

$$24 = 2^3 \times 3$$

$$\sigma(24) = (2^0 + 2^1 + 2^2 + 2^3) \times (3^0 + 3^1) \\ = 15 \times 4 = 60$$

$$n = p_1^{a_1} \times p_2^{a_2} \cdots \times p_m^{a_m}$$

p_i 为质数.

$$\sigma(n) = (p_1^0 + p_1^1 + \cdots + p_1^{a_1}) \times (p_2^0 + \cdots) \times \cdots$$

$$\sigma(n) \text{ 奇数} \rightarrow \begin{cases} p_1^0 + p_1^1 + \cdots + p_1^{a_1} \\ p_2 \\ \vdots \\ p_m \end{cases} \quad \text{均为奇数.}$$

$$p_i = \begin{cases} 2 & 2^0 + 2^1 + 2^2 + \cdots \text{一定是奇数.} \\ \text{others.} & \end{cases}$$

$$\underbrace{p^0 + p^1 + \cdots + p^a}_{p^x \text{ 一定是奇数}} \text{ is } \begin{array}{l} \text{奇} \Rightarrow \text{当 } a \text{ 为偶} \\ \text{偶} \Rightarrow \text{当 } a \text{ 为奇.} \end{array}$$

$$\therefore \sigma(n) = (p_1^0 + p_1^1 + \cdots + p_1^{a_1}) \times (p_2^0 + p_2^1 + \cdots + p_2^{a_2}) \times \cdots$$

① $p_1 \neq 2$. q_i 均为偶数 设 $q_i = 2k_i$

$$\Rightarrow n = p_1^{q_1} p_2^{q_2} \dots p_m^{q_m}$$

$$= (p_1^{k_1} p_2^{k_2} \dots p_m^{k_m})^2 = T^2$$

n 为平方数.

② $p_1 = 2$ $n = 2^{q_1} \cdot (p_2^{k_2} p_3^{k_3} \dots p_m^{k_m})^2$

当 $q_1 = 1$ $n = 2T^2$

$q_1 > 1$ 且 $q_1 = 2q'$ $n = (2^{q'} T)^2 = T'^2$

$q_1 > 1$ 且 $q_1 = 2q' + 1$ $n = 2(2^{q'} T)^2 = 2T'^2$

综上 当 $n = T^2$ 或 $2T^2$ 时, $G(n)$ 为奇数.

$$\text{count}(n = T^2) = \lfloor \sqrt{n} \rfloor$$

$$\text{count}(n = 2T^2) = \lfloor \sqrt{\lfloor \frac{n}{2} \rfloor} \rfloor$$

$$\text{ans} = n - \lfloor \sqrt{n} \rfloor - \lfloor \sqrt{\lfloor \frac{n}{2} \rfloor} \rfloor$$

