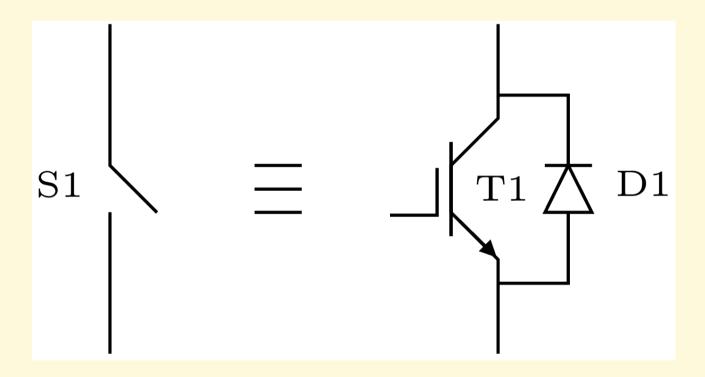
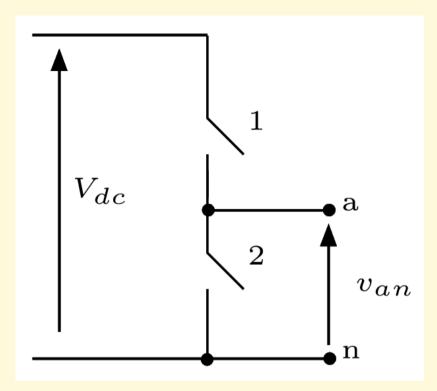
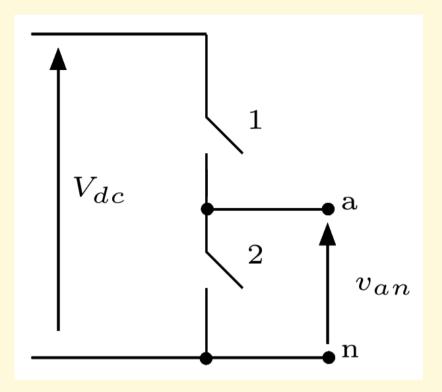
# Voltage source converters (VSCs)

## Switch used:

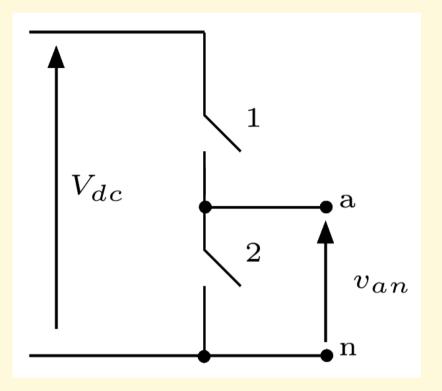






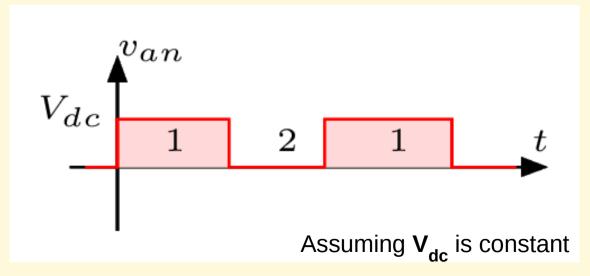
Switches S1 and S2 are complementary to each other

$$v_{an} = V_{dc}$$
 ... if S1 is ON
$$= 0$$
 ... if S2 is ON



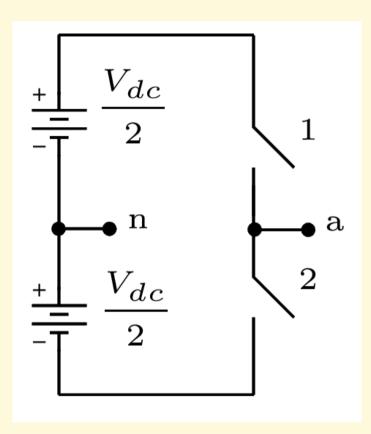
Switches S1 and S2 are complementary to each other

$$v_{an} = V_{dc}$$
 ... if S1 is ON
$$= 0$$
 ... if S2 is ON

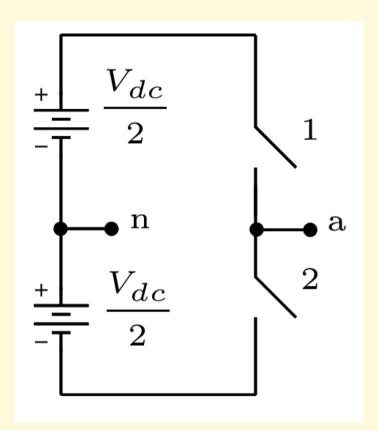


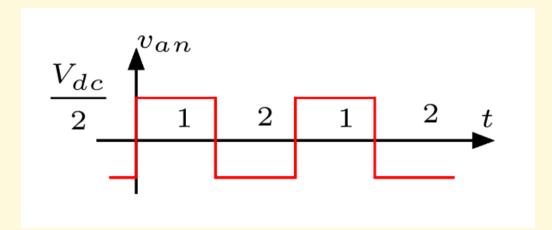


#### Consider:



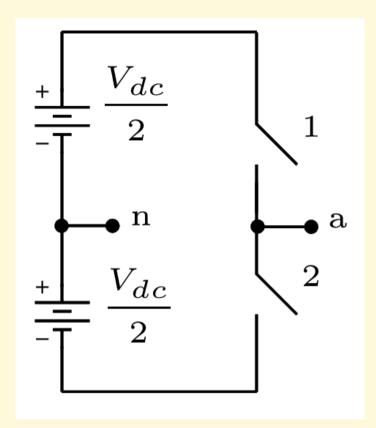
#### Consider:

