- 1. Show (using appropriate examples and schematic diagrams) how ROMs, PALs PLAs and FPGAs can be used to implement combinatorial logical functions. What are their relative advantages and disadvantages?
  - (a) The literals in the combinatorical logic are used to address ROM. This reads the value which is writen there. So you can program the ROM with combinatorical and it will return it when addressed.

Using ROM to implement combinatorical logic ensures that the logical circuit is not changed – and it does also not have to be hardwired.

So the same circuit can be reused without reprogramming even after power loss.

Unfortunately, using ROM for combinatorical logic means accessing memory – which is slow.

And ROM wastes a lot of memory if the expression is sparse. Since ROM cannot be edited, the logical expression is also fixed – which is not ideal.

IE to implement the logical expression  $f = ABC + \bar{A}\bar{C} + \bar{B}\bar{C}$  the ROM would store:

Address	Data
000	1
001	0
010	1
011	0
100	1
101	0
110	0
111	1

Can implement multiple Sunctions in ROM using more bits of data

1 / 10

So using the literals to address the memory and returning the value would implement the combinatorical logic. ie a=0, b=0, c=0 would go to memory address 000 and read f=1.

(b) PALs can be programmed in the AND plane – and then the terms generated in the and plane are OR'd together in an immutable OR plane. For every output which the term is included in, it must be generated again. This means that PALs are innefficient if they have to generate many functions containing the same terms. However, since only the AND plane is programmable, they are fast, simple – and the combinatorical expressions are not fixed.

In the diagram below:

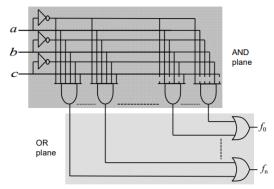
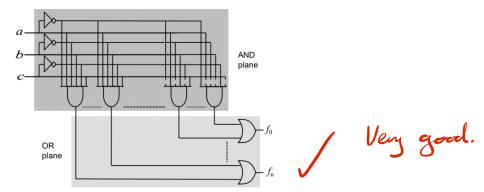


Image from page 10 of the Digital Electronics Lecture Notes

The wires in the AND plane can be turned "off". This means that the expression represented by each AND gate can be changed and so different combinatorical expressions can be represented. However, the OR plane cannot be changed.

IE to represent  $f_0 = ABC + \bar{A}\bar{C}$ , we would turn off wires so that the circuit looked like this.

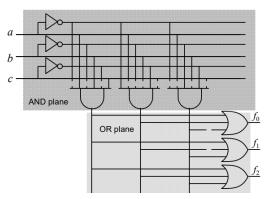


Modified version of an image on page 10 of the Digital Electronics Lecture Notes

(c) PLAs can be programmed in both the AND and OR planes. This means that they are programmable, and so the logical expression they represent can be programmed. They can also re-use terms in other expressions This makes them very efficient. However, since both the AND and OR planes are programmable, PLA's are very complicated and expensive.

To represent a logical expression using a PLA, you turn off wires in the AND plane so that the terms you want to OR together are generated. You then turn off the appropriate wires in the OR plane so that the terms all go into the same function.

IE if you wanted to generate the logical expression  $f_0 = ABC + \bar{A}\bar{C}$  and also wanted to generate the logical expression  $f_1 = ABC + \bar{B}\bar{C}$  you would use the PLA as shown below. This would allow you to reuse the ABC term without having to re-generate it.



Modified version of an image on page 9 of the Digital Electronics Lecture Notes

Excellent.

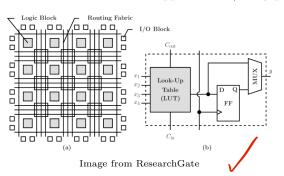
2 / 10

(d) FPGAs are arrays of "Configurable Logic Blocks" (CBS's). Each CLB contains a lookup table (made of SRAM), the ouputs of which are processed with logical expressions and then passed through multiplexers and SR latches (so that you can select which expression to pass on – and to make the CLB's synchronous). FPGA's contain lots (often hundreds) of CLB's. This means they are essentially large arrays of lookup tables and complex logic. The expressions in CLB's are writen in SRAM – this means that when power is lost, the expression vanishes. So it must be re-written every time the power is turned on. Often the data for this is stored in EEPROM, however sometimes it can just be written from the computer itself.

FPGA's can represent incredibly complicated expressions, they can also be reprogrammed. FPGA's also often have common logical expressions pre-programmed into them. For small/mid sized projects, FPGA's are often cheaper than alternatives since they are off-the-shelf and do not have to be custom built. However, FPGA's are expensive and so for large projects it's often cheaper to make the logical circuit specifically. FPGA's do use non-volatile memory and so have to be re-written after the power is turned off. This means that the logical expression must be stored separately. FPGA's can also be memory innefficient if the expression is very sparse. FPGA's are designed for incredibly complicated logical expressions and so are unsuitable for most applications (overly-powerful).

