

# **Non-idealities in Motion Control**

**Quantization errors in encoders**

**Joint friction**

**Back-lash**

**Dead-band**

**Gearbox**

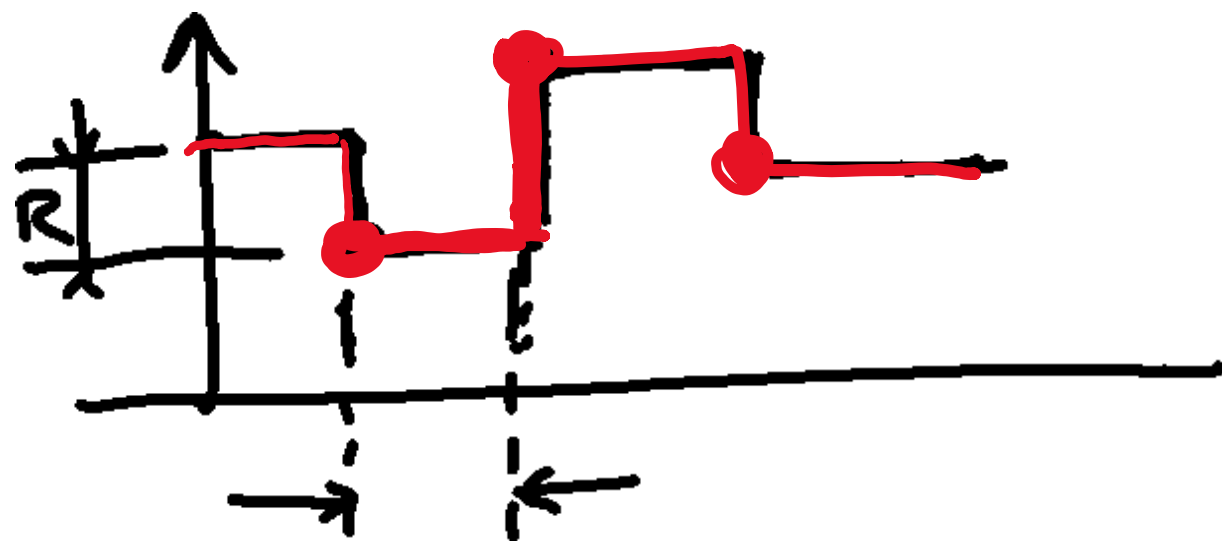
# QUANTIZATION ERRORS IN ENCODERS.



12 bit encoder

$$\theta = \frac{2\pi}{2^{12}} = \frac{2\pi}{4096} = 0.0015 \text{ rad}$$

0.09 deg  
RESOLUTION



$$T_s = \frac{1}{f_s}$$

Sampling frequency

↓ When computing velocity with finite differences, there is  
**QUANTIZATION NOISE**

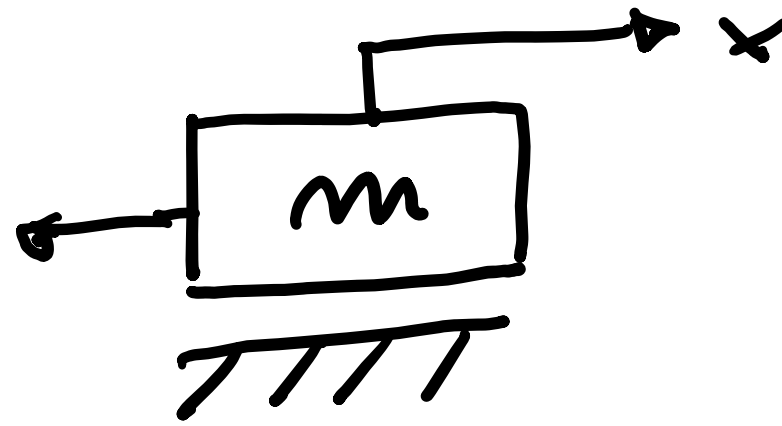
↓ minimum speed that can be measured

1 change in 1 sampling interval  $T_s = 0.001 \text{ s}$

$$\frac{0.09}{0.001} = 90 \text{ deg/s} !$$

# JOINT FRICTION

- bearings
- sliding parts



Frictional force is always opposing motion

$$F_f = F_c \operatorname{sign}(\dot{x}) + B \dot{x} + F_s \quad (\text{if } \dot{x} = 0)$$

Coulomb  
friction

viscous  
friction

stiction  
(static friction)

Coulomb law:

