



# **Frequency control and stability requirements on hydro power plants**

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October 31, 2019



# Outline

Background and research questions

Methodology

Simple test system

Theoretical validation

Tests at Statkraft's power plant

More detailed simulations

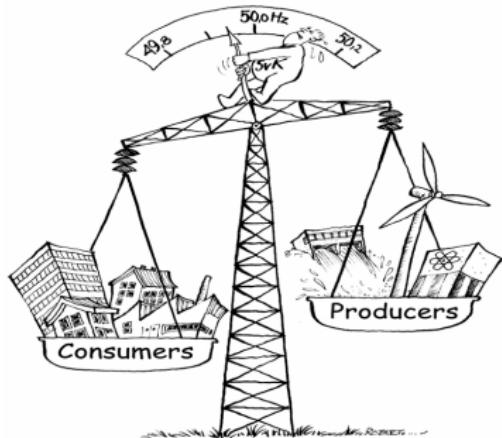
The best way to do the identification

Conclusions and further work



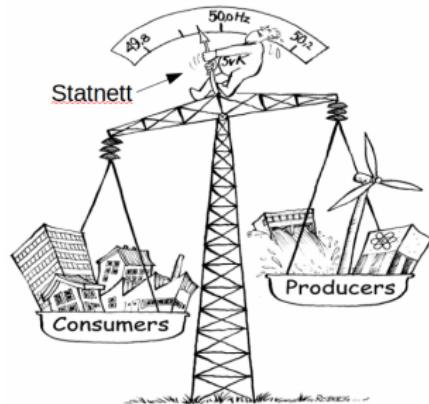
# Load and production balancing

- The power system frequency measures the power balance.



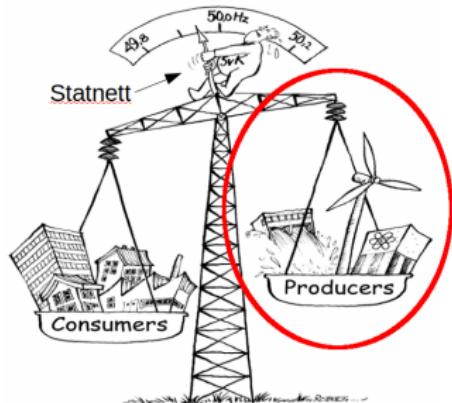
# Load and production balancing

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- It is the responsibility of the TSOs to control the frequency.



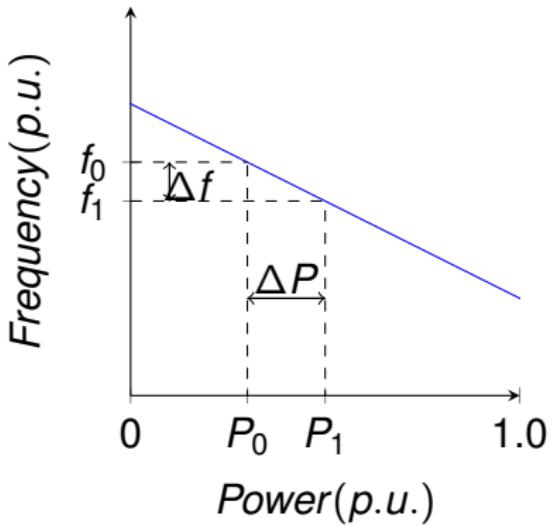
# Load and production balancing

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- However, it is the power plant owners who can control the frequency.

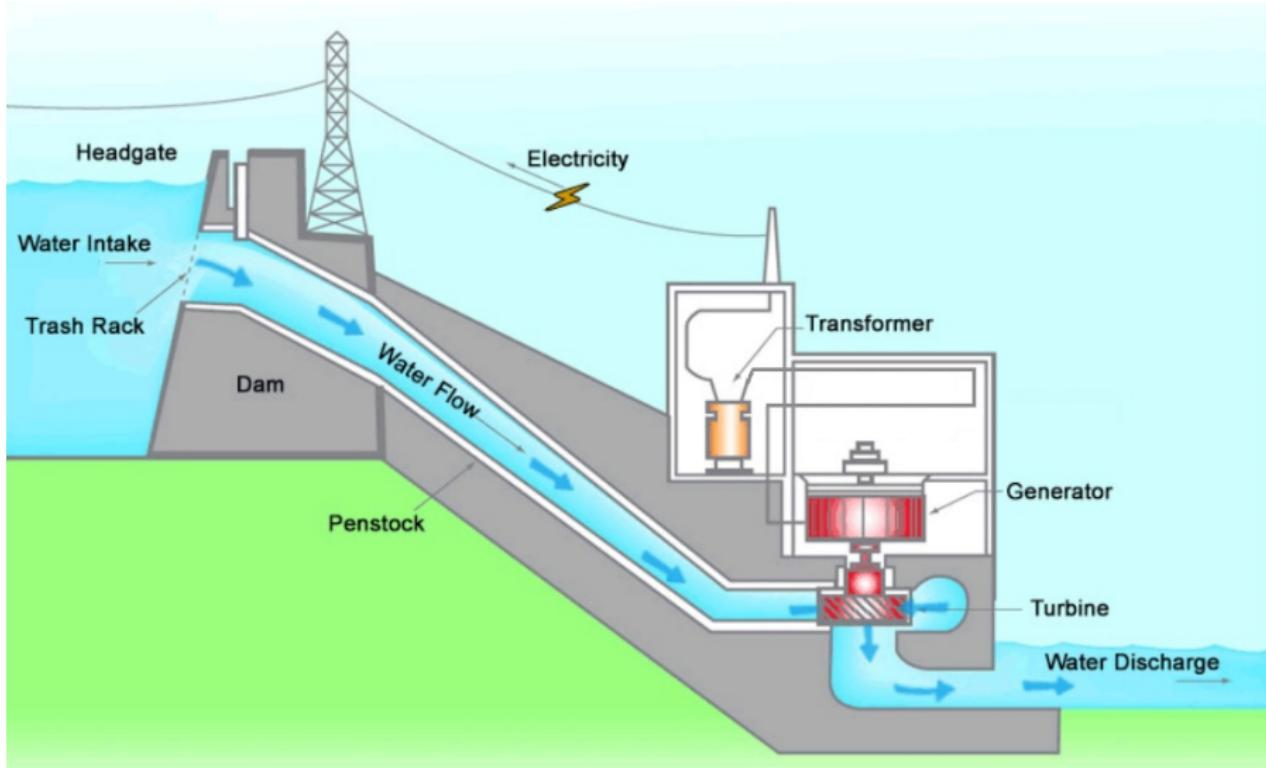


# Load and production balancing

- The power system frequency measures the power balance.
- It is the responsibility of the TSOs to control the frequency.
- However, it is the power plant owners who can control the frequency.
- The TSOs pay all power plant owners above a certain size to provide frequency control.(droop  $\rho = \Delta f / \Delta P$ )

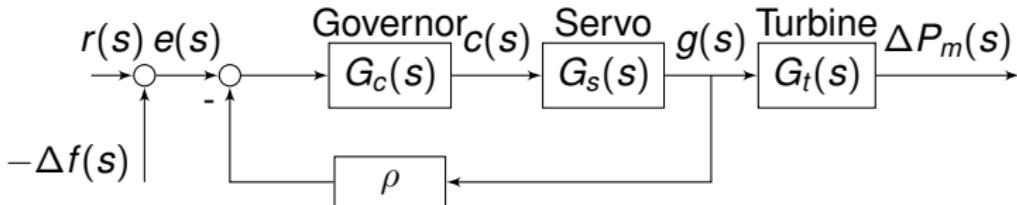


# Hydro power plant



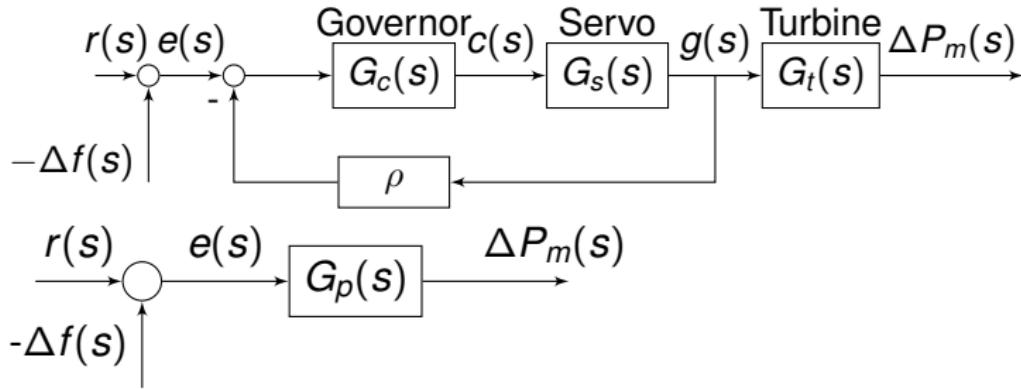
# Implementation of the frequency containment process

- $r(s)$  Reference frequency
- $e(s)$  Control error
- $f(s)$  Frequency
- $c(s)$  Control signal
- $g(s)$  Guide vane opening
- $\Delta P_m(s)$  Mechanical power



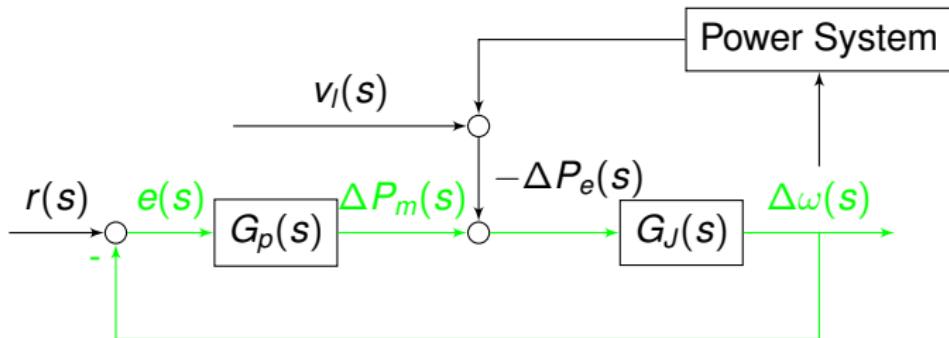
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# The frequency containment process $G_p(s)$ in the power system

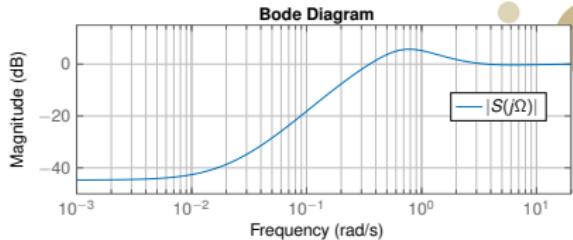
- $G_J(s)$  represents the swing dynamics of the power plant.
- $v_l(s)$  represents stochastic load.



