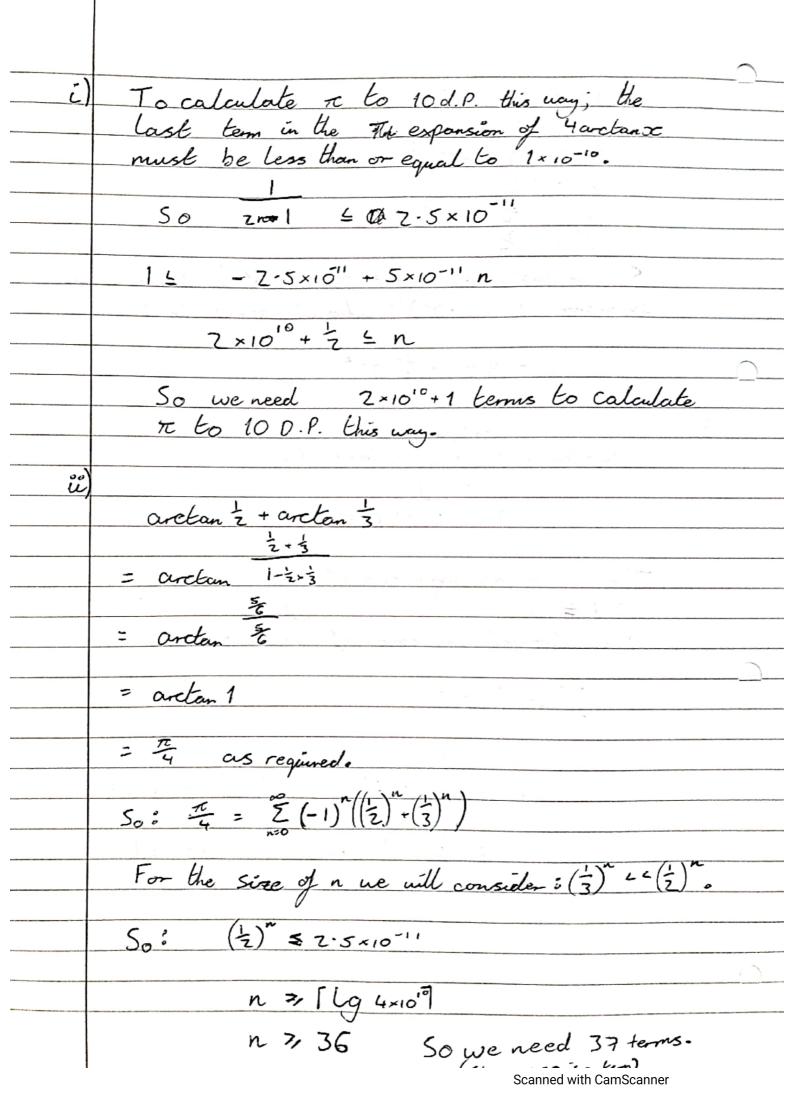
<u> </u>	M: Pour Series
	Harry Langford
	The Carry
1	
	Since about to
	Using Tay lors Theorem
	$(x_1, x_2, x_3, x_4, x_5, x_5, x_5, x_5, x_5, x_5, x_5, x_5$
	$f(x) \approx f(x) + (x-a)f''(a) + (x-a)^{-1}f''(a) + (x-a)^{-1}f''(a)$
	$f(\alpha) = \sin \frac{\pi}{6} = \frac{1}{2}$
	$f''(\alpha) = \cos \xi = \frac{\pi}{2}$
<u></u>	$f^{(2)}(\alpha) = -\sin \frac{\pi}{6} = -\frac{1}{2}$
	$f^{(2)}(\alpha) = -\sin \frac{\pi}{6} = -\frac{1}{2}$ $f^{(3)}(\alpha) = -\cos \frac{\pi}{6} = -\frac{1}{2}$
* **	So: Ell
	Sin 317 = 1 + 180 × 2 x (180) x t - (150) x 1/2 + R.
	$R_n = \frac{(2e-a)^n}{n!} p^{(n)}(\xi)$
	$f^{(n)}(\mathbf{z}) = \sin \mathbf{z}$
-	£ 1
,	$(x-a)^n$
_	:
	(72)41
	$4 = \left(\frac{\pi}{180}\right)^{4} \times 24$
	This is small - and so the approximation is precise.
2.0	Using Taylor's Theorem:
2000)	
	$f(6) = f(6) + \infty f''(6) + \frac{\infty^2}{3} f^{(2)}(6) + \dots$
-	r(0) ~ r(0) + wr (0)+ = r (0)+
,	
	f(c) = arcsin x.
_	P(0) = 0

