

# Lógica Fuzzy com Python: O guia para Iniciantes: Exemplo do aspirador de pó

## Antecedentes (entradas)

Superfície: qual nível de dificuldade da superfície, em uma escala de 0 a 5?

- fácil, moderada, difícil

Sujeira: qual a quantidade de sujeira, em uma escala de 0 a 5?

- leve, moderada, pesada

## Consequente (saída)

Sucção: qual o nível de sucção que o aspirador de pó deve ser configurado, entre 0% e 10%?

- baixa, média, alta

regras

- se a superfície for fácil e a sujeira for leve então a sucção será baixa
- se a superfície for moderada e a sujeira for leve então a sucção será média
- se a superfície for difícil ou a sujeira for pesada então a sucção será alta
- se a superfície for moderada então a sucção será média

## instalação e importação das bibliotecas

- Documentação: <https://pythonhosted.org/scikit-fuzzy/overview.html>

```
In [89]: import numpy as np
import skfuzzy as fuzz
from skfuzzy import control as ctrl
import matplotlib
```

## Antecedentes e consequentes

```
In [90]: superficie = ctrl.Antecedent(np.arange(0,6,1), 'superficie')
sujeira = ctrl.Antecedent(np.arange(0,6,1), 'sujeira')
```

```
In [91]: superficie
```

```
Out[91]: Antecedent: superficie
```

```
In [92]: superficie.universe
```

```
Out[92]: array([0, 1, 2, 3, 4, 5])
```

```
In [93]: sujeira
```

```
Out[93]: Antecedent: sujeira
```

```
In [94]: sujeira.universe
```

```
Out[94]: array([0, 1, 2, 3, 4, 5])
```

```
In [95]: succao = ctrl.Consequent(np.arange(0,11,1),"succao")
```

```
In [96]: succao.universe
```

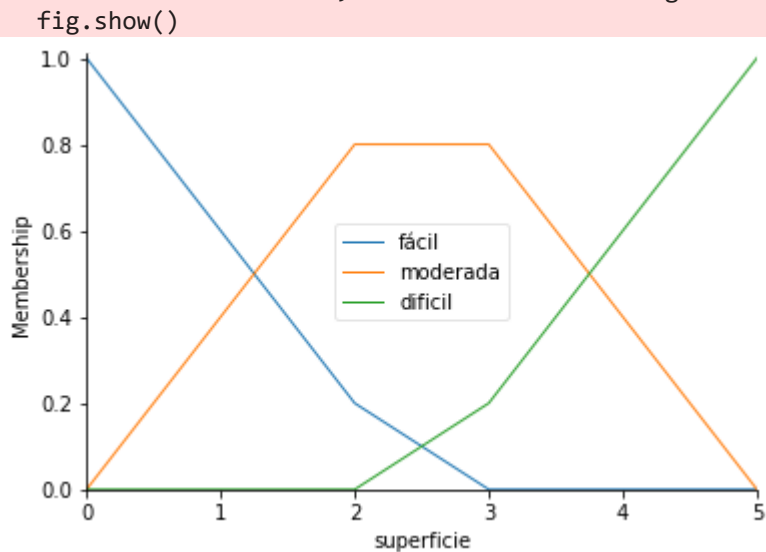
```
Out[96]: array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10])
```

## Membership functions

```
In [97]: superficie.automf(number=3, names=['fácil', 'moderada', 'difícil'])  
sujeira.automf(number=3, names=['leve', 'moderada', 'pesada'])
```

```
In [98]: superficie.view()
```

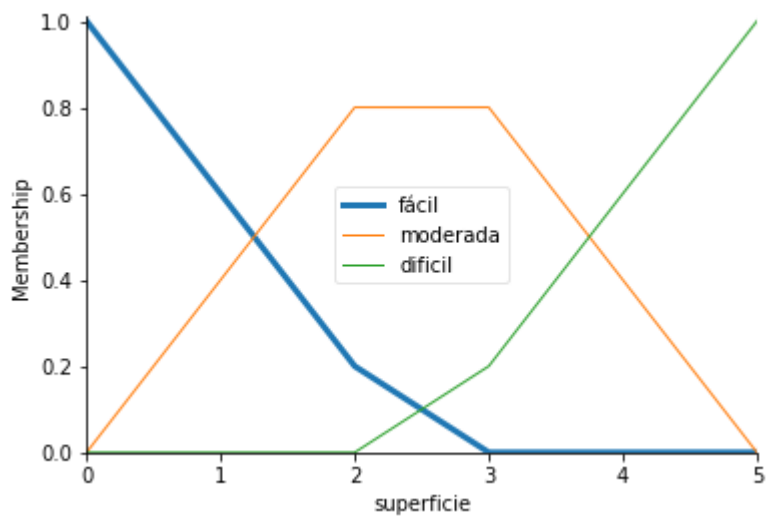
C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\fuzzyvariable.py:122: UserWarning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.



```
In [99]: superficie['fácil'].view()
```

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\term.py:74: UserWarning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

