



Frequency control and stability requirements on hydro power plants

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Outline



Problem

Methodology Paper I

Simple test system Paper II

Theoretical validation Paper III

Tests at Statkraft's power plants Paper IV

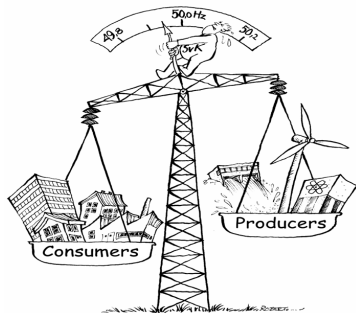
Simulation studies Paper V

The best way to do the identification Paper VI

Conclusions and further work

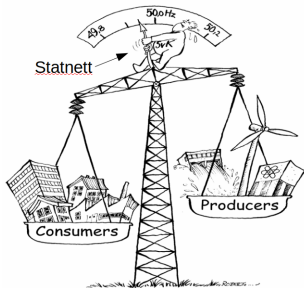
Load and production balancing

- The power system frequency measures the power balance.



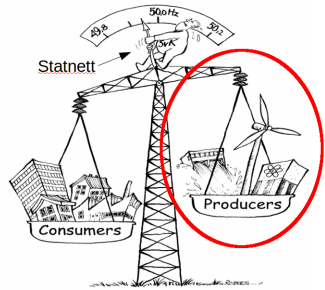
Load and production balancing

- The power system frequency measures the power balance.
- It is the responsibility of Statnett to control the frequency.



Load and production balancing

- The power system frequency measures the power balance.
- It is the responsibility of Statnett to control the frequency.
- However, it is the power plant owners who can control the frequency.



Buying frequency control

- Statnett pays all power plant owners to provide frequency control. (droop $\rho = \Delta f / \Delta P$)

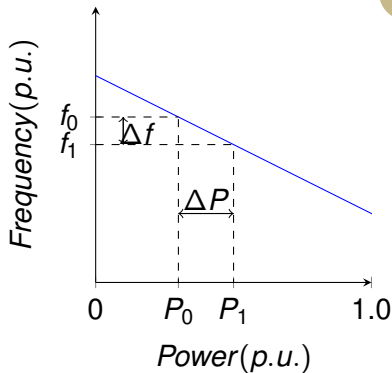


Figure: Frequency control response to step change in frequency

Buying frequency control

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- However, the system is not in steady state.

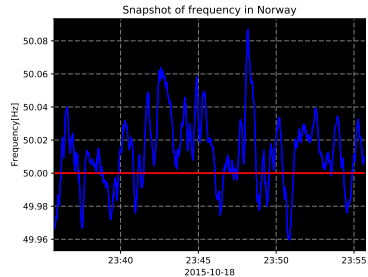


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Buying frequency control

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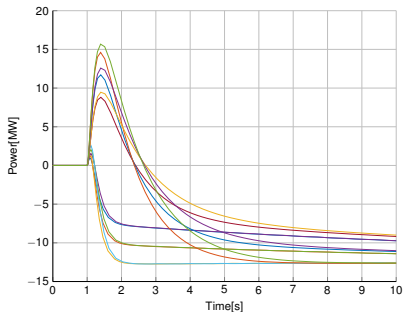


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Buying frequency control

- Statnett pays all power plant owners to provide frequency control. (droop $\rho = \Delta f / \Delta P$)
- However, the system is not in steady state.
- Plants with the same droop settings don't have to behave the same.
- Renewable energy sources such as wind and solar don't contribute.

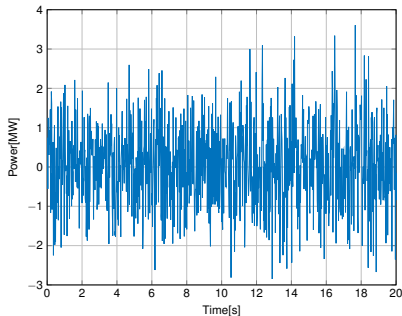
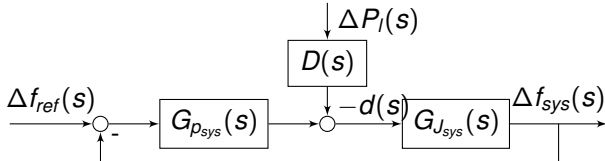


Figure: Frequency control response to step change in frequency

New requirements for frequency control

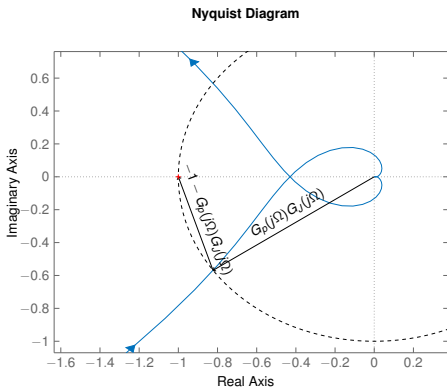
- Puts requirements on an aggregated system model.



New requirements for frequency control

- Puts requirements on an aggregated system model.
- Stability requirement

$$\begin{aligned} M_s &= \max \left| \frac{1}{1 + G_p(j\Omega)G_J(j\Omega)} \right| \\ &= \max |S(j\Omega)| \end{aligned} \quad (1)$$



New requirements for frequency control

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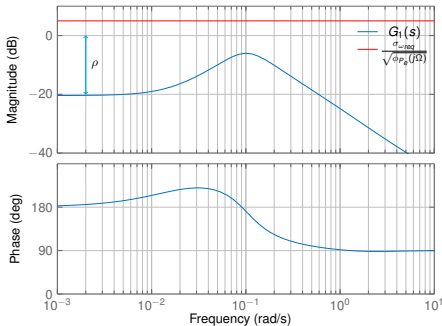
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- Performance requirement

$$|G_1(j\Omega)| < \frac{\sigma_{\omega_{req}}}{\sqrt{\phi_{P_e}(j\Omega)}} \quad (2)$$

$$G_1(s) = S(s)G_J(s) \quad (3)$$

Bode Diagram



New requirements for frequency control

- Puts requirements on an aggregated system model.
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- Requirement per plant stated using a per unit conversion



Future of frequency control



- Power plants have to pass tests to get paid to provide frequency control.
- Only those who pass the tests get paid for the service.

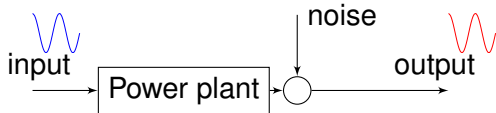


Figure: Test of power plant

Tests proposed by the industry

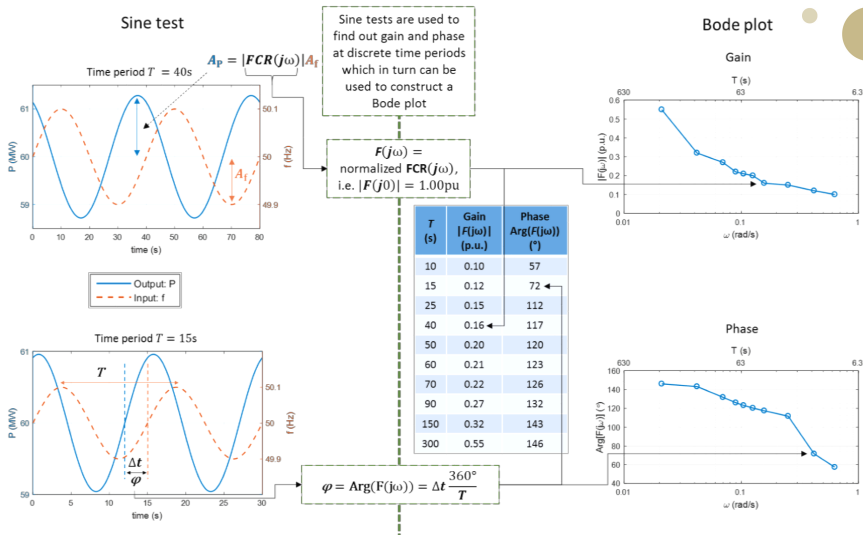
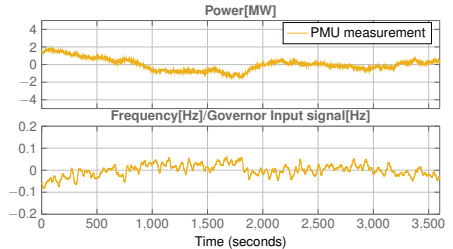


Figure: Testing procedure [source:ENTSO-E]

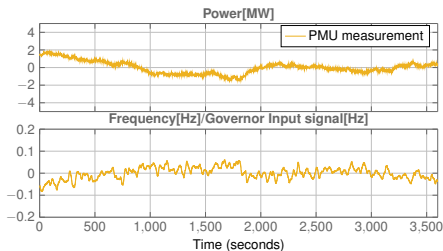
Motivation

- The power system is never really in steady state.



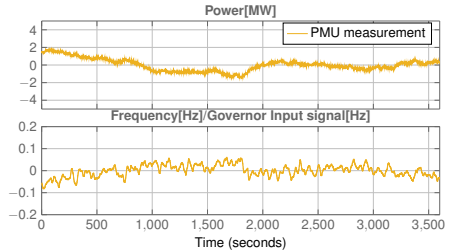
Motivation

- The power system is never really in steady state.
- Can the power plant dynamics be identified from normal operation measurements?



