## **Load characteristics**

#### Some aspects of loads

$$P_L = P_{L0}$$

$$Q_L = Q_{L0}$$

 $P_{LO}$  and  $Q_{LO}$  are the real and reactive power at nominal voltage of  $V_o$  and frequency  $f_o$ 

#### Some aspects of loads

$$P_L = P_{L0} \cdot \left( 1 + k_{pv} \frac{V - V_o}{V_o} \right)$$

$$Q_L = Q_{L0} \cdot \left(1 + k_{qv} \frac{V - V_o}{V_o}\right)$$

Variance with voltage

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#### Some aspects of loads

$$P_{L} = P_{L0} \left( 1 + k_{pv} \frac{V - V_{o}}{V_{o}} \right) \left( 1 + k_{pf} \frac{f - f_{o}}{f_{o}} \right)$$

$$Q_{L} = Q_{L0} \left( 1 + k_{qv} \frac{V - V_{o}}{V_{o}} \right) \left( 1 + k_{qf} \frac{f - f_{o}}{f_{o}} \right)$$

Variance with voltage

Variance with frequency

 $P_{Lo}$  and  $Q_{Lo}$  are the real and reactive power at nominal voltage of  $V_o$  and frequency  $f_o$ 

#### Typical values for load constants

Component	Power factor	$k_{pv}$	k <sub>qv</sub>	k <sub>pf</sub>	<b>k</b> <sub>qf</sub>
Refrigerator	0.8	0.77	2.5	0.53	-1.5
Incandescent lights	1	1.55	0	0	0
Fluorescent lights	0.9	0.96	7.4	1	-2.8
Industrial motors	0.88	0.07	0.5	2.5	1.2
Fan motors	0.87	80.0	1.6	2.9	1.7
Agricultural pumps	0.85	1.4	1.4	5	4
Arc furnace	0.7	2.3	1.6	-1	-1
Transformer (unloaded)	0.64	3.4	11.5	0	-11.8

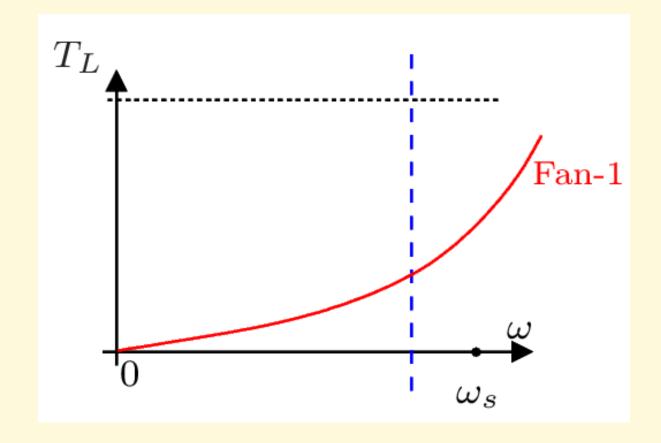
Source: Prabha Kundur, Power System Stability and Controls, TMH-1992.

Load torque for fan as a function of speed is:

$$T_L = \text{constant} \left(\frac{\omega_r}{\omega_s}\right)^2$$

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Load torque of motor as a function of speed is

$$T_m = \frac{3V_e^2 \frac{R_r}{s \omega_s}}{\left(R_e + \frac{R_r}{s}\right)^2 + (X_e + X_r)^2}$$
 ,  $s = \frac{\omega_s - \omega_r}{\omega_s}$ 

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where,

 $\omega_s$  is synchronous speed at the supply frequency

 $R_r$  is rotor resistance

Thevenin impedance and a voltage source

$$V_e = \frac{jX_m}{R_s+j(X_S+X_m)} \, V \ , \ Z_e = R_e+jX_e = \frac{jX_m \, (R_s+jX_s)}{R_s+j(X_S+X_m)} \label{eq:Ve}$$

