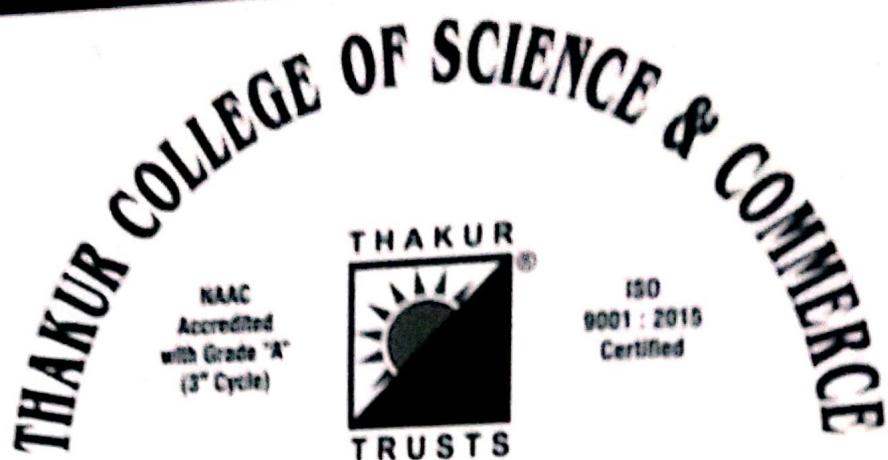


Exam Seat No.



Degree College
Computer Journal
CERTIFICATE

SEMESTER II _____ UID No. _____

Class FYBSC _____ Roll No. 1758 _____ Year 2019 - 20

This is to certify that the work entered in this journal
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who has worked for the year 2020 in the Computer
Laboratory.


Teacher In-Charge


Head of Department

Date: _____

Examiner

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PRACTICAL - 1

AIM : Basics of R software.

- 1) R is a software for statistical analysis and data computing
- 2) It is an effective data handling software and outcome storage is possible.
- 3) It is capable of graphical display
- 4) It is a free software

Q1 Solve the followings

1. $4+6+8 \div 2-5$

$\geq 4+6+8/2-5$

[1] 9

2. $2^2 + 1 - 3[1 + \sqrt{45}]$

$\geq 2^2 + \text{abs}(-3) + \text{sqrt}(45)$

[1] 13. 7082

3/ $5^3 + 7 \times 5 \times 8 + 46/5$

$\geq 5^3 + 7 * 5 * 8 + 46/5$

[1] 4142.

4. $\sqrt{4^2 + 5 \times 3 + 7/6}$
 $\geq \text{sqrt}(4^2 + 5 * 3 + 7/6)$

[1] 6.691567

5. round off

$66 \div 7 + 9 \times 8$
 $\geq \text{round}(66 / 7 + 9 * 8)$

[1] 99

6/ $\geq c(2,3,5,7) * 2$

[1] 4 6 10 14

$\geq c(2,3,5,7) * c(2,3)$

[1] 4 9 10 21

$\geq c(2,3,5,7) * c(2,3,6,2)$
 $\geq c(1,6,2,3) * c(-2,-3,-4,-1)$

[1] 4 9 30 14

[1] -2 -18 -8 -3

$\geq c(2,3,5,7)^2$

[1] 4 9 25 49

$\geq c(4,6,8,9,4,5)^c(1,2,3)$

[1] 4 36 512 9 16 125

$\geq c(6,2,7,5) / c(4,5)$

[1] 1.50 0.40 1.75 1.00

Q3/ $x=20$ $y=30$ $z=2$
 $\geq x^2 + y^3 + z$

[1] 27402

$\geq \text{sqrt}(x^2 + y)$

[1] 20. 93644

$\geq x^2 + y^3$

[1] 1300

51

```

>y>x<-matrix(nrow=4, ncol=2, data=c(1,2,3,
4,5,6,7,8))
>x
[1,] [1,] [2]
[1,] 1 5
[2,] 2 6
[3,] 3 7
[4,] 4 8

```

Q5/Find xy and $2x+3y$ where $x = \begin{bmatrix} 1 & -2 & 6 \\ 3 & 0 & 2 \\ 4 & -5 & 3 \\ 5 & -6 & 5 \end{bmatrix}$

```

>y>xy<-matrix(nrow=3, ncol=3, data=c(4,7,9,-2,0,-5,
6,7,3))
>xy
[1,] [1,] [2] [3]
[1,] 4 -2 6
[2,] 7 0 7
[3,] 9 -5 3

```

Q6/x<-matrix(nrow=3, ncol=3, data=c(10,12,15,
-5,-6,7,9,5))
>y
[1,] [1,] [2] [3]
[1,] 10 -5 7
[2,] 12 -4 9
[3,] 15 6 5

Q7/x+y
[1,] [1,] [2] [3]
[1,] 14 -7 13
[2,] 19 -4 16
[3,] 24 -11 8

55

```

>z<-x+3*y
[1,] [1,] [2] [3]
[1,] 38 -19 33
[2,] 50 -12 41
[3,] 63 -28 21

```

Q8/Marks of students of CS Batch B

```

>x=c(58,20,35,24,46,56,55,45,27,22,47,58,
54,40,50,32,36,29,35,39)
>x

```

>a=c(data)
>breaks=seq(20,60,5)
>a=cut(x, breaks, right=FALSE)
>b=table(a)
>c=transform(b)

a	freq
[20,25]	3
(25,30]	2
(30,35]	1
(35,40]	4
(40,45]	1
(45,50]	3
(50,55]	2
(55,60]	4