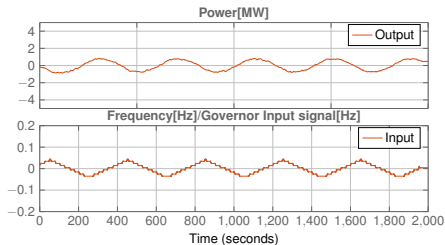
Research questions

- Can power plant dynamics be identified using a PMU?



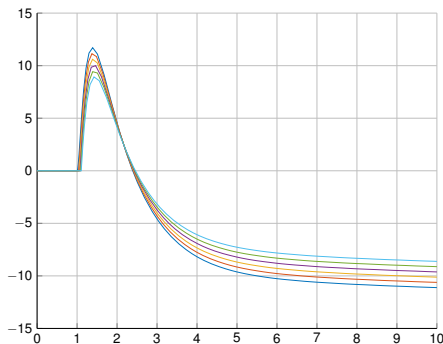
Research questions

- Can power plant dynamics be identified using a PMU?
- Can power plant dynamics be identified using control system measurements without disturbing the operation of the plant?



Research questions

- Can power plant dynamics be identified using a PMU?
- Can power plant dynamics be identified using control system measurements without disturbing the operation of the plant?
- What is the effect of nonlinearities on the identification?



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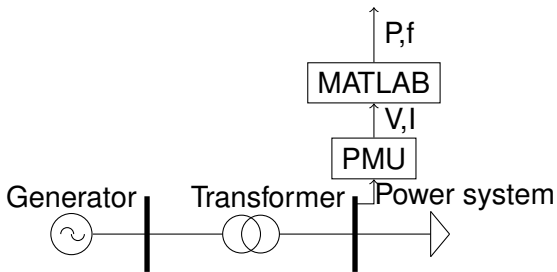
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Background

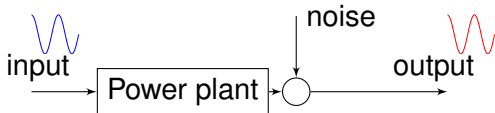
- Idea from¹ can the power plant dynamics be identified using PMUs



¹Dinh Thuc Duong et al. "Estimation of Hydro Turbine-Governor's Transfer Function from PMU Measurements". In: *IEEE PES General Meeting*. Boston: IEEE, July 2016

Background

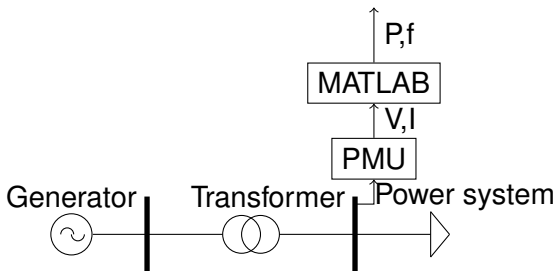
- Idea from¹ can the power plant dynamics be identified using PMUs
- Uses the same input and output measurements as in the requirements:
 - Input: Power system frequency.
 - Output: Electric power.



¹Dinh Thuc Duong et al. "Estimation of Hydro Turbine-Governor's Transfer Function from PMU Measurements". In: [IEEE PES General Meeting. Boston: IEEE, July 2016](#)

Methodology

- Collect several datasets from PMUs.
- Calculate power and frequency from the measurements.
- Identify dynamics using vector fitting.
- Compare models.



Vector fitting basics



$$Y(s) = H(s) \cdot U(s) \quad (4)$$

- Vector fitting fits a transfer function to measured input and output data

Vector fitting basics

- Vector fitting fits a transfer function to measured input and output data
- It assumes the system to have the following structure.

$$Y(s) = H(s) \cdot U(s) \quad (4)$$

$$H(s) = d + \sum_{i=1}^{n_p} \frac{r_i}{s - p_i} \quad (5)$$

Vector fitting basics



$$Y(s) = H(s) \cdot U(s) \quad (4)$$

- Vector fitting fits a transfer function to measured input and output data
- It assumes the system to have the following structure.
- In time domain it is.

$$H(s) = d + \sum_{i=1}^{n_p} \frac{r_i}{s - p_i} \quad (5)$$

$$y(t) \approx \tilde{d}x(t) + \sum_{i=1}^{n_p} \tilde{r}_i x_i - \sum_{i=1}^{n_p} \tilde{k}_i y_i \quad (6)$$

$$x_i = \int_0^t e^{\tilde{p}_i(t-\tau)} x_i(\tau) d\tau \quad (7)$$

$$y_i = \int_0^t e^{\tilde{p}_i(t-\tau)} y_i(\tau) d\tau \quad (8)$$

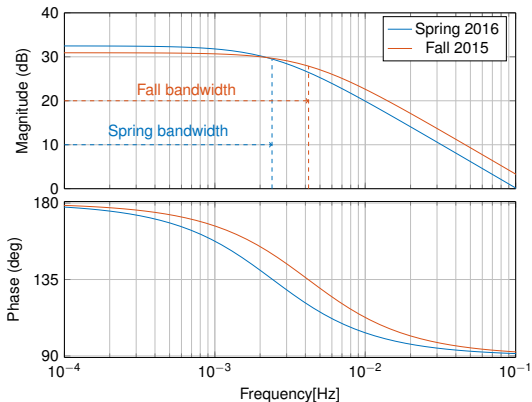
Vector fitting basics ctd.



— Find \tilde{d} , \tilde{r}_i and \tilde{k}_i to minimize:

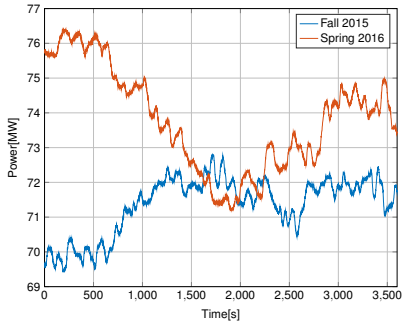
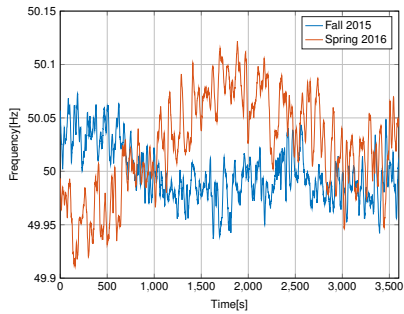
$$y(t) - (\tilde{d}x(t) + \sum_{i=1}^{n_p} \tilde{r}_i x_i - \sum_{i=1}^{n_p} \tilde{k}_i y_i) \quad (9)$$

Estimated droop and bandwidth

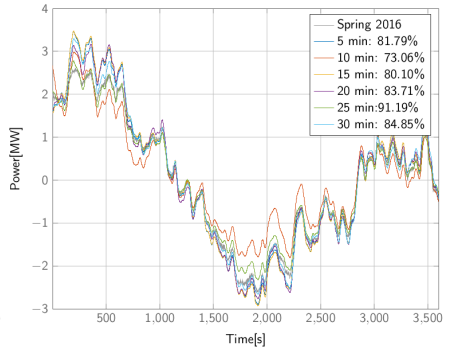
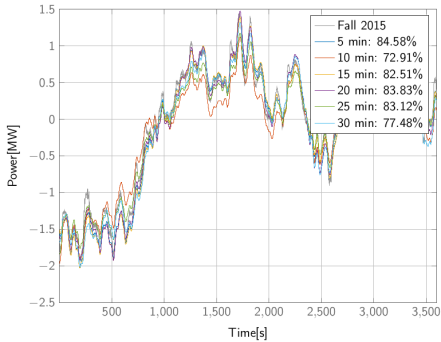


Dataset	Droop[%]	Bandwidth[mHz]
Fall 2015	10	4.16
Spring 2016	8	2.41

Cross validation using distant data sets

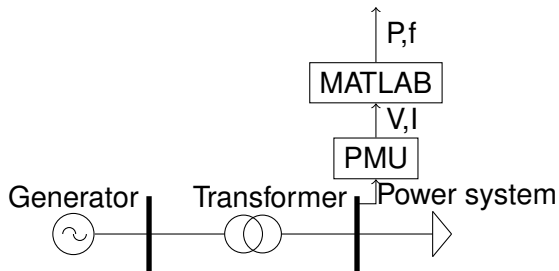


Cross validation using distant data sets



Main contributions to the research questions

- Promising results for 19 datasets.



Main contributions to the research questions

- Promising results for 19 datasets.
- Developed code for interfacing with the PMU data.

The screenshot shows the GitHub repository page for 'Hofsmo / turb_fit'. The repository has 23 commits, 1 branch, 0 releases, and 1 contributor. It is licensed under GPL-3.0. The repository contains several files, including LICENSE, README.md, bode_to_csv.m, create_G0.m, droop_jacobian_bj.m, find_inertia.m, linearize_hygov.m, prepare_case.m, read_top_data.m, read_pmu.m, and read_simulation.m. The README.md file is open, showing the title 'turb_fit' and a description: 'This toolbox provides functions useful for identifying hydro turbines using PMU measurements and signals from the plant.'

