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# Microeconometrics, Empirical project, Group 8

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## Importing data

from Wooldridge, his source: J. Grogger (1991), "Certainty vs. Severity of Punishment," Economic Inquiry 29, 297-309.

```
df<-read.dta("http://fmwww.bc.edu/ec-p/data/wooldridge/crime1.dta")
attach(df)
head(df)</pre>
```

```
##
     narr86 nfarr86 nparr86 pcnv avgsen tottime ptime86 qemp86 inc86 durat black
## 1
                                   17.6
                                            35.2
                  0
                          0 0.38
                                                      12
                                                                   0.0
                          0 0.44
## 2
          2
                  2
                                    0.0
                                             0.0
                                                       0
                                                              1
                                                                  0.8
                                                                           0
                                                                                 0
                                    22.8
                                            22.8
                                                       0
## 3
          1
                  1
                          0 0.33
                                                              0
                                                                  0.0
                                                                          11
                                                                                 1
## 4
          2
                  2
                          1 0.25
                                    0.0
                                             0.0
                                                       5
                                                              2
                                                                  8.8
                                                                          0
                                                                                 0
## 5
          1
                  1
                          0 0.00
                                    0.0
                                             0.0
                                                       0
                                                              2
                                                                  8.1
                                                                           1
                                                                                 0
## 6
          0
                  0
                          0 1.00
                                    0.0
                                             0.0
                                                       0
                                                              4 97.6
                                                                           0
                                                                                 0
##
    hispan born60 pcnvsq pt86sq
                                    inc86sq
                 1 0.1444 144
## 1
          0
                                    0.00000
## 2
                 0 0.1936
                                    0.64000
## 3
          0
                 1 0.1089
                              0
                                    0.00000
                 1 0.0625
                              25
                                   77.44000
## 4
          1
                               0
## 5
          0
                 0.0000
                                    65.61001
## 6
                 1 1.0000
                               0 9525.75977
```

str(df)



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```
$ inc86 : num 0 0.8 0 8.8 8.1 ...
##
   $ durat : num 0 0 11 0 1 ...
##
   $ black : num
                 0 0 1 0 0 0 1 0 1 0 ...
##
   $ hispan : num
                 0 1 0 1 0 0 0 0 0 1 ...
##
   $ born60 : num
                 1 0 1 1 0 1 1 1 1 1 ...
##
   $ pcnvsq : num 0.1444 0.1936 0.1089 0.0625 0 ...
##
   $ pt86sq : num
                144 0 0 25 0 0 0 0 81 0 ...
##
   $ inc86sq: num 0 0.64 0 77.44 65.61 ...
##
   - attr(*, "datalabel")= chr ""
   - attr(*, "time.stamp")= chr "10 Jan 2000 16:54"
##
   - attr(*, "formats")= chr "%9.0g" "%9.0g" "%9.0g" "%9.0g" ...
   ##
                             ...
##
   - attr(*, "val.labels")= chr
                            ...
   - attr(*, "var.labels")= chr
   - attr(*, "version")= int 6
```

#### summary(df)

```
##
        narr86
                          nfarr86
                                            nparr86
                                                                pcnv
##
    Min.
           : 0.0000
                       Min.
                              :0.0000
                                         Min.
                                                :0.0000
                                                           Min.
                                                                   :0.0000
##
    1st Qu.: 0.0000
                       1st Qu.:0.0000
                                         1st Qu.:0.0000
                                                           1st Qu.:0.0000
    Median : 0.0000
                       Median :0.0000
                                         Median :0.0000
                                                           Median :0.2500
##
##
    Mean
          : 0.4044
                       Mean
                              :0.2334
                                         Mean
                                                :0.1255
                                                           Mean
                                                                   :0.3578
##
    3rd Qu.: 1.0000
                       3rd Qu.:0.0000
                                         3rd Qu.:0.0000
                                                           3rd Qu.:0.6700
##
           :12.0000
                       Max.
                              :6.0000
                                                :8.0000
                                                                  :1.0000
##
        avgsen
                          tottime
                                             ptime86
                                                                 qemp86
##
           : 0.0000
                             : 0.0000
                                                : 0.0000
                                                                    :0.000
    Min.
                       Min.
                                          Min.
                                                             Min.
##
    1st Qu.: 0.0000
                       1st Qu.: 0.0000
                                          1st Qu.: 0.0000
                                                             1st Qu.:1.000
    Median : 0.0000
                       Median : 0.0000
                                          Median : 0.0000
                                                             Median :3.000
          : 0.6323
                             : 0.8387
##
    Mean
                       Mean
                                          Mean
                                                : 0.3872
                                                             Mean
                                                                    :2.309
##
    3rd Qu.: 0.0000
                       3rd Qu.: 0.0000
                                          3rd Qu.: 0.0000
                                                             3rd Qu.:4.000
##
    Max.
           :59.2000
                       Max.
                              :63.4000
                                          Max.
                                                 :12.0000
                                                             Max.
                                                                    :4.000
##
        inc86
                          durat
                                            black
                                                              hispan
##
              0.00
                             : 0.000
                                               :0.0000
    Min.
           :
                      \mathtt{Min}.
                                        \mathtt{Min}.
                                                          Min.
                                                                 :0.0000
##
    1st Qu.: 0.40
                      1st Qu.: 0.000
                                        1st Qu.:0.0000
                                                          1st Qu.:0.0000
##
    Median : 29.00
                      Median : 0.000
                                        Median :0.0000
                                                          Median : 0.0000
##
    Mean
           : 54.97
                      Mean
                             : 2.251
                                        Mean
                                               :0.1611
                                                          Mean
                                                                :0.2176
##
    3rd Qu.: 90.10
                      3rd Qu.: 2.000
                                        3rd Qu.:0.0000
                                                          3rd Qu.:0.0000
                             :25.000
                                               :1.0000
##
                                                                 :1.0000
    Max.
           :541.00
                      Max.
                                        Max.
                                                          Max.
##
        born60
                          pcnvsq
                                            pt86sq
                                                              inc86sq
##
           :0.0000
                             :0.0000
                                               : 0.000
   Min.
                      Min.
                                        Min.
                                                           Min.
                                                                         0.00
##
    1st Qu.:0.0000
                      1st Qu.:0.0000
                                        1st Qu.:
                                                  0.000
                                                           1st Qu.:
                                                                         0.16
##
   Median :0.0000
                      Median :0.0625
                                        Median :
                                                  0.000
                                                           Median :
                                                                       841.00
##
           :0.3626
                             :0.2841
                                                  3.951
                                                                     7458.93
    Mean
                      Mean
                                        Mean
                                                           Mean
                      3rd Qu.:0.4489
##
    3rd Qu.:1.0000
                                        3rd Qu.: 0.000
                                                           3rd Qu.:
                                                                     8118.01
           :1.0000
                             :1.0000
                                        Max.
                                               :144.000
                                                           Max.
                                                                   :292681.00
##
    Max.
                      Max.
```

A data.frame with 2725 observations on 16 variables: - narr86: times arrested, 1986 - nfarr86: felony arrests, 1986 - nparr86: property crme arr., 1986 - pcnv: proportion of prior convictions - avgsen: avg sentence length, mos. - tottime: time in prison since 18 (mos.) - ptime86: mos. in prison during 1986 - qemp86: quarters employed, 1986 - inc86: legal income, 1986, \$100s - durat: recent unemp duration - black: =1 if black - hispan: =1 if Hispanic - born60: =1 if born in 1960 - pcnvsq: pcnv^2 - pt86sq: ptime86^2 - inc86sq: inc86^2



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## **Descriptive Statistics**

## **Correlation Plots**