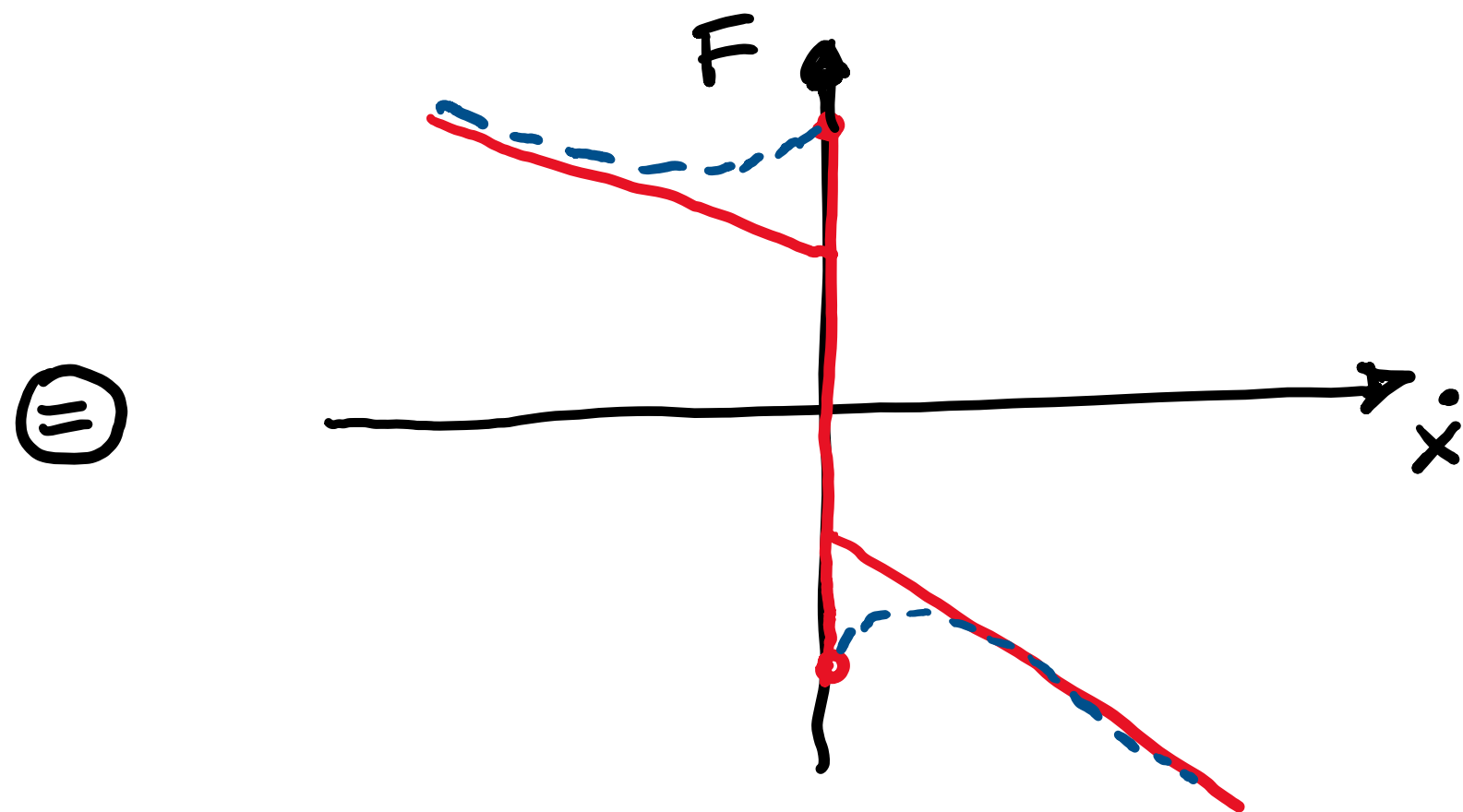
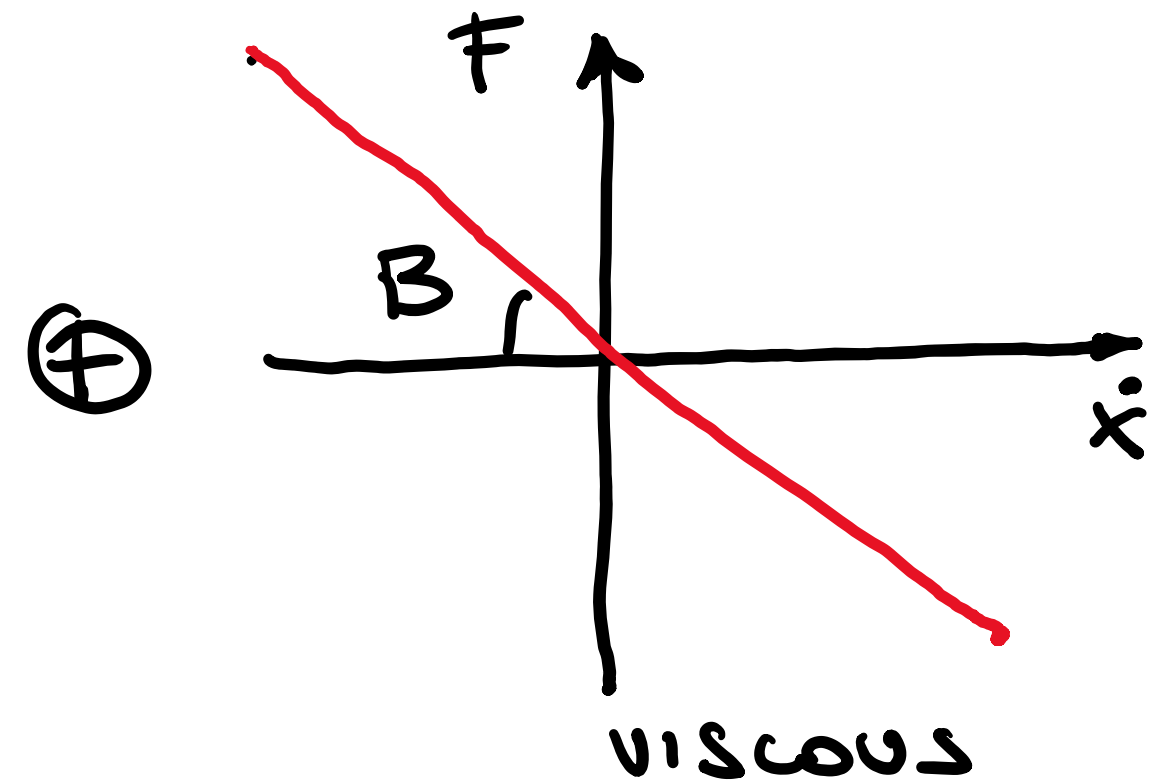
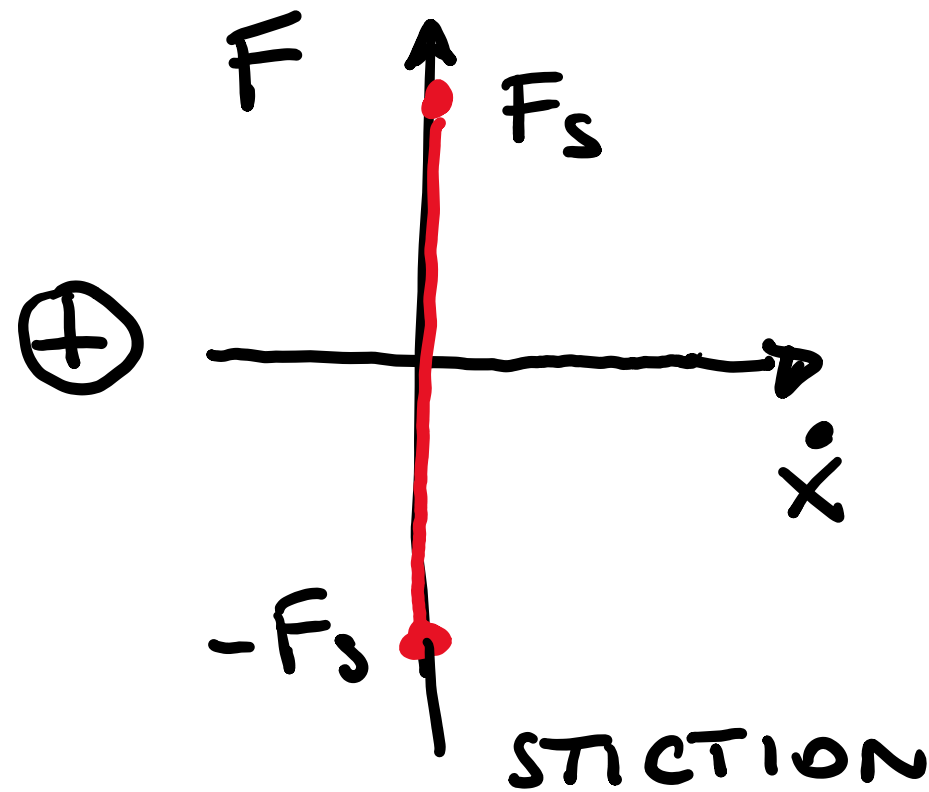
