Risk Analysis for Bank

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Introduction

In this analysis, we investigated the relationship between the credit score and various other measurements. We use *Train.txt* to build a model and then to predict credit scores based on it. We also classify the individuals from *Test.txt* into two groups and we get the proportion of the individuals which are correctly classified by our model. Prediction intervals are also given.

Exploratory Analysis

This data set is composed of 21 measured data about loan applicants. For each applicant, the credit score has been measured, along with the following 20 variables:

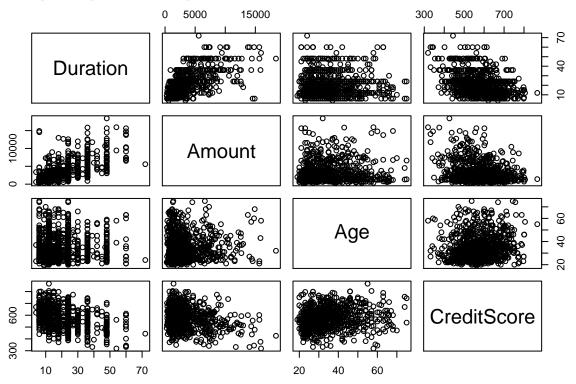
Status, Duration, History, Purpose, Amount, Savings, Employment, Disposable, Personal, OtherParties, Residence, Property, Age, Plans, Housing, Existing, Job, Dependants, Telephone, Foreign, CreditScore.

```
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
  The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
##
## Attaching package: 'car'
  The following object is masked from 'package:dplyr':
##
##
       recode
   'data.frame':
                    800 obs. of 21 variables:
                  : Factor w/ 4 levels "Large", "Negative", ...: 2 4 3 2 3 3 4 4 4 2 ...
##
    $ Status
##
    $ Duration
                  : int 6 48 12 42 36 24 36 30 12 48 ...
                  : Factor w/ 5 levels "A", "B", "C", "D", ...: 5 3 5 3 3 3 5 3 3 ...
##
    $ History
##
   $ Purpose
                  : Factor w/ 10 levels "Business", "Domestic", ...: 8 8 3 4 3 4 10 5 5 1 ...
##
    $ Amount
                         1169 5951 2096 7882 9055 2835 6948 5234 1295 4308 ...
                  : Factor w/ 5 levels "Large", "Low", ...: 4 2 2 2 4 1 2 2 2 2 ...
##
    $ Savings
    $ Employment : Factor w/ 5 levels "Long", "Medium", ...: 5 2 1 1 2 5 2 4 3 3 ...
##
                  : Factor w/ 4 levels "1", "2", "3", "4": 4 2 2 2 2 3 2 4 3 3 ...
##
    $ Disposable
                  : Factor w/ 4 levels "F:DivSepMar",..: 4 1 4 4 4 4 2 1 1 ...
##
    $ Personal
    $ OtherParties: Factor w/ 3 levels "Coapp", "Guarantor",..: 3 3 3 2 3 3 3 3 3 ...
##
                  : Factor w/ 4 levels "1", "2", "3", "4": 4 2 3 4 4 4 2 2 1 4 ...
    $ Residence
                  : Factor w/ 4 levels "Car", "House", ...: 2 2 2 4 3 4 1 1 1 4 ...
    $ Property
```

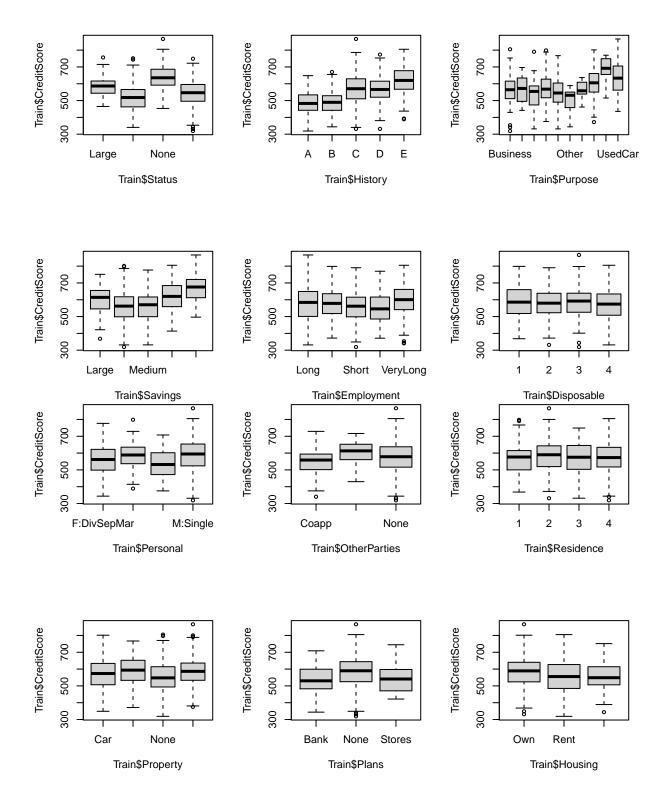
```
: int 67 22 49 45 35 53 35 28 25 24 ...
##
                  : Factor w/ 3 levels "Bank", "None", ...: 2 2 2 2 2 2 2 2 2 2 ...
##
   $ Plans
                  : Factor w/ 3 levels "Own", "Rent", "RentFree": 1 1 1 3 3 1 2 1 2 2 ...
   $ Housing
                  : Factor w/ 4 levels "1","2","3","4": 2 1 1 1 1 1 2 1 1 ...
##
   $ Existing
                  : Factor w/ 4 levels "Management:Self",..: 2 2 4 2 4 2 1 1 2 2 ...
##
                 : Factor w/ 2 levels "1", "2": 1 1 2 2 2 1 1 1 1 1 ...
##
   $ Dependants
                  : Factor w/ 2 levels "No", "Yes": 2 1 1 1 2 1 2 1 1 1 ...
   $ Telephone
                  : Factor w/ 2 levels "No", "Yes": 2 2 2 2 2 2 2 2 2 ...
   $ Foreign
##
   $ CreditScore : num 636 372 678 613 575 ...
```