. Yes, custom
blocks for certain
tasks & may also
have custom silian
support.

Con... not really.
They're good for low-volume pouts.



But also works Ser sequential logic To

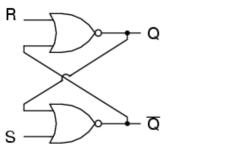
To express a combinatorical logical function in a FPGA, you must split it up, then load parts of the expression into each CLB. Then to evaluate the function with a given set of inputs, subsets of the inputs are passed into the CLB's, they then lookup the result in a lookup table and return them. Which outputs are output is determined by multiplexers. This is usually dependent on other inputs which that specific CLB was not passed.

2. (a) How might one use an SR latch to debounce a SPDT switch? Draw timing diagrams to illustrate your answer.

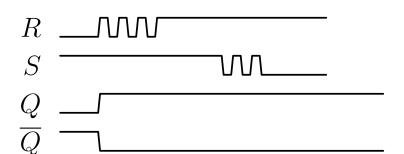
When turned on, a SPDT switch will change which output is set to 1. So at any one time, one output from an SPDT switch will always be 1 and another will always be 0. However, when pressed, the switch may "flicker". To mitigate this, we can attach the two outputs to a RS latch (as the input variables R and S, and then take Q and  $\overline{Q}$  as the new outputs.

This means that when the input flickers, and there are states where both outputs are off, Q and  $\overline{Q}$  will hold their previous values, hence debouncing the switch.

Remember pull-down resistors.

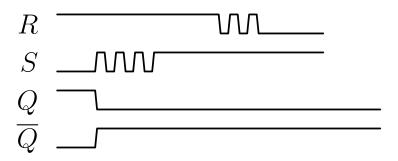


Take the timing diagram where R and S are the inputs from the SPDT switch. Changing R from 1 to 0:



Good.

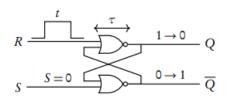
Changing S from 1 to 0:





As shown, the outputs from Q and  $\overline{Q}$  are equivalent but stable versions to the ouputs from the switch. And so the RS Latch has been used to debounce the SPDT switch.

(b) Suppose a NOR gate has a propagation delay equal to  $\tau$ . Further suppose that a particular SR latch is in state Q=1, and a clean pulse of length t appears on the R input in order to reset the latch to state Q=0. What is the minimum possible t, expressed in terms of  $\tau$ , in order for the intended state change to be effected? Support your answer with timing diagrams.

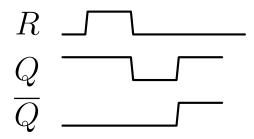


The shortest pulse which will effect the change will have to be long enough to change both Q and  $\overline{Q}$  If a time t=0 R pulses to 1, then at time  $\tau$  the signal change will have propogated through the NOR gate and Q will change to 0. At this point,  $\overline{Q}$  will still be 0 and so the circuit is **not** in a valid state. The signal must propogate throuth the bottom NOR gate to change  $\overline{Q}$  to 1. This takes a further  $\tau$ . So at  $t=2\tau$  the circuit will have completed the state change. So the total time is  $2\tau$ .

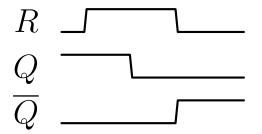
If the pulse is turned off before this time; Q will change back to 1.

So the minimum t which will cause the intended state change to be effected is  $2\tau$ .

If the pulse lasts less than  $2\tau$  (in this case  $\tau$ ) Then the circuit will enter an illegal state. Really? If it's exactly 3 in length (with ideal exacts) 2.

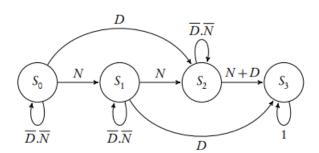


If the pulse lasts  $2\tau$  or more then the state change will be effected properly.





3. A machine has the state diagram shown below, where N and D are the two inputs and N=D=1 cannot occur. The state assignment is  $S_0=[00]$ ,  $S_1=[01]$ ,  $S_2=[10]$  and  $S_3=[11]$ , where the machine starts in state  $S_0$  and finishes in state  $S_3$ . Note that the state  $S_0=[00]$  where  $S_0=[$ 



(a) Write down the state transition table for this machine

Court up in natural binary.