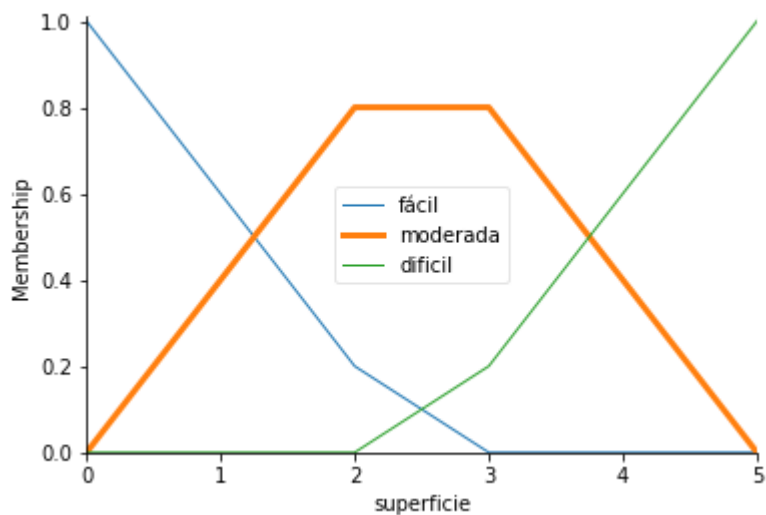
fig.show()



```
In [100...] superficie['moderada'].view()
```

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\term.py:74: UserWarning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

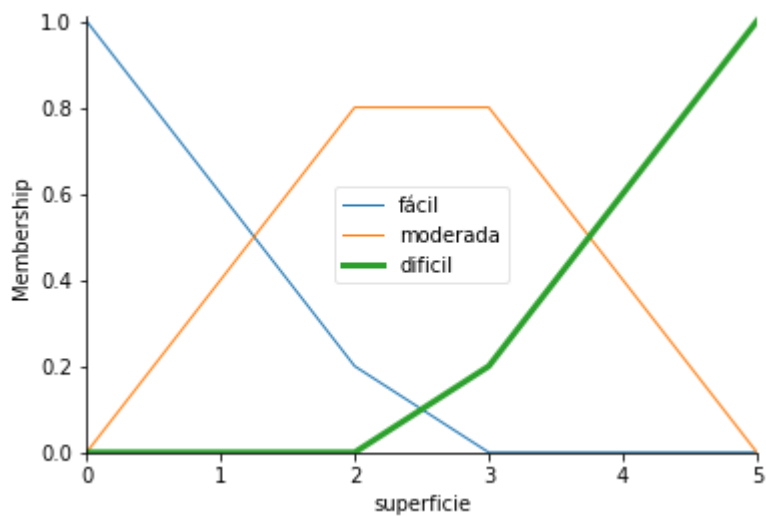
```
fig.show()
```



```
In [101...] superficie['difícil'].view()
```

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\term.py:74: UserWarning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

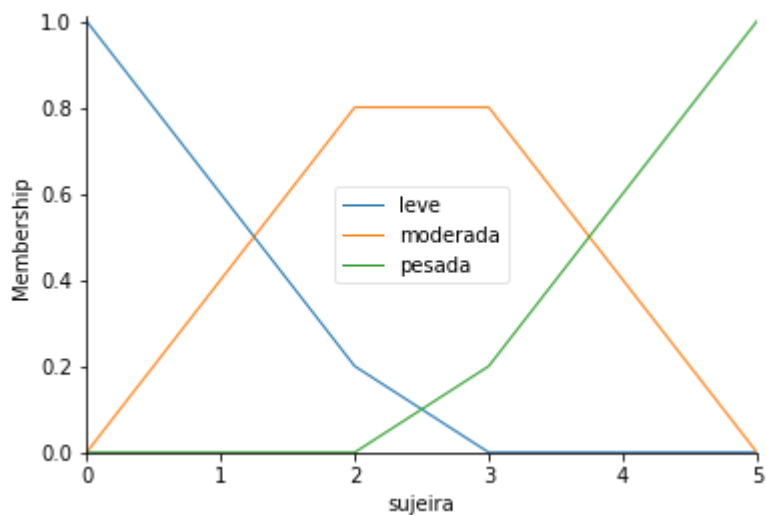
```
fig.show()
```



In [102... `sujeira.view()`

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\fuzzyvariable.py:122: UserWarning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

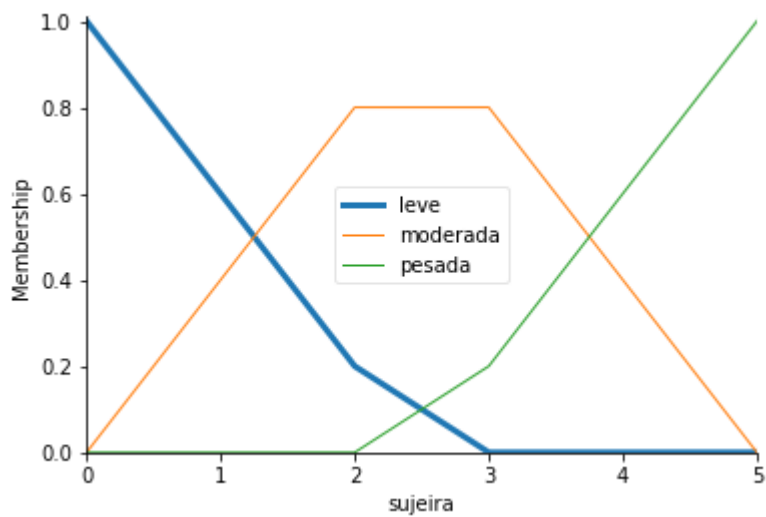
`fig.show()`



In [103... `sujeira['leve'].view()`

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\term.py:74: UserWarning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

