

# Development of an artificial neural network model for predicting minimum miscibility pressure in CO<sub>2</sub> flooding

Y.F. Huang<sup>a,b</sup>, G.H. Huang<sup>a,b,\*</sup>, M.Z. Dong<sup>b</sup>, G.M. Feng<sup>a,b</sup>

<sup>a</sup>Canada–China Center of Energy and Environment Research, Hunan University, Changsha 410082, China

<sup>b</sup>Faculty of Engineering, University of Regina, Regina, SK, Canada S4S 0A2

Accepted 7 June 2002

## Abstract

This paper presents the development of an artificial neural network (ANN) model for the prediction of pure and impure CO<sub>2</sub> minimum miscibility pressures (MMP) of oils. The pure CO<sub>2</sub> MMP of a reservoir fluid (live oil) is correlated with the molecular weight of C<sub>5+</sub> fraction, reservoir temperature, and concentrations of volatile (methane) and intermediate (C<sub>2</sub>–C<sub>4</sub>) fractions in the oil. The impure CO<sub>2</sub> MMP factor,  $F_{\text{imp}}$ , is predicted by correlating the concentration of contaminants (N<sub>2</sub>, C<sub>1</sub>, H<sub>2</sub>S and SO<sub>2</sub>) in CO<sub>2</sub> stream and their critical temperatures. The  $F_{\text{imp}}$  is a correction factor to the MMP of pure CO<sub>2</sub>. The advantage of using the ANN model is evaluated by comparing the measured MMP values with the predicted results from the ANN models as well as those from other statistical methods. The developed ANN models are able to reflect the impacts on CO<sub>2</sub> MMP of molecular weight of C<sub>5+</sub> fraction, reservoir temperature, and solution gas in the oil. The ANN model of impure CO<sub>2</sub> MMP factor can distinguish the effects on MMP of different contaminants in the CO<sub>2</sub> stream. It can also be used to predict the CO<sub>2</sub> MMP of a reservoir oil and the level of contaminants in the CO<sub>2</sub> stream which can be tolerated for a miscible injection.

© 2002 Elsevier Science B.V. All rights reserved.

**Keywords:** Artificial neural network; Minimum miscibility pressure; CO<sub>2</sub> flooding

## 1. Introduction

Over the last two decades, carbon dioxide injection has become the leading enhanced oil recovery (EOR) process for light oils (Grigg and Schechter, 1997). The CO<sub>2</sub> injection can prolong, by 15 to 20 years, the production life of light oil fields nearing depletion under waterflood; the method could recover 15% to

25% of the original oil in place. It also brings environmental benefits by facilitating storage of CO<sub>2</sub> in the reservoir.

In a miscible CO<sub>2</sub> flood, multiple-contact miscibility between the injected CO<sub>2</sub> and the reservoir fluid can be achieved at pressures greater than a minimum value that is referred to as minimum miscibility pressure (MMP). The MMP is the single most important parameter in designing a miscible flood. It has been recognized that the MMP for CO<sub>2</sub> in a reservoir depends on oil temperature, oil composition, and CO<sub>2</sub> purity. The latter parameter is the only one that operators can influence. Some contaminants, mainly

\* Corresponding author. Environmental Engineering Program, Faculty of Engineering, University of Regina, Regina, SK, Canada S4S 0A2. Tel.: +1-306-585-4095; fax: +1-306-585-4855.

E-mail address: [gordon.huang@uregina.ca](mailto:gordon.huang@uregina.ca) (G.H. Huang).

N<sub>2</sub> in the flue gas and CH<sub>4</sub> from the reservoir-produced gas, in CO<sub>2</sub> can either increase or reduce the CO<sub>2</sub> MMP. Since separation of CO<sub>2</sub> could be costly, reinjecting recycled CO<sub>2</sub> without removing hydrocarbon gases could make the process more attractive economically. Therefore, for a reservoir, the CO<sub>2</sub> MMP and the tolerable level of contaminants in the CO<sub>2</sub> stream are key parameters for design of a miscible CO<sub>2</sub> flood system, as well as the associated gas separation and field injection components.

Numerous empirically derived and thermodynamic models for predicting CO<sub>2</sub> MMP have been reported in the literature. Enick et al. (1988) provided a review of the related literature. Some of the empirical correlations disregarded the C<sub>1</sub> through C<sub>4</sub> fraction and were based only on the reservoir temperature and the molar weight of C<sub>5+</sub> fraction in the oil. Alston et al. (1985) offered an empirical correlation that accounts for the effect on MMP caused by solution gas present in reservoir fluids. The minimum miscibility pressure was correlated with reservoir temperature, the oil's C<sub>5+</sub> molecular weight, volatile oil fraction (CH<sub>4</sub> + N<sub>2</sub>), intermediate oil fraction (C<sub>2</sub> to C<sub>4</sub>, H<sub>2</sub>S, and CO<sub>2</sub>), and composition of the CO<sub>2</sub> stream. More recently, Zuo et al. (1993) modified the correlation derived by Johnson and Pollin (1981) by introducing two compositional parameters: the mole fractions of the light and the intermediate components in reservoir fluids. Although these two correlations account for the effect on MMP of solution gas, it was found (Dong et al., 2000) that they could not provide satisfactory prediction of MMP for reservoir oils that had high solution-gas-to-oil ratios and high volatile-component fractions. It was realized (Dong et al., 2000) that, to improve the MMP prediction accuracy, the effects of solution gas in CO<sub>2</sub> (and thus the amounts of volatile and intermediate fractions in oil) should be considered.

Among the empirical models, only those of Alston et al. (1985) and Sebastian et al. (1984) took into account the effects on CO<sub>2</sub> MMP of contaminants in the CO<sub>2</sub> stream. Results of the two models were tested, with the outcomes indicating that the effects of impurities on CO<sub>2</sub> MMP were not effectively reflected.

The development of statistical models for CO<sub>2</sub> MMP prediction has been a subject that involved extensive research efforts, resulting in many publications (Cronquist, 1978; Yellig and Metcalfe, 1980;

Mungan, 1981; Sebastian et al., 1984; Alston et al., 1985; Kovarik, 1985). However, the main concern with statistical techniques is the difficulties in satisfying many rigid assumptions that are essential for justifying their applications, such as those of sample size, linearity, and continuity. One alternative approach for system forecasting is the technique of artificial neural network (ANN) based on the theory of artificial intelligence. The massive interconnections in the ANN framework produces a large number of degrees of freedom, or fitting parameters, and thus may allow it to reflect the system's complexity more effectively than conventional statistical techniques. Recently, methods of artificial neural networks have been applied to petroleum engineering in a number of areas such as well-test analysis, well-log interpretation, reservoir characterization, and more recently, PVT and permeability studies for crude oils (Waller and Rowsell, 1994; Gharbi and Elsharkawy, 1996, 1999).

