

Submitted by
Julian Hofer, B.Sc.

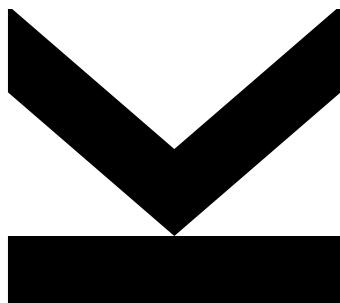
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Supervisor
Prof. Dr. Armando Rastelli

Co-Supervisor
DI Christian Schimpf

month year

Advanced excitation and spectroscopy schemes with quantum dots



Master Thesis
to obtain the academic degree of
Diplom-Ingenieur
in the Master's Program
Technische Physik

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First I would like to thank the head of our group Armando Rastelli for offering me this position and for making sure to always have an open ear, no matter how busy he was at the moment. I would also like to thank Christian Schimpf for taking the role as my unofficial supervisor. I can not think of anyone who would have fulfilled it better than him. Thanks belongs to most of my group members but I want to especially highlight Marcus Reindl and Daniel Huber who granted me the biggest support. Further, I would like to thank Susanne Schwind for solving every administrative issue that came along my way.

Last but not least, I would like to thank my parents for supporting every goal I have ever pursued in my life and of course Sabrina for more reasons than I could ever possibly list.¹

¹This document is set in Palatino, compiled with pdfL^AT_EX2e and Biber. The L^AT_EX template from Karl Voit is based on KOMA script and can be found online: <https://github.com/novoid/LaTeX-KOMA-template>

Zusammenfassung

Geräte, die auf Quantentechnologie basieren, sind prädestiniert, Teil unseres täglichen Lebens zu werden. Halbleiterquantenpunkte mit ihren diskreten elektronischen Zuständen sind vielversprechende Kandidaten für dieses Gebiet und ideal für die Erforschung der Quantenoptik. Aus diesem Grund werden in dieser Arbeit zunächst Herstellungsverfahren und optische Eigenschaften von GaAs-Quantenpunkten vorgestellt.

Die weitere Diskussion ist in zwei Kapitel unterteilt, deren gemeinsamer Nenner GaAs-Quantenpunkte sind. Das erste befasst sich mit der resonanten Zwei-Photonen-Anregung mittels "adiabatic rapid passage". Bei diesem Verfahren werden gechirpte Laserpulse verwendet, deren Charakterisierung, Simulation und Messung den größten Teil dieses Kapitels ausfüllen. Der zweite Teil behandelt die spektrale Auflösung der Quantenpunktemission mittels eines Scanning Fabry-Pérot-Interferometers. Hier wird der Leser zunächst durch den Aufbau der mathematischen Beschreibung der Fabry-Pérot-Modi geführt. Anschließend werden Simulationen vorgestellt, mit deren Hilfe die Komponenten des Interferometers dimensioniert werden. Schließlich wird die Feinstruktur des Biexcitons im Rahmen

Zusammenfassung eines Proof-of-Principle-Experiments aufgelöst.

nach Abstract
anpassen

Abstract

Devices based on quantum technology are promising candidates to become part of our everyday lives. Semiconductor quantum dots with their discrete electronic states are promising candidates for this field and are ideal for research in quantum optics. That is why this thesis starts by introducing fabrication methods and optical properties of droplet-etched GaAs quantum dots.

The further work is splitted in two chapters with GaAs quantum dots as their common denominator. The first one deals with resonant two-photon excitation via adiabatic rapid passage. In this procedure chirped laser pulses are used and their characterization, simulation and measurements will fill the majority of this chapter. The second one investigates the capabilities of resolving quantum dot emission with a scanning Fabry Pérot interferometer. Initially, the reader is guided through the build-up of the mathematical description of the Fabry Pérot modes. Afterwards, simulations will be presented which are used to size the interferometer components. Finally the fine-structure of the biexciton will be resolved in a proof-of-principle experiment.

The detailed outlook over the chapters should be part of the introduction, not of the abstract.

Rewrite the abstract to give a brief overlook over all the work you did.

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Todo list

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Don't refer all the time to the main text. Imagine I'm a reader from a different field. I read the abstract, the introduction and the summary/outlook. Now I should know what you did and why and what are the future plans. At this point I have no idea what MOSAIC is, I have no idea what a pulse expander is, etc. unless you give me a hint in the summary. . .

1. Introduction

In the past century, technology was transformed by the first quantum revolution. Scientists and engineers all around the world utilized certain features of quantum mechanics such as energy quantization and wave-particle duality to create devices which are a nowadays a fixed part of everyone's life. These technologies, ranging from semiconductor devices to LEDs and lasers, became high-performance components which drive the global communication networks and information processing. The second quantum revolution will make use of superposition, entanglement and quantum interference [1]. Entanglement is already the basis of many experiments in quantum computation and its distinct properties are used for quantum cryptography protocols as well. [2]. It describes a physical phenomenon involving two or more particles which quantum states cannot be described independently from each other. Modern optical fibre networks allow to transport photons (and their quantum states) over long distances and are therefore ideal to build up quantum networks [3]. With quantum key distribution (QKD) inherently secure communication would be possible, as it enables to produce a shared random key, which only the two parties wishing to exchange messages know, and which can be used by one of them to encrypt a message and be used by the other to decrypt it. An implementation under the E91 protocol allows to detect eavesdropping even with lossy channels by using entangled photon pairs [4].

However, in order to solve this task several problems have to be solved first. Fibre channels suffer from decoherence and losses, degrading the quantum information to a point where they are unusable for quantum protocols and therefore limiting the maximal communication distance. Usually classical amplifiers would be used in order to counteract transmission losses, however this does not work with quantum states. That is why, multiple teams looked into developing quantum repeaters [5][6][7]. The quantum repeater uses an entangled state in order to transmit a quantum state to another repeater station using quantum teleportation [8].

Additionally, the E91 protocol requires deterministic sources of single entangled photons. Parametric down conversion crystals [9] or single atoms [10] could serve as sources. Sources based on parametric

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down conversion are currently the brightest ones, but their emission is probabilistic. The number of entangled photon pairs emitted per excitation pulse is statistically distributed. Single atoms offer sharp electronic transitions, are free from charge fluctuations and are energetically isolated. Nowadays advanced techniques [11] are used in order to operate with single-atom-based sources, but their dynamics are relatively low, leading to slow operation rates.

Quantum dots provide an alternative source of single entangled photons. Quantum dots are deterministic, emitting maximal one photon pair per excitation and are scalable to nanosized dimensions. With this motivation in mind, droplet-etched GaAs quantum dots as potential sources are investigated, as they are quasi strain-free, of high symmetry and exhibit low values of fine structure splitting (FSS). However, entanglement fidelity is limited by re-excitation of photons at the exciton level to the biexciton level before they can decay to the ground state. This effect can be avoided by resonant two-photon excitation. With these measures on-demand generation of entangled photons gets within reach [12]. However, resonant two-photon excitation requires precise control of the intensity of the exciting field in order to inverse the quantum dot from the ground state to the biexciton state. Exciting via adiabatic rapid passage with frequency-chirped pulses can be an alternative, which is further discussed in chapter 4.

When it comes to characterizing quantum dot (QD) emission, more obstacles arise as fine features of the emission spectrum are not resolvable with a CCD-based spectrometer alone. However, a small-band bandpass filter with adjustable center frequency could scan through the ranges of interest and its output could then be recorded with the CCD. Chapter 5 describes the efforts to build up a scanning Fabry-Pérot interferometer to do exactly that.

Please reformulate. This sounds "inverted". Start with what a Fabry-Perot is and that it does what we want.

2. Droplet etched gallium arsenide quantum dots

2.1. Fabrication and optical properties

Quantum dots (QD) are nanostructures which confine the motion of electrons and holes in all three spatial dimensions. Confinement results in discrete energy levels, which is why QDs are sometimes referred to as *artificial atoms*. The discussion in this section is based on the PhD thesis of Huber [13] and on the master's thesis of Schimpf [14].

Gallium arsenide QDs investigated within this master's thesis are grown by molecular beam epitaxy (MBE) with the self-assembled nanodrill technology described in the work of Wang et al. [15]. As displayed in figure 2.1a the Al forms droplets on $\text{Al}_{0.4}\text{Ga}_{0.6}\text{As}$ after evaporation. The Al reacts with $\text{Al}_{0.4}\text{Ga}_{0.6}\text{As}$, which produces nanoholes etched into the surface. Under ideal conditions, these nanoholes are highly symmetric as can be seen in figure 2.1b. This results into QDs with high in-plane symmetry. The next step is the annealing process in which GaAs is deposited to fill the nanoholes. The QD is finalized by capping the layer with $\text{Al}_{0.4}\text{Ga}_{0.6}\text{As}$ acting as top barrier.

Compared to the band gap of the host material $\text{Al}_{0.4}\text{Ga}_{0.6}\text{As}$ of 1.92 eV at room temperature, the core of the QD, GaAs has a band gap of only 1.42 eV at room temperature. The energy difference between the $\text{Al}_{0.4}\text{Ga}_{0.6}\text{As}$ bandgap and the discrete energy levels forming in the QD are responsible for the 3D confinement and the type-I band alignment depicted in figure 2.1c. Inside of the QD, optical transitions are possible. Transitions between the first energy level in the conduction band (CB) and the valence band (VB), often called the s-shell, are here of special interest. The carriers involved are the electrons (e^-) and the holes (h^+) left behind. These are fermions and therefore only up to two of them can, in accordance with Pauli's exclusion principle, occupy a single energy state. Electrons and holes are strongly localized inside the QD by the confinement potential and influence each other

2. Droplet etched gallium arsenide quantum dots

by Coulomb attraction and exchange interaction [16]. This leads to multi-particle complexes with the most fundamental being the exciton (X), a state of an electron and a hole, bound by Coulomb interaction. Fully occupied s-shells form the biexciton (XX), consisting of two electrons and two holes of opposite spins.

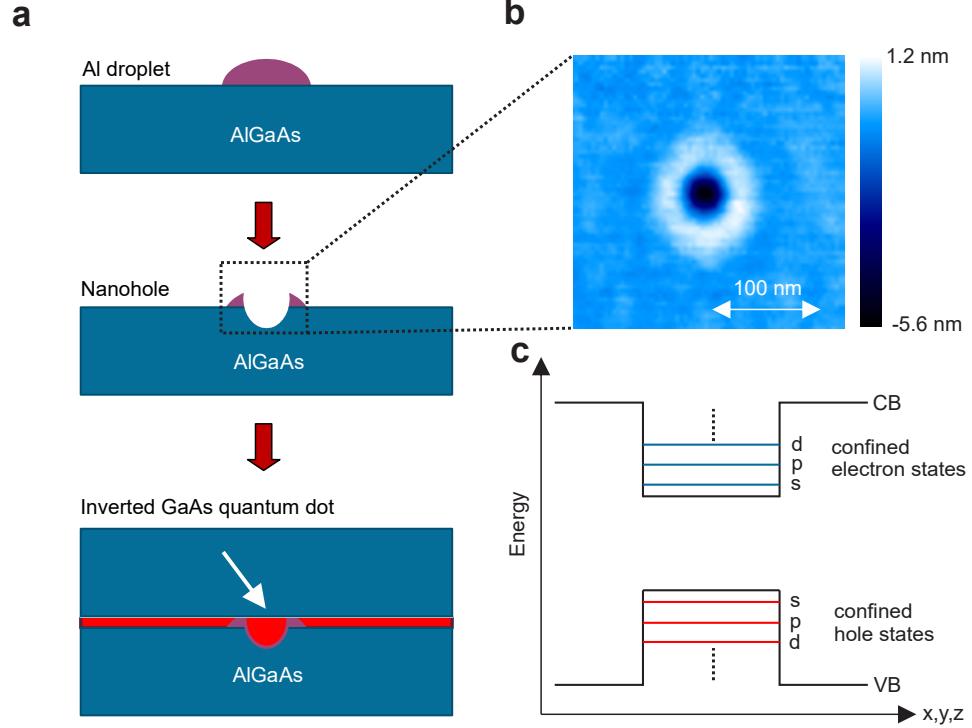


Figure 2.1.: (a) The growth process of a GaAs quantum dot by MBE.

(b) Atomic force microscopy (AFM) image of the nanohole before it is filled with GaAs.

(c) Conduction band (CB) and valence band (VB) of an optically active QD. [13]

In a QD, polarization-entangled photon pairs can be generated via a biexciton-exciton decay cascade [17], illustrated in figure 2.2. The $|XX\rangle$ state forms a full shell, which means that the total angular momentum projection along the quantization axis of the XX complex sums up to $M = 0$. The QD is radially symmetric, therefore M is preserved and $|M\rangle$ are eigenstates of the system. After exciting the QD into the $|XX\rangle$ state (e.g. by optical pumping) it decays by spontaneous recombination of an electron-hole-pair accompanied by the emission of a single photon into the $|X\rangle$ state. The two dipole-allowed radiative transitions lead to only two possible angular momentum states of the exciton:

- $| -1 \rangle$ under emission of a right-circularly-polarized photon $|R_{XX}\rangle$

- $|+1\rangle$ under emission of a left-circularly-polarized photon $|L_{XX}\rangle$

$| -1 \rangle$ and $| +1 \rangle$ are degenerated in energy and decay into the groundstate $| G \rangle$ under emission of $| L_X \rangle$ and $| R_X \rangle$, respectively. The resulting two-photon state is then described by

$$|\psi^+\rangle = \frac{1}{\sqrt{2}} (|L_{XX}\rangle|R_X\rangle + |R_{XX}|L_X\rangle) \quad (2.1)$$

which is one of the four Bell states, representing the maximal entangled two-particle states.

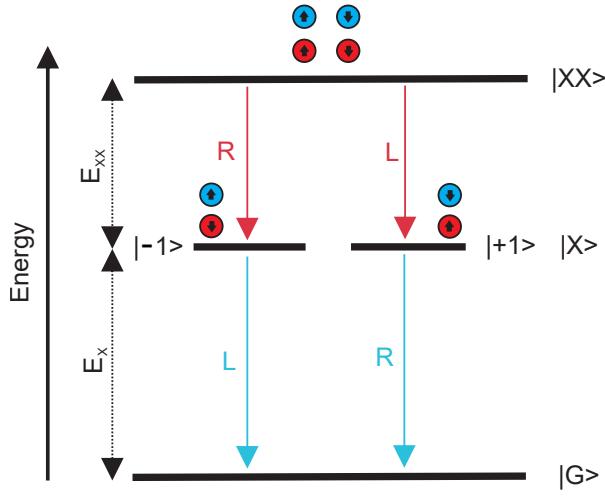


Figure 2.2.: Biexciton-exciton cascade in a QD. The $|XX\rangle$ state can decay via two paths under the emission of a right (left) polarized photon into one of two energetically degenerated $|X\rangle$ states. The $|X\rangle$ state then decays into the ground state $|G\rangle$ under the emission of a left (right) polarized photon. [13]

In order to calculate the life time of the X and XX states and the respective spectral description of the emission the radiative transition rate Γ between quantum mechanical states has to be derived. Γ describes the transition probability per unit time from an initial state $|i\rangle$ to a final state $|f\rangle$ and it can be calculated by Fermi's golden rule if the transition occurs because of a weak perturbation. In the dipole approximation it can be described by

$$\Gamma \propto |\langle f | \mathbf{e} \cdot \hat{\mathbf{p}} | i \rangle|^2 \delta(E_i - E_f - E_P) \quad (2.2)$$

with \mathbf{e} as the unit polarisation vector of the emission, $\hat{\mathbf{p}}$ as the momentum operator of the electron and E_f , E_i and E_P as the energies of the final state, of the initial state and of the emitted photon respectively. The rate equation for the population of the initial state can then be described by

$$\frac{dN_i(t)}{dt} = -\Gamma N_i(t) \quad (2.3)$$

2. Droplet etched gallium arsenide quantum dots

which results into a potential decays as solution

$$N_i(t) = N_i(0)e^{-t/\tau} \quad (2.4)$$

where the lifetime of the initial state is defined as $\tau = 1/\Gamma$.

This can be applied for the X and XX states with decay constants τ_ν and intensity for the emitted light $I_\nu(t)$ where $\nu \in \{X, XX\}$. The Fourier transformation of the electric field yields a Cauchy distribution

$$I_\nu(\omega) = \frac{1}{2\pi\tau_\nu} \frac{1}{(\omega - \omega_\nu)^2 + \left(\frac{1}{2\tau_\nu}\right)^2} \quad (2.5)$$

with $\omega_\nu = e_\nu/\hbar$ as its center frequency.