```
plot(df[,c("narr86", "avgsen", "inc86", "durat")])
                     0 10
                             30
                                  50
                                                              10 15 20 25
       narr86
4
                         avgsen
20
                                                                            500
                                            inc86
                                                              durat
        4 6 8 10
                                                  400
                                            200
cor(df[,c("narr86", "avgsen", "inc86", "durat")])
```

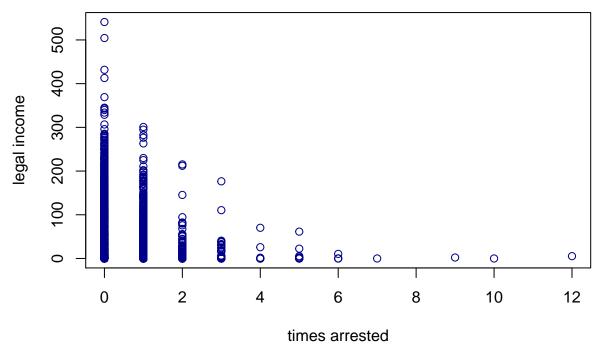
```
## narr86 avgsen inc86 durat
## narr86 1.0000000 0.02929780 -0.18997653 0.08232769
## avgsen 0.02929780 1.00000000 -0.09580596 0.02843162
## inc86 -0.18997653 -0.09580596 1.00000000 -0.34292954
## durat 0.08232769 0.02843162 -0.34292954 1.00000000
```



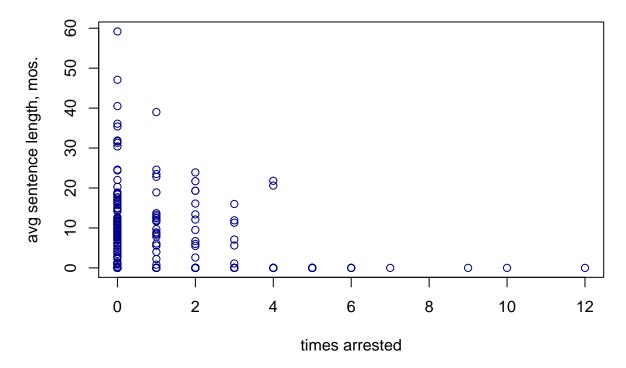
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## Specific Plots:

# Correlation, crime 1986



# Correlation, crime 1986



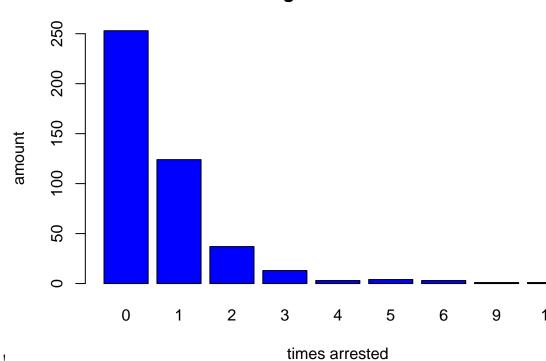
"HISTOGRAMME !"

## [1] "HISTOGRAMME !"



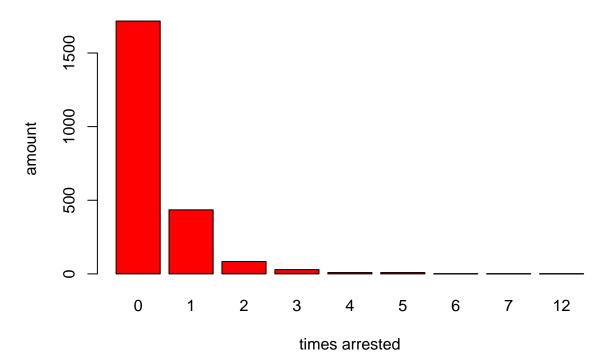
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# Histogram Black/White



"NEEDS CHANGE!!!!!!!!" !!!!

# **Histogram Black/White**



#PART 1



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\*\* Modeling "avgsen" \*\* Building model estimating expected severity of conviction when arrested in 1986 using level of income, employment, total time spend in prison and color (black ad non-black) of the arrested

Our hypothesis is, that the mentioned variables have a significant effect on the average sentence length.

```
avgsen = \beta_0 + \beta_1 inc86 + \beta_2 black + \beta_3 tottime + \beta_4 qemp86
```

## Simple OLS-Estimation

A General OLS estimation including all potential regressors:

```
lm_all<-lm(avgsen~. -nfarr86 - nparr86 , data = df)
summary(lm_all)</pre>
```