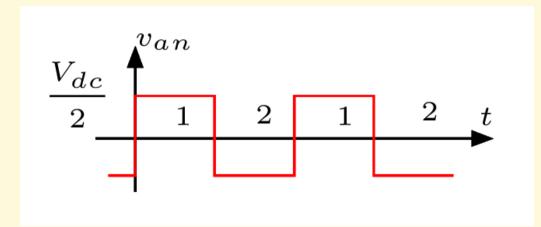




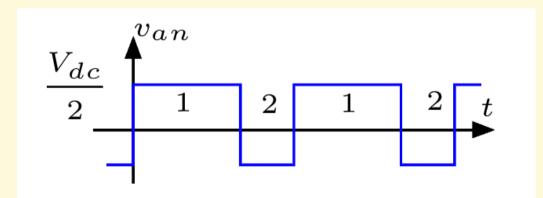
Fundamental + harmonic components

#### Consider:

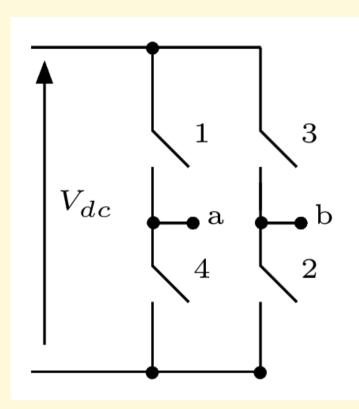


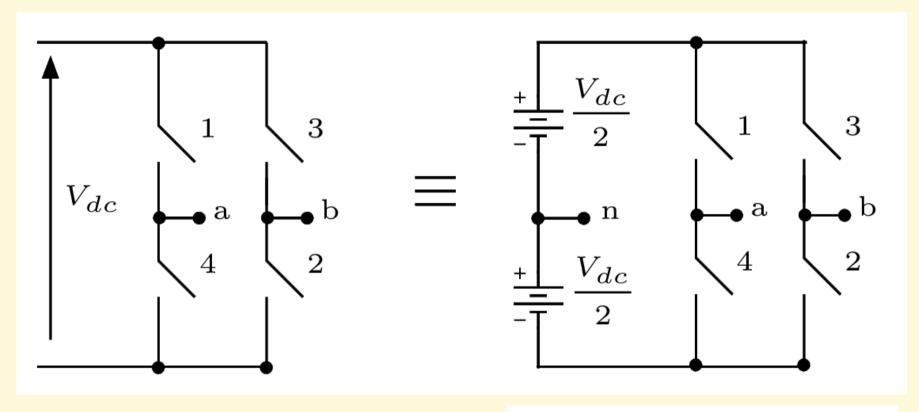


Fundamental + harmonic components

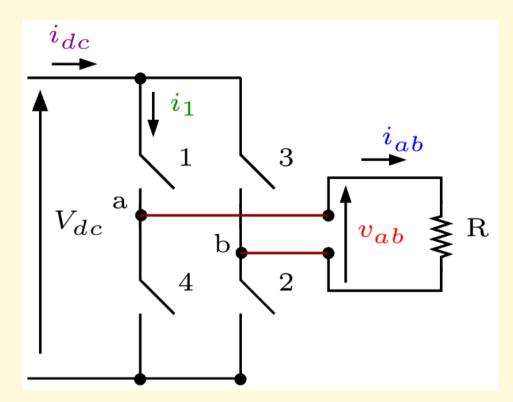


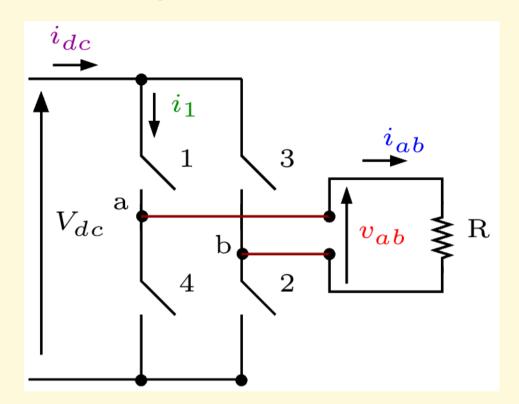
DC + Fundamental + harmonic components

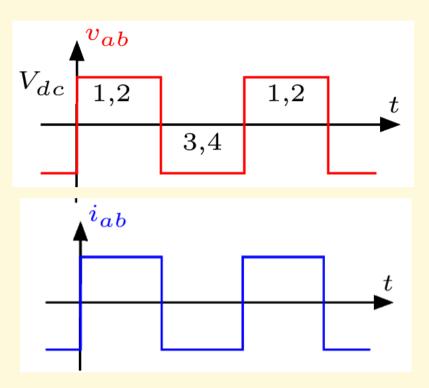


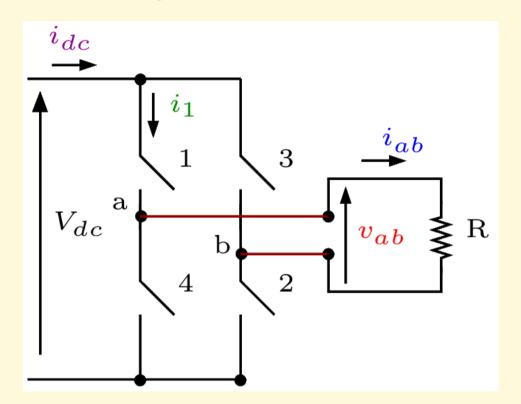


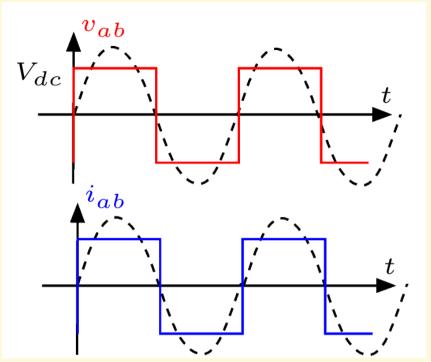