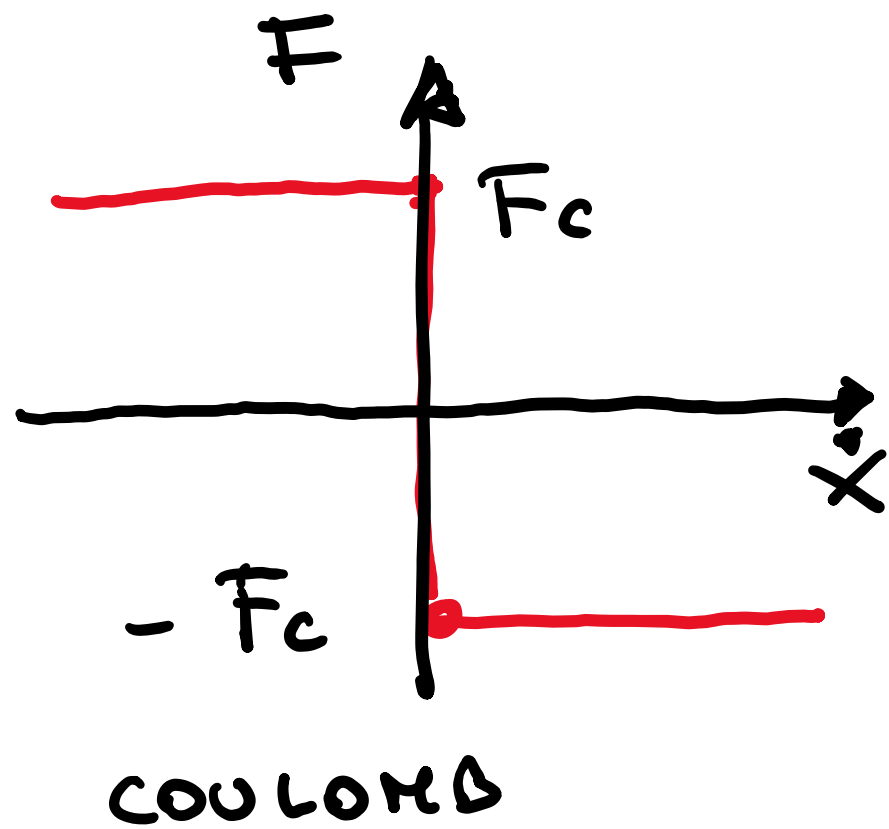
friction force Tangent to contact is related  
To normal force Through friction coeff.  $\mu$