# Stability requirements for frequency control

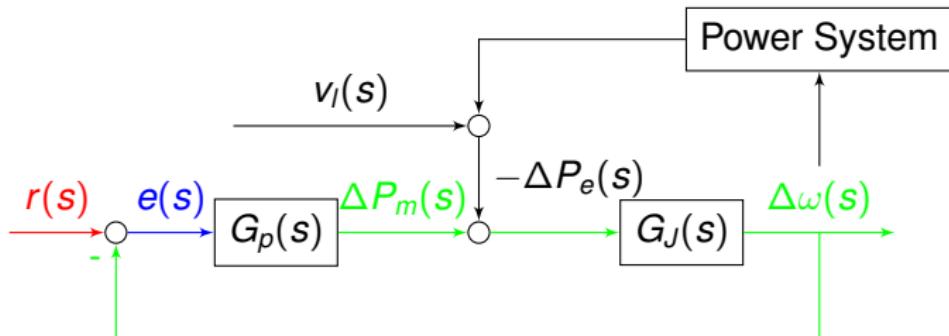
- Stability margin from control theory:

$$\max |S(j\Omega)| < M_s \quad (1)$$



- where:

$$S(s) = \frac{1}{1 + G_p(s)G_J(s)} \quad (2)$$



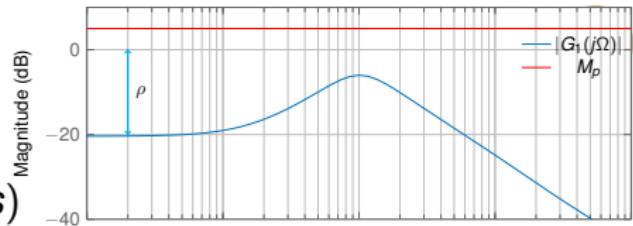
# Performance requirements for frequency control

- We want to contain frequency deviations.

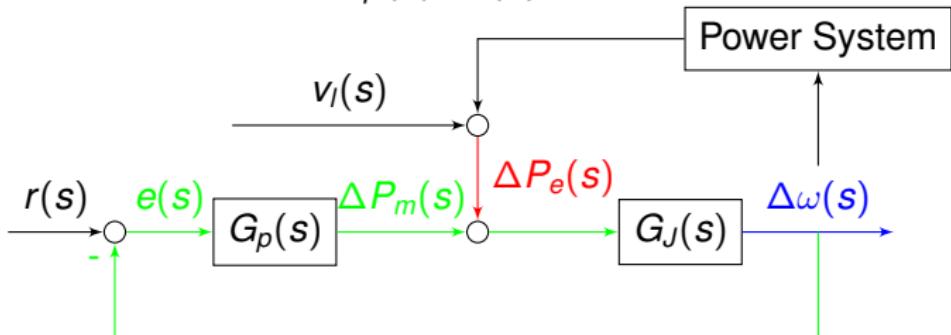
$$\Delta\omega(s) = \frac{G_J}{1 + G_p(s)G_J(s)} \Delta P_e(s) \quad (3)$$

- Define

$$G_1(s) = \frac{G_J}{1 + G_p(s)G_J(s)} \quad (4)$$

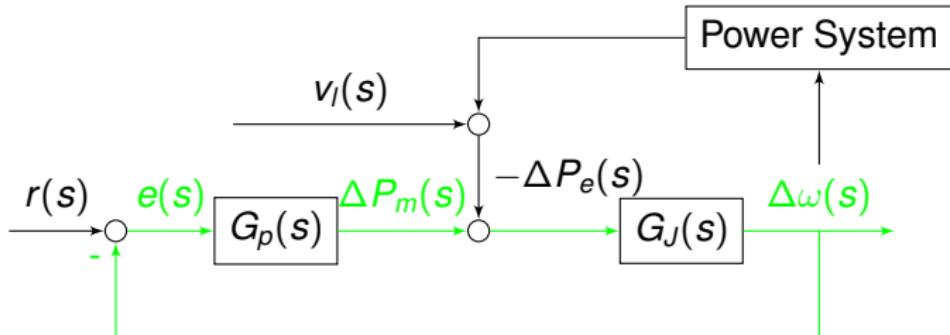


$$|G_1(j\Omega)| < M_p \quad (5)$$



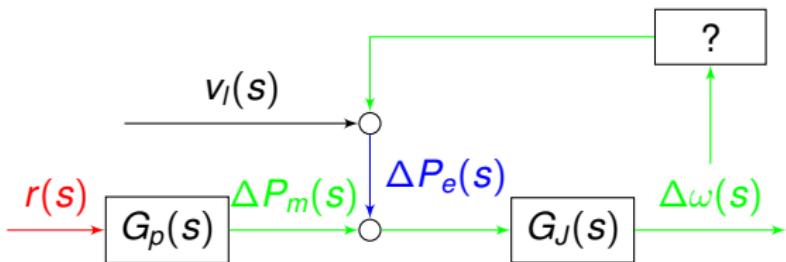
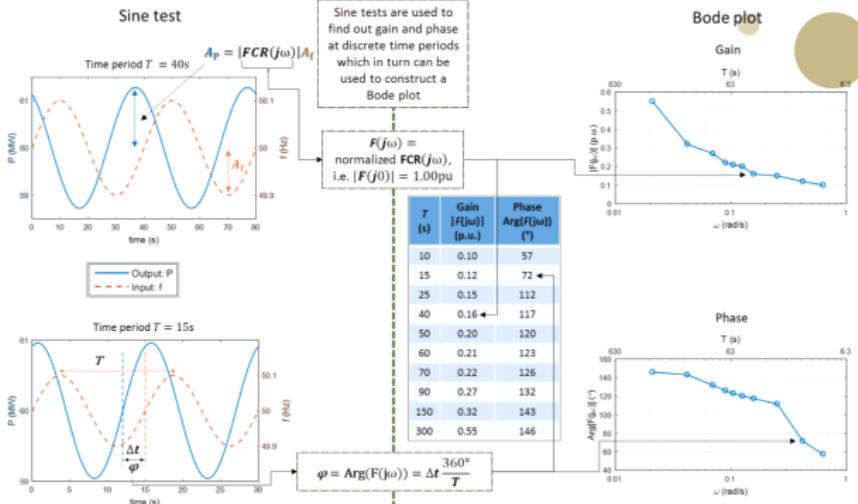
# Future of frequency control

- Power plants have to show that they fulfill:
  - Stability requirement  $|S(j\Omega)| < M_s$
  - Performance requirement  $|G_1(j\Omega)| < M_p$
- To do this they need models of:
  - $G_p(s)$
  - and  $G_J(s)$



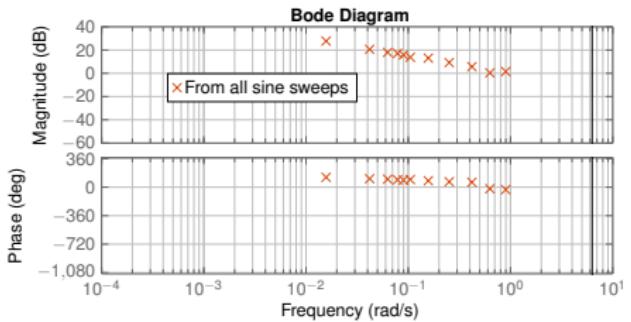
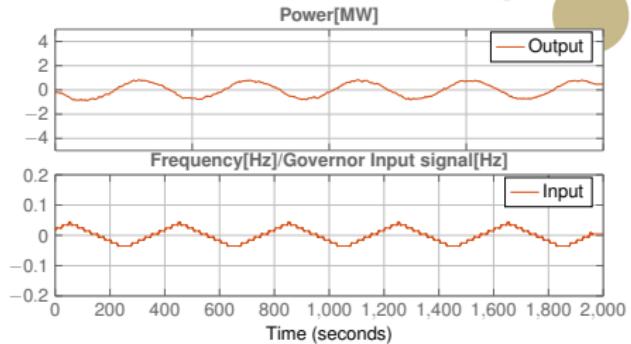
# Industry proposed tests

- Time consuming.
- Use system estimate for  $G_J(s)$ .
- Input  $r(s)$
- Output  $\Delta P_e(s)$



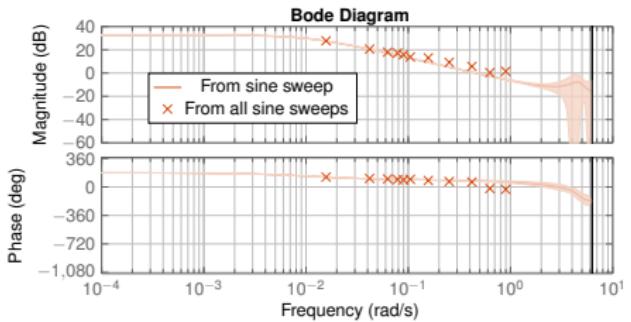
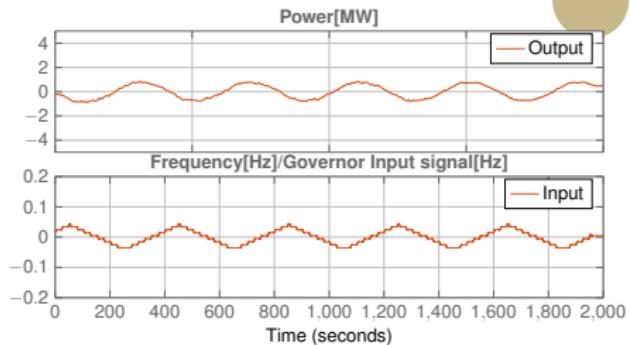
# Example from real tests

- The power plant needs to be disconnected
- Takes up to 20 hours.



# Example from real tests

- The power plant needs to be disconnected
- Takes up to 20 hours.
- Only one sine test needed with system identification.



# Motivation

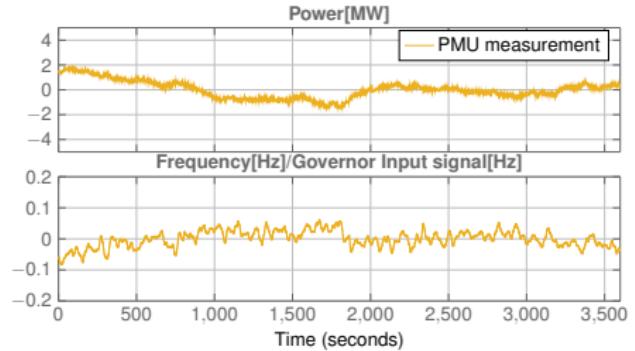


— Can we do the tests easier?

