

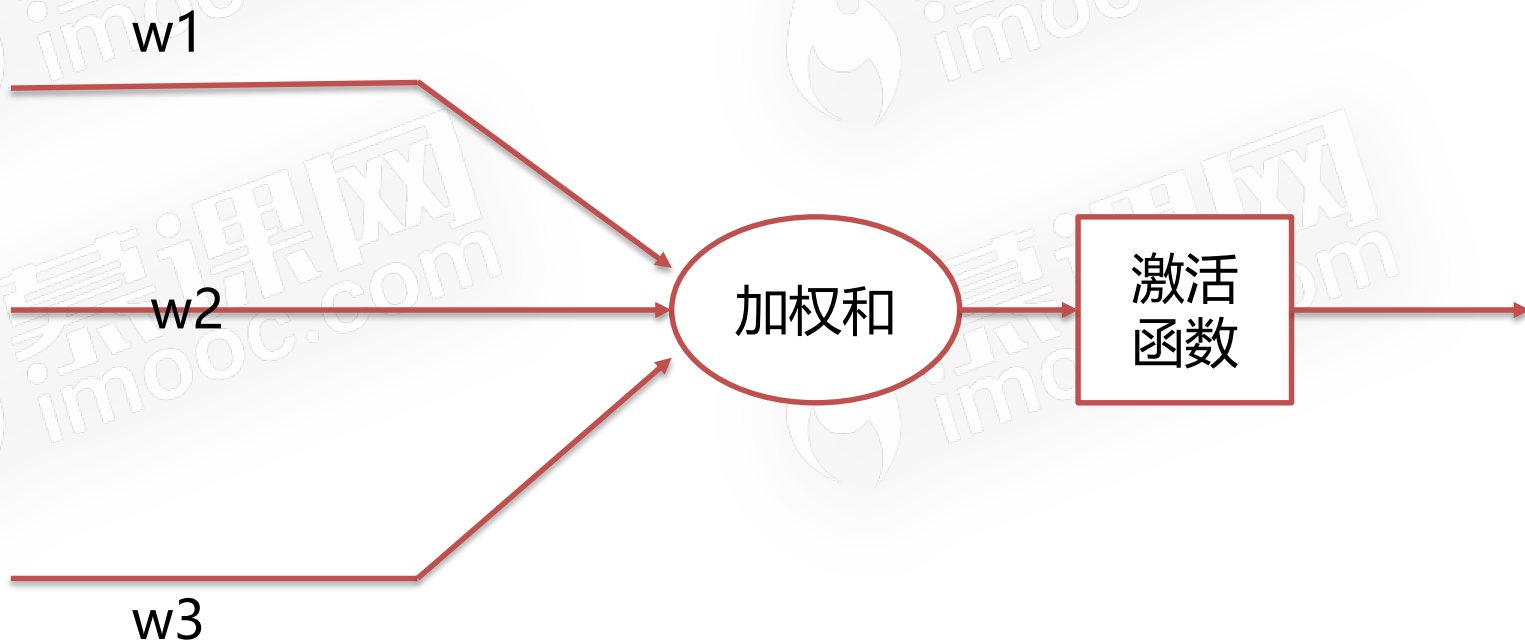
# Personal Recommendation Algorithm

# Main Flow

- 背景知识介绍之深度学习
- DNN网络结构与数学原理
- WD(wide and deep)网络结构与数学原理