Hofsmo / turb_fit

Unwatch 1 Star 0 Fork 0

Code Issues Pull requests Projects Wiki Security Insights Settings

Functions useful for hydro turbine identification

Manage topics

23 commits 1 branch 0 releases 1 contributor GPL-3.0

Branch: master New pull request Create new file Upload files Find file Clone or download

File	Commit Message	Commit Date
LICENSE	Initial commit	2 years ago
README.md	Update README.md	2 years ago
bode_to_csv.m	I added find_inertia and bode to csv	last year
create_G0.m	I added find_inertia and bode to csv	last year
droop_jacobian_bj.m	Added droop Jacobian	last year
find_inertia.m	I added find_inertia and bode to csv	last year
linearize_hygov.m	Commit before pull	last year
prepare_case.m	Added detrend to prepare_case	last year
read_top_data.m	Added function for reading data from top files	last year
read_pmu.m	Added and renamed files from old toolbox	2 years ago
read_simulation.m	Added and renamed files from old toolbox	2 years ago

README.md

turb_fit

This toolbox provides functions useful for identifying hydro turbines using PMU measurements and signals from the plant.

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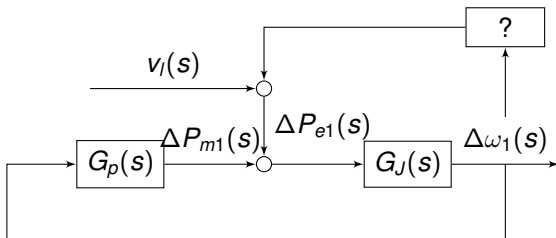
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Motivation

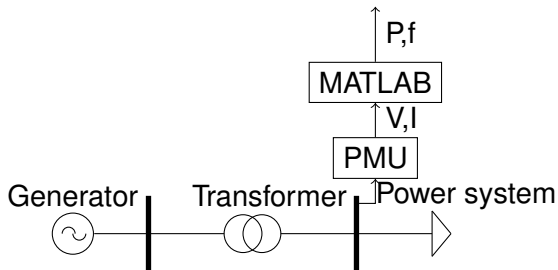


- Explain the problem to my co-supervisor.
- Create a model for analysing the identifiability of hydro power plant dynamics.



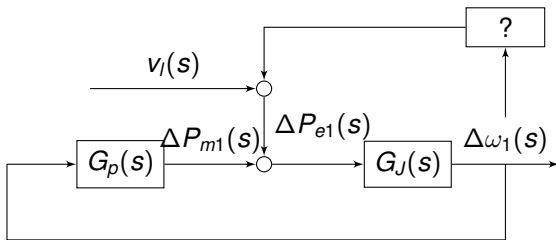
What do we need to model?

- From the PMU we get



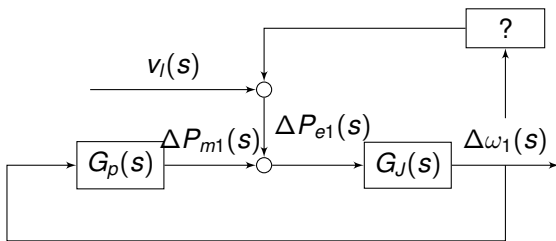
What do we need to model?

- From the PMU we get
 - Power: $\Delta P_{e1}(s)$.



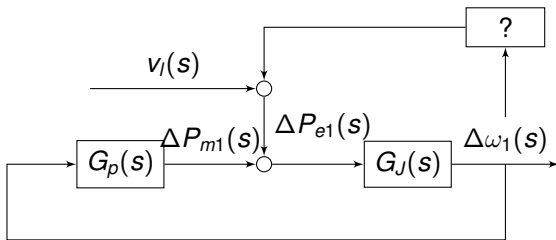
What do we need to model?

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 - Frequency: $\Delta f(s)$.



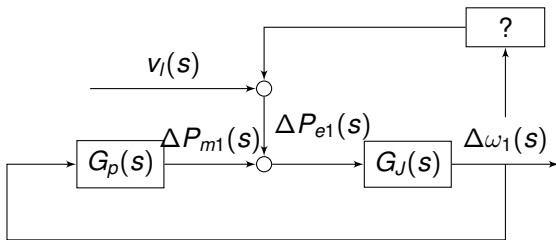
What do we need to model?

- From the PMU we get
 - Power: $\Delta P_{e1}(s)$.
 - Frequency: $\Delta f(s)$.
- We need to model how $\Delta P_{e1}(s)$ and $\Delta f(s)$ is related through the power system.



What do we need to model?

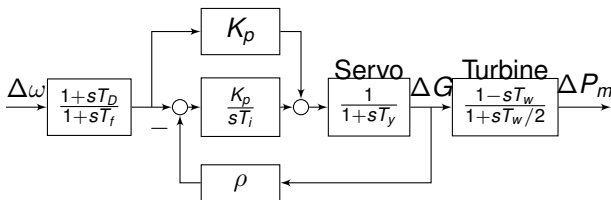
- From the PMU we get
 - Power: $\Delta P_{e1}(s)$.
 - Frequency: $\Delta f(s)$.
- We need to model how $\Delta P_{e1}(s)$ and $\Delta f(s)$ is related through the power system.
- We also need to model the power plant consisting of $G_p(s)$ and $G_J(s)$.



Power plant model

- Model for $G_p(s)$
- Model for $G_J(s)$

$$G_J(s) = \frac{1}{2Hs + K_d} \quad (10)$$



Power system model

- The frequency and power system angle is related.

$$\Delta\theta(s) = \frac{2\pi f_s}{s} f(s) \quad (11)$$

Power system model

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- The angle and power is related.

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$$P_k \approx \sum_{m \in \Omega_k} x_{km}^{-1} \theta_{km} \quad (12)$$

Power system model

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- The angle and power is related.
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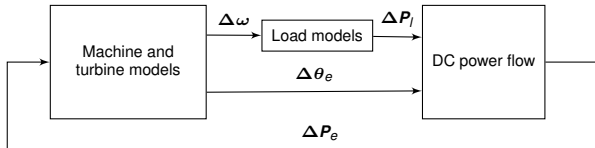
Power system model

- The frequency and power system angle is related.
- The angle and power is related.
- On matrix form.
- In software

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Test system

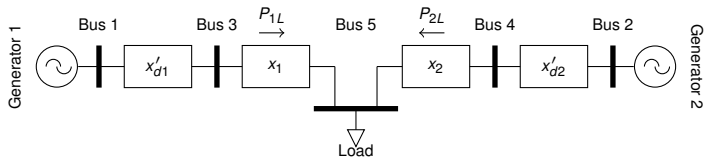
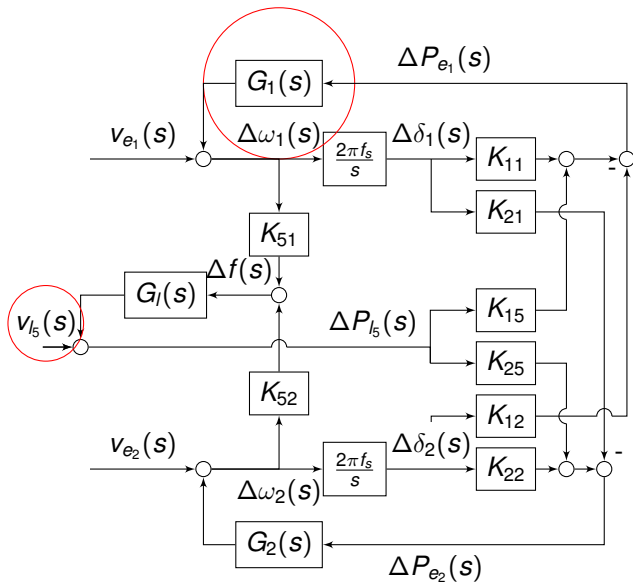
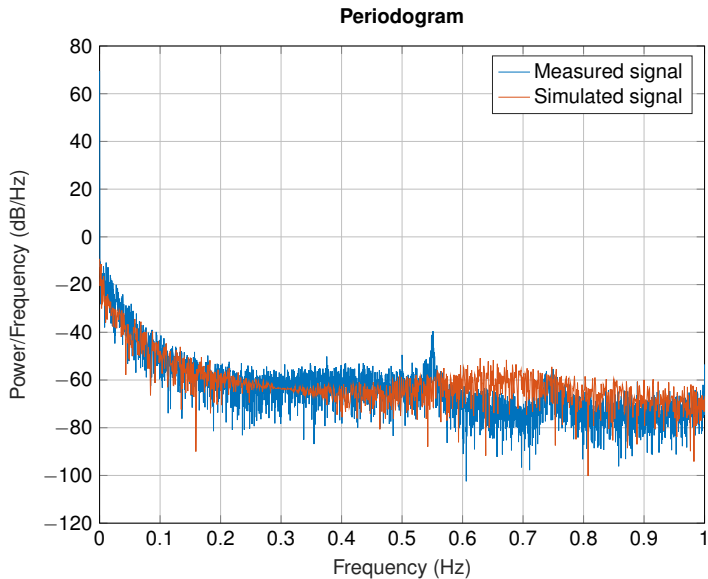


Figure: Single line diagram

Test system



Simulation Result



Main contributions



- Developed simple test system for analysing power plant identifiability using PMUs.
- Developed simple test system used in the proceeding papers for simulations.