2.2. Fine structur splitting

Fine structure splitting (FSS) in a QD describes the energy splitting between the two possible bright $|X\rangle$ states. In GaAs it originates from the exchange interaction between electrons and holes. [18]. The electron-hole exchange Hamilton is described by

$$\mathcal{H}_{ex} = - \sum_{i=x,y,z} a_i J_{h,i} S_{e_i} + b_i J_{h,i}^3 S_{e_i} \quad (2.6)$$

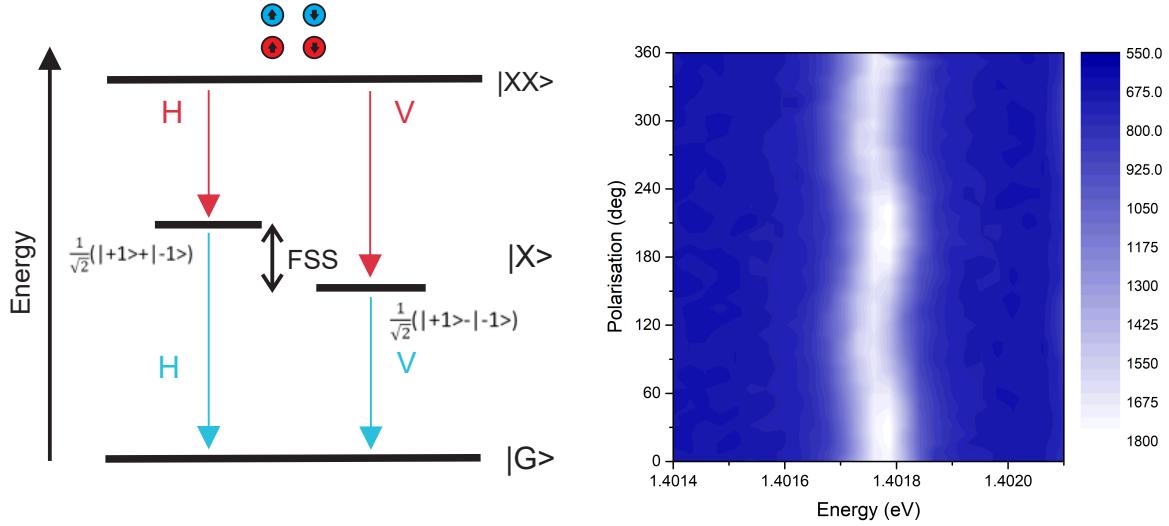
with a_i and b_i as the spin-coupling constants, $J_{h,i}$ as the holes' and S_{e_i} the electrons' total angular momentum. The z-direction is assigned as the crystal growth direction and the bright X states are defined by the projections of $J_{h,i}$ and S_{e_i} to the z-axis, so that $|+1\rangle = |+\frac{3}{2}, -\frac{1}{2}\rangle$ and $| -1\rangle = |-\frac{3}{2}, +\frac{1}{2}\rangle$. The Hamiltonian of equation (2.6) can be described in the bases $\{|+1\rangle, |-1\rangle\}$

$$\mathcal{H}_{ex} = \begin{pmatrix} \langle +1 | \mathcal{H}_{|S|} | +1 \rangle & \langle +1 | \mathcal{H}_{|S|} | -1 \rangle \\ \langle -1 | \mathcal{H}_{|S|} | +1 \rangle & \langle -1 | \mathcal{H}_{|S|} | -1 \rangle \end{pmatrix} = \begin{pmatrix} \Delta_0 & \Delta_1 \\ \Delta_1 & \Delta_0 \end{pmatrix} \quad (2.7)$$

with $\Delta_0 = \frac{3}{4}(a_z + \frac{9}{4}b_z)$ and $\Delta_1 = -\frac{3}{8}(b_x - b_y)$.

In the ideal case the QD is perfectly symmetric along the z-axis, $b_x = b_y$, Δ_1 vanishes and $|+1\rangle$ and $| -1\rangle$ are degenerate eigenstates. If that is not the case, the angular momentum M along the z-direction is not preserved and $|+1\rangle$ and $| -1\rangle$ are no eigenstates of \mathcal{H}_{ex} . The new basis can be found by diagonalising \mathcal{H}_{ex} , described by $\frac{1}{\sqrt{2}}(|+1\rangle + |-1\rangle)$ and $\frac{1}{\sqrt{2}}(|+1\rangle - |-1\rangle)$. In figure 2.3a the $|XX\rangle$ decay path with splitted $|X\rangle$ eigenstates is shown. $|XX\rangle$ exhibit no splitting as the angular momentum

of the electrons and holes add to zero and therefore no exchange interaction occurs. In figure 2.3b photo-luminescence spectra recorded with a linear polariser are shown.



(a) XX decay cascade without X degeneracy because of fine structure splitting. [13]

(b) Photoluminescence spectra of X emission of a GaAs Qd plotted for different polarizer angles. In the image the effect of the linear polarization of the fine structure components is visible. [14]

Figure 2.3.: Fine structure splitting in a GaAs quantum dot.

2.3. Zero-phonon line and phonon sideband

The excitonic emission of GaAs QDs exhibits non-Lorentzian asymmetric broadening. These side bands can be traced back to a coupling to acoustic phonons [19][20]. The discussion of phonon side bands (PSBs) is based on the works of Friedrich and Haarer [21] and Peter et al. [19].

Figure 2.4 displays a schematic representation of the zero phonon line (ZPL) and PSB absorption spectrum. The intensity distribution between the two components depends strongly on temperature.

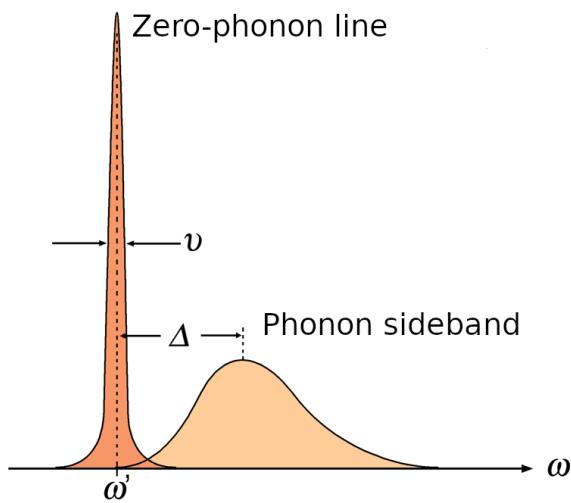
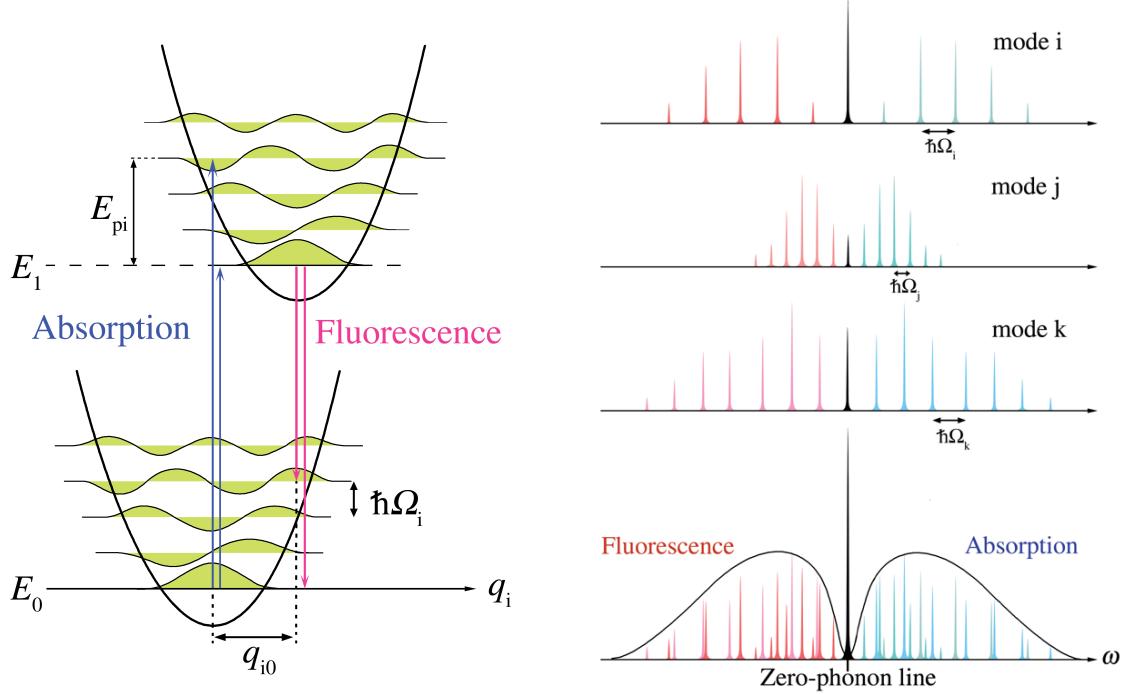


Figure 2.4.: Absorption line shape of an electronic excitation. The emission shape can be determined by mirroring the absorption shape at ω' .

To determine the frequency gap Δ in figure 2.4, the Franc-Condon principles [22] are used. It states that electronic transition between ground and excited state is much faster than the motion in the lattice as the photons carry nearly no momentum. Hence, there is no motion along the configurational coordinates q_i during the energy transitions as depicted in figure 2.5a. The transitions can be displayed as vertical arrows with the shorter arrow describing the ZPL and the longer one describing the PSB. According to the Franc-Condon principles, the more the wave functions of two vibrational energy levels overlap, the likelier is the electronic transition between these two. In the case of figure 2.5a this occurs when the photon energy equals to the energy difference $E_1 - E_0$ plus three quanta of vibrational energy $E_{pi} = \hbar\Omega_i$. The emission follows the same principle.



(a) Energy spectrum of a two-level electronic system with phonon coupling. The arrows describe emission/absorption with and without phonons respectively.

(b) Three lattice normal modes (i, j, k) and the resulting emission/absorption spectrum.

Figure 2.5.: Zero-phonon line and phonon sideband. [23]

Figure 2.5a and 2.5b implicitly assume approximations in addition to the Franck-Condon principles. The lattice vibrational mode has to be well described by a quantum harmonic oscillator. Additionally, it is assumed that only the lowest lattice vibration is excited and that the harmonic oscillator potentials are equal in both states. These preconditions are visible in the parabolic shaped potential wells and equally spaced phonon energy levels in figure 2.5a.

The reason why zero-phonon line is stronger than the phonon side band can be found by examining the superposition of the lattice modes. Each lattice mode m leads to a different energy difference $\hbar\Omega_m$ between phonons. That is why the transitions with phonons result in a energy distribution and the zero-phonon transition add up at the electronic origin $E_1 - E_0$ as can be seen in figure 2.5bb.

The theoretical limit of the spectral range of the zero-phonon line for a GaAs quantum dot can be calculated with the time-energy uncertainty relation

$$\Delta E \cdot \Delta t = \frac{\hbar}{2\pi} \quad (2.8)$$

2. Droplet etched gallium arsenide quantum dots

This gives for typical lifetime of a GaAs quantum dot of $\Delta t = 250 \text{ ps}$

$$\Delta E = 2.64 \mu\text{eV}. \quad (2.9)$$

The frequency uncertainty can be obtained through

$$\Delta\nu = \frac{\Delta E}{h}. \quad (2.10)$$

The wavelength λ relates to ν with the Planck-Einstein relation

$$\lambda(\nu) = \frac{c}{\nu} \quad (2.11)$$

and the wavelength uncertainty $\Delta\lambda$ can be approximated with a Taylor series around ν_0

$$\Delta\lambda = -\lambda'(\nu_0) \cdot \Delta\nu. \quad (2.12)$$

With equation (2.10) and the center wavelength of the zero-phonon line λ_0 in table 2.1 this gives

$$\Delta\lambda = \frac{c}{\nu_0^2} \cdot \Delta\nu = \frac{\lambda_0^2}{c} \cdot \Delta\nu \quad (2.13)$$

$$\approx 1.0 \text{ pm} \quad (2.14)$$

Together with data from Schöll et al. [24] and empirical values measured by our group, this leads to the parameters listed in table 2.1.

Table 2.1.: Parameters of GaAs quantum dots used in the laboratory of semiconductor physics department in Linz. Zero-phonon line calculates from the theoretical limit according to the life time of the excitonic state (as can be seen in equation (2.14)) up to broader lines which are still valued enough to be measured. The phonon sideband resembles data taken from Schöll et al. [24].

Quantum dot emission	Center wavelength λ_0	Spectral range $\Delta\lambda$	Waveform
Zero-phonon line	(700 to 800) nm	(1.0 to 1.4) pm	Cauchy
Phonon sideband	~0.25 nm higher than zero-phonon line	500 pm	Gauss

2.4. Optical excitation of a quantum dot

In this section, the different ways of optically exciting QDs are discussed. It is based on the PhD thesis of Huber [13] and the master's thesis of Schimpf [14]. The excited states of a QD can be populated in various ways. A common way is above-band excitation, depicted in figure 2.6a. Electrons are optically excited by a laser with energies above the band gap of the QDs host material $\text{Al}_{0.4}\text{Ga}_{0.6}\text{As}$ with $E_L = 1.92 \text{ eV}$ at room temperature. Subsequently, electrons and holes are captured by the QDs and relax via phonon-scattering to the lowest energy level, the s-shell. However, because of pronounced recapture processes [25] and spin scattering processes [26], above-band excitation is not favourable for entangled photon generation. Additionally, indistinguishability of the emitted photons is reduced because of fluctuating electric fields. Resonant excitation of electron-hole pairs provides an alternative which is less affected by fluctuating electric fields. As shown in figure 2.6b this technique creates electron-hole-pairs directly in the s-shell.

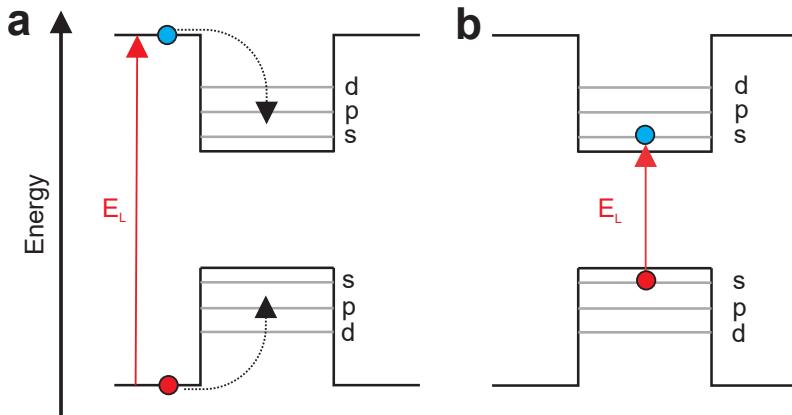


Figure 2.6.: Optical pumping of a QD by (a) above-band excitation and (b) resonant excitation [13]

Resonant excitation can be used in order to populate the $|XX\rangle$ state with near unity population probability [27]. Due to dipole-selection rules, this requires a two-photon-absorption process. Hereby, the energy of a femtosecond-pulse laser E_p is tuned to exactly the half of the XX energy with respect to the ground energy, as sketched in figure 2.7a. Because of Coulomb interaction, two times the X energy with respect to the ground energy $2 \cdot E_X$ is not equal to E_{XX} but differs by the binding energy E_B . The laser is therefore tuned to

$$E_p = E_X - E_B/2. \quad (2.15)$$

Empirically $E_B \approx 3.78 \text{ meV}$ for GaAs QDs. Resonant two-photon absorption is a third-order non-linear effect which involves two photons and electrons at once. It depends on the third-order-susceptibility

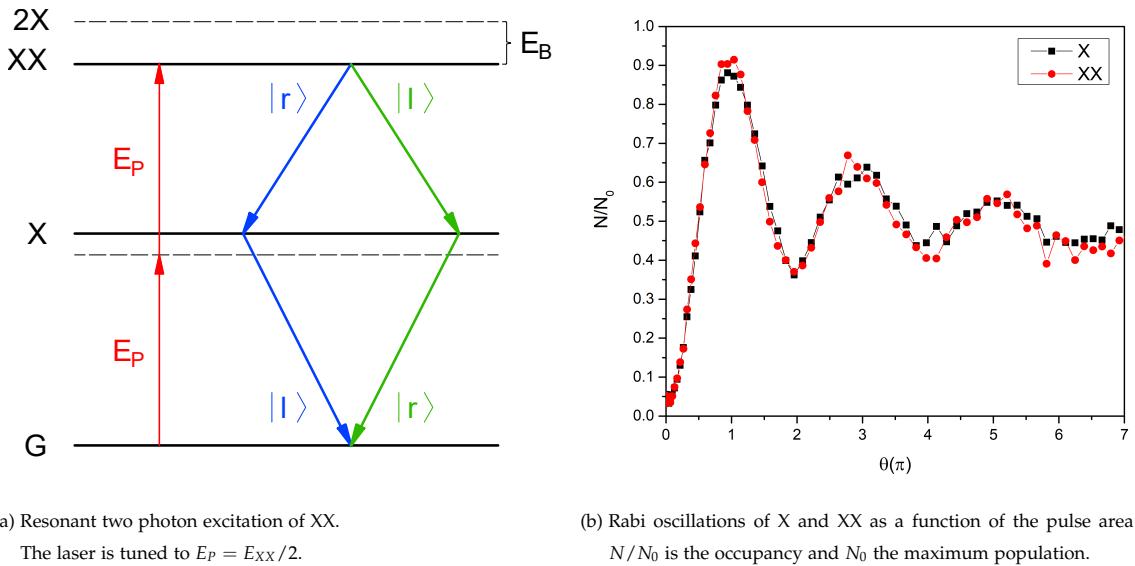
2. Droplet etched gallium arsenide quantum dots

$\chi^{(3)}$ of GaAs and therefore requires relatively high laser power.

As this two-level system is driven in resonance its population exhibits Rabi oscillations. The final population of the XX can be described by

$$N_{XX} = \sin^2\left(\frac{\theta}{2}\right) \quad (2.16)$$

with θ as the pulse area in relation to the Rabi oscillations. θ is not the area of the excitation pulse, but depends on it in a non-trivial way [28]. Measured Rabi oscillations of X and XX are shown in figure 2.7b [27]. Theoretically, the curve should oscillate between occupancies N/N_0 , with N_0 as the maximum population, of 0 and 1. However, as a consequence of phonon damping the occupancy converges to a purely probabilistic value of 0.5 [29].



(a) Resonant two photon excitation of XX.

The laser is tuned to $E_P = E_{XX}/2$.