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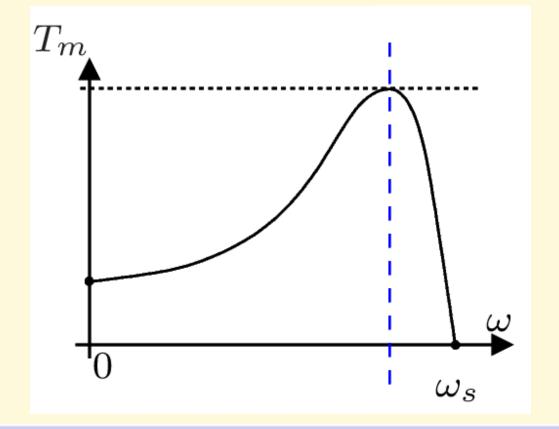
 $X_s$ ,  $X_r$  and  $X_m$  are the stator, rotor and magnetising reactances in at a given frequency

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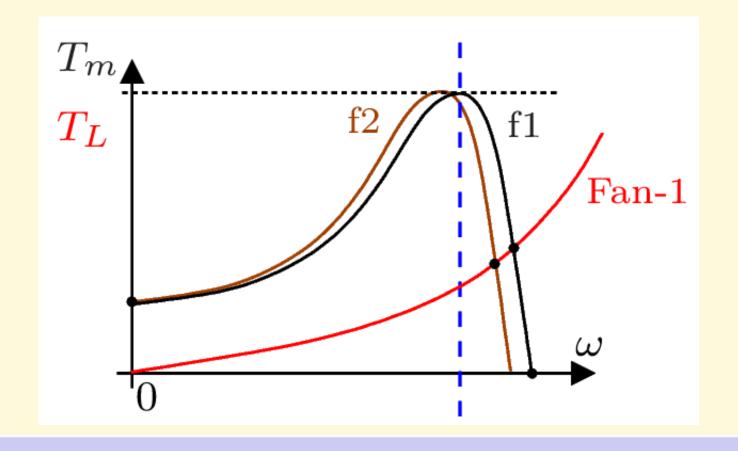


The operating speed is obtained from the equation

$$T_m(\omega_r) = T_L(\omega_r)$$

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Wind energy conversion systems (WECS)

- Now a major source of energy.
- Currently more than 440 GW; expected to exceed 760 GW by 2020.
- Wind turbines with individual capacities of up to 6 to 8 MW are now available.
- Wind farms (onshore and offshore) having overall ratings of hundreds of megawatts are in operation.

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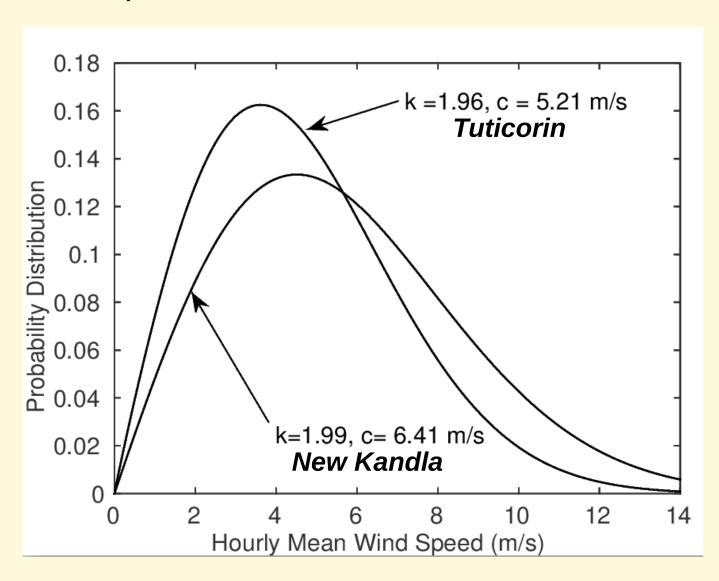
Weibull distribution:

$$p(v_w) = \frac{k}{c} \left(\frac{v_w}{c}\right)^{k-1} e^{\left[-\left(\frac{v_w}{c}\right)^k\right]}$$

where c is the scale factor having the unit of speed and k is a dimensionless shape factor

#### Wind Characteristics

These correspond to the Weibull curves that fit the hourly mean wind speed measured at two locations in India.



