186.835 VU Mathematical Programming

Georg Brandstätter¹, Mario Ruthmair²

¹Austrian Institute of Technology, Integrated Energy Systems, georg.brandstaetter@tuwien.ac.at

²University of Klagenfurt, Department of Mathematics, mario.ruthmair@tuwien.ac.at

SS 2021

Overview

Focus on theory and practical aspects of

Mixed Integer Linear Programming (MIP)

You should have:

- ▶ interest in optimization
- ▶ basic knowledge of (integer) linear programming ("Algorithmics")
- programming skills in C++ or Java or whatever
- basic knowledge of graph theory and linear algebra

Aim of Course

- ► Have a broader knowledge in the area of mathematical optimization
- ▶ Be able to model both academic and real world problems as MIPs
- ▶ Be able to theoretically analyze and compare different mathematical programming formulations for a problem
- ► Have knowledge on common methodology for solving MIPs
- ▶ Be able to develop solution algorithms using MIP frameworks
- ▶ Be aware of certain generalizations / extensions

Organization and Modalities

- ► Important: Please register via TISS! (until end of March)
- All course information is available in TUWEL
- Slide-based video lectures, Q&A live sessions
- ► Homework exercises (max. 20 points):
 - ightharpoonup prepare exercises at home (pprox 12 in total)
 - upload solutions in TUWEL
 - get individual feedback from us
 - ▶ teamwork is ok (\leq 2), but let us know (in your document)
 - ok to use references (e.g., articles, books) but cite them!
- ▶ Programming exercises (max. 40 points) → discussed in separate slides/video
- Written online exam (max. 40 points)
- Grading and requirements for positive grade:
 - ► ≥ 30 points for homework and programming exercises
 - \geq 20 points in written exam
 - ▶ 0-49: **5**, 50-62: **4**, 63-75: **3**, 76-88: **2**, 89-100: **1**

Literature

Most parts of this course follow

- L. A. Wolsey, *Integer Programming*, Wiley, 1998
- ▶ M. Jünger et al., editors, 50 Years of Integer Programming 1958-2008, Springer, 2010.

Further literature:

- ► T. L. Magnanti and L. A. Wolsey, Optimal Trees, In M. O. Ball et al., editors, Network Models, Handbooks in Operations Research and Management Science, Vol. 7, Elsevier, 1995
- ▶ D. Bertsimas and R. Weismantel, Optimization over Integers, Dynamic Ideas, 2005
- ► G. Nemhauser and L. A. Wolsey, *Integer and Combinatorial Optimization*, Wiley, 1999.
- ▶ A. Schrijver, *Theory of Linear and Integer Programming*, Wiley, 1986.
- ▶ W. J. Cook, *In Pursuit of the Traveling Salesman: Mathematics at the Limits of Computation*, Princeton University Press, 2011

Further useful resources

- Mathematical Optimization Society, http://mathopt.org
- ► INFORMS Computing Society, Mathematical Programming Glossary, http://glossary.computing.society.informs.org
- ► NEOS Wiki, http://www.neos-guide.org