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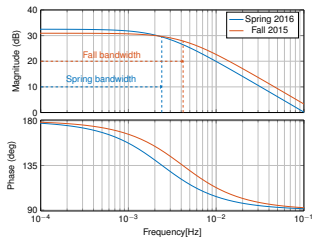
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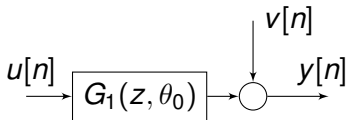
Background

- Why do we get different results?



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- The signals we use are corrupted by noise.



Background



- Why do we get different results?
- The signals we use are corrupted by noise.
- From system identification we have that the error will be asymptotic normally distributed

$$\sqrt{N}(\hat{\theta}_n - \theta^*) \in AsN(0, P_\theta)$$

Background

- Why do we get different results?
- The signals we use are corrupted by noise.
- From system identification we have that the error will be asymptotic normally distributed
- However, first we need to prove the identifiability of the system

True system: \mathcal{S}

x: unbiased

x: biased



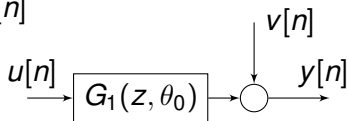
System identification basic

- Assume that a data set $Z^N = \{u[n], y[n] | n = 1 \dots N\}$ has been collected.
- The dataset Z^N is assumed generated by

$$\mathcal{S} : y[n] = G_1(z, \theta_1)u[n] + H_1(z, \theta_1)e[n] \quad (14)$$

- Using the data set Z^N we want to find the parameter vector θ^N minimizing

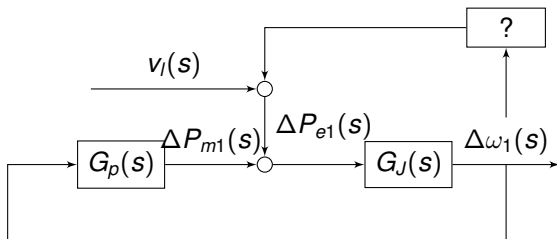
$$\hat{\theta}_N = \arg \min_{\theta} \frac{1}{N} \sum_{n=1}^N [H_1^{-1}(z, \theta)(y[n] - G_1(z, \theta)u[n])]^2 \quad (15)$$



Modeling used for the validation

- The system we are identifying

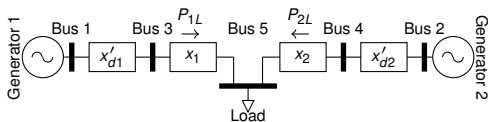
$$G_1(s) = \frac{G_p(s)}{1 + G_p(s)G_J(s)} \quad (16)$$



Modeling used for the validation

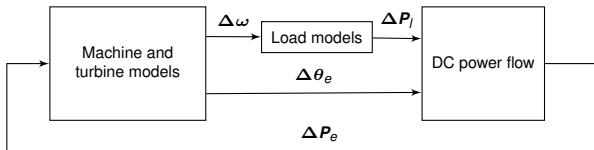
- The system we are identifying
- We use a small power system

(16)



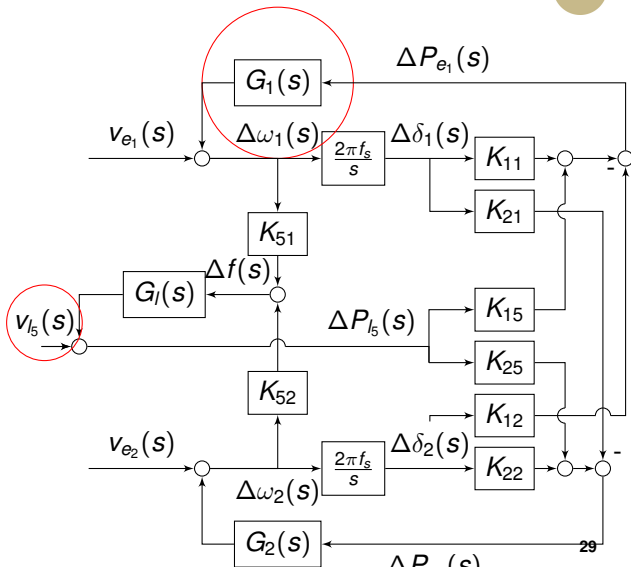
Modeling used for the validation

- The system we are identifying
- We use a small power system
- We use a dc power flow



Modeling used for the validation

- The system we are identifying
- We use a small power system
- We use a dc power flow
- This results in the following block diagram



Results from the theoretical validation



- A consistent estimate of the closed loop transfer function of the turbine and electromechanical dynamics can be obtained by using:

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 - Measured PMU frequency as the output $u[n]$

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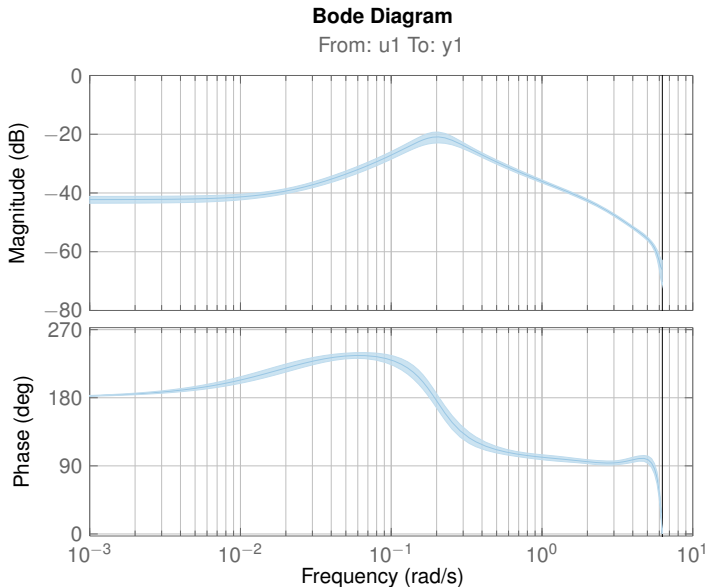
- A consistent estimate of the closed loop transfer function of the turbine and electromechanical dynamics can be obtained by using:
 - Measured PMU frequency as the output $u[n]$
 - Measured PMU power as the input $y[n]$

Results from the theoretical validation

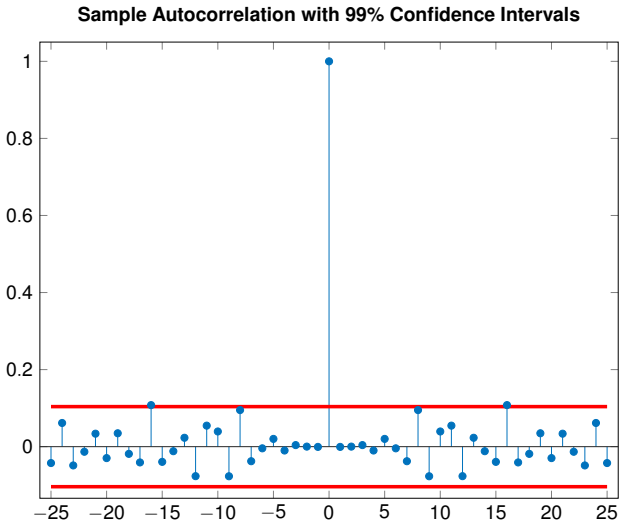


- A consistent estimate of the closed loop transfer function of the turbine and electromechanical dynamics can be obtained by using:
 - Measured PMU frequency as the output $u[n]$
 - Measured PMU power as the input $y[n]$
- The proof was done with the following assumptions.
 - The system is excited by a load acting as a filtered white noise process
 - The measurement error of the electrical power is negligible.
 - The measured frequency is a good estimate of the generator speed.

Model obtained using PMU data



Whiteness test on model identified using PMU data



Main contributions



- To show that the transfer function one is identifying using PMUs is $G_1(s)$.
- To prove under which conditions a consistent estimate of $G_1(s)$ is possible.
- To demonstrate the theory for identification of $G_1(s)$ on real datasets.

Outline



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The best way to do the identification Paper VI

Conclusions and further work

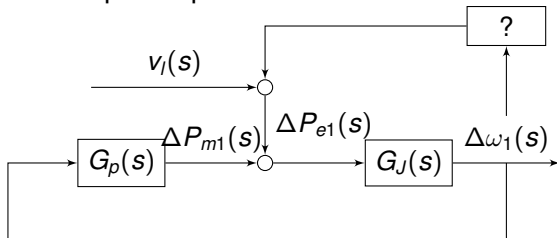
Motivation



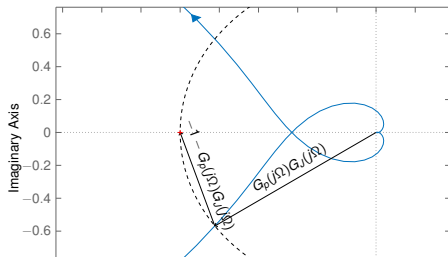
- Relate the results from Paper III and the new requirements.
- Test the methods on more real datasets.
- Demonstrate that industry proposed tests can be done easier.
- Less theoretical presentation in a more industry focused conference.

Alternative requirements

- Place requirements directly on one power plant.

