#### 컴퓨터공학 기초 실험2

Week #4 (Lab #5)

Traffic Light Controller with/without Left Turn Signals

Kwangwoon University Embedded System Architecture Lab





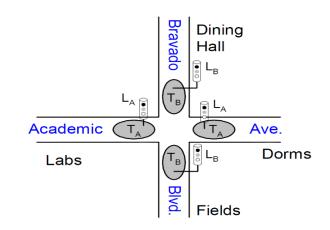
# TRAFFIC LIGHT CONTROLLER





#### **Traffic Light Controller**

- ▶ 신호등을 제어하는 logic을 구현
  - $\checkmark$  신호등  $L_A$ 는 'Academic Ave.'의 차량 통행을 제어하는 신호등
  - $\checkmark$   $L_B$ 는 'Bravado Blvd.'의 차량 통행을 제어하는 신호등
  - ✓ 시간에 따라 변하는 신호등이 아닌 거리에 차량이 있을 때 신호등이 초록색이 되고, 없을 때는 빨간색이 된다.
  - $\checkmark$  차량이 있음을 감지하기 위하여 'Academic Ave.'에 traffic sensor인  $T_A$ 를, 'Bravado Blvd.'에 traffic sensor인  $T_B$ 를 설치







# **Traffic Light Controller(Cont.)**

- ▶ 다음 규칙을 만족해야 한다.
  - ✓ Traffic light는 교통이 없을 때 초록색에서 노란색을 거쳐 빨간색으로 변한다.
  - $\checkmark$  만약 traffic light  $L_A$ 가 초록색이거나 노란색이면, traffic light  $L_B$ 는 빨간색이다. 반대의 경우도 마찬가지이다.





#### **Finite State Machine**

- Design
  - Drawing the finite state diagram
    - Define states
    - Define inputs
    - Define outputs
    - Draw the diagram
  - 2. Encoding states
  - 3. Coding the module header
  - 4. Coding state registers(flip-flops) sequential circuits
  - 5. Coding combinational circuits



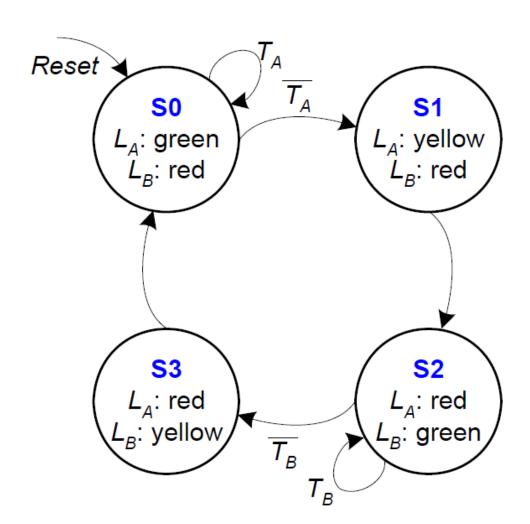


#### **FSM State Transition Diagram**

> Moore FSM: outputs labeled in each state

States: Circles

> Transitions: Arcs







#### **FSM Encoded State Transition Table**

| Curre | nt state | Inp   | uts   | Next state |       |  |
|-------|----------|-------|-------|------------|-------|--|
| $Q_1$ | $Q_0$    | $T_A$ | $T_B$ | $D_1$      | $D_0$ |  |
| 0     | 0        | 0     | Χ     | 0          | 1     |  |
| 0     | 0        | 1     | Χ     | 0          | 0     |  |
| 0     | 1        | X     | X     | 1          | 0     |  |
| 1     | 0        | X     | 0     | 1          | 1     |  |
| 1     | 0        | Χ     | 1     | 1          | 0     |  |
| 1     | 1        | Χ     | X     | 0          | 0     |  |

$$D_1 = Q_1 \oplus Q_0$$

$$D_0 = \overline{Q}_1 \overline{Q}_0 \overline{T}_A + Q_1 \overline{Q}_0 \overline{T}_B$$





# **FSM** output table

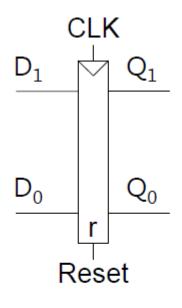
| Curre | nt state | Outputs  |          |          |          |  |  |
|-------|----------|----------|----------|----------|----------|--|--|
| $Q_1$ | $Q_0$    | $L_{A1}$ | $L_{A0}$ | $L_{B1}$ | $L_{B0}$ |  |  |
| 0     | 0        | 0        | 0        | 1        | 0        |  |  |
| 0     | 1        | 0        | 1        | 1        | 0        |  |  |
| 1     | 0        | 1        | 0        | 0        | 0        |  |  |
| 1     | 1        | 1        | 0        | 0        | 1        |  |  |

$$L_{A1} = Q_1$$
 $L_{A0} = \overline{Q}_1 Q_0$ 
 $L_{B1} = \overline{Q}_1$ 
 $L_{B0} = Q_1 Q_0$ 





# **FSM Schematic: State Register**

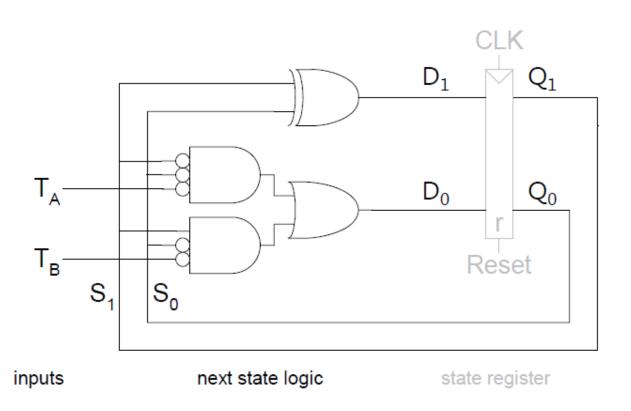


state register





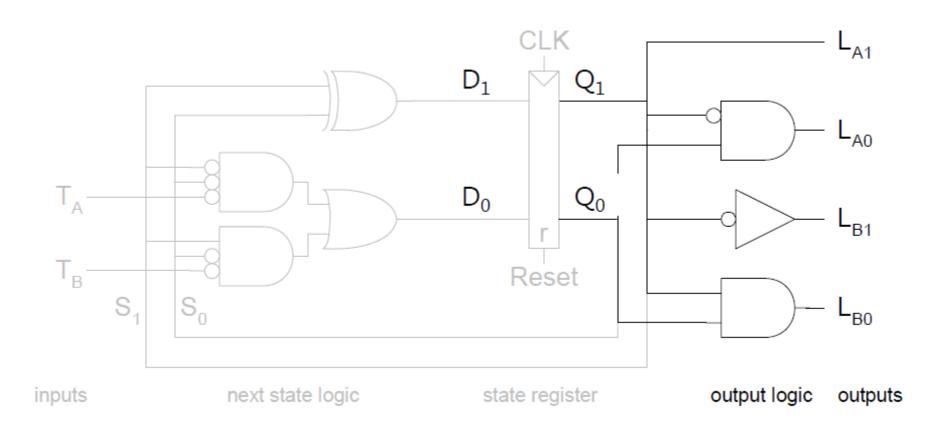
# **FSM Schematic: Next State Logic**







# **FSM Schematic: Output Logic**







# **Traffic Light Controller(Cont.)**

Module configuration

| 구분         | 이름           | 설명   |
|------------|--------------|--|
| Top module | tl_cntr      | Traffic light controller의 top module   |
| Sub module | ns_logic     | Traffic light controller의 next state를 결정하는 combin<br>ational logic   |
| Sub module | _register2_r | 2-bit resettable register with active low asynchronous<br>reset module (내부에 d_ff_r_async를 instance)<br>- 현재 state의 값을 저장하고 있다. |
| Sub module | _dff_r       | Resettable D flip-flop with active low asynchronous re set   |
| Sub module | o_logic      | 현재 state의 값에 기반하여 output 값을 결정하는 com<br>binational logic   |





# **Traffic Light Controller(Cont.)**

> I/O Configuration

| Module<br>이름 | 구분     | 이름                             | 비트 수  | 설명                                       |                                       |
|--------------|--------|--------------------------------|-------|--|---------------------------------------|
|              |        | clk                            | 1-bit | Clock                                    |                                       |
|              | input  | reset_n                        | 1-bit | Active low에 동작하는 reset 신호로 state를<br>초기화 |                                       |
| tl_cntr      |        |                                | Ta    | 1-bit                                    | Traffic sensor A('Academic Ave.'에 위치) |
|              |        | Tb                             | 1-bit | Traffic sensor B('Bravado Blvd.'에 위치)    |                                       |
|              | outnut | 신호등 값 출력 A('Academic Ave'에 위치) |       |  |                                       |
|              | output | Lb                             | 2-bit | 신호등 값 출력 B('Bravado Blvd.'에 위치)          |                                       |





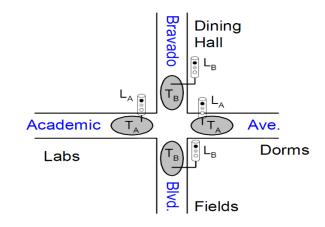
# TRAFFIC LIGHT CONTROLLER WITH LEFT TURN SIGNALS





# **Traffic Light Controller with Left Turn Signals**

- ▶ 신호등을 제어하는 logic을 구현
  - ✓ 앞서 실습한 traffic light controller에 left turn signal을 추가하여 구현
  - $\checkmark$  신호등  $L_A$ 는 'Academic Ave.'의 차량 통행을 제어하는 신호등
  - $\checkmark$   $L_B$ 는 'Bravado Blvd.'의 차량 통행을 제어하는 신호등
  - ✓ 시간에 따라 변하는 신호등이 아닌 거리에 차량이 있을 때 신호등이 초록색이 되고, 없을 때는 빨간색이 된다.
  - $\checkmark$  차량이 있음을 감지하기 위하여 'Academic Ave.'에 traffic sensor인  $T_A, T_{AL}$ 를, 'Bravado Blvd.'에 traffic sensor인  $T_B, T_{BL}$ 를 설치
  - $\checkmark$  Traffic sensor인  $T_A$ ,  $T_B$ 는 직진에 대한 차량 감시
  - $\checkmark$  Traffic sensor인  $T_{AL}$ ,  $T_{BL}$ 은 좌회전에 대한 차량 감시







#### **TLC with LTS(Cont.)**

- ▶ 다음 규칙을 만족해야 한다.
  - ✓ Traffic light는 교통이 없을 때 초록색에서 노란색을 거쳐 좌회전으로 변한다.
  - ✓ Traffic light는 교통이 없을 때 좌회전에서 노란색을 거쳐 빨간색으로 변한다.
  - ✓ Traffic light는 비록 좌회전하는 교통이 없더라도 초록색에서 좌회전으로 우선 변해야 한다.
  - $\checkmark$  만약 traffic light  $L_A$ 가 초록색, 노란색, 좌회전일 동안에  $L_B$ 는 빨간색이어야 한다. 반대의 경우도 마찬가지이다.