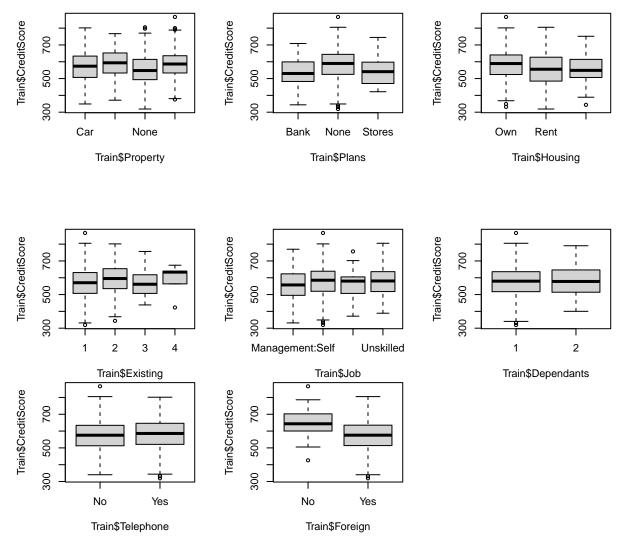
We will only treat Duration, Amount, Age as numerical variables while others will be treated as factors, since other types of variables are either factors or with a very small number of distinct possibilities they can take.

Let's plot the pairwise scatter plots for continuous measurements.



Let's use boxplots for factors:

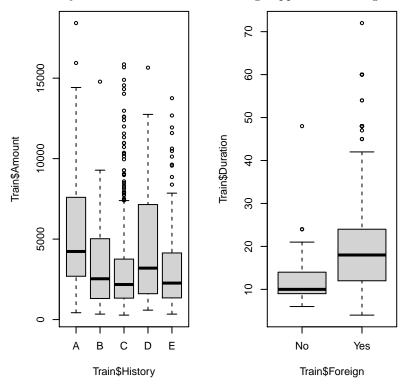




The pariwise scatter plot shows some relationships between each two variables. Focusing on the last row of figures, the associations between CreditScore and all the other variables can be seen. Applicant with higher Duration and Amount seems to have lower CreditScore while applicant with higher Age seems to have higher CreditScore. However, it also is important to note that there exists collinearity between the potential explanatory variables. For instance, applicant with higher Duration tends to have higher Amount, which shows that there seems to be a strong positive association between Duration and Amount. Therefore, it could be the fact that only one or two of these variables are required to explain differences in CreditScore. We can also see that data tend to cluster, especially for Amount and Age and we see a couple of extreme Amount points, which distorts the graph and make the general trend between Amount and other variables harder to determine from the plots. Taking log(Amount) might drastically reduces this effect.

From the boxplots, we can see that applicant with Status (None) or History (E) or Purpose (UsedCar) or Savings (VeryLarge), Employment (VeryLong) or Disposable (3) or Personal (Single) or OtherParties (Guarantor) or Residence (2) or Property (House), Plans (None) or Housing (Own) or Existing (2) or Job (Skilled) or Dependants (1) or Telephone (Yes) or Foreign (No) tends to have higher a CreditScore. However, it seems that some factors like Employment, Disposable, Residence, Existing, Job, Dependants and Telephone do not have a significant affect on the CreditScore so the differences are very small. Moreover, there still exists correlations between these factors and continuous variables. For instance, applicant with worse previous history seems to have higher credit score, which could be explained by the correlation between History and

Amount, i.e. applicant with bad previous loan history can not get much loan since banks are reluctant to lend money to him. We also see that foreign applicant has longer duration of requested loan.



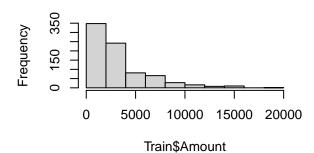
Notice that this is just based on our eyeball so it is not persuasive. We need to use quantitative methods to find an appropriate model.

Let's also check the distribution for continuous variables.

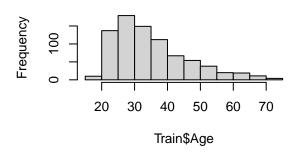
Histogram of Train\$Duration

Lednency 0 20 40 60 Train\$Duration

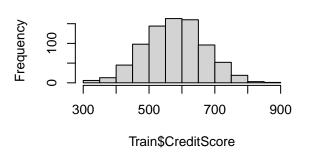
Histogram of Train\$Amount



Histogram of Train\$Age



Histogram of Train\$CreditScore



Interpretation:

From the histogram, besides the good distribution of CreditScore, the Duration, Amount and Age are all positively skewed. In order to rectify the skewness, we apply log transformation for them by Mosteller and Tukey's bulging rule.

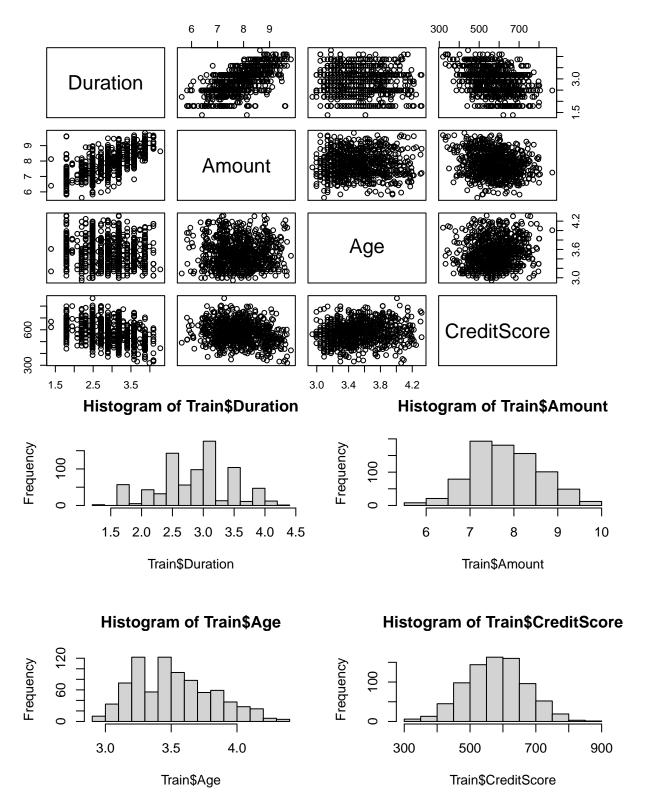
 $Duration \rightarrow log(Duration)$

 $Amount \rightarrow log(Amount)$

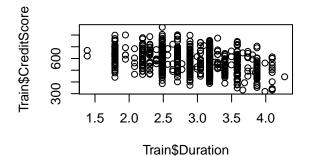
 $Age \rightarrow log(Age)$

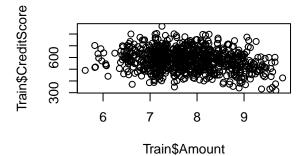
(Please note that the data we use later has already been transformed as above, which will not be shown in the summary output).