This study is an extension of the previous efforts, emphasizing on the development of an ANN model for predicting CO<sub>2</sub> MMP. The main purpose is to examine the effects of (a) solution gas in CO<sub>2</sub>, (b) amount of volatile and intermediate fractions in oil, and (c) their ratio on pure CO<sub>2</sub> MMP, through the developed ANN model. Firstly, the interrelations of pure CO<sub>2</sub> MMPs (of live oils) with (a) molecular weight of C<sub>5+</sub> fraction, (b) reservoir temperature, (c) volatile oil fraction (methane and nitrogen gas), and (d) intermediate oil fraction (C<sub>2</sub>–C<sub>4</sub> and CO<sub>2</sub>, H<sub>2</sub>S) will be analyzed, resulting in a trained ANN model; the trained model will then be used to predict CO<sub>2</sub> MMP, with the results being compared with the measured live oil MMP values reported in the literature. Secondly, the correlations between the impure CO<sub>2</sub> MMP factor ( $F_{\text{imp}}$ ) and the contaminant concentrations (for N<sub>2</sub>, C<sub>1</sub>, H<sub>2</sub>S, and SO<sub>2</sub>) in the CO<sub>2</sub> stream will be examined. The  $F_{\text{imp}}$  represents the effect on CO<sub>2</sub> MMP of contaminants in CO<sub>2</sub> stream. Lastly, the developed ANN models will be used to predict the variations of CO<sub>2</sub> MMP with MW of C<sub>5+</sub> fraction, temperature of reservoir, and contaminant contents in CO<sub>2</sub> stream. In addition, the effectiveness of the developed ANN models will be evaluated by comparing the prediction results with (a) the measured MMP levels and (b) the prediction results from other statistical models.

ANN's main difference from statistical methods is its relinquishment in terms of strict conditions for data samples and associated assumptions. This is applicable to the existing situation of data availability for impure CO<sub>2</sub> MMP factors, which is not good enough for either statistical or numerical modeling. At the same time, analytical models are advantageous over the ANN in terms of its touching the detailed mechanisms of interactions among various impact factors; at the same time, such methods' limitations are also from their attempts to specify the complicated processes by detailed mathematical formulations, since many uncertain, interactive, and dynamic system components can hardly be expressed as accurate analytical formulations. Under such a situation, ANN becomes the only usable tool for analyzing the related effects and interactions; it can be used without violating either a number of prerequisites associated with statistical models or being forced to assuming unrealistic or over-simplified system conditions that are needed for analytical simulation.

## 2. Model development

In biology, a neural network is an array of neurons in the brain that processes information from input stimuli to produce comprehensible sensations. In the computer world, a neural network is a computer architecture that resembles its operators' process numerical inputs to generate outputs that are in some way meaningful to the user. Artificial neural networks (ANNs) are characterized as computational models with particular abilities to adapt, learn, generalize, recognize, cluster, and organize data (Dayhoff, 1990). ANNs are computing tools composed of many simple interconnected elements called neurons by analogy with neurophysiology. ANNs have a unique ability of recognizing underlying relationships between input and output events. They are well suited for modeling systems with complex relationships among incomplete or noisy data sets. Petroleum engineering applications of ANNs include areas such as well-test analysis, well-log interpretation, field development, reservoir characterization, formation damage, production, and drilling.

A typical neuron is shown in Fig. 1. A neuron has two components (Dayhoff, 1990): (1) a weighted

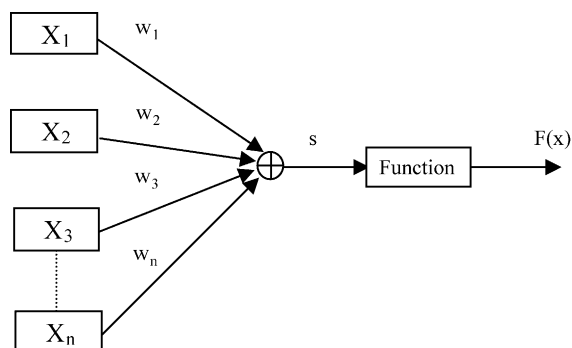


Fig. 1. Basic components of a neuron.

summer which perform a weighted summation of its inputs with components ( $X_1, X_2, X_3, \dots, X_n$ ), i.e.,  $s = \sum w_i X_i + b$ , where  $b$  is the bias of the networks; and (2) a linear, nonlinear or logic function which gives an output corresponding to  $s$ . Here, many kinds of functions can be used, including threshold (logic), sigmoid, hyperbolic tangent and Gaussian functions. In this study, each of them is examined at each neuron during the training process in order to get desired ANNs. In a typical ANN, there are three types of neurons: input neurons which may receive external data, output neurons which send data out of the ANN, and hidden neurons whose signals remain within the ANN. There are three types of layers corresponding to the types of neurons. The hidden neurons may form one or more hidden layers. The neurons in each layer are usually fully interconnected with neurons from neighboring layers. The importance of each inter-neuron connection is determined by its numerical value. A three-layered back-propagation network structure is depicted in Fig. 2 (Dayhoff, 1990). The ANN shown in Fig. 2 has an input layer, an output layer, and one hidden layer. The input layer contains an array of variables into which the input data of the system are read from an external source. Similarly, the predicted data or results, which can be multiple vectors, are written in the output layer. Initially, the input layer receives the input and passes it to the hidden layer. If more hidden layers exist, the processed information from the first hidden layer is then passed the next hidden layer for processing. Finally, the output layer receives information from the last hidden layers. In this study, the number of hidden layer is not fixed. The training tool will automatically

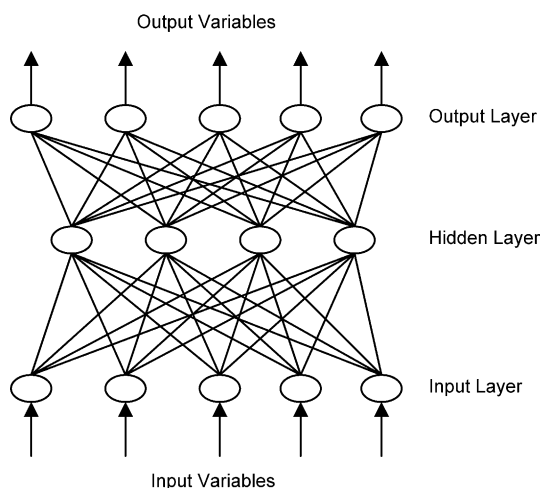


Fig. 2. A fully interconnected three-layered back-propagation network.