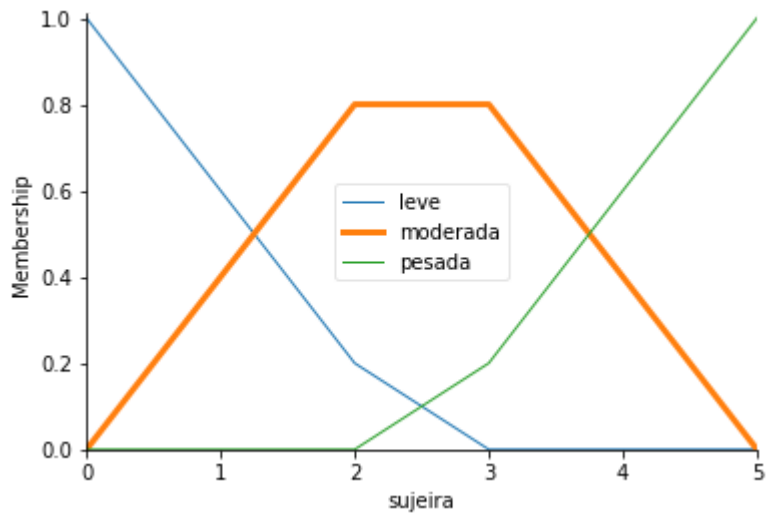
`fig.show()`



In [104... `sujeira['moderada'].view()`

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\term.py:74: UserWarning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

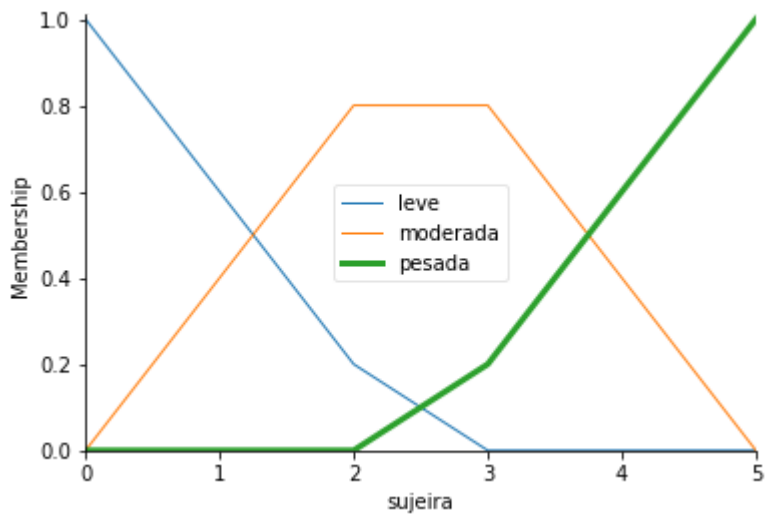
`fig.show()`



In [105... `sujeira['pesada'].view()`

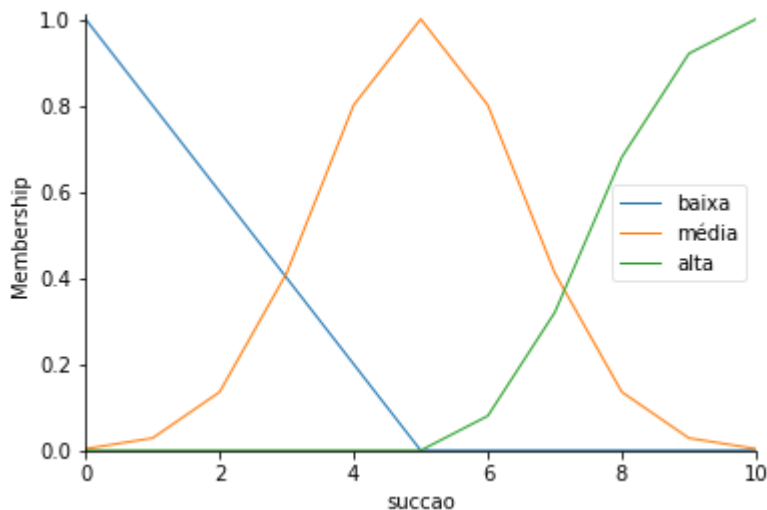
C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\term.py:74: UserWarning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