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		Current State	D	Ν	Next State
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$S_0$	1	0	$S_2$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$S_0$	0	1	$S_1$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$S_0$	0	0	$S_0$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$S_1$	1	0	$S_3$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$S_1$	0	1	$S_2$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$S_1$	0	0.	$S_1 \times \kappa$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$S_2$	<u> </u>	1	$S_3$
$egin{array}{c ccccccccccccccccccccccccccccccccccc$			1	0	$S_3$
$egin{array}{ c c c c c c c c c c c c c c c c c c c$	CW	$S_2$	0	1	$S_3$
$egin{array}{c ccccccccccccccccccccccccccccccccccc$		$S_2^{-}$	0	0	$S_2$
$egin{array}{ c c c c c c c c c c c c c c c c c c c$		$S_3$	<b>-</b> 3/1	1	$S_3$
$egin{array}{ c c c c c c c c c c c c c c c c c c c$		$S_3$	1	0	$S_3$
$oxed{S_3} oxed{0} oxed{0} oxed{S_3}$		$S_3$	0	1	$S_3$
		$S_3$	0	0	$S_3$

Include du 't Cares in state tuble.

(b) Assuming the use of J-K flip-flops for the state registers, write down the modified state transition table and determine the minimised Boolean expressions for the next state functions.

With  $S_0$  as 00,  $S_1$  as 01,  $S_2$  as 10 and  $S_3$  as 11:

$Q_1Q_0$	D	N	$Q_1Q_0$
00	1	0	10
00	0	1	01
00	0	0	00
01	1	0	11
01	0	1	10
01	0	0	01
10	1	1	11
10	1	0	11
10	0	1	11
10	0	0	10
11	1	1	11
11	1	0	11
11	0	1	11
11	0	0	11

J, K, J. K.

 $Q_1$ :

			$Q_1Q_0$			
		00	01	11	10	
DN	00	0	0	1	1	
	01	0	1	1	1	
DN	11	x	x	*	*	
	10	1	1	1	1	

So 
$$Q_1 = Q_1 + N + DQ_0$$
.

 $Q_0$ :

		$Q_iQ_j$			
		00	01	11	10
DM	00	0	1	1	0
	01	1	0	1	1
DN	11	x	x	*	×
	10	0	1	1	1

Not what the question asks for - need S& k inputs.

So 
$$Q_0 = Q_1 \overline{N} + Q_1 N + \overline{Q}_0 N + \overline{Q}_1 D$$

4. Eliminate the redundant states from the following state table using the Row Matching approach.

Row matching allows us to merge two rows into one if the next states and outputs are identical.

Current State	Next State		Outp	$\operatorname{ut}(Z)$
	X = 0	X = 1	X = 0	X = 1
A	A	В	0	0
В	$^{\mathrm{C}}$	D	0	0
$\mathbf{C}$	A	D	0	0
D	${ m E}$	$\mathbf{F}$	0	1
${ m E}$	A	$\mathbf{F}$	0	1
$\mathbf{F}$	G	$\mathbf{F}$	0	1
G	A	$\mathbf{F}$	0	1

By inspection: E and G are identical. Merging them yields the table below:

Current State	Next	State	Outp	$\operatorname{ut}(Z)$
	X = 0	X = 1	X = 0	X = 1
A	A	В	0	0
В	C	D	0	0
$\mathbf{C}$	A	D	0	0
D	${ m E}$	$\mathbf{F}$	0	1
$\mathbf{E}$	A	$\mathbf{F}$	0	1
$\mathbf{F}$	E	$\mathbf{F}$	0	1

Now D and F are identical. Merging them gives the table below:

Current State	Next State		Outp	$\operatorname{ut}(Z)$
	X = 0	X = 1	X = 0	X = 1
A	A	В	0	0
В	С	D	0	0
$\mathbf{C}$	A	D	0	0
D	E	D	0	1
$\mathbf{E}$	A	D	0	1

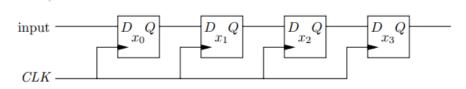
No states in this table are identical. So the table cannot be reduced any further using Row Matching.

## 5. 1 2002 Paper 2 Question 2

(a) A 4-bit shift register constructed from edge-triggered D-type flip flops is shown below. If, on successive rising edges of the clock signal CLK, the input takes on the values 1, 0, 1, 0, 1, 1, 1, 0, what are the contents of the shift register after each edge of the clock? You may assume that the register contains all zeroes initially.



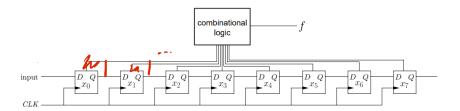
https://www.cl.cam.ac.uk/ teaching/exams/pastpapers/ y2002p2q2.pdf



input	$x_0$	$x_1$	$x_2$	$x_3$	
1	1	0	0	0	
0	0	1	0	0	
1	1	0	1	0	
0	0	1	0	1	
1	1	0	1	0	
1	1	1	0	1	
1	1	1	1	0	
0	0	1	1	1	1

(b) Using a (possibly larger) shift register, show how one may detect a particular pattern in the input shown. As an example, use the 8-bit pattern 0xF0. High order bits precede low-order bits in the input stream

You would take the values  $x_i$  as inputs to a block of combinational logic containing the pattern you wished to check for. f would then return 1 if the inputs matched that pattern.