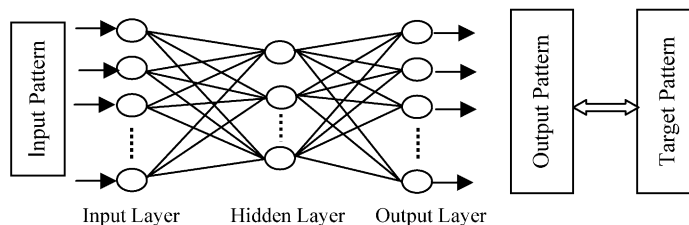
select suitable number of hidden layer to get the desired ANN model.

When an ANN is constructed, small numbers (weights) are assigned randomly to the connections between neurons. In general, the output from neural  $j$  in layer  $k$  can be calculated by the following equation:

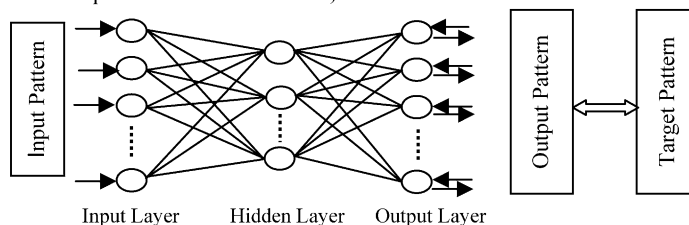
$$u_{jk} = F_k \left( \sum_{i=1}^{N_{k-1}} w_{ijk} u_{i(k-1)} + b_{jk} \right)$$

Coefficients  $w_{ijk}$  and  $b_{jk}$  are connection weight and bias of the network, respectively; they are fitting parameters of the model. The purpose is to obtain a mapping from an input vector to an output one. It is desired that the difference between the predicted and the observed (actual) values in the output vector be as small as possible. The fitting parameters are modified

- (a) Output pattern is calculated, and then compared with target pattern:



- (b) Errors are calculated for the output layer, and then incoming weights are adjusted (The arrows represent flows of information):



- (c) Errors are calculated for the hidden layer, and then the incoming weights are adjusted (Heavy lines indicate that the errors are communicated from the output layer):

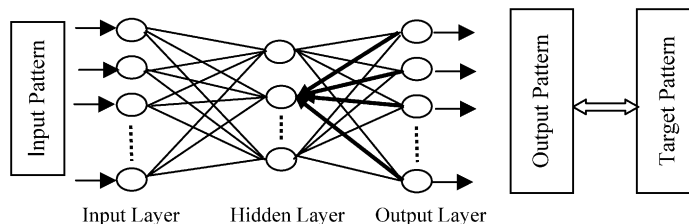


Fig. 3. Basic back-propagation dynamics.

until an error criterion between the input and the output is satisfied based on the topology of the ANN and the learning technique. The adjustment of the weights is defined as the learning process. The ANN is tested with input/output values used in training. After training and testing, the network is ready to perform tasks such as pattern recognition, classification, or function approximation. There are mainly two types of networks, feed-forward networks and recurrent networks. In this study, the back-propagation technique with momentum is used. The fitting procedure from which weights  $w_{ijk}$  are determined is performed using a least-squares minimization routine. In this routine, the sum of root-squared relative errors between the calculated and the experimental data is to be minimized. In general, the back-propagation method uses the following steps (Fig. 3):

- Read a specific input and calculate its corresponding output.
- If the error between the produced output and the desired output is acceptable, then stop.
- If the error is unacceptable in step (b), then the weights are adjusted for all of the interconnections that go into the output layer. Next, an error value is calculated for all of the units in the hidden layer that is just below the output layer. Then, the weights are adjusted for all interconnections that

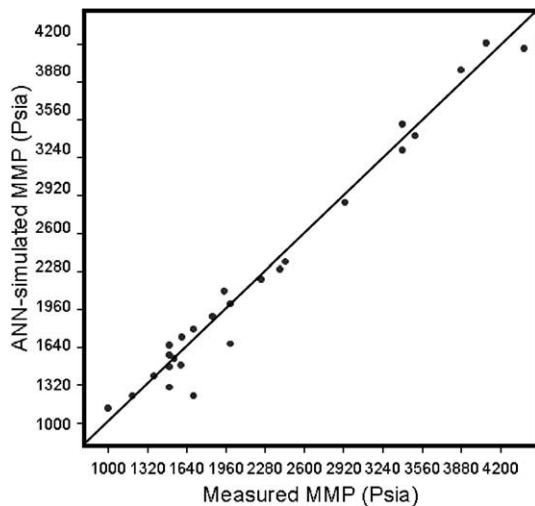


Fig. 4. The measured versus ANN-simulated MMP values (with °F for temperature).

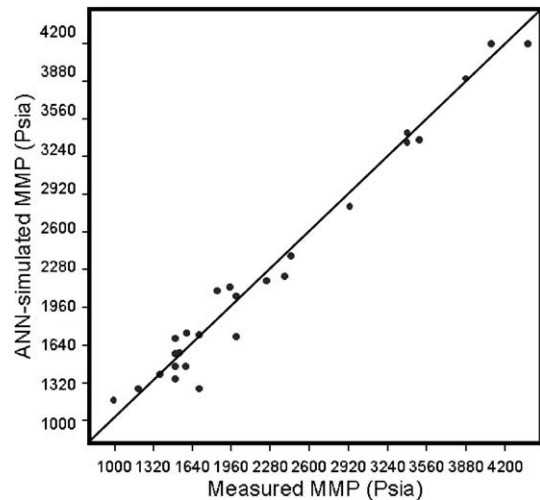


Fig. 5. The measured versus ANN-simulated MMP values (with K for temperature).

go into the hidden layer. The process is continued until the last layer of weights has been adjusted.

Typically, an application of back-propagation requires both a training set and a test set. Both the two sets contain input/output pattern pairs. While the training set is used to train the network, the test set is used to assess the performance of the network after the training is complete. To provide the best test of network performance, the test set should be different from the training set. The most successful ANN architecture is the one that has the smallest prediction error on a data set for which it was not trained. For pure CO<sub>2</sub> MMP modeling, the reservoir temperature  $T$ , molecular weight of C<sub>5+</sub>, volatile oil fraction  $X_{vol}$ , and intermediate oil fraction  $X_{int}$  are selected as input variables. Minimum miscibility pressure (MMP) is the output variable. The data used for developing the ANN model are from Jacobson (1972), Dicharry et al. (1973), Wittstrom and Hagemeyer (1978), White and Lindsay (1972), Graue and Zana (1981), Gardner et al. (1981), Frimodig et al. (1983), Cardenas et al. (1984), and Alston et al. (1985). Two scenarios of reservoir temperature are used: one with the degree Fahrenheit (°F) (Alston et al., 1985) and the other with the Kelvin (K).