$$v_{ab} = v_{an} - v_{bn}$$

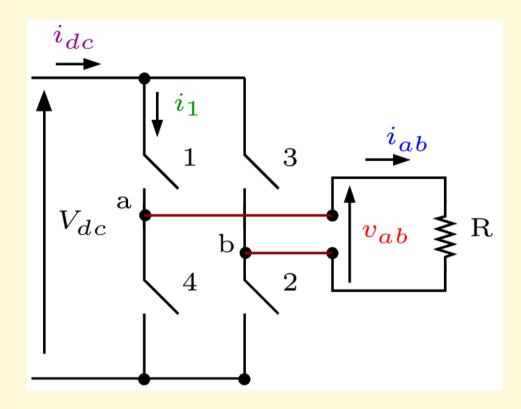


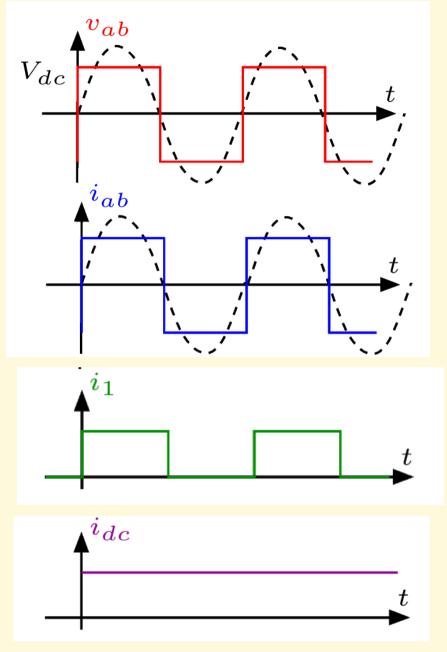


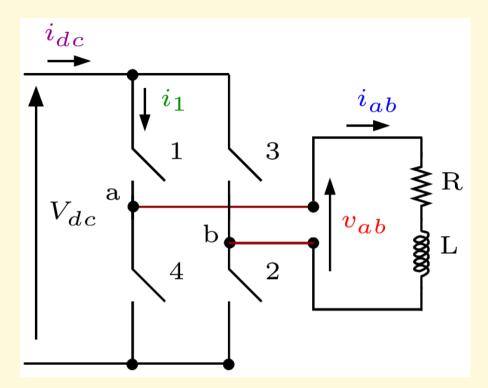


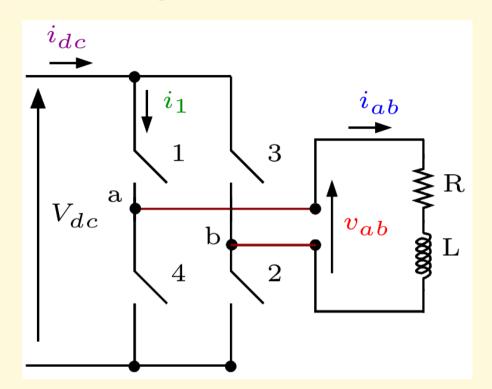


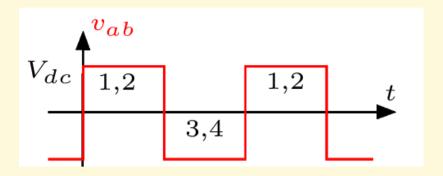


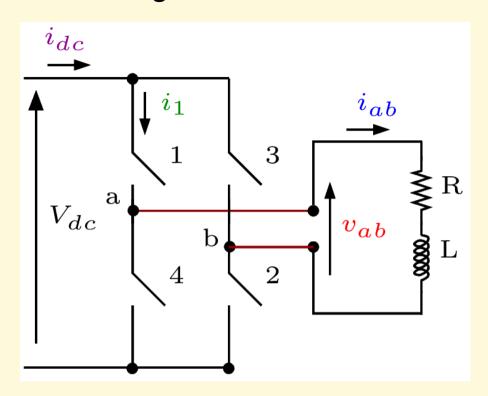


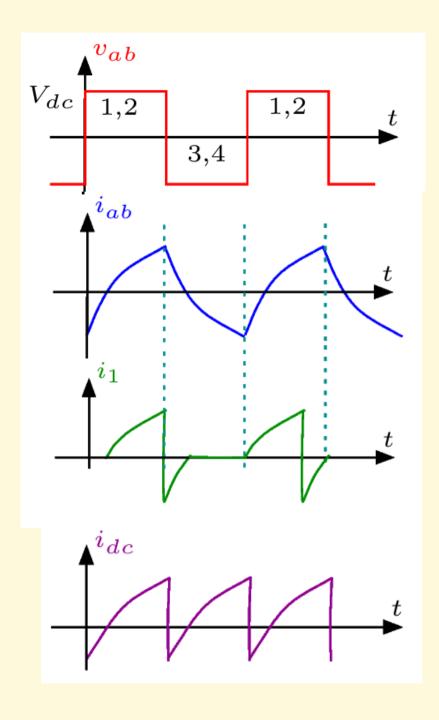




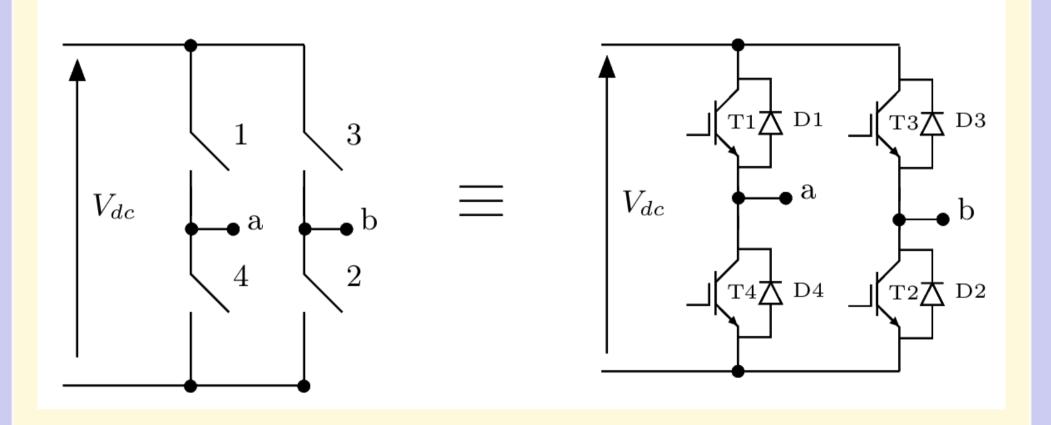






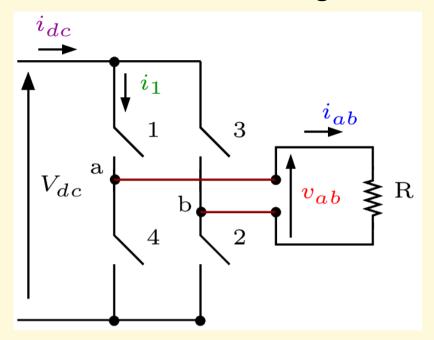


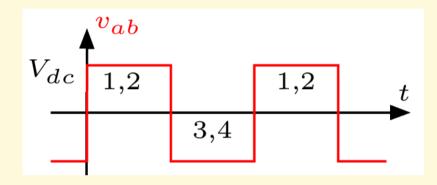
Note: two level full bridge VSC is realized as:



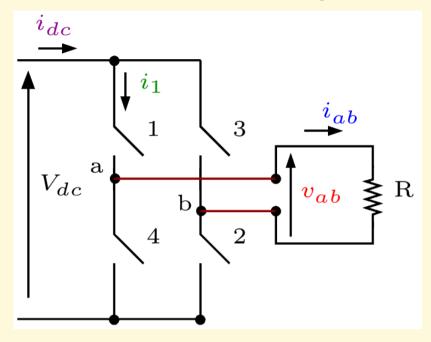


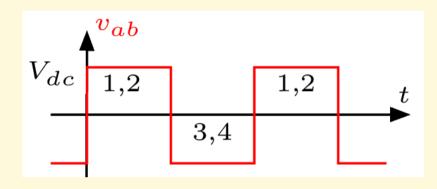
## Full bridge VSC (harmonic elimination)

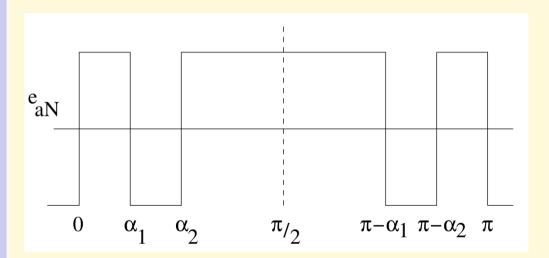




#### Full bridge VSC (harmonic elimination)



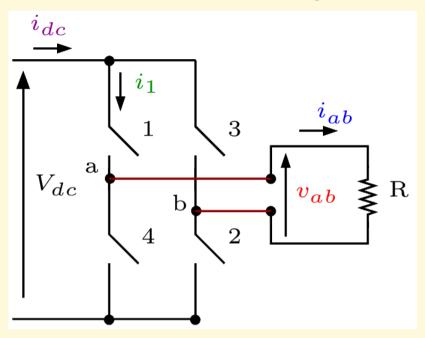


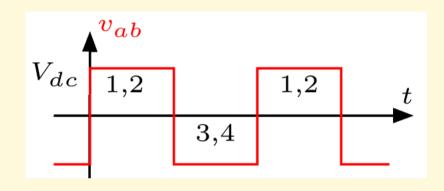


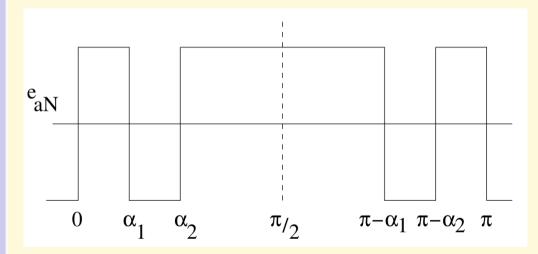
4 voltage reversals in a half cycle

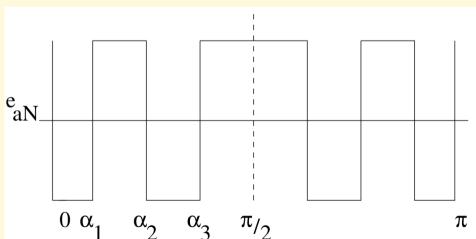
Source: K. R. Padiyar, FACTS controllers in power transmission and distribution, New Age publication, 2007.