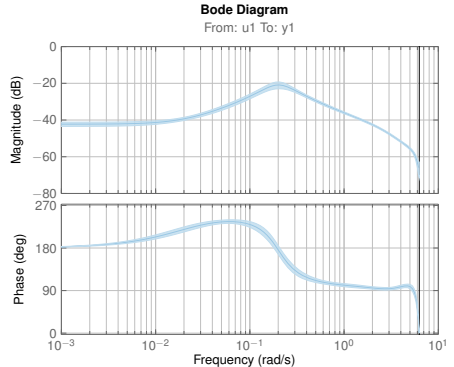


Nyquist Diagram



Alternative requirements

- Place requirements directly on one power plant.
- We already have an estimate of $G_1(s)$.



Alternative requirements



- Place requirements directly on one power plant.
- We already have an estimate of $G_1(s)$.
- We need to find $S(s)$

Estimating $S(s)$



$$G_1(s) = G_J(s)S(s) \quad (17)$$

Estimating $S(s)$



$$G_1(s) = G_J(s)S(s) \quad (17)$$

$$G_J(s) = \frac{1}{2Hs + K_d} \quad (18)$$

Estimating $S(s)$



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$$2H \gg K_d \quad (19)$$

Estimating $S(s)$



$$G_1(s) = G_J(s)S(s) \quad (17)$$

$$G_J(s) = \frac{1}{2Hs + K_d} \quad (18)$$

$$2H \gg K_d \quad (19)$$

$$S(s) \approx 2HsG_1(s) \quad (20)$$

Estimating $S(s)$



—

$$G_1(s) = G_J(s)S(s) \quad (17)$$

—

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—

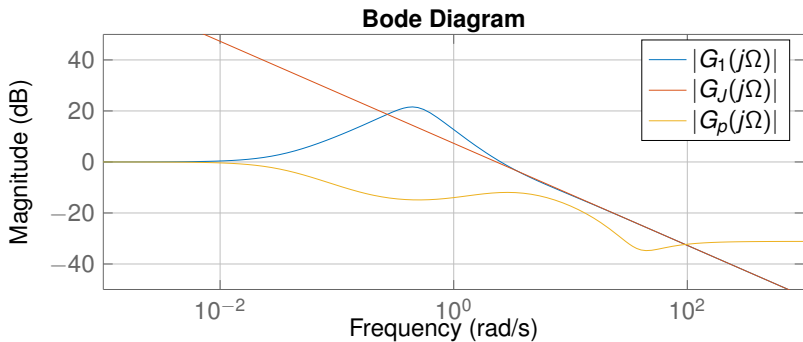
$$2H \gg K_d \quad (19)$$

—

$$S(s) \approx 2HsG_1(s) \quad (20)$$

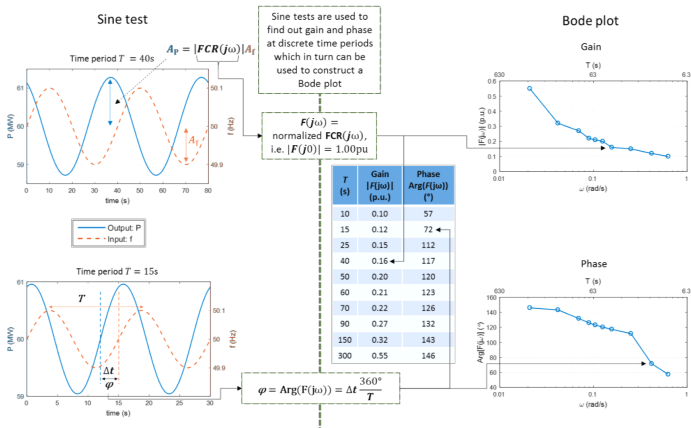
— Need to estimate H

Estimating H



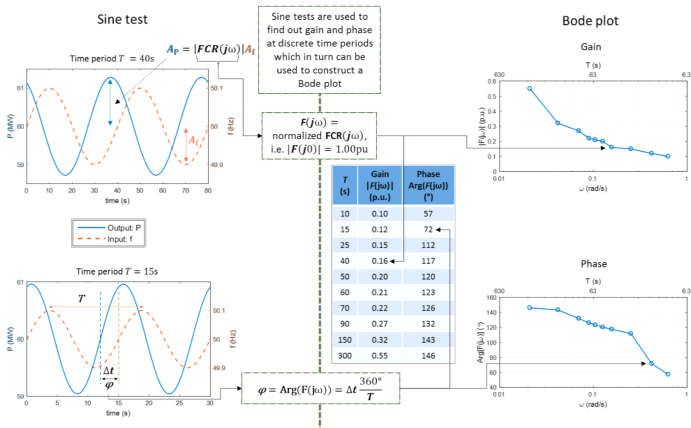
Dataset from Statkraft

— Norway's biggest power producers.



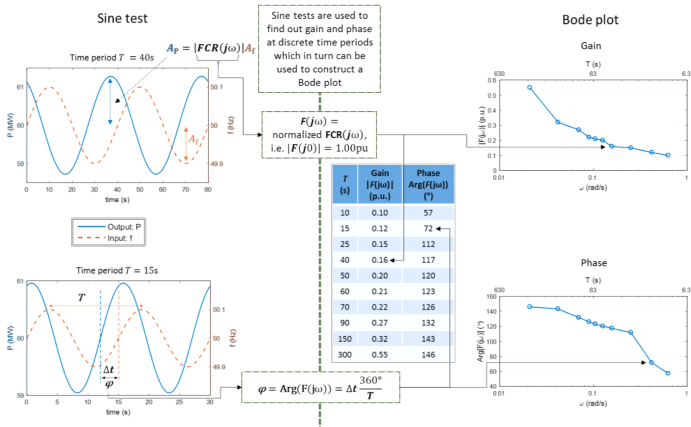
Dataset from Statkraft

- Norway's biggest power producers.
- They performed the tests from the draft requirements

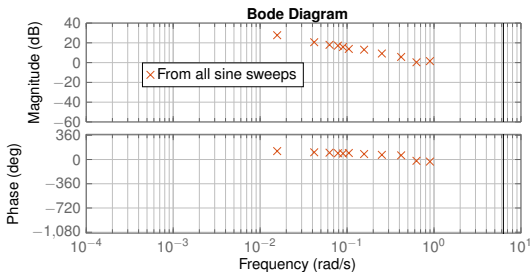
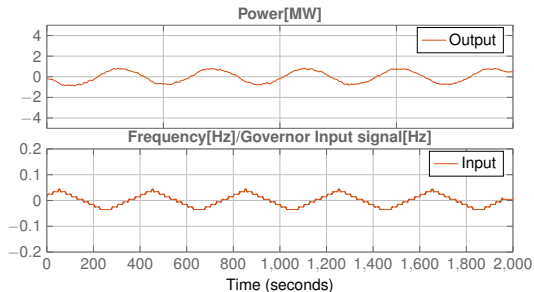


Dataset from Statkraft

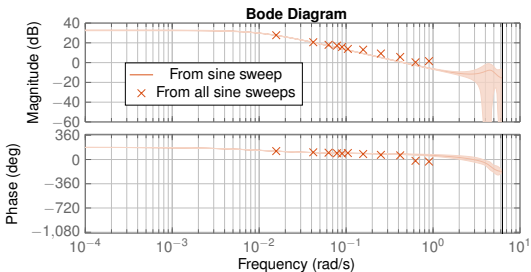
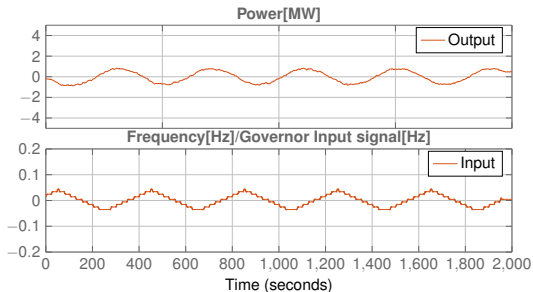
- Norway's biggest power producers.
- They performed the tests from the draft requirements
- By chance I had PMU measurements from the same plant.



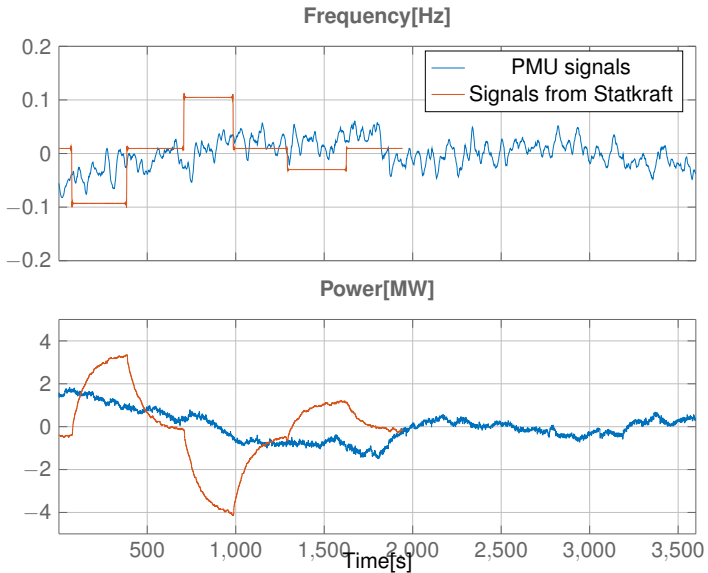
Can the industry proposed tests be done easier?