For modeling the impure CO<sub>2</sub> MMP factor ( $F_{imp}$ ), the concentrations of different components in the gas

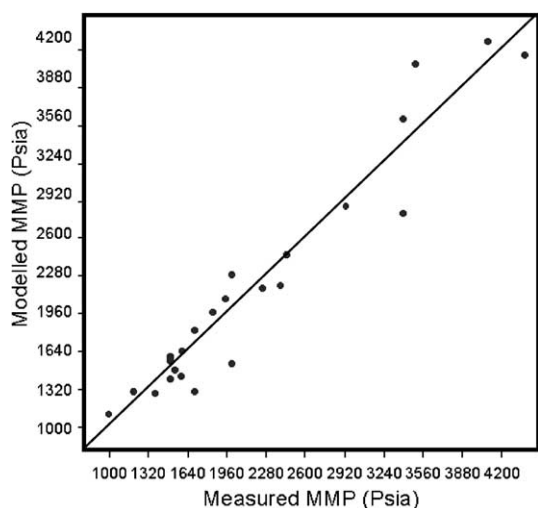


Fig. 6. The measured versus modeled MMP values (from Alston et al., 1985).

mixture ( $\text{CO}_2$  and contaminants) are used as input variables. Based on data availability and importance of the contaminants,  $\text{N}_2$ ,  $\text{CH}_4$ ,  $\text{H}_2\text{S}$ , and  $\text{SO}_2$  are selected for the modeling study; the output variable is  $F_{\text{imp}}$ . For a pure  $\text{CO}_2$  stream,  $F_{\text{imp}}$  is equal to 1. The value of  $F_{\text{imp}}$  for impure  $\text{CO}_2$  is equal to the impure  $\text{CO}_2$  MMP divided by the pure  $\text{CO}_2$  MMP of the same oil. The data used for system training are from Alston et al. (1985) and Dong (1999).

Various neural network architectures were investigated to obtain desired models for predicting pure  $\text{CO}_2$  MMP and impure factor ( $F_{\text{imp}}$ ) as a function of selected input variables. Different scenarios on the number of hidden layers, the number of neurons in each hidden layer, and the type of transfer function for each neuron are analyzed. An architecture of one or two hidden layers is initially used, followed by the selections for the number of neurons and the types of transfer functions (logic, sigmoid, or hyperbolic tan-

Table 1

Statistical analysis for calibration results from the ANN and statistical models (for MMP)

Method	Average relative error (%)	Minimum relative error (%)	Maximum relative error (%)	Standard deviation (psia)	Correlation coefficient
ANN ( $^{\circ}\text{F}$ )	5.91	0.08	27.30	157.57	0.987
ANN (K)	6.48	0.46	25.51	158.61	0.987
Statistical	8.88	0.33	23.34	290.05	0.963

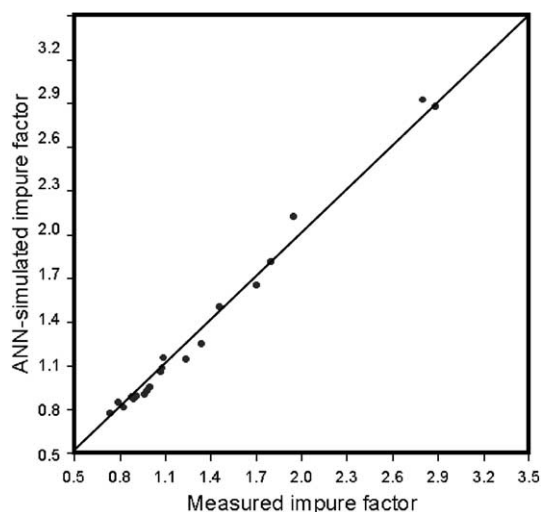


Fig. 7. The measured versus ANN-simulated impure factors.

gent), with the target of obtaining the best fit to the given data.

### 3. The training results

The scatter plots in Figs. 4–6 provide comparisons of the measured  $\text{CO}_2$  MMP levels with the ANN-derived ones as well as those provided by Alston et al. (1985) using statistical models. Figs. 4 and 5 present

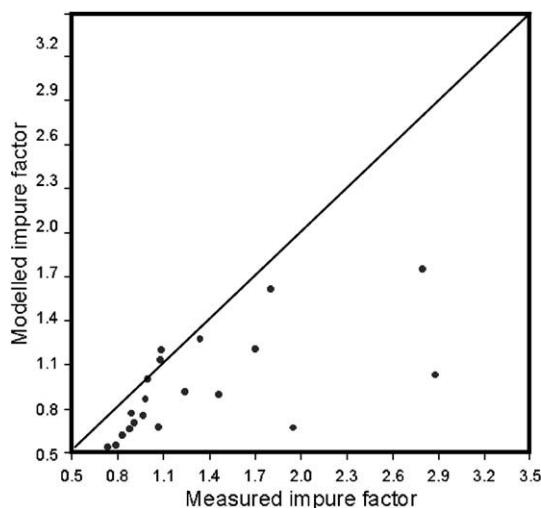


Fig. 8. The measured versus modeled impure factors (from Sebastian et al., 1984).



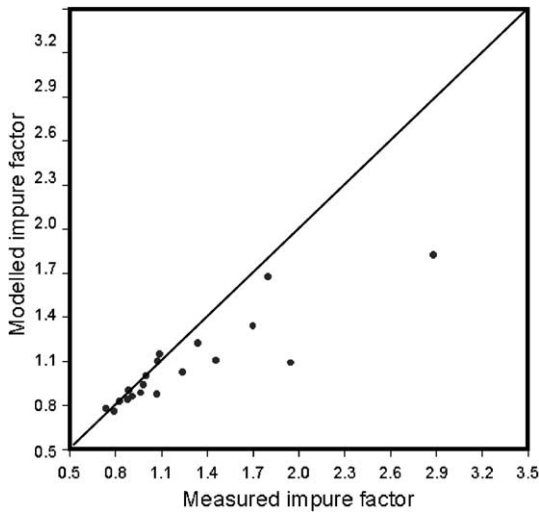


Fig. 9. The measured versus modeled impure factors (from Alston et al., 1985).

the error analysis of results with the input reservoir temperatures expressed as Fahrenheit ( $^{\circ}\text{F}$ ) and Kelvin (K), respectively. It is indicated that, when reservoir temperature is expressed in different units ( $^{\circ}\text{F}$  and K), the related ANN inputs will be different. These different input data will then result in differences in training and calibrating processes for the ANN model, leading to varied relations between the measured and the ANN-simulated MMP values. In this study, the two sets of data were used to verify each other in order to improve the model's performance. Fig. 6 shows the error levels from the model of Alston et al. (1985) based on the same data set but a different method (statistical technique). As shown, the ANN models produce much lower error levels, compared with the statistical approach (Alston et al., 1985).