PRACTICAL - 2

TOPIC : Probability distribution

- 1) Check whether the following are p.m.f or not

x	$p(x)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

If the given data is p.m.f then $\sum p(x) = 1$

$$\begin{aligned} & \therefore p(0) + p(1) + p(2) + p(3) + p(4) + p(5) = p(x) \\ & = 0.1 + 0.2 - 0.5 + 0.4 + 0.3 + 0.5 \\ & = 1.0 \end{aligned}$$

$\therefore p(2) = -0.5$, it can be a probability mass function

$$\therefore p(x) \geq 0 \quad \forall x.$$

x	$p(x)$
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

The condition for p.m.f is $\sum p(x) = 1$

$$\begin{aligned} \sum p(x) &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1.1 \end{aligned}$$

\therefore The given data is not a p.m.f because $\sum p(x) \neq 1$

x	$p(x)$
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

The condition for p.m.f is

$$1) p(x) \geq 0 \quad \forall x \text{ satisfy}$$

$$2) \sum p(x) = 1$$

$$\begin{aligned} \sum p(x) &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1 \end{aligned}$$

\therefore The given data is p.m.f

Note:

\triangleright prob = C(0.2, 0.2, 0.35, 0.15, 0.1)

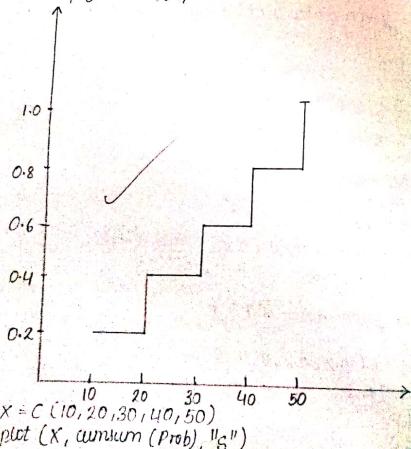
\triangleright sum(prob)

[7]1

Q2 Find the C.d.f for the following p.m.f and sketch the graph

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

$$F(x) = \begin{cases} 0 & x < 10 \\ 0.2 & 10 \leq x < 20 \\ 0.4 & 20 \leq x < 30 \\ 0.75 & 30 \leq x < 40 \\ 0.90 & 40 \leq x < 50 \\ 1.0 & x \geq 50 \end{cases}$$



```
> X = c(10, 20, 30, 40, 50)
> plot(X, cumsum(prob), "s")
```

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Q2 Find

x	1	2	3	4	5	6
$p(x)$	0.15	0.25	0.1	0.2	0.2	0.1

$$\begin{aligned} H(x) &= 0 & x < 1 \\ &= 0.15 & 1 \leq x < 2 \\ &= 0.40 & 2 \leq x < 3 \\ &= 0.50 & 3 \leq x < 4 \\ &= 0.70 & 4 \leq x < 5 \\ &= 0.90 & 5 \leq x < 6 \\ &= 1.00 & x \geq 6 \end{aligned}$$

```
> Prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)
```

```
> sum(Prob)
```

```
[1] 1
```

```
> cumsum(Prob)
```

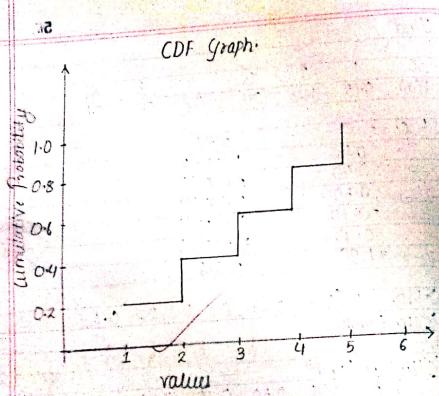
```
[1] 0.15 0.40 0.50 0.70 0.90 1.00
```

```
> X = c(1, 2, 3, 4, 5, 6)
```

```
> plot(X, cumsum(Prob), "s", xlab = "value",
```

```
ylab = "cumulative probability",
```

```
main = "CDF graph", col = "brown")
```



3/ check that whether the following is p.d.f or not

(i) $f(x) = 3 - 2x$; $0 \leq x \leq 1$

(ii) $f(x) = 3x^2$; $0 \leq x \leq 1$

(iii) $f(x) = 3x$

$$= [3x - x^2]_0^1 = 2.$$

$\therefore \int f(x) = 1 \quad \because \text{It is not a pdf}$

2) $f(x) = 3x^2$; $0 < x < 1$

$$\int f(x)$$

$$= \int 3x^2$$

$$= 3 \int x^2$$

$$= 3 \left[\frac{x^3}{3} \right]_0^1 \quad \because x^n = \frac{x^{n+1}}{n+1}$$

$$= x^3$$

$$= 1$$

The $\int f(x) = 1 \quad \therefore \text{It is a pdf}$

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PRACTICAL - 3

TOPIC : Binomial distribution

$$\begin{aligned} \# P(X=x) &= dbinom(x, n, p) \\ \# P(X \leq x) &= pbnom(x, n, p) \\ \# P(X \geq x) &= 1 - pbnom(x, n, p) \\ \# If x \text{ is unknown} \\ P_x &= P(X \leq x) = qbinom(p_1, n, p) \end{aligned}$$