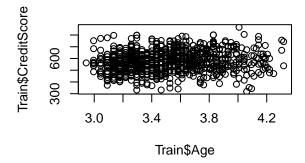
Then we plot to have a look again for our transformed data.



We could see that the positive skewness has been improved by transformation.







From the plot, we can see the general associations:

- negative association between log(Duration) and CreditScore
- negative association between log(Amount) and CreditScore
- positive association between log(Age) and CreditScore

We also see that there might exist unusual points which might provide us more information after we remove them.

Model fitting

We start by fitting the model with all possible explanatory variables included, called *full model*.

```
##
## Call:
## lm(formula = CreditScore ~ ., data = Train)
##
## Residuals:
##
        Min
                  1Q
                                     3Q
                                              Max
                        Median
                                         156.872
## -142.578 -31.468
                        -2.637
                                 32.134
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          778.1479
                                      42.5276
                                                18.297
                                                        < 2e-16 ***
                          -50.4976
## StatusNegative
                                                -6.089 1.82e-09 ***
                                       8.2933
## StatusNone
                           38.5923
                                       8.0445
                                                 4.797 1.94e-06 ***
## StatusSmall
                          -30.6308
                                       8.3314
                                                -3.677 0.000253 ***
## Duration
                          -29.7928
                                       4.6792
                                                -6.367 3.37e-10 ***
## HistoryB
                            2.3532
                                      12.7499
                                                 0.185 0.853618
## HistoryC
                           50.3760
                                       9.9269
                                                 5.075 4.91e-07 ***
```

```
## HistoryD
                           50.5315
                                      10.9453
                                                 4.617 4.59e-06 ***
## HistoryE
                           84.1745
                                       9.9568
                                                 8.454 < 2e-16 ***
## PurposeDomestic
                          -23.4216
                                       17.3277
                                                -1.352 0.176887
                                      10.3391
                                                -5.399 9.04e-08 ***
## PurposeEducation
                          -55.8165
## PurposeFurniture
                           -1.9622
                                       7.5213
                                                -0.261 0.794256
## PurposeNewCar
                          -46.8229
                                       7.1297
                                                -6.567 9.61e-11 ***
## PurposeOther
                          -18.9078
                                      17.1478
                                                -1.103 0.270541
## PurposeRepairs
                          -24.1195
                                      13.6494
                                                -1.767 0.077625 .
  PurposeTelevision
                            1.3915
                                       7.0057
                                                 0.199 0.842610
  PurposeTraining
                           54.9928
                                      22.1630
                                                 2.481 0.013310 *
## PurposeUsedCar
                           36.1735
                                        8.3833
                                                 4.315 1.81e-05 ***
## Amount
                          -23.1024
                                        3.9035
                                                -5.918 4.96e-09 ***
## SavingsLow
                          -11.9734
                                       7.9806
                                                -1.500 0.133955
                            0.2690
## SavingsMedium
                                       9.4066
                                                 0.029 0.977196
## SavingsUnknown
                           26.5590
                                       8.7046
                                                 3.051 0.002361 **
## SavingsVeryLarge
                           64.8429
                                      11.5184
                                                 5.629 2.56e-08 ***
## EmploymentMedium
                                       5.6086
                                                 0.542 0.588226
                            3.0379
## EmploymentShort
                                        6.3078
                                                 0.462 0.643978
                            2.9163
## EmploymentUnemployed
                           -5.7077
                                       9.6405
                                                -0.592 0.553994
## EmploymentVeryLong
                            7.2925
                                       6.2017
                                                 1.176 0.240012
## Disposable2
                          -12.6185
                                       6.6312
                                                -1.903 0.057437
## Disposable3
                          -26.6862
                                       7.0979
                                                -3.760 0.000183 ***
## Disposable4
                          -42.4973
                                       6.8905
                                                -6.167 1.14e-09 ***
## PersonalF:Single
                            9.0694
                                        6.9040
                                                 1.314 0.189372
                                                -1.569 0.117087
## PersonalM:DivSepMar
                          -13.8073
                                       8.8004
## PersonalM:Single
                           30.5786
                                        4.5496
                                                 6.721 3.59e-11 ***
## OtherPartiesGuarantor
                           62.8929
                                      12.4525
                                                 5.051 5.54e-07
## OtherPartiesNone
                           10.7948
                                        9.0777
                                                 1.189 0.234759
## Residence2
                          -11.5905
                                        6.1735
                                                -1.877 0.060844
                                                -1.230 0.218967
## Residence3
                                       7.0604
                           -8.6865
## Residence4
                           -9.0506
                                        6.2039
                                                -1.459 0.145029
## PropertyHouse
                          -10.6165
                                        5.0724
                                                -2.093 0.036688 *
## PropertyNone
                           -7.0200
                                        8.4944
                                                -0.826 0.408830
                            0.9823
                                        4.9688
                                                 0.198 0.843334
## PropertySavings
                                                 2.127 0.033750 *
                                       7.4336
## Age
                           15.8112
## PlansNone
                           33.1283
                                       5.2681
                                                 6.288 5.46e-10 ***
## PlansStores
                           13.2831
                                       9.7897
                                                 1.357 0.175242
## HousingRent
                                                -3.042 0.002435 **
                          -15.6789
                                       5.1547
## HousingRentFree
                                                 0.251 0.802016
                            2.4301
                                        9.6885
## Existing2
                                       4.9211
                                                 0.142 0.887422
                            0.6969
## Existing3
                          -11.6177
                                      12.2024
                                                -0.952 0.341363
## Existing4
                                                -0.382 0.702895
                           -8.7326
                                      22.8863
## JobSkilled
                            1.9408
                                       6.0955
                                                 0.318 0.750265
  JobUnemployed
                            6.1215
                                      14.7725
                                                 0.414 0.678709
## JobUnskilled
                            6.4099
                                       7.5020
                                                 0.854 0.393142
                                                -0.441 0.659428
## Dependants2
                           -2.3503
                                        5.3310
## TelephoneYes
                           13.6043
                                        4.1563
                                                 3.273 0.001113 **
## ForeignYes
                          -55.3346
                                        9.7670
                                                -5.665 2.10e-08 ***
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 49.49 on 745 degrees of freedom
## Multiple R-squared: 0.7233, Adjusted R-squared: 0.7033
## F-statistic: 36.07 on 54 and 745 DF, p-value: < 2.2e-16
```

```
## [1] "fit_full$adj.r.squared = 0.703252"
```