# Motivation



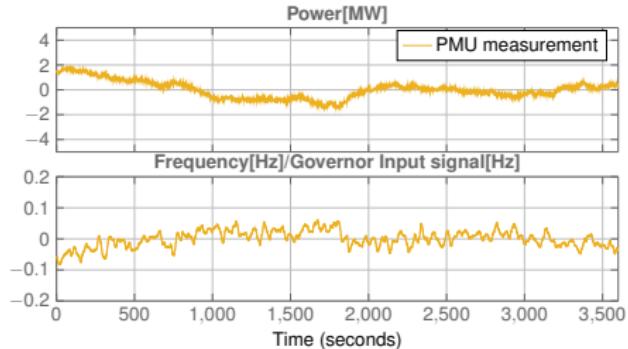
- Can we do the tests easier?
- The power system is never really in steady state.



# Motivation



- Can we do the tests easier?
- The power system is never really in steady state.
- Can the power plant dynamics be identified from normal operation measurements?



## Research questions



- Can power plant dynamics be identified using a PMU?
- Can power plant dynamics be identified using control system measurements without disturbing the operation of the plant?
- What is the effect of nonlinearities on the identification?

# Outline

Background and research questions

## Methodology

Simple test system

Theoretical validation

Tests at Statkraft's power plant

More detailed simulations

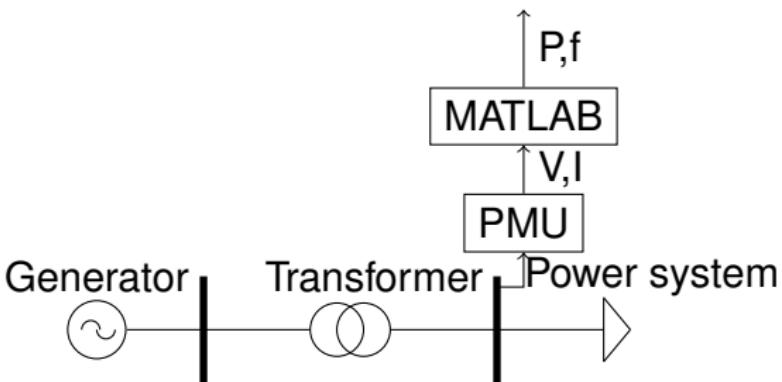
The best way to do the identification

Conclusions and further work



# Methodology

- Collect data from PMU or control system.
- Preprocess data.
- Calculate power and frequency from the measurements.
- Identify models.
- Validate models.



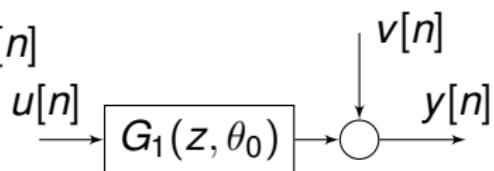
# System identification basic

- Assume that a data set  $Z^N = \{u[n], y[n] | n = 1 \dots N\}$  has been collected.
- The dataset  $Z^N$  is assumed generated by

$$\mathcal{S} : y[n] = G_1(z, \theta_1)u[n] + H_1(z, \theta_1)e[n]$$

- Using the data set  $Z^N$  we want to find the parameter vector  $\theta^N$  minimizing

$$\hat{\theta}_N = \arg \min_{\theta} \frac{1}{N} \sum_{n=1}^N [H_1^{-1}(z, \theta)(y[n] - G_1(z, \theta)u[n])]^2$$



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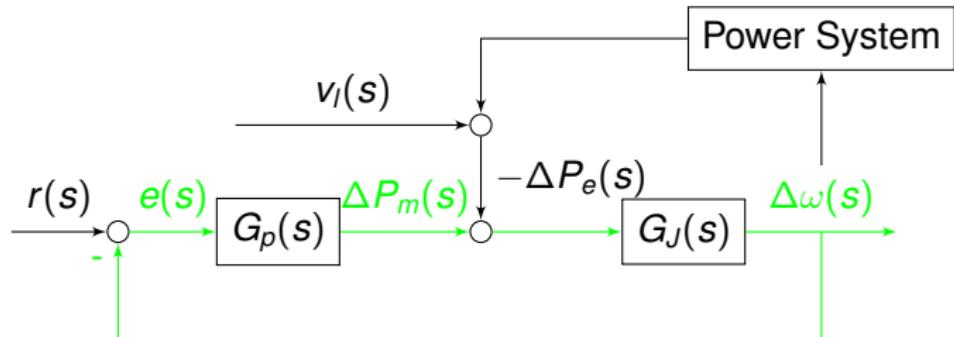
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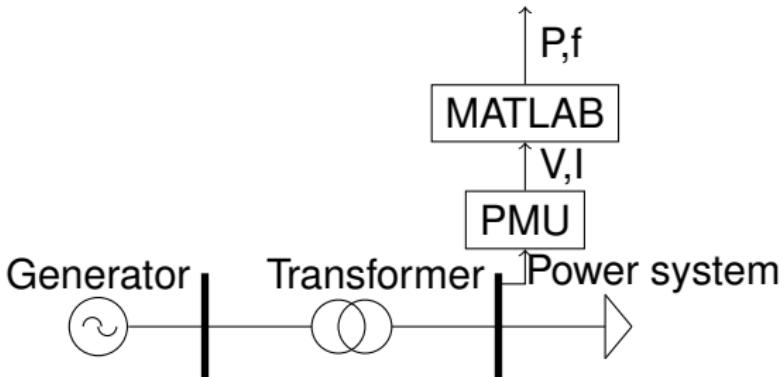


- Create a model for analysing the identifiability of hydro power plant dynamics.



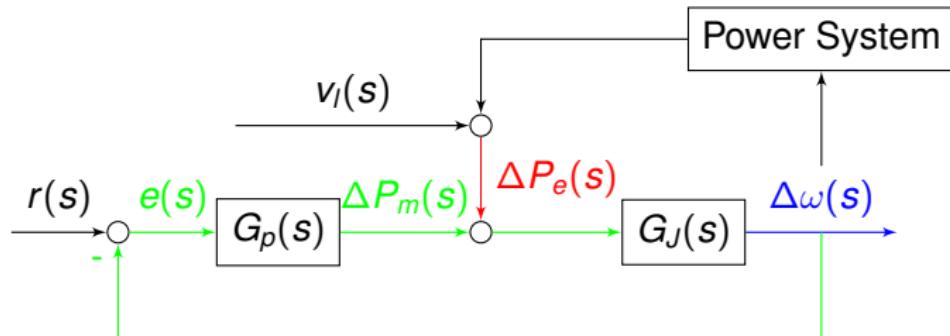
# What do we need to model?

- From the PMU we get
  - Power:  $\Delta P_e(s)$ .
  - Frequency:  $\Delta f(s) \approx 2\pi\Delta\omega(s)$ .



# What do we need to model?

- From the PMU we get
  - Power:  $\Delta P_e(s)$ .
  - Frequency:  $\Delta f(s) \approx 2\pi\Delta\omega(s)$ .
- We need to model how  $\Delta P_e(s)$  and  $\Delta f(s)$  is related through the power system.
- We need to model the external perturbation.
- We also need to model the power plant consisting of  $G_p(s)$  and  $G_J(s)$ .

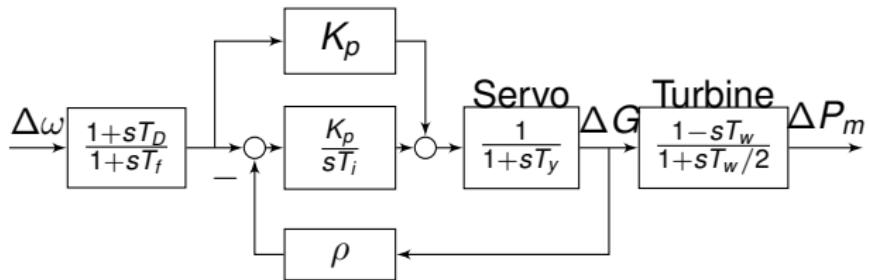


# Power plant model



- Model for  $G_p(s)$
- Model for  $G_J(s)$

$$G_J(s) = \frac{1}{2Hs + K_d} \quad (6)$$



# Power system model

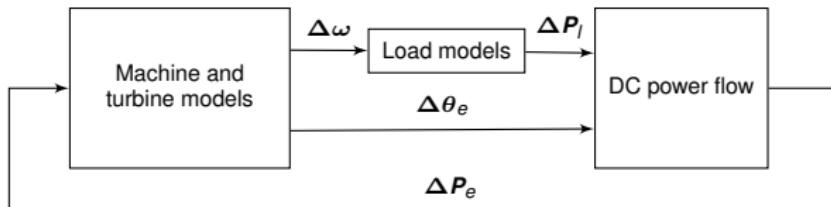


- The frequency and power system angle is related.
- The angle and power is related.
- On matrix form.