$$F_c = F_t = \mu F_n \rightarrow \text{normal force}$$

↳ depends on 2 materials in contact

↳ independent from speed of sliding

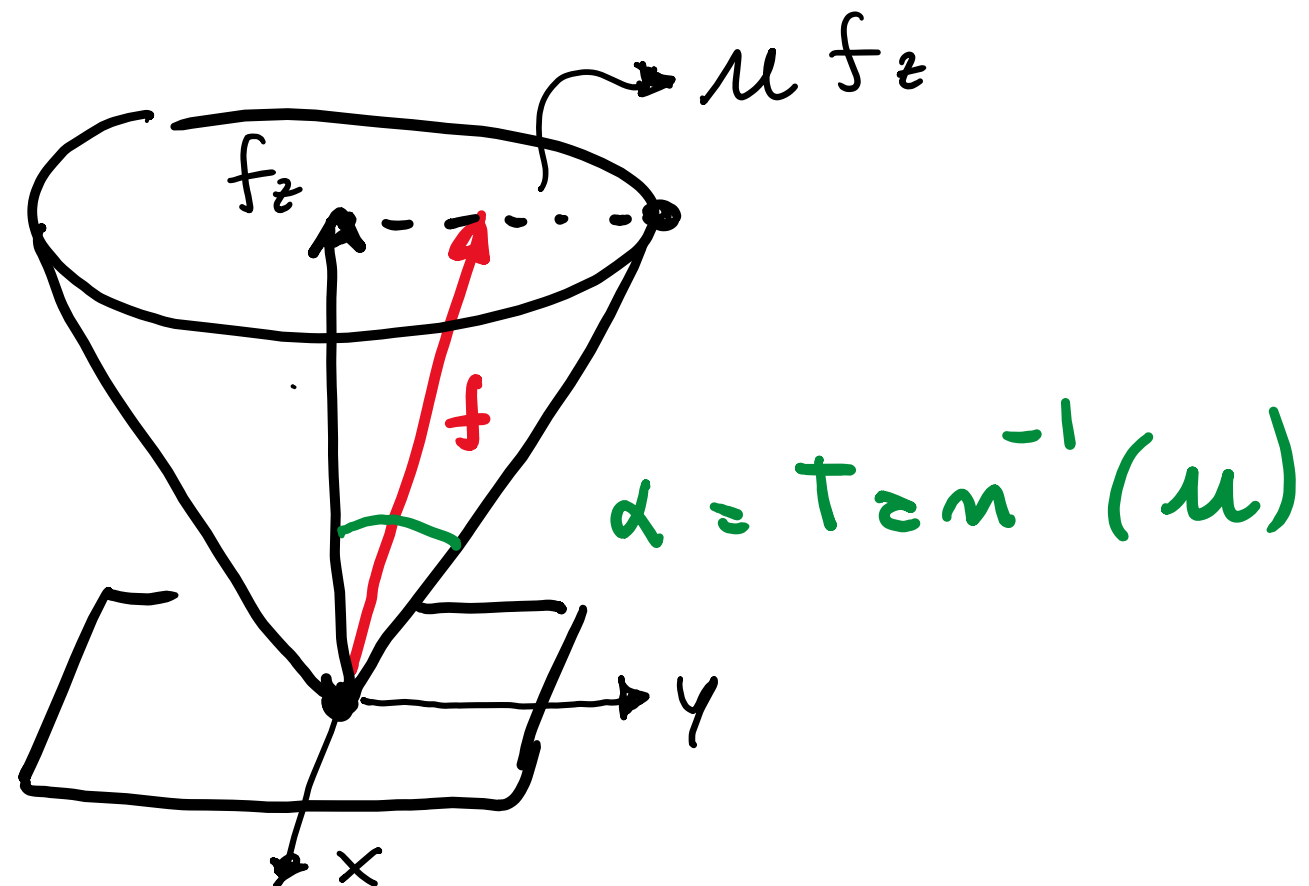
**STiction** : called break away friction  
is like Coulomb friction at 0 speed and  
is slightly higher



**Stribeck effect**  
positive slope,  
destabilizing  
effect / stick-slip

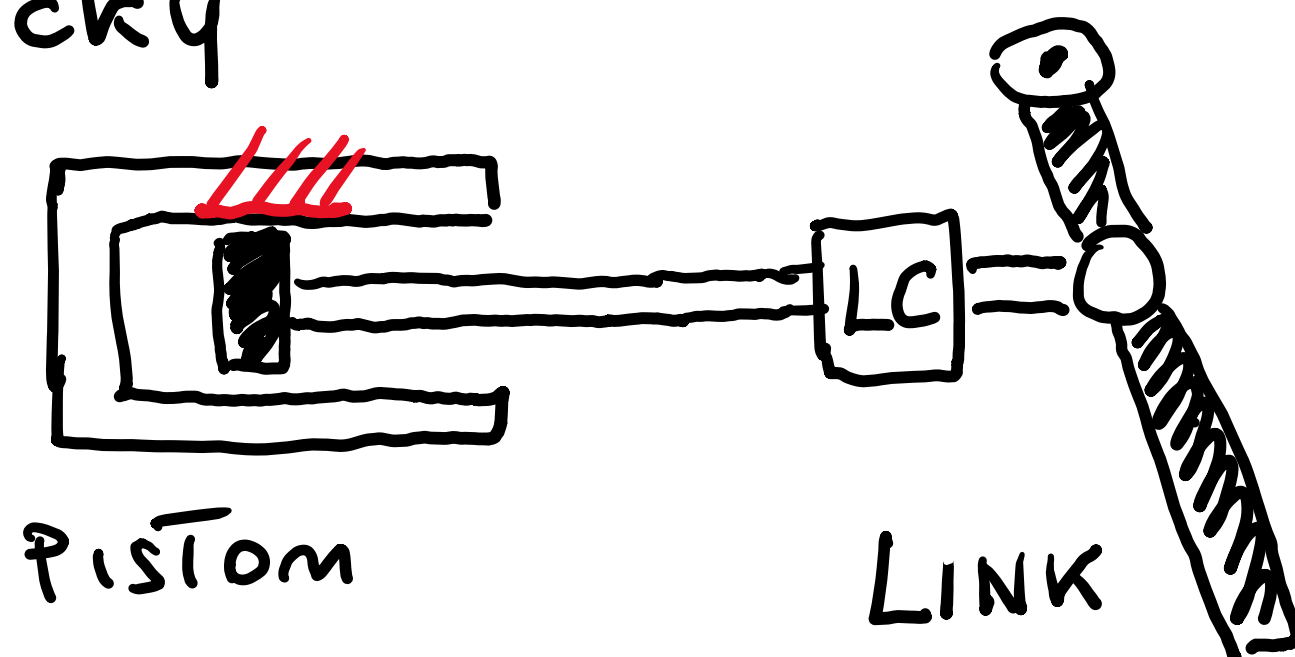
- in this course we neglect stiction
- coulomb law can be interpreted as