We see from the summary output that the $R_{adj}^2 = 0.703252$ suggests a relatively good fit.

Such small p-values for Status tell us to reject H_0 , which is an evidence that it has strong association with CreditScore. This could also been seen apparently from previous exploratory plots. As well as for History, applicant with History (C) or History (D) or History (E) tends to have a much higher credit score than History (A).

For continuous variables, Duration and Amount are strongly associated with CreditScore by their p-values < 0.001 while Age also has a very small p-value = 0.03375 < 0.05, so we reject H_0 at 5% level. From the exploratory plots, applicant with longer Duration or larger Amount has lower CreditScore, while applicant with higher Age has a higher CreditScore.

However, variables such as Employment, Residence, Existing, Job and Dependants have p-values greater than 0.1, which are not significant at the 10% level after accounting for other factors. So there is no evidence that these variables are associated with CreditScore. The p-values for Residence2 and PurposeRepairs are greater than 0.05 but less than 0.1, which could be considered as mildly significant. From the exploratory plots, we see that applicant with 2 years in current residence have a higher credit score than others in full years residence while applicant with purpose of Repairs have a higher credit score than other purposes.

The full model is not an ideal model since least significant variables are also included and it is too complex, which might cause over-fit and affect the accuracy for prediction. So the next step is to see which variables should be retained in order to find the most important predictors.

Model selection

Due to a large number of variables, best subsets regression is not a good choice since there will be 2^{20} models to be fitted. Therefore, we try using the stepwise regression to optimize our variables selection in our model by using the AIC as the criterion.