#### **Finite State Machine**

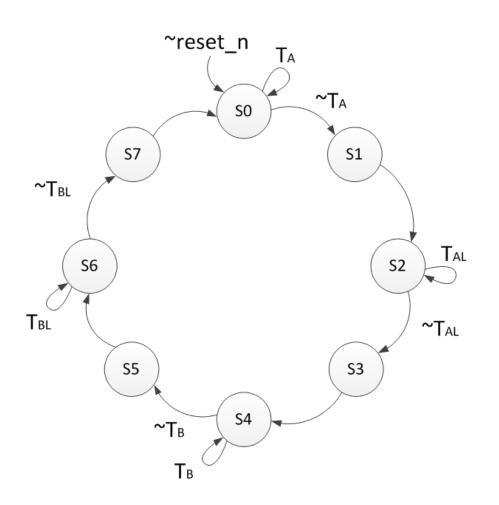
- Design
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    - Define states
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  - 2. Encoding states
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# **FSM State Transition Diagram**

#### Moore FSM

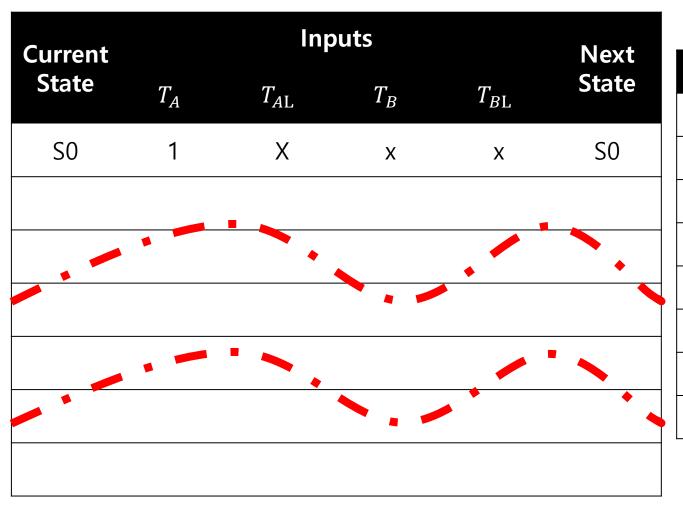


| State | $L_A$  | $L_B$  |
|-------|--------|--------|
| S0    | Green  | Red    |
| S1    | Yellow | Red    |
| S2    | Left   | Red    |
| S3    | Yellow | Red    |
| S4    | Red    | Green  |
| S5    | Red    | Yellow |
| S6    | Red    | Left   |
| S7    | Red    | Yellow |





#### **FSM State Transition Table**



| State | Code |
|-------|------|
| S0    | 000  |
| S1    | 001  |
| S2    | 010  |
| S3    | 011  |
| S4    | 100  |
| S5    | 101  |
| S6    | 110  |
| S7    | 111  |





#### **FSM Encoded State Transition Table**

| $Q_2$ | $Q_1$ | $Q_0$ | $T_A$ | $T_{AL}$ | $T_B$ | $T_{BL}$ | $D_2$ | $D_1$ | $D_0$ |
|-------|-------|-------|-------|----------|-------|----------|-------|-------|-------|
| 0     | 0     | 0     | 0     | X        | X     | X        | 0     | 0     | 1     |
| 0     | 0     | 0     | 1     | Х        | Х     | Х        | 0     | 0     | 0     |
| 0     | 0     | 1     | X     | X        | X     | X        | 0     | 1     | 0     |
| 0     | 1     | 0     | Х     | 0        | X     | Х        | 0     | 1     | 1     |
| 0     | 1     | 0     | Х     | 1        | X     | X        | 0     | 1     | 0     |
| 0     | 1     | 1     | Х     | Х        | Х     | Х        | 1     | 0     | 0     |
| 1     | 0     | 0     | Х     | Х        | 0     | Х        | 1     | 0     | 1     |
| 1     | 0     | 0     | Х     | Х        | 1     | Х        | 1     | 0     | 0     |
| 1     | 0     | 1     | X     | X        | X     | X        | 1     | 1     | 0     |
| 1     | 1     | 0     | X     | X        | X     | 0        | 1     | 1     | 1     |
| 1     | 1     | 0     | Х     | Х        | Х     | 1        | 1     | 1     | 0     |
| 1     | 1     | 1     | Х     | Х        | Х     | Х        | 0     | 0     | 0     |





#### **FSM Encoded State Transition Table**

| $Q_2$ | $Q_1$ | $Q_0$ | $T_A$ | $T_{AL}$ | $T_B$ | $T_{BL}$ | $D_2$ | $D_1$ | $D_0$ |
|-------|-------|-------|-------|----------|-------|----------|-------|-------|-------|
| 0     | 0     | 0     | 0     | Х        | Х     | Х        | 0     | 0     | 1     |
| 0     | 0     | 0     | 1     | Х        | Х     | Х        | 0     | 0     | 0     |
| 0     | 0     | 1     | X     | X        | X     | X        | 0     | 1     | 0     |
| 0     | 1     | 0     | Х     | 0        | Х     | Х        | 0     | 1     | 1     |
| 0     | 1     | 0     | Х     | 1        | Х     | Х        | 0     | 1     | 0     |
| 0     | 1     | 1     | Х     | Х        | Х     | Х        | 1     | 0     | 0     |
| 1     | 0     | 0     | X     | X        | 0     | X        | 1     | 0     | 1     |
| 1     | 0     | 0     | Х     | Х        | 1     | X        | 1     | 0     | 0     |
| 1     | 0     | 1     | Х     | Х        | Х     | Х        | 1     | 1     | 0     |
| 1     | 1     | 0     | Х     | Х        | Х     | 0        | 1     | 1     | 1     |
| 1     | 1     | 0     | Х     | Х        | Х     | 1        | 1     | 1     | 0     |
| 1     | 1     | 1     | Х     | Х        | Х     | Х        | 0     | 0     | 0     |

$$D_2 =$$

$$\nu_1$$
 –

$$D_0 =$$





#### quine-mccluskey method of Next State $D_2$ (1/10)

| $Q_2$ | $Q_1$ | $Q_0$ | $T_A$ | $T_{AL}$ | $T_B$ | $T_{BL}$ | $D_2$ | $D_1$ | $D_0$ |
|-------|-------|-------|-------|----------|-------|----------|-------|-------|-------|
| 0     | 0     | 0     | 0     | Х        | Х     | Х        | 0     | 0     | 1     |
| 0     | 0     | 0     | 1     | Х        | Х     | Х        | 0     | 0     | 0     |
| 0     | 0     | 1     | X     | X        | X     | X        | 0     | 1     | 0     |
| 0     | 1     | 0     | Х     | 0        | Х     | Х        | 0     | 1     | 1     |
| 0     | 1     | 0     | Х     | 1        | Х     | Х        | 0     | 1     | 0     |
| 0     | 1     | 1     | Х     | Х        | Х     | Х        | 1     | 0     | 0     |
| 1     | 0     | 0     | X     | X        | 0     | X        | 1     | 0     | 1     |
| 1     | 0     | 0     | X     | X        | 1     | Х        | 1     | 0     | 0     |
| 1     | 0     | 1     | Х     | Х        | Х     | Х        | 1     | 1     | 0     |
| 1     | 1     | 0     | X     | Х        | X     | 0        | 1     | 1     | 1     |
| 1     | 1     | 0     | X     | X        | X     | 1        | 1     | 1     | 0     |
| 1     | 1     | 1     | Х     | Х        | Х     | Х        | 0     | 0     | 0     |





#### quine-mccluskey method of Next State $D_2$ (2/10)

| $Q_2$ | $Q_1$ | $Q_0$ | $T_A$ | $T_{AL}$ | $T_B$ | $T_{BL}$ | Deci. |
|-------|-------|-------|-------|----------|-------|----------|-------|
| 0     | 1     | 1     | 0     | 0        | 0     | 0        | 48    |
| 0     | 1     | 1     | 0     | 0        | 0     | 1        | 49    |
| 0     | 1     | 1     | 0     | 0        | 1     | 0        | 50    |
| 0     | 1     | 1     | 0     | 0        | 1     | 1        | 51    |
| 0     | 1     | 1     | 0     | 1        | 0     | 0        | 52    |
| 0     | 1     | 1     | 0     | 1        | 0     | 1        | 53    |
| 0     | 1     | 1     | 0     | 1        | 1     | 0        | 54    |
| 0     | 1     | 1     | 0     | 1        | 1     | 1        | 55    |
| 0     | 1     | 1     | 1     | 0        | 0     | 0        | 56    |
| 0     | 1     | 1     | 1     | 0        | 0     | 1        | 57    |
| 0     | 1     | 1     | 1     | 0        | 1     | 0        | 58    |
| 0     | 1     | 1     | 1     | 0        | 1     | 1        | 59    |
| 0     | 1     | 1     | 1     | 1        | 0     | 0        | 60    |
| 0     | 1     | 1     | 1     | 1        | 0     | 1        | 61    |
| 0     | 1     | 1     | 1     | 1        | 1     | 0        | 62    |
| 0     | 1     | 1     | 1     | 1        | 1     | 1        | 63    |
| 1     | 0     | 0     | 0     | 0        | 0     | 0        | 64    |
| 1     | 0     | 0     | 0     | 0        | 0     | 1        | 65    |
| 1     | 0     | 0     | 0     | 0        | 1     | 0        | 66    |
| 1     | 0     | 0     | 0     | 0        | 1     | 1        | 67    |
| 1     | 0     | 0     | 0     | 1        | 0     | 0        | 68    |
| 1     | 0     | 0     | 0     | 1        | 0     | 1        | 69    |
| 1     | 0     | 0     | 0     | 1        | 1     | 0        | 70    |
| 1     | 0     | 0     | 0     | 1        | 1     | 1        | 71    |
| 1     | 0     | 0     | 1     | 0        | 0     | 0        | 72    |
| 1     | 0     | 0     | 1     | 0        | 0     | 1        | 73    |
| 1     | 0     | 0     | 1     | 0        | 1     | 0        | 74    |
| 1     | 0     | 0     | 1     | 0        | 1     | 1        | 75    |
| 1     | 0     | 0     | 1     | 1        | 0     | 0        | 76    |
| 1     | 0     | 0     | 1     | 1        | 0     | 1        | 77    |
| 1     | 0     | 0     | 1     | 1        | 1     | 0        | 78    |
| 1     | 0     | 0     | 1     | 1        | 1     | 1        | 79    |