- 1) Find the probability of exactly 10 success in hundred trials with $p=0.4$
- 2) Suppose there are 12 mcq, each question has 5 options out of which 1 is correct. Find the probability of having exactly 4 correct answers
 i) At least 4 correct answers
 ii) More than 5 correct answers.
- 3) Find the complete distribution when $n=5$ and $p=0.1$
- 4) $n=12, p=0.25$ find the following probabilities.
 i) $P(X=5)$ iii) $P(X>7)$
 ii) $P(X \leq 5)$ iv) $P(5 < X < 7)$

1) $X \sim binom(10, 0.2)$
 $P(X=3) = 0.1303653$

2) $dbinom(4, 12, 0.2)$
 $\boxed{P(X \geq 4) = 0.6}$
 $pbnom(4, 12, 0.2)$
 $\boxed{P(X \leq 4) = 0.4}$
 $1 - pbnom(5, 12, 0.2)$
 $\boxed{P(X > 5) = 0.394058}$
 $qbinom(5, 12, 0.2)$
 $\boxed{P(X \leq 5) = 0.50004}$
 $1 - 0.52035$
 $2 - 0.04290$
 $3 - 0.00810$
 $4 - 0.00045$
 $5 - 0.00001$

3) $dbinom(5, 12, 0.25)$
 $\boxed{P(X=4) = 0.1032414}$
 $pbnom(5, 12, 0.25)$
 $\boxed{P(X \leq 4) = 0.9455938}$
 $1 - pbnom(5, 12, 0.25)$
 $\boxed{P(X > 5) = 0.00298151}$
 $dbinom(6, 12, 0.25)$
 $\boxed{P(X \leq 6) = 0.04014945}$

(5)

- e
- 5) The probability of a salesman making a sale to customer 0.15. Find the probability of
 - No sales till 10 customer
 - More than 3 sales out of 20 customer.
 - 6) A salesman has 20% probability of making a sale to customer. Out of 30 customers what minimum number of sales he can make with 88% of probability
 - 7) X follows binomial distribution with $n=10, p=0.3$ plot the graph of p.m.f and c.d.f.

```

>dbinom(0,10,0.15)
[1] 0.1068744
>l=dbinom(3,20,0.15)
[1] 0.3522742
>qbinom(0.88,130,0.2)
[1] 9
60
>n=10
>p=0.3
>x=0:n
>pmb=dbinom(x,n,p)
>unprob=pbiniom(x,n,p)
>d=data.frame("X values"=x,"probability"=prob)
>print(d)
   X value    probability
1     0        0.0282
2     1        0.1210
3     2        0.2334
4     3        0.2668
5     4        0.2001
6     5        0.1029
7     6        0.0367
8     7        0.0090
9     8        0.0014
10    9        0.0001
11   10       0.0000
  
```

PRACTICAL - 4

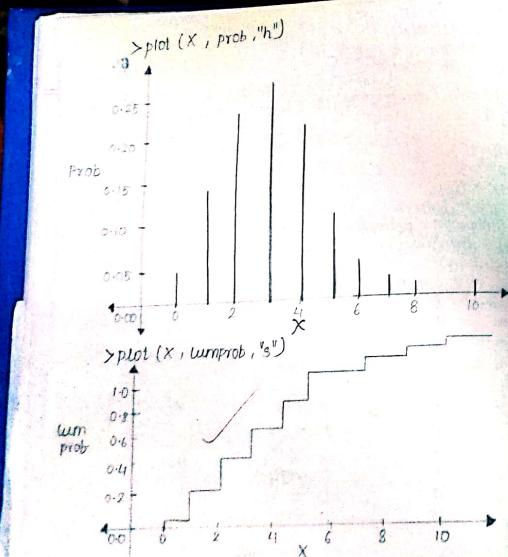
AIM : Normal Distribution.

- $p(x=x) = dnorm(x, \mu, \sigma)$
- $p(x < x) = pnorm(x, \mu, \sigma)$
- $p(x > x) = 1 - pnorm(x, \mu, \sigma)$
- To generate random numbers from a normal distribution (n random numbers) the R code is $xnorm(n, \mu, \sigma)$

Q1 A random variable X follows normal distribution with Mean $\mu = 12$ and $\sigma = 3$. Find
 i) $P(X \leq 15)$ ii) $P(10 \leq X \leq 13)$ iii) $P(X \geq 14)$
 iv) Generate 5 observations (random numbers)

CODE :

```
>p1 = pnorm(15,12,3)
>p1
[1] 0.8413447
>cat("P(X \leq 15) = ", p1)
P(X \leq 15) = 0.8413447
>p2 = pnorm(13,12,3) - pnorm(10,12,3)
>p2
[1] 0.3780661
>cat("P(10 \leq X \leq 13) = ", p2)
P(10 \leq X \leq 13) = 0.3780661
>p3 = 1 - pnorm(14,12,3)
>p3
[1] 0.2524925
```



Q3 Generate 5 random numbers from a normal distribution $\mu=15$, $\sigma=4$. Find sample mean, median, S.D and print it.