# 神经元

- 什么神经元？

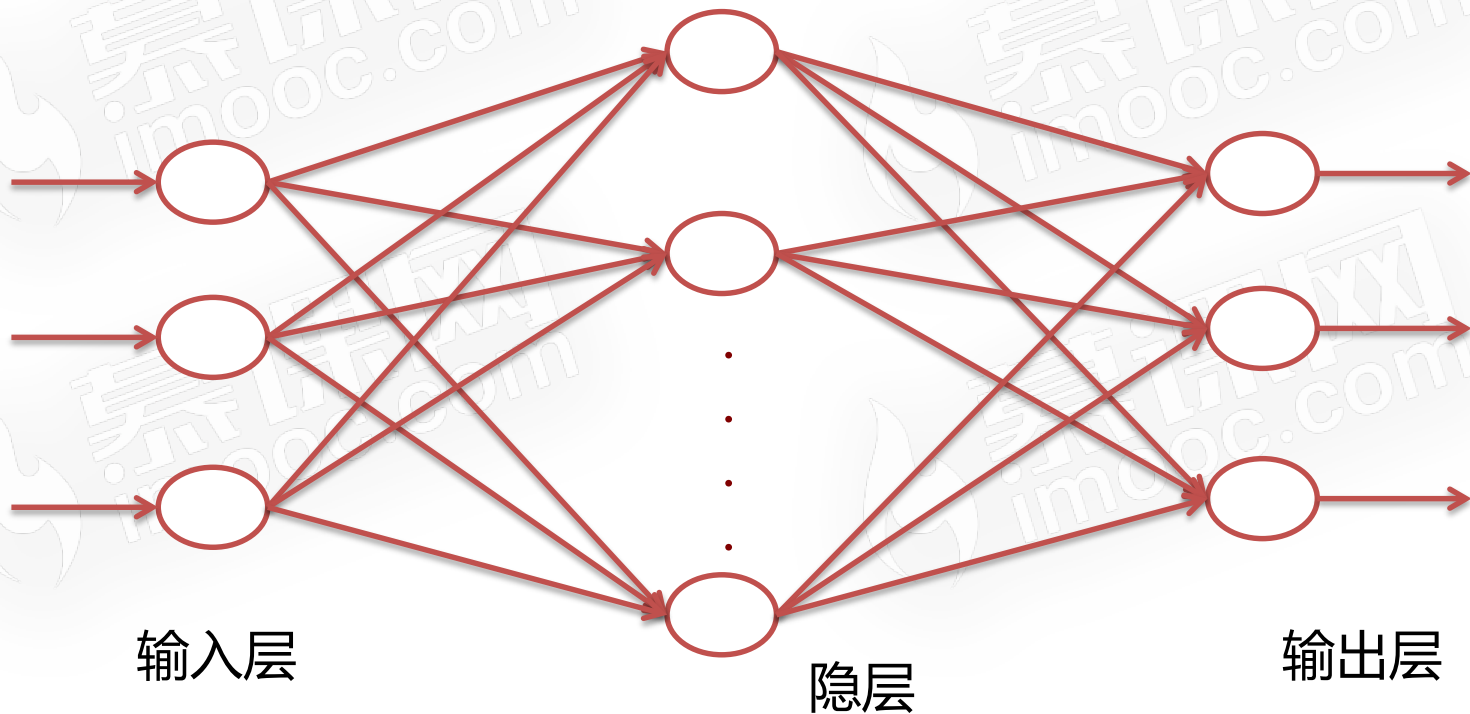


# 激活函数

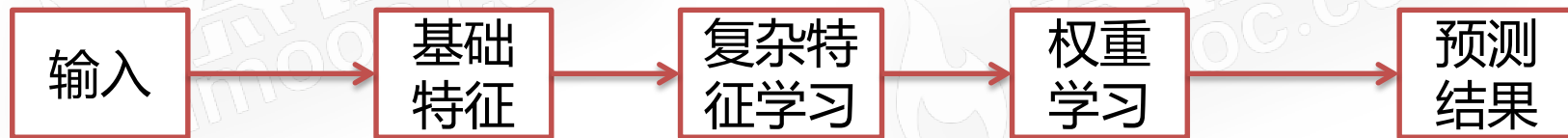
- sigmoid
- tanh
- relu

# 神经网络

- 什么是神经网络?