- --> A wind turbine can be thought of as intercepting a moving tube of wind which has a cross-sectional area  $(A_{w})$  in  $m^{2}$ .
- --> The mass of air flowing through this cross-section in h seconds is given by,

$$M = A_w \rho v_w h$$

where,

 $\rho$  is the density of air in kg/m³ and  $\nu_{_{W}}$  is the wind velocity in m/s.

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If this entire kinetic energy was to be extracted by the wind turbine, then its *power output* would be

$$P_o = \frac{1}{2} A_w \rho v_w^3$$

- --> This is not feasible as the wind has to continuously flow past the turbine, and cannot be abruptly halted.
- -->In practice only a fraction  $C_p$  (also called the turbine power coefficient) of this energy can be extracted.
- --> The theoretical maximum value of  $C_p$ , which is also called the **Betz** limit, is approximately **0.59**.

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- --> Thus, the power output of a wind turbine  $P_{\rm m}$  in W, can be expressed as follows:

 $P_m = \frac{1}{2} A_w \rho C_p v_w^3$ 

where,  $C_p$  is a function of the 'tip-speed ratio'  $\lambda$ , and the pitch angle of the turbine blades  $\beta$ .

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- --> Thus, the power output of a wind turbine P in W, can be expressed as follows:  $P_m = \frac{1}{2}\,A_w\,\rho\,C_p v_w^{\ 3}$

 $2^{1-w} p \circ p \circ w$ 

where,  $C_p$  is a function of the 'tip-speed ratio'  $\lambda$ , and the pitch angle of the turbine blades  $\beta$ .

The tip speed ratio is given as  $\ \lambda = \frac{\omega_m' \, R}{v_w}$ 

 $\omega_m'$  is the speed of the turbine in rad/s.

--> The following expression may be used for power system studies:

$$C_p = c_1 \left( \frac{c_2}{\lambda_i} - c_3 \beta - c_4 \beta^{c_5} - c_6 \right) e^{\frac{-c_7}{\lambda_i}}$$

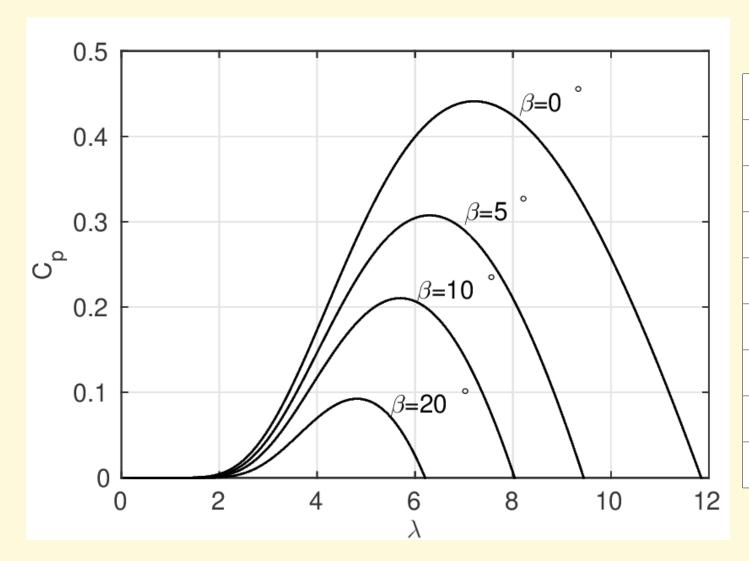
where,

$$\frac{1}{\lambda_i} = \frac{1}{\lambda + c_8 \beta} - \frac{c_9}{\beta^3 + 1}$$

--> The pitch angle  $\beta$  is expressed in degrees in these equations.

--> The coefficients  $c_1$  to  $c_9$  can be determined by using a numerical optimization procedure which minimizes the error between the power curve obtained from these equations and the one obtained from the manufacturer's documentation.