$$\Delta\theta(s) = \frac{2\pi f_s}{s} f(s) \quad (7)$$

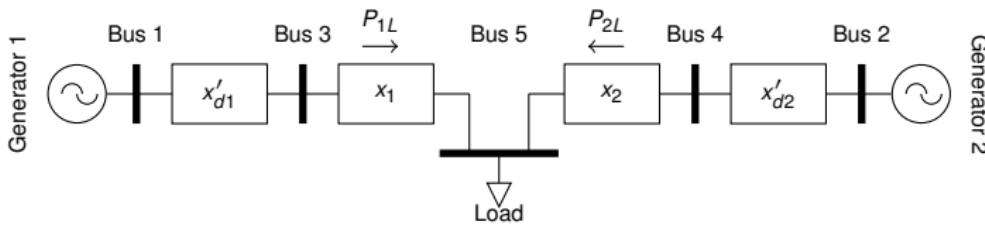
$$P_k \approx \sum_{m \in \Omega_k} x_{km}^{-1} \theta_{km} \quad (8)$$

$$\mathbf{P} = \mathbf{Y}\boldsymbol{\theta} \quad (9)$$



# Single line diagram of test system

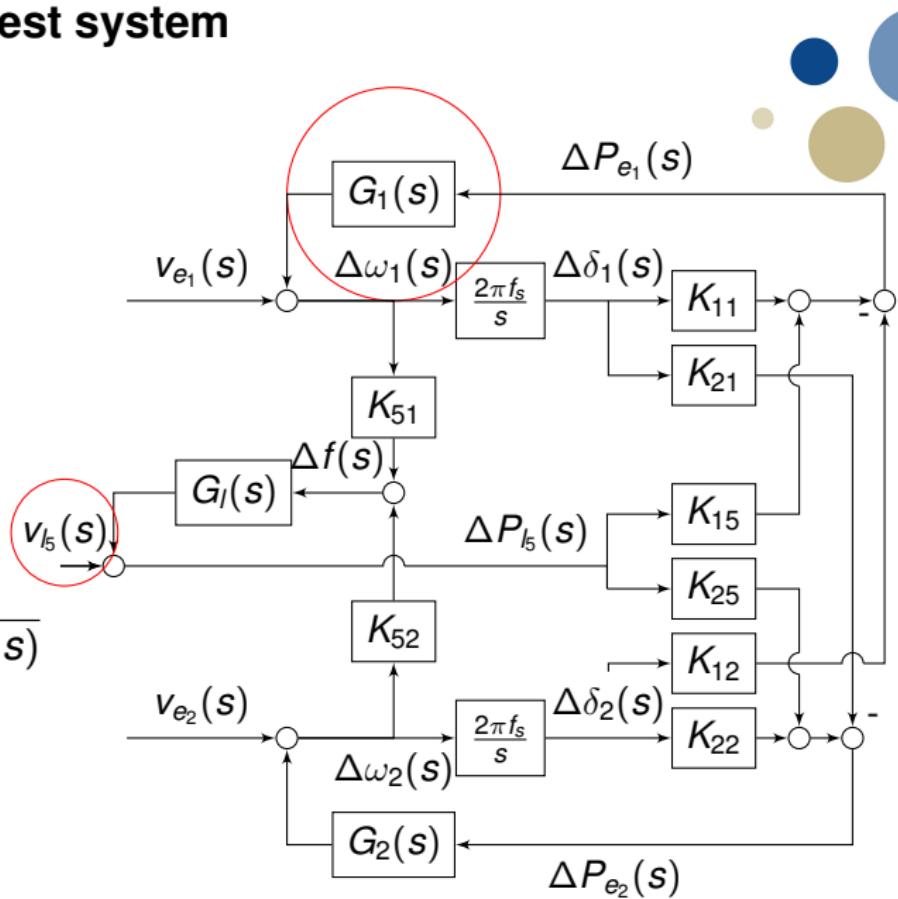
- Generator 1 is the plant we study.
- Generator 2 represents the rest of the power system.
- The load represents the stochastic behaviour of all loads.
- $x_1$  and  $x_2$  are line reactances.
- $x'_{d1}$  and  $x'_{d2}$  are generator reactances.



# Block diagram of test system

- $G_1(s)$  the plant we investigate.
- $v_{l5}(s)$  external perturbation.

$$G_1(s) = \frac{G_J}{1 + G_p(s)G_J(s)}$$



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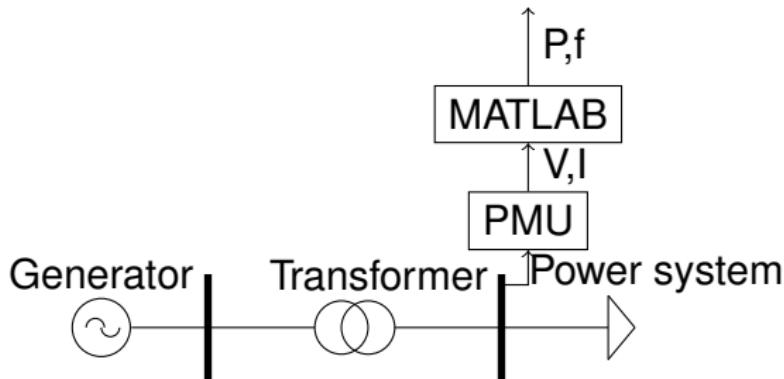
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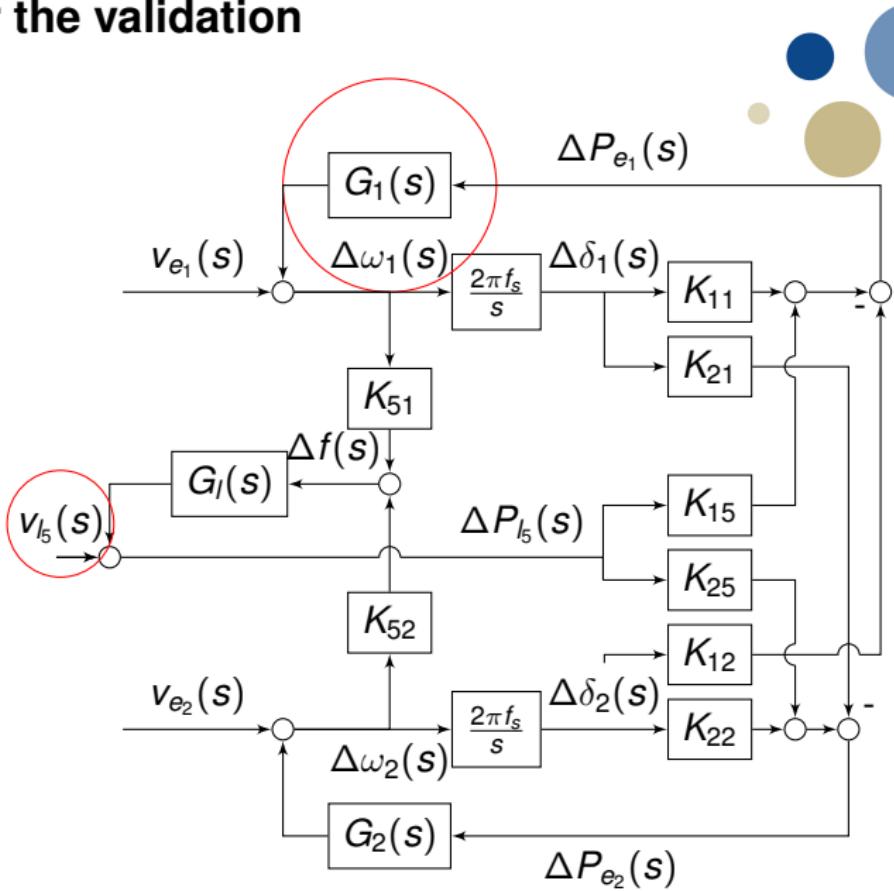
# Motivation

- To validate the PMU method analytically.



# Modelling used for the validation

- The system we want to identify is  $G_1(s)$ .
- The external perturbation to the system is  $v_I(s)$ .



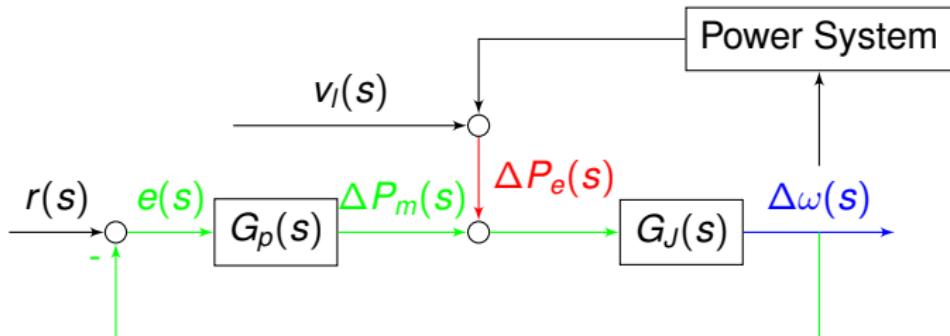
# What can we identify using a PMU

- $\Delta\omega(s)$  is related to  $\Delta P_e(s)$  by:

$$\Delta\omega(s) = \frac{G_J}{1 + G_p(s)G_J(s)} \Delta P_e(s)$$

- This means that we can identify:

$$G_1(s) = \frac{G_J}{1 + G_p(s)G_J(s)}$$



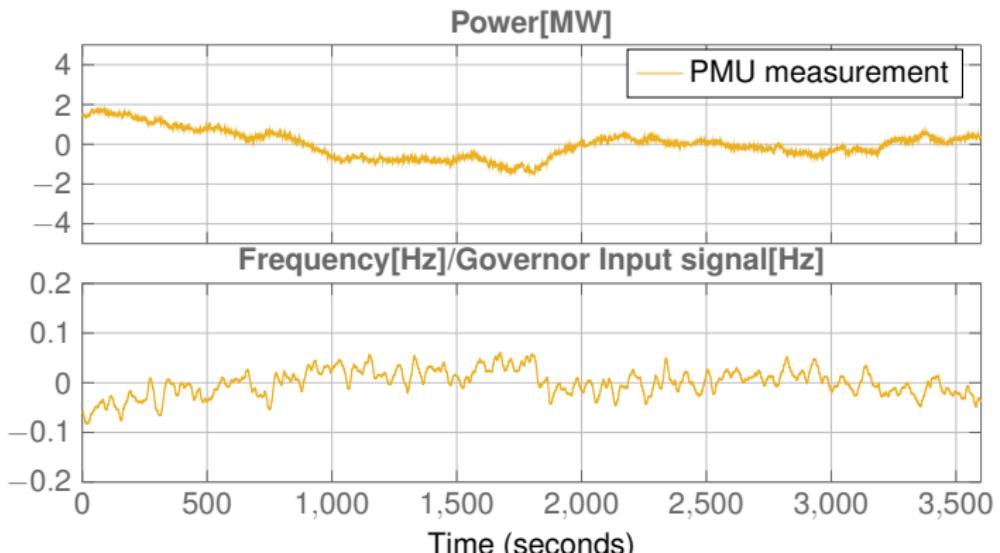
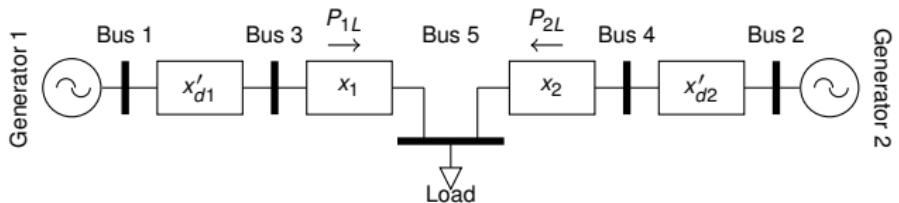
## Assumptions for the theoretical validation



- The system is excited by a load acting as a filtered white noise process
- The measurement error of the electrical power is negligible.
- The measured frequency is a good estimate of the generator speed.