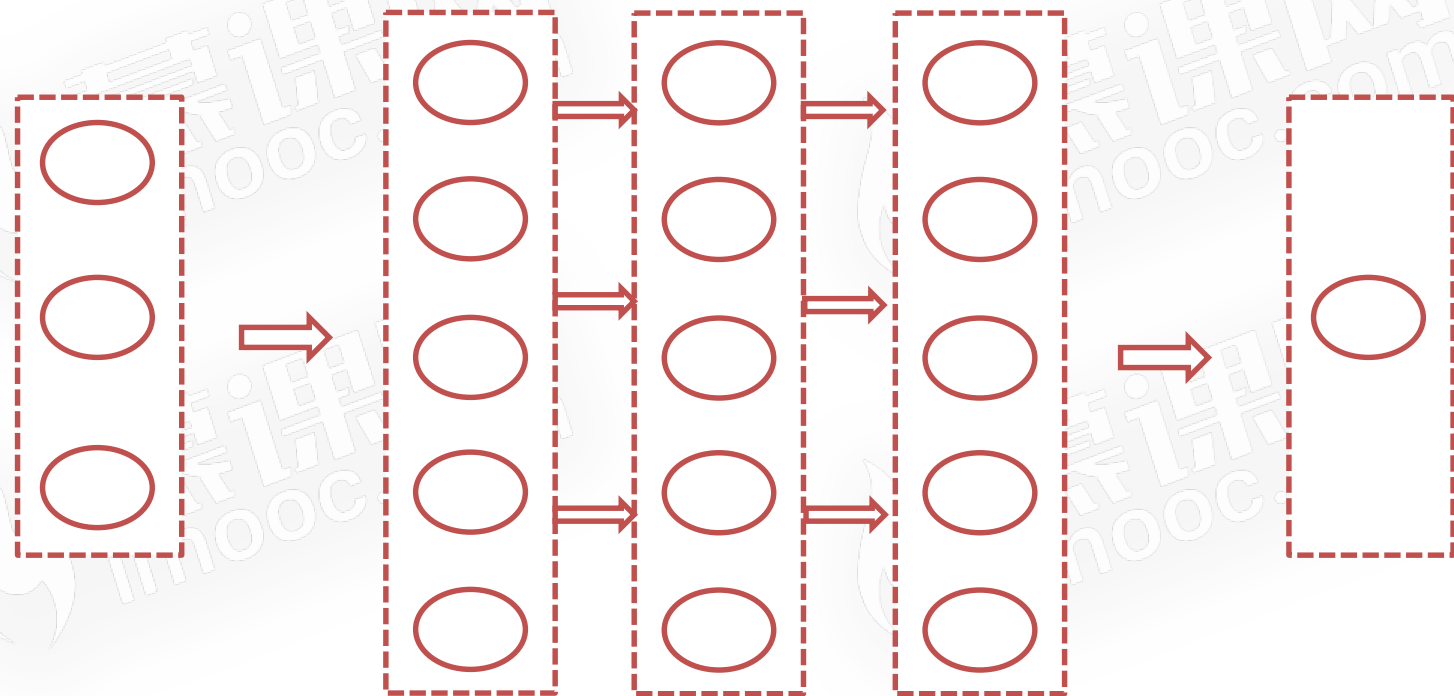


# DL DIFFS ML



# Personal Recommendation Algorithm

# DNN网络结构



输入层

隐层

输出层



# DNN模型参数

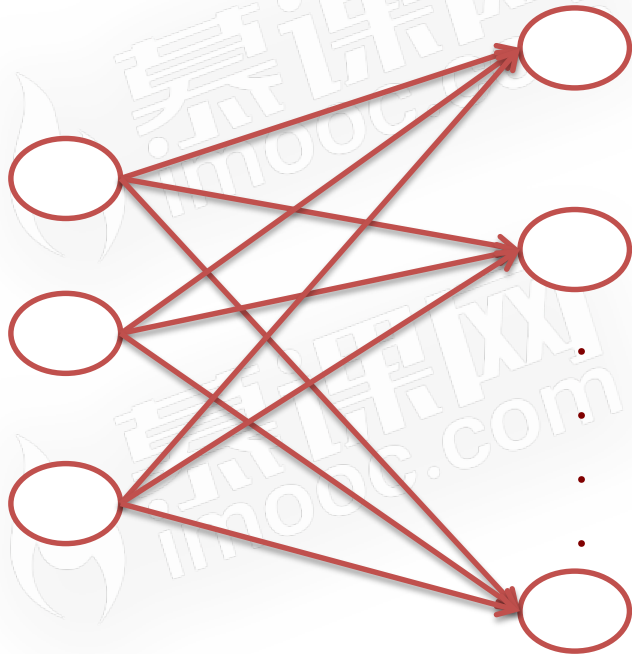
- 隐层层数，每个隐层神经元个数，激活函数
- 输入输出层向量维度
- 不同层之间神经元的连接权重 $W$ 与偏移值 $B$

# 前向传播

- 节点的输出值

$$a_j^t = f\left(\sum_k w_{jk}^t a_k^{t-1} + b_j^t\right)$$

$$z_j^t = \sum_k w_{jk}^t a_k^{t-1} + b_j^t$$



# 反向传播

- Our Target

$$\frac{\partial L}{\partial w_{jk}^t} \quad \frac{\partial L}{\partial b_j^t}$$

- What We Have

$$\frac{\partial L}{\partial a_j^T} \quad \frac{\partial L}{\partial z_j^T}$$

# 反向传播

- 推导

$$\frac{\partial L}{\partial b'_j} = \frac{\partial L}{\partial z'_j} * \frac{\partial z'_j}{\partial b'_j} = \frac{\partial L}{\partial z'_j}$$