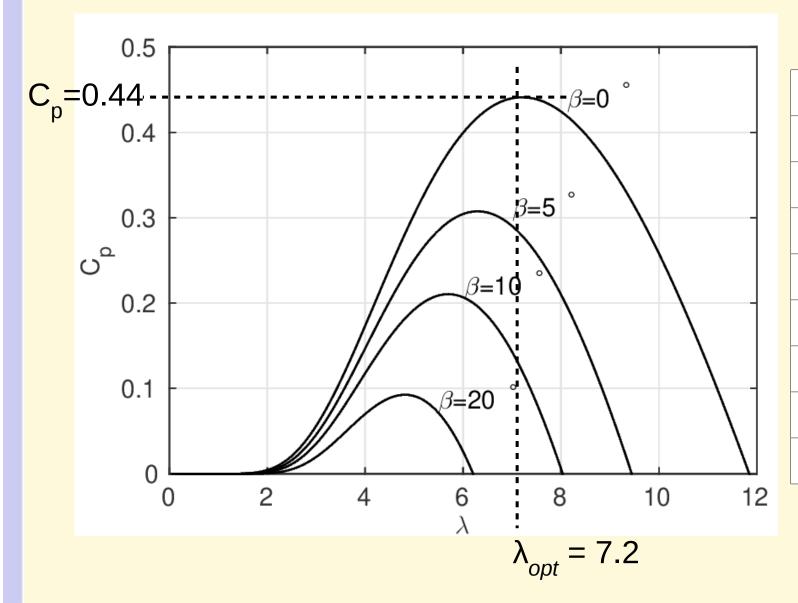
#### Wind Turbines



## Turbine parameters

$C_1$	0.73
C <sub>2</sub>	151
C <sup>3</sup>	0.58
<b>C</b> <sub>4</sub>	0.002
<b>C</b> <sub>5</sub>	2.14
<b>C</b> <sub>6</sub>	13.2
<b>C</b> <sub>7</sub>	18.4
C <sub>8</sub>	-0.02
C <sub>9</sub>	-0.003

#### **Wind Turbines**



## Turbine parameters

0.73	
151	
0.58	
0.002	
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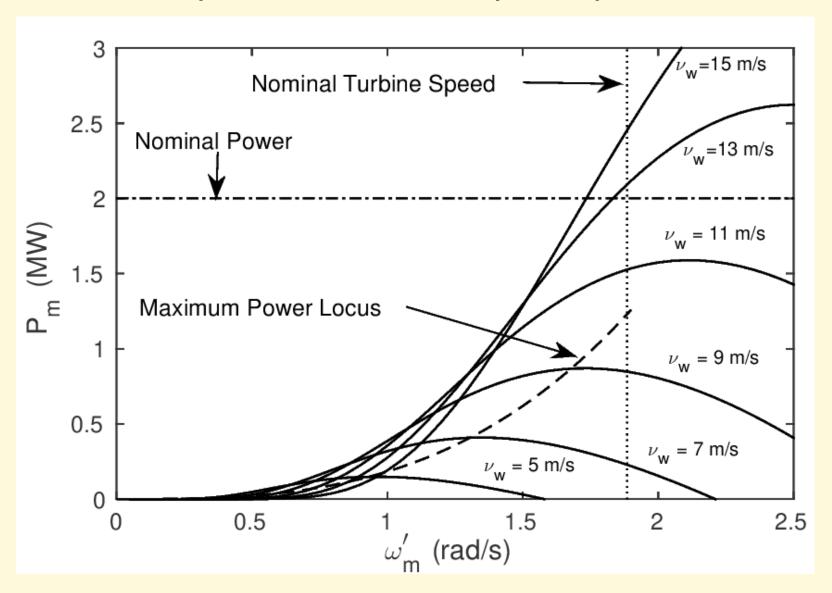
# Wind Turbines: Maximum Power Extraction (for various wind speeds)

--> For the turbine parameters given in the previous slide, for  $\beta = 0^{\circ}$ , the approximate optimum value of  $C_{p} = 0.44$  which occurs when  $\lambda_{opt} = 7.2$  units.