### Full bridge VSC (harmonic elimination)





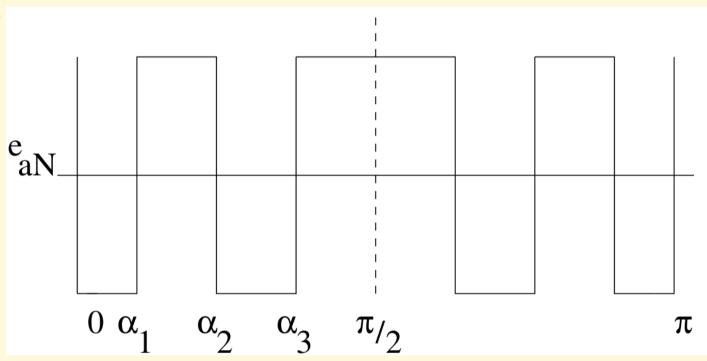




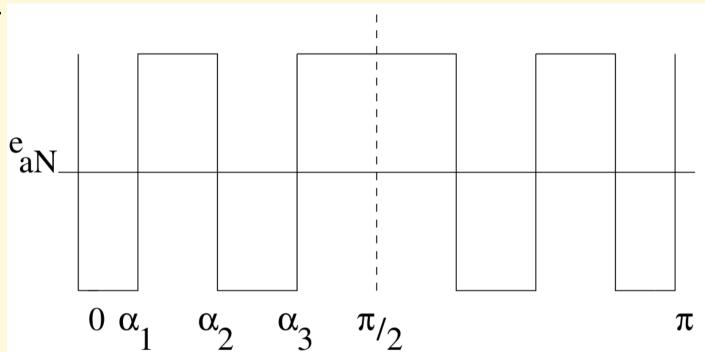
4 voltage reversals in a half cycle

6 voltage reversals in a half cycle

Consider



Consider



The switching angles are estimated using numerical methods:

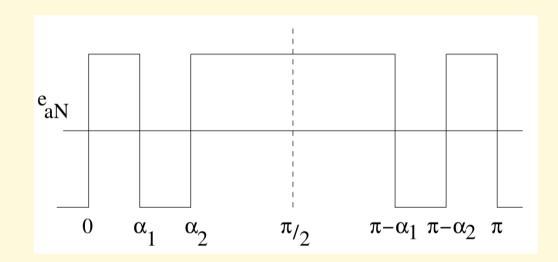
$$\bar{m} = 2[\cos \alpha_1 - \cos \alpha_2 + \cos \alpha_3] - 1$$
 $0 = 2[\cos 5\alpha_1 - \cos 5\alpha_2 + \cos 5\alpha_3] - 1$ 
 $0 = 2[\cos 7\alpha_1 - \cos 7\alpha_2 + \cos 7\alpha_3] - 1$ 

#### Example:

If there are two voltage reversals in a quarter cycle, the values of  $\alpha_1$  and  $\alpha_2$  for eliminating 5<sup>th</sup> and 7<sup>th</sup> voltage harmonic are

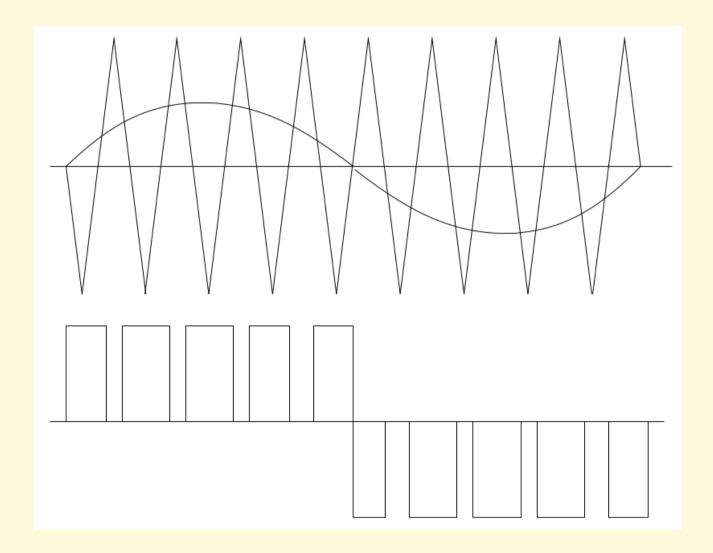
$$\alpha_1 = 16.2^{\circ}$$
 $\alpha_2 = 22^{\circ}$ 