For the example 0xF0, the combinational logic expression would be  $f=\bar{x}_0\bar{x}_1\bar{x}_2\bar{x}_3\bar{x}_4\bar{x}_5\bar{x}_6\bar{x}_7$ .

(c) The input stream is framed by a one byte frame pattern (0xF0) every 256 bytes. However, the frame pattern may also appear at an arbitrary position in the input stream.

It is required to design a framing circuit which generates two outputs: framelock, which is asserted when the circuit "believes" it has determined where the frame boundaries are, and frame pointer, which is asserted on the clock edge immediately after the frame marker is detected. The circuit "believes" itself to be locked to the frame structure when two successive frame patterns have been found 256 bytes (i.e. 2048 bits) apart. The circuit should not respond to unaligned frame patterns while it believes itself to be in lock or if, once in lock, it has missed fewer than two expected frame patterns.

Draw a state diagram for the finite state control of the circuit. You may assume the existence of an 11-bit resettable counter. You should consider the process of assuming lock, maintaining lock and the accommodation of a single missed framing pattern. State explicitly any additional assumptions you make.

I'm not sure I fully understood this question, however have written a full explanation of how to implement a system which detects a first frame marker and then waits to match with a second frame marker 2048 bits after the first. If it doesn't find it, it will then go back to the waiting state. If it receives this it will set a RS latch indicating "framelock" to 1, and send a single pulse (the "frame pointer") then move to another state which outputs a continuous signal indicaign "framelock".

You'd implement an 8-bit shift register.

There would then be a block of combinational logic which would take the values in the shift register, the "framelock" bit as an input. It would display positive only when the framelock was, the values in the shift register matched the pattern.

If the combinational logic is 1 and the counter is not on, then the clock will start counting. If the combinational logic is 1 and the clock is 2048, then a RS latch which outputs "framelock" will be set to 1, and a single pulse indicating the "frame pointer" will be set to 1. The combinational logic being positive would set a RS latch to 1 and make the counter start counting. If the RS latch was already on, however it would not do this.

Sure. We can develop this in the SU.

The following is a state diagram of this:

X means the pattern is matched

Y means the counter is 2048 (2047)

 $S_1$  is the waiting state – where the circuit is waiting for the first frame marker.

 $S_2$  is the counting state – where the circuit is counting 2048 bits and waiting for the second marker.

 $S_3$  is when the "frame pointer" and "framelock" are both 1.

 $S_4$  is where the circuit is locked – "framelock" is 1..

Frank pointer should just be I for I clock period.

denote Machine

If this is

a Morre Machine

Sy

Sy

Sy

Sy

A lot of

gend ideas here

Sy

We'll discuss.

(d) Outline the complexity in gates and flip flops for an implementation of the framing circuit.

You would need circuitry for the combinational logic, (a 8 input and gate or equivalent in 2-input and gates), two RS latches to hold the current state of the circuit. Other small pieces of logic to transition between states.

6. The input to the first stage of a five-stage shift register is obtained from the exclusive-OR function of the outputs of the 3rd and 5th stages. Consider at the start that all 5 stages have a 1 output that shifts to the right on the application of each clock pulse. What is the output sequence expressed as a decimal number, taking the right (5th) stage as the least significant bit? After how many clock pulses does it repeat? What happens if all 5 stages have 0 set on them at the start?

In order to achieve the behaviour where you cycle through every possible number (except 0), is it important that you connect together the outputs of the  $3^{rd}$  and  $5^{th}$  stages, specifically? Would this work for any length of shift register (not just those with 5 stages)?

The output sequence is 31.

It cycles through all possible integers (except 0).

It is 31 clock pulses before the sequence repeats.

Maybe talk about state eucoding.

If all 5 stages have 0 set on them at the start then the sequence remains at 0.

It is not important to connect together the outputs from of the  $3^{rd}$  and  $5^{th}$  stages specifically. For example, cycling also works with the  $2^{nd}$  and  $5^{th}$  stage. It is however, essential that one of the bits is the **last** bit. But the other bit being the  $3^{rd}$  bit in this case is coincidental.

This does not work for any length of shift register. Take for example a shift register of length 6. The  $3^{rd}$  and  $5^{th}$  bits cause it to cycle infinitely, never returning to 111111. In order for a shift register of length 6 to return to 111111, it would have to be in a state 111110. However, when it is in this state; the output from the XOR of the  $3^{rd}$  and  $5^{th}$  bits is 0. So a shift register of length 6 will not return to 111111 by XOR-ing together it's 3rd and 5th bits.

For: Mr Matthew Ireland

related to factorisation
of polynomials - if the
polynomial can't be
Sactorised, then output
will loop through all
A.