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```
CODE:  
> xnorm(15, 15, 4)  
[1] 10.3649 9.793249 9.953444 13.345904  
[2] 17.509668  
> am = mean(x)  
> me = median(x)  
> sd = sqrt(var(x))  
> v = (n-1) * var(x)/n  
> v  
[1] 11.09965  
> sd = sqrt(v)  
> sd  
[1] 3.33163  
> sd  
[1] 3.33163
```

a

```
> cat("P(X>14) = ", p3)  
P(X>14) = 0.2526495  
> p4 = rnorm(5, 12, 3)  
> p4  
[1] 15.254723 16.548505 11.280515 6.419944 12.27216  
2. X follows normal distribution with  $\mu=10$ ,  $\sigma^2=2$ .  
Find i)  $P(X<7)$  ii)  $P(5 < X < 12)$  iii)  $P(X>12)$ .  
iv) Generate 10 observations V. Find k such that  
 $P(X < K) = 0.4$ .
```

CODE:

```
> a1 = rnorm(7, 10, 2)  
[1] 0.668072  
> a2 = rnorm(5, 10, 2) - pnorm(12, 10, 2)  
[1] -0.8351351  
> a3 = 1 - pnorm(12, 10, 2)  
[1] 0.1586553  
> a4 = rnorm(10, 10, 2)  
[1] 11.608931 9.920417 12.639741 8.073354  
8.72380 9.193726 9.366829 11.707106  
9.587584 10.715006  
> a5 = rnorm(04, 10, 2)  
> a5  
[1] 9.493306.
```

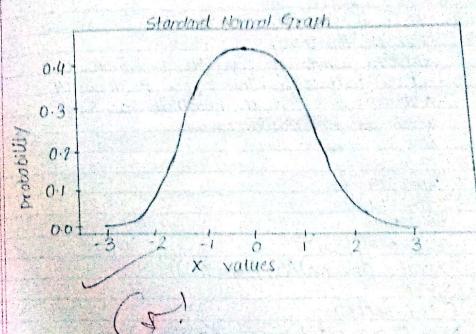
Q4 $X \sim N(30, 100), \sigma = 10$
i) $P(X \leq 40)$
ii) $P(X > 35)$
iii) $P(25 \leq X \leq 35)$
iv) Find k such that $P(X \leq k) = 0.6$

```
> f1 = pnorm(40, 30, 10)
> f1
[1] 0.841349
> f2 = 1 - pnorm(35, 30, 10)
> f2
[1] 0.3085375
> f3 = pnorm(25, 30, 10) - pnorm(35, 30, 10)
> f3
[1] -0.3829249
> f4 = qnorm(0.6, 30, 10)
> f4
[1] 32.53249
```

Q5 Plot the standard normal graph.

```
> x = seq(-3, 3, by = 0.1)
> y = dnorm(x)
> plot(x, y, xlab = "x values", ylab = "probability",
main = "standard normal graph")
```

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PRACTICAL - 5

TOPIC : Normal and t-test

$H_0: \mu = 15$ $H_1: \mu \neq 15$

Test the hypothesis
Random sample of size 400 is drawn and
it is calculated. The sample mean is 14.
And S.D is 3. Test the hypothesis at 5%
level of significance

0.05 > accept the value

0.05 < less than reject

> $m_0 = 15$

> $m_x = 14$

> $n = 400$

> $s_d = 3$

> $z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$

> z_{cal}

[1] -6.666667

> z_{cal} ("calculated value of z is = ", z_{cal})

calculated value of z is = -6.666667

> $pvalue = 2 * (1 - normabs(z_{cal}))$

> $pvalue$

[1] 2.616746e-11

"The value is less than 0.05 we will
reject the value of $H_0 = \mu = 15$

2) Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$
A random sample size of 400 is drawn
with sample mean = 10.2 and $s_d = 2.25$

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Test the hypothesis at

> $m_0 = 10$

> $n = 400$

> $m_x = 10.2$

> $s_d = 2.25$

> $z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$

> z_{cal}

[1] 1.77778

> $pvalue = 2 * (1 - normabs(z_{cal}))$

> $pvalue$

[1] 0.07544036

"The value pvalue is greater than 0.05

: The value is accepted

3) Test the hypothesis $H_0: p = 0.2$
A sample is collected and calculated the sample proportional
as 0.125. Test the hypothesis at 5% level of significance
(sample size is 900)

> $p = 0.2$

> $p = 0.125$

> $n = 900$

> $q = 1 - p$

> $z_{cal} = (p - p_0) / \sqrt{p_0 * q / n}$

> z_{cal} ("calculated value of z is = ", z_{cal})

[1] calculated value of z is = -3.75

> $pvalue = 2 * (1 - normabs(z_{cal}))$

> $pvalue$

[1] 0.0001768346 (Reject)

4) last year farmer's lost 20% of their crops. A random sample of 60 fields are collected and it is found that 9 field crops are threat polluted. Test the hypothesis at 1% level of significance.

```

>p=0.2
>p=9/60
>n=60
>zcal=(p-p)/(sqrt(p*(1-p)/n))
>zcal
[1] -0.9652458
>pvalue = 2*(1-pnorm(abs(zcal)))
>pvalue
[1] 0.3329216
  
```

\therefore The value is 0.1 so value is accepted.

5) Test the hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of significance.