(b) Rabi oscillations of X and XX as a function of the pulse area θ .

N/N_0 is the occupancy and N_0 the maximum population.

Figure 2.7.: Resonant two photon excitation [14]

2.5. Single photon emission

The XX-X cascade shown in figure 2.7a results in a single photon pair per emission cycle. Single photons are necessary for quantum cryptography and quantum optics in general which motivates the following discussion of this topic based on the thesis of Huber [13]. The single photon purity of the $|XX\rangle$ to $|X\rangle$ and the $|X\rangle$ to $|G\rangle$ signals, respectively, can be determined by performing a Hanbury-Brown-Twiss (HBT) experiment. An example of an HBT setup is shown in figure 2.8a and

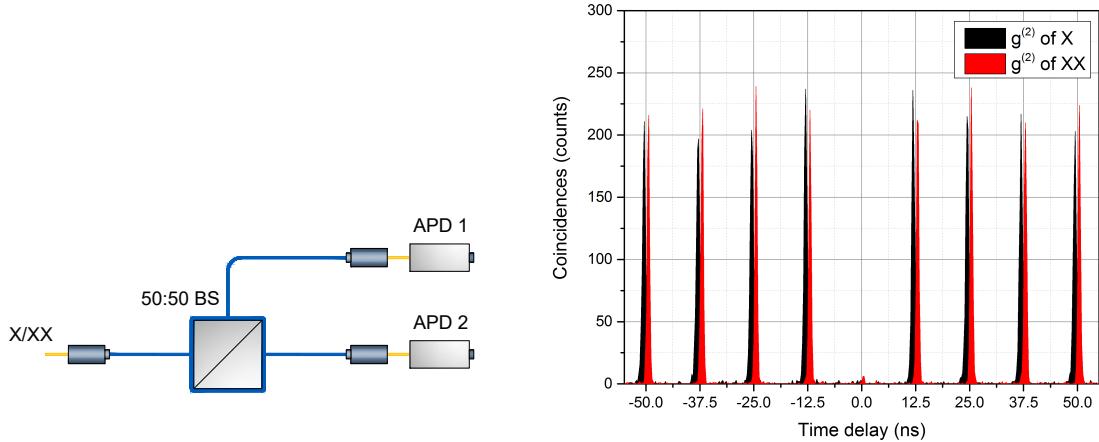
consists of two avalanche photodiodes (APDs) used as single photon detectors and a beam splitter. The measurements at the two detectors can be used in order to calculate the second-order correlation function, which is defined as

$$g^{(2)} = \frac{\langle I(t)I(t + \tau) \rangle}{\langle I(t) \rangle \langle I(t + \tau) \rangle} \quad (2.17)$$

with $I(t)$ as the light intensity and τ as the time delay. When a single photon enters the input of the beam splitter (BS) it can only be measured at one output, but never at both simultaneously. Assuming a perfect single photon emitter, a coincidence measurement between APD1 and APD2 will result in $g^{(2)}(\tau) = 0$ at zero time delay. Subsequently, side peaks are expected at $\tau_s = z/R$ with R as the repetition rate of the laser and $z \in \mathbb{Z} \setminus \{0\}$. The single photon purity can then be defined as

$$\kappa(b) = \frac{A_0(b)}{A_s(b)} \quad (2.18)$$

with A_0 as the area under $g^{(2)}(\tau)$ around $\tau = 0$ and A_s as the average area under the side peaks at τ_s . The time bin b has to be chosen so that it includes a full side peak. If b would be chosen too small it would falsely increase κ , if chosen too high it includes unnecessary much noise.



(a) Setup to measure the Hanbury-Brown-Twiss effect.
Single photons can be measured only at one APDs, but not at both at the same time.

(b) Second-order auto-correlation function $g^{(2)}$ of X and XX. The low height of the peak at zero time delay compared to the height of the side peaks suggest the suitability of the quantum do as a single photon emitter.

Figure 2.8.: Hanbury-Brown-Twiss HBT experiment [14]

3. Methods

Einleitung

3.1. Optical setup

The setup used for the measurements described in following chapters is sketched in figure 3.1.

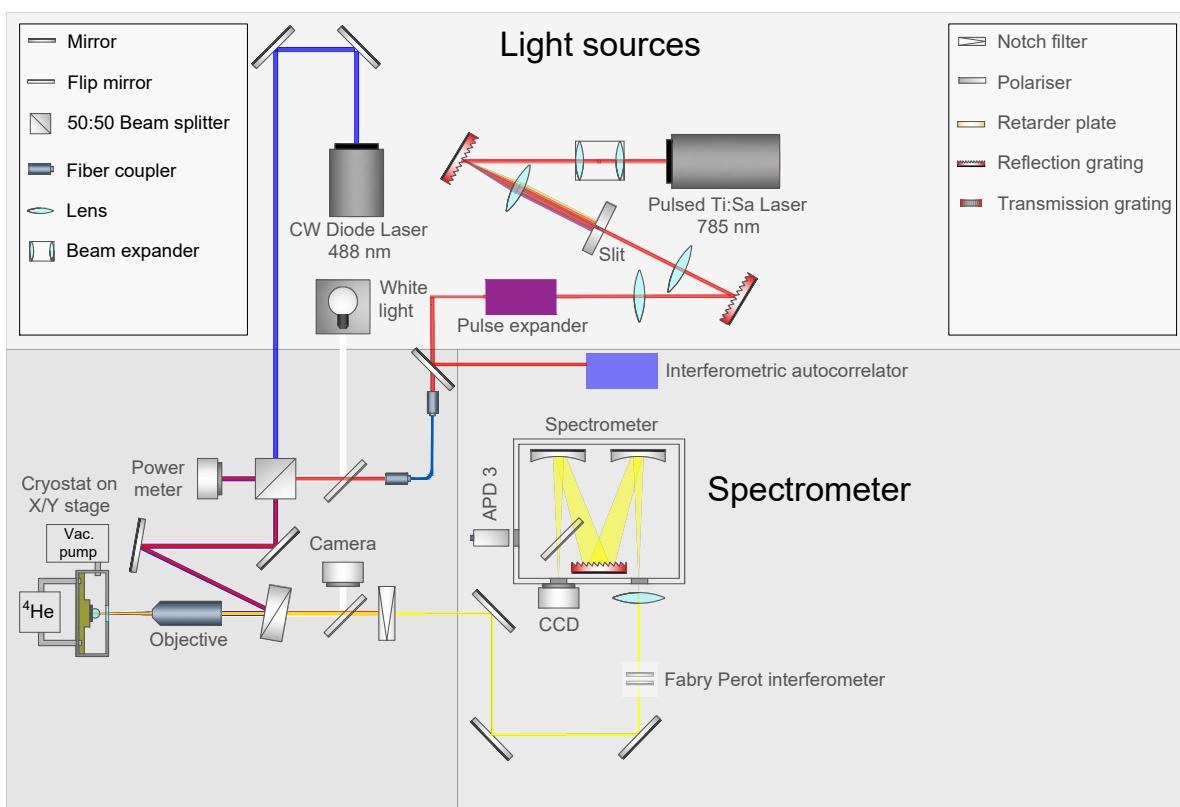


Figure 3.1.: Complete experimental setup, which was used in order to quantify the chirp of the Ti:Sa Laser and resolve spectral emission of a quantum dot [14].

3. Methods

3.2. Pulse shaper

In order to resonantly excite the $|XX\rangle$ state a pulsed Ti:Sa laser with a full width at half maximum (FWHM) pulse duration of $\tau_p \approx 100$ fs is used. Under the assumption that the laser pulse is of Gaussian shape and that it is chirp-free (more on that in chapter 4), the spectral bandwidth $\Delta\nu$ can be described by

$$\Delta\nu\tau_p \approx 0.44. \quad (3.1)$$

This corresponds to a spectral range of $\Delta E = h\Delta\nu = 18.2$ meV. As can be seen in equation (2.15), the spectral range should be smaller than $E_B/2 \approx 1.89$ meV, which is not fulfilled with the laser beam alone.

The pulse shaper sketched in the upper part of figure 3.1 is used in order to tune ΔE and additionally the centre emission energy to our requirements. The laser beam is sent through a Keplerian telescope in order to expand its beam diameter from 3.4 mm to 6 mm. It gets dispersed by a diffraction grating and focused by a lens so that the spectral components are ordered along a plane where the slit is placed. The centre energy can be adjusted with the slit position and the spectral range with the slit width. The setup is mirrored with an additional lens and diffraction grating, which transform the laser beam again into real space.

3.3. Micro photo-luminescence

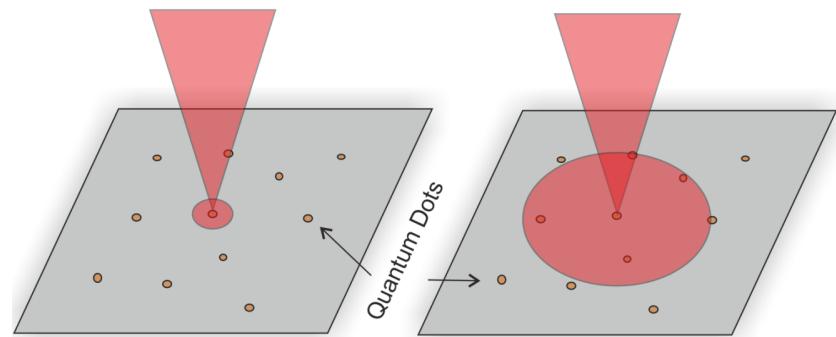


Figure 3.2.: Laser beam of different spot sizes illuminating quantum dots [30].

The following chapters will investigate the optical properties of QD. In order to achieve that, it is necessary to excite and collect light of only a single one. This is achieved by micro photo-luminescence (MPL), which involves (i) reducing the diameter of the excitation laser beam and (ii) using samples with a low QD density [30]. (i) can be improved by using an objective, where its minimal achievable spot size d is described by

$$d = \frac{\lambda}{2 \cdot NA} \quad (3.2)$$

with NA as the numerical aperture. As the wavelength of the laser λ is adjusted according parameter of the QD, NA is the adjustable factor. In our laboratory, an objective of $NA = 0.62$ is used, allowing laser spot sizes in the order of the excitation wavelength. A QD density of $\approx 1/\lambda^2$ is therefore necessary in order to examine single QD emission.

The sample containing the QDs is mounted inside the cryostat, which is cooled down to 4 K. This is necessary as the influence of dephasing processes increases with higher temperature due to carrier-phonon interaction. The laser beam is then focused on the sample by the objective and the QD emission is then collected by the very same objective and passed through a beam splitter.

4. Entangled photon generation using adiabatic rapid passage with frequency-chirped pulses

4.1. Introduction and motivation

In order to efficiently use the biexciton decay cascade, the biexciton state has to be prepared beforehand in a robust way. This chapter deals with the efficient inversion of the QD from the ground state to the biexciton level via adiabatic rapid passage (ARP). ARP uses chirped pulses, which need to be measured and deterministically adjusted in order to effectively use them. Therefore, the majority of this chapter will focus on the chirp and how to determine and adjust it, with the help of simulations and later with measurements.

4.2. Chirp

A chirped signal is a signal of which the frequency changes over time. For example, the frequency of a linearly chirped signal $f(t)$ would be described by

$$f(t) = ct + f_0 \quad (4.1)$$

where f_0 is the starting frequency at $t = 0$ and c is the chirpiness. A linear chirped sinusoidal wave is depicted in figure 4.1.

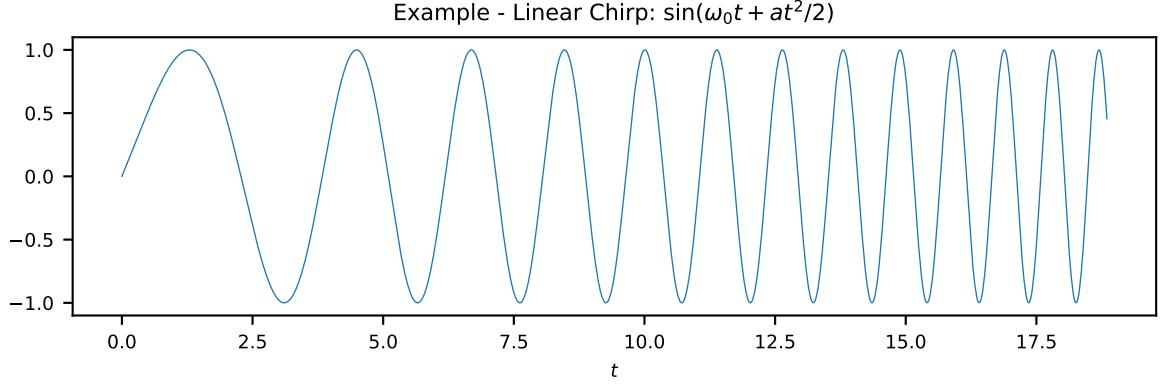


Figure 4.1.: A chirped sinusoidal wave which increases in frequency over time.

As this chapter is concentrated on exciting QDs with frequency-chirped pulses, the mathematical description of chirped laser pulses will now be discussed. The electric field of a laser $E(t)$ has the shape

$$E(t) \sim \text{Re} \left(f^{1/2}(t) \cdot \exp(-i\omega t - i\phi(t)) \right) \quad (4.2)$$

with the central frequency ω and the linear chirp $\phi(t)$.

Depending on the laser either a Gaussian or a hyperbolic secant describes the pulse shape more accurately [31, 32]

- Gaussian pulse:

- Pulse shape of

$$f_{gauss}(t) = \left(\frac{A_{gauss}}{\sqrt{2 \cdot \pi \cdot \tau_0 \cdot \tau}} \exp\left(-\frac{t^2}{2 \cdot \tau^2}\right) \right)^2 \quad (4.3)$$

with the normalization constant A_{gauss} , the pulse duration τ_0 , the central frequency ω and the chirp coefficient α .

- Linear chirp of

$$\phi_{gauss}(t) = \frac{a_{gauss} t^2}{2} \quad (4.4)$$

where $\tau = \sqrt{\alpha^2 / \tau_0^2 + \tau_0^2}$ characterizes the chirped pulse length and $a = \alpha / (\alpha^2 + \tau_0^4)$ is the frequency chirp rate.

- Secant pulse:

- Pulse shape of

$$f_{secant}(t) = A_{secant} \cdot \operatorname{sech}^2\left(\frac{t}{\tau_0}\right) = A_{secant} \cdot \left(\frac{2}{\exp(\frac{t}{\tau_0}) + \exp(-\frac{t}{\tau_0})}\right)^2 \quad (4.5)$$

with the normalization constant A_{secant} , the pulse duration τ_0 , the central frequency ω and the chirp coefficient α .

- Linear chirp of

$$\phi_{secant}(t) = \alpha_{secant} \left(\frac{t}{\tau_0}\right)^2 \quad (4.6)$$

The following discussion will assume a Gaussian laser shape as described by equation (4.3) and (4.4). A simulation for E is plotted for different chirp parameters α suitable to display strong and weak chirps in figure 4.2. As can be seen there, the chirp parameter strongly influences the shape of the electric field. If E could be measured directly, the chirp could be easily estimated. Unfortunately our Ti:Sa laser can produce laser pulses as short as 100 fs and response times of photodiodes and oscilliscopes are in the best case in the order of 200 fs. This means they cannot even measure the duration of these ultrashort pulses let alone resolve the pulse shape.

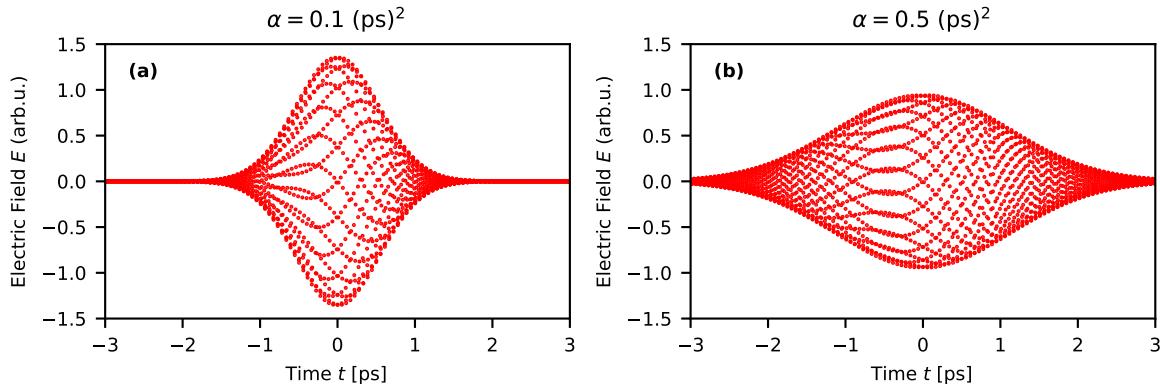


Figure 4.2.: Electric field E of Gaussian laser pulse of pulse duration $\tau_0 = 0.5$ ps for chirp of (a) $\alpha = 0 \text{ ps}^2$ and (b) $\alpha = 0.5 \text{ ps}^2$

4.3. Measuring the chirp with interferometric autocorrelation

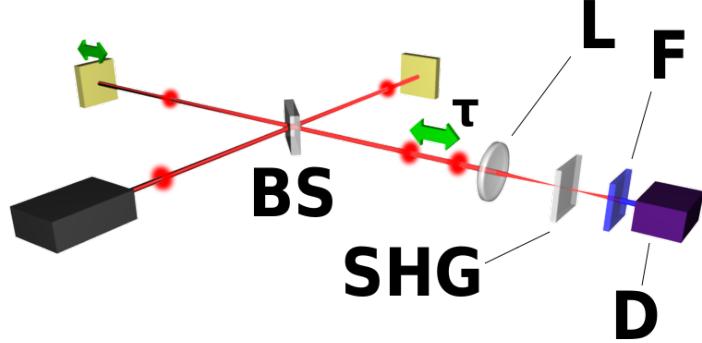


Figure 4.3.: Schematics of an interferometric autocorrelator, where **L** is a converging lens, **SHG** a second-harmonic generation crystal, **BS** a beam splitter, τ the interval between two pulses, **D** the detector and **F** a spectral filter to block the fundamental wavelength [33].