| $Q_2$ | $Q_1$ | $Q_0$ | $T_A$ | $T_{AL}$ | $T_B$ | $T_{BL}$ | Deci. |
|-------|-------|-------|-------|----------|-------|----------|-------|
| 1     | 0     | 1     | 0     | 0        | 0     | 0        | 80    |
| 1     | 0     | 1     | 0     | 0        | 0     | 1        | 81    |
| 1     | 0     | 1     | 0     | 0        | 1     | 0        | 82    |
| 1     | 0     | 1     | 0     | 0        | 1     | 1        | 83    |
| 1     | 0     | 1     | 0     | 1        | 0     | 0        | 84    |
| 1     | 0     | 1     | 0     | 1        | 0     | 1        | 85    |
| 1     | 0     | 1     | 0     | 1        | 1     | 0        | 86    |
| 1     | 0     | 1     | 0     | 1        | 1     | 1        | 87    |
| 1     | 0     | 1     | 1     | 0        | 0     | 0        | 88    |
| 1     | 0     | 1     | 1     | 0        | 0     | 1        | 89    |
| 1     | 0     | 1     | 1     | 0        | 1     | 0        | 90    |
| 1     | 0     | 1     | 1     | 0        | 1     | 1        | 91    |
| 1     | 0     | 1     | 1     | 1        | 0     | 0        | 92    |
| 1     | 0     | 1     | 1     | 1        | 0     | 1        | 93    |
| 1     | 0     | 1     | 1     | 1        | 1     | 0        | 94    |
| 1     | 0     | 1     | 1     | 1        | 1     | 1        | 95    |
| 1     | 1     | 0     | 0     | 0        | 0     | 0        | 96    |
| 1     | 1     | 0     | 0     | 0        | 0     | 1        | 97    |
| 1     | 1     | 0     | 0     | 0        | 1     | 0        | 98    |
| 1     | 1     | 0     | 0     | 0        | 1     | 1        | 99    |
| 1     | 1     | 0     | 0     | 1        | 0     | 0        | 100   |
| 1     | 1     | 0     | 0     | 1        | 0     | 1        | 101   |
| 1     | 1     | 0     | 0     | 1        | 1     | 0        | 102   |
| 1     | 1     | 0     | 0     | 1        | 1     | 1        | 103   |
| 1     | 1     | 0     | 1     | 0        | 0     | 0        | 104   |
| 1     | 1     | 0     | 1     | 0        | 0     | 1        | 105   |
| 1     | 1     | 0     | 1     | 0        | 1     | 0        | 106   |
| 1     | 1     | 0     | 1     | 0        | 1     | 1        | 107   |
| 1     | 1     | 0     | 1     | 1        | 0     | 0        | 108   |
| 1     | 1     | 0     | 1     | 1        | 0     | 1        | 109   |
| 1     | 1     | 0     | 1     | 1        | 1     | 0        | 110   |
| 1     | 1     | 0     | 1     | 1        | 1     | 1        | 111   |





#### quine-mccluskey method of Next State $D_2$ (3/10)

| Num of 1 | input   |
|----------|---|
| 0        |   |
| 1        | 64 1000000  |
| 2        | 48 0110000<br>65 1000001<br>66 1000010<br>68 1000100<br>72 1001000<br>80 1010000<br>96 1100000  |
| 3        | 49 0110001<br>50 0110010<br>52 0110100<br>56 0111000<br>67 1000011<br>69 1000101<br>70 1000110<br>73 1001001<br>74 1001010<br>81 1010001<br>82 1010010<br>84 101100<br>88 1011000<br>97 1100001<br>98 1100100<br>100 1100100<br>104 1101000 |

| Num of 1  51 0110011 53 0110101 54 0110110 57 0111001 58 0111010 60 0111100 71 1000111 75 1001011 77 1001101 78 1001110 83 1010011 85 1010101 86 1010110 89 1011001  |
|--|
| 53 0110101<br>54 0110110<br>57 0111001<br>58 0111010<br>60 0111100<br>71 1000111<br>75 1001011<br>77 1001101<br>78 1001110<br>83 1010011<br>85 1010101<br>86 1010110 |
| 54 0110110<br>57 0111001<br>58 0111010<br>60 0111100<br>71 1000111<br>75 1001011<br>77 1001101<br>78 1001110<br>83 1010011<br>85 1010101<br>86 1010110               |
| 57 0111001<br>58 0111010<br>60 0111100<br>71 1000111<br>75 1001011<br>77 1001101<br>78 1001110<br>83 1010011<br>85 1010101<br>86 1010110                             |
| 58 0111010<br>60 0111100<br>71 1000111<br>75 1001011<br>77 1001101<br>78 1001110<br>83 1010011<br>85 1010101<br>86 1010110   |
| 60 0111100<br>71 1000111<br>75 1001011<br>77 1001101<br>78 1001110<br>83 1010011<br>85 1010101<br>86 1010110   |
| 71 1000111<br>75 1001011<br>77 1001101<br>78 1001110<br>83 1010011<br>85 1010101<br>86 1010110   |
| 75 1001011<br>77 1001101<br>78 1001110<br>83 1010011<br>4 85 1010101<br>86 1010110   |
| 77 1001101<br>78 1001110<br>83 1010011<br>85 1010101<br>86 1010110   |
| 78 1001110<br>83 1010011<br>85 1010101<br>86 1010110   |
| 4 83 1010011<br>85 1010101<br>86 1010110   |
| 85 1010101<br>86 1010110   |
| 85 1010101<br>86 1010110   |
| 1  |
| l 89 1011001   |
| 1  |
| 90 1011010   |
| 92 1011100   |
| 99 1100011   |
| 101 1100101  |
| 102 1100110  |
| 105 1101001  |
| 106 1101010  |
| 108 1101100  |
| 55 0110111   |
| 59 0111011   |
| 61 0111101   |
| 62 0111110   |
| 79 1001111   |
| 87 1010111   |
| 5 91 1011011   |
| 93 1011101<br>94 1011110   |
| 103 1100111  |
| 103 1100111  |
| 107 1101011  |
| 110 1101110  |

| Num of 1 | input       |
|----------|-------------|
|          | 63 0111111  |
| 6        | 95 1011111  |
|          | 111 1101111 |





#### quine-mccluskey method of Next State $D_2$ (4/10)

| -                |  |
|------------------|--|
| First Comparison | input  |
| 0                | ·  |
| 1                | (65,64)100000-<br>(66,64)10000-0<br>(68,64)1000-00<br>(72,64)100-000<br>(80,64)10-0000<br>(96,64)1-00000   |
| 2                | ( 49 , 48 ) 011000-<br>( 50 , 48 ) 011000-<br>( 52 , 48 ) 0110-00<br>( 56 , 48 ) 011-000<br>( 67 , 65 ) 10000-1<br>( 69 , 65 ) 1000-01<br>( 73 , 65 ) 10-0001<br>( 81 , 65 ) 10-0001<br>( 97 , 65 ) 1-00001<br>( 70 , 66 ) 100001-<br>( 70 , 66 ) 1000-10<br>( 74 , 66 ) 100-010<br>( 82 , 66 ) 10-0010<br>( 82 , 66 ) 10-0010<br>( 98 , 66 ) 1-00010<br>( 70 , 68 ) 100010-<br>( 70 , 68 ) 100010-<br>( 70 , 68 ) 100010-<br>( 70 , 68 ) 1000100<br>( 70 , 68 ) 1000100<br>( 70 , 68 ) 1-00100<br>( 71 , 72 ) 100100-<br>( 72 , 72 ) 100100-<br>( 73 , 72 ) 100100-<br>( 74 , 72 ) 1001000<br>( 74 , 72 ) 1001000<br>( 75 , 72 ) 1001000<br>( 76 , 72 ) 1001000<br>( 77 , 72 ) 1001000<br>( 88 , 72 ) 10-1000<br>( 81 , 80 ) 1010000-<br>( 82 , 80 ) 1010000-<br>( 83 , 80 ) 1010000-<br>( 84 , 80 ) 1010000-<br>( 84 , 80 ) 1010000-<br>( 98 , 96 ) 110000-<br>( 98 , 96 ) 110000-<br>( 100 , 96 ) 1100-00<br>( 100 , 96 ) 1100-00<br>( 100 , 96 ) 1100-00 |

| First Comparison | input   |
|------------------|---|
| First Comparison | (51, 49) 01100-1 (53, 49) 0110-01 (57, 49) 011-001 (51, 50) 011001- (54, 50) 0110-10 (58, 50) 011-010 (53, 52) 011010- (54, 52) 011010- (54, 52) 011010- (54, 52) 011-100 (57, 56) 011100- (58, 56) 011100- (58, 56) 011100- (58, 56) 01110-0 (60, 56) 0111-00 (71, 67) 1000-11 (75, 67) 100-011 (83, 67) 10-0011 (71, 69) 10011- (77, 69) 100-101 (85, 69) 10-0101 (101, 69) 1-00101 (101, 69) 1-00101 (101, 69) 1-00101 (71, 70) 100011- (78, 70) 100-110 (86, 70) 10-0110 (102, 70) 1-00110 (102, 70) 1-00110 (105, 73) 1001-01 (89, 73) 10-1001 (105, 73) 10-1001 (105, 73) 10-1001 (106, 74) 10-1010 (106, 74) 10-1010 (107, 76) 100110- (108, 76) 10-1100 (108, 76) 1-01100 (108, 76) 1-01100 (108, 76) 1-01100 (108, 76) 1-01100 (108, 76) 1-01100 (108, 76) 1-01100 (108, 76) 1-01100 (108, 76) 1-01100 (108, 76) 1-01100 (108, 76) 1-01100 |
|                  | (89 . 81 ) 101-001  |

| First Comparison | input                 |
|------------------|-----------------------|
|                  | ( 83 , 82 ) 101001-   |
|                  | ( 86 , 82 ) 1010-10   |
|                  | ( 90 , 82 ) 101-010   |
|                  | ( 85 , 84 ) 101010-   |
|                  | ( 86 , 84 ) 10101-0   |
|                  | ( 92 , 84 ) 101-100   |
|                  | ( 89 , 88 ) 101100-   |
|                  | ( 90 , 88 ) 10110-0   |
|                  | ( 92 , 88 ) 1011-00   |
| _                | (99, 97) 11000-1      |
| 3                | (101, 97) 1100-01     |
|                  | ( 105 , 97 ) 110-001  |
|                  | (99, 98) 110001-      |
|                  | (102, 98) 1100-10     |
|                  | (106, 98) 110-010     |
|                  | (101,100)110010-      |
|                  | (102,100)11001-0      |
|                  | (108,100)110-100      |
|                  | (105, 104) 110100-    |
|                  | (106,104)11010-0      |
|                  | ( 108 , 104 ) 1101-00 |