```

>X=c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 11.94, 11.89,
  12.16, 12.04)
>n= length(x)
>n
[1] 10
>mx=mean(x)
>mx
[1] 12.107
  
```

>variance = (n-1) * var(x) / n
>variance
[1] 0.019521
>sd = sqrt(variance)
>sd
[1] 0.1397176
>m0 = 12.5
>t = (mx - m0) / (sd / sqrt(n))
>t
[1] -8.894909
>pvalue = 2*(1-pnorm(abs(t)))
>pvalue
[1] 0
 \therefore The value is less than 0.05 the value is accepted.

(S)

PRACTICAL - 6

AIM : Large sample test

1. Let the population mean (the amount spent per customer in a restaurant) is 250. A sample of 100 customers selected the sample mean is calculated as 275 and SD 30. Test the hypothesis that the population mean is 250 or not at 5% level of significance.
2. In a random sample of 1000 students it is found that 750 like blue pen test the hypothesis that the population proportion is 0.8 at 1% level of significance.
3. Solution:
 $\hat{m}_0 = 250$
 $\hat{m}_x = 275$
 $S_d = 30$
 $n = 100$
 $Z_{cal} = (\hat{m}_x - m_0) / (S_d / \sqrt{n})$
 (Calculated value of Z is = "Zcal")
 Z_{cal} (calculated value of Z is = 8.333333)
 $P_{value} = 2 * (1 - norm (abs (Zcal)))$
 P_{value}
 (The value is less than 0.01 we will reject the null hypothesis)

\hat{m}_0

\hat{m}_x

S_d

n

$Z_{cal} (p - p) / (\sqrt{p(1-p)/n})$

Z_{cal} (calculated value of Z is = "Zcal")

(Calculated value of Z is = "Zcal")

$P_{value} = 2 * (1 - norm (abs (Zcal)))$

P_{value}

(The value is less than 0.01 we reject !)

3. In random sample of size 1000 & 2000 are drawn from two population with same SD 2.5 the sample means are 67.5 & 68.5 test the hypothesis $H_0: \mu_1 = \mu_2$ at 5% level of significance.

4. A study of noise level in 2 hospital is given below test the claim that 2 hospital have same level of noise at 1% level of significance

Hos.A	Hos.B
84	34
61.2	59.4
7.9	7.5

(The value is less than 0.05 we will reject the null hypothesis)

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5. In a sample of 600 students 400 used blue ink. In another sample of 900 students 450 use blue ink. Test the hypothesis that the proportion of students using blue ink in two colleges are equal or not at 1% level of significance.

3. Solution :

```
>n1 = 1000
>n2 = 900
>mx1 = 67.5
>mx2 = 68
>sdl = 2.5
>sdl2 = 2.5
>zcal = (mx1 - mx2) / sqrt((sd1^2/n1) + (sd2^2/n2))
>zcal
[1] -5.163978
>pvalue = 2 * (1 - pnorm(abs(zcal)))
>pvalue
[1] 2.417564e-07 :: (Rejected)
```

4.

```
>n1 = 84
>n2 = 84
>mx1 = 61.2
>mx2 = 59.4
>sdl = 7.9
>sdl2 = 7.5
>zcal = (mx1 - mx2) / sqrt((sd1^2/n1) + (sd2^2/n2))
>zcal
[1] 1.162528
>pvalue = 2 * (1 - pnorm(abs(zcal)))
>pvalue
```

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[1] 0.24550211
 \therefore The value is greater than 0.01 we accept the value

5. $H_0 : P_1 = P_2$ against $H_1 : P_1 \neq P_2$
>n1 = 600
>n2 = 900
>p1 = 400/600
>p2 = 450/900
>p = (n1 * p1 + n2 * p2) / (n1 + n2)
>p
[1] 0.566067
>q = 1 - p
>q
[1] 0.4333333
>zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))
>zcal
[1] 6.381534
>pvalue = 2 * (1 - pnorm(abs(zcal)))
>pvalue
[1] 1.95322e-10
 \therefore Value is less than 0.01 the value is rejected

a

6. $H_0 : p_1 = p_2$ vs $H_1 : p_1 \neq p_2$