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\beta''(x) = (1-x^2)^{-\frac{1}{2}}
                   f"(0) = 1
                  f'''(\infty) = \infty(1-\infty^2)^{-\frac{3}{2}}
                  f^{(a)}(0) = 0
                   f'''(x) = (1-x^2)^{-\frac{1}{2}} + 3x^2(1-x^2)^{-\frac{1}{2}}
                   f^{(4)}(\infty) = 9x(1-x^2)^{-\frac{5}{2}} + 15x^3(1-x^2)^{-\frac{3}{2}}
                   f(4)(0) = 0
                   f^{(s)}(x) = 9(1-x^2)^{-\frac{1}{2}} + 9C_{1}^{2}(1-x^2)^{-\frac{3}{2}} + 105x^{\frac{3}{2}}(1-x^2)^{-\frac{3}{2}}
                  f(5)(0) = 9
         So the first three nonzero terms are f'"(0); f''(0); f''(0)
        \therefore \text{ are Sin} \propto \simeq \propto + \frac{x^2}{6} + \frac{9x^5}{120}
b) Hx)=tan x
   f(0) = 0
   f"(5c) = sec*5c
    f(1)(0) = 1
    f (2) ( sc) = 25ec x tom x
    P(2)(0) = 0
    f^{(3)}(\infty) = 2 \sec^4 \infty + 4 \sec^2 \infty \tan^2 \infty
    f^{(3)}(0) = 2
f^{(4)}(50) = 16 \sec^2 x \tan x = 8 \sec^2 x \tan^3 x
       So: \tan \propto \approx \propto + \frac{2}{3} + \frac{2 \times 5}{15}
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	$f(\infty) = (1+\infty)^{-\frac{1}{2}}$
	P(0) = 1
	$f''(x) = -\frac{1}{2}(1+x)^{-\frac{1}{2}}$
	$f'''(0) = -\frac{1}{2}$
	$f^{(2)}(x) = \frac{3}{4}(1+x)^{-\frac{1}{2}}$
	f(2)(0) = 34
	So the first three non-zero terms of the Taylor Screen expansion of $(1+x)^{-\frac{1}{2}}$ about $x=0$ is:
	Je Comment of Comment
	1 - \frac{1}{2}x + \frac{3}{8}x^2
	2 2 3 3 1 1 2 2 3 3 1 4 1 3 1 2 2 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
3,	(d
	$\arctan x = \int \frac{d}{dx} (\arctan x) dx$
	$= \int \frac{1}{1+\infty^2} dx$
	The binomial expansion of $1+x^2$ is valid if $1x1 \le 1$.
	1x141.
	The binomial expansion of 1+x2 is
	2
	$\sum_{n \geq 0} (-1)^n \chi^{2n}$
	$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty$
	i. arctanx = $\int_{-\infty}^{\infty} (-1)^n x^{2n} dx for x \le 1$ $= \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n-1}}{2n+1} for x \le 1$
	$=\frac{x^{2n+1}}{2}$
	= 2 (-1) Zn+1 for 1x1 &1
	A
	As required,



