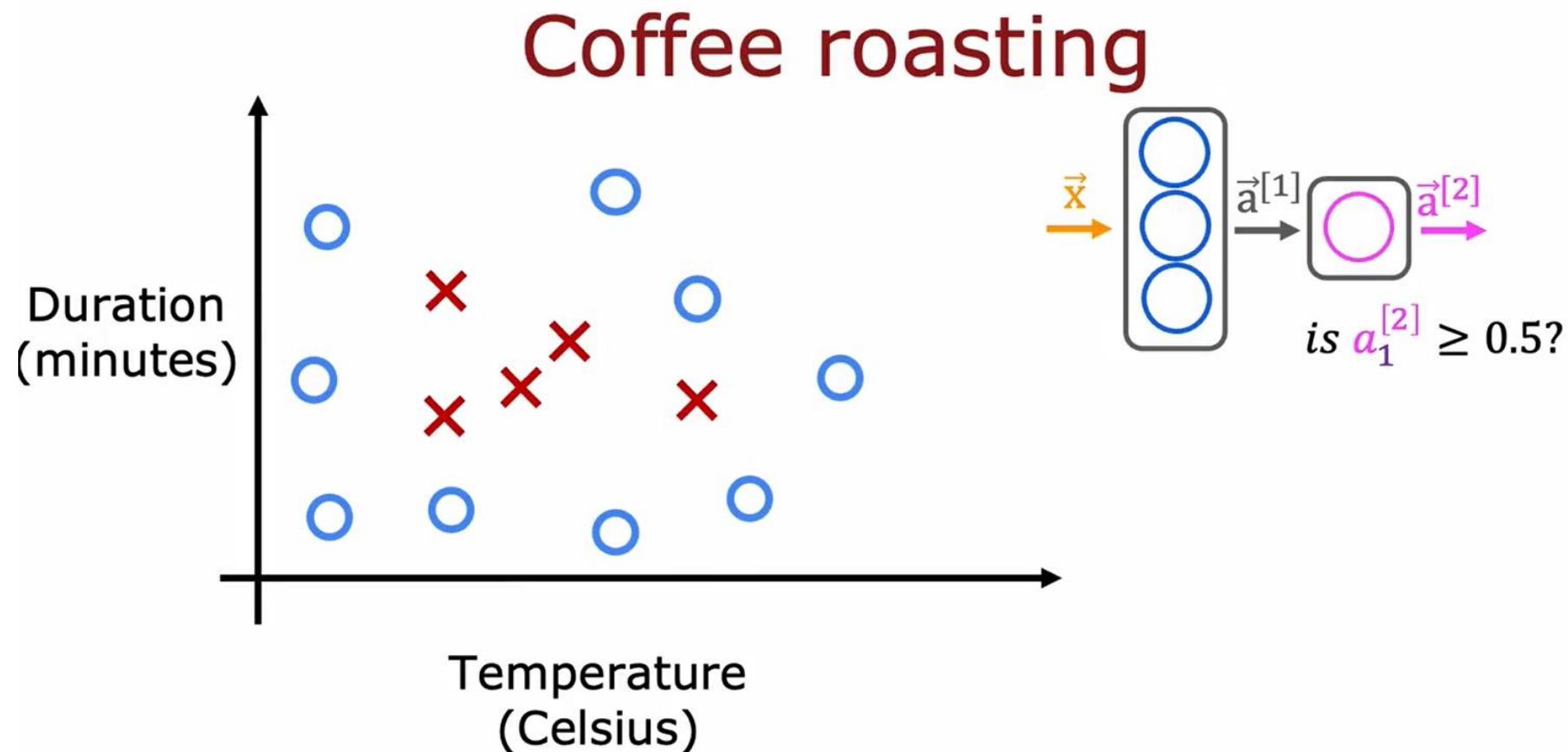
Inference: Making Predictions

Handwritten digit recognition

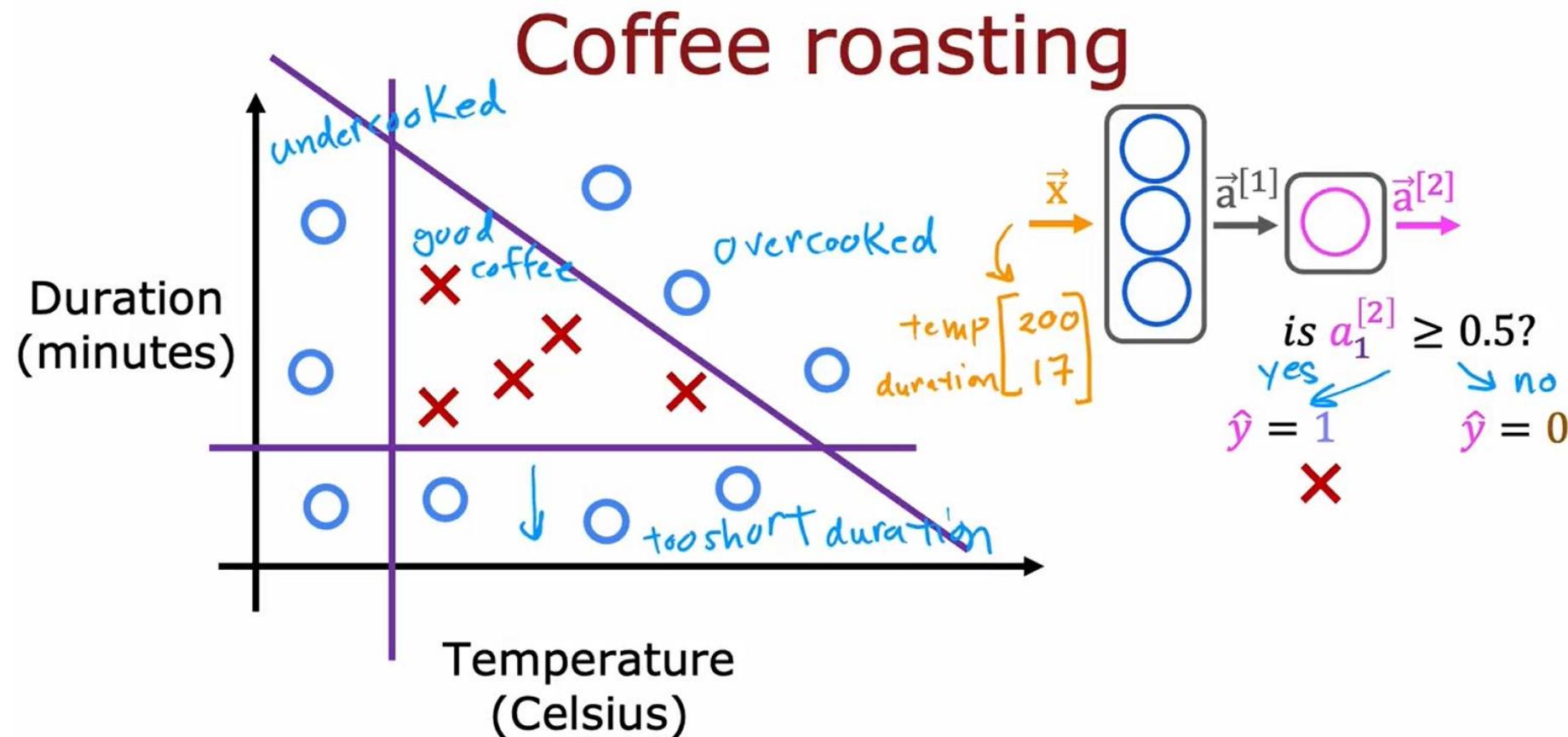


3. TensorFlow Implementation

Inference in Code

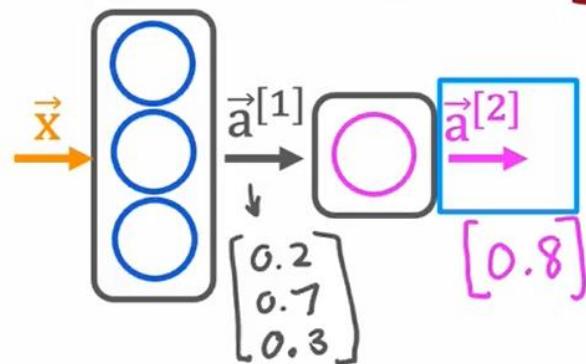


Inference in Code



Inference in Code

Build the model using TensorFlow



```
x = np.array([[200.0, 17.0]])
layer_1 = Dense(units=3, activation='sigmoid')
a1 = layer_1(x)
```