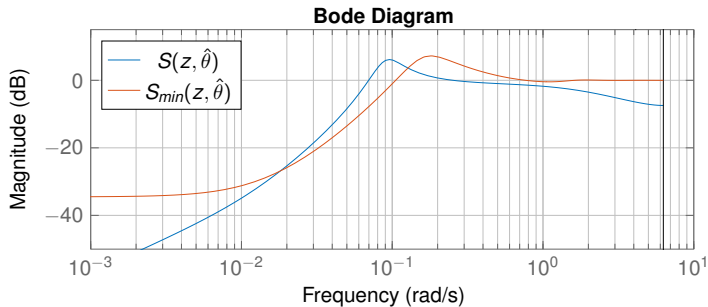
Can the industry proposed tests be done easier?



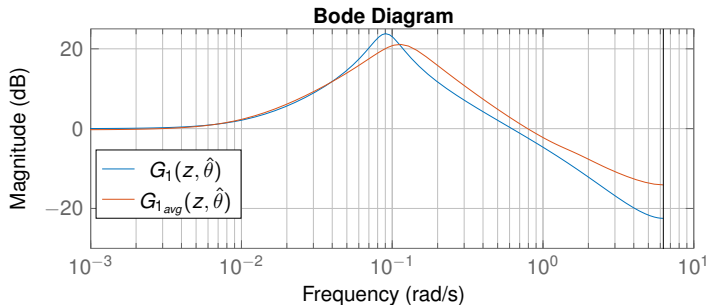
Datasets used



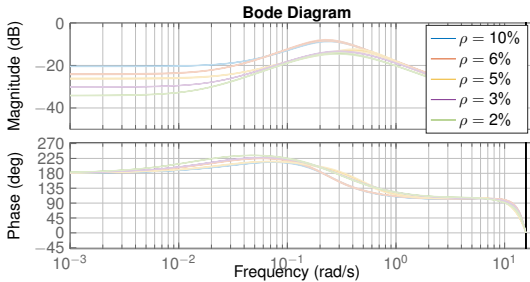
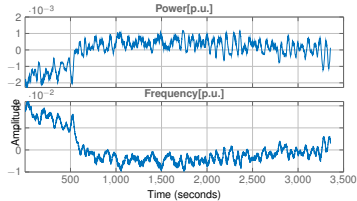
Estimated sensitivity functions



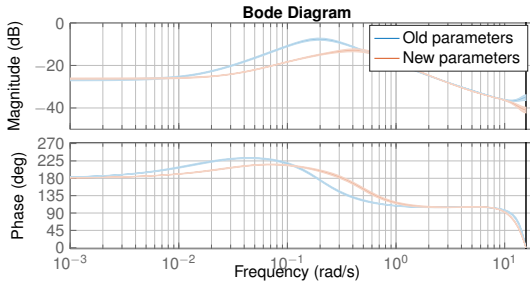
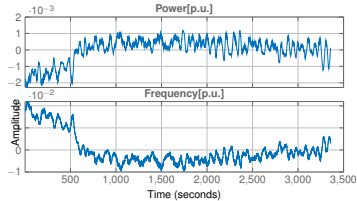
Estimated $G_1(s)$



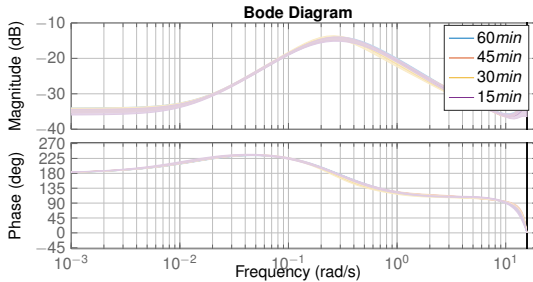
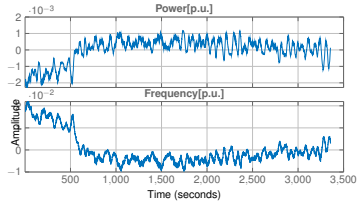
Control system data in closed loop



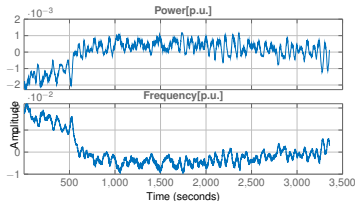
Control system data in closed loop



Control system data in closed loop



Control system data in closed loop



Droop	60min	45min	30min	15min
10%	9.5%	9.5%	9.5%	9.5%
6%	6.2%	6.0%	5.9%	6.1%
5%	4.9%	4.9%	5.0%	5.1%
3%	3.1%	3.1%	3.1%	2.9%
2%	2.0%	1.8%	1.8%	1.7%

Main Contributions



- Proposal for alternative tests.
- Demonstrating that the proposed methods can detect parameter changes.
- Demonstrated that the industry proposed tests can be done easier.

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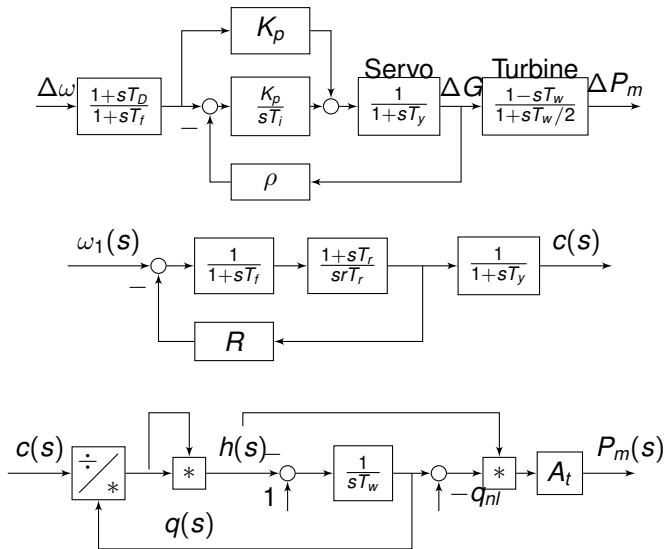
Conclusions and further work

Motivation



- Test with a more detailed power plant model.
- Test with a more detailed power system model.
- Investigate some of the assumptions from previous papers.

More detailed power plant model



More detailed power system model



- Added the frequency divider formula to the simple test system.

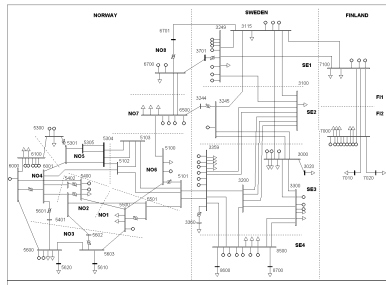
$$\omega_l = \mathbf{1} + \mathbf{D}(\omega_e - \mathbf{1}) \quad (21)$$

where

$$\mathbf{D} = -\mathbf{B}_{22}^{-1} \mathbf{B}_{21} \quad (22)$$

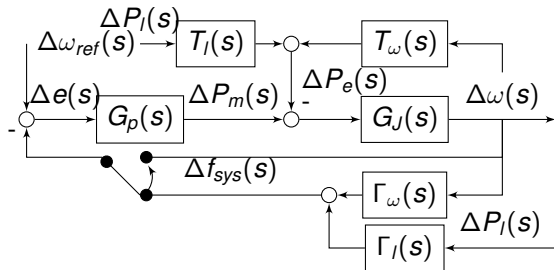
More detailed power system model

- Added the frequency divider formula to the simple test system.
- Used the Nordic 44 test system in PSS/E.