Table 1 shows the outputs of statistical analyses for calibration results from the ANN and statistical models for MMP forecasting. It is indicated that the developed ANN models have lower calibration errors

than those developed by Alston et al. (1985). In detail, for the ANN model, the calibrated relative errors are 5.91% for  $^{\circ}\text{F}$  and 6.48% for K, and the correlation coefficients are both 0.987. In comparison, for the statistical model (Alston et al., 1985), the calibrated relative error is 8.88%, and the correlation coefficient is 0.963.

The scatter plots as shown in Figs. 7–9 provide comparisons of the measured impure factor ( $F_{\text{imp}}$ ) values with the ANN-derived ones as well as those provided by Sebastian et al. (1984) and Alston et al. (1985) based on the same data set but different statistical models. Much lower error levels were encountered from the results of the ANN model, compared with those of statistical approaches (Sebastian et al., 1984; Alston et al., 1985). Table 2 shows the outputs of statistical analyses for calibration results from the ANN and statistical models for impure factor ( $F_{\text{imp}}$ ) forecasting. It is indicated that the developed ANN model has lower calibration errors than those developed by Sebastian et al. (1984) and Alston et al. (1985).

#### 4. Application to MMP and $F_{\text{imp}}$ forecasting

After the ANN models were established, they could then be used for MMP and  $F_{\text{imp}}$  forecasting under a variety of conditions. With measured data sets that were not used for training, the modeling outputs could then be compared with measured values to verify the model's accuracy. The data from Rhuma (1992) were used to validate the accuracy of ANN outputs for pure  $\text{CO}_2$  MMP. ANN verifications for  $F_{\text{imp}}$  predictions were not conducted due to data unavailability. The following applications of ANN for  $F_{\text{imp}}$  forecasting were based on an assumption that its accuracy is comparable to that of MMP forecasting.

The predicted results of pure  $\text{CO}_2$  MMP are showed in Figs. 10–12. Among them, Figs. 10

Table 2  
Statistical analysis for calibration results from the ANN and statistical models (for impure factor)

Method	Average relative error (%)	Minimum relative error (%)	Maximum relative error (%)	Standard deviation	Correlation coefficient
ANN	3.83	0.12	8.87	0.07	0.99
Statistical (Alston et al.)	13.25	0.16	44.14	0.45	0.80
Statistical (Sebastian et al.)	25.25	0	65.68	0.62	0.63

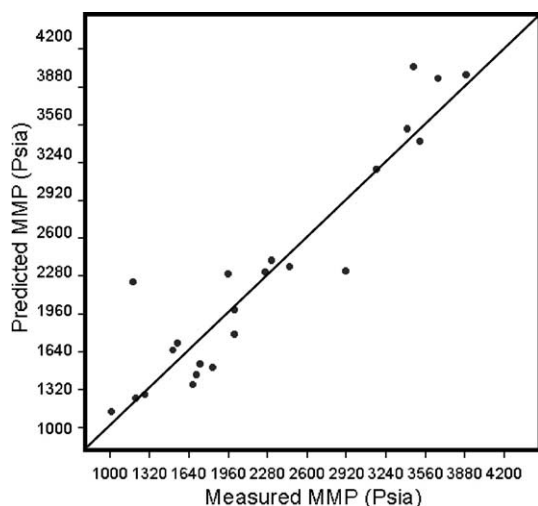


Fig. 10. The measured versus ANN-predicted MMP values (with °F for temperature).

and 11 are the prediction results of MMP obtained from ANN models under different reservoir temperatures (°F and K); Fig. 12 shows the results from Alston et al. (1985) using statistical methods. As shown, higher prediction accuracies were obtained by the ANN models, compared with those by statistical approaches.

Table 3 shows the results of error analyses for prediction outputs from the developed ANNs and the

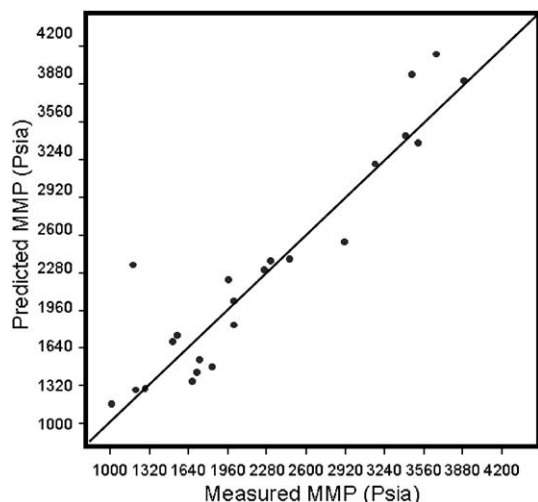


Fig. 11. The measured versus ANN-predicted MMP values (with K for temperature).

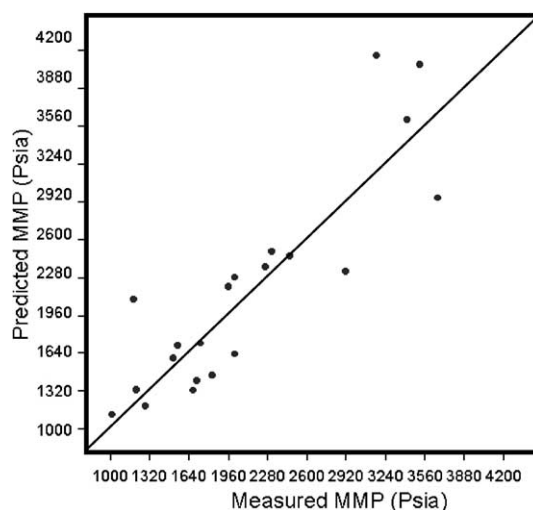


Fig. 12. The measured versus statistically predicted MMP values (from Alston et al., 1985).

statistical models of Alston et al. (1985). It is indicated that outputs from the ANNs are more accurate than those from the models of Alston et al. (1985). Compared with the calibration results as shown in Table 1, the relative errors and standard deviations become higher, while the correlation coefficients are lower. In detail, the average relative errors are 12.08% for °F and 12.32% for K, and correlation coefficients are 0.936 for °F and 0.939 for K. However, the accuracy and correlation level are still much higher than those of statistical models (relative error=17.05%, and correlation=0.896).