$$\frac{\partial L}{\partial w'_{jk}} = \frac{\partial L}{\partial z'_j} * \frac{\partial z'_j}{\partial w'_{jk}} = \frac{\partial L}{\partial z'_j} * a_k^{t-1}$$

$$z'_j = \sum_k w'_{jk} a_k^{t-1} + b'_j$$

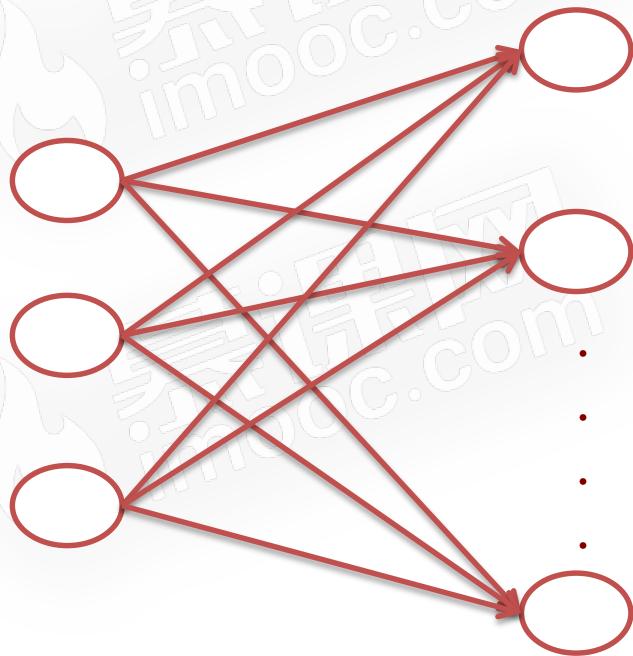
# 反向传播

- 核心

$$\frac{\partial L}{\partial z_j^{t-1}} = \sum_k \frac{\partial L}{\partial z_k^t} \frac{\partial z_k^t}{\partial z_j^{t-1}}$$

$$z_k^t = \sum_j w_{kj}^t a_j^{t-1} + b_k^t$$

$$\frac{\partial z_k^t}{\partial z_j^{t-1}} = \frac{\partial z_k^t}{\partial a_j^{t-1}} \frac{\partial a_j^{t-1}}{\partial z_j^{t-1}} = w_{kj}^t \frac{\partial a_j^{t-1}}{\partial z_j^{t-1}}$$