Stepwise regression

Let's fit the full model and use the backward stepwise regression.

```
## Start: AIC=6295.92
  CreditScore ~ Status + Duration + History + Purpose + Amount +
##
       Savings + Employment + Disposable + Personal + OtherParties +
##
       Residence + Property + Age + Plans + Housing + Existing +
       Job + Dependants + Telephone + Foreign
##
##
##
                  Df Sum of Sq
                                    RSS
                                           AIC
                   4
                           6721 1831580 6290.9
## - Employment
## - Job
                   3
                           2609 1827468 6291.1
## - Existing
                   3
                           2921 1827780 6291.2
## - Residence
                   3
                           8754 1833613 6293.7
## - Dependants
                            476 1825335 6294.1
                   1
## <none>
                                1824859 6295.9
## - Property
                   3
                          15268 1840128 6296.6
## - Age
                         11082 1835941 6298.8
                   1
## - Housing
                   2
                         24818 1849677 6302.7
## - Telephone
                   1
                         26243 1851102 6305.3
## - Foreign
                   1
                         78622 1903481 6327.7
## - OtherParties
                   2
                         85881 1910741 6328.7
## - Amount
                         85797 1910656 6330.7
                   1
```

```
## - Plans
                        101747 1926606 6335.3
## - Duration
                        99299 1924158 6336.3
                   1
## - Disposable
                   3
                        126664 1951523 6343.6
## - Personal
                   3
                        145829 1970689 6351.4
## - Savings
                   4
                        281432 2106291 6402.7
## - History
                   4
                        296658 2121518 6408.4
## - Purpose
                   9
                        526935 2351794 6480.9
## - Status
                        988780 2813639 6636.3
                   3
##
## Step: AIC=6290.86
  CreditScore ~ Status + Duration + History + Purpose + Amount +
       Savings + Disposable + Personal + OtherParties + Residence +
##
       Property + Age + Plans + Housing + Existing + Job + Dependants +
##
##
       Telephone + Foreign
##
##
                  Df Sum of Sq
                                   RSS
                                          AIC
                   3
                          2676 1834256 6286.0
## - Existing
## - Job
                   3
                          3327 1834907 6286.3
## - Residence
                          9103 1840683 6288.8
                   3
## - Dependants
                           351 1831931 6289.0
## <none>
                               1831580 6290.9
## - Property
                   3
                         14669 1846249 6291.2
## - Age
                         15893 1847473 6295.8
                   1
## - Housing
                   2
                         24291 1855871 6297.4
## - Telephone
                   1
                         26006 1857586 6300.1
## - Foreign
                   1
                        78974 1910555 6322.6
## - OtherParties
                   2
                        85705 1917285 6323.4
## - Amount
                   1
                        88030 1919610 6326.4
## - Plans
                   2
                       100146 1931726 6329.5
## - Duration
                   1
                       98149 1929729 6330.6
## - Disposable
                   3
                        125143 1956723 6337.7
## - Personal
                   3
                        152284 1983865 6348.8
## - Savings
                   4
                        290564 2122144 6400.7
                   4
                        301439 2133019 6404.7
## - History
## - Purpose
                   9
                        530002 2361582 6476.2
## - Status
                   3
                       1000070 2831650 6633.4
##
## Step: AIC=6286.03
## CreditScore ~ Status + Duration + History + Purpose + Amount +
       Savings + Disposable + Personal + OtherParties + Residence +
##
##
       Property + Age + Plans + Housing + Job + Dependants + Telephone +
##
       Foreign
##
##
                  Df Sum of Sq
                                          AIC
                                   RSS
## - Job
                   3
                          3915 1838172 6281.7
## - Residence
                   3
                          9102 1843359 6284.0
## - Dependants
                   1
                           422 1834678 6284.2
## <none>
                               1834256 6286.0
## - Property
                   3
                         15287 1849544 6286.7
## - Age
                   1
                         15183 1849439 6290.6
## - Housing
                   2
                         24230 1858486 6292.5
## - Telephone
                   1
                        25083 1859339 6294.9
## - Foreign
                       78633 1912890 6317.6
                   1
## - OtherParties 2
                        85356 1919612 6318.4
```

```
89471 1923727 6322.1
## - Amount
                  1
## - Duration
                        97300 1931556 6325.4
                  1
## - Plans
                  2
                        104800 1939056 6326.5
## - Disposable
                  3
                       123624 1957881 6332.2
## - Personal
                  3
                        150738 1984994 6343.2
## - Savings
                   4
                        292897 2127153 6396.5
## - History
                        340631 2174887 6414.3
## - Purpose
                        529892 2364149 6471.1
                   9
## - Status
                       1008684 2842940 6630.6
##
## Step: AIC=6281.74
## CreditScore ~ Status + Duration + History + Purpose + Amount +
       Savings + Disposable + Personal + OtherParties + Residence +
##
       Property + Age + Plans + Housing + Dependants + Telephone +
##
       Foreign
##
##
                  Df Sum of Sq
                                   RSS
                                          AIC
## - Residence
                         8632 1846803 6279.5
## - Dependants
                          169 1838340 6279.8
                   1
## - Property
                   3
                         13745 1851917 6281.7
## <none>
                               1838172 6281.7
## - Age
                         15465 1853636 6286.4
                       24777 1862948 6288.4
## - Housing
                  2
## - Telephone
                         22655 1860827 6289.5
                   1
                         80681 1918853 6314.1
## - Foreign
                   1
## - OtherParties 2
                         88444 1926616 6315.3
## - Duration
                        96615 1934787 6320.7
                   1
## - Amount
                        98442 1936613 6321.5
                   1
## - Plans
                   2
                      103740 1941912 6321.7
                  3 132072 1970243 6331.2
## - Disposable
## - Personal
                  3
                       151437 1989608 6339.1
## - Savings
                   4
                        295645 2133816 6393.0
## - History
                   4
                        343312 2181483 6410.7
                   9
                        534110 2372281 6467.8
## - Purpose
## - Status
                   3
                       1014374 2852546 6627.3
##
## Step: AIC=6279.48
## CreditScore ~ Status + Duration + History + Purpose + Amount +
##
       Savings + Disposable + Personal + OtherParties + Property +
##
       Age + Plans + Housing + Dependants + Telephone + Foreign
##
                  Df Sum of Sq
##
                                   RSS
                                          ATC
## - Dependants
                   1
                           252 1847056 6277.6
## - Property
                   3
                         12030 1858833 6278.7
                               1846803 6279.5
## <none>
## - Age
                         15658 1862461 6284.2
                   1
## - Housing
                   2
                         27489 1874293 6287.3
## - Telephone
                   1
                         23036 1869839 6287.4
## - Foreign
                   1
                        79864 1926667 6311.4
## - OtherParties
                  2
                         84991 1931794 6311.5
## - Duration
                        95945 1942748 6318.0
                   1
## - Plans
                   2
                      102742 1949545 6318.8
## - Amount
                   1 102240 1949043 6320.6
                       133672 1980475 6329.4
## - Disposable
                  3
```

```
## - Personal
                   3
                        148334 1995138 6335.3
## - Savings
                   4
                        291778 2138582 6388.8
## - History
                        339799 2186602 6406.6
                   4
## - Purpose
                   9
                        539302 2386106 6466.4
## - Status
                   3
                       1019646 2866449 6625.2
##
## Step: AIC=6277.59
  CreditScore ~ Status + Duration + History + Purpose + Amount +
##
       Savings + Disposable + Personal + OtherParties + Property +
##
       Age + Plans + Housing + Telephone + Foreign
##
##
                  Df Sum of Sq
                                    RSS
## - Property
                         12294 1859350 6276.9
## <none>
                                1847056 6277.6
                         15533 1862588 6282.3
## - Age
                   1
## - Housing
                   2
                         27512 1874567 6285.4
## - Telephone
                         23210 1870266 6285.6
                   1
## - Foreign
                         79678 1926733 6309.4
                   1
## - OtherParties
                         84821 1931877 6309.5
                   2
## - Duration
                   1
                         95756 1942811 6316.0
## - Plans
                   2
                        103372 1950428 6317.2
## - Amount
                        102221 1949277 6318.7
                   1
## - Disposable
                   3
                        133442 1980497 6327.4
## - Personal
                   3
                        154229 2001285 6335.8
## - Savings
                   4
                        291634 2138690 6386.9
## - History
                   4
                         341249 2188304 6405.2
## - Purpose
                   9
                        543096 2390152 6465.8
                   3
## - Status
                       1019402 2866457 6623.2
##
## Step: AIC=6276.9
  CreditScore ~ Status + Duration + History + Purpose + Amount +
##
       Savings + Disposable + Personal + OtherParties + Age + Plans +
##
       Housing + Telephone + Foreign
##
##
                  Df Sum of Sq
                                    RSS
                                           AIC
## <none>
                                1859350 6276.9
## - Age
                          14215 1873565 6281.0
## - Housing
                   2
                         29256 1888606 6285.4
## - Telephone
                         25915 1885265 6286.0
                   1
## - OtherParties
                   2
                         81759 1941109 6307.3
## - Foreign
                   1
                         77593 1936943 6307.6
## - Duration
                         92007 1951357 6313.5
                   1
## - Plans
                   2
                        100841 1960191 6315.2
## - Amount
                        100075 1959425 6316.8
                   1
## - Disposable
                   3
                        132982 1992331 6326.2
## - Personal
                   3
                        156712 2016062 6335.6
## - Savings
                   4
                        291121 2150471 6385.3
## - History
                   4
                         342290 2201640 6404.1
## - Purpose
                   9
                        552050 2411400 6466.9
## - Status
                   3
                       1018039 2877389 6620.2
```