In order to estimate the pulse width τ_0 interferometric autocorrelation (IAC) is used. Basically, a nonlinear crystal is added to a Michelson interferometer in order to generate a signal governed by [34]

$$I_M(\tau) = \int_{-\infty}^{+\infty} \langle |(E(t) + E(t - \tau))^2|^2 \rangle dt. \quad (4.7)$$

Here $\langle \rangle$ denotes averaging over fast oscillations of the electric field.

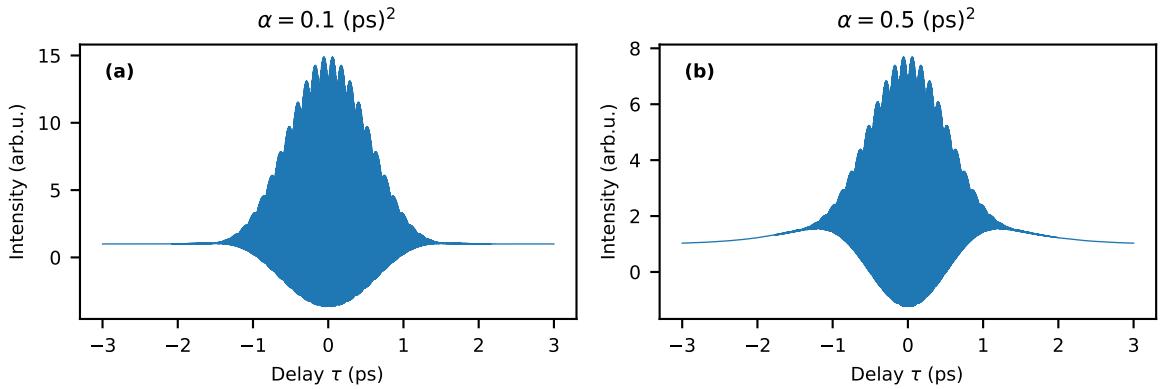


Figure 4.4.: Intensity of IAC of a Gaussian laser pulse of pulse duration $\tau_0 = 0.5$ ps with applied MOSAIC filter for chirp of (a) $\alpha = 0 \text{ ps}^2$ and (b) $\alpha = 0.5 \text{ ps}^2$

Under the use of equation 4.2, equation (4.7) can be expanded to

$$I_M(\tau) = 1 + 2 \int f(t)f(t+\tau)dt + \int f(t)f(t+\tau)\cos(2\omega\tau + 2\Delta\phi)dt \\ + 2 \int f^{1/2}(t)f^{3/2}(t+\tau)\cos(\omega\tau + \Delta\phi)dt + 2 \int f^{3/2}(t)f^{2/2}(t+\tau)\cos(\omega\tau + \Delta\phi)dt \quad (4.8)$$

where $\Delta\phi(t, \tau) = \phi(t + \tau) - \phi(t)$ and $\int f(t)dt = 1$.

As can be seen in figure 4.4 the chirp parameter α has hardly any measurable influence on the resulting signal. However, certain modifications to the IAC signal introduced by Hirayama and Sheik-Bahae [32] make it much more sensitive to the temporal chirp. It is called modified-spectrum autointerferometric correlation (MOSAIC) and it performs the following transformations on the IAC spectrum: the ω terms are eliminated and the 2ω term is doubled. The MOSAIC signal is then described by

$$I_{M,filtered}(\tau) = 1 + 2 \int f(t)f(t+\tau)dt + 2 \int f(t)f(t+\tau)\cos(2\omega\tau + 2\Delta\phi)dt. \quad (4.9)$$

When the MOSAIC filter is applied on the data shown in figure 4.4 it results in a signal as shown in figure 4.5. Here the influence of the chirp is clearly visible in the lower envelope.

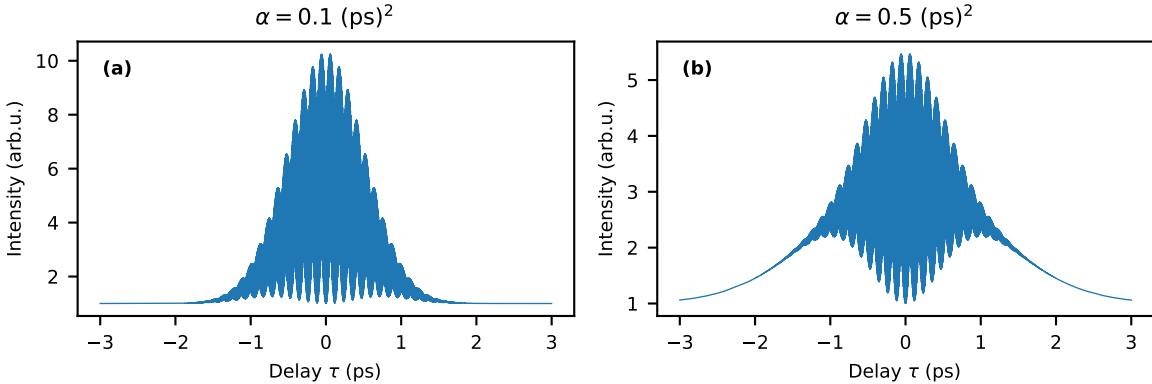


Figure 4.5.: Intensity of IAC of a Gaussian laser pulse of pulse duration $\tau_0 = 0.5$ ps with applied MOSAIC filter for chirp of (a) $\alpha = 0 \text{ ps}^2$ and (b) $\alpha = 0.5 \text{ ps}^2$

4. Entangled photon generation using adiabatic rapid passage with frequency-chirped pulses

The points of the lower envelope can be obtained by determining the local minima of the signal as shown in figure 4.6.

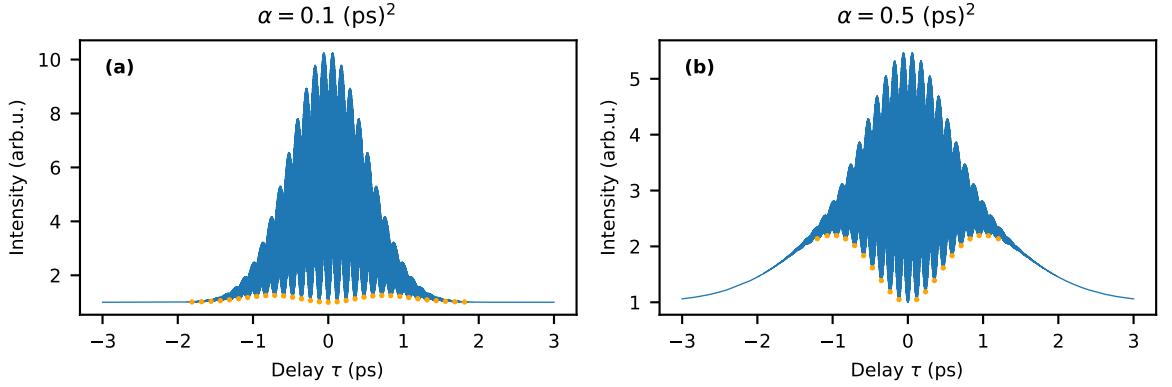


Figure 4.6.: Intensity of IAC of a Gaussian laser pulse of pulse duration $\tau_0 = 0.5$ ps with applied MOSAIC filter for chirp of (a) $\alpha = 0 \text{ ps}^2$ and (b) $\alpha = 0.5 \text{ ps}^2$. The orange dots are results of a numerical peak finder algorithm, executed in order to find local minima.

The lower bound (minima envelope) of the MOSAIC trace can be derived by use of the standard textbook procedure [35]

$$S_{\text{MOSAIC}}^{\min}(\tau) = 1 + 2 \cdot g(\tau) - 2 \cdot [g_s^2(\tau) + g_c^2(\tau)]^{1/2} \quad (4.10)$$

with

$$g(\tau) = \int f(t)f(t+\tau)dt \quad (4.11)$$

$$g_s(\tau) = \int f(t)f(t+\tau)\sin(2\Delta\phi)dt \quad (4.12)$$

$$g_c(\tau) = \int f(t)f(t+\tau)\cos(2\Delta\phi)dt \quad (4.13)$$

The points of the lower envelope determined before can now be fitted in order to obtain the chirp parameter α as shown in figure 4.7. It is visible that the fitted values of α correspond to the expected values.

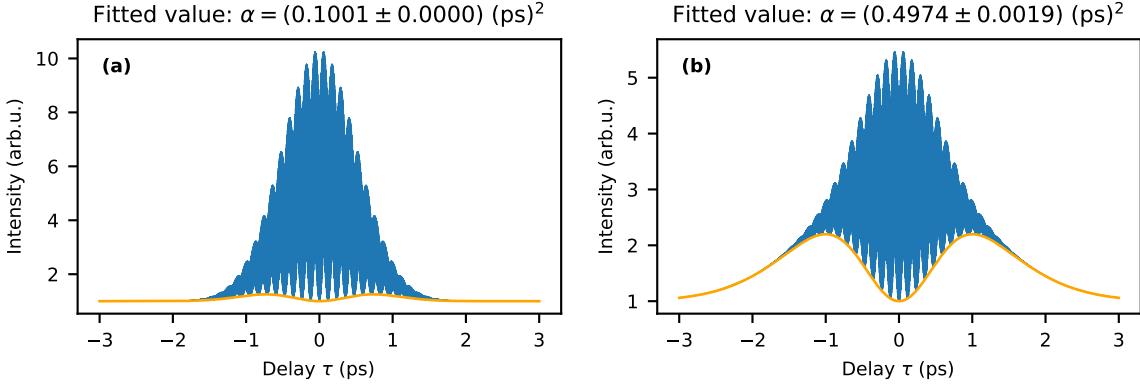


Figure 4.7.: Intensity of IAC of a Gaussian laser pulse of pulse duration $\tau_0 = 0.5$ ps with applied MOSAIC filter for chirp of (a) $\alpha = 0 \text{ ps}^2$ and (b) $\alpha = 0.5 \text{ ps}^2$. The orange line is a fit for the lower envelope of the MOSAIC signal in order to obtain α .

4.4. Deterministically adjusting the chirp with a pulse expander

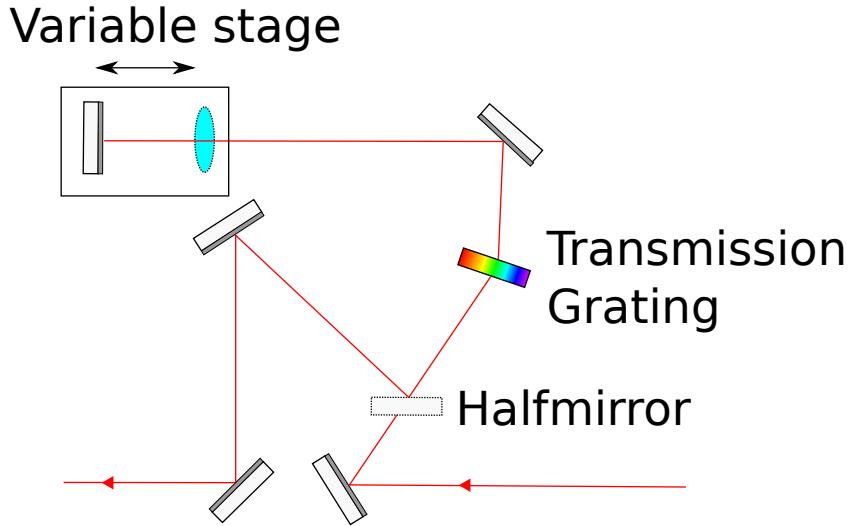


Figure 4.8.: Scheme of a folded pulse expander as described by Martinez [36]. The light enters on the right side, passes the halfmirror, and enters the system of transmission grating, lens and mirrors. Afterwards it hits the halfmirror and exits on the left hand.

In the optimal case the chirp of the pulse can be deterministically adjusted in order to most efficiently excite the QD via adiabatic rapid passage (which will be introduced in section 4.5). Grating compressors

as discussed by Martinez [36] were originally used to compensate the broadening effect fibers have on pulses. However, together with a telescope they have the inverse effect and can be used to induce a chirp. A setup like this is sketched in figure 4.8 and it will in future references in this work be called *pulse expander*. Its main elements are the transmission grating and the lens and a folded setup using a mirror after the lens is used in order to need only one of each. and the accumulated group velocity dispersion of the setup can be adjusted by changing the optical distance between these two. The accumulated group velocity dispersion can be adjusted by varying the optical distance d between the focal plane of the lens and the transmission grating and it is described by

$$\frac{d^2\Phi}{d\omega^2} = k\beta^2 2d \quad (4.14)$$

where β is a value depending on the parameters of the grating and the lens.

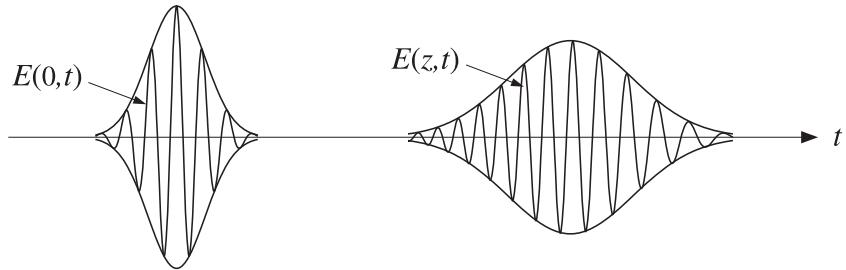


Figure 4.9.: Influence of group velocity dispersion for example inside a fiber on a Gaussian pulse [37]

As can be seen in figure 4.9, a group velocity dispersion has a similar effect on a Gaussian pulse as a chirp. In fact, the frequency chirp rate a_{gauss} introduced in equation (4.4) can be put into relation with it by: [37]

$$a_{gauss} = \frac{\frac{d^2\Phi}{d\omega^2}}{\tau_0^4 + \left(\frac{d^2\Phi}{d\omega^2}\right)^2} \quad (4.15)$$

4.5. Adiabatic rapid passage

One way to invert the QD from the ground state $|G\rangle$ to the biexciton state $|XX\rangle$ is by exciting it with a narrow-band laser pulse of constant centre frequency, which is equals to half of the ground state biexciton transition frequency. As described in equation (2.16), if the pulse area $\theta = \pi$, a population inversion from the $|G\rangle$ state to the $|XX\rangle$ occurs. However, the π -pulse method is not generally a robust scheme. In order to ensure the inversion, precise control of the field intensity is required [31]. Adiabatic rapid passage (ARP) with frequency chirped is a much more robust alternative to this Rabi-flopping

scheme. Here, the frequency of the laser signal is swept through resonance, starting slightly above or below the resonance frequency. The biexciton state can be populated with nearly perfect efficiency [31] if the process is performed adiabatically [38]

$$\Omega_0 \gg |d/dt\omega(t)| \quad (4.16)$$

where Ω_0 is the peak Rabi frequency and $\omega(t)$ is the center frequency of the laser pulse.

In figure 4.10 simulations in order to determine the final biexciton occupation for different biexciton binding energies Δ by Glässl et al. [31] are presented. Here, a linearly-chirped Gaussian laser pulse as discussed in section 4.2 was assumed.

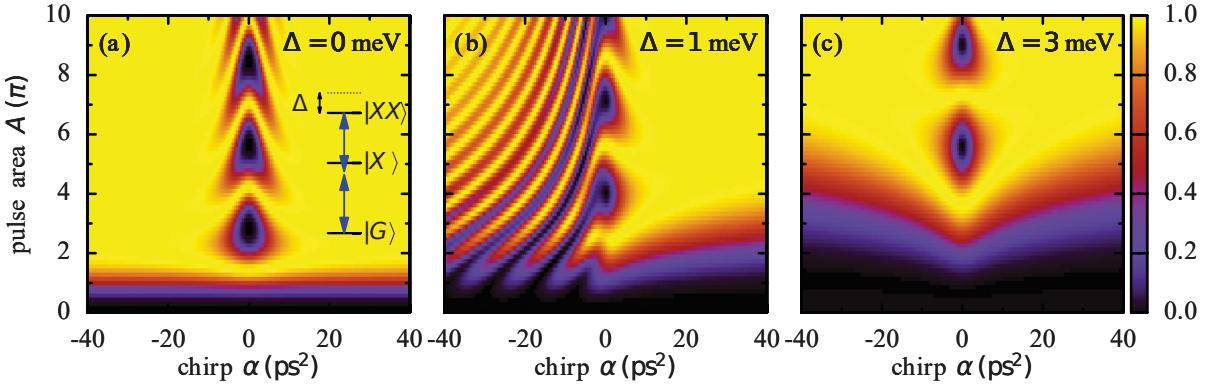


Figure 4.10.: Final biexciton occupation after chirped Gaussian pulse of pulse duration $\tau_0 = 2$ ps. It is plotted vertically as a function of the original pulse area A and vertically as a function of the chirp α for biexciton binding energies of (a) $\Delta = 0$, (b) 1, and (c) 3 meV [31].

