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PAC learning exercise - homa Baryhamadi 400422042

(P.1) P.1: we have two situation for this hypothesis if we have a positive value that appear in S the answer will be h_+ and if we have negative value the answer will be h_- so according to the rule of ERM this algorithm is an ERM

(P.2) according to PAC learnability we should fix distribution D over \mathcal{X} so if x_+ appear in training data's our algorithm returns a perfect hypothesis. and if $D\{x_+\} < \epsilon \Rightarrow$ in any case we have error of at most ϵ and if $D\{x_+\} > \epsilon \Rightarrow x_+ \notin S$.
so H is PAC learnable & $m_H(\epsilon, S) \leq \left\lceil \frac{\log(1/\delta)}{\epsilon} \right\rceil$

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(3.3) By attention to ERM we should find tightest circle which contain all the positive containing. if h^* be a circle with zero error it has radius by r^* & if we consider \bar{r} as a scalar radius and for $\varepsilon, \delta \in (0, 1)$ we can define $D_{\mathcal{H}}(\{u: \bar{r} \leq |u| \leq r^*\}) = \varepsilon$ and for this distribution we know $L_D(h_S) \geq \varepsilon$

(4.6) we can write by definition:

$$\frac{P_{X \sim D_1}[h(X)=f(X)] + \dots + P_{X \sim D_m}[h(X)=f(X)]}{m} < 1 - \varepsilon$$

and we know $L_S(h)=0$

$$\Rightarrow [L_S(h)=0] = \prod_{i=1}^m P_{X \sim D_i}[h(u)=f(u)]$$

$$= \left(\left(\prod_{i=1}^m P_{X \sim D_i}[h(u)=f(u)] \right)^{\frac{1}{m}} \right)^m$$

$$= \left(\frac{\sum_{i=1}^m P_{X \sim D_i}[h(u)=f(u)]}{m} \right)^m$$

$$< (1 - \varepsilon)^m = e^{-\varepsilon m}$$

(10.4) suppose that H is agnostic PAC learnable and let A be a learning algorithm. show H is PAC learnable using A and also we have D & and we have $\inf L_D(h) = 0$

for every positive integer $m \geq m_H(\epsilon, \delta) \Rightarrow L_D(h) \leq \inf L_D(h') + \epsilon$

$$= 0 + \epsilon$$

$$= \epsilon$$

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(w.r) we know that H_d is the class in \mathbb{R}^d , Since $H_4 \subset H_5$ the error class of H_5 is smaller however the complexity of H_5 is larger so the estimation error be larger if we have limited amount of training example we would prefer to learn the smaller class.