# Assumptions for the theoretical validation

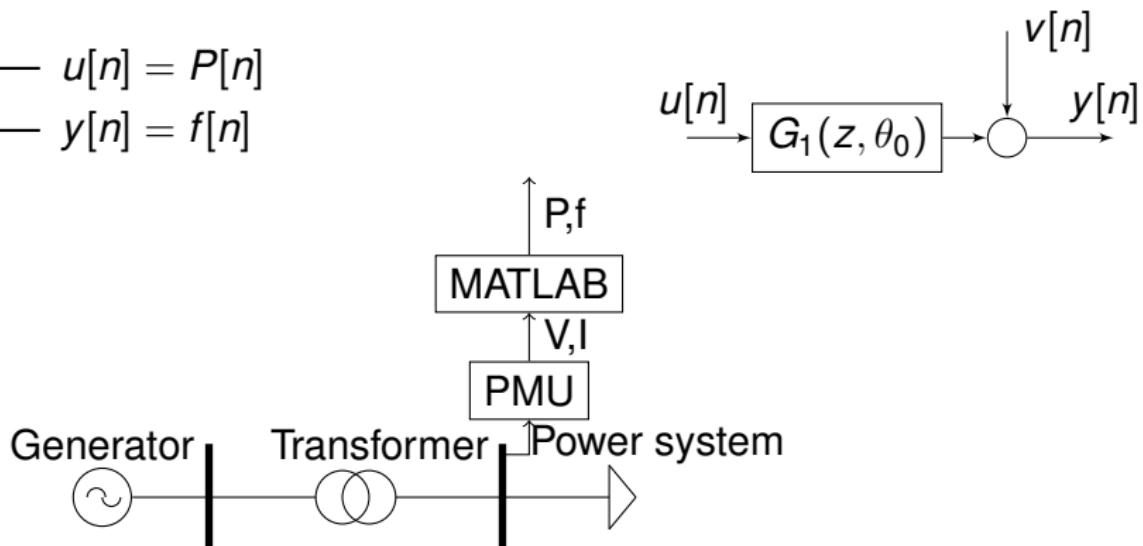
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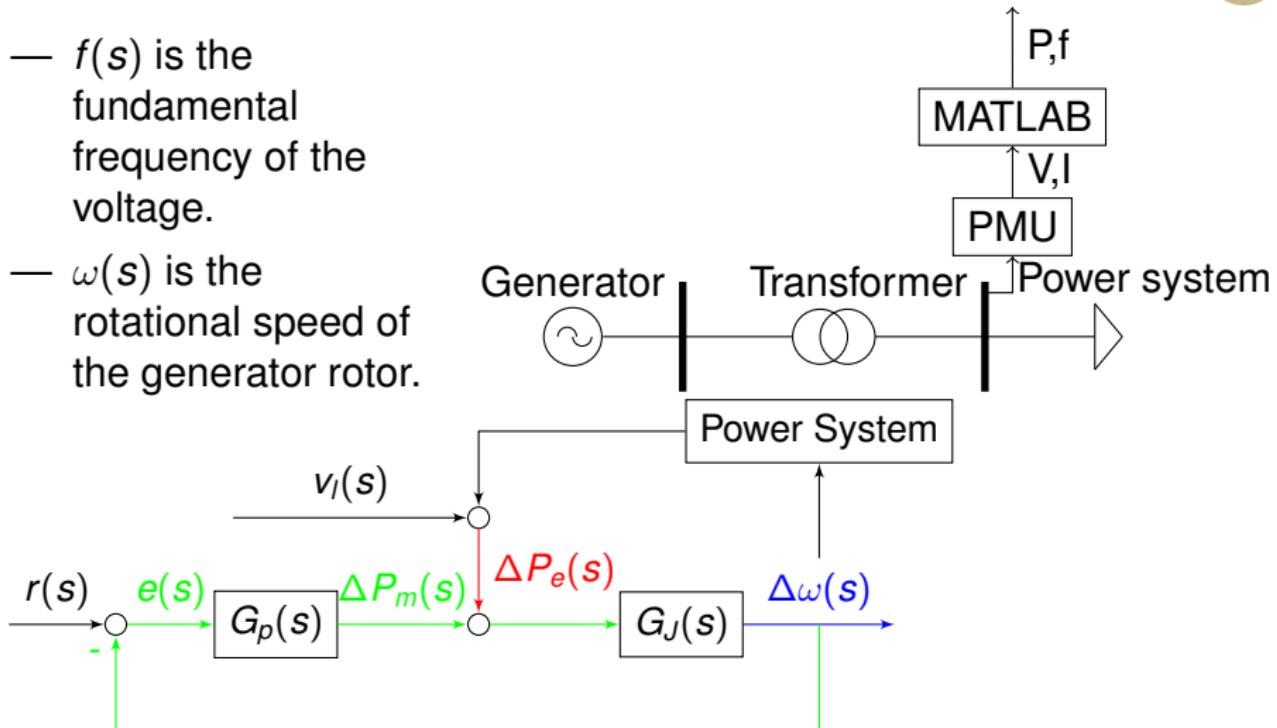
- $u[n] = P[n]$
- $y[n] = f[n]$



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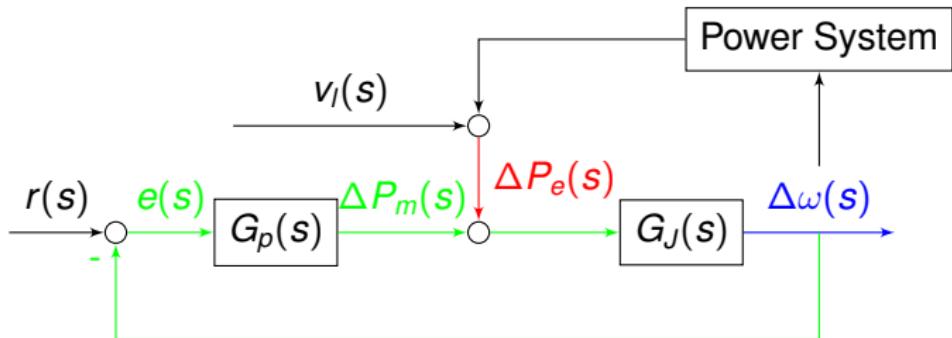
- $f(s)$  is the fundamental frequency of the voltage.
- $\omega(s)$  is the rotational speed of the generator rotor.



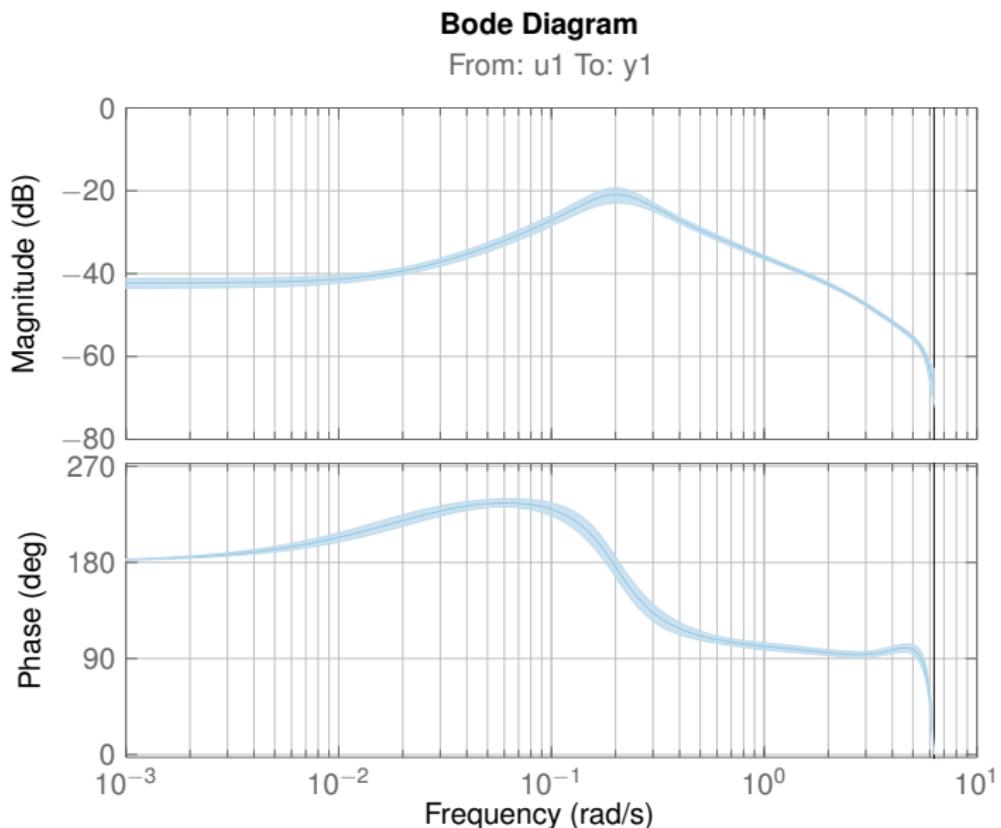
## Results from the theoretical validation

- A consistent estimate of  $G_1(s)$  can be obtained by using:
  - Measured PMU frequency as the output  $u[n]$
  - Measured PMU power as the input  $y[n]$
  - If there is a delay between  $\Delta\omega(s)$  and  $\Delta P_e(s)$ .

$$G_1(s) = \frac{G_J}{1 + G_p(s)G_J(s)}$$



# Model obtained using PMU data



## Main contributions



- To show that the transfer function that can be identified using a PMU is  $G_1(s)$ .
- To prove under which conditions a consistent estimate of  $G_1(s)$  is possible.
- To demonstrate the theory for identification of  $G_1(s)$  on a real dataset.