```
##
## lm(formula = avgsen ~ . - nfarr86 - nparr86, data = df)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
  -14.4560 -0.0948 -0.0346
                                0.0093
                                        16.7462
##
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.743e-02 7.345e-02
                                       0.237
                                               0.8124
               -4.337e-02 3.060e-02
                                     -1.418
                                               0.1564
## narr86
## pcnv
                3.163e-01 2.467e-01
                                       1.282
                                               0.1998
                7.103e-01 5.712e-03 124.346
                                               <2e-16 ***
## tottime
                9.820e-02
                           7.117e-02
                                       1.380
                                               0.1678
## ptime86
## qemp86
                                               0.1824
                3.911e-02 2.932e-02
                                       1.334
## inc86
               -1.652e-03
                          1.286e-03
                                     -1.284
                                               0.1991
## durat
               -3.538e-04
                           6.318e-03
                                      -0.056
                                               0.9553
## black
               1.361e-01
                           7.193e-02
                                       1.893
                                               0.0585 .
               -2.537e-02
                           6.304e-02
                                      -0.402
                                               0.6875
## hispan
## born60
               -1.248e-02
                           5.225e-02
                                      -0.239
                                               0.8113
               -3.393e-01
                                               0.1749
## pcnvsq
                           2.500e-01
                                      -1.357
## pt86sq
               -1.364e-02
                           6.247e-03
                                      -2.183
                                               0.0291 *
## inc86sq
                3.373e-06
                          4.077e-06
                                       0.827
                                               0.4081
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.298 on 2711 degrees of freedom
## Multiple R-squared: 0.8637, Adjusted R-squared: 0.8631
## F-statistic: 1322 on 13 and 2711 DF, p-value: < 2.2e-16
```

Interpretation: A high R-squared is observable. Only few variables are significant for 0.05 and 0.1 significance level. Also the p-Value of the F-statistic is low, which implies that there are some variables which can be used to explain the average sentence length.

We have proceeded our further estimation of aven after excluding variables which have considerably high p-values.



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The average severity is regressed on the income in 1986, employment in 1986, color (black and non-black) and total time spend in prison.

```
lm_sev<-lm(avgsen~ tottime+ black+ qemp86+ inc86, data = df)
summary(lm_sev)</pre>
```

```
##
## lm(formula = avgsen ~ tottime + black + qemp86 + inc86, data = df)
## Residuals:
       Min
                 1Q
                    Median
                                   3Q
                                           Max
## -14.2801 -0.0774 -0.0329
                               0.0213 17.2152
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.0374053 0.0476873 -0.784
                                            0.4329
              0.7064354 0.0054793 128.928
                                             <2e-16 ***
## tottime
## black
               0.1402641 0.0690914
                                      2.030
                                             0.0424 *
              0.0425101 0.0221607
                                             0.0552 .
## qemp86
                                      1.918
## inc86
              -0.0007928 0.0005335 -1.486
                                             0.1374
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.301 on 2720 degrees of freedom
## Multiple R-squared: 0.8626, Adjusted R-squared: 0.8624
## F-statistic: 4268 on 4 and 2720 DF, p-value: < 2.2e-16
```

## Censored

```
summary(tobit(avgsen~ tottime+ black+ qemp86+ inc86, left=-Inf, right = 60, data=df))
```

```
##
## Call:
## tobit(formula = avgsen ~ tottime + black + qemp86 + inc86, left = -Inf,
##
      right = 60, data = df)
##
## Observations:
##
           Total Left-censored
                                    Uncensored Right-censored
##
            2725
                              0
                                          2725
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.0374053 0.0476435 -0.785
                                             0.4324
## tottime
              0.7064354 0.0054743 129.046
                                              <2e-16 ***
               0.1402641 0.0690279
## black
                                      2.032
                                              0.0422 *
## qemp86
              0.0425101 0.0221403
                                     1.920
                                              0.0549 .
              -0.0007928 0.0005330 -1.487
                                              0.1369
## inc86
## Log(scale)
              0.2625665 0.0135457 19.384
                                              <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```



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```
##
## Scale: 1.3
##
## Gaussian distribution
## Number of Newton-Raphson Iterations: 6
## Log-likelihood: -4582 on 6 Df
## Wald-statistic: 1.71e+04 on 4 Df, p-value: < 2.22e-16</pre>
```

An output of an OLS-Estimation is given:

```
summary((lm_sev))
```

```
##
## Call:
## lm(formula = avgsen ~ tottime + black + qemp86 + inc86, data = df)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    ЗQ
##
  -14.2801 -0.0774 -0.0329
                                0.0213
                                       17.2152
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.0374053
                          0.0476873
                                     -0.784
                                               0.4329
## tottime
               0.7064354
                           0.0054793 128.928
                                               <2e-16 ***
                                               0.0424 *
## black
                0.1402641
                           0.0690914
                                       2.030
## qemp86
                0.0425101
                           0.0221607
                                       1.918
                                               0.0552 .
               -0.0007928
                          0.0005335
                                     -1.486
                                               0.1374
## inc86
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.301 on 2720 degrees of freedom
## Multiple R-squared: 0.8626, Adjusted R-squared: 0.8624
## F-statistic: 4268 on 4 and 2720 DF, p-value: < 2.2e-16
```

Interpretation: We see almost the same R-squared as from the previous OLS-Estimation. The significant variables for 0.05 significance level are the total time spend in prison and the color. No significance of the other variables is proven.

#### Problems with the OLS

Some of the variables may be endogenous E.g assumptions may be violated. => Testing this way may not be correct.

## IV-Regression (using 2SLS-Estimation)

Use instrumental variables in the estimation of the expected severity. Define: endogenous var: income86, qemp86, tottime exogenuos var: black instruments: durat, nparr, nfarr, narr, ptime86

The regression code is given by:



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```
IV_sev1<-ivreg(avgsen~ tottime+ black+ qemp86+ inc86 | black+ durat+ narr86+ nfarr86+ ptime86
summary(IV_sev1, diagnostics=TRUE)</pre>
```

```
##
## Call:
## ivreg(formula = avgsen ~ tottime + black + qemp86 + inc86 | black +
##
       durat + narr86 + nfarr86 + nparr86 + ptime86, data = df)
##
## Residuals:
##
         Min
                    10
                          Median
                                        30
                                                 Max
## -11.72068 -0.17947
                       -0.09283
                                   0.02787
                                            21.82055
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.122938
                           0.132308
                                     0.929 0.35288
                                            < 2e-16 ***
## tottime
                0.627074
                           0.026174 23.958
## black
                0.258763
                           0.090411
                                      2.862
                                             0.00424
## qemp86
               -0.099968
                           0.185116
                                    -0.540 0.58922
## inc86
                0.003139
                           0.006011
                                      0.522 0.60157
##
## Diagnostic tests:
##
                               df1 df2 statistic p-value
## Weak instruments (tottime)
                                 5 2718
                                           46.827 < 2e-16 ***
                                 5 2718
                                          258.873 < 2e-16 ***
## Weak instruments (qemp86)
## Weak instruments (inc86)
                                 5 2718
                                          105.504 < 2e-16 ***
## Wu-Hausman
                                 3 2717
                                            4.503 0.00371 **
## Sargan
                                     NA
                                            2.277 0.32028
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.364 on 2720 degrees of freedom
## Multiple R-Squared: 0.8491, Adjusted R-squared: 0.8488
## Wald test:
                309 on 4 and 2720 DF, p-value: < 2.2e-16
```

Interpretation: Here a high R-squared is observed. Tottime and black are the only significant variables for 0.05 significance level. Furthermore, diagnostics of the instruments are provided. We observe small p-values, which means that instruments are not weak e.g they are appropriate. The value of the Hausmans-test is smaller than than the significance level of 0.05. Thus, meaning that instruments and residuals can be considered as uncorrelated.