With the developed ANNs models for MMP and  $F_{imp}$  forecasting, we can further study the variations of MMP under different reservoir temperatures,  $C_5+$  molecular weights, volatile oil fractions, and intermediate oil fractions. According to Alston et al. (1985), if the volatile oil fraction and intermediate oil fraction vary at the same rate, the MMP will remain constant. This is because the ratio of volatile oil fraction to intermediate

Table 3  
Error analysis for prediction outputs

Method	Average relative error (%)	Minimum relative error (%)	Maximum relative error (%)	Standard deviation (psia)	Correlation coefficient
ANN (°F)	12.08	0.51	86.88	333.31	0.936
ANN (K)	12.32	0.09	96.83	337.32	0.939
Statistical	17.05	0.29	76.24	552.21	0.896



oil fraction is constant, even though the contents of solution gas are changing. In the real field, however, MMP will change even when the volatile oil fraction and the intermediate oil fraction vary at the same rate. In this study, the base points for the contents of solution gas are selected as  $X_{vol} = 16.09\%$  and  $X_{int} = 19.68\%$ . Thus, the contents of solution gas will then increase with increments of 2%, 4%, ..., of the base points. In this way, the ratio of volatile oil fraction to intermediate oil fraction will keep to be a constant, while the contents of solution gas are changing dynamically. Using the developed ANN model, variations of MMP under given reservoir temperature and  $C_{5+}$  molecular weight but varying contents of solution gas can be examined.

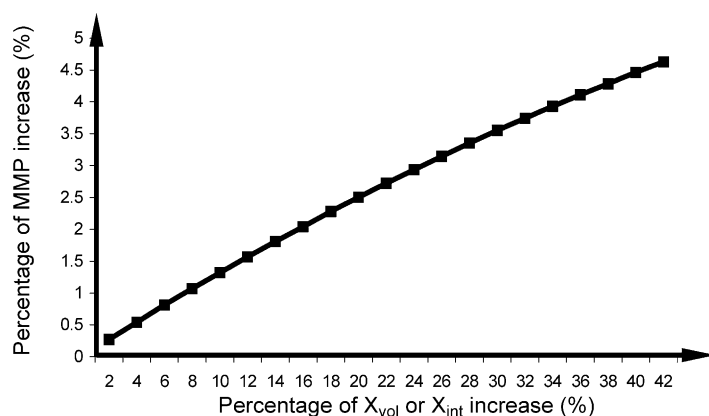
In general, MMP will be constant if effect of volatile-oil-fraction variation is the same as that of intermediate-oil-fraction variation. However, as shown in Fig. 13, MMP is an increasing function of the mole fractions of volatile oil and intermediate oil, even though  $X_{vol}/X_{int}$  is a constant. This indicates that the effect of  $X_{vol}$  variation is greater than that of  $X_{int}$  variation; conversely, if MMP was a decreasing function, the effect of  $X_{int}$  would be greater than that of  $X_{vol}$ . This result is consistent with the experimental results from Dong (1999).

Through the developed ANN models, variations of  $CO_2$  MMP under different reservoir temperatures and  $C_{5+}$  molecular weights can be examined, with the

volatile oil fraction ( $X_{vol}$ ) and the intermediate oil fraction ( $X_{int}$ ) being fixed at 10.5% and 14.28%, respectively. Figs. 14 and 15 show that the MMPs increase with reservoir temperature and  $C_{5+}$  molecular weight. The relation between MMP and reservoir temperature is close to linear when the level of  $C_{5+}$  molecular weight is high. For many reservoir oils with nearly equal values of volatile and intermediate fractions, the developed ANNs can be used to quantify the relation between  $CO_2$  MMP and reservoir temperature under different  $C_{5+}$  molecular weights, such that forecasting of  $CO_2$  MMP becomes possible.

It is generally recognized that the effect of an impurity (or contaminant) on  $CO_2$  MMP depends on whether the impurity can enhance the  $CO_2$ 's solubility. This idea of the solubility was used to estimate the effects of impurities on  $CO_2$  MMP by Alston et al. (1985) and Sebastian et al. (1984), where they incorporated an average critical temperature of the gas mixture within the correlations. It was indicated that solvency could be improved if  $CO_2$  was diluted with an impurity whose critical temperature was higher than that of  $CO_2$ . However, the solvency deteriorated if  $CO_2$  was diluted with an impurity with a lower critical temperature. In general, the effects of  $H_2S$  and  $SO_2$  on MMP are less dramatic than those of  $CH_4$  and  $N_2$ .

Fig. 7 shows an excellent agreement between predicted and measured  $F_{imp}$  values. Thus, the



Note: (1) The base points of volatile and intermediate oil fractions are:  $X_{vol} = 16.09\%$  and  $X_{int} = 19.68\%$ ;

(2) The percentage of  $X_{vol}$  increase = the percentage of  $X_{int}$  increase.

Fig. 13. Variations of MMP with solution-gas contents (at  $T = 316$  K and  $M_{C_{5+}} = 196.1$ ).

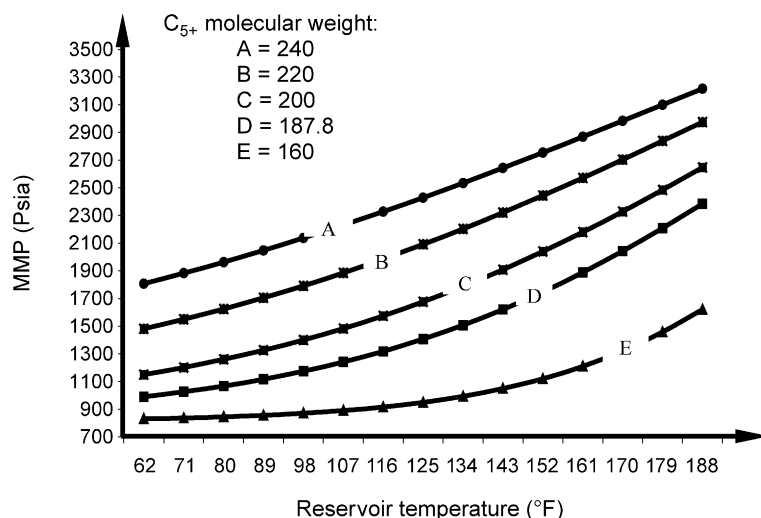


Fig. 14. Variations of MMP with temperature and  $C_{5+}$  molecular weight (at  $X_{\text{int}} = 10.5\%$  and  $X_{\text{vol}} = 14.28\%$ ) (with °F for temperature).

effects of each impurity ( $N_2$ ,  $C_1$ ,  $H_2S$  or  $SO_2$ ) in the  $CO_2$  stream on the MMP can be examined by simulating  $F_{\text{imp}}$  levels under different mole fractions using the developed ANN model. The results are shown in Fig. 16, indicating that  $N_2$  has the most significant effect; a small variation in  $N_2$  content could result in a great fluctuation in  $CO_2$  MMP level. The content of  $C_1$  is also an increasing function of  $CO_2$  MMP level, with a less significant effect. In comparison, the contents of  $H_2S$  and  $SO_2$

are slightly decreasing functions of MMP. Therefore,  $N_2$  is the most important impurity which should be well considered before the recycled  $CO_2$  is reinjected.