#### quine-mccluskey method of Next State $D_2$ (5/10)

| First Comparison | input                                     |
|------------------|---|
|                  | ( 55 , 51 ) 0110-11                       |
|                  | ( 59 , 51 ) 011-011                       |
|                  | ( 55 , 53 ) 01101-1                       |
|                  | ( 61 , 53 ) 011-101                       |
|                  | ( 55 , 54 ) 011011-                       |
|                  | (62,54)011-110                            |
|                  | ( 59 , 57 ) 01110-1                       |
|                  | (61,57)0111-01                            |
|                  | ( 59 , 58 ) 011101-                       |
|                  | ( 62 , 58 ) 0111-10                       |
|                  | ( 61 , 60 ) 011110-                       |
|                  | (62,60)01111-0                            |
|                  | (79,71)100-111                            |
|                  | (87,71)10-0111                            |
|                  | (103, 71) 1-00111                         |
|                  | (79,75)1001-11                            |
| 4                | (91,75)10-1011                            |
|                  | (107, 75) 1-01011                         |
|                  | (79,77)10011-1                            |
|                  | (93,77)10-1101                            |
|                  | (109 , 77 ) 1-01101<br>(79 , 78 ) 100111- |
|                  | (94,78)10-1110                            |
|                  | (110, 78) 1-01110                         |
|                  | (87,83)1010-11                            |
|                  | (91,83)101-011                            |
|                  | (87,85)10101-1                            |
|                  | (93, 85) 101-101                          |
|                  | (87,86)101011-                            |
|                  | (94, 86) 101-110                          |
|                  | (91,89)10110-1                            |
|                  | (93, 89) 1011-01                          |
|                  | (91,90)101101-                            |
|                  | (94,90)1011-10                            |

| First Comparison | input   |
|------------------|---|
| 4                | (93, 92) 101110-<br>(94, 92) 10111-0<br>(103, 99) 1100-11<br>(107, 99) 110-011<br>(103, 101) 11001-1<br>(109, 101) 110-101<br>(103, 102) 110011-<br>(110, 102) 110-110<br>(107, 105) 1101-1<br>(109, 105) 1101-01<br>(107, 106) 1101-10<br>(109, 108) 11011-0 |
| 5                | (63,55)011-111<br>(63,59)0111-11<br>(63,61)01111-1<br>(63,62)011111-<br>(95,79)10-1111<br>(111,79)1-01111<br>(95,87)101-111<br>(95,91)1011-11<br>(95,93)10111-1<br>(95,94)101111-<br>(111,103)110-111<br>(111,109)11011-1                                     |





#### quine-mccluskey method of Next State $D_2$ (6/10)

| Second Comparison | input  |
|-------------------|--|
| 0                 |  |
| 1                 | (67, 66, 65, 64) 10000<br>(69, 68, 65, 64) 1000-0-<br>(73, 72, 65, 64) 100-00-<br>(81, 80, 65, 64) 10-000-<br>(97, 96, 65, 64) 1-0000-<br>(70, 68, 66, 64) 10000<br>(74, 72, 66, 64) 100-0-0<br>(82, 80, 66, 64) 10-00-0<br>(98, 96, 66, 64) 1-000-0<br>(76, 72, 68, 64) 10000<br>(84, 80, 68, 64) 10-0-00<br>(100, 96, 68, 64) 1-0-00<br>(88, 80, 72, 64) 10000<br>(104, 96, 72, 64) 1-0-000  |
| 2                 | (51, 50, 49, 48) 01100<br>(53, 52, 49, 48) 0110-0-<br>(57, 56, 49, 48) 0110-0-<br>(54, 52, 50, 48) 01100<br>(58, 56, 50, 48) 01100<br>(60, 56, 52, 48) 01100<br>(71, 69, 67, 65) 10001<br>(75, 73, 67, 65) 100-0-1<br>(83, 81, 67, 65) 10-00-1<br>(99, 97, 67, 65) 1-000-1<br>(77, 73, 69, 65) 10001<br>(85, 81, 69, 65) 10001<br>(101, 97, 69, 65) 1-00-01<br>(101, 97, 69, 65) 1-00-01<br>(105, 97, 73, 65) 1-0-001<br>(71, 70, 67, 66) 100-1-<br>(75, 74, 67, 66) 100-01-<br>(83, 82, 67, 66) 10010<br>(86, 82, 70, 66) 10010 |

| Second Comparison | input   |
|-------------------|---|
| 2                 | (102, 98, 70, 66) 1-00-10<br>(90, 82, 74, 66) 10010<br>(106, 98, 74, 66) 1-0-010<br>(71, 70, 69, 68) 10001<br>(77, 76, 69, 68) 100-10-<br>(85, 84, 69, 68) 10-010-<br>(101, 100, 69, 68) 100-1-0<br>(86, 84, 70, 68) 10-01-0<br>(102, 100, 70, 68) 10-01-0<br>(102, 100, 70, 68) 10-100<br>(108, 100, 76, 68) 10-100<br>(75, 74, 73, 72) 10010<br>(77, 76, 73, 72) 10010<br>(89, 88, 73, 72) 10010<br>(90, 88, 74, 72) 1001-0<br>(90, 88, 74, 72) 10010-0<br>(90, 88, 74, 72) 10010-0<br>(92, 84, 80, 1001-0)<br>(106, 104, 74, 72) 1-010-0<br>(106, 104, 74, 72) 1-010-0<br>(108, 104, 76, 72) 1-01-00<br>(83, 82, 81, 80) 10100<br>(85, 84, 81, 80) 1010-0-<br>(89, 88, 81, 80) 1010-0-<br>(90, 88, 82, 80) 101-00-<br>(106, 104, 74, 72) 1001-00<br>(107, 104, 70, 70, 100, 100, 100, 100, 100, 100, |