## Manual Check if Instuments are adequate

1. Check if regressors and instruments are correlated

```
i1lm_sev1<- lm(tottime~ black+ durat+ narr86+ nfarr86+ nparr86+ ptime86, data=df)
summary(i1lm_sev1)</pre>
```

```
##
## Call:
## lm(formula = tottime ~ black + durat + narr86 + nfarr86 + nparr86 +
```



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```
ptime86, data = df)
##
##
## Residuals:
##
   Min
            1Q Median
                        ЗQ
                             Max
## -9.254 -0.662 -0.306 -0.281 55.743
##
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.28080 0.10601
                              2.649 0.00812 **
## black
            1.09852
                       0.23369
                               4.701 2.72e-06 ***
## durat
            0.02531
                     0.01845
                              1.372 0.17013
                               2.167 0.03031 *
## narr86
             0.38140
                       0.17599
            -0.11213
                       0.25363 -0.442 0.65845
## nfarr86
## nparr86
            -0.46308
                       0.23883 -1.939 0.05261 .
            0.65619
                       0.04338 15.127 < 2e-16 ***
## ptime86
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 4.397 on 2718 degrees of freedom
## Multiple R-squared: 0.09124,
                               Adjusted R-squared: 0.08923
## F-statistic: 45.48 on 6 and 2718 DF, p-value: < 2.2e-16
i2lm_sev1<- lm(qemp86~ black+ durat+ narr86+ nfarr86+ nparr86+ ptime86, data=df)
summary(i2lm_sev1)
##
## lm(formula = qemp86 ~ black + durat + narr86 + nfarr86 + nparr86 +
     ptime86, data = df)
##
## Residuals:
##
     Min
             1Q Median
                           3Q
## -2.7583 -0.9233 0.2340 1.0767 4.6960
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.923252 0.031584 92.554 < 2e-16 ***
            ## black
            ## durat
## narr86
            ## nfarr86
            ## nparr86
            -0.009608
                       0.071160 -0.135 0.89260
## ptime86
            ## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.31 on 2718 degrees of freedom
## Multiple R-squared: 0.3398, Adjusted R-squared: 0.3383
## F-statistic: 233.1 on 6 and 2718 DF, p-value: < 2.2e-16
i3lm_sev1<- lm( inc86~ black+ durat+ narr86+ nfarr86+ nparr86+ ptime86, data=df)
summary(i3lm_sev1)
```



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```
##
## Call:
## lm(formula = inc86 ~ black + durat + narr86 + nfarr86 + nparr86 +
      ptime86, data = df)
##
##
## Residuals:
     Min
             10 Median
                           30
                                 Max
## -74.93 -44.37 -16.33 30.17 465.97
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 75.0256
                           1.4557 51.539 < 2e-16 ***
              -14.8285
                           3.2092 -4.621 4.00e-06 ***
## black
## durat
               -4.7147
                           0.2533 -18.612 < 2e-16 ***
## narr86
                           2.4168 -4.275 1.97e-05 ***
              -10.3329
## nfarr86
               -1.7791
                           3.4829
                                   -0.511
                                             0.610
               -2.1158
                           3.2797 -0.645
                                             0.519
## nparr86
               -5.6714
                           0.5957 -9.520 < 2e-16 ***
## ptime86
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 60.38 on 2718 degrees of freedom
## Multiple R-squared: 0.1806, Adjusted R-squared: 0.1788
## F-statistic: 99.86 on 6 and 2718 DF, p-value: < 2.2e-16
```

R-squared >> 0 is observed in every regression => first criterion is met.

2. Check if errors and instruments are uncorrelated.

```
resid_sev1<-resid(IV_sev1)</pre>
lm_resid_sev1<-lm(resid_sev1~black+ durat+ narr86+ nfarr86+ nparr86+ ptime86, data=df)</pre>
summary(lm_resid_sev1)
##
## Call:
## lm(formula = resid_sev1 ~ black + durat + narr86 + nfarr86 +
##
      nparr86 + ptime86, data = df)
##
## Residuals:
       Min
                  1Q Median
                                    3Q
## -11.7167 -0.1842 -0.0872 0.0257 21.8264
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
                           0.032882 -0.121
## (Intercept) -0.003974
                                               0.904
                0.001268
                           0.072489
                                     0.017
                                               0.986
## black
                                               0.847
## durat
               0.001107
                           0.005722
                                    0.193
                           0.054592
                                     0.865
                                               0.387
## narr86
               0.047213
## nfarr86
               -0.017087
                           0.078673 -0.217
                                               0.828
               -0.102002
                           0.074083 -1.377
                                               0.169
## nparr86
## ptime86
               -0.002650
                           0.013456 -0.197
                                               0.844
## Residual standard error: 1.364 on 2718 degrees of freedom
```



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```
## Multiple R-squared: 0.0008356, Adjusted R-squared: -0.00137 ## F-statistic: 0.3789 on 6 and 2718 DF, p-value: 0.8929
```

A really small R-squared is observed. The p-values of variables are considerably higher than 0.05 significance level.

What can be done in addition is a test on  $n^*R^{2}$  , where  $R^{2}$  is the non-centered  $R^{2}$  (\$  $R^{2}$  used)

```
summary(lm_resid_sev1)$r.squared*length(resid_sev1)
```

```
## [1] 2.2771
```

Value is smaller than the Chi-square value on 2 df and 0.05 significance level=> also the second criterion is met.

## PART 2

Building a model, which aims at estimating probability of arrest during 1986. A dependend binory variable, describing the states: arrested and not arrested, is to be regressed.

In this part we test the hypothesis that every single regressor has a significant impact on the dependend variable.

## Simple OLS Regression, LPM

## OLS estimation of the variable narr86

Regressing the variable narr86 on almost all variables