## FRICTION CONE



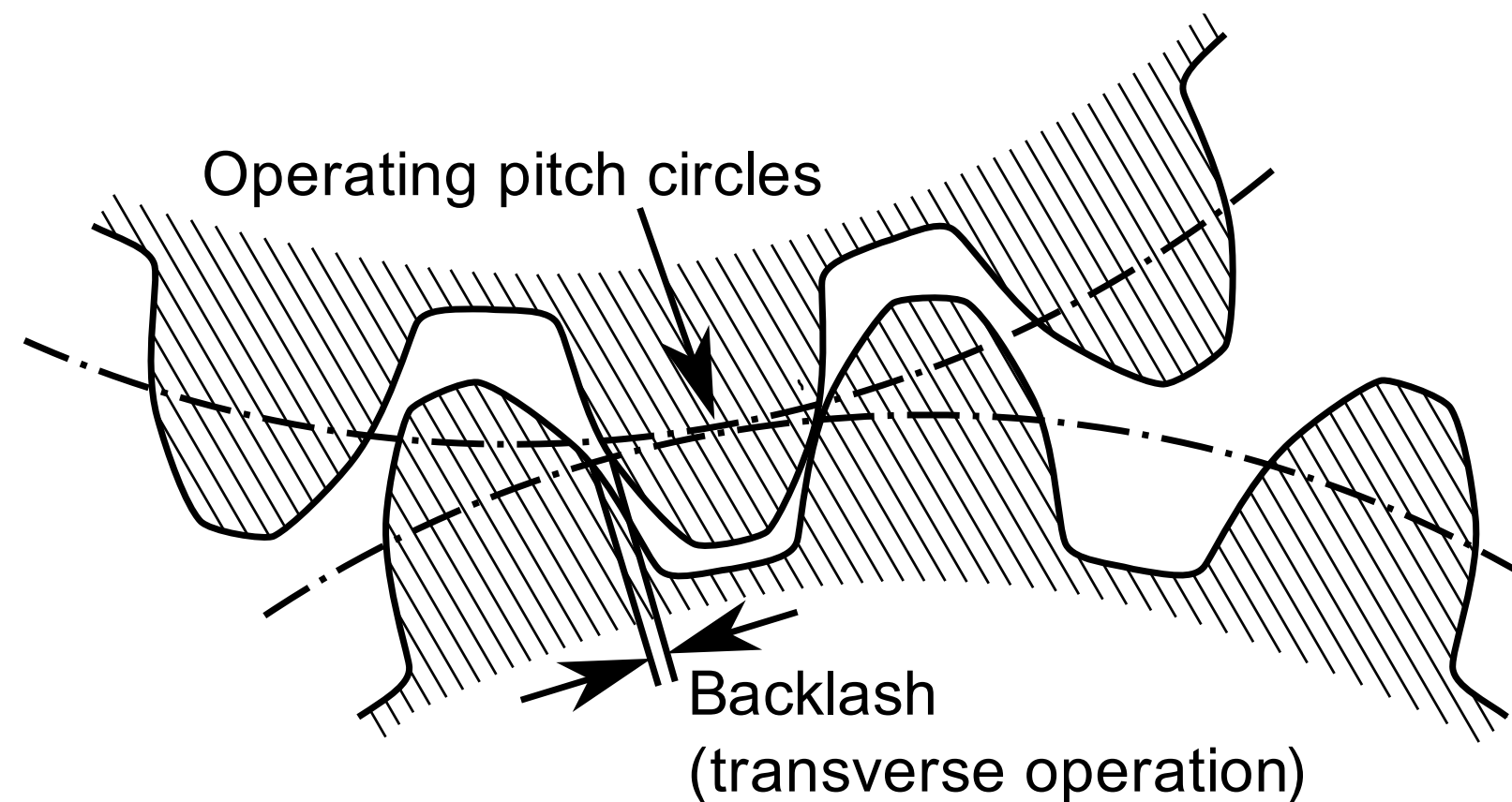
during slippage  
 $f$  is lying on the  
 cone boundary