$$\alpha_2 = 22^{\circ}$$



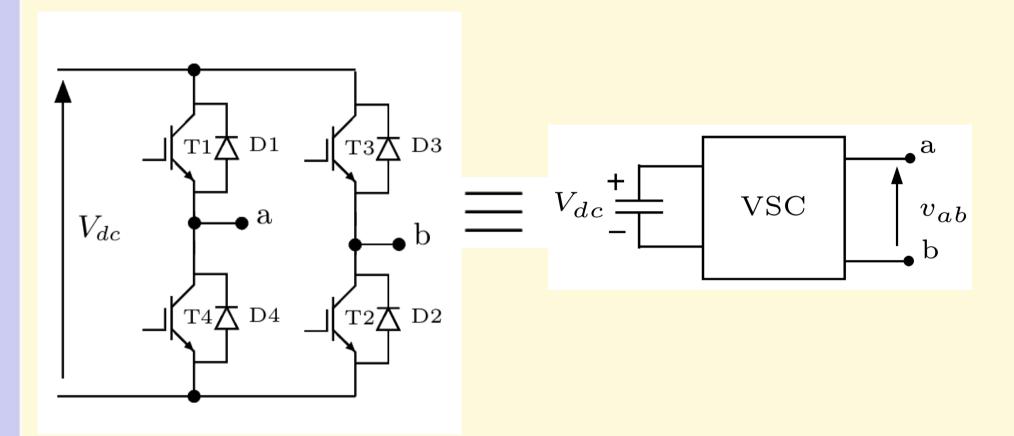
The modulation index is:

$$\bar{m} = 1 - 2(\cos \alpha_1 - \cos \alpha_2) = 0.934$$

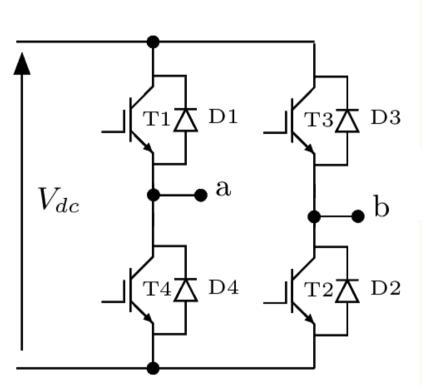


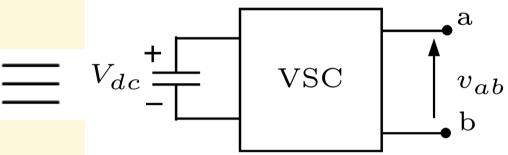
Sine triangle PWM

#### VSC block equivalent

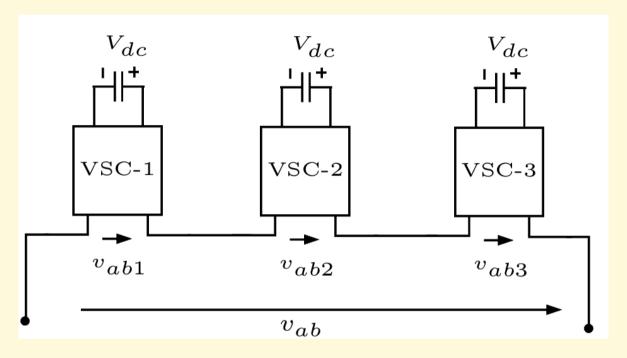


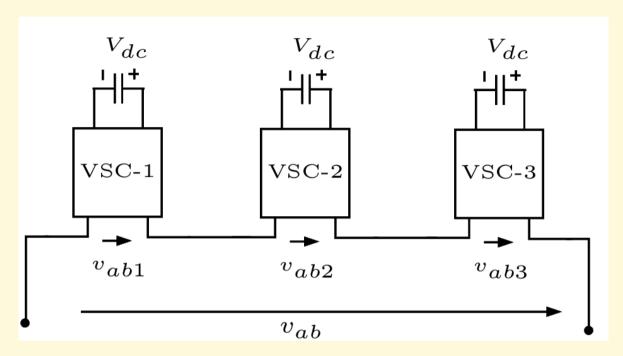
#### VSC block equivalent





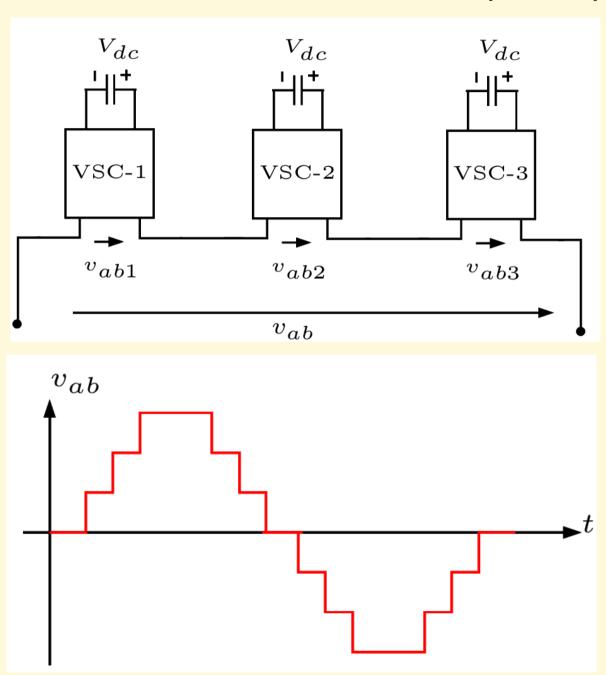
Possible output levels: +V<sub>dc</sub>, 0, -V<sub>dc</sub>