```
##
## Call:
## lm(formula = narr86 ~ pcnv + avgsen + tottime + ptime86 + qemp86 +
      inc86 + durat + black + hispan + born60 + pcnvsq + pt86sq +
##
##
      inc86sq, data = df)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -1.5542 -0.4622 -0.2097 0.2374 11.3955
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 5.618e-01 4.481e-02 12.537 < 2e-16 ***
                                      3.697 0.000222 ***
               5.710e-01 1.544e-01
## pcnv
## avgsen
              -1.708e-02
                          1.205e-02
                                     -1.418 0.156417
               1.203e-02 9.277e-03
## tottime
                                     1.297 0.194806
               2.936e-01 4.432e-02
## ptime86
                                    6.624 4.19e-11 ***
## qemp86
              -2.706e-02 1.840e-02 -1.471 0.141512
              -3.348e-03 8.048e-04 -4.160 3.28e-05 ***
## inc86
              -7.652e-03 3.962e-03 -1.931 0.053535 .
## durat
## black
               2.936e-01 4.481e-02 6.551 6.80e-11 ***
```



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```
1.616e-01 3.944e-02
                                    4.098 4.29e-05 ***
## hispan
## born60
              -3.767e-02 3.278e-02 -1.149 0.250623
              -7.488e-01 1.563e-01 -4.792 1.74e-06 ***
## pcnvsq
              -3.044e-02 3.879e-03 -7.846 6.12e-15 ***
## pt86sq
## inc86sq
               7.148e-06 2.555e-06
                                    2.798 0.005178 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.8146 on 2711 degrees of freedom
## Multiple R-squared: 0.1051, Adjusted R-squared: 0.1008
## F-statistic: 24.5 on 13 and 2711 DF, p-value: < 2.2e-16
```

We will proceed our estimations ommitting insignificant variables from this estimation.

## The Chosen Model:

After omitting the insignificant variables, we create the following model:

```
narr86 = \beta_0 + \beta_1 \ pcnv + \beta_2 \ ptime86 + \beta_3 \ inc86 + \beta_4 \ black + \beta_5 \ hispan + \beta_6 \ pcnvsq + \beta_7 \ pt86sq + \beta_8 \ inc86sq
```

```
##
## Call:
## lm(formula = narr86 ~ pcnv + ptime86 + inc86 + black + hispan +
##
      pcnvsq + pt86sq + inc86sq, data = df)
##
## Residuals:
##
               1Q Median
                               3Q
                                      Max
## -1.5498 -0.4692 -0.2159 0.2309 11.4326
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 4.896e-01 3.227e-02 15.173 < 2e-16 ***
## pcnv
               5.500e-01 1.533e-01
                                      3.587 0.00034 ***
## ptime86
               2.880e-01 4.388e-02
                                      6.563 6.30e-11 ***
## inc86
              -3.906e-03 5.257e-04 -7.430 1.45e-13 ***
## black
              2.908e-01 4.464e-02 6.514 8.71e-11 ***
## hispan
              1.623e-01 3.938e-02 4.120 3.89e-05 ***
## pcnvsq
              -7.286e-01 1.552e-01 -4.695 2.80e-06 ***
## pt86sq
              -2.946e-02 3.850e-03 -7.652 2.72e-14 ***
## inc86sq
              8.377e-06 2.096e-06 3.996 6.60e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.815 on 2716 degrees of freedom
## Multiple R-squared: 0.1026, Adjusted R-squared: 0.09991
## F-statistic: 38.8 on 8 and 2716 DF, p-value: < 2.2e-16
## [1] "Robust Standard Errors"
## t test of coefficients:
```



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```
##
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.8963e-01 3.1484e-02 15.5517 < 2.2e-16 ***
               5.4998e-01 1.6713e-01 3.2908 0.001012 **
## pcnv
               2.8797e-01 6.9228e-02 4.1597 3.286e-05 ***
## ptime86
## inc86
              -3.9062e-03 4.6991e-04 -8.3126 < 2.2e-16 ***
## black
              2.9076e-01 5.7624e-02 5.0457 4.816e-07 ***
## hispan
              1.6227e-01 3.9962e-02 4.0606 5.034e-05 ***
              -7.2855e-01 1.6900e-01 -4.3109 1.684e-05 ***
## pcnvsq
## pt86sq
              -2.9464e-02 5.8454e-03 -5.0405 4.948e-07 ***
## inc86sq
               8.3771e-06 1.7314e-06 4.8384 1.382e-06 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Interpretation: First to notice is the neglection of parameter restrictions: E.g. negative values cannot easily be interpreted in this scenario.

Although OLS yields unbiased estimators, heteroskedasticity among other things leads to inefficient ones.

Additionally: Errors also not normal

## LOGIT model

We are creating a binary variable arr86, when a person gets arrested at least once. Define: arr86 = 1 if arrested in 1986 arr86 = 0 if not arrested in 1986

```
df$arr86 <- ifelse(df$narr86>0 ,1 ,0)
```

We create a Logit-Model with all variables

```
log_all <- glm(arr86 ~ pcnv + avgsen + tottime + ptime86 + qemp86 + inc86 + durat + black + hispan + box
summary(log_all)</pre>
```

```
##
## Call:
  glm(formula = arr86 ~ pcnv + avgsen + tottime + ptime86 + qemp86 +
##
       inc86 + durat + black + hispan + born60 + pcnvsq + pt86sq +
##
       inc86sq, family = binomial(link = "logit"), data = df)
##
## Deviance Residuals:
##
       Min
                 1Q
                     Median
                                  3Q
                                          Max
## -2.1656 -0.8658 -0.5644
                              1.1201
                                        2.6271
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -7.302e-01 1.225e-01 -5.960 2.53e-09 ***
## pcnv
               4.390e-01 4.348e-01
                                     1.010 0.312619
## avgsen
               2.614e-02 4.384e-02
                                      0.596 0.550956
               -3.245e-02 3.562e-02 -0.911 0.362387
## tottime
               1.263e+00 2.523e-01 5.007 5.52e-07 ***
## ptime86
## qemp86
               1.373e-01 5.144e-02
                                      2.669 0.007607 **
              -1.448e-02 2.471e-03 -5.860 4.63e-09 ***
## inc86
```



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1.235e-02 1.039e-02 1.189 0.234550