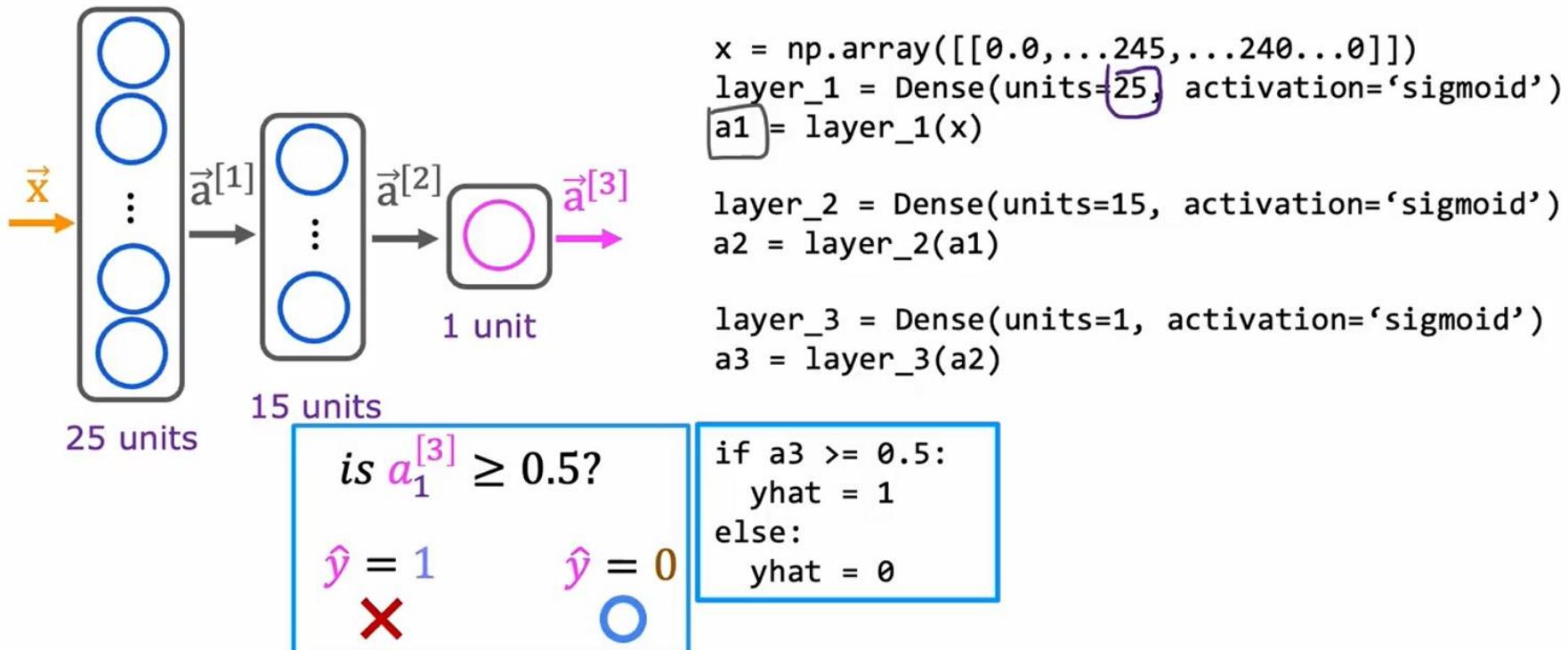
```
layer_2 = Dense(units=1, activation='sigmoid')
a2 = layer_2(a1)
```

is $a_1^{[2]} \geq 0.5?$
yes $\hat{y} = 1$ no $\hat{y} = 0$

```
if a2 >= 0.5:
    yhat = 1
else:
    yhat = 0
```

Inference in Code

Model for digit classification



Data in TensorFlow

Feature vectors

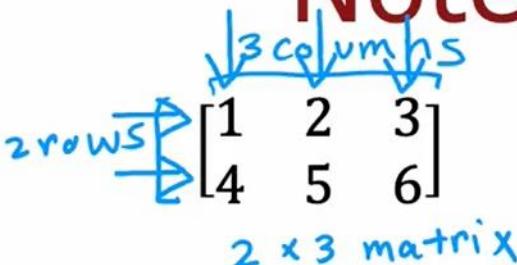
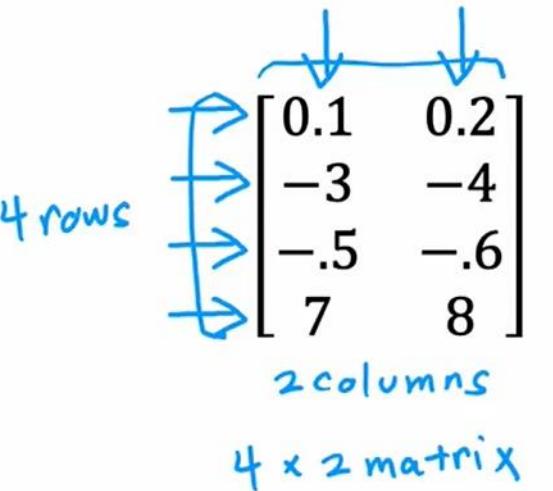
temperature (Celsius)	duration (minutes)	Good coffee? (1/0)
200.0	17.0	1
425.0	18.5	0
...

x = np.array([[200.0, 17.0]]) ←
[[200.0, 17.0]]

why?