#### quine-mccluskey method of Next State $D_2$ (7/10)

| (55, 53, 51, 49) 01101 (59, 57, 51, 49) 01101 (61, 57, 53, 49) 01101 (55, 54, 51, 50) 0110-1- (59, 58, 51, 50) 0110-1- (62, 58, 54, 50) 01110 (62, 58, 54, 50) 01110 (62, 60, 53, 52) 011-10- (62, 60, 54, 52) 011-10- (62, 60, 54, 52) 01110 (61, 60, 57, 56) 01110 (62, 60, 58, 56) 01110 (62, 60, 58, 56) 01110 (79, 75, 71, 67) 10011 (87, 83, 71, 67) 10-0-11 (103, 99, 71, 67) 1-00-11 (107, 99, 75, 67) 10-011 (107, 99, 75, 67) 10-011 (109, 101, 77, 69) 100-1-1 (87, 85, 71, 69) 100-11- (87, 85, 71, 69) 100-11- (87, 85, 71, 69) 100-11- (93, 85, 77, 69) 100-11- (109, 101, 77, 69) 1-0-101 (109, 101, 77, 69) 1-0-101 (109, 101, 77, 69) 1-0-110 (109, 101, 77, 69) 1-0-110 (109, 78, 71, 70) 100-11- (87, 86, 71, 70) 100-11- (87, 86, 71, 70) 100-11- (91, 89, 75, 73) 10011 (91, 89, 75, 73) 10-10-1 (107, 105, 75, 73) 1-010-1 (107, 105, 75, 73) 1-010-1 (109, 105, 77, 73) 1-010-1 (109, 105, 75, 73) 1-010-1 (109, 105, 75, 74) 10-011- (91, 90, 75, 74) 10-011- (91, 90, 75, 74) 10-011- (91, 90, 75, 74) 10-011- (91, 90, 78, 74) 10-110- (107, 106, 75, 74) 1-0101- (94, 90, 78, 74) 10-1-10 (79, 78, 77, 76) 100-11- (91, 90, 78, 74, 76) 10011 (93, 92, 77, 76) 100-110- (93, 92, 77, 76) 100-110-   | Second Comparison | input                           |
|--|-------------------|---------------------------------|
| (59, 57, 51, 49) 011-0-1 (61, 57, 53, 49) 011-0-1 (55, 54, 51, 50) 0110-1 (59, 58, 51, 50) 011-01- (62, 58, 54, 50) 011-01- (62, 58, 54, 50) 011-10- (61, 60, 53, 52) 01101 (61, 60, 53, 52) 011-10- (62, 60, 54, 52) 011-10- (62, 60, 54, 52) 011-10- (62, 60, 54, 52) 011-10- (62, 60, 58, 56) 01110 (61, 60, 57, 56) 01110 (61, 60, 57, 56) 01110 (62, 60, 58, 56) 0111-0- (79, 75, 71, 67) 100-11 (87, 83, 71, 67) 100-11 (91, 83, 75, 67) 10-011 (91, 83, 75, 67) 10-011 (107, 99, 75, 67) 10-011 (107, 99, 75, 67) 10-011 (109, 101, 77, 69) 100-1-1 (87, 85, 71, 69) 100-1-1 (93, 85, 77, 69) 10-101 (109, 101, 77, 69) 1-0-101 (79, 78, 71, 70) 100-11- (87, 86, 71, 70) 100-11- (87, 86, 71, 70) 100-11- (94, 86, 78, 70) 10-101 (109, 101, 77, 75, 73) 10011 (91, 89, 75, 73) 10-10-1 (107, 105, 75, 73) 1-010-1 (109, 105, 77, 73) 1-010-1 (109, 105, 77, 73) 1-010-1 (109, 105, 77, 73) 1-010-1 (109, 105, 77, 73) 1-010-1 (109, 105, 77, 73) 1-010-1 (107, 106, 75, 74) 1-0101- (107, 106, 75, 74) 1-0101- (107, 106, 78, 74) 1-01-10 (107, 78, 77, 76) 10011   | Second Comparison | input                           |
| (61, 57, 53, 49) 01101<br>(55, 54, 51, 50) 0110-1-<br>(59, 58, 51, 50) 011-01-<br>(62, 58, 54, 53, 52) 011-10-<br>(61, 60, 53, 52) 011-10-<br>(61, 60, 53, 52) 011-10-<br>(62, 60, 54, 52) 011-10-<br>(62, 60, 54, 52) 011-10-<br>(62, 60, 58, 56) 01110-<br>(61, 60, 57, 56) 01110-<br>(62, 60, 58, 56) 01111-0<br>(79, 75, 71, 67) 100-11<br>(87, 83, 71, 67) 100-11<br>(103, 99, 71, 67) 10-0-11<br>(107, 99, 75, 67) 10011<br>(107, 99, 75, 67) 10011<br>(109, 101, 71, 69) 100-1-1<br>(87, 85, 71, 69) 10-1-1<br>(87, 85, 77, 69) 10-101<br>(199, 101, 77, 69) 10-101<br>(199, 101, 77, 69) 10-101<br>(199, 101, 77, 69) 10-110<br>(109, 101, 77, 69) 10-110<br>(109, 101, 77, 69) 10-110<br>(109, 101, 77, 69) 10-110<br>(109, 101, 77, 76) 10-110<br>(101, 102, 78, 70) 10-110<br>(101, 102, 78, 70) 10-110<br>(107, 105, 75, 73) 10-10-1<br>(107, 105, 75, 73) 10-10-1<br>(109, 105, 77, 73) 1-01-01<br>(199, 105, 77, 73) 1-01-01<br>(107, 106, 75, 74) 1-0101-<br>(107, 106, 75, 74) 1-01-10<br>(107, 106, 78, 74) 1-01-10<br>(107, 106, 78, 74) 1-01-10 |                   |                                 |
| (55, 54, 51, 50) 0110-1-<br>(59, 58, 51, 50) 011-01-<br>(62, 58, 54, 50) 011-10-<br>(61, 60, 53, 52) 011-10-<br>(61, 60, 53, 52) 011-10-<br>(62, 60, 54, 52) 011-1-0-<br>(62, 60, 54, 52) 011-1-0-<br>(62, 60, 58, 56) 01110<br>(61, 60, 57, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0-<br>(79, 75, 71, 67) 100-11-<br>(87, 83, 71, 67) 10-0-11-<br>(103, 99, 71, 67) 1-0-011-<br>(107, 99, 75, 67) 10-011-<br>(107, 99, 75, 67) 10-011-<br>(103, 101, 71, 69) 100-1-1-<br>(87, 85, 71, 69) 10-10-1-<br>(87, 85, 77, 69) 10-101-<br>(199, 101, 77, 69) 1-0-101-<br>(199, 101, 77, 69) 1-0-101-<br>(199, 101, 77, 69) 1-0-101-<br>(199, 101, 77, 69) 1-0-110-<br>(109, 101, 77, 69) 1-0-110-<br>(109, 101, 77, 69) 1-0-110-<br>(101, 102, 78, 70) 10-110-<br>(107, 105, 78, 73) 1-01-01-<br>(107, 105, 75, 73) 1-01-01-<br>(109, 105, 77, 73) 1-01-01-<br>(199, 78, 75, 74) 10-101-<br>(190, 78, 77, 74) 1-01-10-<br>(107, 106, 78, 74) 1-01-10-<br>(107, 106, 78, 74) 1-01-10-<br>(107, 78, 77, 76) 10011  |                   |                                 |
| (59, 58, 51, 50) 011-01-<br>(62, 58, 54, 50) 011-10<br>(55, 54, 53, 52) 01101-<br>(61, 60, 53, 52) 011-10-<br>(62, 60, 54, 52) 011-10-<br>(62, 60, 54, 52) 011-10-<br>(61, 60, 57, 56) 01110<br>(61, 60, 57, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0-<br>(79, 75, 71, 67) 100-11<br>(87, 83, 71, 67) 10-0-11<br>(103, 99, 71, 67) 10-0-11<br>(107, 99, 75, 67) 10-011<br>(107, 99, 75, 67) 10-011<br>(107, 99, 75, 67) 10-011<br>(103, 101, 71, 69) 100-1-1<br>(87, 85, 71, 69) 10-101-1<br>(83, 85, 77, 69) 10-101<br>(109, 101, 77, 69) 10-101<br>(109, 101, 77, 69) 10-101<br>(109, 101, 77, 69) 10-11-<br>(87, 86, 71, 70) 10-011-<br>(87, 86, 71, 70) 10-011-<br>(87, 86, 71, 70) 10-11-<br>(103, 102, 71, 70) 10-110<br>(109, 105, 77, 73) 10-1-10<br>(107, 105, 75, 73) 1010-1<br>(91, 89, 75, 73) 10-1-01<br>(107, 105, 75, 73) 10-10-1<br>(93, 89, 77, 73) 10-1-01<br>(109, 105, 77, 73) 1-010-1<br>(109, 105, 77, 74) 10-101-<br>(107, 106, 75, 74) 1-011-1<br>(101, 106, 78, 74) 10-1-10<br>(101, 106, 78, 74) 1-01-10   |                   |                                 |
| (62, 58, 54, 50) 01110<br>(55, 54, 53, 52) 01101<br>(61, 60, 53, 52) 011-10-<br>(62, 60, 54, 52) 011-10-<br>(59, 58, 57, 56) 01110<br>(61, 60, 57, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0-<br>(62, 60, 58, 56) 01110<br>(79, 75, 71, 67) 10011<br>(87, 83, 71, 67) 100-011<br>(103, 99, 71, 67) 100-011<br>(107, 99, 75, 67) 1-0-011<br>(107, 99, 75, 67) 10-011<br>(79, 77, 71, 69) 100-1-1<br>(87, 85, 71, 69) 100-1-1<br>(87, 85, 71, 69) 10-101-1<br>(103, 101, 71, 69) 1-001-1<br>(109, 101, 77, 69) 1-0011-<br>(109, 101, 77, 69) 1-0011-<br>(109, 101, 77, 69) 10-011-<br>(101, 102, 78, 70) 10-110-<br>(101, 102, 78, 70) 10-110-<br>(101, 102, 78, 70) 10-110-<br>(107, 105, 75, 73) 1001<br>(107, 105, 75, 73) 1-010-1<br>(109, 105, 77, 73) 1001-1-<br>(107, 106, 75, 74) 10-101-<br>(107, 106, 75, 74) 10-101-<br>(107, 106, 75, 74) 10-1101-<br>(107, 106, 75, 74) 10-1101-<br>(107, 106, 78, 74) 10-1-10<br>(94, 90, 78, 74) 10-1-10<br>(110, 106, 78, 74) 1-01-10   |                   |                                 |
| (61, 60, 53, 52) 011-10-<br>(62, 60, 54, 52) 011-10-<br>(59, 58, 57, 56) 01110<br>(61, 60, 57, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0-<br>(79, 75, 71, 67) 100-11<br>(87, 83, 71, 67) 10-0-11<br>(103, 99, 71, 67) 1-0-011<br>(107, 99, 75, 67) 1-0-011<br>(107, 99, 75, 67) 1-0-011<br>(107, 97, 77, 1, 69) 100-1-1<br>(87, 85, 71, 69) 100-1-1<br>(87, 85, 71, 69) 10-101-1<br>(109, 101, 77, 69) 1-0-101<br>(109, 101, 77, 69) 1-0-101<br>(109, 101, 77, 69) 1-0-101<br>(103, 102, 71, 70) 100-11-<br>(87, 86, 71, 70) 10-011-<br>(103, 102, 71, 70) 1-0-110<br>(104, 102, 78, 70) 10-110<br>(107, 105, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 1-010-1<br>(109, 105, 77, 73) 1-010-1<br>(107, 106, 75, 74) 10-110-<br>(107, 106, 75, 74) 10-110-<br>(107, 106, 75, 74) 1-011-10<br>(100, 106, 78, 74) 1-01-10  |                   |                                 |
| (62, 60, 54, 52) 011-1-0<br>(59, 58, 57, 56) 01110<br>(61, 60, 57, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0-<br>(79, 75, 71, 67) 100-11<br>(87, 83, 71, 67) 10-0-11<br>(103, 99, 71, 67) 1-0-011<br>(107, 99, 75, 67) 1-0-011<br>(107, 99, 75, 67) 1-0-011<br>(103, 101, 71, 69) 10-1-1<br>(87, 85, 71, 69) 10-1-1<br>(87, 85, 77, 69) 10-1-1<br>(109, 101, 77, 69) 1-0-101<br>(109, 101, 77, 69) 1-0-101<br>(109, 101, 77, 69) 1-0-101<br>(103, 102, 71, 70) 10-011-<br>(87, 86, 71, 70) 10-011-<br>(87, 86, 71, 70) 10-11-<br>(103, 102, 71, 70) 10-110<br>(100, 102, 78, 70) 10-110<br>(101, 102, 78, 70) 10-10<br>(107, 105, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 10-1-01<br>(109, 105, 77, 73) 1-010-1<br>(109, 105, 77, 73) 10-1-01<br>(109, 105, 77, 73) 10-1-01   |                   |                                 |
| (59, 58, 57, 56) 01110 (61, 60, 57, 56) 0111-0- (62, 60, 58, 56) 0111-0- (62, 60, 58, 56) 0111-0- (79, 75, 71, 67) 10011 (87, 83, 71, 67) 10-0-11 (103, 99, 71, 67) 1-00-11 (107, 99, 75, 67) 1-0-011 (107, 99, 75, 67) 1-0-011 (107, 99, 75, 67) 1-0-011 (109, 101, 71, 69) 100-1-1 (87, 85, 71, 69) 10-01-1 (93, 85, 77, 69) 10101 (109, 101, 77, 69) 1-0-101 (109, 101, 77, 69) 1-0-101 (103, 102, 71, 70) 100-11- (87, 86, 71, 70) 10-011- (94, 86, 78, 70) 10110 (110, 102, 78, 70) 1-0-110 (110, 102, 78, 70) 1-0-110 (107, 105, 75, 73) 10011 (107, 105, 75, 73) 1-010-1 (93, 89, 77, 73) 1-010-1 (109, 105, 77, 73) 1-010-1 (109, 105, 77, 73) 1-010-1 (91, 90, 75, 74) 10011 (91, 90, 75, 74) 10-101- (107, 106, 75, 74) 10-110 (107, 106, 75, 74) 1-0101- (94, 90, 78, 74) 10-110 (110, 106, 78, 74) 1-01-10 (110, 106, 78, 74) 1-01-10  |                   |                                 |
| (61, 60, 57, 56) 0111-0-<br>(62, 60, 58, 56) 0111-0<br>(79, 75, 71, 67) 100-11<br>(87, 83, 71, 67) 10-0-11<br>(103, 99, 71, 67) 1-00-11<br>(107, 99, 75, 67) 1-0-011<br>(79, 77, 71, 69) 100-1-1<br>(87, 85, 71, 69) 10-01-1<br>(87, 85, 71, 69) 10-01-1<br>(87, 85, 77, 69) 10-01-1<br>(93, 85, 77, 69) 10-101<br>(109, 101, 77, 69) 1-0-101<br>(79, 78, 71, 70) 100-11-<br>(87, 86, 71, 70) 10-011-<br>(103, 102, 71, 70) 10-011-<br>(103, 102, 71, 70) 1-0011-<br>(94, 86, 78, 70) 10110<br>(110, 102, 78, 70) 10-110<br>(110, 102, 78, 70) 10-110<br>(107, 105, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 1-010-1<br>(109, 105, 77, 73) 1-010-1<br>(109, 105, 77, 73) 1-010-1<br>(91, 90, 75, 74) 10011-<br>(91, 90, 75, 74) 10-101-<br>(94, 90, 78, 74) 10-110-<br>(107, 106, 75, 74) 10-110-<br>(107, 106, 75, 74) 10-110-<br>(107, 106, 78, 74) 1-01-10<br>(110, 106, 78, 74) 1-01-10   |                   |                                 |
| (62,60,58,56)01110 (79,75,71,67)10011 (87,83,71,67)10-0-11 (103,99,71,67)10-0-11 (107,99,75,67)10011 (107,99,75,67)10011 (107,99,75,67)10011 (107,99,75,67)10-011 (107,99,75,76)10-01-1 (87,85,71,69)10-01-1 (87,85,71,69)10101 (109,101,77,69)10101 (109,101,77,69)10101 (109,101,77,69)10-011- (87,86,71,70)10-011- (87,86,71,70)10-011- (103,102,71,70)10-011- (104,86,78,70)10110 (110,102,78,70)10-110 (110,102,78,70)10-110 (107,105,75,73)10011 (91,89,75,73)10-10-1 (91,89,75,73)10-10-1 (93,89,77,73)10-10-1 (107,105,75,73)1-010-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1 (107,106,75,74)10-11- (91,90,75,74)10-11- (91,90,75,74)10-110- (107,106,75,74)10-110 (107,106,75,74)1-0101- (107,106,75,74)1-0101- (107,106,75,74)1-0101- (107,106,75,74)1-011- (107,106,75,74)1-01-10 (110,106,78,74)1-01-10   |                   | (61 60 57 56) 01110             |
| (79,75,71,67)10011 (87,83,71,67)100-0-11 (103,99,71,67)10-0-11 (107,99,75,67)10011 (107,99,75,67)10011 (107,99,75,67)10-011 (107,99,75,67)10-011 (107,99,75,67)10-011 (108,101,71,69)10-1-1 (109,101,77,69)10101 (109,101,77,69)10101 (109,101,77,69)10101 (109,101,77,0)10-011- (103,102,71,70)10-011- (103,102,71,70)10-011- (103,102,71,70)10-011- (104,86,78,70)10110 (110,102,78,70)10-110 (110,102,78,70)10-110 (107,105,75,73)10-10-1 (107,105,75,73)10-10-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1 (109,105,77,73)1-010-1   |                   |                                 |
| (103, 99, 71, 67) 1-00-11 (91, 83, 75, 67) 10011 (107, 99, 75, 67) 1-0-011 (79, 77, 71, 69) 100-1-1 (87, 85, 71, 69) 10-01-1 (87, 85, 71, 69) 10-01-1 (93, 85, 77, 69) 10101 (109, 101, 77, 69) 10101 (109, 101, 77, 69) 1-0-101 (103, 102, 71, 70) 100-11- (87, 86, 71, 70) 10-011- (103, 102, 71, 70) 10-011- (104, 86, 78, 70) 10110 (110, 102, 78, 70) 10110 (110, 102, 78, 70) 1-0-110 (107, 105, 75, 73) 10011 (91, 89, 75, 73) 10-10-1 (109, 105, 77, 73) 1-01-01 (109, 105, 77, 73) 1-01-01 (109, 78, 75, 74) 1001-1- (91, 90, 75, 74) 10-101- (107, 106, 75, 74) 1-0101- (107, 106, 75, 74) 1-0101- (107, 106, 78, 74) 1-01-10 (110, 106, 78, 74) 1-01-10 (110, 106, 78, 74) 1-01-10  |                   |                                 |
| (91, 83, 75, 67) 10011<br>(107, 99, 75, 67) 1-0-011<br>(79, 77, 71, 69) 100-1-1<br>(87, 85, 71, 69) 10-01-1<br>(103, 101, 71, 69) 10-101<br>(93, 85, 77, 69) 10101<br>(109, 101, 77, 69) 1-0-101<br>(79, 78, 71, 70) 100-11-<br>(87, 86, 71, 70) 10-011-<br>(103, 102, 71, 70) 10-011-<br>(104, 86, 78, 70) 10110<br>(110, 102, 78, 70) 10-110<br>(110, 102, 78, 70) 10-110<br>(107, 105, 75, 73) 1001-1<br>(107, 105, 75, 73) 10-10-1<br>(109, 105, 77, 73) 10-1-01<br>(109, 105, 77, 73) 10-1-01<br>(109, 105, 77, 74) 10-101-<br>(107, 106, 75, 74) 10-101-<br>(107, 106, 75, 74) 10-1-10<br>(110, 106, 78, 74) 10-1-10<br>(110, 106, 78, 74) 10-1-10<br>(110, 106, 78, 74) 10011   |                   |                                 |
| ( 107 , 99 , 75 , 67 ) 1-0-011<br>( 79 , 77 , 71 , 69 ) 100-1-1<br>( 87 , 85 , 71 , 69 ) 10-01-1<br>( 103 , 101 , 71 , 69 ) 1-001-1<br>( 109 , 101 , 77 , 69 ) 10101<br>( 109 , 101 , 77 , 69 ) 10-011-<br>( 87 , 86 , 71 , 70 ) 100-11-<br>( 87 , 86 , 71 , 70 ) 10-011-<br>( 103 , 102 , 71 , 70 ) 1-0011-<br>( 104 , 86 , 78 , 70 ) 10110<br>( 110 , 102 , 78 , 70 ) 10-110<br>( 110 , 102 , 78 , 70 ) 10-110<br>( 79 , 77 , 75 , 73 ) 10011<br>( 91 , 89 , 75 , 73 ) 10-10-1<br>( 107 , 105 , 75 , 73 ) 1-01-01<br>( 109 , 105 , 77 , 73 ) 1-01-01<br>( 109 , 105 , 77 , 73 ) 1-01-01<br>( 109 , 105 , 77 , 74 ) 10-101-<br>( 107 , 106 , 75 , 74 ) 10-110-<br>( 107 , 106 , 75 , 74 ) 10-1-10<br>( 110 , 106 , 78 , 74 ) 1-01-10<br>( 110 , 106 , 78 , 74 ) 1-01-10<br>( 110 , 106 , 78 , 74 ) 1-01-10  |                   | (103, 99, 71, 67) 1-00-11       |
| (79, 77, 71, 69) 100-1-1<br>(87, 85, 71, 69) 10-01-1<br>(103, 101, 71, 69) 1-001-1<br>(93, 85, 77, 69) 10101<br>(109, 101, 77, 69) 1-0-101<br>(79, 78, 71, 70) 100-11-<br>(87, 86, 71, 70) 10-011-<br>(103, 102, 71, 70) 1-0011-<br>(94, 86, 78, 70) 10110<br>(110, 102, 78, 70) 10110<br>(79, 77, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 10-10-1<br>(93, 89, 77, 73) 10-10-1<br>(93, 89, 77, 73) 10-10-1<br>(109, 105, 77, 73) 10-10-1<br>(109, 105, 77, 74) 10-101-<br>(91, 90, 75, 74) 10-101-<br>(107, 106, 75, 74) 10-110-<br>(107, 106, 75, 74) 10-1-10<br>(110, 106, 78, 74) 1-01-10<br>(110, 106, 78, 74) 1-01-10   |                   |                                 |
| (87, 85, 71, 69) 10-01-1<br>(103, 101, 71, 69) 1-001-1<br>(93, 85, 77, 69) 10101<br>(109, 101, 77, 69) 1-0-101<br>(79, 78, 71, 70) 100-11-<br>(87, 86, 71, 70) 10-011-<br>(103, 102, 71, 70) 1-0011-<br>(94, 86, 78, 70) 10110<br>(110, 102, 78, 70) 10110<br>(110, 102, 78, 70) 10-110<br>(79, 77, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 1-010-1<br>(93, 89, 77, 73) 1-01-01<br>(109, 105, 77, 73) 1-01-01<br>(109, 105, 77, 74) 10-110-<br>(107, 106, 75, 74) 10-101-<br>(94, 90, 78, 74) 10-1-10<br>(110, 106, 78, 74) 1-01-10<br>(110, 106, 78, 74) 1-01-10  |                   |                                 |
| 3  |                   |                                 |
| (109, 101, 77, 69) 1-0-101<br>(79, 78, 71, 70) 100-11-<br>(87, 86, 71, 70) 10-011-<br>(103, 102, 71, 70) 1-0011-<br>(94, 86, 78, 70) 10110<br>(110, 102, 78, 70) 1-0-110<br>(79, 77, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 1-010-1<br>(93, 89, 77, 73) 10-1-01<br>(109, 105, 77, 73) 1-01-01<br>(79, 78, 75, 74) 1001-1-<br>(91, 90, 75, 74) 10-101-<br>(107, 106, 75, 74) 10-1-10<br>(107, 106, 78, 74) 1-01-10<br>(110, 106, 78, 74) 1-01-10<br>(110, 106, 78, 77, 76) 10011   | 3                 | ( 103 , 101 , 71 , 69 ) 1-001-1 |
| (79, 78, 71, 70) 100-11-<br>(87, 86, 71, 70) 10-011-<br>(103, 102, 71, 70) 1-0011-<br>(94, 86, 78, 70) 10110<br>(110, 102, 78, 70) 1-0-110<br>(79, 77, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 1-010-1<br>(93, 89, 77, 73) 10-1-01<br>(109, 105, 77, 73) 1-01-01<br>(109, 105, 77, 73) 1-01-01<br>(79, 78, 75, 74) 10-101-<br>(91, 90, 75, 74) 10-101-<br>(107, 106, 75, 74) 10-1-10<br>(100, 106, 78, 74) 1-01-10<br>(110, 106, 78, 74) 1-01-10<br>(79, 78, 77, 76) 10011   |                   |                                 |
| (87,86,71,70)10-011-<br>(103,102,71,70)1-0011-<br>(94,86,78,70)10110<br>(110,102,78,70)1-0-110<br>(79,77,75,73)10011<br>(91,89,75,73)10-10-1<br>(107,105,75,73)10-10-1<br>(93,89,77,73)10-1-01<br>(109,105,77,73)1-01-01<br>(109,105,77,73)1-01-01<br>(79,78,75,74)1001-1-<br>(91,90,75,74)10-101-<br>(107,106,75,74)10-1-10<br>(100,106,78,74)1-01-10<br>(110,106,78,74)1-01-10<br>(79,78,77,76)10011   |                   |                                 |
| (103,102,71,70)1-0011-<br>(94,86,78,70)10110<br>(110,102,78,70)1-0-110<br>(79,77,75,73)10011<br>(91,89,75,73)10-10-1<br>(107,105,75,73)1-010-1<br>(93,89,77,73)10-1-01<br>(109,105,77,73)1-01-01<br>(109,105,77,73)1-01-01<br>(79,78,75,74)1001-1-<br>(91,90,75,74)10-101-<br>(107,106,75,74)10-110-<br>(94,90,78,74)10-1-10<br>(110,106,78,74)1-01-10<br>(79,78,77,76)10011   |                   |                                 |
| (94, 86, 78, 70) 10110<br>(110, 102, 78, 70) 1-0-110<br>(79, 77, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 1-010-1<br>(93, 89, 77, 73) 10-1-01<br>(109, 105, 77, 73) 1-01-01<br>(79, 78, 75, 74) 1001-1-<br>(91, 90, 75, 74) 10-101-<br>(107, 106, 75, 74) 10-1-10<br>(94, 90, 78, 74) 10-1-10<br>(110, 106, 78, 74) 1-01-10<br>(79, 78, 77, 76) 10011   |                   |                                 |
| (79, 77, 75, 73) 10011<br>(91, 89, 75, 73) 10-10-1<br>(107, 105, 75, 73) 1-010-1<br>(93, 89, 77, 73) 10-1-01<br>(109, 105, 77, 73) 1-01-01<br>(79, 78, 75, 74) 1001-1-<br>(91, 90, 75, 74) 10-101-<br>(107, 106, 75, 74) 1-0101-<br>(94, 90, 78, 74) 10-1-10<br>(110, 106, 78, 74) 1-01-10<br>(79, 78, 77, 76) 10011   |                   | ( 94 , 86 , 78 , 70 ) 10110     |
| (91,89,75,73)10-10-1<br>(107,105,75,73)1-010-1<br>(93,89,77,73)10-1-01<br>(109,105,77,73)1-01-01<br>(79,78,75,74)1001-1-<br>(91,90,75,74)10-101-<br>(107,106,75,74)1-0101-<br>(94,90,78,74)10-1-10<br>(110,106,78,74)1-01-10<br>(79,78,77,76)10011   |                   |                                 |
| ( 107 , 105 , 75 , 73 ) 1-010-1<br>( 93 , 89 , 77 , 73 ) 10-1-01<br>( 109 , 105 , 77 , 73 ) 1-01-01<br>( 79 , 78 , 75 , 74 ) 1001-1-<br>( 91 , 90 , 75 , 74 ) 10-101-<br>( 107 , 106 , 75 , 74 ) 1-0101-<br>( 94 , 90 , 78 , 74 ) 10-1-10<br>( 110 , 106 , 78 , 74 ) 1-01-10<br>( 79 , 78 , 77 , 76 ) 10011  |                   |                                 |
| (93,89,77,73)10-1-01<br>(109,105,77,73)1-01-01<br>(79,78,75,74)1001-1-<br>(91,90,75,74)10-101-<br>(107,106,75,74)1-0101-<br>(94,90,78,74)10-1-10<br>(110,106,78,74)1-01-10<br>(79,78,77,76)10011   |                   |                                 |
| (109, 105, 77, 73) 1-01-01<br>(79, 78, 75, 74) 1001-1-<br>(91, 90, 75, 74) 10-101-<br>(107, 106, 75, 74) 1-0101-<br>(94, 90, 78, 74) 10-1-10<br>(110, 106, 78, 74) 1-01-10<br>(79, 78, 77, 76) 10011   |                   |                                 |
| (79, 78, 75, 74) 1001-1-<br>(91, 90, 75, 74) 10-101-<br>(107, 106, 75, 74) 1-0101-<br>(94, 90, 78, 74) 10-1-10<br>(110, 106, 78, 74) 1-01-10<br>(79, 78, 77, 76) 10011   |                   |                                 |
| ( 107 , 106 , 75 , 74 ) 1-0101-<br>( 94 , 90 , 78 , 74 ) 10-1-10<br>( 110 , 106 , 78 , 74 ) 1-01-10<br>( 79 , 78 , 77 , 76 ) 10011   |                   | ( 79 , 78 , 75 , 74 ) 1001-1-   |
| (94,90,78,74)10-1-10<br>(110,106,78,74)1-01-10<br>(79,78,77,76)10011   |                   |                                 |
| ( 110 , 106 , 78 , 74 ) 1-01-10<br>( 79 , 78 , 77 , 76 ) 10011   |                   |                                 |
| (79,78,77,76)10011   |                   |                                 |
|  |                   |                                 |
|  |                   |                                 |