In Fig. 16, MMP is an increasing function of  $N_2$  concentration. The MMP increases rapidly when the  $N_2$  concentration is between 4% and 9%. Thus, keeping  $N_2$  concentration lower than 4% would be a desired strategy. Attempts to reduce  $N_2$  concentration to lower than 4% could lead to low efficiencies and

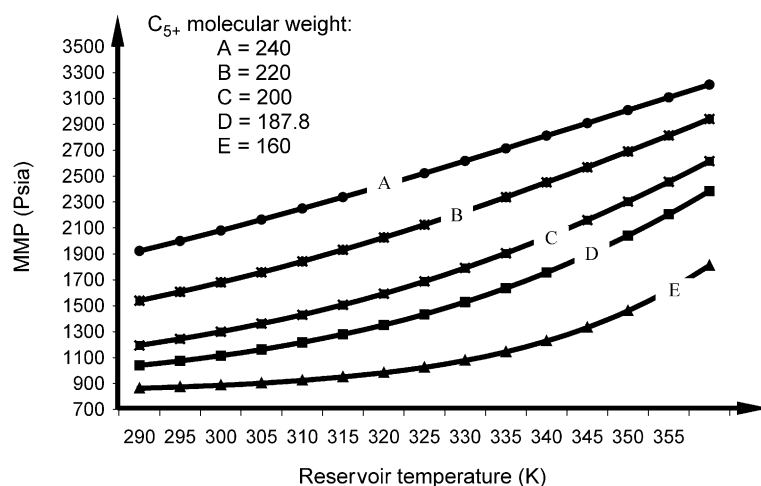


Fig. 15. Variations of MMP with temperature and  $C_{5+}$  molecular weight (at  $X_{\text{int}} = 10.5\%$  and  $X_{\text{vol}} = 14.28\%$ ) (with K for temperature).

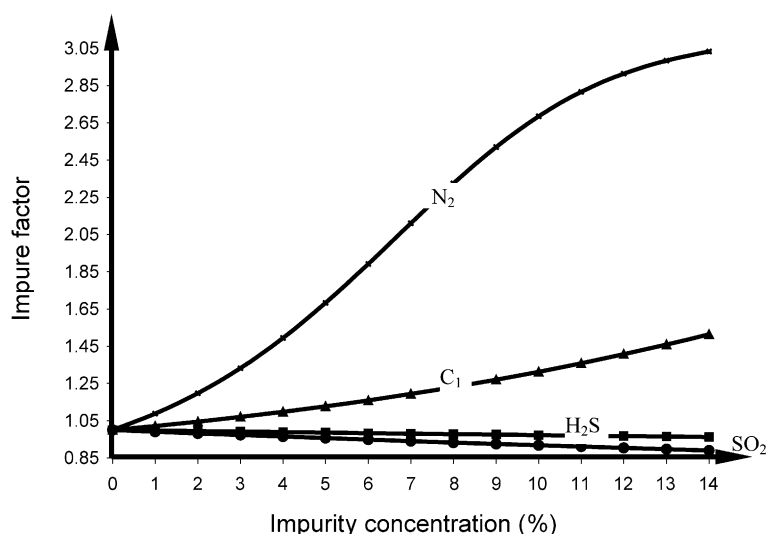


Fig. 16. The predicted values of impure factor as functions of impurity concentrations.

high costs. This information is important for determining the desired removal rate of N<sub>2</sub> in the recycled CO<sub>2</sub> stream.

## 5. Discussion

Conventional pressure, volume and temperature (PVT) simulation techniques can directly address complexities associated with factors that affect the MMP level. However, such simulation efforts often suffer from problems of data unavailability for specifying complicated state equations and quantifying interrelationships among various system components. This might lead to over simplification of the related processes and thus reduced prediction accuracy. On the other hand, although statistical models have lower requirements in terms of data availability, the associated difficulties in satisfying many rigid assumptions that are essential for justifying their applications have affected their performances.

In this study, the ANN approach is for the first time used to predict MMP and  $F_{\text{imp}}$ . The results demonstrate that, under conditions with limited field information, the ANN approach could produce a higher accuracy than statistical models.

Prediction of CO<sub>2</sub> MMP is critical for CO<sub>2</sub> flooding in enhanced oil recovery processes. An

inaccurate prediction may result in significant consequences. For example, recommendation for a too high operating level of MMP may result in greatly inflated operation costs as well as occupational health concerns. On the other hand, if the suggested MMP is too low, the miscible displacement process would become ineffective, leading to a high risk of system failure. Thus, a higher prediction accuracy would bring significant economic benefits.

In the last few years, more and more attentions have been paid on the use of recycled CO<sub>2</sub> for enhanced oil recovery, because of the worldwide concern on the issue of greenhouse gas emissions. In the recycled CO<sub>2</sub> stream, however, a variety of impurities exist and may significantly affect the MMP. At the same time, it is costly to purify the CO<sub>2</sub> stream. Therefore, identification of a suitable level of impurity removal rate (and thus a suitable level of impurity contents in the CO<sub>2</sub> stream which can be tolerated for miscible injections) is desired. The developed ANN model for  $F_{\text{imp}}$  forecasting can supply such information in terms of the relations between  $F_{\text{imp}}$  levels and impurity contents in the CO<sub>2</sub> stream, and thus help to identify an optimum removal rate. Thus, the chance of economic losses due to either unnecessarily too high removal rate (and thus an increased operating costs) or too low rate (and thus a raised risk of inflated MMP) can be minimized.

## 6. Conclusions

In this study, ANN models for predicting CO<sub>2</sub> minimum miscibility pressures (MMP) and impure CO<sub>2</sub> MMP factor ( $F_{\text{imp}}$ ) have been developed. The interrelations of CO<sub>2</sub> MMPs with molecular weight of C<sub>5+</sub> fraction, reservoir temperature, volatile oil fraction, and intermediate oil fraction have been analyzed, resulting in a trained ANN model. Moreover, correlations between the impure CO<sub>2</sub> MMP factor ( $F_{\text{imp}}$ ) and the contaminant concentrations in the CO<sub>2</sub> stream have been examined. The developed ANN models have been used then to predict the variations of CO<sub>2</sub> MMP with MW of C<sub>5+</sub> fraction, temperature of reservoir, and contaminant contents in CO<sub>2</sub> stream. The effectiveness of the developed ANN models was also evaluated by comparing its prediction results with measured MMP levels and prediction results from other statistical models. The modeling results indicate that reasonable predictions have been generated. Especially, under conditions with limited field information, the ANN approach could produce a higher accuracy than statistical models.

In this study, the ANN approach is for the first time used to predict MMP and  $F_{\text{imp}}$ . With the increased prediction accuracy, the developed models can help to identify the desired operating levels of MMP and the suitable levels of impurity removal rates in enhanced oil recovery processes. Pool operators can thus optimize the injection gas to improve the process economics. This provision of effective decision support would bring tremendous economic efficiencies for oil industries. In practical applications of the model, continuous updates of the modeling system are recommended as long as new field operation data become available. The developed ANN models are user-friendly and can be easily utilized by engineers in petroleum industry.