Data in TensorFlow

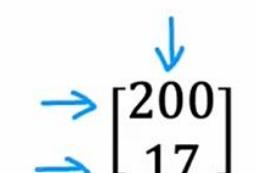
Note about numpy arrays

 <p>2 rows 3 columns 2×3 matrix</p>	<pre>x = np.array([[1, 2, 3], [4, 5, 6]])</pre>	<p>2D array</p>
 <p>4 rows 2 columns 4×2 matrix</p>	<pre>x = np.array([[0.1, 0.2], [-3.0, -4.0], [-0.5, -0.6], [7.0, 8.0]])</pre>	<p>2×3 4×2 1×2 2×1</p>
	<pre>[[0.1, 0.2], [-3.0, -4.0], [-0.5, -0.6], [7.0, 8.0]]</pre>	

Data in TensorFlow

Note about numpy arrays

`x = np.array([[200, 17]])`  $\begin{bmatrix} 200 & 17 \end{bmatrix}$ 1×2

`x = np.array([[200], [17]])`  $\begin{bmatrix} 200 \\ 17 \end{bmatrix}$ 2×1

 `→ x = np.array([200,17])`

 1D
"vector"

Data in TensorFlow

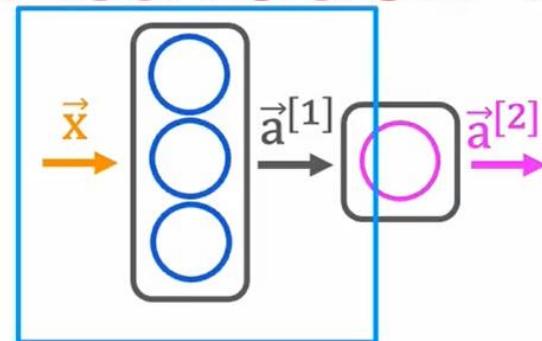
Feature vectors

temperature (Celsius)	duration (minutes)	Good coffee? (1/0)
200.0	17.0	1
425.0	18.5	0
...

```
x = np.array([[200.0, 17.0]]) ←  
[[200.0, 17.0]]  
↓      ↓  
→ [200.0 17.0]      1 x 2
```

Data in TensorFlow

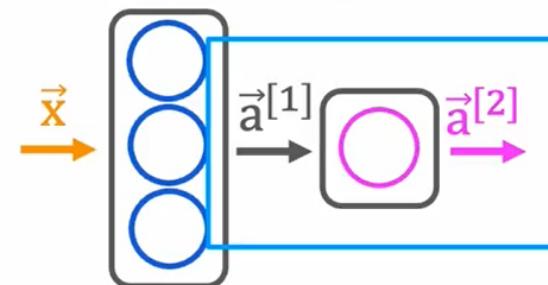
Activation vector



```
x = np.array([[200.0, 17.0]])
layer_1 = Dense(units=3, activation='sigmoid')
a1 = layer_1(x)
→ [0.2, 0.7, 0.3] 1 x 3 matrix
→ tf.Tensor([[0.2 0.7 0.3]], shape=(1, 3), dtype=float32)
→ a1.numpy()
array([[0.2, 0.7, 0.3]], dtype=float32)
```

Data in TensorFlow

Activation vector



```
→ layer_2 = Dense(units=1, activation='sigmoid')  
→ a2 = layer_2(a1)
```

↳ **[0.8]** ↲

1 x 1

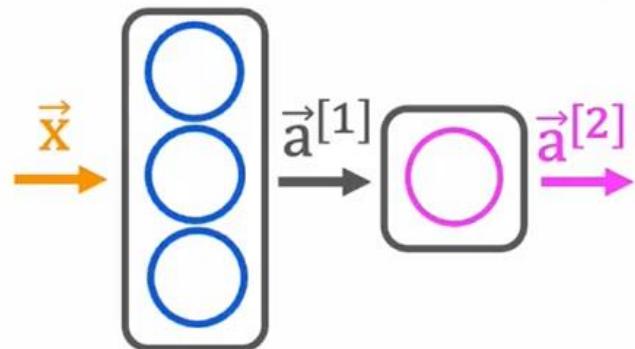
```
→ tf.Tensor([[0.8]], shape=(1, 1), dtype=float32)
```

```
→ a2.numpy()
```

```
array([[0.8]], dtype=float32)
```

