

Tutorial 3

EE302 Control Systems 20th Feb 2020.

Q-1 Consider $x \rightarrow \begin{matrix} + \\ \circ \\ - \end{matrix} \rightarrow \begin{matrix} \text{---} \\ \text{---} \end{matrix} \rightarrow \begin{matrix} \text{---} \\ \text{---} \end{matrix} \rightarrow y$. Assume (in this problem) closed loop is stable.

Consider inputs: step, ramp, parabolic inputs.

For type 0, type 1, type 2 systems, obtain steady state error (for each of the 3 inputs.)

	type 0	type 1	type 2
step	---	---	---
ramp	---	---	---
parabolic	---	---	---

Q-2: Suppose G above is

$$\frac{k}{s^3 + 4s^2 + 2s + 9}$$

Find range of k for closed loop stability using Routh Hurwitz table.

Q-3: Suppose G (in prob 1) is $\frac{k}{(s^2 + s + 1)(s + 5)}$.

(a) Find range of k for closed loop stability.

(b) Approximate G by a 2nd order system \tilde{G} (but same position constant) and for \tilde{G} obtain range of k for closed loop stability.

Q-3: Routh-Hurwitz table.

(a) Find number of OLHP/ORHP/jR roots of $3s^7 + 9s^6 + 6s^5 + 4s^4 + 7s^3 + 8s^2 + 2s + 6$.

(b) Deduce with reason just Hurwitz or not-Hurwitz (without Routh-Hurwitz) & with the table for (at least 2 diff. reasons).

(c) For $s^5 + 2s^4 + 3s^3 + 6s^2 + 5s + 3$, find OLHP, ORHP, jR breakup using ϵ -method & reciprocal polynomial (reverse coefficients).

(d) Find OLHP, ORHP, jR breakup for $(s^5 + 7s^4 + 6s^3 + 42s^2 + 8s + 56) = p(s)$ and also for $sp(s) \rightarrow$ with & without extracting s as a factor. (entire row is zero at some stage.).

Q-4: For $s^6 + s^5 - 6s^4 - s^2 - s + 6 =: p(s)$

split $p(s)$ into $p_{\text{even}}(s) + p_{\text{odd}}(s) = P_{\text{higher}} + P_{\text{lower}}$ (say).

Perform successive division of P_{higher} by P_{lower} to see that we get Routh-Hurwitz table exactly.

Q-5: For the polynomial

$$(2.04 + 6q_1 + 6q_2 + 2q_1q_2) + s(q_1 + q_2 + 2) + s^2(q_1 + q_2 + 2) + s^3$$

sketch the stable region in the q_1, q_2 parameter space.

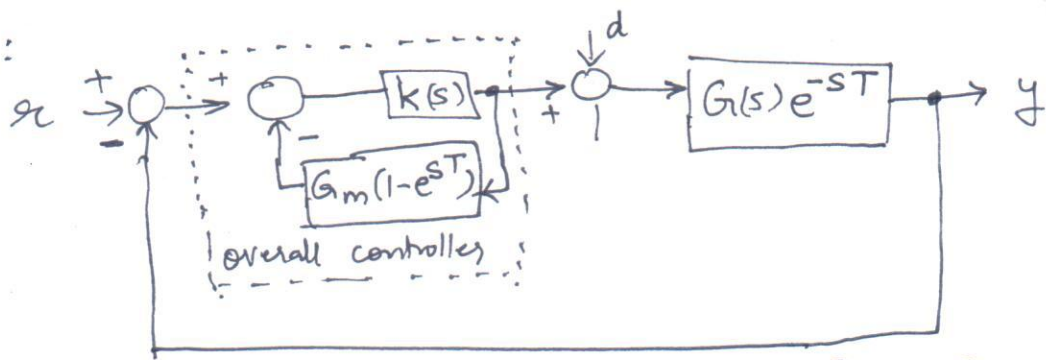
Q-6: Can $(1 + s + se^{-s}) = 0$ have a root in the RHP?

Justify using proper arguments. (This is called "transcendental equation" & arises due to pure delays)

Q-7: Pure delays in the system are eliminated in the closed loop using "the Smith predictor" making Controller design easier.

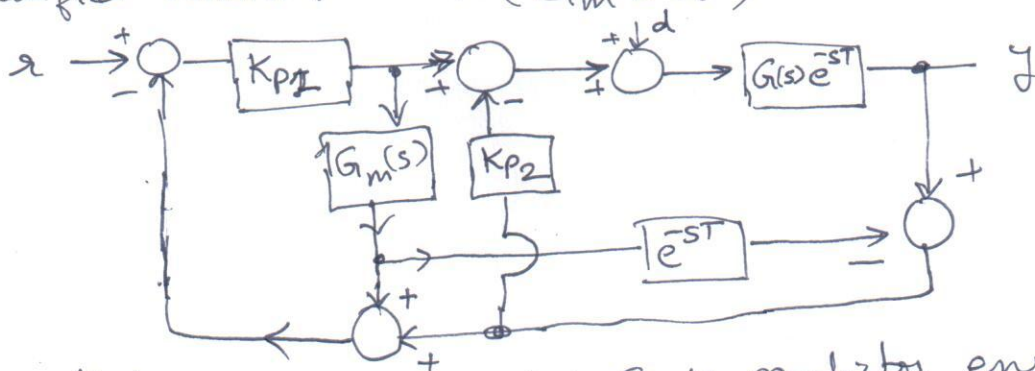
Consider the following configuration (proposed by O.J. Smith in 1959.)

Q-7 contd:



e^{-sT} \equiv pure delay of time T. Smith predictor: $G_m = G$

- (a) Show that if $G(s)$ is of type 0, then $K(s) = K_p + \frac{K_I}{s}$ results in zero steady state error to step input and also rejects constant disturbance d . (Assume closed loop is stable.)
- (b) Will the above setup work if the system is of type 1?
- (c) Modified Smith predictor ($G_m = G$)



Show that the above modified Smith predictor ensures constant disturbance rejection & perfect tracking for $D(s) = \frac{1}{s} = R(s)$ when G is type 1 plant. (Assume closed loop is stable.)

- Q-8: Root locus: For following examples, draw root locus and find (if relevant) (a) Breakaway/breakin point, corresponding k value, (b) $j\omega$ crossing ω value & relevant k value, (c) Real axis segments, (d) Range of k (within $[0, \infty)$) to have stability, (e) Asymptotes angles, intersection

$$\frac{(s+1)(s+3)}{(s+2)(s+4)}, \quad \frac{(s+1)(s+3)}{(s+4)(s+6)}, \quad \frac{\omega_n s}{s^2 + \omega_n^2}, \quad \frac{(s-1)(s-2)}{(s+3)(s+4)}$$

- Q-9: Find gain k to have 15% OS for following open loop systems: $\frac{1}{s(s+2)}$, $\frac{1}{(s+0.01)(s+2)}$, $\frac{s+1}{(s+4)(s+2)}$.

For that k value, find steady state error for step input.

- Q-10 For above transfer functions (Q-9), find value of k that gives 10 seconds settling time (for step input).

- Q-11: Consider $d(s) + k n(s)$. Show that condition on k for repeated root in s is same as that for breakaway/breakin