--> The maximum power that can be extracted as a function of turbine speed is given by:

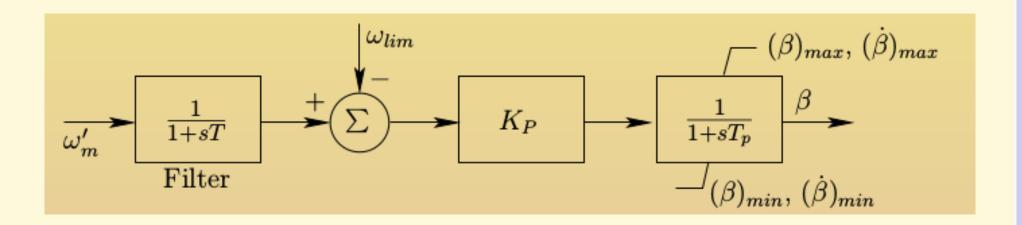
$$P_{m_{opt}} = \left[ \frac{1}{2} \frac{\rho A_w R^3 C_{p_{opt}}}{\lambda^3_{opt}} \right] (\omega'_m)^3 = k_{opt} (\omega'_m)^3$$

# Wind Turbines: Power Extracted vs Turbine Speed (for various wind speeds)



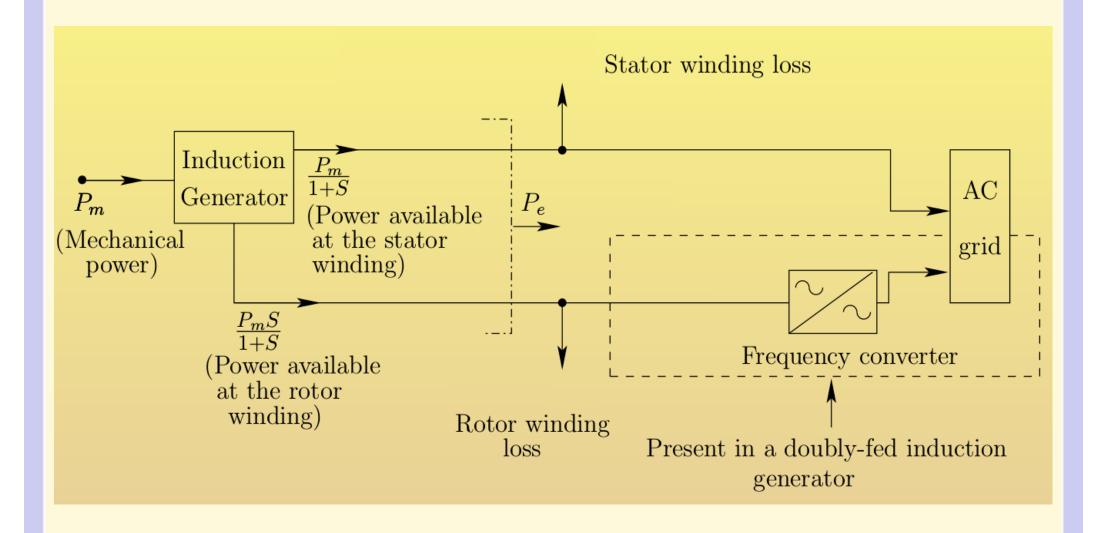
$$\beta = 0^{\circ}, R = 37.5 \text{ m}, \rho = 1.225 \text{ kg/m}^3$$