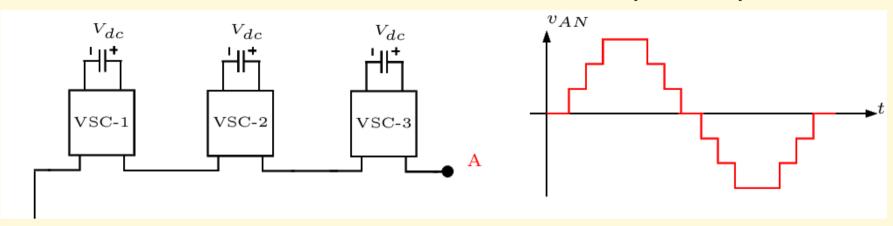


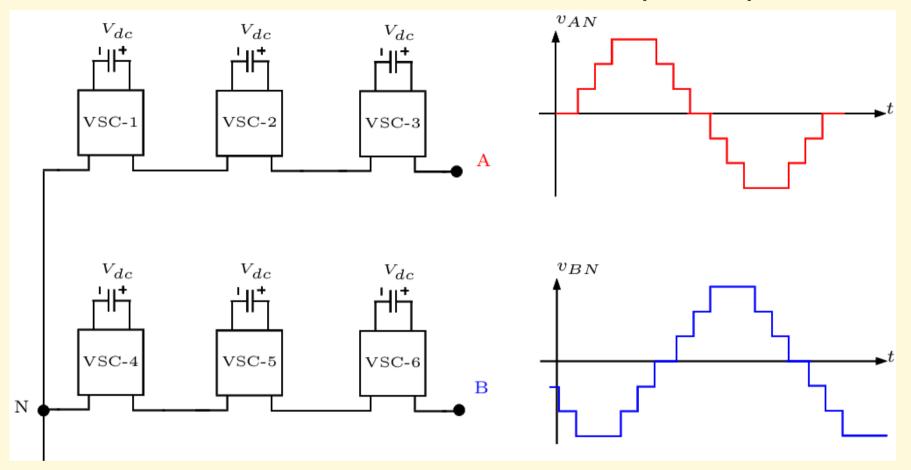


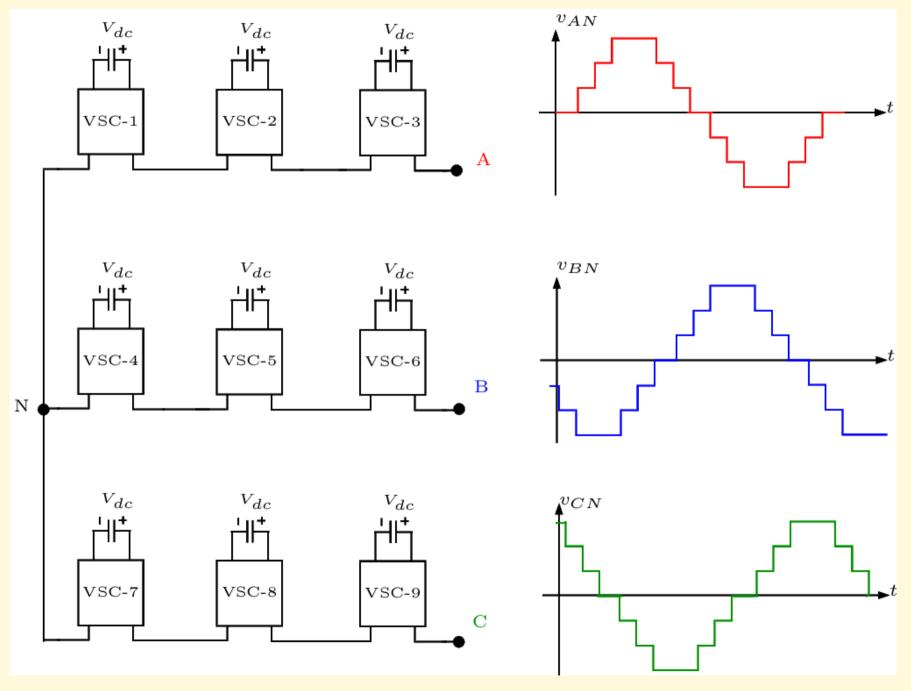
#### Possible output levels:

$$+3V_{dc}$$
,  $+2V_{dc}$ ,  $+V_{dc}$ , 0,  $-V_{dc}$ ,  $-2V_{dc}$ ,  $-3V_{dc}$ 



