mlspline for fnc

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```
## setting
ag2 <- mlsplines::generate_response_smooth(J=50, mod="glm", e_sigma=2, N_s=50)
ag22 <- mlsplines::generate response smooth(J=50, mod="glm", e sigma=2, N s=100)
ag4 <- mlsplines::generate_response_smooth(J=50, mod="glm", e_sigma=4, N_s=50)
ag44 <- mlsplines::generate_response_smooth(J=50, mod="glm", e_sigma=4, N_s=100)
ag8 <- mlsplines::generate_response_smooth(J=50, mod="glm", e_sigma=8, N_s=50)
ag88 <- mlsplines::generate_response_smooth(J=50, mod="glm", e_sigma=8, N_s=100)
al2 <- mlsplines::generate_response_smooth(J=50, mod="lm", e_sigma=2, N_s=50)
al22 <- mlsplines::generate_response_smooth(J=50, mod="lm", e_sigma=2, N_s=100)
al4 <- mlsplines::generate_response_smooth(J=50, mod="lm", e_sigma=4, N_s=50)
al44 <- mlsplines::generate_response_smooth(J=50, mod="lm", e_sigma=4, N_s=100)
al8 <- mlsplines::generate_response_smooth(J=50, mod="lm", e_sigma=8, N_s=50)
al88 <- mlsplines::generate response smooth(J=50, mod="lm", e sigma=8, N s=100)
bg2 <- mlsplines::generate response(J=50, mod="glm", e sigma=2, N s=50)
bg22 <- mlsplines::generate_response(J=50, mod="glm", e_sigma=2, N_s=100)
bg4 <- mlsplines::generate_response(J=50, mod="glm", e_sigma=4, N_s=50)
bg44 <- mlsplines::generate_response(J=50, mod="glm", e_sigma=4, N_s=100)
bg8 <- mlsplines::generate_response(J=50, mod="glm", e_sigma=8, N_s=50)
bg88 <- mlsplines::generate_response(J=50, mod="glm", e_sigma=8, N_s=100)
bl2 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=2, N_s=50)
bl22 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=2, N_s=100)
bl4 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=4, N_s=50)
bl44 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=4, N_s=100)
bl8 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=8, N_s=50)
bl88 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=8, N_s=100)
#lambda
lam1 \leftarrow seq(100, 1000, by=1)
lam2 \leftarrow seq(10, 100, by=0.1)
lam3 \leftarrow seq(1, 10, by=0.01)
lam4 \leftarrow seq(0.1, 1, by=0.001)
lam5 \leftarrow seq(0.01, 0.1, by=0.0001)
lam6 \leftarrow seq(0.001, 0.01, by=0.00001)
lam7 \leftarrow seq(0.0001, 0.001, by=0.000001)
lam8 <- seq(0.00001, 0.0001, by=0.0000001)
lam9 \leftarrow seq(0.000001, 0.00001, by=0.00000001)
lam0 <- seg(0.0000001, 0.000001, by=0.000000001)
lambda <- c(1000, 100, 10, 1, 0.1, 0.01, 0.001, 0.0001, 0.00001, 0.000001)
# Single RMSE (mean of itr=200) ag2
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```
lambda <- c(1000, 100, 10, 1, 0.1, 0.01, 0.001, 0.0001, 0.00001, 0.000001)