The central frequency is chosen so that for $\alpha = 0$ it resonates to ground state biexciton transition, which is sketched in figure 4.10. For $\alpha = 0$ Rabi oscillations are visible and its period depends strongly on the biexciton binding energy Δ . However, for $\alpha \gg 0$ biexciton preparation becomes insensitive to small variations to the pulse area A as long it exceeds a certain threshold. This is therefore the regime which would be the most suitable to work in. In the case of $\alpha < 0$ this insensitivity does not appear for moderate values of Δ as can be seen in figure 4.10(b).

4.6. Measurements and discussion

Here I miss details about the measurement strategy. Explain why we measured such a short pulse. The goal was expanding much longer pulses for the final ARP. Go deeper here.

In order to determine the chirp of a laser pulse which only passed the pulse shaper as shown in figure 3.1, it was sent to the IAC. Afterwards, a signal was measured where an additional pulse expander was inserted as discussed in section 4.4. The comparison between these two is shown in figure 4.11. Compared to the simulations in figure 4.4 it is visible that the IAC of the laser pulse without the pulse expander fits the expected shape well, while the one with the pulse expander does not. Possible reasons could be that the chirp is too high for the model used in the simulation to work or that the pulse expander introduces side effects not considered in the simulation.

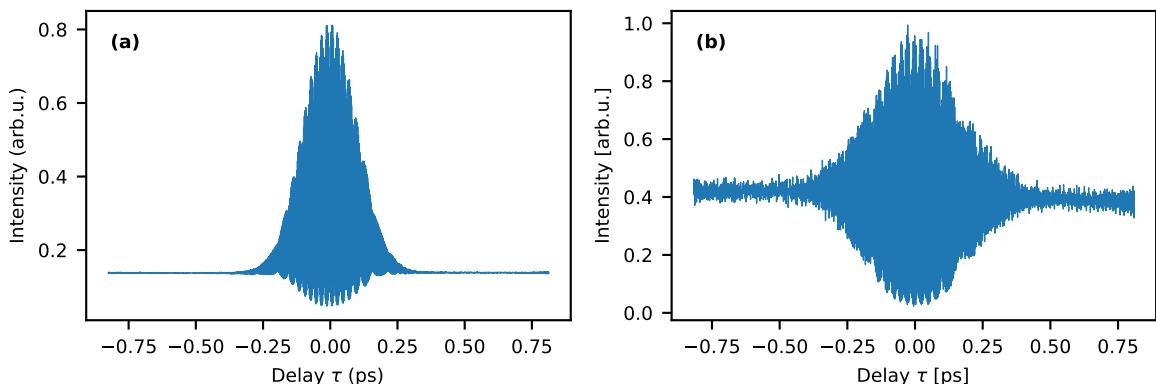


Figure 4.11.: Measured IAC of Ti:Sa Laser without (a) and with (b) pulse expander before the autocorrelator.

The same signals after applying the MOSAIC filter are shown in figure 4.12. It is visible that the lower envelopes in figure 4.12(a) and 4.12(b) do not resemble the expected ones in figure 4.5. As the laser signal without pulse expander was assumed to be relatively unchirped, it is already unexpected that the lower envelope differs that much from a constant line at zero intensity. One explanatory approach could be that the laser was already chirped to begin with. However, this would not explain why the shape of the lower envelope differs from the characteristic one of the simulation.

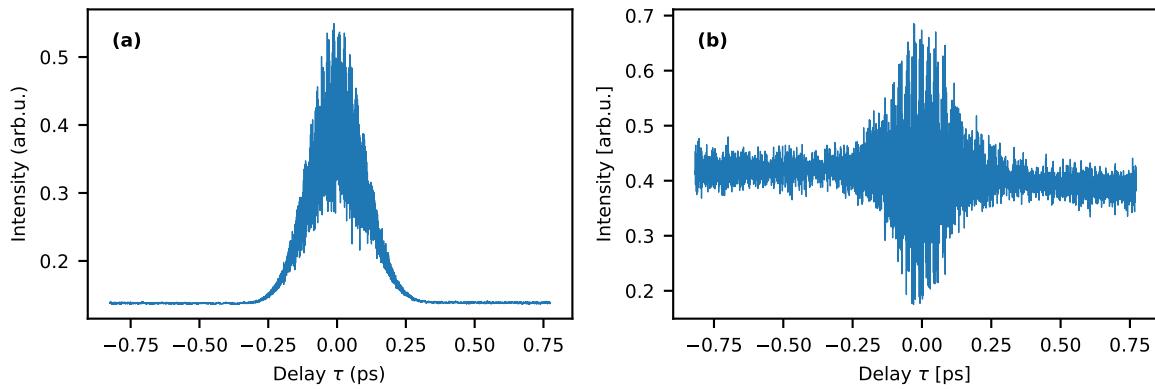


Figure 4.12.: Measured IAC of Ti:Sa Laser with applied MOSAIC filter without (a) and with (b) pulse expander before the autocorrelator.

Conclusion?
What can we
do to over-
come this in
the future?

5. Building up a scanning Fabry-Pérot interferometer from scratch

5.1. Introduction and motivation

The Fabry Pérot interferometer (FPI) is an optical resonator developed by Charles Fabry and Alfred Pérot. An incoming light beam will only be transmitted through the resonator consisting of two semi-transparent mirrors if it fulfills the resonance condition.[39]. The resonance frequencies can be changed by adjusting the mirror distance. By measuring the intensity at the output of the FPI, this can be used to resolve fine features of an electromagnetic spectrum, like e.g. the emitted light from the exciton-groundstate radiative decay described in section 2.3. The following chapter introduces basics of electromagnetic radiation, describes simulations performed to size the components of the FPI and displays measurement techniques used to obtain the resolved exciton spectrum.

5.2. Transverse modes of electromagnetic radiation

5.2.1. Gaussian beam

In this chapter, light beams are described by the wave picture according to Meschede [40]. They fulfil the Maxwell equations and therefore their electric field $\mathbf{E}(\mathbf{r}, t)$ fulfills the wave equation

$$\left(\nabla^2 - \frac{1}{c^2} \frac{\partial}{\partial t^2} \right) \mathbf{E}(\mathbf{r}, t) = 0. \quad (5.1)$$

Along the propagation direction z a light beam behaves similarly to a plane wave with constant amplitude A_0 which is a known solution to the wave equation (5.1)

$$E(z, t) = A_0 e^{-i(\omega t - kz)}. \quad (5.2)$$

5. Building up a scanning Fabry-Pérot interferometer from scratch

However, far from its source light is expected to behave like a spherical wave

$$E(\mathbf{r}, t) = A_0 \frac{e^{-i(\omega t - \mathbf{k}\mathbf{r})}}{|\mathbf{k}\mathbf{r}|}. \quad (5.3)$$

To get a better understanding of the propagation of light, only paraxial (near the z-axis) parts of the spherical wave are considered. Additionally, the wave is split into its longitudinal (z-axis) part and its transversal part and beams with axial symmetry are assumed, which only depend on a transversal coordinate ρ . Under these circumstances $\mathbf{k}\mathbf{r}$ can be replaced with kr and because of $\rho \ll r, z$ the Fresnel approximation can be applied:

$$E(\mathbf{r}) = \frac{A(\mathbf{r})}{|\mathbf{k}\mathbf{r}|} e^{ik\mathbf{r}} \simeq \frac{A(z, \rho)}{kz} \exp\left(i \frac{k\rho^2}{2z}\right) e^{ikz} \quad (5.4)$$

with $r = \sqrt{z^2 + \rho^2} \simeq z + \rho^2/2z$.

Equation (5.4) resembles the plain wave in equation (5.2), with the spacial phase transversal modulated by $\exp(ik\rho^2/2z)$. Another spherical wave solution can be obtained by applying the following replacement (z_0 is a real number)

$$z \rightarrow q(z) = z - iz_0 \quad (5.5)$$

with $q(z)$ as the complex beam parameter. Thereby, the fundamental (or TEM₀₀) Gaussian mode has been constructed

$$E(z, \rho) \simeq \frac{A_0}{kq(z)} \exp\left(i \frac{k\rho^2}{2q(z)}\right) e^{ikz}. \quad (5.6)$$

The electric and magnetic fields of Gauss modes are transversal to its propagation direction. These waveforms are called transversal electric and magnetic modes with indices (m, n) . Its fundamental solution is the TEM₀₀-Mode, which is the most important one and will therefore be examined in more detail in the rest of this subsection.

By executing the replacement $q(z) \rightarrow z - iz_0$ explicitly the equation (5.6) can be expressed as

$$\frac{1}{q(z)} = \frac{z + iz_0}{z^2 + z_0^2} = \frac{1}{R(z)} + i \frac{2}{k\omega^2(z)}, \quad (5.7)$$

with new variables z_0 , $R(z)$ and $\omega(z)$ being introduced. With the decomposition of the Fresnel factors into real and imaginary part, two factors can be identified: one complex phase factor, which describes the curvature of the wavefronts and a real factor, which describes the envelope of the beam. Therefore, the exponential in equation (5.6) becomes

$$\exp\left(i \frac{k\rho^2}{2q(z)}\right) \rightarrow \exp\left(i \frac{k\rho^2}{2R(z)}\right) \exp\left(-\left(\frac{\rho}{\omega(z)}\right)^2\right) \quad (5.8)$$

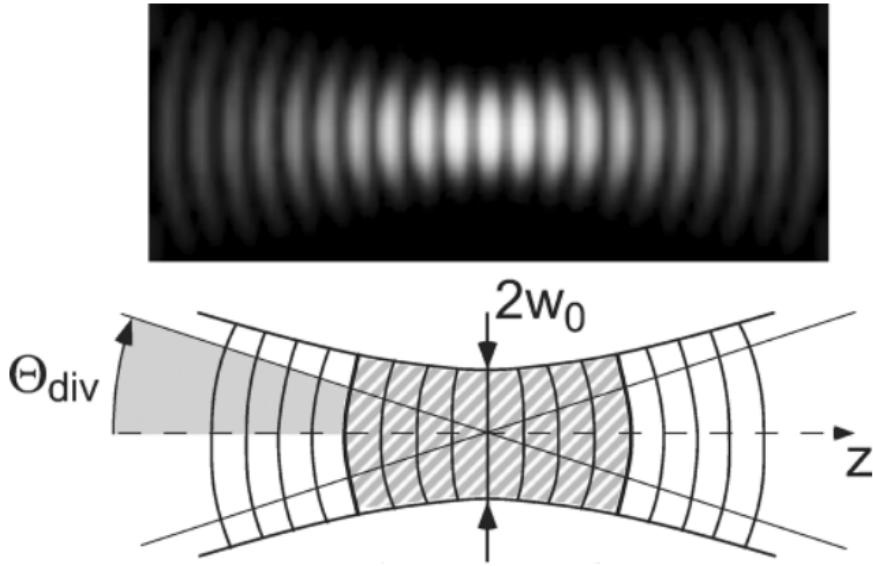


Figure 5.1.: A Gaussian beam near its beam waist. Near the center they resemble plan wave fronts, while outside they converge towards spherical wave fronts. They Rayleighzone is shaded at the lower part of the figure.[40]

For a proper description of a Gaussian beam as shown in figure 5.1 the following parameters have to be introduced

- **Evolving radius of curvature $R(z)$:**

$$R(z) = z(1 + (z_0/z)^2) \quad (5.9)$$

- **Beam waist $2\omega_0$:**

$$\omega_0^2 = \lambda z_0 / \pi \quad (5.10)$$

The beam waist $2\omega_0$ or beam radius ω_0 describes the smallest beam cross section at $z = 0$. If the wave propagates inside a medium with the refractive index n , λ has to be replaced with λ/n . The cross section of the beam waist is then $\omega_0^2 = \lambda z_0 / (\pi n)$.

A Gaussian beam can be completely characterized at every point z on the beam axis either with the parameter couple (ω_0, z_0) or alternatively with the real and imaginary part of $q(z)$. The parameters of the Gaussian beam are transformed by the ray transfer matrix

$$q_{out} = \frac{Aq_{in} + B}{Cq_{in} + D} \quad (5.11)$$

with the parameters A, B, C, D determined by the optical element transforming the Gaussian beam described by q_{in} .

where do
this elements
come from
and which
basis is used
by this ma-
trix formalism.
Without these
definitions,
these letters
mean nothing.

5.2.2. Higher Gauss modes

The wave equation (5.1) can be simplified by only allowing monochromatic waves with harmonic time dependence

$$\mathbf{E}(\mathbf{r}, t) = \text{Re} \left(\mathbf{E}(\mathbf{r}) e^{-i\omega t} \right). \quad (5.12)$$

With $\omega^2 = c^2 \mathbf{k}^2$, the *Helmholtz equation* can be deduced, which only depends on the location \mathbf{r}

$$(\nabla^2 + \mathbf{k}^2) \mathbf{E}(\mathbf{r}) = 0. \quad (5.13)$$

In favor of a formal treatment of the Gaussian modes, the Helmholtz equation is split into its transversal and longitudinal contributions,

$$\nabla^2 + k^2 = \frac{\partial^2}{\partial z^2} + \nabla_T^2 + k^2 \quad \text{with} \quad \nabla_T^2 = \frac{\partial}{\partial x^2} + \frac{\partial}{\partial y^2}. \quad (5.14)$$

Additionally, the electric field E of equation (5.4) is inserted into the Helmholtz equation. It is also assumed that the amplitude A only changes slowly in the order of the wavelength,

$$\frac{\partial}{\partial z} A = A' \ll kA, \quad (5.15)$$

which allows the approximation

$$\frac{\partial^2}{\partial z^2} A e^{ik\rho^2/(2z)} \frac{e^{ikz}}{kz} \simeq (2ikA' - k^2 A) e^{ik\rho^2/(2z)} \frac{e^{ikz}}{kz}, \quad (5.16)$$

and results in the *paraxial Helmholtz equation*,

$$\left(\nabla_T^2 + 2ik \frac{\partial}{\partial z} \right) A(\rho, z) = 0. \quad (5.17)$$

The fundamental solution is the TEM₀₀ mode in equation (5.6). Examples of higher modes can be found in figure 5.2.

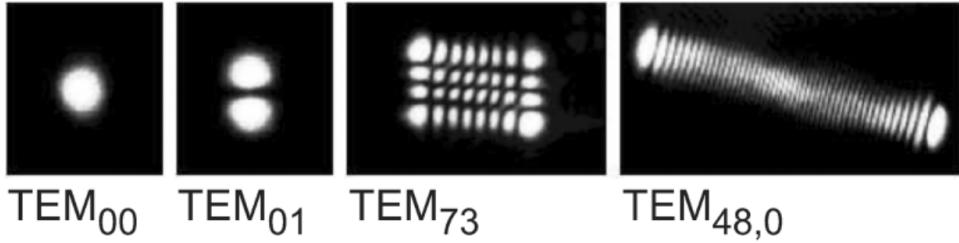


Figure 5.2.: Gaussian modes higher order of a simple Ti-sapphire laser. The asymmetry of the high modes are caused by technical inaccuracies of the resonator elements (mirrors, laser crystal).

5.3. Fundamentals of Fabry-Pérot interferometers

5.3.1. Resonator losses

For the following discussion of the FPI, a two-mirror-resonator with the reflecting surfaces facing each other and air as medium in between is assumed. The theoretical foundation is provided by the work of Ismail et al. [41].

The time the light needs for one roundtrip is given by

$$t_{RT} = \frac{2l}{c} \quad (5.18)$$

where l is the geometrical length of the resonator and c is the speed of light in air.

The photon-decay time τ_c of the interferometer is then given by

$$\frac{1}{\tau_c} = -\frac{\ln(R_1 \cdot R_2)}{t_{RT}} \quad (5.19)$$

where R_1 and R_2 are the corresponding intensity reflectivities of the mirrors.

The number of photons at frequency ν inside the resonator is described by the differential rate equation

$$\frac{d}{dt} \varphi(t) = -\frac{1}{\tau_c} \varphi(t). \quad (5.20)$$

With a number φ_s of photons at $t = 0$ the integration gives

$$\varphi(t) = \varphi_s e^{-t/\tau_c} \quad (5.21)$$

5.3.2. Resonance frequencies, free spectral range and spectral line shapes

The round-trip phase shift at frequency ν is given by

$$2\phi(\nu) = 2\pi\nu t_{RT} = 2\pi\nu \frac{2l}{c} \quad (5.22)$$

where $\phi(\nu)$ is the single-pass phase shift between the mirrors.

Resonances are visible for frequencies ν at which the light interferes constructively after one round trip. Two adjacent resonance frequencies differ in their round trip phase shift by 2π . Hence, the free spectral range $\Delta\nu_{FSR}$, the frequency difference between two adjacent resonance frequencies, can be calculated from equation (5.22)

$$2\Delta\phi_{FSR} = 2\pi \quad (5.23)$$

$$\Rightarrow 2\pi\Delta\nu_{FSR} \frac{2l}{c} = 2\pi \quad (5.24)$$

$$\Rightarrow \Delta\nu_{FSR} = \frac{c}{2l} \quad (5.25)$$

According to equation (5.21) the number of photons decays with the photon-decay time τ_c . With $E_{q,s}$ representing the initial amplitude, the electric field at ν_q is given by

$$E_q(t) = \begin{cases} E_{q,s} \cdot e^{i2\pi\nu_q t} \cdot e^{-t/(2\tau_c)} & t \geq 0 \\ 0 & t < 0 \end{cases}. \quad (5.26)$$

The Fourier transformation of the electric field can be expressed as

$$\tilde{E}_q(\nu) = \int_{-\infty}^{\infty} E_q(t) e^{-i2\pi\nu t} dt = E_{q,s} \int_0^{\infty} e^{[1/(2\tau_c) + i2\pi(\nu - \nu_q)]t} dt = E_{q,s} \frac{1}{(2\tau_c)^{-1} + i2\pi(\nu - \nu_q)}. \quad (5.27)$$

The normalized spectral line shape per unit frequency is then given by

$$\tilde{\gamma}_q(\nu) = \frac{1}{\tau_c} \left| \frac{\tilde{E}_q(\nu)}{E_{q,s}} \right|^2 = \frac{1}{\tau_c} \left| \frac{1}{(2\tau_c)^{-1} + i2\pi(\nu - \nu_q)} \right|^2 = \frac{1}{\tau_c} \frac{1}{(2\tau_c)^{-2} + 4\pi^2(\nu - \nu_q)^2} \quad (5.28)$$

$$= \frac{1}{\pi} \frac{1/(4\pi\tau_c)}{1/(4\pi\tau_c)^2 + (\nu - \nu_q)^2} \quad (5.29)$$

with $\int \tilde{\gamma}_q(\nu) d\nu = 1$.