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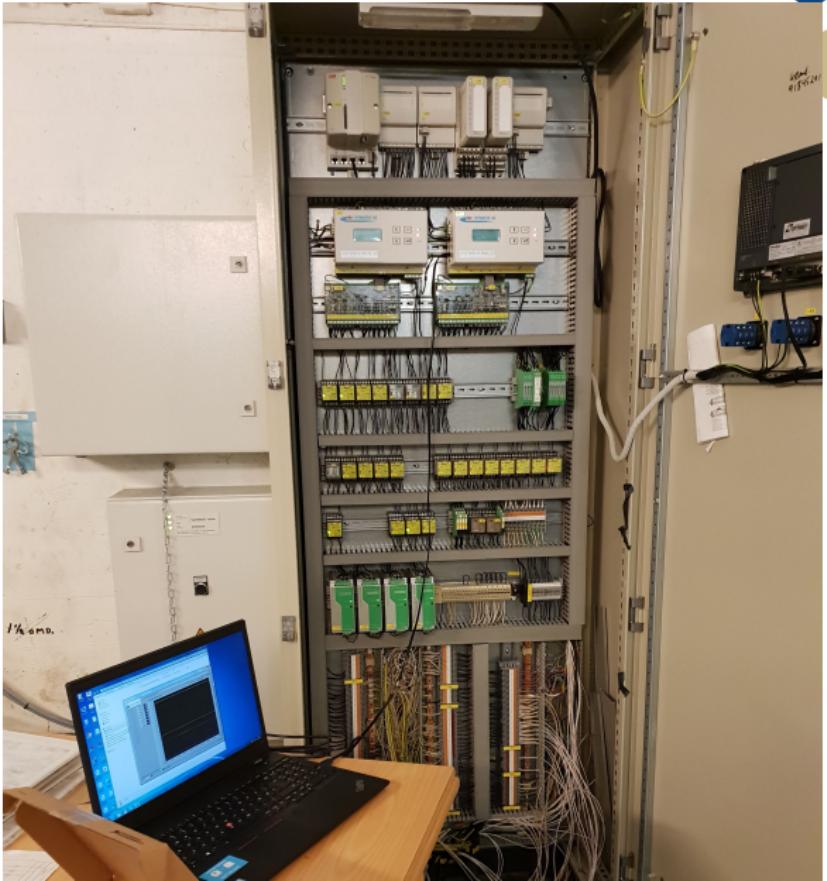
- Test the method on more real datasets.
- Demonstrate that the method can detect parameter changes.

# Power plant location



# Getting data from the control system

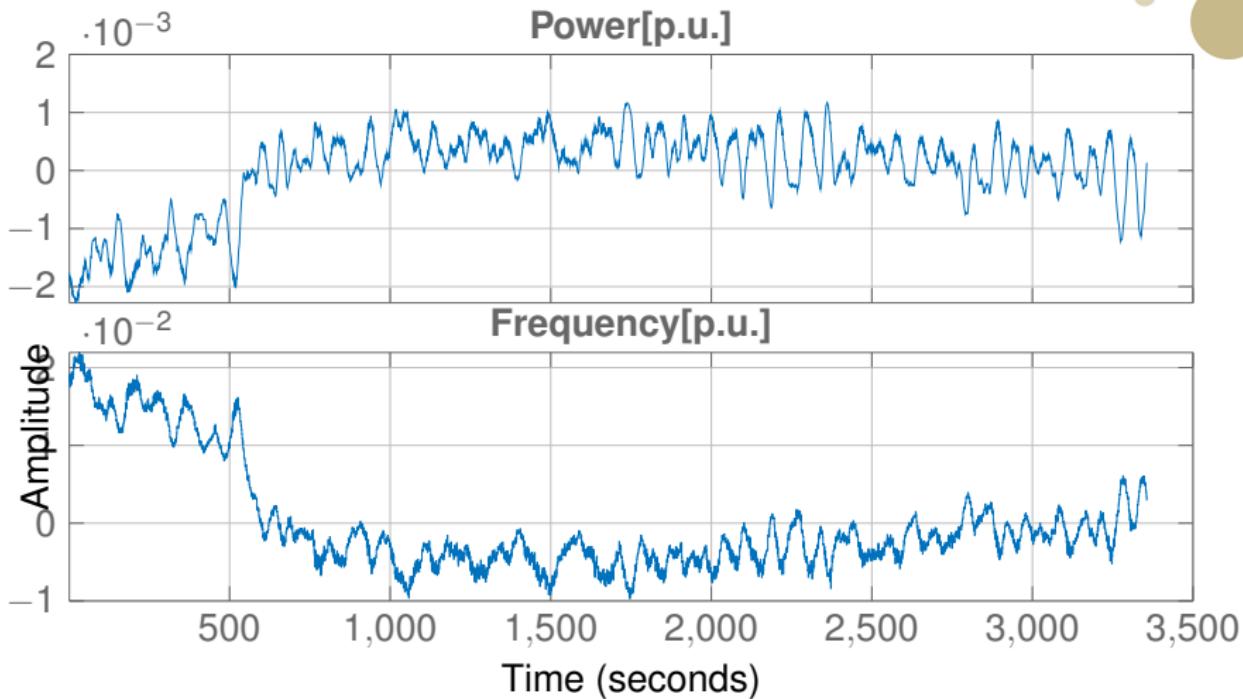
- Collected Electric power  $\Delta P_e$
- and power system frequency  $\Delta f$ .



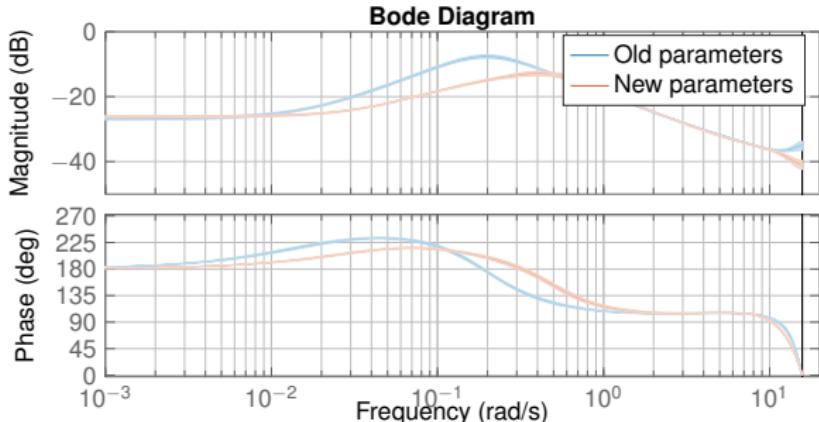
# Measurement transformer



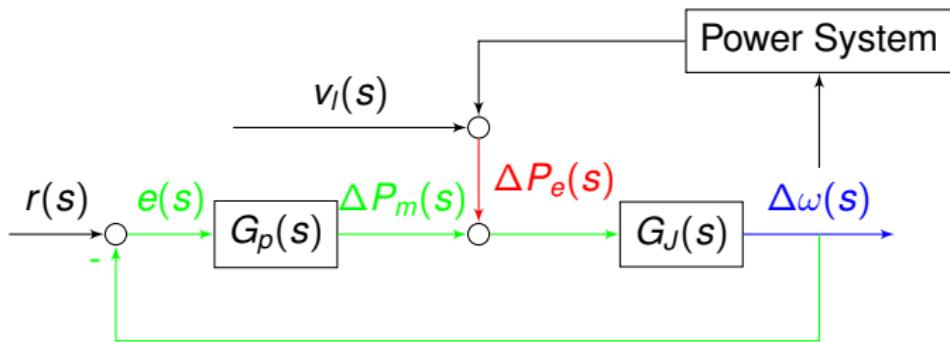
## Example of dataset



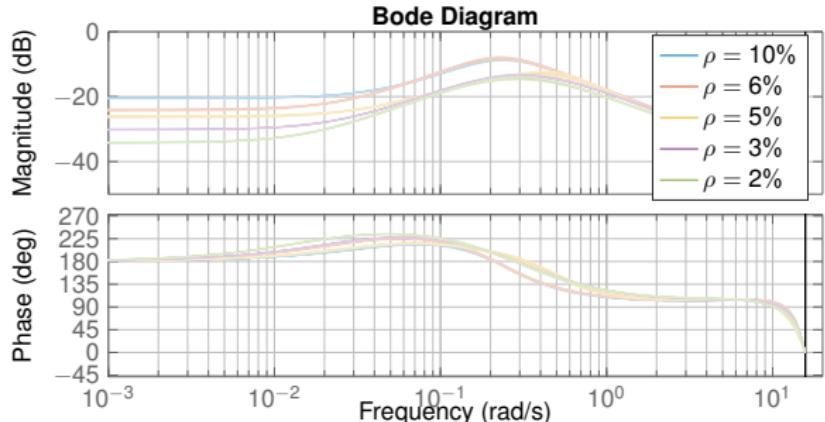
# Detecting a new tuning



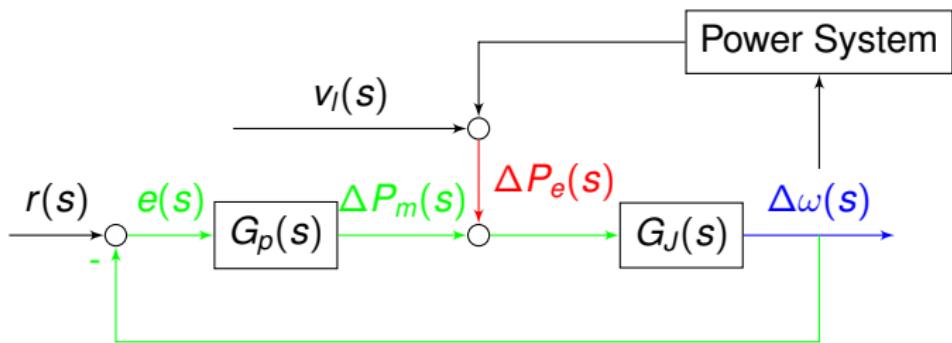
$$G_1(s) = \frac{G_J}{1 + G_p(s)G_J(s)}$$



# Detecting droop changes



$$G_1(s) = \frac{G_J}{1 + G_p(s)G_J(s)}$$



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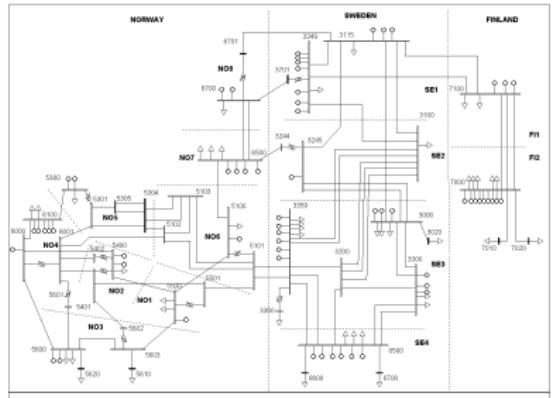
# Motivation



- Test with a more detailed power plant model.
- Test with a more detailed power system model.
- Investigate the frequency assumption.