- ⊖ identify and compensate friction can be Tricky



is better to locate  
 the load cell link  
 side

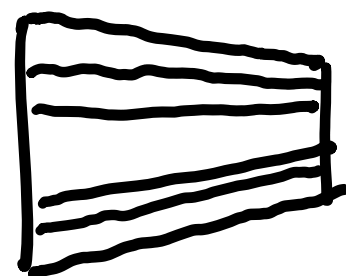
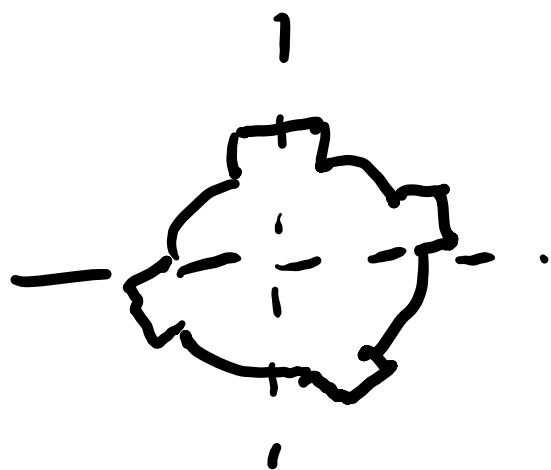
# BACK LASH



clearance or lost of motion in a mechanism due to gaps between parts (eg teeth of gear wheel)

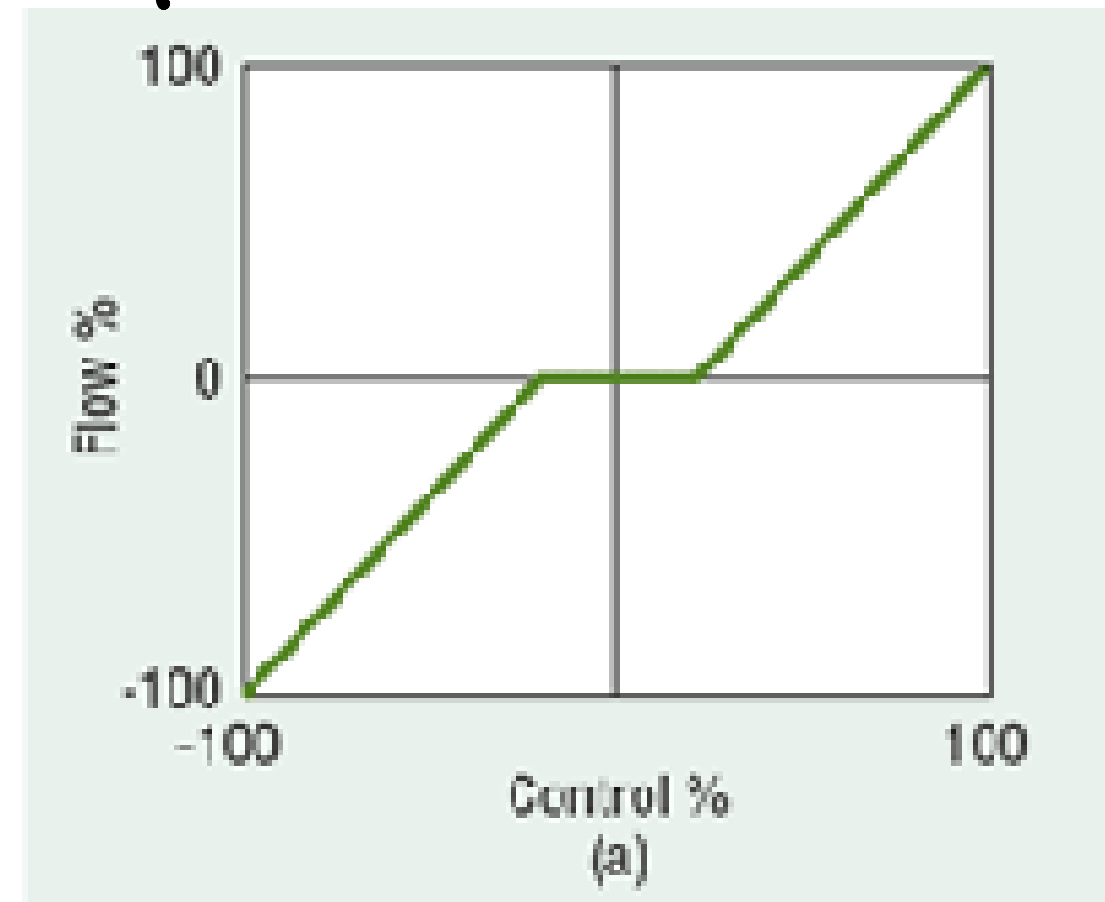
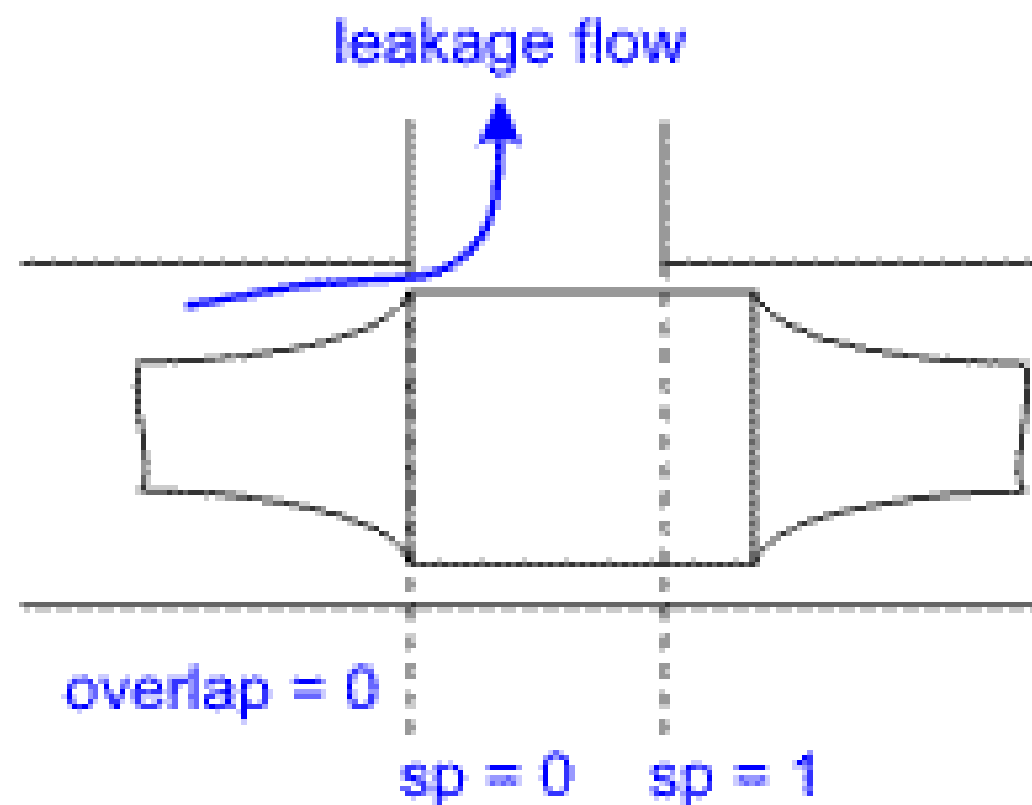
⊖ effect on control: limit cycle instabilities, vibrations