The AIC value is 6295.92 for full model, after backward stepwise regression, the AIC has been reduced to 6276.9 and the current model is the relatively optimized model and let's check its summary output.

```
##
## Call:
  lm(formula = CreditScore ~ Status + Duration + History + Purpose +
##
       Amount + Savings + Disposable + Personal + OtherParties +
##
       Age + Plans + Housing + Telephone + Foreign, data = Train)
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                        Max
  -139.51 -31.67
                      -2.61
                              32.64
                                     161.55
##
   Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
                          773.15372
                                      39.30008
                                                19.673 < 2e-16 ***
##
   (Intercept)
  StatusNegative
                          -50.87728
                                       8.13959
                                                 -6.251 6.80e-10 ***
## StatusNone
                           37.58202
                                       7.92566
                                                  4.742 2.53e-06 ***
## StatusSmall
                          -31.32648
                                       8.24029
                                                 -3.802 0.000155 ***
## Duration
                                       4.57978
                                                 -6.141 1.32e-09 ***
                          -28.12235
## HistoryB
                           -0.84901
                                      12.38169
                                                 -0.069 0.945350
## HistoryC
                           48.63893
                                       9.46070
                                                  5.141 3.47e-07 ***
## HistoryD
                           49.07111
                                      10.79740
                                                  4.545 6.40e-06 ***
## HistoryE
                           82.21082
                                       9.79985
                                                  8.389 2.37e-16 ***
## PurposeDomestic
                          -24.81449
                                      17.11427
                                                 -1.450 0.147490
                                                 -5.215 2.37e-07 ***
## PurposeEducation
                          -52.96452
                                      10.15649
## PurposeFurniture
                            0.15346
                                       7.37124
                                                  0.021 0.983395
## PurposeNewCar
                          -46.23655
                                       7.04418
                                                -6.564 9.69e-11 ***
## PurposeOther
                          -19.87584
                                      16.57907
                                                 -1.199 0.230958
## PurposeRepairs
                                                -1.905 0.057123
                          -25.63507
                                      13.45493
## PurposeTelevision
                            2.30334
                                       6.93365
                                                  0.332 0.739832
## PurposeTraining
                           59.37339
                                      21.67226
                                                  2.740 0.006295 **
## PurposeUsedCar
                                       8.21757
                                                  4.612 4.67e-06 ***
                           37.90101
## Amount
                          -23.88738
                                       3.73000
                                                 -6.404 2.64e-10 ***
## SavingsLow
                          -13.14080
                                       7.86423
                                                 -1.671 0.095140 .
## SavingsMedium
                            0.06139
                                       9.28806
                                                  0.007 0.994728
## SavingsUnknown
                           25.83608
                                       8.59536
                                                  3.006 0.002736 **
## SavingsVeryLarge
                                      11.29406
                                                  5.531 4.37e-08 ***
                           62.47214
## Disposable2
                          -11.97283
                                       6.48331
                                                -1.847 0.065176
## Disposable3
                          -26.72090
                                       6.94964
                                                 -3.845 0.000131 ***
## Disposable4
                                                 -6.286 5.48e-10 ***
                          -41.89259
                                       6.66438
## PersonalF:Single
                                       6.75865
                                                  1.175 0.240303
                            7.94241
## PersonalM:DivSepMar
                          -13.30743
                                       8.70654
                                                -1.528 0.126818
## PersonalM:Single
                           30.06153
                                       4.33588
                                                  6.933 8.78e-12 ***
## OtherPartiesGuarantor
                                                  5.028 6.17e-07 ***
                           61.12648
                                      12.15645
## OtherPartiesNone
                           11.94918
                                       8.90652
                                                  1.342 0.180118
## Age
                           16.27202
                                       6.74177
                                                  2.414 0.016030 *
## PlansNone
                           32.27987
                                       5.16452
                                                  6.250 6.81e-10 ***
## PlansStores
                           11.89419
                                       9.68139
                                                  1.229 0.219615
## HousingRent
                          -16.91325
                                       4.89081
                                                 -3.458 0.000574 ***
## HousingRentFree
                           -3.76808
                                       6.15605
                                                 -0.612 0.540658
## TelephoneYes
                           12.64238
                                       3.87933
                                                  3.259 0.001168 **
## ForeignYes
                          -54.42600
                                       9.65159
                                                 -5.639 2.41e-08 ***
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 49.4 on 762 degrees of freedom
```

```
## Multiple R-squared: 0.7181, Adjusted R-squared: 0.7044
## F-statistic: 52.46 on 37 and 762 DF, p-value: < 2.2e-16</pre>
```

The result tells us that we could use the model:

 $CreditScore \sim Status + log(Duration) + History + Purpose + log(Amount) + Savings + Disposable + Personal + Other Parties + log(Age) + Plans + Housing + Telephone + Foreign. \ Let's call it \textit{fit1}.$

[1] "fit1\$adj.r.squared = 0.704389"

