

BiM466 Fuzzy Logic – Homework 1

Simulation of a inverted pendulum system with a fuzzy controller shown by Fig. 1 Pendulum is hold in vertical position and its difference equations for small oscillations is given by:

$$x_1(k+1) = x_1(k) + x_2(k)$$

$$x_2(k+1) = x_1(k) + x_2(k) - u(k)$$

where x_1 is the vertical deviation angle (θ), x_2 is the change of deviation angle at unit time ($\Delta\theta$) and u is the control input (torque). Domains of x_1 , x_2 and u are $[-2^0, 2^0]$, $[-5\text{dps}, 5\text{dps}]$ and $[-24, 24]$ respectively with the membership functions given in fig. 2. The rule base of the fuzzy controller is given in table 1. Complete the table 2 if the fuzzy controller uses Mamdani's **max-product inference engine** and **weighted average of centroids**.

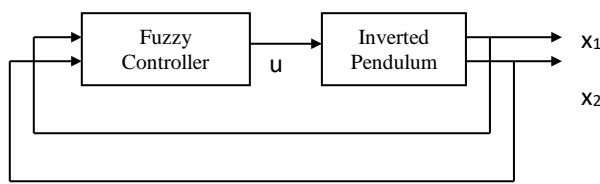


Table 1

	x ₂			
	u	P	Z	N
x ₁	P	PB	P	Z
	Z	P	Z	N
	N	Z	N	NB

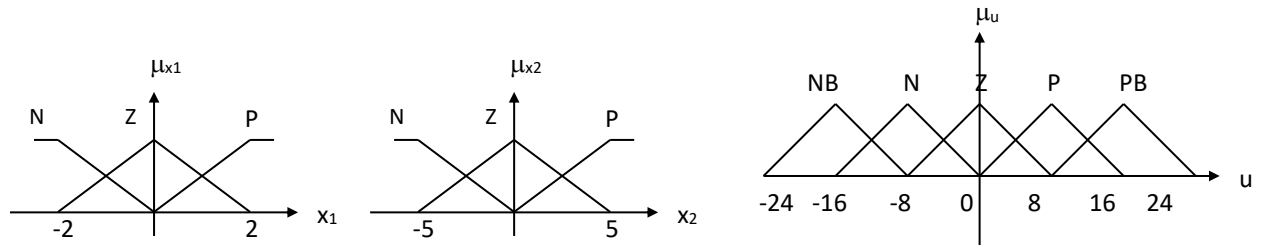


Fig. 2

Table 2

k	$x_1(k)$	$x_2(k)$	$u(k)$
0	1	-4	
1			
2			