| Second Comparison | input   |
|-------------------|---|
| 3                 | (109, 108, 77, 76) 1-0110-<br>(94, 92, 78, 76) 10-11-0<br>(110, 108, 78, 76) 1-011-0<br>(87, 85, 83, 81) 10101<br>(91, 89, 83, 81) 10101<br>(87, 86, 83, 82) 1010-1-<br>(91, 90, 83, 82) 101-01-<br>(91, 90, 86, 82) 10110<br>(87, 86, 85, 84) 1010<br>(94, 90, 86, 82) 10110<br>(87, 86, 85, 84) 1010<br>(93, 92, 85, 84) 1011-0-<br>(94, 92, 86, 84) 10110<br>(93, 92, 89, 88) 10110<br>(93, 92, 89, 88) 1011-0-<br>(103, 101, 99, 97) 11001<br>(107, 105, 99, 98) 1100-1-<br>(107, 106, 99, 98) 1100-1-<br>(107, 106, 99, 98) 1100-1-<br>(101, 106, 102, 98) 11010<br>(103, 102, 101, 100) 11001<br>(109, 108, 101, 100) 110-10-<br>(107, 106, 105, 104) 11010<br>(107, 106, 105, 104) 11010<br>(107, 106, 105, 104) 11010<br>(109, 108, 105, 104) 11010<br>(107, 106, 105, 104) 11010<br>(107, 106, 105, 104) 11010<br>(109, 108, 105, 104) 11010 |