The ANN method has been utilized in a number of applications in petroleum industry. This study is an extension of the previous efforts. It is the first attempt in using ANN to facilitate forecasting of CO<sub>2</sub> minimum miscibility pressures (MMP) and impure CO<sub>2</sub> MMP factors. When applying the ANN to this new area, a number of innovative considerations need to be made to effectively reflect the effects of many impact factors and their interactions. For example, the interrelations of CO<sub>2</sub> MMPs with molecular weight of C<sub>5+</sub>

fraction, reservoir temperature, volatile oil fraction, and intermediate oil fraction, as well as the correlations between the impure CO<sub>2</sub> MMP factor and the contaminant concentrations in the CO<sub>2</sub> stream, have been examined through the developed ANN framework. These interrelationships could hardly be addressed through traditional approaches, while the ANN approach shows advantages in reflecting such complex uncertainty and nonlinearity.

## Acknowledgements

This research has been supported by the Natural Science and Engineering Research Council of Canada.

## References

- Alston, R.B., Kokolis, G.P., James, C.F., 1985. CO<sub>2</sub> minimum miscibility pressures: a correlation for impure CO<sub>2</sub> streams and live oil systems. *SPE J.*, 268–274 (April).
- Cardenas, R.L., et al., 1984. Laboratory design of a gravity-stable, miscible CO<sub>2</sub> process. *J. Pet. Technol.*, 111–118 (Jan.).
- Cronquist, C., 1978. Carbon dioxide dynamic miscibility with light reservoir oils. *Proc. Fourth Annual U.S. DOE Symposium*, Tulsa, vol. 1B-oil, pp. 28–30 (Aug.).
- Dayhoff, J.E., 1990. *Neural Network Architectures*, Van Nostrand-Reinhold, New York.
- Dicharry, R.M., Peryman, T.L., Ronquille, J.D., 1973. Evaluation and design of a CO<sub>2</sub> miscible flood project-SACROC unit, Kelly-Snyder field. *J. Pet. Technol.*, 1309–1318 (Nov.).
- Dong, M., 1999. Task 3—minimum miscibility pressure (MMP) studies, in the Technical Report: Potential of Greenhouse Storage and Utilization through Enhanced Oil Recovery. Petroleum Technology Research Centre, Saskatchewan Research Council (SRC Publication No. P-110-468-C-99), September.
- Dong, M., Huang, S., Srivastava, R., 2000. Effect of solution gas in oil on CO<sub>2</sub> minimum miscibility pressure. *J. Can. Pet. Technol.* 39 (11), 53–61.
- Enick, R.M., Holder, G.D., Morsi, B.I., 1988. A thermodynamic correlation for the minimum miscibility pressure in CO<sub>2</sub> flooding of petroleum reservoirs. *SPE Reservoir Engineering*, 81–92 (Feb.).
- Gardner, J.W., Orr, F.M., Patel, P.D., 1981. The effect of phase behavior on CO<sub>2</sub> flood displacement efficiency. *J. Pet. Technol.*, 2067–2081 (Nov.).
- Frimodig, J.P., Reese, N.A., Williams, C.A., 1983. Carbon dioxide flooding evaluation of high-pour-point, paraffinic red wash reservoir oil. *Soc. Pet. Eng. J.*, 587–594 (Aug.).
- Gharbi, R.B., Elsharkawy, A.M., 1996. Neural network model for estimating the PVT properties of Middle East crude oils. *In Situ* 20 (4), 367–394.

- Gharbi, R.B., Elsharkawy, A.M., 1999. Neural network model for estimating the PVT properties of Middle East crude oils. *SPE Reserv. Evalu. Eng.* 2 (3), 255–265 (June).
- Graue, D.J., Zana, E.T., 1981. Study of a possible CO<sub>2</sub> flood in rangely field. *J. Pet. Technol.*, 1312–1318 (July).
- Grigg, R.B., Schechter, D.S., 1997. State of the industry in CO<sub>2</sub> floods. SPE Paper 38849 Presented at the 1997 SPE Annual Technical Conference and Exhibition held in San Antonio, Texas, October 5–8.
- Jacobson, H.A., 1972. Acid gases and their contribution to miscibility. *J. Can. Pet. Technol.*, 56–59 (April–June).
- Johnson, J.P., Pollin, J.S., 1981. Measurement and correlation of CO<sub>2</sub> miscibility pressures. Paper SPE 9790 Presented at the 1981 SPE/DOE Enhanced Oil Recovery Symposium, Tulsa, April 5–8.
- Kovarik, F.S., 1985. A minimum miscibility pressure study using impure CO<sub>2</sub> and West Texas oil systems: data base, correlations and compositional simulation. Paper SPE 14689 Presented at the 1985 SPE Production Technology Symposium, Lubbock, Nov. 11–12.
- Mungan, N., 1981. Carbon dioxide flooding-fundamentals. *J. Can. Pet. Technol.*, 87–92 (Jan.).
- Rhuma, A.N., 1992. Minimum Miscibility Pressures of CO<sub>2</sub>/Hydrocarbon System: Evaluation of Existing Prediction Methods and Development of a New Correlation. MSc Thesis, University of Saskatchewan, Canada.
- Sebastian, H.M., Wenger, R.S., Renner, T.A., 1984. Correlation of minimum miscibility pressure for impure CO<sub>2</sub> streams. Paper SPE 12648 Presented at the 1984 SPE/DOE Enhanced Oil Recovery Symposium, Tulsa, April 15–18. *JPT* (1985), 37 (2), 268–274.
- Waller, M.D., Rowsell, P.J., 1994. Intelligent well control. *Trans. Inst. Min. Metall.* 103, 47–51.
- White, T.M., Lindsay, R.F., 1972. Enhanced oil recovery by CO<sub>2</sub> miscible displacement in the Little Knife Field, Billings County, North Dakota. Proc., 5th Annual DOE Symposium on Enhanced Oil and Gas Recovery and Improved Drilling Technology, Tulsa 2-Oil, N-5.
- Wittstrom Jr., M.D., Hagemeier, M.E., 1978. A review of Little Knife Field development, North Dakota. Proc., Williston Basin Symposium. Montana Geological Survey, Montana, USA, pp. 361–368.
- Yellig, W.F., Metcalfe, R.S., 1980. Determination and prediction of CO<sub>2</sub> minimum miscibility pressures. *J. Pet. Technol.*, 160–168 (Jan.).
- Zuo, Y.X., Chu, J.Z., Ke, S.L., Guo, T.M., 1993. A study of the minimum miscibility pressure for miscible flooding systems. *J. Pet. Sci. Eng.* 8, 315–328.