#### Wind Turbines: Pitch and Stall Control

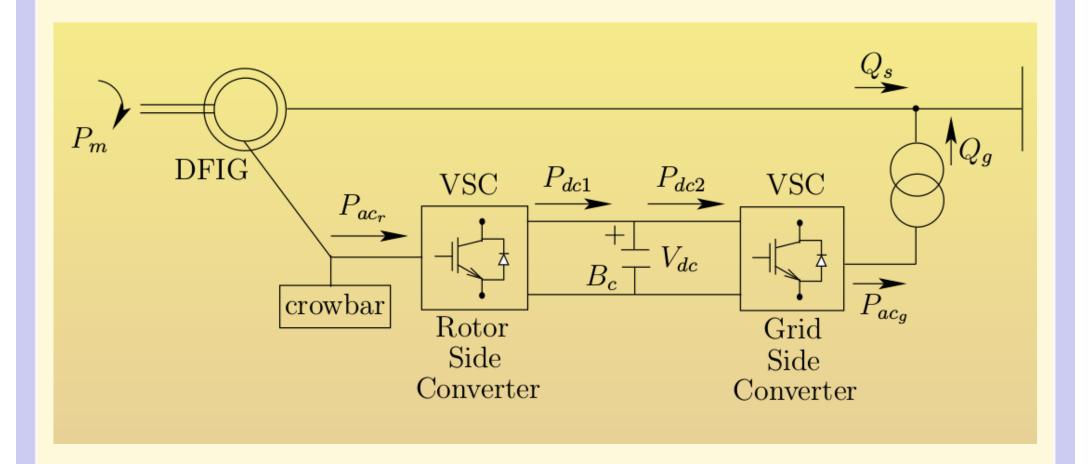


- --> Pitch  $(\beta)$  control involves turning the blades around their longitudinal axis.
- --> This reduces Cp , which is a function of  $\beta$ , thereby reducing the power output.
- --> The rotor aerodynamics may be designed to stall (lose power) when the wind speed exceeds a certain level. This is known as stall control.