iii)	4 arctan = - arctan = 39
	\$ 1 5
	= 2 arctan 1- 15 - arctan 239
	= Zarctan 12 - arctan 239
	$= \frac{5}{12} + \frac{5}{12}$ $= \frac{25}{174}$
	= arctan 1 - 144
	= arctan 119 - arctan 239
	= arctan 119 - arctan 239
	$= \frac{120}{119} - \frac{1}{239}$ $= \arctan \frac{1 + \frac{120}{119} + \frac{1}{239}}{1 + \frac{120}{119} + \frac{1}{239}}$
	(120×2)9-119
	= arctan (119×239+120)
	(120×239-119)
	= arctan 120×239-119/
	= arctan 1
	- 1.
	For the nue will consider: (239) 44 (5).
	100 10 000 0000 0000 00000 000000000000
	So to calculate To to 10 d. P.
	16 x(5) = 1x10-10
	1.6 × 10 " = 3"
4	[logs 1.6x10"] & n
	V
The second secon	~ n7,17
	So we need 18 terms (since n=0 is a tem)

_
Δ.

3.
$$(x^{3}+x^{2}+1)^{\frac{1}{3}}-(x^{2}+x)^{\frac{1}{2}}$$

$$= x(1+\frac{1}{3}(\frac{1}{x}+\frac{1}{x})-\frac{1}{9}(\frac{1}{x}+\frac{1}{x})^{\frac{1}{4}}-1-\frac{1}{2}(\frac{1}{x})+\frac{1}{6}(\frac{1}{x})^{\frac{1}{4}}$$

$$= x(1+\frac{1}{3}(\frac{1}{x}+\frac{1}{x})-\frac{1}{9}(\frac{1}{x}+\frac{1}{x})^{\frac{1}{4}}+0(\frac{1}{x})^{\frac{1}{4}}$$

$$= x((\frac{1}{3}-\frac{1}{2})(\frac{1}{x})-(\frac{1}{4}+\frac{1}{8})(\frac{1}{x})+0(\frac{1}{x}))$$

$$= x(-\frac{1}{6x}+\frac{1}{72x}+0(\frac{1}{x}))$$

$$= x(-\frac{1}{6x}+\frac{1}{72x}+\frac{1}{$$

$$= L\left(-6l^{2} \cdot O(l^{2})\right)$$

$$= -6l + O(l^{2})$$

$$=$$

Since x_o is close to x_j in general $f'(x_o) \approx f''(x)$.

So: $\frac{f(x_o)}{x} = \frac{f(x_o)}{x}$ So, in general $x_0 - \frac{f(x_0)}{f'''(x_0)}$ is a better approximation to x than to when f(x) = 0 and x_0 is an approximate

Solution.

as required. ___ y= lnx lnx=Ex 0 = 62e - Cn2c So f(x) = Ex - lnx f'(x) = E - x

	$f(\infty)$	$\widehat{}$
	>c- f'(x)	
	the state of the s	
	$= \frac{\varepsilon x - \ln x}{\varepsilon - \pm}$	
	$= x - \epsilon - \dot{x}$	
	Ex2-xlnx	
	$= \infty - \varepsilon \times -1$	
	$Ex-1-Ex^2+xlnx$	
	$=$ $\varepsilon x - 1$	
	$Ex-1-Ex^2+xhx$	
	So $x_{mi} = \varepsilon x - 1$	
	Let xo = 1	
	E-1-E	
-	20 ∞,= E-1	
	= E-I	$\underline{\hspace{1cm}}$
	= 1-6	
	$\frac{1}{C} = \frac{1}{1 + \frac{1}{2}} = \frac{1}{1 + \frac{1}{$	
	E × 1-E -1 - (1-E)2 + 1-E ln 1-E	
	$x_2 = \varepsilon$	
	1-E -1	
	<i>E</i>	
	$x_2 = \frac{\varepsilon}{-1 + \varepsilon - 1 - \varepsilon} + \ln 1 - \varepsilon$	
	E-1+6	

2E-1 - 1-E + Li-E E 1-E 1 + (E-1)(2E-1)+ ZE-1 = 1 + (E-1)(ZE-1) + (E-1)(ZE-1) = 1 - $2(1+E+E^2+O(E^3))+2(1+2E+4E^2+O(E^3))$ = 1 - 2 m-2E-ZE2+O(E)+Z+4E+8E2 = 1+2E+6E2+0(E3)