And the corresponding coefficients of this model are:

| ## | (Intercept) | StatusNegative | StatusNone |
|----|--------------------------|--------------------------|-------------------------------|
| ## | 773.15371693 | -50.87727687 | 37.58202440 |
| ## | StatusSmall | Duration | HistoryB |
| ## | -31.32648063 | -28.12234742 | -0.84900773 |
| ## | HistoryC | HistoryD | HistoryE |
| ## | 48.63892583 | 49.07110935 | 82.21081593 |
| ## | PurposeDomestic | PurposeEducation | PurposeFurniture |
| ## | -24.81448928 | -52.96452379 | 0.15346238 |
| ## | PurposeNewCar | PurposeOther | PurposeRepairs |
| ## | -46.23655326 | -19.87584346 | -25.63507120 |
| ## | PurposeTelevision | PurposeTraining | ${\tt PurposeUsedCar}$ |
| ## | 2.30333989 | 59.37338536 | 37.90101249 |
| ## | Amount | SavingsLow | ${\tt SavingsMedium}$ |
| ## | -23.88737916 | -13.14079907 | 0.06138926 |
| ## | SavingsUnknown | ${\tt SavingsVeryLarge}$ | Disposable2 |
| ## | 25.83607730 | 62.47214238 | -11.97282733 |
| ## | Disposable3 | Disposable4 | PersonalF:Single |
| ## | -26.72090375 | -41.89259098 | 7.94241256 |
| ## | PersonalM:DivSepMar | PersonalM:Single | ${\tt OtherPartiesGuarantor}$ |
| ## | -13.30742764 | 30.06152846 | 61.12647839 |
| ## | ${\tt OtherPartiesNone}$ | Age | PlansNone |
| ## | 11.94917690 | 16.27202187 | 32.27987009 |
| ## | PlansStores | HousingRent | ${\tt HousingRentFree}$ |
| ## | 11.89419015 | -16.91325132 | -3.76808462 |
| ## | TelephoneYes | ForeignYes | |
| ## | 12.64238486 | -54.42600184 | |

We find that the least significant variables such as Employment, Residence, Existing, Job and Dependants have been removed from the full model.

We see that continuous variables log(Duration), log(Amount) are significant at 5% level while log(Age) is significant at 10% level. Considering the exploratory plots, for Duration and Amount, there is a strong negative association between CreditScore and them while for Age, mild positive association is seen.

We also see the strong association between Status, History, Purpose, Savings, Disposable, Personal, OtherParties, Plans, Housing, Telephone, Foreign and CreditScore. Notice that this is not simultaneous interpretation, every variables is interpreted after accounting for others. Considering previous exploratory plots, we see that applicant with Status (None) or History (E) or Purpose (Training) or Savings (Verylarge) or Disposable (3) or Personal (Single), OtherParties (Guarantor) or Plans (None) or Housing (Own) or Telephone (Yes) or Foreign (Yes) has a higher CreditScore.

Note that the $R_{adj}^2 = 0.704389$ still suggests a good fit, which has been increased from $R_{adj}^2 = 0.703252$ of full model.

Moreover, it is worthwhile to note that the model is not guaranteed to be the best model since not every possible model is evaluated.