#### Doubly fed induction generator (DFIG) – Power flow

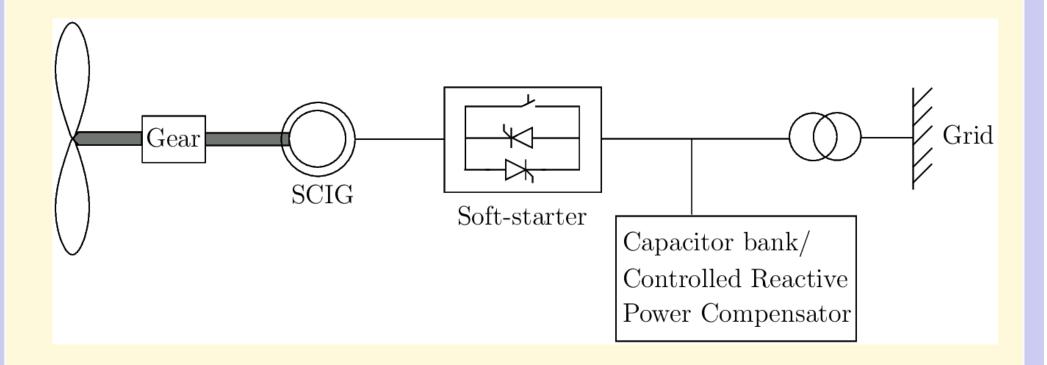


#### Doubly fed induction generator (DFIG) – Power flow

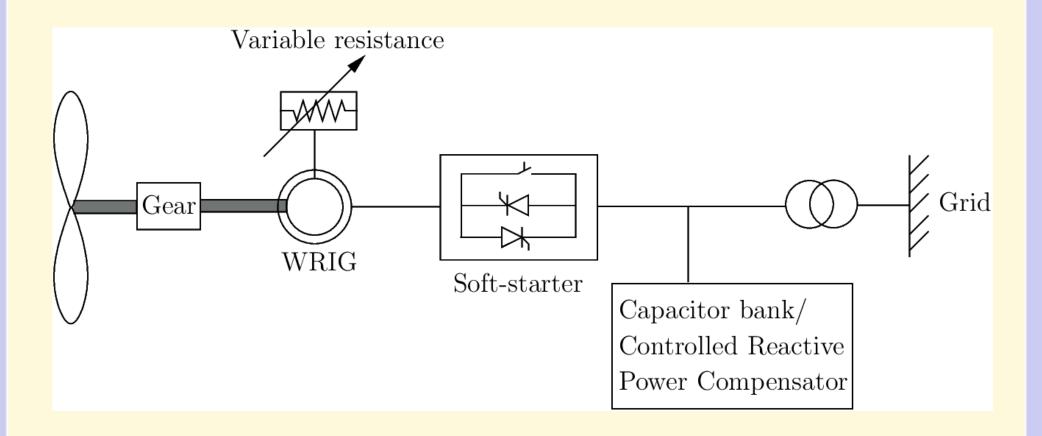




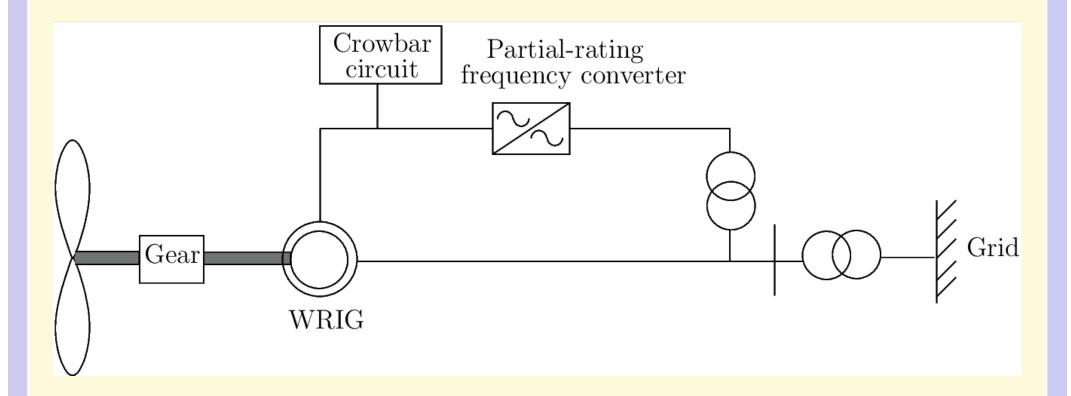
#### Generator and Power Electronic Configurations - Type I



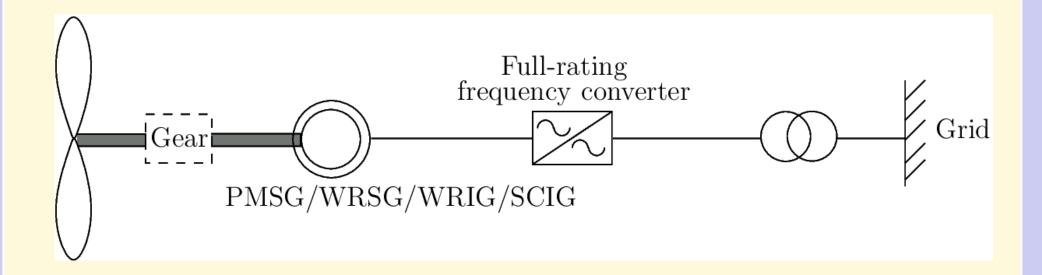
#### Generator and Power Electronic Configurations - Type II



#### Generator and Power Electronic Configurations - Type III

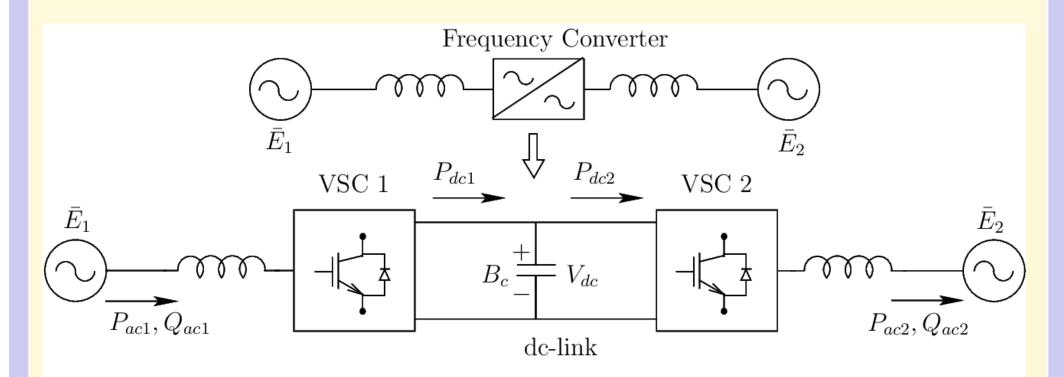


#### Generator and Power Electronic Configurations - Type IV





#### Generator and Power Electronic Configurations Frequency Conversion using VSCs



- (1)  $P_{ac1}=P_{dc1}$ ,  $P_{ac2}=P_{dc2}$  (lossless converter)
- (2)  $P_{dc1}=P_{dc2}$  in steady state
- (3)  $Q_{ac1}$ ,  $Q_{ac2}$  are independently controllable



**Transmission lines and cables**