`fig.show()`



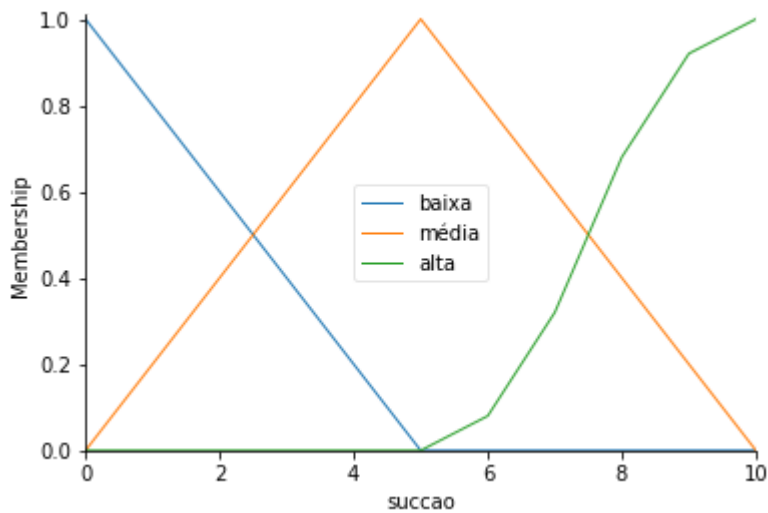
```
In [129...] succao['baixa'] = fuzz.trimf(succao.universe,[0,0,5])
succao.view()
```

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\fuzzyvariable.py:122: User Warning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.  
fig.show()



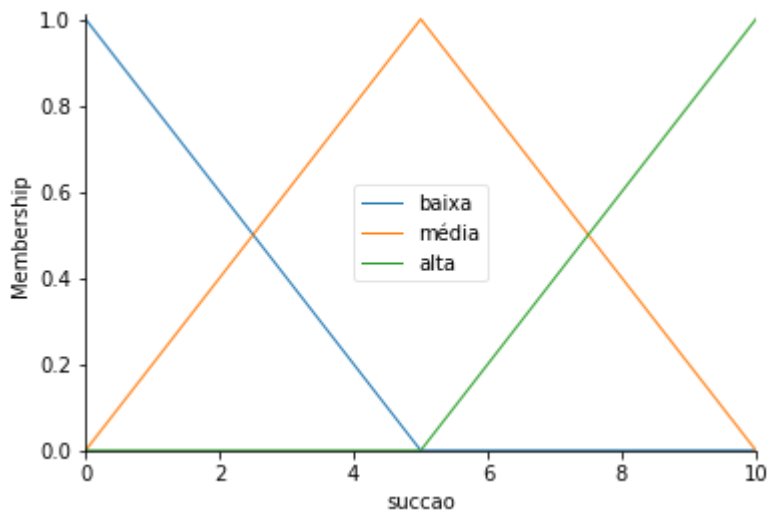
```
In [131...] succao['média'] = fuzz.trimf(succao.universe,[0,5,10])
succao.view()
```

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\fuzzyvariable.py:122: User Warning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.  
fig.show()



```
In [132...] succao['alta'] = fuzz.trimf(succao.universe, [5,10,10])
succao.view()
```

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\fuzzyvariable.py:122: User Warning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.  
fig.show()



```
In [133...] regra1 = ctrl.Rule(superficie['fácil'] | sujeira['leve'], succao['baixa'])
regra2 = ctrl.Rule(superficie['moderada'] | sujeira['leve'], succao['média'])
regra3 = ctrl.Rule(superficie['difícil'] | sujeira['pesada'], succao['alta'])
#regra4 = ctrl.Rule(superficie['moderada'], succao['média'])
```

## Sistema de controle

```
In [134...] #sistema_controle = ctrl.ControlSystem([regra1,regra2,regra3, regra4])
sistema_controle = ctrl.ControlSystem([regra1,regra2,regra3])
```

```
In [135...] sistema = ctrl.ControlSystemSimulation(sistema_controle)
```

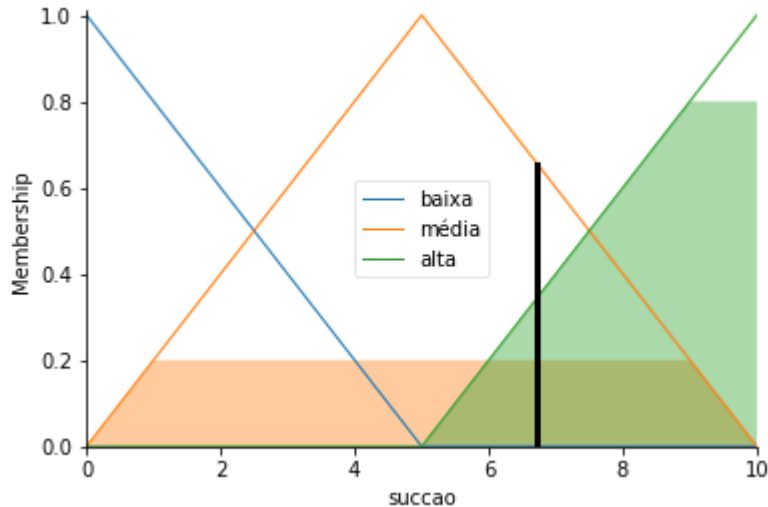
```
In [145...] sistema.input['superficie'] = 4.5
sistema.input['sujeira'] = 4
sistema.compute()
```

```
In [146... print(sistema.output['succao'])
succao.view(sim=sistema)
```

6.725490196078432

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\fuzzyvariable.py:122: User Warning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

fig.show()