#### quine-mccluskey method of Next State $D_2$ (8/10)

| Second Comparison | input  |
|-------------------|--|
| 4                 | (63,59,55,51)01111<br>(63,61,55,53)011-1-1<br>(63,62,55,54)011-11-<br>(63,61,59,57)01111<br>(63,62,59,58)0111-1-<br>(63,62,61,60)01111<br>(95,87,79,71)10111<br>(111,103,79,71)1-0-111<br>(111,107,79,75)10-1-11<br>(111,107,79,75)10-1-11<br>(111,109,79,77)10-11-1<br>(111,109,79,77)1-011-1<br>(111,110,79,78)10-111-<br>(111,110,79,78)10-111-<br>(111,110,79,78)10-111-<br>(111,110,79,78)10-111-<br>(111,110,79,78)10-111-<br>(111,110,79,78)1011<br>(111,110,103,99)1011<br>(111,109,103,101)11011<br>(111,109,103,101)110-1-1<br>(111,110,103,102)110-11-<br>(111,110,107,106)11011<br>(111,110,107,106)1101 |





#### quine-mccluskey method of Next State $D_2$ (9/10)

#### **Prime Implicants**

(67.66.65.64) 10000--(69,68,65,64)1000-0-(73,72,65,64)100-00-(81,80,65,64)10-000-(97.96.65.64) 1-0000-(70,68,66,64)1000--0 (74,72,66,64)100-0-0 (82,80,66,64)10-00-0 (98.96.66.64) 1-000-0 (76,72,68,64)100--00 (84.80.68.64)10-0-00 (100,96,68,64)1-00-00 (88, 80, 72, 64) 10--000 (104, 96, 72, 64) 1-0-000 (51,50,49,48)01100--(53 . 52 . 49 . 48 ) 0110-0-(57,56,49,48)011-00-(54,52,50,48)0110--0 (58, 56, 50, 48) 011-0-0 (60,56,52,48)011--00 (71,69,67,65)1000--1 (75,73,67,65)100-0-1 (83,81,67,65)10-00-1 (99, 97, 67, 65) 1-000-1 (77,73,69,65)100--01 (85 . 81 . 69 . 65 ) 10-0-01 (101, 97, 69, 65) 1-00-01 (89,81,73,65)10--001 (105, 97, 73, 65) 1-0-001 (71,70,67,66)1000-1-(75 . 74 . 67 . 66 ) 100-01-(83,82,67,66)10-001-(99, 98, 67, 66) 1-0001-(78,74,70,66)100—10 (86,82,70,66)10-0-10 (102, 98, 70, 66) 1-00-10 (90, 82, 74, 66) 10--010 (106, 98, 74, 66) 1-0-010 (71,70,69,68)10001--(77.76.69.68) 100-10(85,84,69,68)10-010-101 . 100 . 69 . 68 ) 1-0010-( 78 , 76 , 70 , 68 ) 100-1-0 (86,84,70,68)10-01-0 102,100,70,68)1-001-0 (92,84,76,68)10--100 ( 108 . 100 . 76 . 68 ) 1-0-100 (75,74,73,72)10010--(77,76,73,72)1001-0-(89, 88, 73, 72) 10-100-105 . 104 . 73 . 72 ) 1-0100-(78,76,74,72)1001--0 90,88,74,72)10-10-0 106, 104, 74, 72) 1-010-0 92,88,76,72)10-1-00 ( 108 , 104 , 76 , 72 ) 1-01-00 〔83 . 82 . 81 . 80 **) 10100--**(85,84,81,80)1010-0-(89, 88, 81, 80) 101-00-86,84,82,80)1010--0 90,88,82,80)101-0-0 92 . 88 . 84 . 80 ) 101--00 「99,98,97,96)11000--101, 100, 97, 96) 1100-0-105 , 104 , 97 , 96 ) 110-00-102 . 100 . 98 . 96 ) 1100--0 106, 104, 98, 96) 110-0-0 108, 104, 100, 96) 110--00 55, 53, 51, 49) 0110--1 59, 57, 51, 49) 011-0-1 (61,57,53,49)011--01 55 . 54 . 51 . 50 ) 0110-1-59, 58, 51, 50) 011-01-62,58,54,50)011--10 55 , 54 , 53 , 52 ) 01101--(61,60,53,52)011-10-(62.60.54.52)011-1-0 <sup>\*</sup>59 , 58 , 57 , 56 ) 01110--(61,60,57,56)0111-0-(62,60,58,56)0111--0 (79,75,71,67)100--11 (87,83,71,67)10-0-11

(103, 99, 71, 67) 1-00-11 (91,83,75,67)10--011 (107, 99, 75, 67) 1-0-011 (79.77.71.69)100-1-1 (87,85,71,69)10-01-1 (103 . 101 . 71 . 69 ) 1-001-1 ( 93 , 85 , 77 , 69 ) 10--101 (109, 101, 77, 69) 1-0-101 (79,78,71,70)100-11-(87.86.71.70)10-011-(103, 102, 71, 70) 1-0011-(94,86,78,70)10--110 (110, 102, 78, 70) 1-0-110 (79,77,75,73)1001--1 (91.89.75.73)10-10-1 ( 107 . 105 . 75 . 73 ) 1-010-1 (93, 89, 77, 73) 10-1-01 (109, 105, 77, 73) 1-01-01 (79.78.75.74)1001-1-(91,90,75,74)10-101-(107.106.75.74)1-0101-( 94 , 90 , 78 , 74 ) 10-1-10 (110, 106, 78, 74) 1-01-10 (79, 78, 77, 76) 10011--( 93 . 92 . 77 . 76 ) 10-110-(109, 108, 77, 76) 1-0110-(94,92,78,76)10-11-0 (110, 108, 78, 76) 1-011-0 (87,85,83,81)1010--1 (91,89,83,81)101-0-1 ( 93 , 89 , 85 , 81 ) 101--01 (87,86,83,82)1010-1-(91,90,83,82)101-01-(94,90,86,82)101--10 (87,86,85,84)10101--(93.92.85.84)101-10-(94,92,86,84)101-1-0 (91,90,89,88)10110--(93,92,89,88)1011-0-