```

> n1=200
> n2=200
> p1=14/200
> p2=30/200
> p=(n1*p1+n2*p2)/(n1+n2)
> p
[1] 0.185
> q=1-p
> z
[1] 0.815
> zcal=(p1-p2)/sqrt(p*q*(1/n1+1/n2))
> zcal
[1] 1.802741
> pvalue=2*(1-pnorm(abs(zcal)))
> pvalue
[1] 0.0714283
::Accept ==> greater than 0.05.

```

(Handwritten note: *Ans*)

PRACTICAL - 7

TOPIC : small sample test

The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 71, 72. Test the hypothesis that the sample comes from the population with average 66.

$H_0 : \mu = 66$

$>x = c(66, 63, 66, 67, 68, 69, 70, 71)$

$>t < t(x)$

one sample t-test

data : x

$t = 68.319, df = 9, pvalue = 1.558e-13$

alternative hypothesis

true mean is not equal to 0

95 percent confidence interval

65.65131 70.14829

sample estimate

mean of x

67.9

\therefore The pvalue is less than 0.05 we reject the hypothesis at 5% level of significance.

2. Two groups of students scored the following marks. Test the hypothesis that there is no significant difference between the 2 groups.

GR1 = 18, 22, 23, 21, 17, 20, 17, 23, 20, 22, 21
 GR2 = 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H₀: There is not difference b/w the 2 groups.

>X = c(18, 22, 23, 21, 17, 20, 17, 23, 20, 22, 21)
 >Y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)

>t.test(X, Y)
 Welch two sample t-test

data : X and Y
 t = 2.2573 df = 16.376 p-value = 0.03798
 alternative hypothesis:

True difference in means is not equal to 0
 95 percent confidence interval:
 0.1628205 5.0311795

sample estimates:
 mean of X mean of Y
 20.1 17.5

>t-value = 0.03798
 >if (pvalue > 0.05) {cat("accept H₀")}
 >else {cat("reject H₀")}
 >reject H₀.

(Paired t-test)

3) The sales data of 56 shops before & after a special campaign are given below.

70

Before : 53, 28, 31, 48, 50, 42

After : 58, 29, 30, 55, 56, 45

Test the hypothesis that the campaign is effective or not.

H₀ : There is no significant difference of sales before & after campaign.

>x = c(Before)

>y = c(After)

>t.test(X, Y, paired = T, alternative = "greater")

paired t-test

data : X & Y

t = -2.7815, df = 5, pvalue = 0.9808

alternative hypothesis:

True difference in means is greater than 0

95 percent confidence interval:

-6.035547 inf

sample estimates

mean of the difference

-3.5

∴ pvalue is greater than 0.05, we accept the hypothesis at 5% level of significance.

4) Following are the weights before & after the diet program. Is the diet program effective?

Before : 120, 125, 115, 130, 123, 119
 After : 100, 114, 95, 90, 115, 99

Sol: H_0 : There is no significant difference
 $>x = c(\text{Before})$
 $>y = c(\text{After})$
 $>t\text{-test}(x, y, \text{paired} = T, \text{alternative} = "less")$
 paired t-test
 data : $x \& y$
 $t = 4.30158, df = 5, p\text{value} = 0.9963$
 alternative hypothesis : true difference in means is less than 0.
 95 percent confidence interval:
 $-inf \ 24.0295$

sample estimates:
 mean of the differences
 19.83333

\because p-value is greater than 0.05 we accept the hypothesis at 5% level of significance.

5) 2 medicines are applied to two groups of patient respectively.

gr1 : 10, 12, 13, 11, 14
 gr2 : 8, 9, 12, 14, 15, 10, 9
 Is there any significant difference b/w 2 medicines
 H_0 : There is no significant difference
 $>x = c(grp1)$
 $>y = c(grp2)$
 $>t\text{-test}(x, y)$
 data : $x \& y$
 $t = 0.80384, df = 9, 7.594, p\text{value} = 0.4406$
 alternative hypothesis : true difference in means is not equal to 0
 95 percent confidence interval
 $-0.9698553 \ 4.2981886$
 Sample estimates:
 mean of x mean of y
 12.0000 10.33333

\because p-value is greater than 0.05 we accept the hypothesis at 5% level of significance.

(c)

PRACTICAL - 8

TOPIC : Large and small Test

Questions.

- The arithmetic mean of a sample of 100 items from a large population is 52. If the standard deviation is 7, test the hypothesis that the population mean is 55 against the alternative it is more than 55 at 5% level.
 $H_0: \mu = 55 \quad H_1: \mu > 55$
 $n = 100$
 $m = 52$
 $s = 7$
 $z_{cal} = (m - m_0) / (s / \sqrt{n})$
 z_{cal}
 $z_{cal} = 4.285714$
 $p\text{value} = 2 * (1 - \text{norm}(abs(z_{cal})))$
 $p\text{value}$
 $[1] 8.2153e-05$

"The value is less than 0.05 we will reject the value $H_0: \mu = 55$

- In a big city 350 out of 700 males are found to be smokers. Does this information supports that exactly half of the males in the city are smokers? Test at 1% level.

$s^2 = p = 0.5 \quad H_0: H_1: p = 0.5$
 $q = 1 - p$
 $p = 350/700$
 $n = 700$
 $z_{cal} = (p - p_0) / \sqrt{(p * q / n)}$
 z_{cal}
 $[1] 0$
 $p\text{value} = 2 * (1 - \text{norm}(abs(z_{cal})))$
 $p\text{value}$
 $[1] 1$

"The value of 1 is greater than 0.01 we accept the Hypothesis."

- Two random article from a factory A are found to have 2% defective, 1500 articles from a 2nd factory B are found to have 1% defective. Test at 5% level that the two factory are similar or not.

$s^2 = H_0: p_1 = p_2 \quad H_1: p_1 \neq p_2$
 $n_1 = 1000$
 $n_2 = 1500$
 $p_1 = 0.02$
 $p_2 = 0.01$
 $p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$
 p
 $[1] 0.014$
 $q = 1 - p$
 q
 $[1] 0.986$

```

>zcal = (p1-p2)/sqrt(p1*(1-p1)/n1 + p2*(1-p2)/n2)
>zcal
[1] 2.084842
>pvalue = 2 * (1 - pnorm(abs(zcal)))
>pvalue
[1] 0.03705364
:: pvalue is less than 0.05 we reject the hypothesis.

```

Q4. A sample of size 400 was drawn at a sample mean is 99. Test at 5% level that the sample comes from a population with mean 100 and variance 64.

Soln:-

```

H0: μ1 = 100
>m2 = 99
>m0 = 100
>sd = 8
>n = 400
>zcal = ((m2 - m0)/(sd / sqrt(n)))
>zcal
[1] 2.5
>pvalue = 2 * (1 - pnorm(abs(zcal)))
>pvalue
[1] 0.01241933
:: pvalue is less than 0.05 we reject the hypothesis.

```

Q5. The flower stems are selected and the heights are found to (cm) 63, 63, 68, 69, 71, 71, 72. Test the hypothesis that the mean height is 66 or not at 1% LOS.