lam <- NULL</pre>
RMSE_Single <- NULL
for(j in 1:200){
  GCV vec <- NULL
  al8 <- mlsplines::generate_response_smooth(J=50, mod="lm", e_sigma=8, N_s=50)
  beta hat <- NULL
  for(m in 1:50){
   results <- mlsplines::granular(unlist(al8$x_list[m]), unlist(al8$y[m]), mod = "lm")
    beta_hat <- rbind(beta_hat,results)</pre>
  K <- mlsplines::make_K(al8$z)</pre>
  beta_hat_vec <- unlist(beta_hat[,1])</pre>
  RMSE_Single[j] <- rbind(sqrt((1/50)*t(al8$true_mu- beta_hat_vec))%*%(al8$true_mu- beta_hat_vec)))
  }
smRMSE <- mean(RMSE_Single)</pre>
ssdRMSE <- sd(RMSE_Single)</pre>
# multilevel RMSE (mean of itr=200) al8
lam <- NULL
RMSE Multilevel <- NULL
for(j in 1:200){
  GCV_vec <- NULL
  al8 <- mlsplines::generate_response_smooth(J=50, mod="lm", e_sigma=8, N_s=50)
  beta_hat <- NULL
  for(m in 1:50){
    results <- mlsplines::granular(unlist(al8$x_list[m]), unlist(al8$y[m]), mod = "lm")
    beta_hat <- rbind(beta_hat,results)</pre>
  K <- mlsplines::make_K(al8$z)</pre>
    for(i in 1:length(lambda)){
      EM_out <- mlsplines::main_EM(beta_hat_vec = unlist(beta_hat[,1]), V = diag(unlist(beta_hat[,2])),</pre>
      GCV_vec <- rbind(GCV_vec,EM_out$GCV)</pre>
  lam[j] <- rbind(lambda[which.min(GCV_vec)])</pre>
  EM_out <- mlsplines::main_EM(beta_hat_vec = unlist(beta_hat[,1]), V = diag(unlist(beta_hat[,2])), K =</pre>
  RMSE_Multilevel[j] <- rbind(sqrt((1/50)*t(al8$true_mu-EM_out$mu)%*%(al8$true_mu-EM_out$mu)))
}
mmRMSE <- mean(RMSE_Multilevel)
msdRMSE <- sd(RMSE_Multilevel)</pre>
```

```
# naive RMSE (mean of itr=200) al8
lam <- NULL
RMSE Naive <- NULL
for(j in 1:200){
  GCV_vec <- NULL
  al8 <- mlsplines::generate_response_smooth(J=50, mod="lm", e_sigma=8, N_s=50)
  beta_hat <- NULL
  for(m in 1:50){
    results <- mlsplines::granular(unlist(al8$x_list[m]), unlist(al8$y[m]), mod = "lm")
    beta_hat <- rbind(beta_hat,results)</pre>
  K <- mlsplines::make_K(al8$z)</pre>
    for(i in 1:length(lambda)){
      naive_out <- mlsplines::naive_ss(beta_hat_vec = unlist(beta_hat[,1]), lambda = lambda[i], K = K)</pre>
      GCV_vec <- rbind(GCV_vec,naive_out$GCV)</pre>
    }
  lam[j] <- rbind(lambda[which.min(GCV_vec)])</pre>
  naive_out <- mlsplines::naive_ss(beta_hat_vec = unlist(beta_hat[,1]), K = K, lam[j])</pre>
  RMSE_Naive[j] <- rbind(sqrt((1/50)*t(al8$true_mu-naive_out$mu)%*%(al8$true_mu-naive_out$mu)))
nmRMSE <- mean(RMSE_Naive)
nsdRMSE <- sd(RMSE_Naive)</pre>
result_mean <- cbind(smRMSE, nmRMSE, mmRMSE)</pre>
result_sd <- c(ssdRMSE, nsdRMSE, msdRMSE)</pre>
result1 <- data.frame(c(result_mean),c(result_sd))</pre>
result1
     c.result_mean. c.result_sd.