(94,92,90,88)1011--0 ( 103 . 101 . 99 . 97 ) 1100--1 107, 105, 99, 97) 110-0-1 (109, 105, 101, 97) 110--01 103 , 102 , 99 , 98 ) 1100-1-107, 106, 99, 98) 110-01-(110.106.102.98)110--10 103 , 102 , 101 , 100 ) 11001--109, 108, 101, 100) 110-10-(110, 108, 102, 100) 110-1-0 ( 107 . 106 . 105 . 104 ) 11010--109, 108, 105, 104) 1101-0-(110, 108, 106, 104) 1101--0 63, 59, 55, 51) 011--11 (63,61,55,53)011-1-1 63 . 62 . 55 . 54 ) 011-11-´63 . 61 . 59 . 57 ) 0111--1 (63,62,59,58)0111-1-63,62,61,60)01111--95, 87, 79, 71) 10--111 ( 111 , 103 , 79 , 71 ) 1-0-111 95 . 91 . 79 . 75 ) 10-1-11 (111,107,79,75)1**-01-**11 95,93,79,77)10-11-1 (111, 109, 79, 77) 1-011-1 95, 94, 79, 78) 10-111-( 111 , 110 , 79 , 78 ) 1-0111-95, 91, 87, 83) 101--11 95, 93, 87, 85) 101-1-1 95,94,87,86)101-11-95, 93, 91, 89) 1011--1 95,94,91,90)1011-1-95, 94, 93, 92) 10111--(111, 107, 103, 99) 110--11 (111, 109, 103, 101) 110-1-1 (111, 110, 103, 102) 110-11-(111 . 109 . 107 . 105 ) 1101--1 (111, 110, 107, 106) 1101-1-(111, 110, 109, 108) 11011--





#### quine-mccluskey method of Next State $D_2$ (10/10)

#### part of table

|    | 01100 | 0110-0- | 011-00- | 01100 | 011-0-0 | 01100 | 01101 | 011-0-1 | 01101 | 0110-1- | 011-01- | 01110 | 01101 | 011-10- | 011-1-0 | 01111 | 011-1-1 | 011-11 |
|----|-------|---------|---------|-------|---------|-------|-------|---------|-------|---------|---------|-------|-------|---------|---------|-------|---------|--------|
| 48 | Χ     | Χ       | Χ       | Χ     | Χ       | Χ     |       |         |       |         |         |       |       |         |         |       |         |        |
| 49 | Χ     | Х       | Х       |       |         |       | Χ     | Χ       | Χ     |         |         |       |       |         |         |       |         |        |
| 50 | Χ     |         |         | Х     | Χ       |       |       |         |       | Х       | Х       | Х     |       |         |         |       |         |        |
| 51 | Х     |         |         |       |         |       | Х     | Х       |       | Х       | Х       |       |       |         |         | Х     |         |        |
| 52 |       | Х       |         | Х     |         | Х     |       |         |       |         |         |       | Х     | Х       | Х       |       |         |        |
| 53 |       | Х       |         |       |         |       | Х     |         | Х     |         |         |       | Х     | Х       |         |       | Х       |        |
| 54 |       |         |         | Х     |         |       |       |         |       | Х       |         | Х     | Х     |         | Х       |       |         | Х      |

•

$$D_2 = \overline{Q_2}Q_1Q_0 + Q_2\overline{Q_1} + Q_2Q_1\overline{Q_0}$$

$$D1, D0 = ?$$





# **Output Table**

| State | $L_A$  | $L_B$  |
|-------|--------|--------|
| S0    | Green  | Red    |
| S1    | Yellow | Red    |
| S2    | Left   | Red    |
| S3    | Yellow | Red    |
| S4    | Red    | Green  |
| S5    | Red    | Yellow |
| S6    | Red    | Left   |
| S7    | Red    | Yellow |

| Color  | Code |
|--------|------|
| Green  | 00   |
| Yellow | 01   |
| Left   | 10   |
| Red    | 11   |





# **Output Encoded Table**

| $Q_2$ | $Q_1$ | $Q_0$ | $L_{A1}$ | $L_{A0}$ | $L_{B1}$ | $L_{B0}$ |
|-------|-------|-------|----------|----------|----------|----------|
| 0     | 0     | 0     | 0        | 0        | 1        | 1        |
| 0     | 0     | 1     | 0        | 1        | 1        | 1        |
| 0     | 1     | 0     | 1        | 0        | 1        | 1        |
| 0     | 1     | 1     | 0        | 1        | 1        | 1        |
| 1     | 0     | 0     | 1        | 1        | 0        | 0        |
| 1     | 0     | 1     | 1        | 1        | 0        | 1        |
| 1     | 1     | 0     | 1        | 1        | 1        | 0        |
| 1     | 1     | 1     | 1        | 1        | 0        | 1        |

$$L_{A1} = L_{A0} = L_{B1} = L_{B0} = L_{B0}$$





| $Q_2$ | $Q_1$ | $Q_0$ | $L_{A1}$ |
|-------|-------|-------|----------|
| 0     | 0     | 0     | 0        |
| 0     | 0     | 1     | 0        |
| 0     | 1     | 0     | 1        |
| 0     | 1     | 1     | 0        |
| 1     | 0     | 0     | 1        |
| 1     | 0     | 1     | 1        |
| 1     | 1     | 0     | 1        |
| 1     | 1     | 1     | 1        |



|   | 00 | 01 | 11 | 10 |
|---|----|----|----|----|
| 0 | 0  | 0  | 0  | 1  |
| 1 | 1  | 1  | 1  | 1  |

가로는 각각  $Q_1,Q_0$ 타내며, 세로는  $Q_2$ 를 나타낸다.





| $Q_2$ | $Q_1$ | $Q_0$ | $L_{A0}$ |
|-------|-------|-------|----------|
| 0     | 0     | 0     | 0        |
| 0     | 0     | 1     | 1        |
| 0     | 1     | 0     | 0        |
| 0     | 1     | 1     | 1        |
| 1     | 0     | 0     | 1        |
| 1     | 0     | 1     | 1        |
| 1     | 1     | 0     | 1        |
| 1     | 1     | 1     | 1        |



|   | 00 | 01 | 11 | 10 |
|---|----|----|----|----|
| 0 | 0  | 1  | 1  | 0  |
| 1 | 1  | 1  | 1  | 1  |

가로는 각각  $Q_1, Q_0$ 타내며, 세로는  $Q_2$ 를 나타낸다.





| $Q_2$ | $Q_1$ | $Q_0$ | $L_{B1}$ |
|-------|-------|-------|----------|
| 0     | 0     | 0     | 1        |
| 0     | 0     | 1     | 1        |
| 0     | 1     | 0     | 1        |
| 0     | 1     | 1     | 1        |
| 1     | 0     | 0     | 0        |
| 1     | 0     | 1     | 0        |
| 1     | 1     | 0     | 1        |
| 1     | 1     | 1     | 0        |

$$L_{B1} =$$

|   | 00 | 01 | 11 | 10 |
|---|----|----|----|----|
| 0 | 1  | 1  | 1  | 1  |
| 1 | 0  | 0  | 0  | 1  |

가로는 각각  $Q_1,Q_0$ 타내며, 세로는  $Q_2$ 를 나타낸다.





| $Q_2$ | $Q_1$ | $Q_0$ | $L_{B0}$ |
|-------|-------|-------|----------|
| 0     | 0     | 0     | 1        |
| 0     | 0     | 1     | 1        |
| 0     | 1     | 0     | 1        |
| 0     | 1     | 1     | 1        |
| 1     | 0     | 0     | 0        |
| 1     | 0     | 1     | 1        |
| 1     | 1     | 0     | 0        |
| 1     | 1     | 1     | 1        |



|   | 00 | 01 | 11 | 10 |
|---|----|----|----|----|
| 0 | 1  | 1  | 1  | 1  |
| 1 | 0  | 1  | 1  | 0  |

가로는 각각  $Q_1,Q_0$ 타내며, 세로는  $Q_2$ 를 나타낸다.





# **Module Configuration**

| 구분         | 이름             | 설명   |
|------------|----------------|--|
| Top module | tl_cntr_w_left | Traffic light controller의 top module   |
| Sub module | ns_logic       | Traffic light controller의 next state를 결정하는 combinati<br>onal logic   |
| Sub module | _register3_r   | 3-bit resettable register with active low asynchronous res<br>et module(내부에 d_ff_r_async를 instance)<br>- 현재의 state 값을 저장 |
| Sub module | _dff_r         | Resettable D flip-flop with active low asynchronous reset  |
| Sub module | o_logic        | 현재 state의 값에 기반하여 output 값을 결정하는 combin<br>ational logic   |





# I/O Configuration

| 구분     | 이름      | 비트 수  | 설명  |
|--------|---------|-------|---|
| input  | clk     | 1-bit | Clock   |
|        | reset_n | 1-bit | Active low에 동작하는 reset 신호로 state를 초기화               |
|        | Та      | 1-bit | Traffic sensor A('Academic Ave.'에 위치하여 직진 감지)       |
|        | Tal     | 1-bit | Traffic sensor AL('Academic Ave.'에 위치하여 좌회전<br>감지)  |
|        | Tb      | 1-bit | Traffic sensor B('Bravado Blvd.'에 위치하여 직진 감지)       |
|        | Tbl     | 1-bit | Traffic sensor BL('Bravado Blvd.'에 위치하여 좌회전 감<br>지) |
| output | La      | 2-bit | 신호등 값 출력 A('Academic Ave'에 위치)                      |
|        | Lb      | 2-bit | 신호등 값 출력 B('Bravado Blvd.'에 위치)                     |





#### **Assignment 5**

- Report
  - ✓ 자세한 사항은 lab document 참고
- Submission
  - ✓ Soft copy
    - 기한: 강의 당일부터 2주 (KLAS 과제란 참고)
    - 실습 미수강은 디지털 논리2 조교 공지에 따름
    - 늦은 숙제는 이틀 후 까지만 받음(20% 감점)





# 채점기준

| 세부사항          |  |     | 최<br>상 | 상  | 중  | 하 | 최<br>하 |
|---------------|--|-----|--------|----|----|---|--------|
| 소스코드          | Source code가 잘 작성 되었는가?<br>(Structural design으로 작성되었는가?) | 10  | 10     | 8  | 5  | 3 | 0      |
|               | 주석을 적절히 달았는가?  |     | 20     | 15 | 10 | 5 | 0      |
| 설계검증<br>(보고서) | 보고서를 성실히 작성하였는가?<br>(보고서 형식에 맞추어 작성)                     | 30  | 30     | 20 | 10 | 5 | 0      |
|               | 합성결과를 설명하였는가?  | 10  | 10     | 8  | 5  | 3 | 0      |
|               | 검증을 제대로 수행하였는가?<br>(모든 입력 조합, waveform 설명)               |     | 30     | 20 | 10 | 5 | 0      |
| 총점            |  | 100 |        |    |    |   |        |





#### References

- Altera Co., <u>www.altera.com/</u>
- D. M. Harris and S. L. Harris, Digital Design and Computer Architecture, Morgan Kaufmann, 2007
- ▶ 이준환, 디지털논리회로2 강의자료, 광운대학교, 컴퓨터 공학과, 2012





Q&A

Thank you