# 反向传播

- 对于输入 $x$ ，设置合理的输入向量
- 前向传播逐层逐个神经元求解加权和与激活值

# 反向传播

- 对于输出层求解输出层损失函数对于 $z$ 值的偏导
- 反向传播逐层求解损失函数对 $z$ 值的偏导
- 得到 $w$ 与 $b$ 的梯度

# Personal Recommendation Algorithm



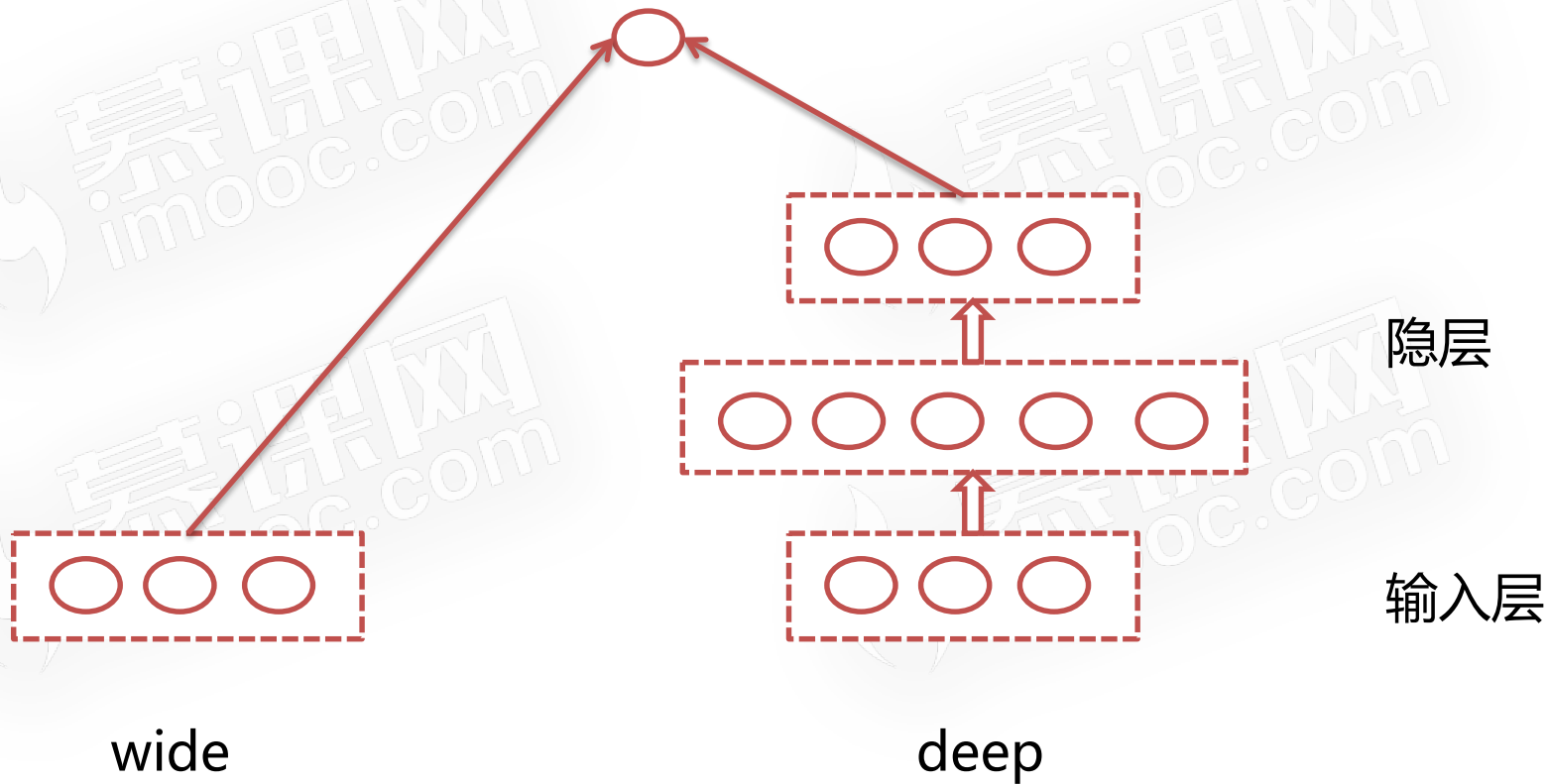
# Wide And Deep Model

- $w$  &  $d$ 的物理意义
- $w$  &  $d$ 的网络结构
- $w$  &  $d$ 的数学原理

# 物理意义

- 论文：wide & deep learning for Recommender Systems
- Generalization and Memorization

# 网络结构



# 模型输出

- 模型输出

$$a_{out}^T = h(w_{wide}, w_{deep}) = \sigma(w_{wide} [x, x_{cross}] + w_{deep} a_{out}^{T-1} + b^T)$$

# WD model的反向传播

- wide侧参数学习

$$\frac{\partial L}{\partial w_{widej}} = \frac{\partial L}{\partial a^T} \frac{\partial a^T}{\partial z^T} \frac{\partial z^T}{\partial w_{widej}} = \frac{\partial L}{\partial a^T} \sigma'(z^T) x_{widej}$$

# WD model的反向传播

- Deep侧参数学习

$$\frac{\partial L}{\partial z_j^{t-1}} = \sum_k \frac{\partial L}{\partial z_k^t} \frac{\partial z_k^t}{\partial a_j^{t-1}} \frac{\partial a_j^{t-1}}{\partial z_j^{t-1}} = \sum_k \frac{\partial L}{\partial z_k^t} w_{deepkj}^t \frac{\partial a_j^{t-1}}{\partial z_j^{t-1}}$$

$$z_k^t = \sum_j w_{deepkj}^t a_j^{t-1} + b_k^t \rightarrow t \neq T$$

$$\frac{\partial L}{\partial b_j^t} = \frac{\partial L}{\partial z_j^t} * \frac{\partial z_j^t}{\partial b_j^t} = \frac{\partial L}{\partial z_j^t}$$

$$z_k^t = \left( \sum_j w_{deepkj}^t a_j^{t-1} + b_k^t \right) + w_{wide} * X \rightarrow t = T$$

$$\frac{\partial L}{\partial w_{jk}^t} = \frac{\partial L}{\partial z_j^t} * \frac{\partial z_j^t}{\partial w_{jk}^t} = \frac{\partial L}{\partial z_j^t} * a_k^{t-1}$$

# server架构

