From binomial distribution to Poisson distribution Binomial distribution fck, n,p) = Pr(k; n,p) = Pr(X=k) (n=1 → special case: Bernoulli distribution) = (k pk(1-p)n-k evenly divide I unit time into n pieces
each piece is to a time bin's length Assumptions: O An mont occurs in a time bin independently of events occurring in other time bins. 2) At most one event can occur in one time bin Pr {x=k] = Ch pk(1-p) n-k EX = np = n average number of events that occur in a fixed interval (unit time) P= 7 $P_r\{x=k\} = \binom{k}{n} \binom{n}{n}^k \left(-\frac{n}{n}\right)^{n-k}$ We need to let n-00, then I can be an average rate applicable at any time point. $P_{r}[X=k] = \lim_{n\to\infty} G_{r}^{k}(\frac{1}{n})^{k}(1-\frac{1}{n})^{n-k}$

 $\frac{C_n^k}{n^k} \lambda^k \cdot \left(-\frac{\lambda}{n} \right)^n \cdot \left(-\frac{\lambda}{n} \right)$ $\lim_{n\to\infty}\frac{c_n^k}{n^k}=\frac{n(n-1)\cdots(n-k+1)}{k!\cdot n^k}=$ Pr(X=k) = nke-n Poisson distribution We can define It over any unit time, that is, the unit of it can be per day, per year, or per second Actually, we can rewrite this equation as $\Re[k, n] = \frac{n^k e^{-n}}{k!}$, then we have $Pr\{k, \Pi t\} = \frac{(\Pi t)^k e^{-\Pi t}}{n!}$ This is the probability time t, equivalent to We can easily derive this resetting t as the unit equation by repeating the time. process from binamial distribution to Poisson distribution by setting the unit time as t instead of 1.

The time interval because two consecutive evenes in a Poisson distribution follows the exponential distribution.

Proof:
$$Pr\{0 \text{ events in } (0,X)\} = Pr\{0, \Lambda X\} = e^{-\Lambda X}$$

$$Pr\{\text{or least 1 event in } (0,X)\} = 1 - e^{-\Lambda X}$$

J(y) = the probability density function of Y -> Can be obtained by differentiating the cumulative distribution of Y.

by differentiating the cumulative distribution of 1.

$$f(y) = \frac{d Pr\{Y > y\}}{dy} = \frac{d [1 - Pr\{Y < y\}]}{dy} = \frac{d [1 - Pr\{at last] \text{ event}}{dy}$$

fy1= Re-Ny