By defining the full-width-at-half-maximum linewidth (FWHM) $\Delta\nu_c$, $\tilde{\gamma}_q(\nu)$ can be obtained

$$\Delta\nu_c = \frac{1}{2\pi\tau_c} \Rightarrow \tilde{\gamma}_q(\nu) = \frac{1}{\pi} \frac{\Delta\nu_c/2}{(\Delta\nu_c/2)^2 + (\nu - \nu_q)^2}. \quad (5.30)$$

Afterwards the Cauchy lines are normalized so that the peak is at unity

$$\gamma_{q,L}(\nu) = \frac{\pi}{2} \Delta\nu_c \tilde{\gamma}_q(\nu) = \frac{(\Delta\nu_c)^2}{(\Delta\nu_c)^2 + 4(\nu - \nu_q)^2} \quad (5.31)$$

with $\gamma_{q,L}(\nu_q) = 1$.

5.3.3. Airy distribution of Fabry-Pérot interferometers

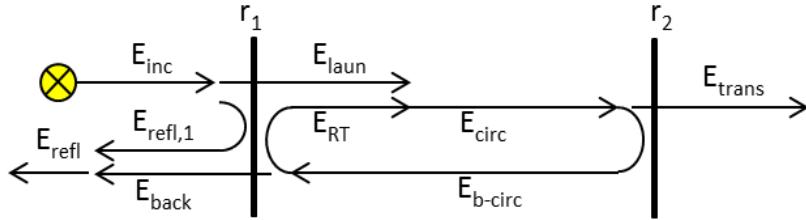


Figure 5.3.: FPI with electric field mirror reflectivities r_1 and r_2 . Indicated in this figure are the electric fields resulting from an incoming E_{inc} , the reflected field $E_{refl,1}$ and transmitted field E_{laun} . E_{circ} and $E_{circ,b}$ circulate inside the resonator, resulting in E_{RT} after one round-trip. E_{back} is the backwards transmitted field.[42]

The response of the FPI is calculated with the circulating-field approach [41], where a steady-state is assumed. E_{circ} is the result of E_{laun} interfering with E_{RT} . E_{laun} is the transmission of the incoming light E_{inc} and E_{RT} is E_{circ} after one round-trip in the resonator, i.e., after the outcoupling losses of mirror 1 and 2. Therefore, the field E_{circ} can be calculated from E_{laun} by

$$E_{circ} = E_{laun} + E_{RT} = E_{laun} + r_1 r_2 e^{-i2\phi} E_{circ} \Rightarrow \frac{E_{circ}}{E_{laun}} = \frac{1}{1 - r_1 r_2 e^{-i2\phi}} \quad (5.32)$$

where r_1 and r_2 are the electric-field reflectivities of mirror 1 and 2.

The generic Cauchy distribution only considers light inside the mirrors and is defined as

$$A_{circ} = \frac{I_{circ}}{I_{laun}} = \frac{|E_{circ}|^2}{|E_{laun}|^2} = \frac{1}{|1 - r_1 r_2 e^{-i2\phi}|^2} = \frac{1}{(1 - \sqrt{R_1 R_2})^2 + 4\sqrt{R_1 R_2} \sin^2(\phi)} \quad (5.33)$$

by using

$$\begin{aligned} |1 - r_1 r_2 e^{-i2\phi}|^2 &= |1 - r_1 r_2 \cos(2\phi) + i r_1 r_2 \sin(2\phi)|^2 = [1 - r_1 r_2 \cos(2\phi)]^2 + r_1^2 r_2^2 \sin^2(2\phi) \\ &= 1 + R_1 R_2 - 2\sqrt{R_1 R_2} \cos(2\phi) = (1 - \sqrt{R_1 R_2})^2 + 4\sqrt{R_1 R_2} \sin^2(\phi) \end{aligned}$$

and additionally $R_i = r_i^2$ and $\cos(2\phi) = 1 - 2\sin^2(\phi)$.

5. Building up a scanning Fabry-Pérot interferometer from scratch

Commonly, light is sent through the FPI. Therefore the following sections will use the Airy distribution A'_{trans} described by

$$A'_{trans} = \frac{I_{trans}}{I_{inc}} = \frac{I_{circ} \cdot (1 - R_2)}{I_{laun} / (1 - R_1)} = (1 - R_1)(1 - R_2) A_{circ} = \frac{(1 - R_1)(1 - R_2)}{(1 - \sqrt{R_1 R_2})^2 + 4\sqrt{R_1 R_2} \sin^2(\phi)} \quad (5.34)$$

with $\phi = \frac{\pi v}{\Delta\nu_{FSR}}$.

A'_{trans} is displayed in figure 5.4 for $R_1 = R_2$. The peak value at one of its resonance frequencies calculates as follows

$$\max(A'_{trans}) = \frac{(1 - R_1)(1 - R_2)}{(1 - \sqrt{R_1 R_2})^2} \stackrel{R_1=R_2}{=} 1. \quad (5.35)$$

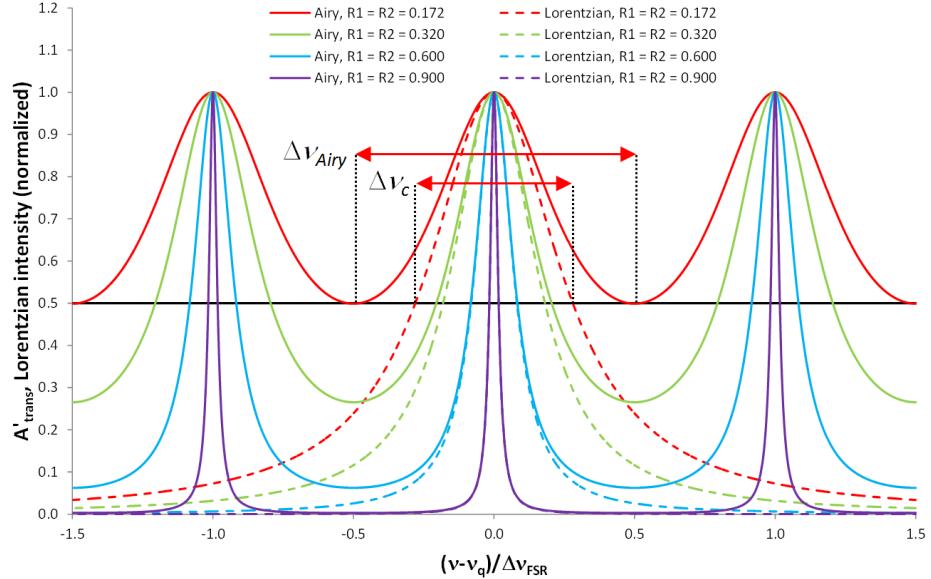


Figure 5.4.: Airy distribution A'_{trans} as described in equation (5.34) compared to the Cauchy lines $\gamma_{q,L}$ as described in equation (5.31) [42].

5.3.4. Airy linewidth and finesse

The airy linewidth is defined as the FWHM of A'_{trans} . It can be set in relation with the free spectral range $\Delta\nu_{FSR}$ and the mirror reflectivities as follows.

A'_{trans} decreases to half of its peak value at $A'_{trans}(v_q)/2$ when the phase shift ϕ changes by the amount

$\Delta\phi$ so that the denominator of A'_{trans} in equation (5.34) is twice as big

$$\left(1 - \sqrt{R_1 R_2}\right)^2 = 4\sqrt{R_1 R_2} \sin^2(\Delta\phi) \quad (5.36)$$

$$\Rightarrow \Delta\phi = \arcsin\left(\frac{1 - \sqrt{R_1 R_2}}{2\sqrt[4]{R_1 R_2}}\right) \quad (5.37)$$

With equation (5.22) and (5.25), the phase shift can be expressed as

$$\phi = \frac{\pi\nu}{\Delta\nu_{FSR}} \quad (5.38)$$

$$\Rightarrow \Delta\phi = \frac{\pi(\Delta\nu_{Airy}/2)}{\Delta\nu_{FSR}}. \quad (5.39)$$

Therefore, with equation (5.37) and (5.39) the FWHM linewidth is given by

$$\Delta\nu_{Airy} = \Delta\nu_{FSR} \frac{2}{\pi} \arcsin\left(\frac{1 - \sqrt{R_1 R_2}}{2\sqrt[4]{R_1 R_2}}\right). \quad (5.40)$$

The finesse of the Airy distribution of a FPI is defined as

$$F_{Airy} := \frac{\Delta\nu_{FSR}}{\Delta\nu_{Airy}} = \frac{\pi}{2} \left[\arcsin\left(\frac{1 - \sqrt{R_1 R_2}}{2\sqrt[4]{R_1 R_2}}\right) \right]^{-1} \quad (5.41)$$

and is therefore only dependent on the mirror reflectivities R_1 and R_2 .

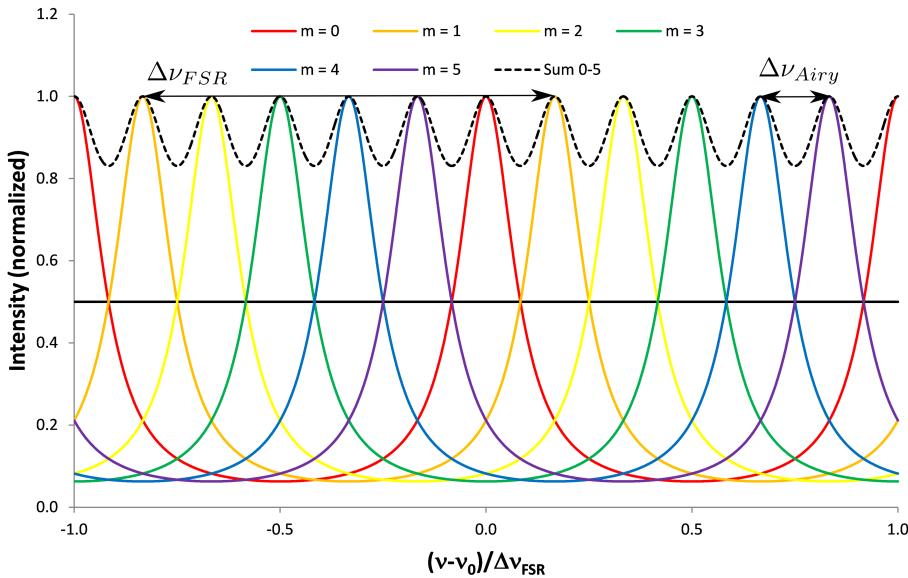


Figure 5.5.: Demonstration of the physical meaning of the Airy finesse F_{Airy} . The coloured lines are Airy distributions created by light at distinct frequencies ν_m , while scanning the resonator length. When the light occurs at frequencies $\nu_m = \nu_q + m\Delta\nu_{Airy}$, the adjacent Airy distributions are separated from each other by ν_{Airy} , therefore fulfilling the Taylor criterion. Since in this example $F_{Airy} = 6$ exactly six peaks fit inside the free spectral range. As can be seen in the figure the Airy finesse F_{Airy} quantifies the maximum number of peaks that can be resolved [42].

5. Building up a scanning Fabry-Pérot interferometer from scratch

The Airy finesse is the determining property when it comes to the spectral resolution of the FPI. This can be made visible by comparing its message with the Taylor criterion for the resolution of two adjacent peaks. The Taylor criterion proposes that two spectral lines are resolvable when the separation of the maxima is greater than the FWHM. As displayed in figure 5.5, the Airy finesse is equal to the number of Airy distributions originating from light at certain frequencies ν_m which do not overlap at a point higher than half of their maxima. Hence, the Airy finesse describes the spectral resolution in a way that is consistent with the Taylor criterion.

5.3.5. Mode matching and spatial filtering

One fundamental challenge of Fabry Pérot interferometry is how to efficiently couple an incident beam of light into a given mode of the resonator. The following discussion is based on the work of Yariv, Yeh, and Yariv [43] and Meschede [40].

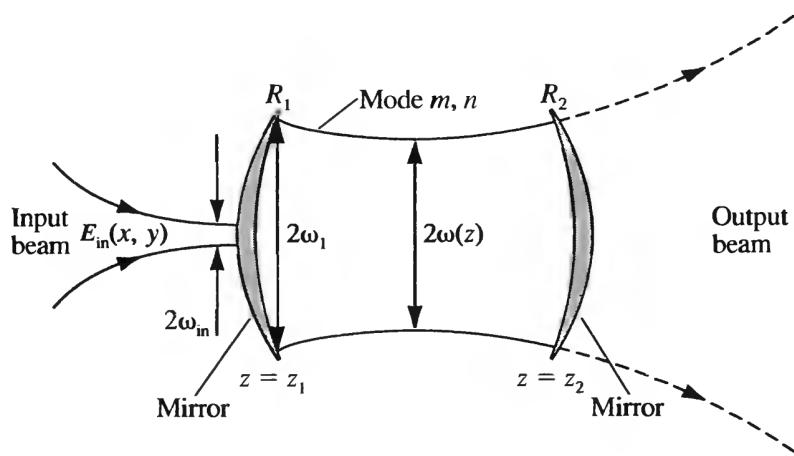


Figure 5.6.: Incident monochromatic beam of light exciting transverse mode m, n of a resonator [43]

In sketched with figure 5.6, an input beam E_{in} propagates into the resonator and potentially excite its modes $E_{mn}(x, y)$, where m, n are the transverse mode integers of the Gaussian beam of the optical resonator. Since $E_{mn}(x, y)$ describes a complete orthogonal set of wavefunctions they satisfy

$$\iint E_{mn}(x, y) E_{m'n'}^*(x, y) dx dy = 0 \quad \text{unless } m = m' \text{ and } n = n'. \quad (5.42)$$

and

$$E_{in}(x, y) = \sum_{mn} a_{mn} E_{mn}(x, y) \quad (5.43)$$

where a_{mn} are constants. By multiplying both sides of equation (5.43) with E_{mn}^* , integrating over the whole x - y -plane and using equation (5.42), the following expression can be obtained

$$a_{mn} = \frac{\iint E_{in}(x,y)E_{mn}^*(x,y)dxdy}{\iint E_{mn}(x,y)E_{mn}^*(x,y)dxdy} \quad (5.44)$$

The efficiency of coupling an incident field into a spatial mode E_{mn} is defined as

$$\eta_{mn} = \frac{\text{Power coupled into mode } mn}{\text{Total incident power}} = \frac{\iint |a_{mn}E_{mn}(x,y)|^2 dxdy}{\iint |E_{in}(x,y)|^2 dxdy}. \quad (5.45)$$

By inserting equation (5.44) into equation (5.45) the following expression can be obtained

$$\eta_{mn} = \frac{|\iint E_{in}(x,y)E_{mn}^*(x,y)dxdy|^2}{\iint |E_{in}(x,y)|^2 dxdy \cdot \iint |E_{mn}(x,y)|^2 dxdy}. \quad (5.46)$$

From equation (5.46) can be deduced that for an input beam with the *same* spatial dependency as the mode to be excited

$$E_{in}(x,y) \sim E_{mn}(x,y) \quad (5.47)$$

all of the incident power goes into E_{mn} , i.e. $\eta_{mn} = 1$ and all other $\eta_{m'n'}$ are zero. Usually, the fundamental TEM₀₀ mode is desired and equation (5.46) implies that a pure Gaussian beam excites only the fundamental mode and the interferometer will then irradiate a pure Gaussian beam as well. In practise, additional measures are necessary such as matching the radius of curvature by Gaussian beam focusing.

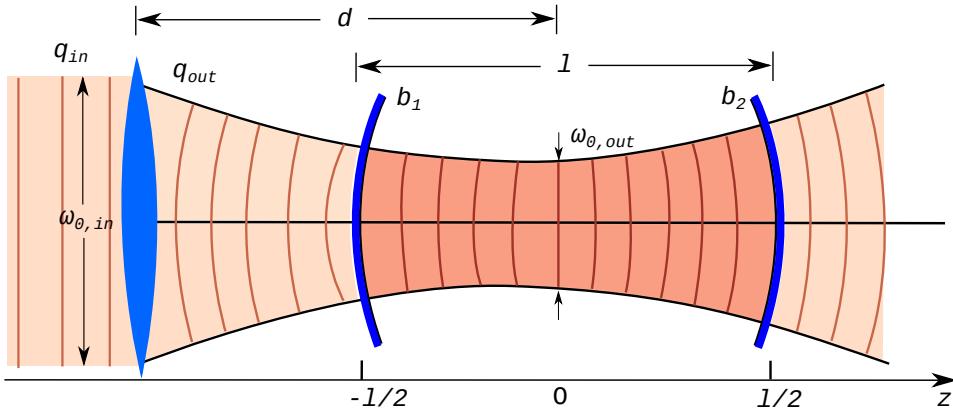


Figure 5.7.: Mode matching of an Gaussian beam into a Fabry Pérot interferometer. Incoming Gaussian beam described by q_{in} transformed by a lens into a Gaussian beam described by q_{out} . The parameters b_1 and b_2 describe the radii of the two mirrors.