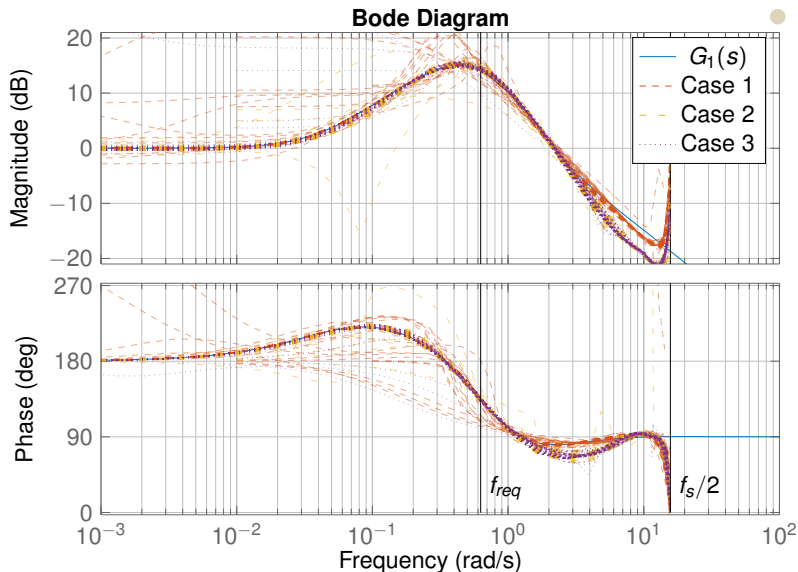


Identification cases

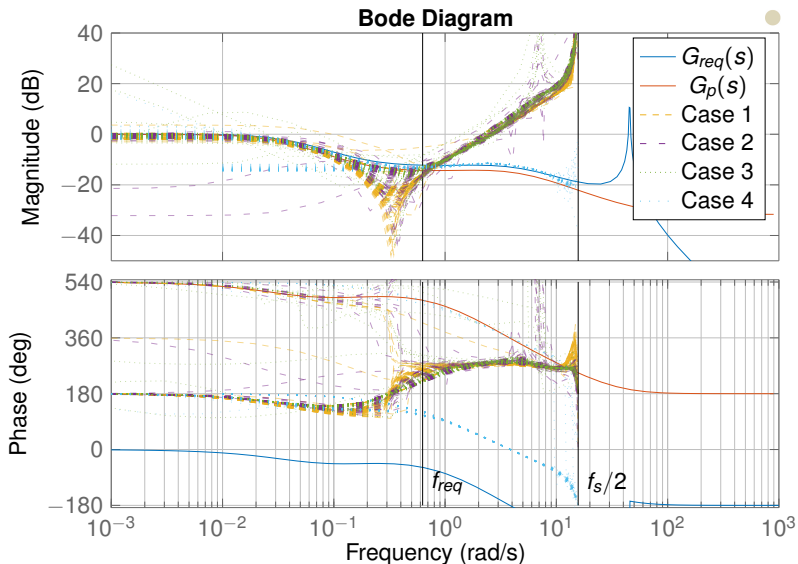
1. **Case 1** Normal operation and speed feedback.
2. **Case 2** Normal operation, speed feedback and PMU.
3. **Case 3** Normal operation, frequency feedback and PMU.
4. **Case 4** Open loop operation.



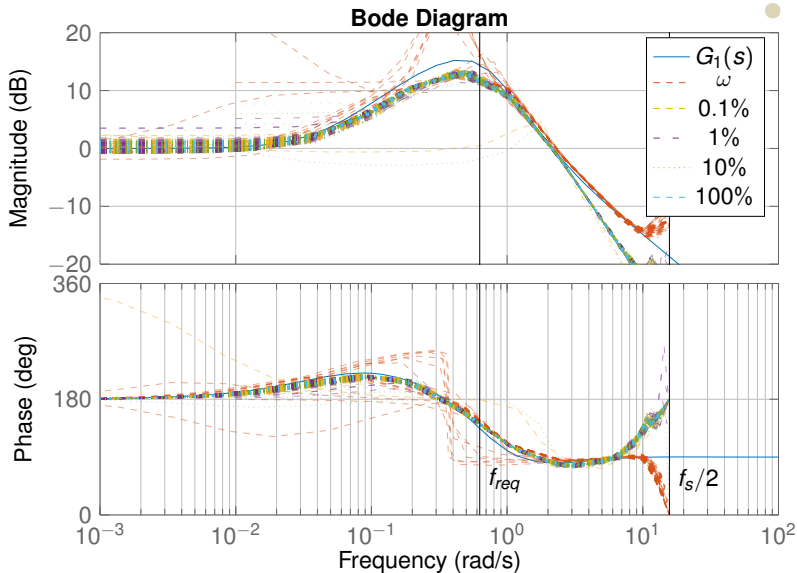
Test the different cases



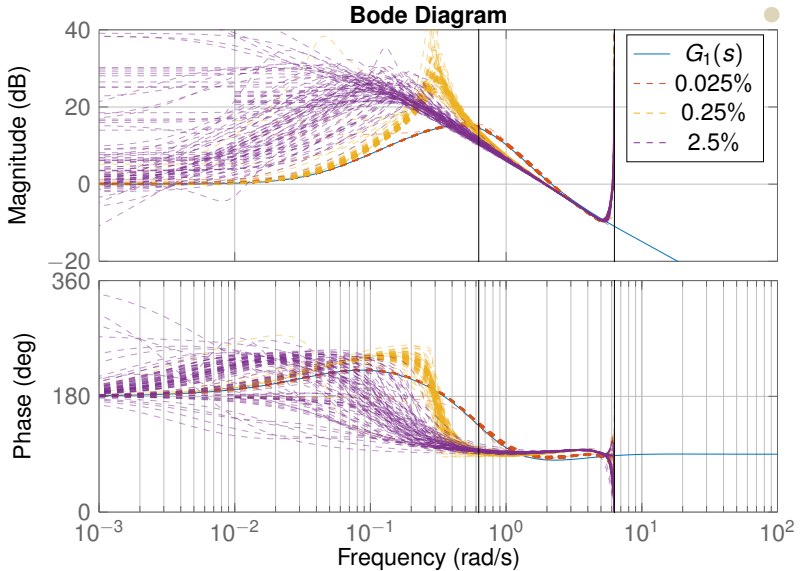
Test the different cases



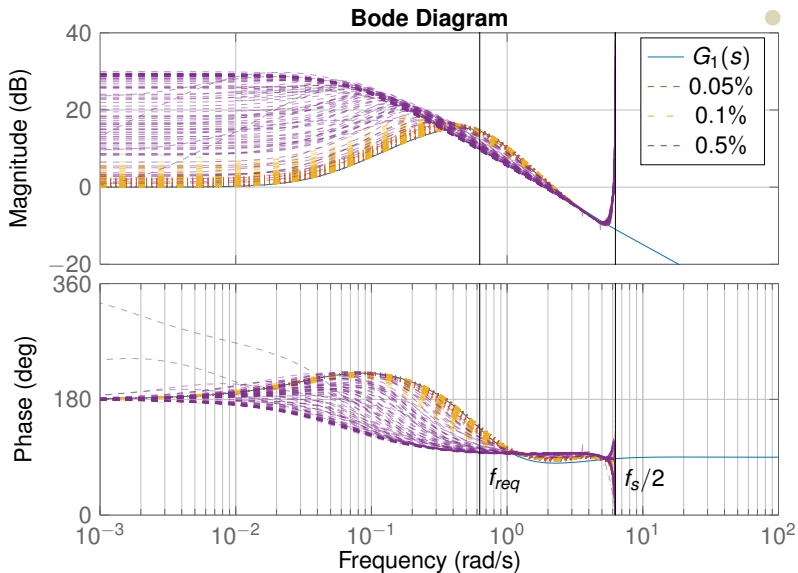
Test frequency assumption



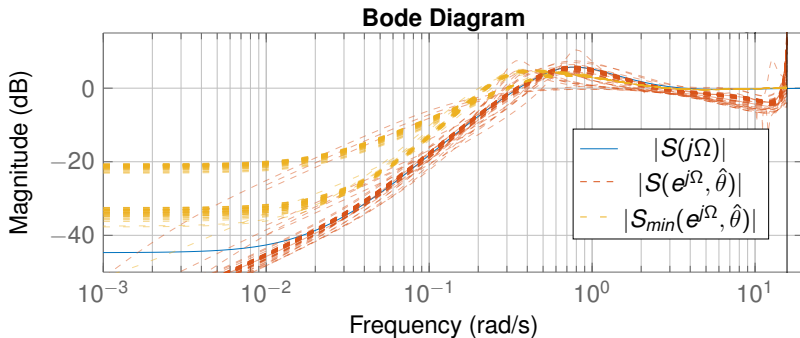
Test backlash



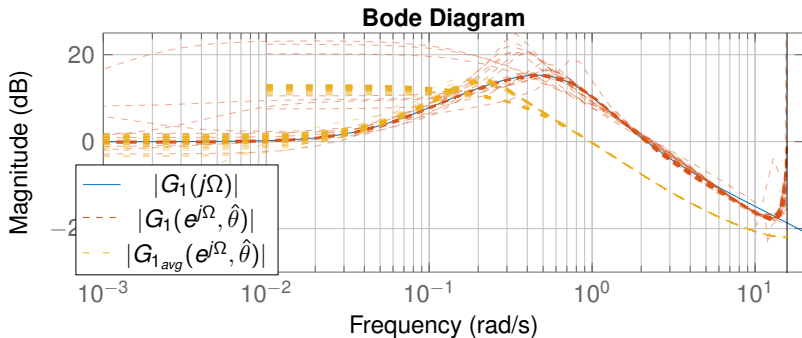
Test deadband



Sensitivity function $S(s)$



Disturbance rejection function $G_1(s)$



Comparison of stability margins



Method	Median	Root mean square error (RMSE)
$\max S(j\Omega) $	1.84	0
$\max S(e^{j\Omega}, \hat{\theta}) $, Case 1	1.84	0.25
$\max S(e^{j\Omega}, \hat{\theta}) $, Case 2	1.75	0.34
$\max S(e^{j\Omega}, \hat{\theta}) $, Case 3	1.74	0.39
$\max S_{\min}(e^{j\Omega}, \hat{\theta}) $	1.66	0.25

Comparison of estimated inertias



Case	Median	RMSE
Actual	3.5	0
Case 1	3.40	0.46
Case 2	3.33	0.40
Case 3	3.27	0.43

Major contributions



- Tested the methods with a more detailed power plant model.
- Tested the methods with a more detailed power system model.
- Investigate some of the assumptions from previous papers.