## Signif. codes: 0 '\*\*\* 0.001 '\*\* 0.01 '\* 0.05 '.' 0.1 ' 1

7.322e-01 1.209e-01 6.058 1.38e-09 \*\*\*

## durat

## black

```
## hispan
                                4.386e-01 1.129e-01 3.886 0.000102 ***
                                -1.587e-02 9.635e-02 -0.165 0.869192
## born60
## pcnvsq
                                -1.552e+00 4.618e-01 -3.361 0.000776 ***
                                -1.742e-01 3.911e-02 -4.453 8.48e-06 ***
## pt86sq
## inc86sa
                                2.468e-05 8.186e-06 3.015 0.002570 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
               Null deviance: 3216.4 on 2724 degrees of freedom
## Residual deviance: 2871.9 on 2711 degrees of freedom
## AIC: 2899.9
##
## Number of Fisher Scoring iterations: 8
Pr(arr86=1|X) = \frac{exp(\beta_0+\beta_1\ pcnv+\beta_2\ ptime86+\beta_3\ inc86+\beta_4\ black+\beta_5\ hispan+\beta_6\ pcnvsq+\beta_7\ pt86sq+\beta_8\ inc86+\beta_4\ black+\beta_5\ hispan+\beta_6\ pcnvsq+\beta_7\ pt86sq+\beta_8\ inc86+\beta_4\ black+\beta_5\ hispan+\beta_6\ pcnvsq+\beta_7\ pt86sq+\beta_8\ inc86+\beta_8\ inc86+\beta_8\ hispan+\beta_6\ pcnvsq+\beta_7\ pt86sq+\beta_8\ inc86+\beta_8\ inc86+\beta_8\ hispan+\beta_6\ pcnvsq+\beta_7\ pt86sq+\beta_8\ hispan+\beta_8\ 
log <- glm(arr86 ~ ptime86 + qemp86 + inc86 + black + hispan + pcnvsq + pt86sq + inc86sq , data = df
summary(log)
##
## Call:
## glm(formula = arr86 ~ ptime86 + qemp86 + inc86 + black + hispan +
               pcnvsq + pt86sq + inc86sq, family = binomial(link = "logit"),
               data = df
##
##
## Deviance Residuals:
              \mathtt{Min}
                         1Q
                                              Median
                                                                             3Q
                                                                                               Max
## -2.1653 -0.8654 -0.5673 1.1359
                                                                                        2.6267
##
## Coefficients:
                                     Estimate Std. Error z value Pr(>|z|)
## (Intercept) -6.312e-01 9.372e-02 -6.735 1.64e-11 ***
                               1.251e+00 2.467e-01 5.070 3.97e-07 ***
## ptime86
## qemp86
                                1.175e-01 4.857e-02 2.420
                                                                                                       0.0155 *
## inc86
                                -1.458e-02 2.459e-03 -5.929 3.05e-09 ***
                                  7.297e-01 1.202e-01 6.073 1.26e-09 ***
## black
## hispan
                                 4.471e-01 1.116e-01 4.008 6.13e-05 ***
## pcnvsq
                              -1.114e+00 1.379e-01 -8.079 6.55e-16 ***
                               -1.733e-01 3.847e-02 -4.504 6.67e-06 ***
## pt86sq
## inc86sq
                                 2.480e-05 8.170e-06 3.036
                                                                                                   0.0024 **
## ---
```



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```
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 3216.4 on 2724 degrees of freedom
## Residual deviance: 2875.7 on 2716 degrees of freedom
## AIC: 2893.7
##
## Number of Fisher Scoring iterations: 8
For comparison a Probit-Model with same regressors is given:
prob <- glm(arr86 ~ ptime86 + qemp86 + inc86 + black + hispan + pcnvsq + pt86sq + inc86sq , data = d
summary(prob)
##
## Call:
## glm(formula = arr86 ~ ptime86 + qemp86 + inc86 + black + hispan +
      pcnvsq + pt86sq + inc86sq, family = binomial(link = "probit"),
##
      data = df)
##
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                  3Q
                                          Max
## -2.1724 -0.8682 -0.5697
                              1.1467
                                       2.7138
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -3.917e-01 5.648e-02 -6.936 4.04e-12 ***
               7.387e-01 1.400e-01 5.278 1.31e-07 ***
## ptime86
## qemp86
              6.771e-02 2.898e-02
                                     2.337 0.01944 *
## inc86
              -8.503e-03 1.417e-03 -6.001 1.96e-09 ***
## black
              4.373e-01 7.299e-02 5.992 2.08e-09 ***
## hispan
              2.615e-01 6.643e-02
                                      3.936 8.28e-05 ***
              -6.503e-01 7.687e-02 -8.461 < 2e-16 ***
## pcnvsq
## pt86sq
              -1.021e-01 2.183e-02 -4.676 2.93e-06 ***
              1.520e-05 4.623e-06 3.287 0.00101 **
## inc86sq
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 3216.4 on 2724 degrees of freedom
## Residual deviance: 2876.2 on 2716 degrees of freedom
## AIC: 2894.2
##
## Number of Fisher Scoring iterations: 8
```

#### Models diagnostics

## Calculation of MC Faddens pseudo R<sup>2</sup>



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```
r_log<- 1-(log$deviance/log$null.deviance)
r_prob<- 1-(prob$deviance/prob$null.deviance)</pre>
```

MC Faddens pseudo R<sup>2</sup> for Logit is r<sub>log</sub> and for Probit it is r<sub>prob</sub>.

## Scaling of probit to logit (ptime86)

The factor between our Probit and Logit is factor\_log\_prob. And it is close to 1.6 ##Interpretation of Coefficients: Odds and Average-Marginal-Effects

```
# for logit
odds<- exp(log$coefficients)</pre>
## (Intercept) ptime86
                                            inc86
                                                                   hispan
                               qemp86
                                                        black
    0.5319334 3.4933867
##
                            1.1247170
                                       0.9855262
                                                   2.0743757
                                                                1.5637392
##
                 pt86sq
                              inc86sq
       pcnvsq
##
    0.3282620 0.8409137
                            1.0000248
fav <- mean(dnorm(predict(log,type="link")))</pre>
fav*coef(log)
##
    (Intercept)
                      ptime86
                                     qemp86
                                                    inc86
                                                                  black
## -1.391845e-01 2.758107e-01 2.591507e-02 -3.214709e-03 1.608863e-01
                                     pt86sq
                                                  inc86sq
         hispan
                       pcnvsq
## 9.857880e-02 -2.456187e-01 -3.820432e-02 5.468947e-06
```

## Classification table

```
tab <- table(true= df\sarr86, pred= ifelse(fitted(log)>0.5,1,0))
tab
       pred
##
## true
           0
                 1
      0 1883
               87
##
      1 625 130
##
TP<-tab[2,2]
FP<-tab[2,1]
FN<-tab[1,2]
TN<-tab[1,1]
accuracy=(TP+TN)/length(narr86)
specificity<-TN/(FP+TN)</pre>
sensitivity<-TP/(TP+FN)
```