In order to match the radius of curvature of the incoming Gaussian beam with the radius of curvature of the resonator a lens is inserted as depicted in figure 5.7. Light with a beam waist of ω_{01} gets focused

into the resonator. Transformations by thin lenses can be described with the ABCD-rule introduced in subsection 5.2.1:

$$\begin{pmatrix} A & B \\ C & D \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ \frac{-1}{f} & 1 \end{pmatrix} \quad (5.48)$$

with f as the wavelength of the lens. The incoming beam described by q_{in} is transformed by the lens into a beam described by q_{out} according to equation (5.10) and (5.11)

$$q_{in} = z + i \frac{\pi n \omega_{0,in}^2}{\lambda} \quad \text{and} \quad q_{out} = \frac{q_{in}}{q_{in} \cdot \frac{-1}{f} + 1} = z + i \frac{\pi n \omega_{0,out}^2}{\lambda} \quad (5.49)$$

with $n \approx 1$ for air. Together with equation (5.10) the following relation can be deduced

$$\omega_{0,out}^2 = \frac{\omega_{0,in}^2}{\left(1 - \frac{z}{f}\right)^2 + \left(\frac{\pi \omega_{0,in}}{\lambda f}\right)^2}. \quad (5.50)$$

The radii of curvature have to match. For given mirrors (described by R_{mirror}) and lens (described by f) the input beam waist has to be adjusted according to equation (5.9) and (5.10)

$$R_{mirror} \stackrel{!}{=} R_{gauss}(z = l/2) \quad (5.51)$$

$$R_{mirror} \stackrel{!}{=} \frac{l}{2} \left(1 + \left(\frac{2z_{0,out}}{l}\right)^2\right) \quad (5.52)$$

$$R_{mirror} \stackrel{!}{=} \frac{l}{2} \left(1 + \left(\frac{2\omega_{0,out}^2 \pi}{l \lambda}\right)^2\right). \quad (5.53)$$

Inserting equation (5.53) into equation (5.50) results in the condition for mode matching

$$R_{mirror} = \frac{l}{2} \left(1 + \left(\frac{\frac{2\omega_{0,in}^2 \pi}{l \lambda}}{\left(\left(1 - \frac{z}{f}\right)^2 + \left(\frac{\pi \omega_{0,in}}{\lambda f}\right)^2\right) l \lambda}\right)^2\right). \quad (5.54)$$

One way to further suppress higher modes is *spatial filtering*. It can be seen in figure 5.2 that the effective area of a mode increases with its order (m, n). Figure 5.8 shows one way to suppress higher modes consisting of a focusing lens and a pin hole which diameter matches the one of the TEM₀₀ mode.

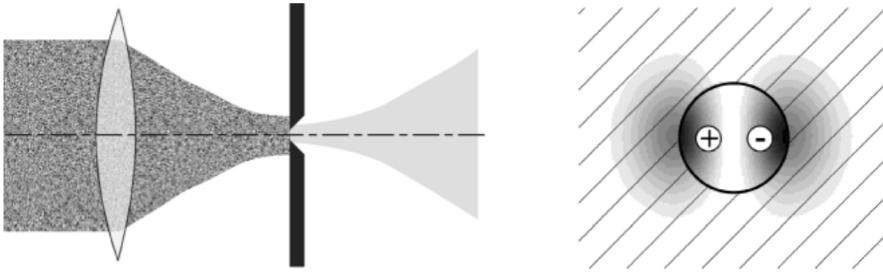


Figure 5.8.: Spatial filtering of Gauss modes. In front of the aperture, the beam consists of a superposition of multiple Gauss modes. In the example of TEM₀₁ is displayed how higher modes are suppressed by the aperture. [40]

5.3.6. Confocal setup

If the incoming beam would represent a perfect TEM₀₀ mode, spatial filtering would not be necessary and mode matching would not have to be done as precise. Unfortunately, this can not always be guaranteed and counteractions like mode matching and spatial filtering discussed in subsection 5.3.5 are tedious and error prone. Arranging the mirrors of an FPI into a confocal arrangement reduces the need for these measures. By giving up the ability to choose different free spectral ranges with a given pair of mirrors, the confocal setup liberates from mode matching considerations as the cavity is mode degenerated, i.e. the frequency of certain axial and transverse cavity modes are the same. The following discussion is based on the work of Hercher [44].

A quasi-monochromatic beam of wavelength λ_0 is composed of transverse modes TEM_{mnq}, where the subscripts m and n denote the amplitude distribution of the normal mode on a surface of constant phase and q the number of axial modes inside the resonator. Each of these modes resonates for mirror separations satisfying

$$l = \frac{\lambda_0}{2} \{q + (1 + m + n) \cos^{-1} [(1 - l/b_1)(1 - l/b_2)]^{1/2}\} \quad (5.55)$$

where the parameters b_1 and b_2 describe the radii of the two mirrors as can be seen in figure 5.7.

For the confocal setup $l = b_1 = b_2$ justifies the approximation

$$l \approx \frac{\lambda_0}{2} [q + (1 + m + n)]. \quad (5.56)$$

The modes resonate at mirror separations of either

$$l = \frac{\lambda_0}{2}(p+1) \quad p \in \mathbb{N} \text{ and } (m+n) \text{ even}, \quad (5.57)$$

$$l = \frac{\lambda_0}{2}(p) \quad p \in \mathbb{N} \text{ and } (m+n) \text{ odd}. \quad (5.58)$$

If mode matching is not executed, it can be assumed that the incoming beam consists of an approximately equal number of even and odd transverse modes. The resonance cavity length l does not depend on n, m and q anymore but only on one integer p . The transversal modes are degenerate and fulfil

$$l = \frac{\lambda_0 p}{2}. \quad (5.59)$$

It can be additionally concluded from equation (5.59) that a change of $\lambda_0/2$ in the mirror separation scans through one free spectral range.

5.4. Simulation

The goal in building up a scanning FPI is to resolve features of the emission spectra of GaAs quantum dots described in chapter 2. More precisely, it is intended to resolve the shape of the ZPL and the PSB. Equation 5.41 shows that the finesse is constant for a given pair of mirrors. If the spectrum to be resolved is broad, a higher free spectral range $\Delta\nu_{FSR}$ has to be chosen, under the loss of resolution. If the spectrum contains fine details which need to be resolved, a lower ν_{Airy} has to be chosen, which results in a lower free spectral range $\Delta\nu_{FSR}$. Hence, the thin ZPL and the broad PSB can not be resolved with the same setup. Instead, the mirror distances have to be adjusted and in the confocal setup discussed in subsection 5.3.6 the mirrors have to be changed as well.

The zero-phonon line is described with a Cauchy distribution

$$\Phi_{ZPL}(\lambda) = \frac{1}{\pi \cdot \Delta\lambda_{ZPL} \cdot 0.5 \left[1 + \left(\frac{\lambda - \lambda_{0,ZPL}}{\Delta\lambda_{ZPL} \cdot 0.5} \right)^2 \right]} \quad (5.60)$$

with $\lambda_{0,zero}$ as the center wavelength and $\Delta\lambda_{ZPL}$ as the spectral range of the zero-phonon line which can be found in table 2.1.

The phonon side band is described with a Gauss distribution

$$\Phi_{PSB}(\lambda) = \frac{1}{\sqrt{2 \cdot \pi \cdot \Delta\lambda_{PSB}^2}} \cdot \exp \left(-\frac{(\lambda - \lambda_{0,PSB})^2}{2 \cdot \Delta\lambda_{PSB}^2} \right) \quad (5.61)$$

5.4. Simulation

with $\lambda_{0,PSB}$ as the center wavelength and $\Delta\lambda_{PSB}$ as the spectral range of the phonon side band which can be found in table 2.1 as well.

Together they describe the excitonic emission of the QD

$$\Phi_{dot}(\lambda) = \Phi_{ZPL}(\lambda) + \Phi_{PSB}(\lambda) \quad (5.62)$$

depicted in figure 5.9.

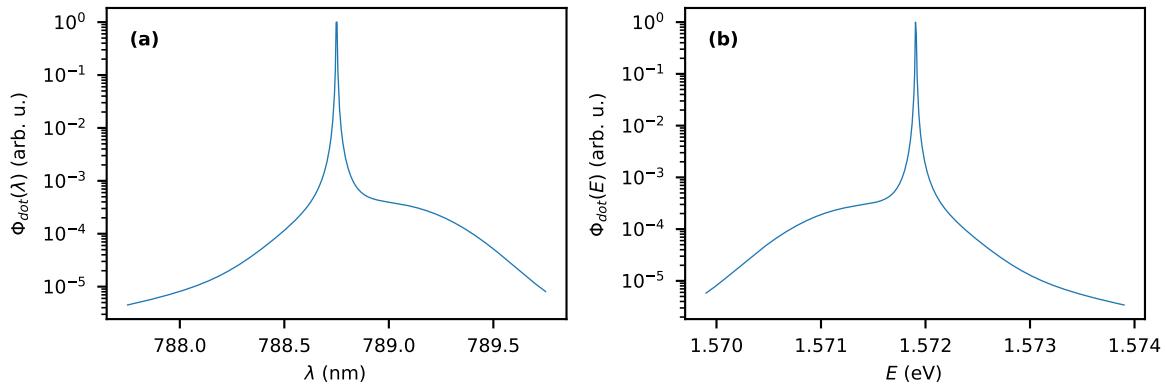


Figure 5.9.: Simulated exciton emission of a GaAs quantum dot plotted dependant on (a) the wavelength λ or (b) the energy E . The parameters can be found in table 2.1.

$\Phi_{dot}(E)$ is transmitted through the FPI. As discussed the mirror distance l is adjusted to a value which depends if a resolved ZPL or a resolved PSB is desired. A comparison of the FPI transmission $A'_{trans}(E)$ described in equation 5.34 with $R_1 = R_2 = 98\%$ and $\Phi_{dot}(E)$ is shown in figure 5.10.

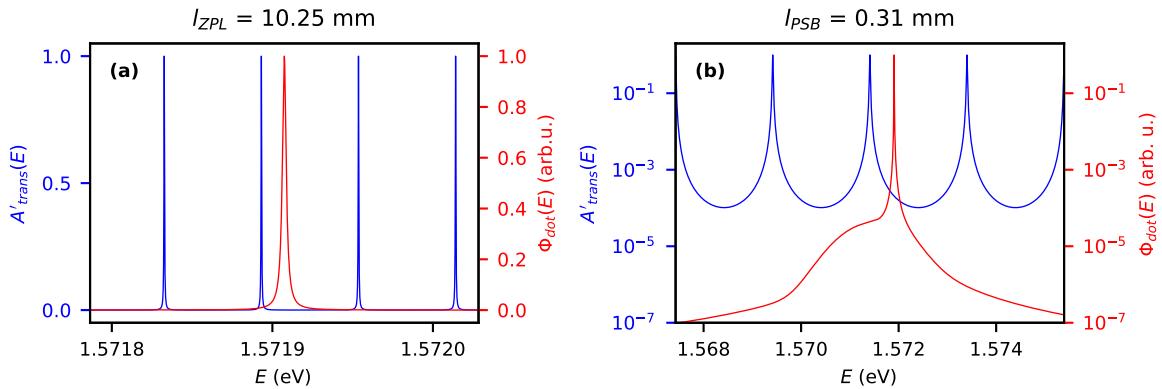


Figure 5.10.: Transmission of the FPI modes A'_{trans} compared to the exciton emission $\Phi_{dot}(E)$ for (a) ZPL and (b) PSB.

5. Building up a scanning Fabry-Pérot interferometer from scratch

The FPI scans by continuously varying the mirror distance l with a certain stepsize Δl and measuring the output-photon-flux every time. This process is sketched in figure 5.11.

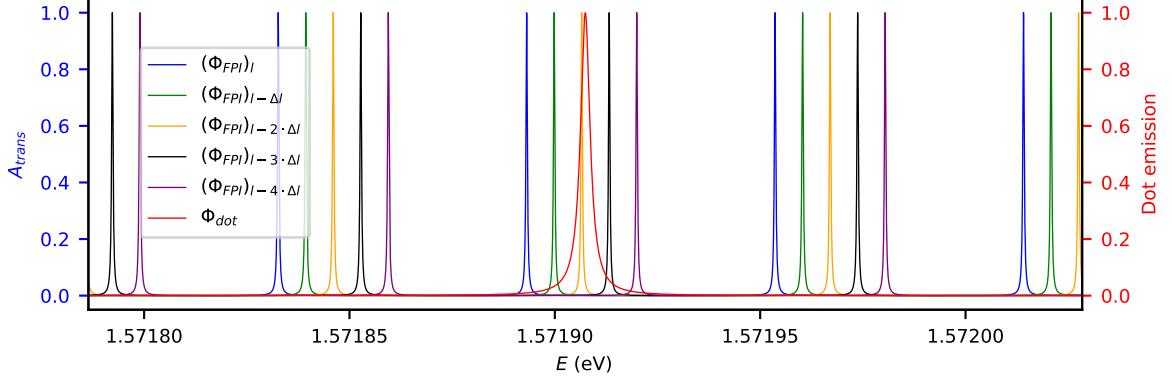


Figure 5.11.: Transmissions of the FPI modes A'_{trans} (blue) for different mirror distances $l - m \cdot \Delta l$ with $m \in \mathbb{N}$ compared to the exciton emission $\Phi_{dot}(E)$ (red).

The unnormalized output-photon-flux of the scanning FPI is then described with the convolution of $\Phi_{dot}(E)$ and $A'_{trans}(E)$

$$\tilde{\Phi}_{FPI}(E) = \int_{E_0-n\cdot\Delta}^{E_0+n\cdot\Delta} \Phi_{dot}(E') A'_{trans}(E - E') dE' \quad (5.63)$$

with E_0 as the central energy of the exciton emission line, Δ as the free spectral range and $2n = 4$ as the number of airy peaks considered for the numerical convolution.

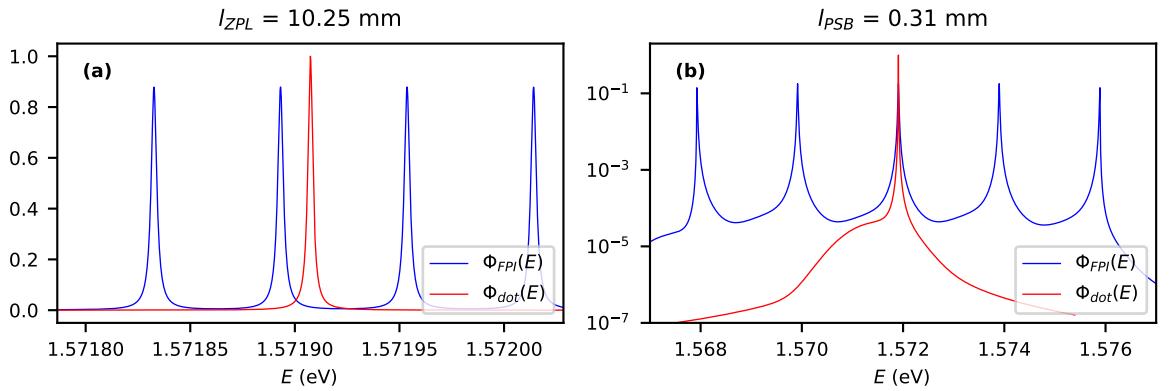


Figure 5.12.: Output-photon-flux of the scanning FPI $\Phi_{FPI}(E)$ (blue) compared to the exciton emission $\Phi_{dot}(E)$ (red) for (a) ZPL and (b) PSB.

$\tilde{\Phi}_{FPI}(E)$ can then be normalized with the integral of $A'_{trans}(E)$ over the same range

$$\Phi_{FPI}(E) = \frac{\tilde{\Phi}_{FPI}(E)}{\int_{E_0-n\cdot\Delta}^{E_0+n\cdot\Delta} A'_{trans}(E) dE} \quad (5.64)$$

A comparison of $\Phi_{FPI}(E)$ and $\Phi_{dot}(E)$ is shown in figure 5.12.

From now on, only the ZPL-path is shown as no new information is gained by examining both. In order to estimate the accuracy of the scanning FPI, the FPI modes are shifted by ΔE in order to overlap with $\Phi_{dot}(E)$ as depicted in figure 5.13(a)

$$\bar{\Phi}_{FPI}(E) = \Phi_{FPI}(E - \Delta E). \quad (5.65)$$

Afterwards, the absolute difference between those two $|\Phi_{dot}(E) - \bar{\Phi}_{FPI}(E)|$ is calculated as shown in figure 5.13(b). Now the relative error of $\Phi_{fabry,perot}(E)$ for the given parameters and compared to the actual excitonic QD emission can be calculated

$$\epsilon = \frac{\int_{E_0-\Delta/2}^{E_0+\Delta/2} |\bar{\Phi}_{FPI}(E) - \Phi_{dot}(E)| dE}{\int_{E_0-\Delta/2}^{E_0+\Delta/2} \Phi_{dot}(E) dE} \quad (5.66)$$

For the parameters in the ZPL path this gives $\epsilon_{ZPL} = 10.57\%$.