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Motivation



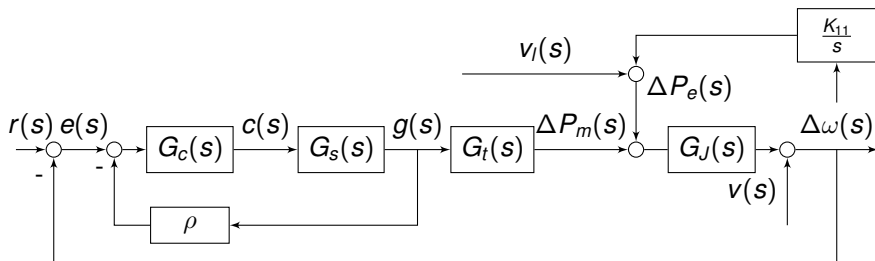
- How to best identify hydro power plant dynamics given access to control system data.

Systems to be identified

$$e(s) = G_1(s)\Delta P_{e1}(s) + S(s)r(s) \quad (23)$$

$$\Delta\omega_1(s) = G_s(s)G_t(s)G_J(s)c(s) - G_J(s)\Delta P_{e1}(s) \quad (24)$$

$$G_p(s) = \frac{G_c(s)G_s(s)G_t(s)G_J(s)}{G_J(s)(1 + \rho G_c(s)G_s(s))} \quad (25)$$



Systems to be identified



$$e(s) = G_1(s)\Delta P_{e1}(s) + S(s)r(s) \quad (23)$$

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— Two approaches.

Systems to be identified



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- Two approaches.
- Extra excitation is needed.

Systems to be identified



$$e(s) = G_1(s)\Delta P_{e1}(s) + S(s)r(s) \quad (23)$$

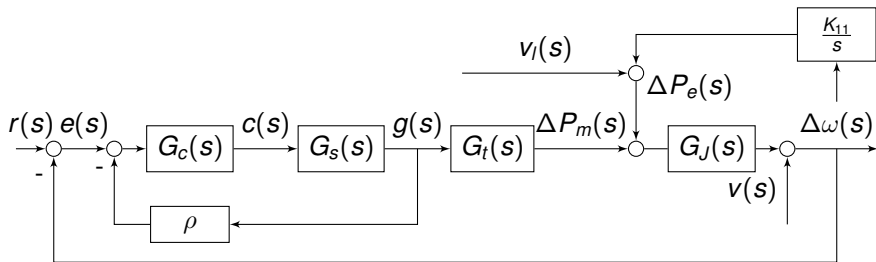
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$$G_p(s) = \frac{G_c(s)G_s(s)G_t(s)G_J(s)}{G_J(s)(1 + \rho G_c(s)G_s(s))} \quad (25)$$

- Two approaches.
- Extra excitation is needed.
- PMU approach is a special case without extra excitation.

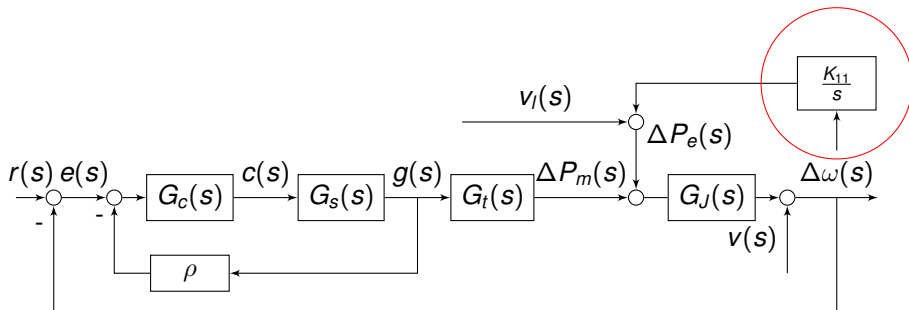
Identifiability

— The systems can be identified



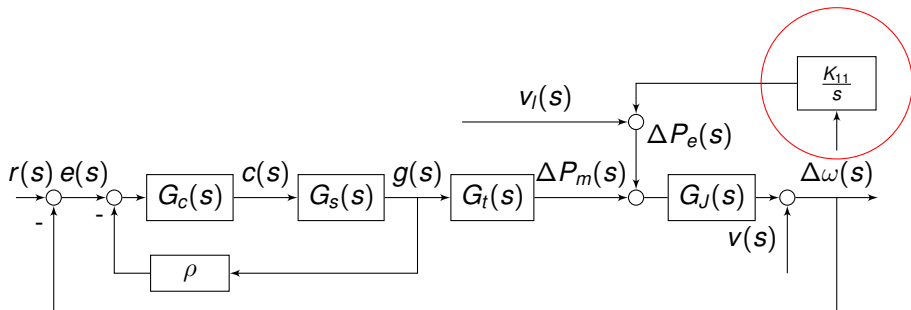
Identifiability

- The systems can be identified
- However, there is a lack of delay



Identifiability

- The systems can be identified
- However, there is a lack of delay
- This is no problem if $v(s) \ll v_I(s)$.



Identifying $G_p(s)$ and $G_J(s)$

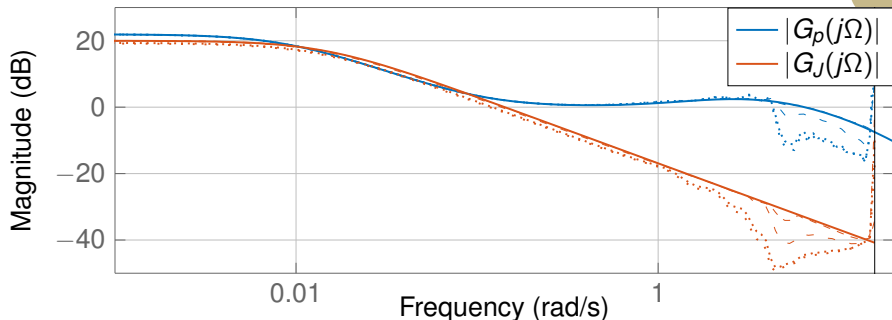


Figure: The mean value of $|G_p(e^{j\Omega}, \hat{\theta}_N)|$ and $|G_J(e^{j\Omega}, \hat{\theta}_N)|$ calculated from the MCS. The solid lines are the analytical calculated versions and the dashed loosely dashed dotted and loosely dotted lines represent an SNR of 50dB, 26dB, 6dB, and 3dB respectively

Identifying $S(s)$

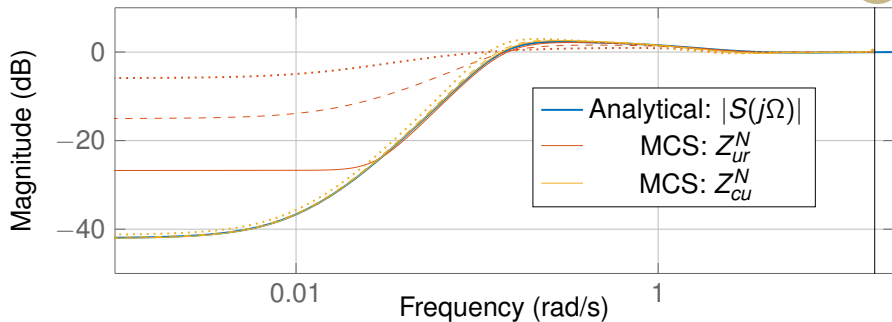


Figure: The mean value of $|S(e^{j\Omega}, \hat{\theta}_N)|$ calculated analytical and from the MCS. The solid, dashed and dotted lines represent an SNR of 50dB, 26dB, and 6dB respectively

Identifying $G_1(s)$

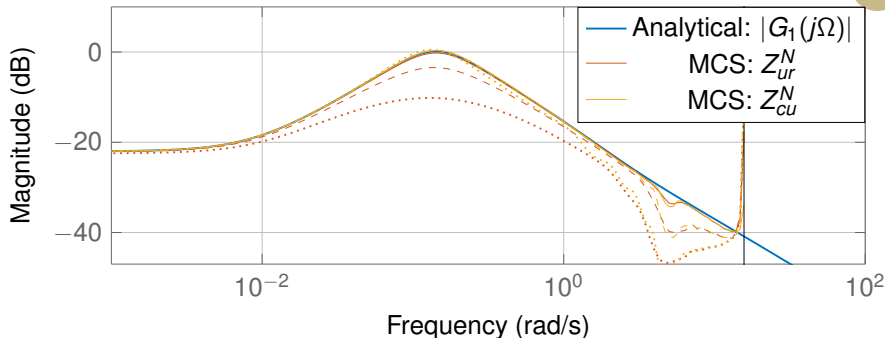


Figure: The mean value of $|G_1(e^{j\Omega}, \hat{\theta}_N)|$ calculated analytical and from the MCS. The solid, dashed and dotted lines represent an SNR of 50dB, 26dB, and 6dB respectively

Major contributions



- Demonstrated two methods for finding transfer functions for checking the requirements in closed loop.
- Analytical validation of the demonstrated methods.
- Addressed the delay condition.

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Conclusions



- The requirements can be checked using PMU-measurements, however, the results will be biased for faster dynamics.
- The requirements can be checked using control system measurements in normal operation, however, the results may be biased for faster dynamics.
- The requirements can be checked using measurement from normal operation with extra excitation

Further work



- Validate approaches in the lab
- Solve the delay condition.
- Handle backlash.
- Investigate the alternative requirements.