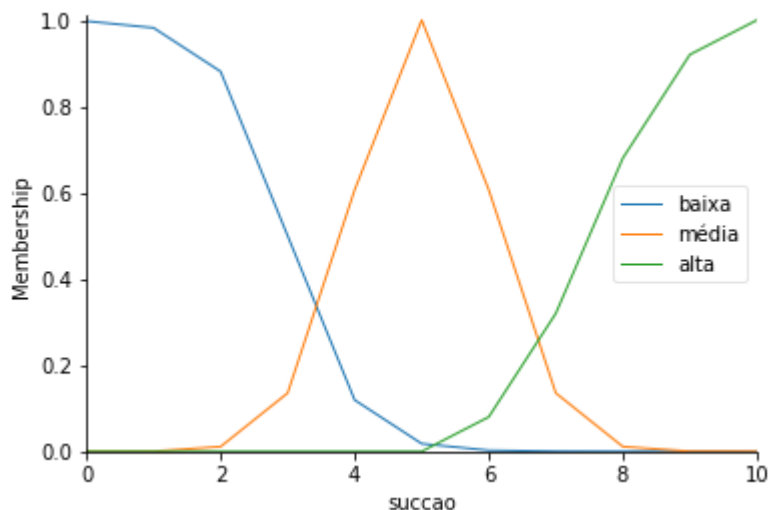


## Outras funções

```
In [147... succao['baixa'] = fuzz.sigmf(succao.universe,3,-2)
succao['média'] = fuzz.gaussmf(succao.universe, 5, 1)
succao['alta'] = fuzz.pimf(succao.universe,5,10,10,11)
succao.view()
```

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\fuzzyvariable.py:122: User Warning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.

fig.show()



```
In [148... regra1 = ctrl.Rule(superficie['fácil'] | sujeira['leve'], succao['baixa'])
regra2 = ctrl.Rule(superficie['moderada'] | sujeira['leve'], succao['média'])
```



```
regra3 = ctrl.Rule(superficie['difícil'] | sujeira['pesada'], succao['alta'])
#regra4 = ctrl.Rule(superficie['moderada'], succao['média'])
```

```
In [149...] #sistema_controle = ctrl.ControlSystem([regra1,regra2,regra3, regra4])
sistema_controle = ctrl.ControlSystem([regra1,regra2,regra3])
```

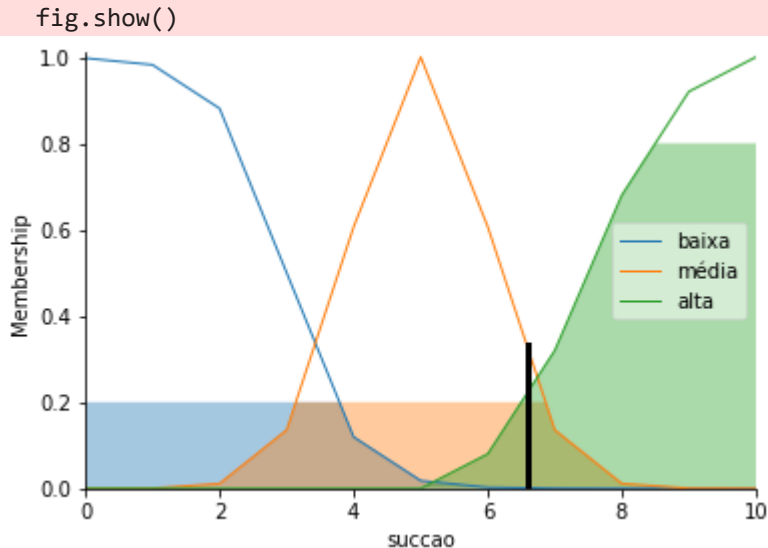
```
In [150...] sistema = ctrl.ControlSystemSimulation(sistema_controle)
```

```
In [153...] sistema.input['superficie'] = 4.5
sistema.input['sujeira'] = 2
sistema.compute()
```

```
In [154...] print(sistema.output['succao'])
succao.view(sim=sistema)
```

6.582062331030227

C:\Users\clist\anaconda3\lib\site-packages\skfuzzy\control\fuzzyvariable.py:122: User Warning: Matplotlib is currently using module://matplotlib\_inline.backend\_inline, which is a non-GUI backend, so cannot show the figure.



## HARD FUZZY

### instalação e inportação das bibliotecas

- Documentação: <https://pythonhosted.org/scikit-fuzzy/overview.html>

```
In [1]: import numpy as np
import skfuzzy as fuzz
from skfuzzy import control as ctrl
import matplotlib.pyplot as plt
```

### Antecedentes e consequentes

```
In [2]: x_superficie = np.arange(0,6,1)
x_sujeira = np.arange(0,6,1)
```

```
x_succao = np.arange(0,11,1)
```

```
In [3]: x_superficie, x_sujeira, x_succao
```