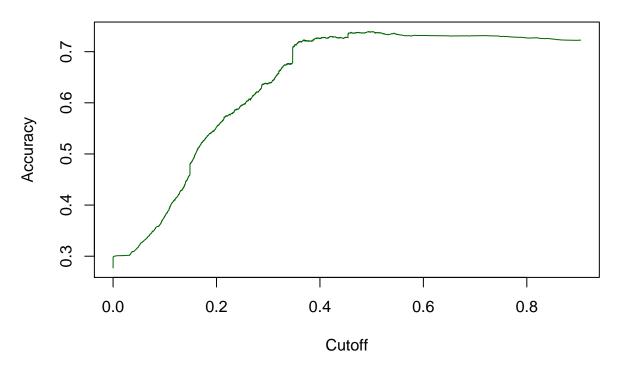
h accuracy = 0.7387156,  $h_0$  specificity = 0.7507974 and  $h_1$  sensitivity = 0.5990783



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```
pred <- prediction(fitted(log),df$arr86)
plot(performance(pred, "acc"),col="darkgreen",main="Accuracy vs. Probability cutoff")</pre>
```

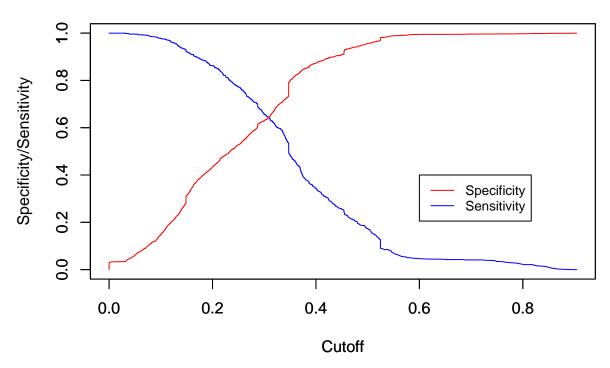
# Accuracy vs. Probability cutoff





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# Sensitivity/Specificity vs. Probability cutoff



```
# -->adjusted cutoff value ... 0.3
tab_cut <- table(true= df$arr86, pred= ifelse(fitted(log)>0.3,1,0))
tab_cut
```

```
## true 0 1
## co 1242 728
## 1 258 497
```

## ROC

```
## Warning in roc.default(response = df$narr86, predictor = predict.glm(log, :
## 'response' has more than two levels. Consider setting 'levels' explicitly or
## using 'multiclass.roc' instead

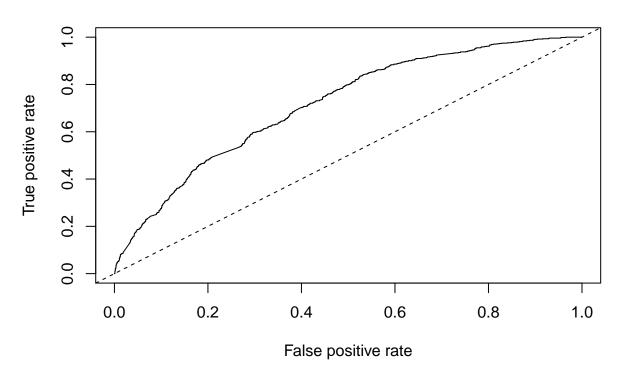
## Setting levels: control = 0, case = 1

## Setting direction: controls < cases</pre>
```



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## Area under the curve: 0.6885

The area under the ROC curve (AUC) amounts to auc\_number.

## Ordered Logit Model

```
"Excluding narr86 > 4"
```

## [1] "Excluding narr86 > 4"

```
dfn<- df %>%
  subset(df$narr<4)
head(dfn)</pre>
```

##		narr86	nfarr86	nparr86	pcnv	avgsen	tottime	ptime86	qemp86	inc86	durat	black
##	1	0	0	0	0.38	17.6	35.2	12	0	0.0	0	0
##	2	2	2	0	0.44	0.0	0.0	0	1	0.8	0	0
##	3	1	1	0	0.33	22.8	22.8	0	0	0.0	11	1
##	4	2	2	1	0.25	0.0	0.0	5	2	8.8	0	0
##	5	1	1	0	0.00	0.0	0.0	0	2	8.1	1	0
##	6	0	0	0	1.00	0.0	0.0	0	4	97.6	0	0
##		hispan born60 pcnvsq pt86sq		inc86sq arr86		36						
##	1	0	1 (	0.1444	144	0.00	000	0				
##	2	1	0 (	0.1936	0	0.64	000	1				
##	3	0	1 (	0.1089	0	0.00	000	1				



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```
## 4
         1
                1 0.0625
                            25 77.44000
                0 0.0000 0 65.61001
## 5
         0
                                             1
## 6
         0
                1 1.0000
                            0 9525.75977
results.olog<-oglmx(narr86 ~ 0 + ptime86 + qemp86 + inc86 + black + hispan + pcnvsq + pt86sq + inc86s
                    delta=0,threshparam = NULL)
summary(results.olog)
## Ordered Logit Regression
## Log-Likelihood: -1879.718
## No. Iterations: 7
## McFadden's R2: 0.08034072
## AIC: 3781.436
##
             Estimate Std. error t value Pr(>|t|)
## ptime86 1.2034e+00 2.1007e-01 5.7286 1.013e-08 ***
## qemp86 1.1647e-01 4.7887e-02 2.4323 0.015004 *
## inc86 -1.4482e-02 2.4354e-03 -5.9463 2.742e-09 ***
           7.1837e-01 1.1827e-01 6.0740 1.248e-09 ***
## black
## hispan 4.6009e-01 1.1109e-01 4.1415 3.450e-05 ***
## pcnvsq -1.0727e+00 1.3805e-01 -7.7702 7.837e-15 ***
## pt86sq -1.6925e-01 3.4249e-02 -4.9418 7.742e-07 ***
## inc86sq 2.4796e-05 8.1111e-06 3.0570 0.002236 **
## ---- Threshold Parameters ----
                   Estimate Std. error t value Pr(>|t|)
##
## Threshold (0->1) 0.672784 0.094188 7.143 9.131e-13 ***
## Threshold (1->2) 2.552963  0.117131  21.796 < 2.2e-16 ***
## Threshold (2->3) 3.999906  0.178077  22.462 < 2.2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
"marginal effects"
## [1] "marginal effects"
margins.oglmx(results.olog,ascontinuous = TRUE) #treating discrete variables like continuous ones, give
## Marginal Effects on Pr(Outcome==0)
           Marg. Eff Std. error t value Pr(>|t|)
## ptime86 -2.0013e-01 2.9566e-02 -6.7690 1.297e-11 ***
## qemp86 -1.9371e-02 7.9601e-03 -2.4335 0.014954 *
           2.4084e-03 4.1095e-04 5.8606 4.611e-09 ***
## inc86
          -1.1947e-01 2.0067e-02 -5.9538 2.620e-09 ***
## black
## hispan -7.6518e-02 1.8633e-02 -4.1065 4.016e-05 ***
## pcnvsq 1.7840e-01 2.3231e-02 7.6791 1.602e-14 ***
           2.8148e-02 4.7822e-03 5.8858 3.960e-09 ***
## pt86sq
## inc86sq -4.1237e-06 1.3576e-06 -3.0375 0.002385 **
## -----
## Marginal Effects on Pr(Outcome==1)
           Marg. Eff Std. error t value Pr(>|t|)
##
## ptime86 1.5488e-01 2.4154e-02 6.4123 1.433e-10 ***
## qemp86 1.4991e-02 6.1684e-03 2.4303 0.015086 *
```