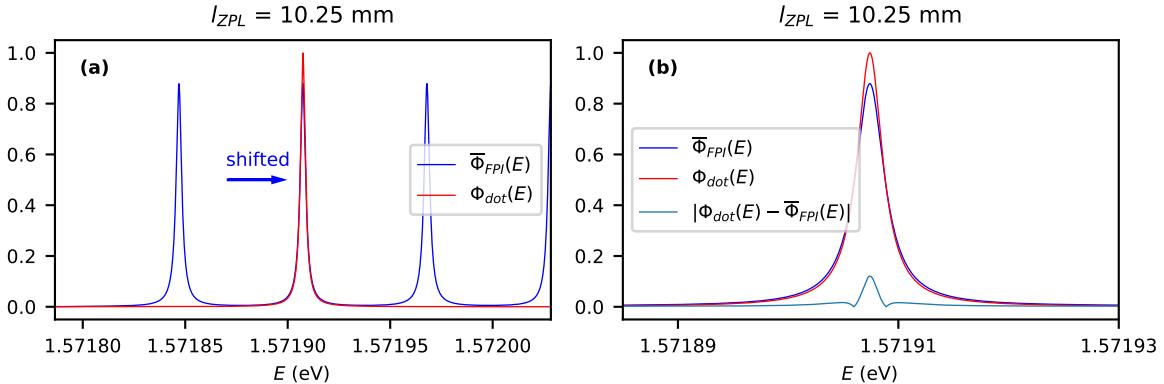


Figure 5.13.: In (a) the shifted output-photon-flux of the scanning FPI $\bar{\Phi}_{FPI}(E)$ (blue) compared to the exciton emission $\Phi_{dot}(E)$ (red) is displayed. In (b) the absolute difference between those two $|\bar{\Phi}_{FPI}(E) - \Phi_{dot}(E)|$ (light blue) is additionally shown.

5.5. Setup and measurement

Multiple FPI setups were built up in order to test their suitability to resolve QD emission. The first version featured planar mirrors, while their distance was coarsely tunable with an adjustable platform and finely tunable with a piezoelectrical actuator. However this setup with planar mirrors proved to be highly unstable and was therefore discarded. The second version used smaller, planar-convex mirrors and a ground plate made of molybdenum. This resulted in a stable FPI which was also adjustable for various free-spectral ranges. The measurements discussed in section 5.6 are obtained with this setup. However, the effort needed to mode-match for every measurement is too large to actually use it in further experiments. That is why the confocal setup will be used in the future, even though the freedom to adjust the free-spectral range is lost.

In order to obtain the spectral emission of the input signal, the FPI is used in the scanning mode. Here one of the mirrors is attached to a piezoelectric actuator which moves the mirror stepwise after every measurement as shown in figure 5.14. A minimal sketch of the setup is visible in figure 3.1.

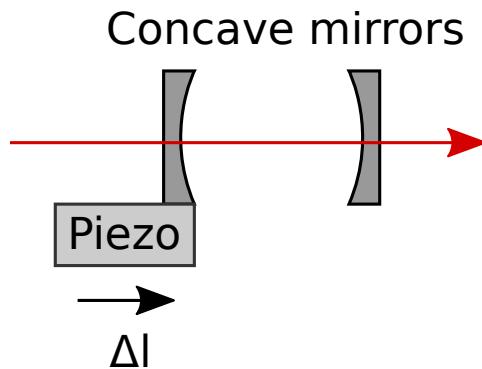


Figure 5.14.: Scanning Fabry Pérot interferometer

Better: 4.5
 Setup and Measurement
 General stuff
 4.5.1 Scanning mode with fast photo-diodes 4.5.2 Stepwise mode (find better name) with CCD

1) What APDs, which time resolution 2) What scanning frequency and why 3) Show pictures of the measurement itself and describe features, errors etc. 5) What time range did you define, how did you configure the correlation hardware. 4)

We did not connect the TTL-Output of the Funky-Generator directly to the Hydrapharp, as it uses a different stan-

Before the scanning FPI can be used to measure QD emission, it has to be aligned first. As every sweep with the charge-coupled devices (CCDs) takes time in the order of minutes, APDs were used. A function generator is used to drive the piezoelectrical actuator and the correlation hardware (here: Picoquant Hydrapharp 400) correlates the measurements of the APD with the TTL-output of the function generator. The complete setup is sketched in figure 5.15.

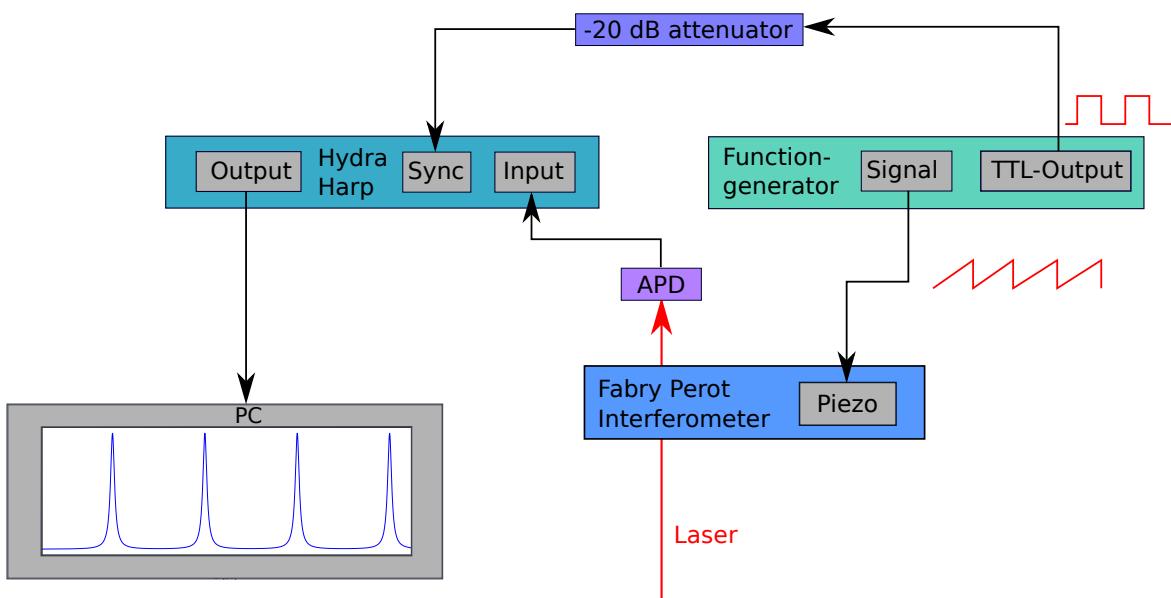


Figure 5.15.: Live avalanche photodiode setup

5.6. Measurements and discussion

In the following measurements the FPI was set up in the non-confocal mode and HeNe laser signals were used in order to align it. This involves for one setting the mirrors coming before the FPI so that the laser beam goes straight and centred through the FPI mirrors and then setting the FPI mirrors so that they are parallel and a single laser beam emerges as is shown in figure 5.16.

5. Building up a scanning Fabry-Pérot interferometer from scratch

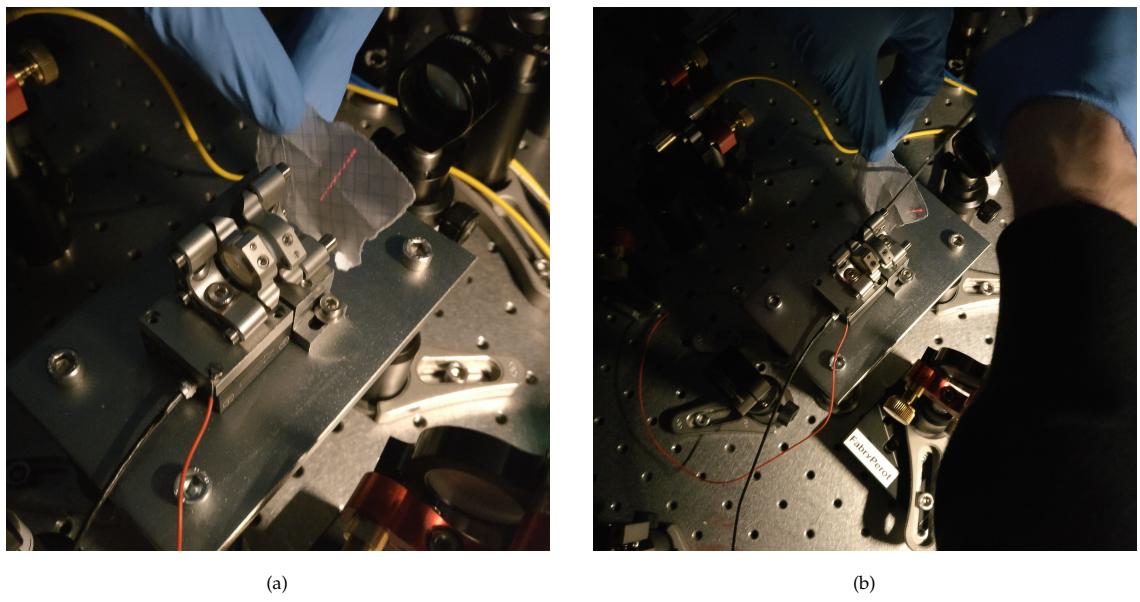


Figure 5.16.: Aligning the Fabry Pérot interferometer

Without spatial restriction strong TEM-modes of higher order are visible in figure 5.17(a). To counteract, a pinhole is inserted and adjusted which results in the measurement visible in figure 5.17(b).

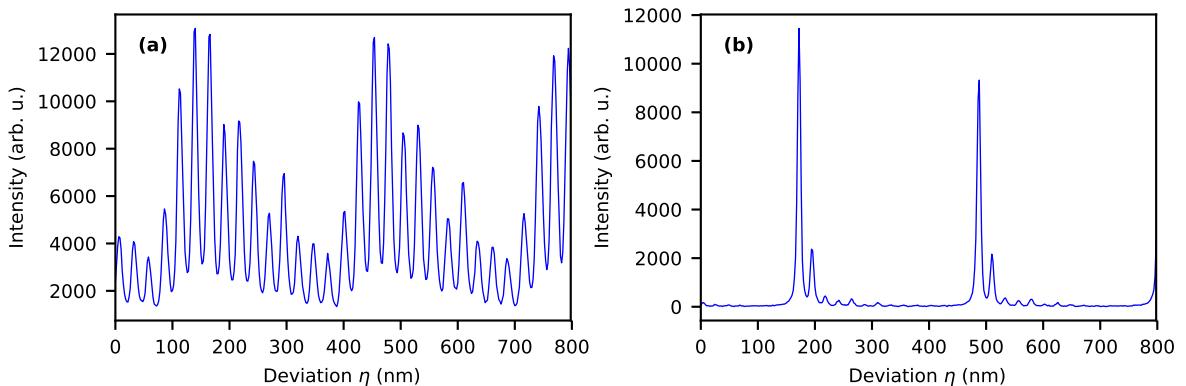


Figure 5.17.: Transmission measurement of FPI with ground mirror distance $l \approx 2$ mm and HeNe laser. (a) was aligned without spatial filtering with a pinhole and (b) involved a pinhole.

Set up like this, the GaAs QD sample AS2o8 was measured. First a polarization map of the exciton was recorded in order to determine the FSS $E_{FSS} = 24.42(39)$ μeV with the data shown in figure 5.18.

how does this work. Explain more details, this is not trivial

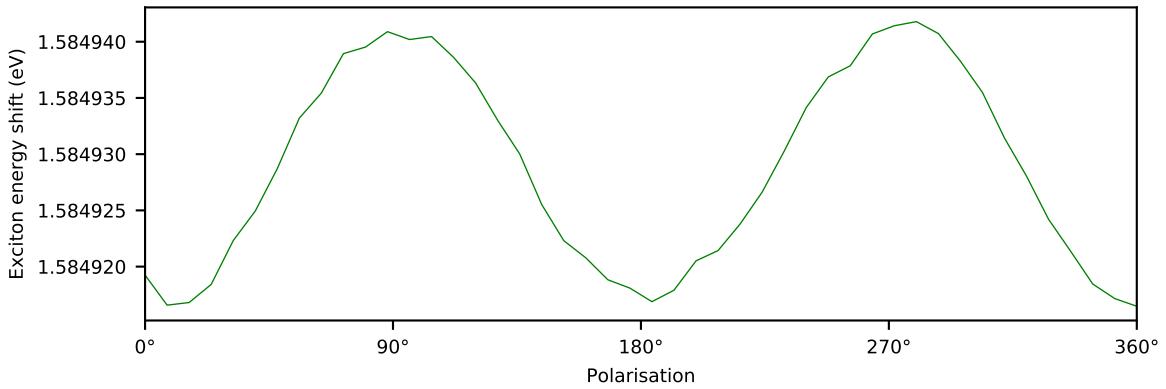


Figure 5.18.: Polarization map of exciton of QD in sample AS208.

Afterwards the output of the QD through the FPI was measured while the mirror distance was stepwisely changed which is shown in figure 5.19. The x-scale on the top of figure 5.19 was calculated by correlating the distance between the two adjacent peaks with the FSS determined with the data of figure 5.18. For this QD results in a conversion between the deviations $\eta = 1 \text{ nm} \hat{=} \zeta = 1.19(2) \mu\text{eV}$.

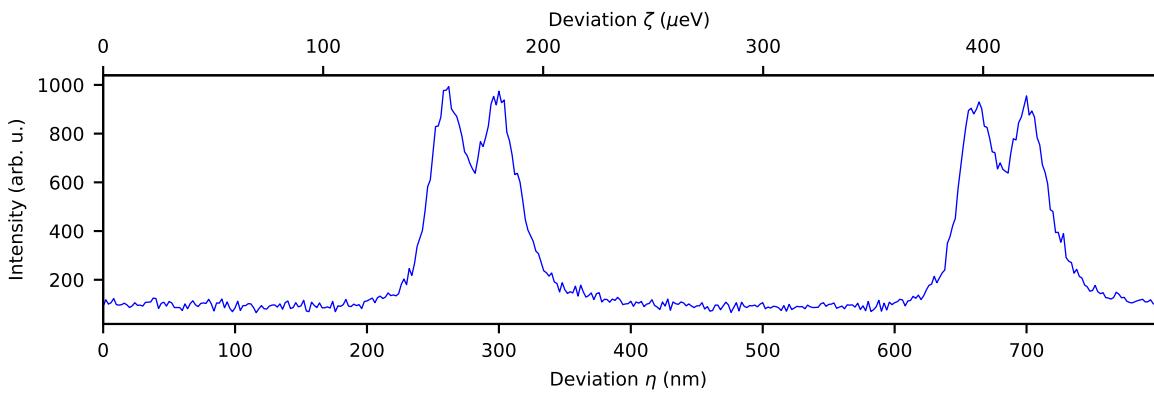


Figure 5.19.: Finestructure measurement of biexciton of QD in sample AS208 by passing thorough FPI and sweeping the mirror distance. Ground mirror distance was $l \approx 2 \text{ mm}$.

- What does this comparison tell us?
- Did it fit the calculation?
- Where are the side peaks we saw in the HeNe measurement?
- What about the stability?
- Are there calculations, expected temperature drifts, etc. Are there differences between the expected Finesse and the measured one, and why? Is this expected?

6. Summary and outlook

The first topic presented in this thesis is entangled photon generation using ARP with frequency-chirped-pulses. The obstacles in quantifying the chirp just with IAC were discussed and one possible solution (MOSAIC) was presented. Finally, the pulse expander, used for deterministically adjusting the chirp, was introduced and measurements with and without the pulse expander were presented. However, the Ti:Sa laser used for these experiments later turned out to be heavily chirped to begin with, which made comparisons difficult. Additionally, it had to be sent away for reparation, which blocked further investigations. The next steps will be to investigate MOSAIC under different scenarios and then, if the chirp can be adjusted, attempt to excite the GaAs QDs via ARP.

The second topic presented is the build-up of a scanning FPI from scratch. After setting up the theoretical foundation of electromagnetic waves and different FPI setups, simulations were presented in order to determine component parameters suitable for the wanted FPI mode properties. Afterwards, measurements were presented, which involved aligning the FPI with a HeNe laser, mode matching and spatial filtering. Finally, measurements of the FSS of a GaAs QD were presented and evaluated in order to confirm the consistency between the measured and the simulated results for the free spectral range. The next steps will be to set up the FPI in the confocal mode and measure with it the FSS as well. It might be advisable to buy multiple sets of mirrors in order to fulfil different needs regarding spectral width and resolution. When this is accomplished the scanning FPI can be used as "black box", which comes into action whenever fine details of QD emission need to be resolved.

Don't refer all the time to the main text. Imagine I'm a reader from a different field. I read the abstract, the introduction and the summary/outlook. Now I should know what you did and why and what are the future plans. At this point I have no idea what MOSAIC is, I have no idea what a pulse expander is, etc. unless you give me a hint in the summary.

Appendix

Appendix A.

Acronyms

QKD	quantum key distribution	1
QD	quantum dot	2
FSS	fine structure splitting	2
MBE	molecular beam epitaxy	3
CB	conduction band	3
VB	valence band	3
X	exciton	4
XX	biexciton	4
ZPL	zero phonon line	8
PSB	phonon side band	8
APD	avalanche photodiode	13
HBT	Hanbury-Brown-Twiss	12
BS	beam splitter	13
FWHM	full width at half maximum	16
MPL	micro photo-luminescence	17
ARP	adiabatic rapid passage	19
IAC	interferometric autocorrelation	22
MOSAIC	modified-spectrum autointerferometric correlation	23
FPI	Fabry P��rot interferometer	31
CCD	charge-coupled device	49

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