## 1
          0.9208478 0.11012538
## 2
          0.3929885
                      0.11408158
          0.3626143 0.09472641
## 3
# Single RMSE (mean of itr=200) bl8
lam <- NULL
RMSE_Single <- NULL
for(j in 1:200){
  GCV_vec <- NULL
  bl8 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=8, N_s=50)
  beta_hat <- NULL
  for(m in 1:50){
    results <- mlsplines::granular(unlist(bl8$x_list[m]), unlist(bl8$y[m]), mod = "lm")
    beta_hat <- rbind(beta_hat,results)</pre>
```

```
}
 K <- mlsplines::make_K(bl8$z)</pre>
 beta_hat_vec <- unlist(beta_hat[,1])</pre>
 RMSE_Single[j] <- rbind(sqrt((1/50)*t(bl8$true_mu- beta_hat_vec)),*%(bl8$true_mu - beta_hat_vec)))
}
smRMSE <- mean(RMSE_Single)</pre>
ssdRMSE <- sd(RMSE_Single)</pre>
# multilevel RMSE (mean of itr=200) bl8
lambda \leftarrow c(10000, 1000, 100, 10, 1, 0.1, 0.01, 0.001, 0.0001)
lam <- NULL
RMSE_Multilevel <- NULL
for(j in 1:200){
 GCV_vec <- NULL
 bl8 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=8, N_s=50)
 beta_hat <- NULL
 for(m in 1:50){
   results <- mlsplines::granular(unlist(bl8$x_list[m]), unlist(bl8$y[m]), mod = "lm")
   beta_hat <- rbind(beta_hat,results)</pre>
 K <- mlsplines::make_K(bl8$z)</pre>
 for(i in 1:length(lambda)){
   EM_out <- mlsplines::main_EM(beta_hat_vec = unlist(beta_hat[,1]), V = diag(unlist(beta_hat[,2])), K
   GCV_vec <- rbind(GCV_vec,EM_out$GCV)</pre>
 lam[j] <- rbind(lambda[which.min(GCV_vec)])</pre>
 EM_out <- mlsplines::main_EM(beta_hat_vec = unlist(beta_hat[,1]), V = diag(unlist(beta_hat[,2])), K =</pre>
 RMSE_Multilevel[j] <- rbind(sqrt((1/50)*t(bl8$true_mu-EM_out$mu)%*%(bl8$true_mu-EM_out$mu)))
}
mmRMSE <- mean(RMSE_Multilevel)</pre>
msdRMSE <- sd(RMSE_Multilevel)</pre>
# naive RMSE (mean of itr=200) bl8
lam <- NULL
RMSE_Naive <- NULL
for(j in 1:200){
 GCV_vec <- NULL
 bl8 <- mlsplines::generate_response(J=50, mod="lm", e_sigma=8, N_s=50)
```

```
beta_hat <- NULL
  for(m in 1:50){
    results <- mlsplines::granular(unlist(bl8$x list[m]), unlist(bl8$y[m]), mod = "lm")
    beta_hat <- rbind(beta_hat,results)</pre>
  }
  K <- mlsplines::make_K(bl8$z)</pre>
  for(i in 1:length(lambda)){
    naive_out <- mlsplines::naive_ss(beta_hat_vec = unlist(beta_hat[,1]), K = K, lambda[i])</pre>
    GCV_vec <- rbind(GCV_vec,naive_out$GCV)</pre>
  lam[j] <- rbind(lambda[which.min(GCV_vec)])</pre>
  naive_out <- mlsplines::naive_ss(beta_hat_vec = unlist(beta_hat[,1]), K = K, lam[j])</pre>
  RMSE_Naive[j] <- rbind(sqrt((1/50)*t(bl8$true_mu-naive_out$mu)%*%(bl8$true_mu-naive_out$mu)))
nmRMSE <- mean(RMSE_Naive)</pre>
nsdRMSE <- sd(RMSE_Naive)</pre>
result_mean <- cbind(smRMSE, nmRMSE, mmRMSE)</pre>
result_sd <- c(ssdRMSE, nsdRMSE, msdRMSE)</pre>
result2 <- data.frame(c(result_mean),c(result_sd))</pre>
result2
##
     c.result_mean. c.result_sd.
          0.9268547 0.10248117
## 1
## 2
          0.7519503 0.10809077
## 3
          0.6991136 0.09733331
```