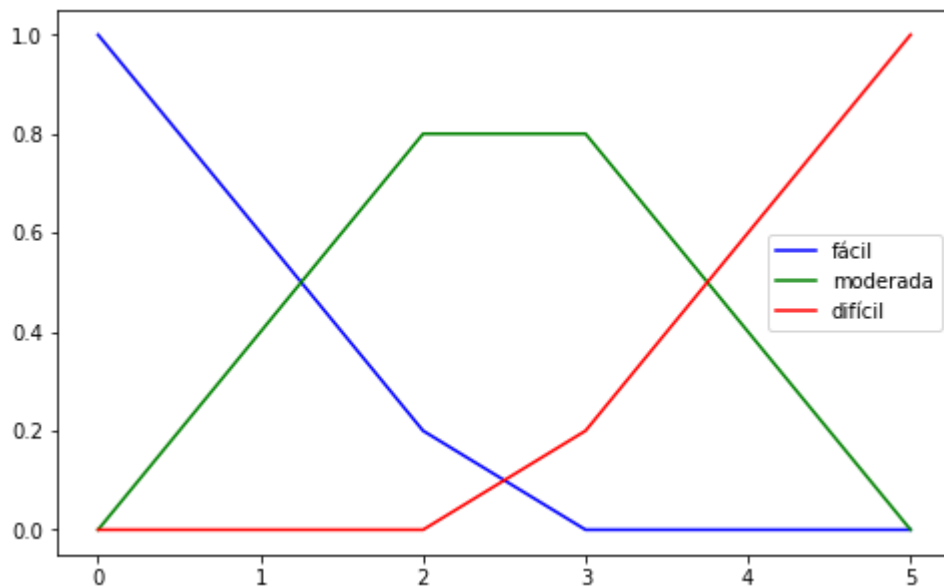
```
Out[3]: (array([0, 1, 2, 3, 4, 5]),  
        array([0, 1, 2, 3, 4, 5]),  
        array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10]))
```

## Tipo de superfície

```
In [4]: y_superficie_facil = fuzz.trimf(x_superficie, [0,0,2.5])  
        y_superficie_moderada = fuzz.trimf(x_superficie,[0,2.5,5])  
        y_superficie_dificil = fuzz.trimf(x_superficie, [2.5, 5,5])
```

```
In [10]: fig, ax = plt.subplots(figsize = (8,5))  
         ax.plot(x_superficie, y_superficie_facil, 'b', label="fácil")  
         ax.plot(x_superficie, y_superficie_moderada, 'g', label="moderada")  
         ax.plot(x_superficie, y_superficie_dificil, 'r', label="difícil")  
         ax.legend()
```

```
Out[10]: <matplotlib.legend.Legend at 0x174bf3dcf70>
```

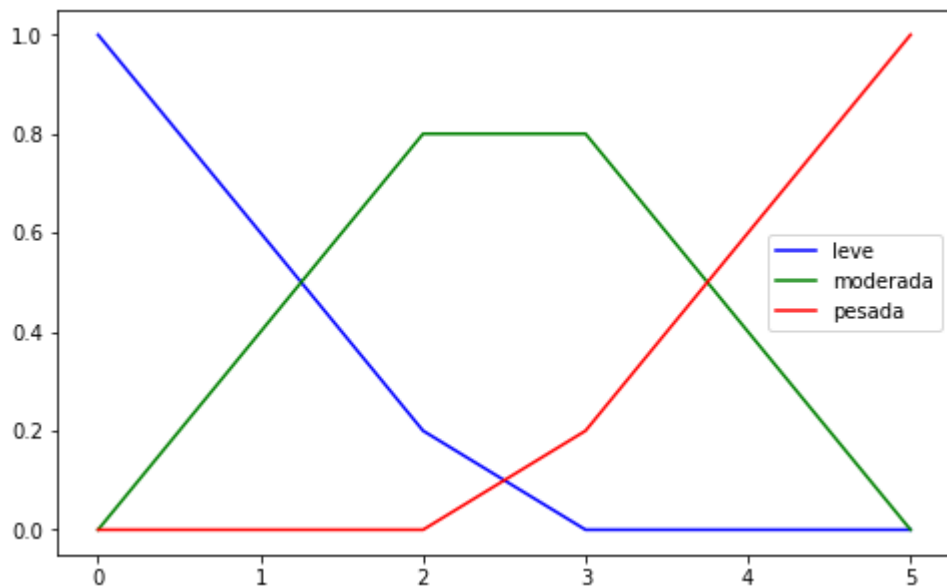


## Tipo de sujeira

```
In [11]: y_sujeira_leve = fuzz.trimf(x_sujeira, [0,0,2.5])  
         y_sujeira_moderada = fuzz.trimf(x_sujeira, [0,2.5,5])  
         y_sujeira_pesada = fuzz.trimf(x_sujeira, [2.5,5,5])
```

```
In [12]: fig, ax = plt.subplots(figsize = (8,5))  
         ax.plot(x_sujeira, y_sujeira_leve, 'b', label="leve")  
         ax.plot(x_sujeira, y_sujeira_moderada, 'g', label="moderada")  
         ax.plot(x_sujeira, y_sujeira_pesada, 'r', label="pesada")  
         ax.legend()
```

```
Out[12]: <matplotlib.legend.Legend at 0x174bf56ba90>
```