solution: improve mechanical design (e.g. conic fits)

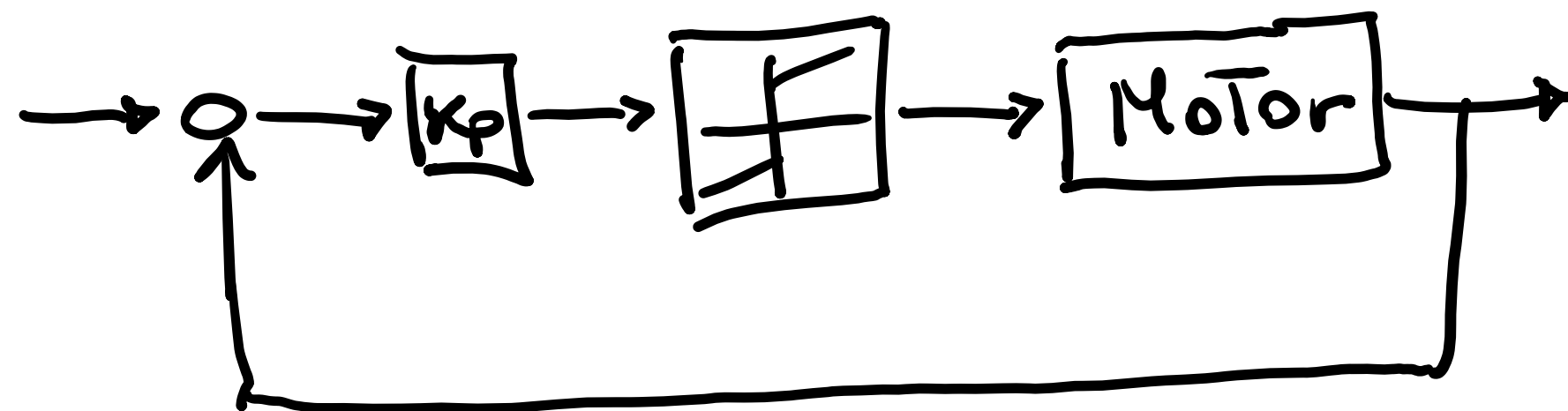
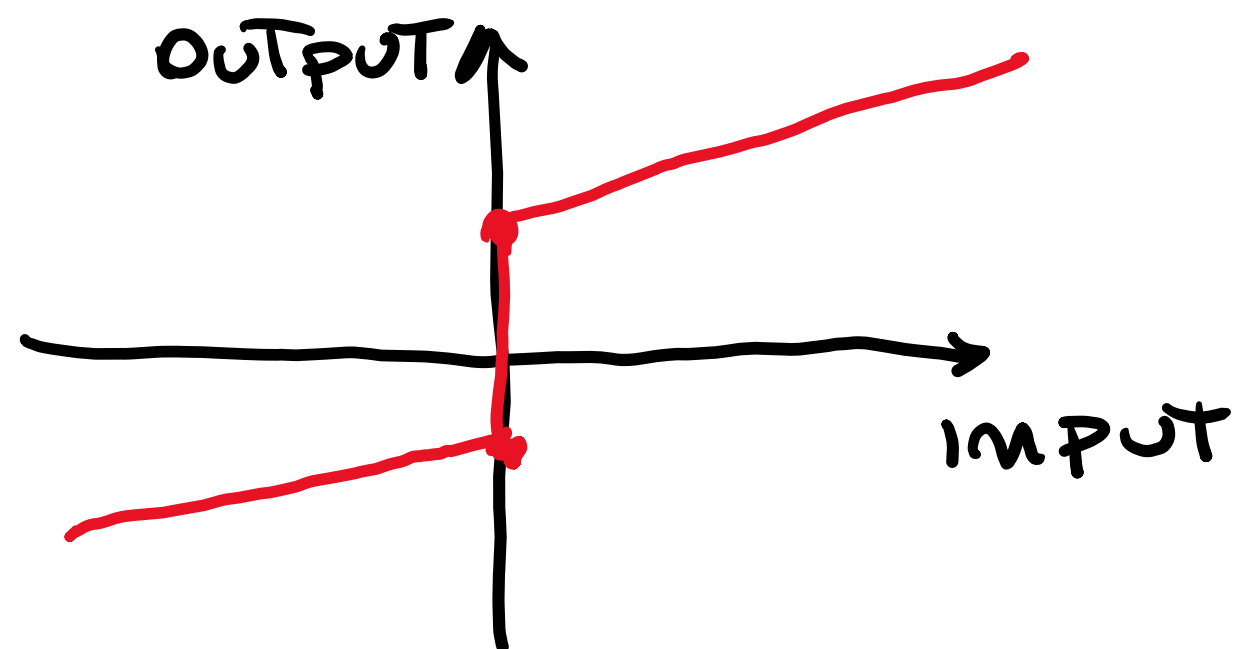