```

SD0: H0 : μ = 66
>x = c(63, 63, 68, 69, 71, 71, 72)
>t.test(x)

```

One sample t-test
 data : x
 $t = 47.94$, $df = 6$, $pvalue = 5.522e-09$
 alternative hypothesis: true mean is not equal to 0
 95 percent confidence interval :
 64.66479 71.62092
 sample estimates :
 mean of x
 68.14286
 $\therefore p$ value is < 0.05 less than we reject the hypothesis.

Q6 Two random samples were drawn from 2 normal population and their values are A - 66, 67, 75, 76, 62, 64, 88, 90, 92 B - 64, 66, 694, 78, 82, 85, 87, 92, 93, 95, 97. Test whether the population have the same variance at 5% LOS.

Sol:-

```
> z = c(66, 67, 75, 76, 88, 90, 92)
> y = c(64, 66, 694, 78, 82, 92, 93, 95, 97)
H0 : S1 = S2
> var.test(z, y)
```

F test to compare two variance
data : X & y.

$F = 0.63833$

num. df = 8

denom. df = 9.

pvalue = 0.5383

alternative hypothesis : true ratio of variance is not equal to 1.

95 percent confidence interval:

0.1556172 2.91398

sample estimate:

ratio of variances

0.6383349

\therefore pvalue is 0.05 we accept the value.

Q7 A company producing light bulbs finds that mean life span of the population of bulbs is 1200 hours with s.d 125. A sample of 100 bulbs have mean 1150 hours. Test whether the difference between population and sample mean is significantly different?

```
sol: H0:  $H_1: \mu = 1200$ 
> mx = 1150
> m0 = 1200
> sd = 125
> n = 100
> zcal = (mx - m0) / (sd / sqrt(n))
> zcal
[1] -4
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 6.334288e-05
```

\therefore pvalue is less than we reject the hypothesis.

Q8 From each of two consignments of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples in two assignments are significantly different at 1% LOS?

	Sample size	No. of bad apples
consignment 1	200	44
consignment 2	300	56

```

soln: H0: p1 = p2
>n1=200
>n2=300
>p1=44/200
>p2=66/300
>p=(n1*p1+n2*p2)/(n1+n2)
>p
[1] 0.2
>q=1-p
>zcal=(p1-p2)/sqrt(p*(1-p)*(1/n1+1/n2))
>zcal
[1] 0.9128709
>pvalue=2*(1-pnorm(abs(zcal)))
>pvalue
[1] 0.3613104
∴ p-value is less than 0.05 we reject
the hypothesis.

```

(Q)

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PRACTICAL - 9

TOPIC : Non-parametric Testing of Hypothesis using R - environment

1. The following data represent earnings (in dollars) for a random sample of five common stocks listed on the New York stock exchange. Test whether median earnings is 4 dollars.

Data : 168, 3.35, 2.50, 6.23, 3.24.

```

>x<-c(1.68, 3.35, 2.50, 6.23, 3.24);
>n<-length(x);
>n
[1] 5
>x>4;
[1] FALSE FALSE FALSE TRUE FALSE
>s<-sum(x>4); s;
[1] 1
>binom.test(s,n,p=0.5, alternative = "greater");
Exact binomial test
data: x and n
number of successes = 1, number of trials = 5, p-value
alternative hypothesis: true probability of success is greater than 0.5
95 percent confidence interval:
0.01020622 1.0000000
Sample estimate:
probability of success
0.2.

```

2. The scores of 8 students in reading before and after tuion are as follows:
Test whether there is effect of reading

student no:	1	2	3	4	5	6	7	8
Score before	10	15	16	12	09	07	11	12
Score After	13	16	15	13	09	10	13	10

CODE :
 > b <- c(10,15,16,12,09,07,11,12);
 > a <- c(13,16,15,13,08,10,13,10);
 > D <- b-a;
 > wilcox.test(D, alternative = "greater");

wilcoxon signed rank test with
continuity correction data: D
 $N = 10.5$, p-value = 0.8722
alternative hypothesis: true location is greater than 0
Warning message:
In wilcox.test.default(D, alternative = "greater"),
cannot compute exact p-value with ties
 \therefore p-value is greater than 0.05 we accept it

3. The diameter of a ball bearing was measured by 7 inspectors each using two different kinds of calipers. The results were, test whether average ball bearing for

Inspector	1	2	3	4	5	6
Caliper1	0.265	0.268	0.266	0.267	0.269	0.264
Caliper2	0.263	0.262	0.270	0.261	0.271	0.260

caliper 1 and caliper 2 are same.

CODE :
 > X <- c(0.265, 0.268, 0.266, 0.267, 0.269, 0.264);
 > Y <- c(0.263, 0.262, 0.270, 0.261, 0.271, 0.260);
 > wilcox.test(X, Y, alternative = "greater")

wilcoxon rank sum test

data : X and Y
 $w = 24$, $p = 0.197$

alternative hypothesis: true location shift is greater than 0

\therefore p-value is less than the greater than 0.05 we accept it

Q. An office has three elective typewriters A, B, and C. In a study of machine usage, firm has kept records of machine usage rate of seven weeks. Machine A has got 60% repair for two weeks. It is of interest to find out which machine has better usage rate. Analyze the following data on usage rates and determine if there is a significant difference in average usage rate.

A	B	C
12.3	15.7	32.4
15.4	10.8	11.2
10.3	45.0	35.1
8.0	12.3	25.0
14.6	8.2	8.2
	20.1	18.4
-	26.3	32.5

CODE :