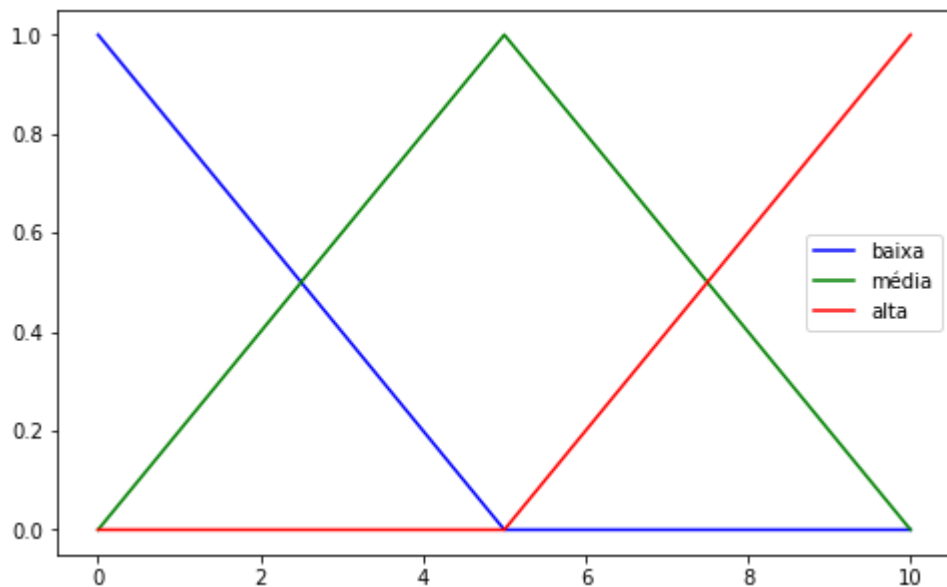


## Sucção

```
In [13]: y_succao_baixa = fuzz.trimf(x_succao,[0,0,5])
y_succao_media = fuzz.trimf(x_succao,[0,5,10])
y_succao_alta = fuzz.trimf(x_succao,[5,10,10])
```

```
In [14]: fig, ax = plt.subplots(figsize = (8,5))
ax.plot(x_succao, y_succao_baixa, 'b', label="baixa")
ax.plot(x_succao, y_succao_media, 'g', label="média")
ax.plot(x_succao, y_succao_alta, 'r', label="alta")
ax.legend()
```

```
Out[14]: <matplotlib.legend.Legend at 0x174bcac0fd0>
```



## Entradas (inputs)

```
In [21]: superficie_nivel_facil = fuzz.interp_membership(x_superficie, y_superficie_facil, 4.5)
superficie_nivel_moderada = fuzz.interp_membership(x_superficie, y_superficie_moderada,
```

```
superficie_nivel_dificil = fuzz.interp_membership(x_superficie, y_superficie_dificil,
```

```
In [22]: superficie_nivel_facil, superficie_nivel_moderada, superficie_nivel_dificil
```

```
Out[22]: (0.0, 0.2, 0.8)
```

```
In [23]: sujeira_nivel_leve = fuzz.interp_membership(x_sujeira, y_sujeira_leve,4.0)
sujeira_nivel_moderada = fuzz.interp_membership(x_sujeira, y_sujeira_moderada,4.0)
sujeira_nivel_pesada = fuzz.interp_membership(x_sujeira, y_sujeira_pesada,4.0)
```

```
In [24]: sujeira_nivel_leve, sujeira_nivel_moderada, sujeira_nivel_pesada
```

```
Out[24]: (0.0, 0.4, 0.6)
```

## Regra 1

- se a superfície for fácil e a sujeira for leve então a sucção será baixa

```
In [25]: superficie_nivel_facil, sujeira_nivel_leve
```

```
Out[25]: (0.0, 0.0)
```

```
In [26]: ativacao_regra1 = np.fmax(superficie_nivel_facil, sujeira_nivel_leve)
ativacao_regra1
```

```
Out[26]: 0.0
```

```
In [27]: ativacao_succao_baixa = np.fmin(ativacao_regra1, y_succao_baixa)
ativacao_succao_baixa
```

```
Out[27]: array([0., 0., 0., 0., 0., 0., 0., 0., 0., 0., 0.])
```

## Regra 2

- se a superfície for moderada e a sujeira for leve então a sucção será média

```
In [28]: superficie_nivel_moderada, sujeira_nivel_leve
```

```
Out[28]: (0.2, 0.0)
```

```
In [31]: ativacao_regra2 = np.fmax(superficie_nivel_moderada, sujeira_nivel_leve)
ativacao_regra2
```

```
Out[31]: 0.2
```

```
In [32]: y_succao_media
```

```
Out[32]: array([0. , 0.2, 0.4, 0.6, 0.8, 1. , 0.8, 0.6, 0.4, 0.2, 0. ])
```

```
In [34]: ativacao_succao_media = np.fmin(ativacao_regra2, y_succao_media)
ativacao_succao_media
```

```
Out[34]: array([0. , 0.2, 0.2, 0.2, 0.2, 0.2, 0.2, 0.2, 0.2, 0.2, 0. ])
```