# DEAD BAND

- present in hydraulic valves / motor drivers
- gain is zero for very low inputs



## DEAD BAND COMPENSATION





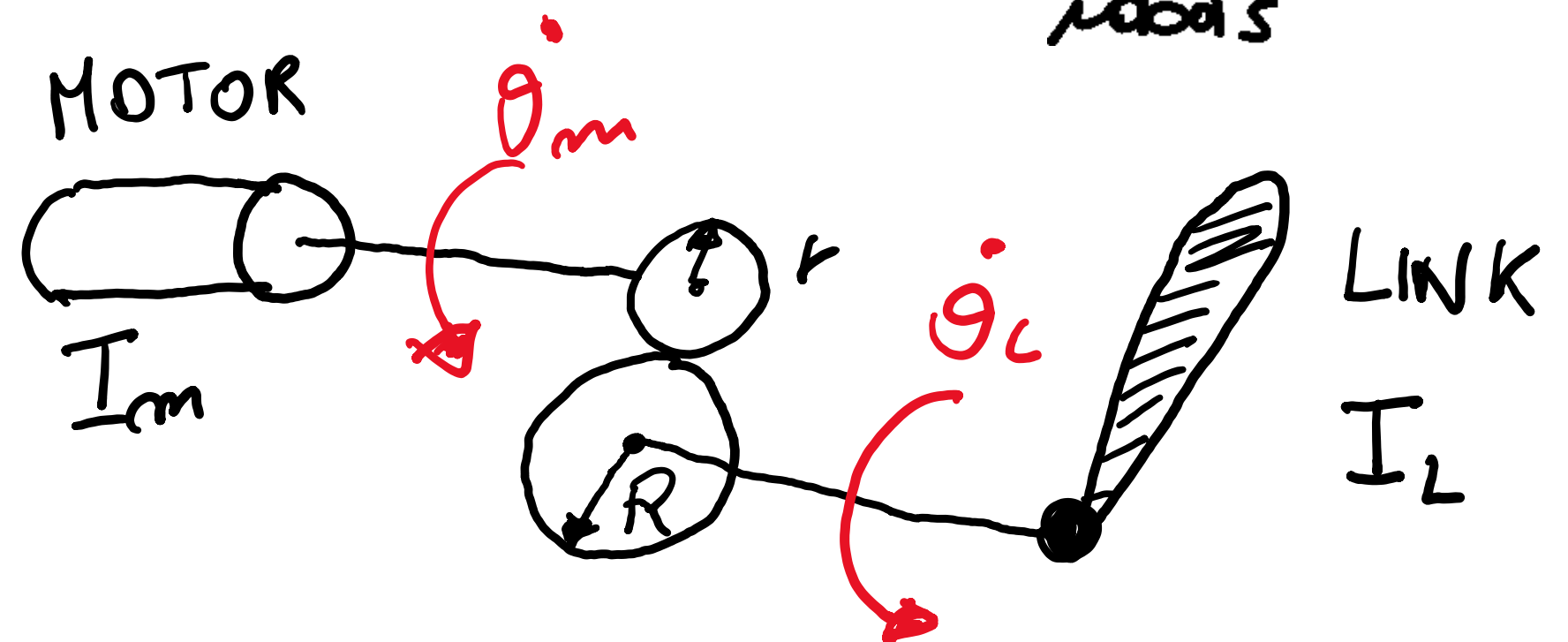
## GEAR BOX

- used to amplify the low torque of electrical motors (employ smaller motors  $\rightarrow$  less weight)

$\downarrow$   
fundamental  
in legged  
robots



## HARMONIC DRIVE GEAR BOX



$$\text{GEAR RATIO} = N = \frac{R}{r} \quad (\text{eg } 100)$$



$$P_m \approx \dot{\theta}_m \tau_m = \dot{\theta}_L \tau_L = P_L \quad \Rightarrow \quad \begin{cases} \dot{\theta}_L = \frac{\dot{\theta}_m}{N} \\ \tau_L = \tau_m N \end{cases}$$

reduces speed

amplifies torque

What about inertia?

$$\bar{I}_m = \frac{\tau_L}{\ddot{\theta}_L} = \frac{\tau_m N}{\frac{\ddot{\theta}_m}{N}} = \frac{\tau_m}{\ddot{\theta}_m} N^2 = I_m N^2$$

reflected motor inertia on load

Therefore the **EFFECTIVE INERTIA** link side is

$$I_e = I_L + \bar{I}_m$$

↳ if  $N \uparrow \uparrow$  it can significantly change the twist response!

↳ changes with the configuration

RULE OF THUMB

$$\hat{I} = \frac{1}{4} \left( \sqrt{I_{e_{\min}}} + \sqrt{I_{e_{\max}}} \right)^2 \quad \text{geometric average}$$



## References:

- Springer Handbook of Robotics - Bruno Siciliano, Oussama Khatib: Forces and Friction (chapter 27.3)
- Control System Design Guide (Fourth Edition), Chapter 12, 2012 - George Ellis: Nonlinear Behavior and Time Variation