## inc86 -1.8639e-03 3.1974e-04 -5.8294 5.561e-09 \*\*\*



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```
9.2459e-02 1.5651e-02 5.9077 3.468e-09 ***
## hispan 5.9217e-02 1.4462e-02 4.0948 4.226e-05 ***
## pcnvsq -1.3806e-01 1.8168e-02 -7.5989 2.986e-14 ***
## pt86sq -2.1783e-02 3.8930e-03 -5.5955 2.200e-08 ***
## inc86sq 3.1914e-06 1.0519e-06 3.0340 0.002413 **
## -----
## Marginal Effects on Pr(Outcome==2)
           Marg. Eff Std. error t value Pr(>|t|)
## ptime86 3.3936e-02 5.2208e-03 6.5002 8.021e-11 ***
## qemp86 3.2847e-03 1.3806e-03 2.3792 0.0173512 *
## inc86 -4.0839e-04 7.9020e-05 -5.1682 2.364e-07 ***
          2.0258e-02 3.8561e-03 5.2536 1.492e-07 ***
## black
## hispan 1.2975e-02 3.3740e-03 3.8456 0.0001203 ***
## pcnvsq -3.0250e-02 4.7919e-03 -6.3128 2.740e-10 ***
## pt86sq -4.7729e-03 8.1075e-04 -5.8870 3.933e-09 ***
## inc86sq 6.9925e-07 2.3911e-07 2.9244 0.0034511 **
## -----
## Marginal Effects on Pr(Outcome==3)
           Marg. Eff Std. error t value Pr(>|t|)
## ptime86 1.1314e-02 2.1670e-03 5.2209 1.781e-07 ***
## qemp86 1.0951e-03 4.8226e-04 2.2707 0.0231675 *
## inc86 -1.3615e-04 3.1761e-05 -4.2867 1.813e-05 ***
          6.7539e-03 1.5499e-03 4.3575 1.316e-05 ***
## black
## hispan
         4.3256e-03 1.2554e-03 3.4457 0.0005696 ***
## pcnvsq -1.0085e-02 2.0714e-03 -4.8687 1.124e-06 ***
## pt86sq -1.5912e-03 3.2368e-04 -4.9160 8.833e-07 ***
## inc86sq 2.3312e-07 8.5305e-08 2.7328 0.0062807 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Alternative model with fixed thresholds (restrictions)
results.ologalt<-oglmx(narr86 ~ 0 + ptime86 + qemp86 + inc86 + black + hispan + pcnvsq + pt86sq + inc
"Unrestricted model"
## [1] "Unrestricted model"
summary(results.olog)
## Ordered Logit Regression
## Log-Likelihood: -1879.718
## No. Iterations: 7
## McFadden's R2: 0.08034072
## AIC: 3781.436
             Estimate Std. error t value Pr(>|t|)
## ptime86 1.2034e+00 2.1007e-01 5.7286 1.013e-08 ***
## qemp86 1.1647e-01 4.7887e-02 2.4323 0.015004 *
          -1.4482e-02 2.4354e-03 -5.9463 2.742e-09 ***
## inc86
           7.1837e-01 1.1827e-01 6.0740 1.248e-09 ***
## black
## hispan 4.6009e-01 1.1109e-01 4.1415 3.450e-05 ***
## pcnvsq -1.0727e+00 1.3805e-01 -7.7702 7.837e-15 ***
## pt86sq -1.6925e-01 3.4249e-02 -4.9418 7.742e-07 ***
```



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```
## inc86sq 2.4796e-05 8.1111e-06 3.0570 0.002236 **
## ---- Threshold Parameters ----
                  Estimate Std. error t value Pr(>|t|)
##
## Threshold (0->1) 0.672784 0.094188 7.143 9.131e-13 ***
## Threshold (1->2) 2.552963
                            0.117131 21.796 < 2.2e-16 ***
## Threshold (2->3) 3.999906  0.178077  22.462 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
"Alternative model with fixed thresholds"
## [1] "Alternative model with fixed thresholds"
summary(results.ologalt)
## Ordered Logit Regression
## Log-Likelihood: -1926.135
## No. Iterations: 8
## McFadden's R2: 0.05763094
## AIC: 3870.27
## ---- Mean Equation -----
           Estimate Std. error t value Pr(>|t|)
## ptime86 7.8028e-01 1.2531e-01 6.2266 4.766e-10 ***
## qemp86 1.8333e-01 2.5754e-02 7.1185 1.091e-12 ***
## inc86 -9.4246e-03 1.5021e-03 -6.2744 3.509e-10 ***
          6.4795e-01 6.5476e-02 9.8959 < 2.2e-16 ***
## black
         4.4269e-01 6.4611e-02 6.8515 7.305e-12 ***
## hispan
## pcnvsq -4.5389e-01 8.4327e-02 -5.3825 7.344e-08 ***
## pt86sg -1.0628e-01 2.0740e-02 -5.1242 2.989e-07 ***
## inc86sq 1.5782e-05 4.9918e-06 3.1615 0.001569 **
## ---- SD Equation -----
      Estimate Std. error t value Pr(>|t|)
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Likelihoodratio-Test to compare unrestricted and restricted model
library("lmtest")
lrtest(results.olog,results.ologalt)
## Likelihood ratio test
## Model 1: narr86 ~ 0 + ptime86 + qemp86 + inc86 + black + hispan + pcnvsq +
      pt86sq + inc86sq
## Model 2: narr86 ~ 0 + ptime86 + qemp86 + inc86 + black + hispan + pcnvsq +
##
      pt86sq + inc86sq
    #Df LogLik Df Chisq Pr(>Chisq)
## 1 11 -1879.7
      9 -1926.1 -2 92.834 < 2.2e-16 ***
## 2
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