Building a Neural Network

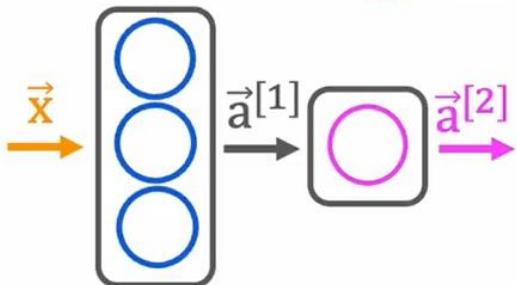
What you saw earlier



```
→ x = np.array([[200.0, 17.0]])  
→ layer_1 = Dense(units=3, activation="sigmoid")  
→ a1 = layer_1(x)  
  
→ layer_2 = Dense(units=1, activation="sigmoid")  
→ a2 = layer_2(a1)
```

Building a Neural Network

Building a neural network architecture



```
→ layer_1 = Dense(units=3, activation="sigmoid")
→ layer_2 = Dense(units=1, activation="sigmoid")
→ model = Sequential([layer_1, layer_2])
```



		y
200	17	1
120	5	0
425	20	0
212	18	1

targets

```
x = np.array([[200.0, 17.0],
              [120.0, 5.0],
              [425.0, 20.0],
              [212.0, 18.0]])
```

4 x 2

```
y = np.array([1,0,0,1])
```

```
model.compile(...)
```

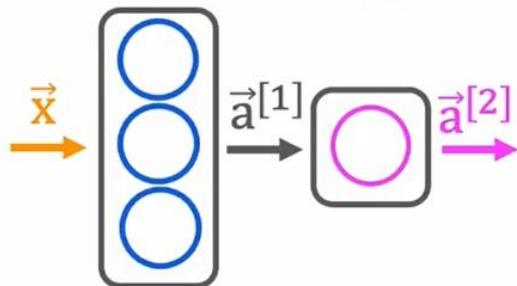
```
model.fit(x,y)
```

← more about this next week!

```
→ model.predict(x_new) ←
```

Building a Neural Network

Building a neural network architecture



```
→ model = Sequential([
→   Dense(units=3, activation="sigmoid"),
→   Dense(units=1, activation="sigmoid")])
```

		y
200	17	1
120	5	0
425	20	0
212	18	1

targets

```
x = np.array([[200.0, 17.0],
[120.0, 5.0],
[425.0, 20.0],
[212.0, 18.0]])
```

4 x 2

```
y = np.array([1,0,0,1])
model.compile(...)
```

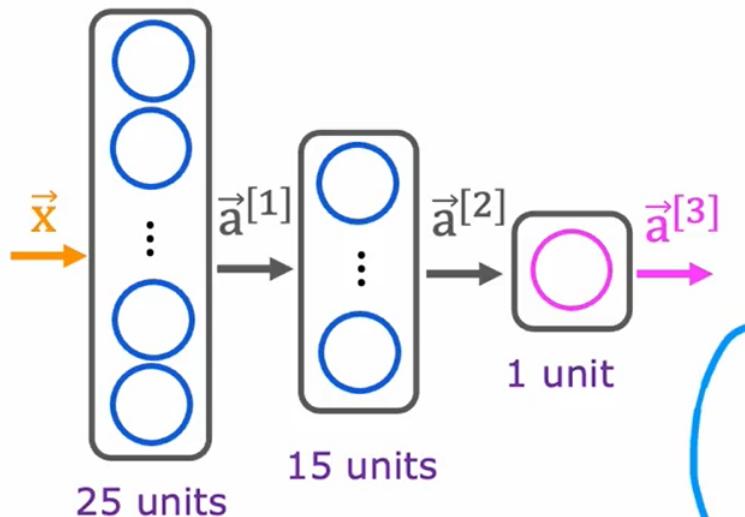
model.fit(x,y)

← more about this next week!

```
→ model.predict(x_new) ←
```

Building a Neural Network

Digit classification model



```
→ layer_1 = Dense(units=25, activation="sigmoid")
→ layer_2 = Dense(units=15, activation="sigmoid")
→ layer_3 = Dense(units=1, activation="sigmoid")
→ model = Sequential([layer_1, layer_2, layer_3])
model.compile(...)

x = np.array([[0..., 245, ..., 17],
              [0..., 200, ..., 184]])
y = np.array([1,0])

model.fit(x,y)
→ model.predict(x_new)
```