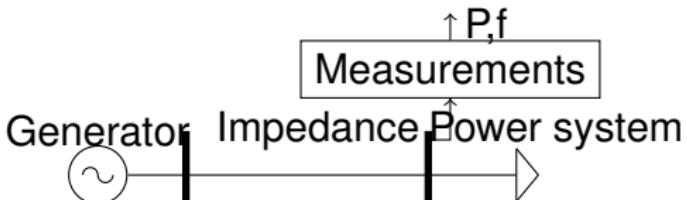
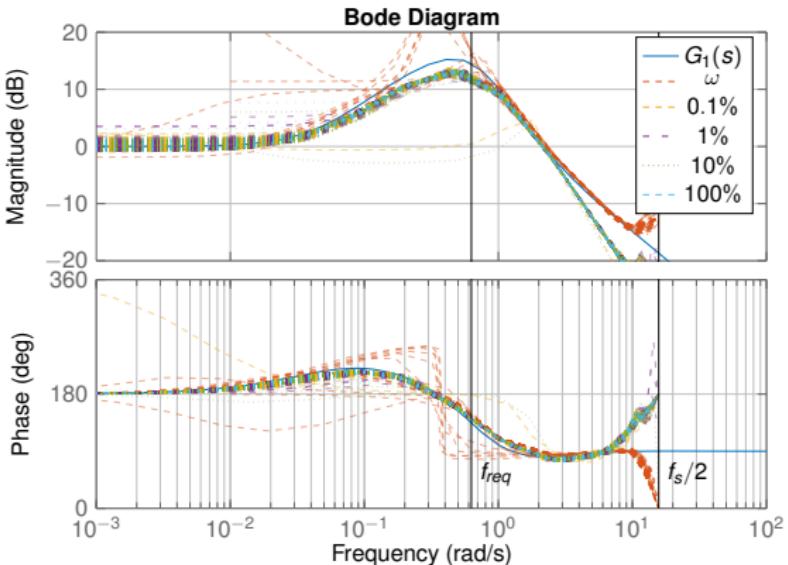
## More detailed power system model

- Used the Nordic 44 test system in PSS/E.



# Test frequency assumption

- $f(s)$  is the fundamental frequency of the measured voltage.
- $\omega(s)$  is the rotational speed of the generator rotor.
- Increased the impedance between the generator and PMU.
- 100 simulations for each



## Main contribution



- Demonstrated that the results for faster dynamics are biased if the frequency is measured instead of the rotational speed of the rotor.

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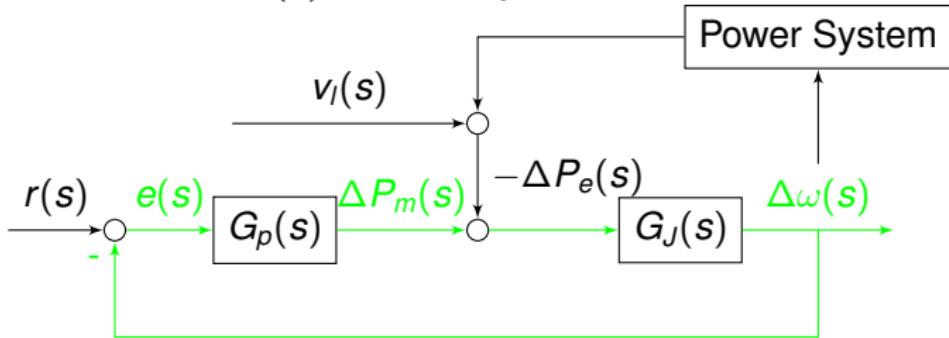
- How to best check the requirements given access to control system data.

# What do we want to check

- Stability requirement  $|S(j\Omega)| < M_s$
- Performance requirement  $|G_1(j\Omega)| < M_p$
- In the requirements this is done by identifying.
  - $G_p(s)$  in open loop
  - and  $G_J(s)$  from the system

$$S(s) = \frac{1}{1 + G_p(s)G_J(s)}$$

$$G_1(s) = \frac{G_J}{1 + G_p(s)G_J(s)}$$

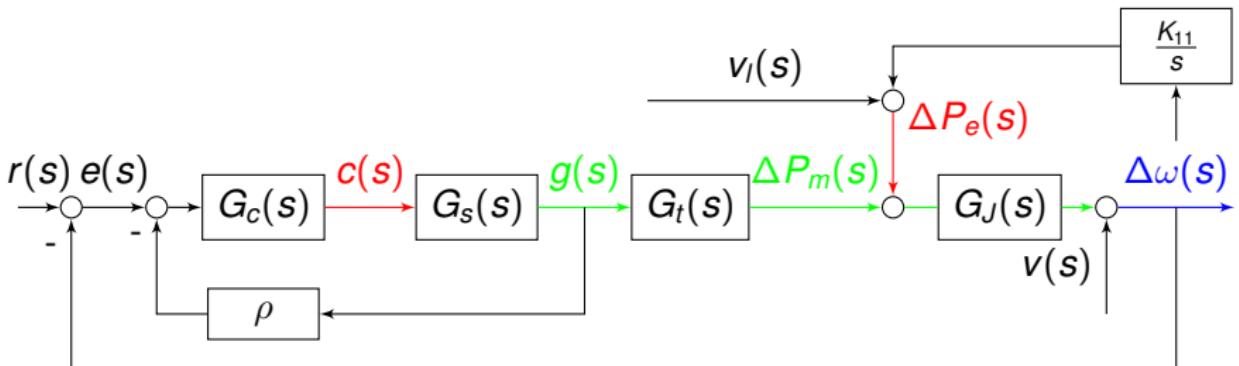


## Identify $G_p(s)$ and $G_J(s)$ in closed loop, Method 1

$$\Delta\omega(s) = G_s(s)G_t(s)G_J(s)c(s) - G_J(s)\Delta P_e(s) \quad (10)$$

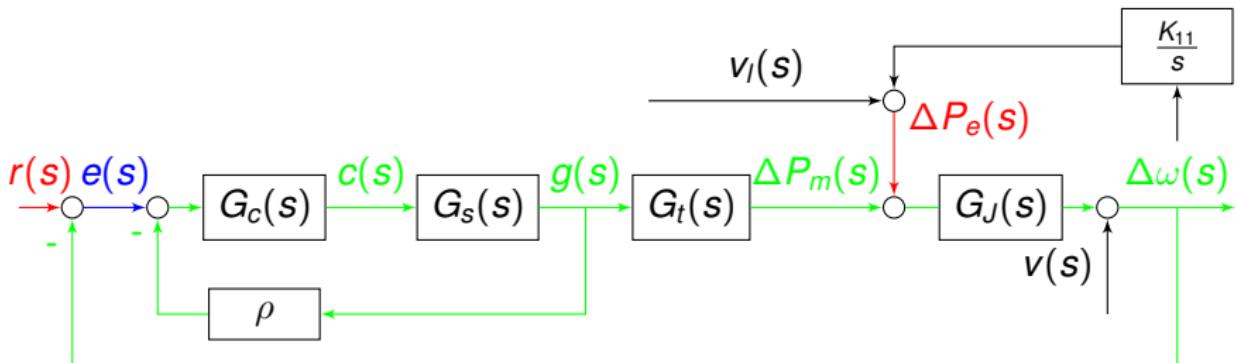
— Assume  $G_c(s)$  to be known.

$$G_p(s) = \frac{G_c(s)G_s(s)G_t(s)G_J(s)}{G_J(s)(1 + \rho G_c(s)G_s(s))} \quad (11)$$



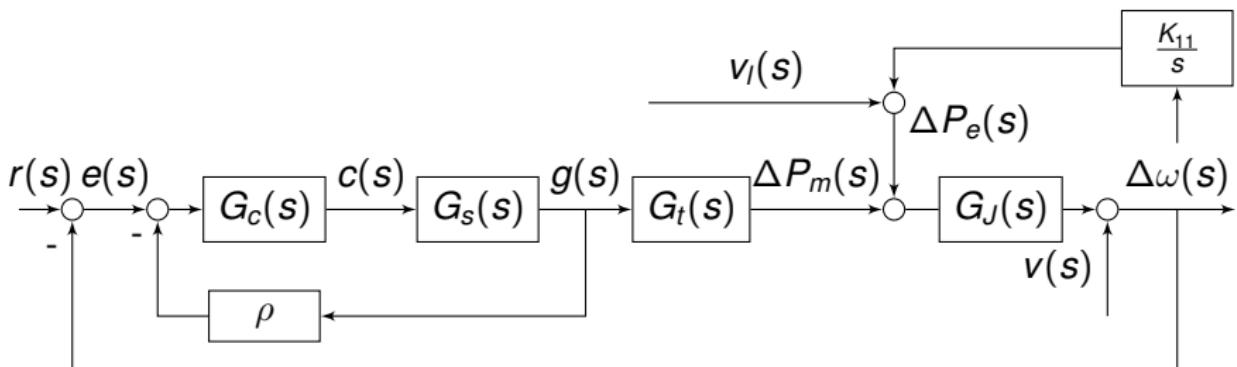
## Identify $G_1(s)$ and $S(s)$ directly in closed loop, Method 2