```
> X <- c(12.3, 15.4, 10.3, 8.0, 14.6);
> n1 <- length(X);
> n1
[1] 5
> y <- c(15.7, 10.8, 45.0, 12.3, 8.2, 20.1, 26.3);
> n2 <- length(y);
> n2
[1] 7
> z <- c(32.4, 41.2, 35.1, 25.0, 8.2, 18.4, 32.5);
> n3 <- length(z);
> n3
[1] 7
```

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```
> X <- c(x, y, z);
> g <- c(rep(1, n1), rep(2, n2), rep(3, n3));
> kruskal.test(X, g)
```

Kruskal-Wallis rank sum test

data : X and g.
Kruskal-Wallis chi-squared = 5.217, df = 2,
p-value = 0.07365.

∴ p-value is greater than 0.05 we accept it



PRACTICAL - 910

AIM : Chi-square test & ANOVA (Analysis of variance)

Q1: use the following data to test whether the condition of home & condition of child care independent or not.

cond. child	cond. home	
clean	dirty	
clean	70	50
dirty	80	20

H₀: condition of home & child care independent

>x = c(70, 80, 35, 50, 20, 45)

>m = 3

>n = 2

>y = matrix(x, nrow = m, ncol = n)

>y

	[1,1]	[1,2]
[1,]	70	50
[2,]	80	20
[3,]	35	45

>pv = chisq.test(y)

>pv

Pearson's chi-squared test.

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Data: Y

X - Squared = 25.646

df = 2

p-value = 2.698e-06

II They are dependent

∴ p-value is less than 0.05 we reject the hypothesis at 5% level of significance.

Q2: Test the hypothesis that vaccination & disease are independent or not.

vaccine

Disease	Affected	Not Affected
---------	----------	--------------

Affected	70	46
----------	----	----

Non-Affected	35	37
--------------	----	----

H₀: Disease & vaccine are independent.

>x = c(70, 35, 46, 37)

>m = 2

>n = 2

>y = matrix(x, nrow = m, ncol = n)

>y

	[1,1]	[1,2]
--	-------	-------

[1,]	70	46
------	----	----

[2,]	35	37
------	----	----

```

>pv = chisq.test(Y)
>pv
Pearson's chi-squared test with
Yates' continuity correction
data: Y
X-squared = 2.0275
df = 1
p-value = 0.1545

```

∴ p-value is more than 0.05 we accept the hypothesis at 5% level of significance
 They are Independent.

Q.3. Perform a ANOVA for the following data.

TYPE	OBSERVATIONS
A	50, 52,
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

H0 : The mean's are equal for A,B,C,D.

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```

>x1 = c(50, 52)
>x2 = c(53, 55, 53)
>x3 = c(60, 58, 57, 56)
>x4 = c(52, 54, 54, 55)
>d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))
>names(d) = c("values", "ind")
>one.way.test(values ~ ind, data = d)
One-way analysis of means
data: values and ind
F = 11.935, df = 3, denom df = 9,
Pr(>F) = 0.00183
p-value is less than 0.05 we reject the
hypothesis
>anova = aov(values ~ ind, data = d)
>summary(anova)

```

Df	Sum Sq	Mean Sq	F value	Pr (> F)
Ind	3	31.06	23.688	11.93
Residuals	9	18.17	2.019	0.00183**

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Q4 Following data gives a life of time of 4 brands.

life

A	20, 23, 18, 17, 18, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14, 16

H0 : The means of A, B, C, D are equal.

> X1 = C(20, 23, 18, 17, 18, 22, 24)

> X2 = C(B)

> X3 = C(C)

> X4 = C(D)

> d = stack (list (b1 = X1, b2 = X2, b3 = X3, b4 = X4))

> summary (d)

[1] values "Ind"

> one way but (values ~ Ind, data = d, var.equal = T)

one-way analysis of variance

data : values ~ Ind

F = 6.8495, num df = 3, denom df = 20

p-value is less than 0.05 we reject the

hypothesis

anova = aov (values ~ Ind, data = d)

> summary (anova)

Ind	df	sumsq	meansq	Fvalue	Pr(>F)
Residuals	20	89.06	4.453	6.8495	0.0023**

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1

> X = read.csv("C:/users/admin/Desktop/80
marks.csv")

> X

	stats	maths
1	410	60
2	45	48
3	92	47
4	15	20
5	37	25
6	36	27
7	49	57
8	59	58
9	20	25
10	27	27

> am = mean (X \$ stats)

> am

[1] 37

> am1 = mean (X \$ stats)

> am1

[1] 39.4

> m1 = median (X \$ stats)

> m1

[1] 38.5

> m2 = median (X \$ maths)

[1] 37

> n = length (X \$ stats)

[1] 10

Q8.

> sd = sqrt ((n-1) * var (x \$ stats)/n)

> sd

[1] 12.6491

> n1 = length (x \$ maths)

> n1

[1] 10

> sd1 = sqrt ((n-1) * var (x \$ maths)/n)

> sd1

[1] 15.2

> cor (x \$ stats, x \$ maths)

[1] 0.830618

(8)

✓