## Regra 3

- se a superfície for difícil ou a sujeira for pesada então a sucção será alta

```
In [35]: superficie_nivel_dificil, sujeira_nivel_pesada
```

```
Out[35]: (0.8, 0.6)
```

```
In [37]: ativacao_regra3 = np.fmax(superficie_nivel_dificil, sujeira_nivel_pesada)
ativacao_regra3
```

```
Out[37]: 0.8
```

```
In [38]: y_succao_alta
```

```
Out[38]: array([0. , 0. , 0. , 0. , 0. , 0. , 0.2, 0.4, 0.6, 0.8, 1. ])
```

```
In [39]: ativacao_succao_alta = np.fmin(ativacao_regra3, y_succao_alta)
ativacao_succao_alta
```

```
Out[39]: array([0. , 0. , 0. , 0. , 0. , 0. , 0.2, 0.4, 0.6, 0.8, 0.8])
```

## Gráficos com as intersecções

```
In [40]: x_succao
```

```
Out[40]: array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10])
```

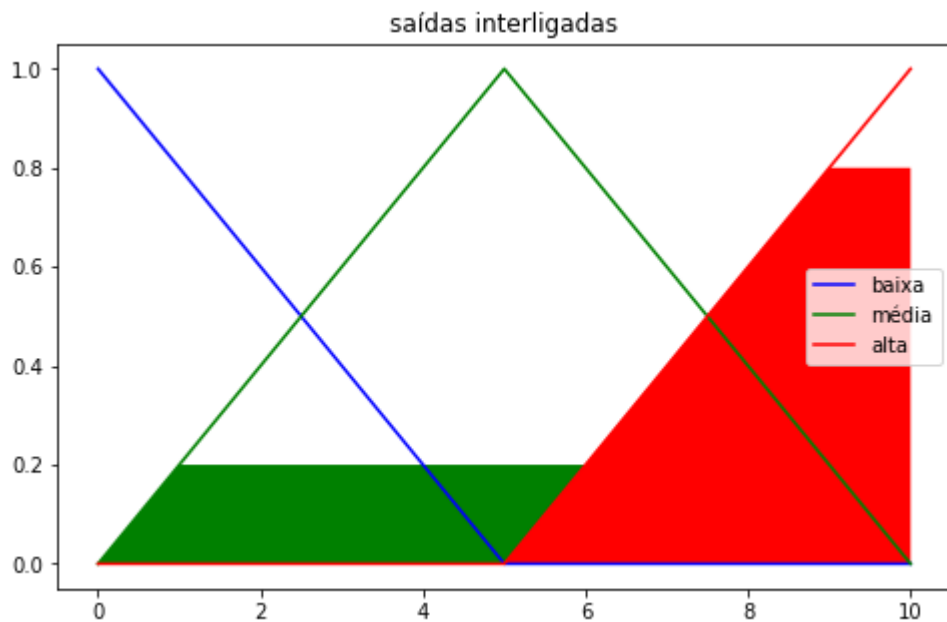
```
In [41]: x_succao0 = np.zeros_like(x_succao)
x_succao0
```

```
Out[41]: array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0])
```

```
In [42]: x_succao.shape, x_succao0.shape
```

```
Out[42]: ((11,), (11,))
```

```
In [46]: fig, ax = plt.subplots(figsize=(8,5))
ax.plot(x_succao, y_succao_baixa, 'b', label='baixa')
ax.fill_between(x_succao, x_succao0, ativacao_succao_baixa, facecolor='b')
ax.plot(x_succao, y_succao_media, 'g', label='média')
ax.fill_between(x_succao, x_succao0, ativacao_succao_media, facecolor='g')
ax.plot(x_succao, y_succao_alta, 'r', label='alta')
ax.fill_between(x_succao, x_succao0, ativacao_succao_alta, facecolor='r')
ax.set_title('saídas interligadas')
ax.legend();
```



## Defuzzificação

- centroid (centroid)
- bisector (bisector)
- mean of maximum (mom)
- mim of maximum (som)
- max of maximum (lom)

```
In [47]: controle = np.fmax(ativacao_succao_baixa, np.fmax(ativacao_succao_alta,ativacao_succao_media))
         controle
```

```
Out[47]: array([0. , 0.2, 0.2, 0.2, 0.2, 0.2, 0.2, 0.4, 0.6, 0.8, 0.8])
```

```
In [48]: succcao = fuzz.defuzz(x_succao, controle, 'centroid')
         #succcao = fuzz.defuzz(x_succao, controle, 'bisector')
         #succcao = fuzz.defuzz(x_succao, controle, 'mom')
         #succcao = fuzz.defuzz(x_succao, controle, 'som')
         #succcao = fuzz.defuzz(x_succao, controle, 'lom')
         succcao
```

```
Out[48]: 6.725490196078432
```

```
In [49]: succcao_ativacao = fuzz.interp_membership(x_succao, controle, succcao)
```

```
In [50]: fig, ax = plt.subplots(figsize=(8,5))
         ax.plot(x_succao, y_succao_baixa, 'b', label='baixa')
         ax.plot(x_succao, y_succao_media, 'g', label='média')
         ax.plot(x_succao, y_succao_alta, 'r', label='alta')
         ax.fill_between(x_succao, x_succao0, controle, facecolor='purple')
         ax.plot([succcao, succcao], [0, succcao_ativacao], 'black')
         ax.set_title('defuzzificação')
         ax.legend();
```