$$e(s) = G_1(s)\Delta P_e(s) + S(s)r(s) \quad (12)$$



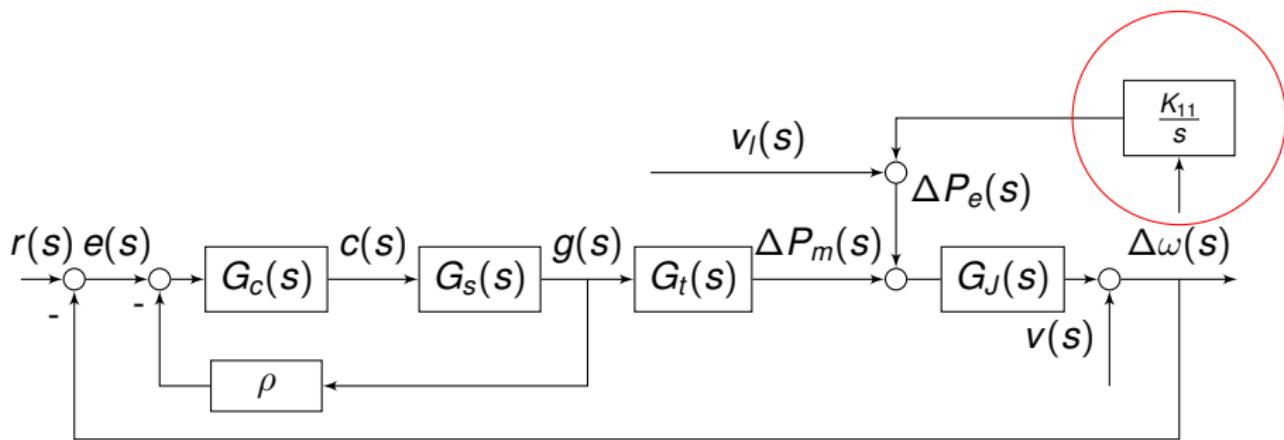
# Identifiability

- The systems can be identified



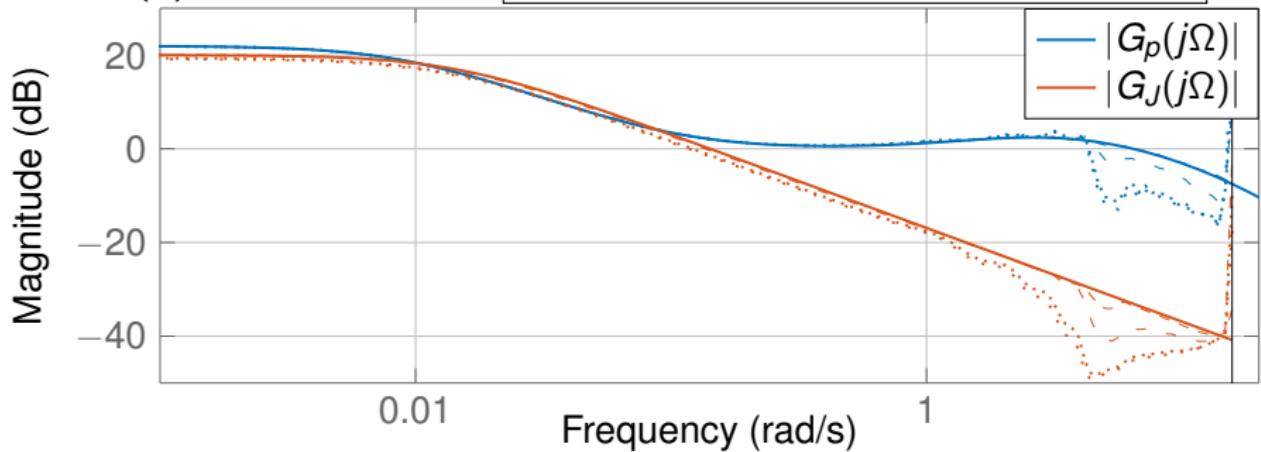
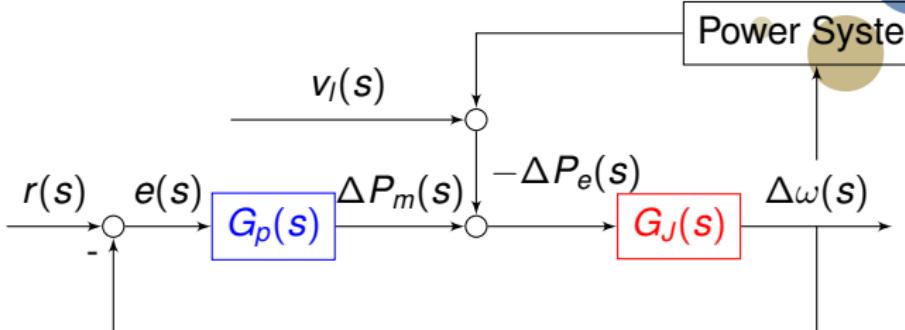
# Identifiability

- The systems can be identified
- However, there is a lack of delay
- This is no problem if the effect of  $v(s)$  in  $\Delta P_e(s)$  is small compared to the effect of  $v_I(s)$ .



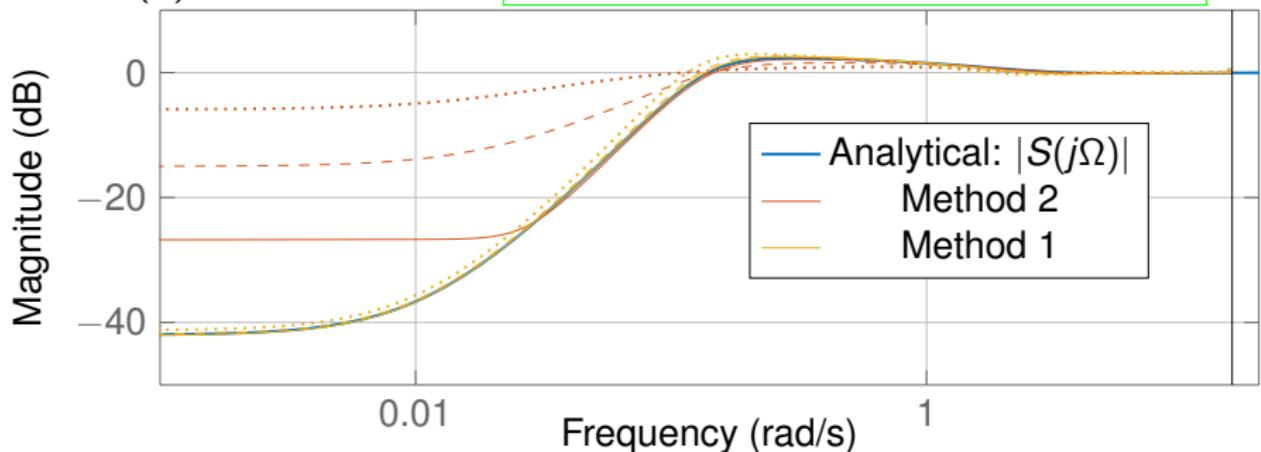
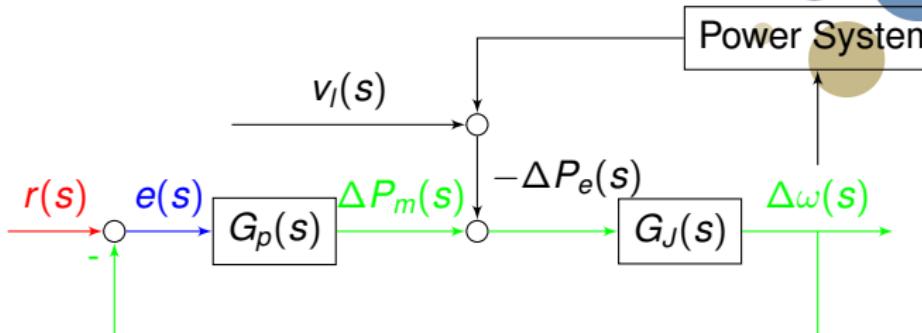
# Identifying $G_p(s)$ and $G_J(s)$ with different $v(s)$ amplitudes

— Mean frequency response from 1000 simulations for each amplitude of  $v(s)$



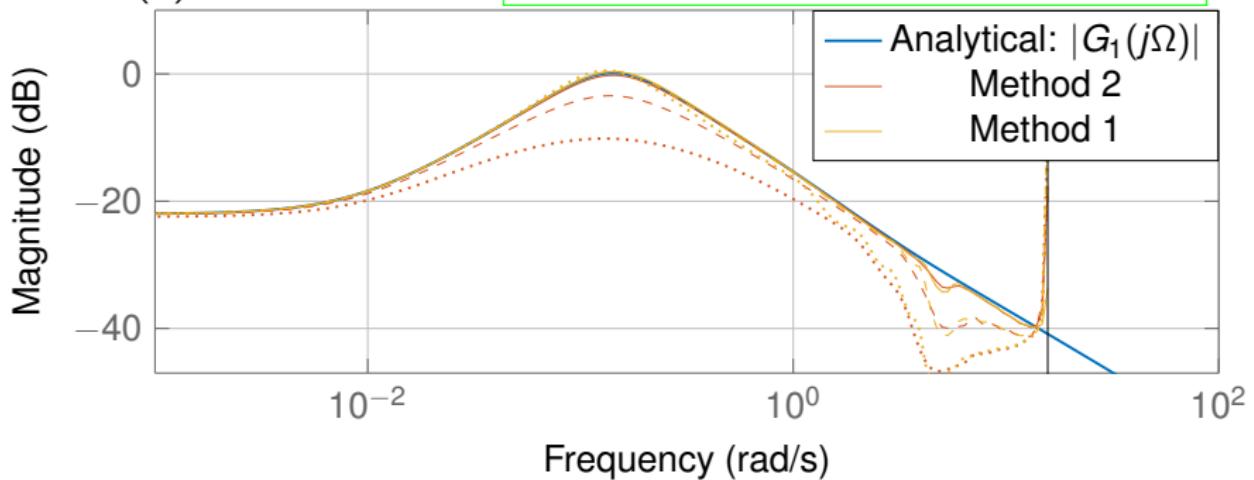
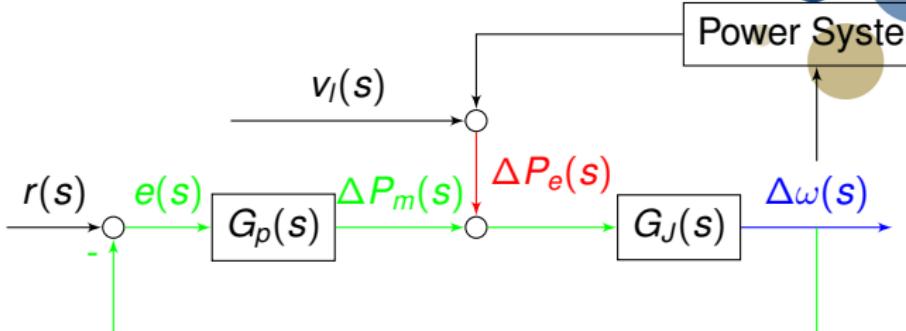
## Identifying $S(s)$ with different $v(s)$ amplitudes

- Mean frequency response from 1000 simulations for each amplitude of  $v(s)$



# Identifying $G_1(s)$ with different $v(s)$ amplitudes

- Mean frequency response from 1000 simulations for each amplitude of  $v(s)$



## Main contributions



- Demonstrated two methods for finding transfer functions for checking the requirements in closed loop.
- The best method for finding the transfer functions is to first identify  $G_p(s)$  and  $G_J(s)$ .
- Analytical validation of the demonstrated methods.
- Discussed the delay condition introduced earlier.

# Outline

Background and research questions

Methodology

Simple test system

Theoretical validation

Tests at Statkraft's power plant

More detailed simulations

The best way to do the identification

Conclusions and further work



# Conclusions



- The requirements can be checked using PMU-measurements, however, the results will be biased for faster dynamics, since we are measuring the frequency instead of the rotational speed of the machine.
- The requirements can be checked using control system measurements in normal operation, however, the results may be biased for faster dynamics, because of the delay condition.
- The requirements can be checked using measurement from normal operation with extra excitation. The added excitation will help on potential bias.

## Further work

- Validate approaches in the lab
- Solve the delay condition.
- Handle backlash.