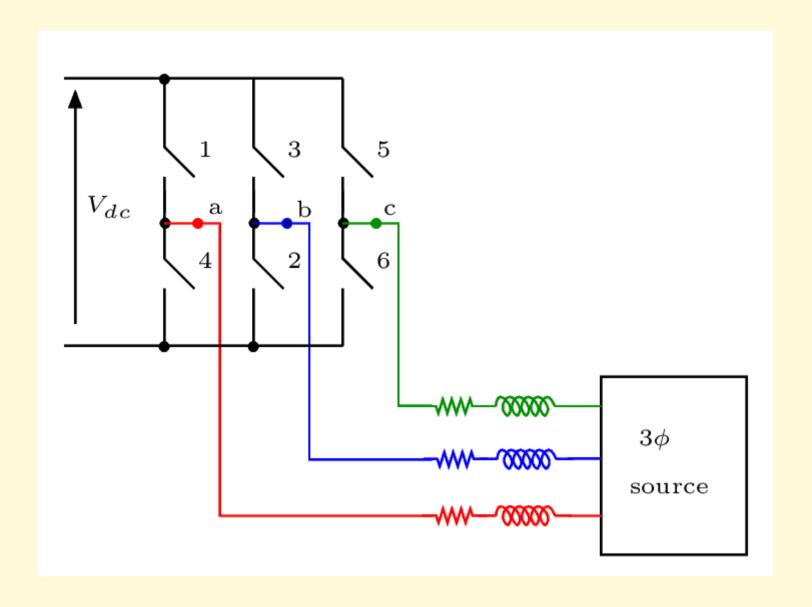




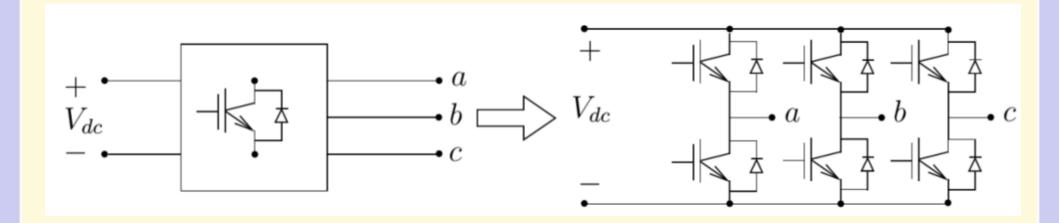




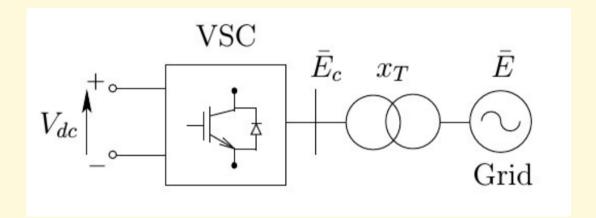
#### Three-phase two level bridge circuit



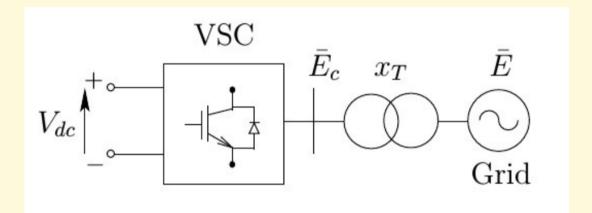
## Three-phase two level bridge circuit

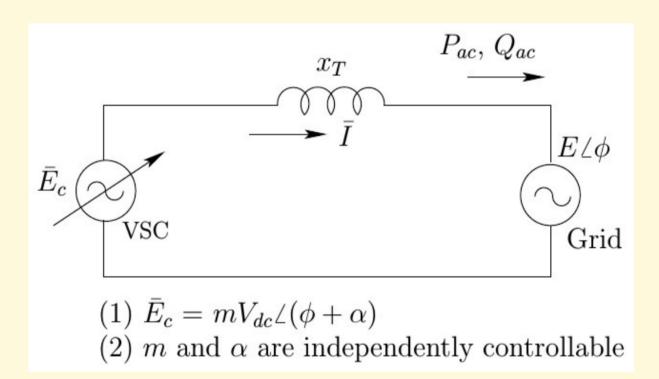


#### VSC Connected to Grid

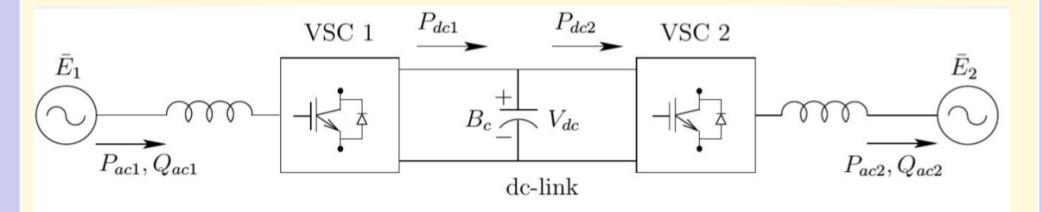


#### VSC Connected to Grid



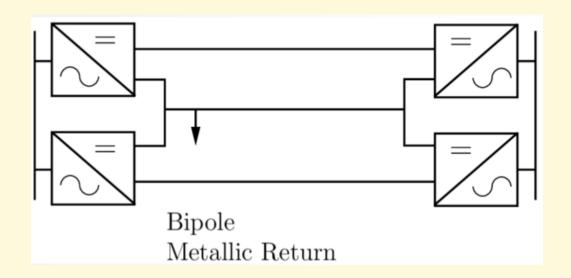


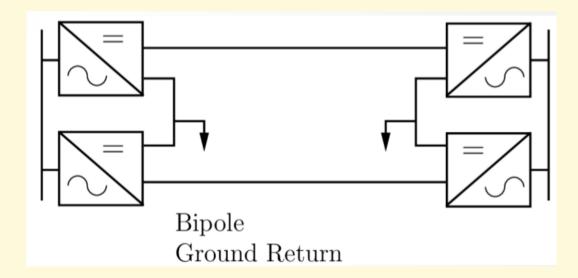
#### Example: Monopolar HVDC link



- (1)  $P_{ac1}=P_{dc1}$ ,  $P_{ac2}=P_{dc2}$  (loss-less converter)
- (2)  $P_{dc1}=P_{dc2}$  in steady state
- (3)  $Q_{ac1}$ ,  $Q_{ac2}$  are independently controllable

# **HVDC Configurations**





## **HVDC Configurations**