Let's fit the null model and use backward stepwise regression.

```
## Start: AIC=7215.8
## CreditScore ~ 1
##
##
                  Df Sum of Sq
                                   RSS
                                          AIC
## + Status
                   3
                       2200712 4394551 6897.0
## + History
                       1022360 5572903 7089.1
## + Duration
                   1
                       753652 5841611 7120.7
## + Savings
                   4
                        727667 5867596 7130.3
## + Purpose
                   9
                        778272 5816991 7133.3
## + Amount
                   1
                        296237 6299026 7181.0
## + Plans
                   2
                        279726 6315537 7185.1
## + Personal
                  3
                        214591 6380672 7195.3
## + Foreign
                        132694 6462569 7201.5
                   1
## + Housing
                   2
                        147124 6448139 7201.8
## + Employment
                        177175 6418088 7202.0
                   4
## + Age
                   1
                        114494 6480769 7203.8
## + Property
                   3
                        118914 6476349 7207.2
## + Existing
                   3
                        114313 6480950 7207.8
## + OtherParties 2
                         50477 6544786 7213.7
## <none>
                               6595263 7215.8
## + Job
                   3
                         47843 6547420 7216.0
## + Telephone
                   1
                         13145 6582118 7216.2
## + Disposable
                   3
                         40413 6554850 7216.9
## + Dependants
                   1
                          6029 6589234 7217.1
## + Residence
                         21928 6573335 7219.1
##
## Step: AIC=6897.01
## CreditScore ~ Status
##
##
                                   RSS
                                          AIC
                  Df Sum of Sq
## + Duration
                   1
                        626765 3767786 6775.9
## + History
                   4
                        557015 3837536 6796.6
## + Purpose
                   9
                        433981 3960570 6831.8
## + Savings
                   4
                        353882 4040669 6837.8
## + Amount
                   1
                        259565 4134986 6850.3
## + Plans
                   2
                        198835 4195716 6864.0
## + Foreign
                        146638 4247914 6871.9
                   1
## + Personal
                   3
                        138797 4255754 6877.3
## + OtherParties
                  2
                         88580 4305972 6884.7
## + Property
                   3
                         98303 4296249 6884.9
## + Age
                         72840 4321711 6885.6
                   1
## + Housing
                   2
                         56558 4337993 6890.6
## + Employment
                   4
                         64969 4329583 6893.1
## + Disposable
                   3
                         48487 4346064 6894.1
## + Existing
                   3
                         41800 4352752 6895.4
## + Job
                   3
                         35434 4359118 6896.5
## <none>
                               4394551 6897.0
## + Dependants
                          4168 4390384 6898.3
## + Telephone
                   1
                         1304 4393247 6898.8
## + Residence
                   3
                         11233 4383319 6901.0
```

```
##
## Step: AIC=6775.91
## CreditScore ~ Status + Duration
##
                 Df Sum of Sq
                                  RSS
## + Purpose
                       537367 3230419 6670.8
## + History
                       438103 3329683 6685.0
                  4
## + Savings
                       374012 3393774 6700.3
## + Personal
                  3
                      187698 3580088 6741.0
## + Plans
                  2 153705 3614081 6746.6
                  4 96931 3670856 6763.1
## + Employment
                     67601 3700185 6763.4
61188 3706599 6764.8
## + Foreign
                  1
## + Age
                  1
## + Housing
                  2
                    62149 3705638 6766.6
                     59418 3708368 6767.2
## + OtherParties
                  2
                     54167 3713619 6770.3
## + Existing
                  3
## + Telephone
                        30809 3736977 6771.3
                  1
## <none>
                              3767786 6775.9
## + Property
                  3
                        24770 3743016 6776.6
## + Disposable
                  3
                        23557 3744230 6776.9
## + Dependants
                  1
                        1534 3766252 6777.6
## + Amount
                  1
                           88 3767698 6777.9
## + Job
                  3
                       10639 3757148 6779.6
## + Residence
                        4858 3762928 6780.9
##
## Step: AIC=6670.81
## CreditScore ~ Status + Duration + Purpose
##
##
                 Df Sum of Sq
                                  RSS
                                         AIC
## + History
                  4
                       458753 2771665 6556.3
## + Savings
                  4
                       312434 2917985 6597.4
## + Personal
                  3
                       181194 3049225 6630.6
## + Plans
                  2 151796 3078623 6636.3
## + Foreign
                  1 100960 3129459 6647.4
                     82647 3147772 6652.1
## + Age
                  1
## + Housing
                  2 80402 3150017 6654.6
## + Employment
                  4 79048 3151371 6659.0
                  3 58231 3172188 6662.3
## + Existing
                     43629 3186790 6663.9
## + OtherParties 2
## + Telephone
                  1 24305 3206114 6666.8
## + Property
                        33824 3196595 6668.4
## <none>
                              3230419 6670.8
                      7711 3222707 6670.9
## + Amount
                  1
## + Dependants
                        6524 3223895 6671.2
                  1
## + Disposable
                  3
                     19150 3211269 6672.1
## + Job
                  3
                        14028 3216390 6673.3
## + Residence
                         7506 3222913 6674.9
##
## Step: AIC=6556.28
## CreditScore ~ Status + Duration + Purpose + History
##
##
                 Df Sum of Sq
                                  RSS
                                         AIC
## + Savings
                  4
                       282607 2489058 6478.2
## + Personal
                  3
                       155732 2615933 6516.0
```

```
## + Foreign
                  1
                       107079 2664586 6526.8
## + Plans
                        78211 2693455 6537.4
                  2
## + OtherParties 2
                        72063 2699603 6539.2
## + Age
                        45092 2726574 6545.2
                  1
## + Housing
                  2
                        51515 2720151 6545.3
## + Employment
                  4
                      43819 2727846 6551.5
## + Disposable
                  3
                     28885 2742781 6553.9
                       14159 2757507 6554.2
## + Telephone
                  1
                       11738 2759927 6554.9
## + Dependants
                  1
## + Amount
                  1
                        9588 2762077 6555.5
                  3
## + Property
                        21656 2750010 6556.0
## <none>
                               2771665 6556.3
                  3
## + Job
                      15396 2756270 6557.8
                       3920 2767746 6561.1
                  3
## + Residence
## + Existing
                  3
                        1084 2770582 6562.0
##
## Step: AIC=6478.24
## CreditScore ~ Status + Duration + Purpose + History + Savings
##
##
                  Df Sum of Sq
                                   RSS
## + Personal
                  3
                       147554 2341505 6435.4
## + Foreign
                  1
                       101883 2387175 6446.8
## + OtherParties 2
                     86610 2402448 6453.9
                      77615 2411444 6456.9
## + Plans
                  2
## + Housing
                  2 53644 2435414 6464.8
                  1 31316 2457742 6470.1
3 41048 2448010 6470.9
## + Age
## + Disposable
                  1 10806 2478252 6476.8
1 10730 2478328 6476.8
1 9886 2479172 6477.1
## + Amount
## + Telephone
## + Dependants
## <none>
                               2489058 6478.2
## + Employment
                   4
                      23382 2465677 6478.7
                  3
## + Property
                       12533 2476525 6480.2
## + Job
                  3
                        11837 2477221 6480.4
## + Residence
                  3
                         3051 2486007 6483.3
## + Existing
                  3
                          512 2488546 6484.1
##
## Step: AIC=6435.35
## CreditScore ~ Status + Duration + Purpose + History + Savings +
##
       Personal
##
##
                  Df Sum of Sq
                                   RSS
                                          AIC
                     89856 2251648 6406.0
## + Foreign
                  1
## + Plans
                   2
                        89615 2251890 6408.1
## + OtherParties 2
                        85623 2255882 6409.6
## + Disposable
                   3
                        62512 2278993 6419.7
                   2
                        28484 2313021 6429.6
## + Housing
## + Amount
                   1
                       21520 2319984 6430.0
                       11992 2329513 6433.2
## + Age
                  1
## + Telephone
                  1
                        7566 2333939 6434.8
## <none>
                               2341505 6435.4
                  3
## + Property
                      16404 2325101 6435.7
## + Job
                  3
                        15183 2326322 6436.1
## + Dependants
                  1
                            16 2341488 6437.3
```

```
## + Residence
                          5590 2335915 6439.4
## + Existing
                   3
                          2944 2338561 6440.3
                          8072 2333432 6440.6
## + Employment
##
## Step: AIC=6406.05
## CreditScore ~ Status + Duration + Purpose + History + Savings +
       Personal + Foreign
##
##
                  Df Sum of Sq
                                   RSS
                                          AIC
## + Plans
                   2
                         85249 2166399 6379.2
## + OtherParties
                   2
                         81153 2170496 6380.7
                         52299 2199350 6393.2
## + Disposable
                   3
## + Amount
                   1
                         25026 2226622 6399.1
## + Housing
                   2
                        28869 2222780 6399.7
## + Age
                        14374 2237275 6402.9
                   1
## + Telephone
                   1
                       12314 2239334 6403.7
## <none>
                               2251648 6406.0
## + Property
                   3
                         13215 2238434 6407.3
## + Dependants
                            39 2251609 6408.0
                   1
                   3
                         10771 2240878 6408.2
## + Job
## + Residence
                   3
                        6892 2244756 6409.6
## + Existing
                   3
                          2461 2249187 6411.2
                          6672 2244976 6411.7
## + Employment
##
## Step: AIC=6379.17
## CreditScore ~ Status + Duration + Purpose + History + Savings +
##
       Personal + Foreign + Plans
##
##
                  Df Sum of Sq
                                          AIC
                                   RSS
## + OtherParties
                         88026 2078374 6350.0
                   2
## + Disposable
                   3
                         50543 2115856 6366.3
## + Housing
                   2
                         35178 2131221 6370.1
## + Amount
                   1
                         26064 2140335 6371.5
## + Age
                         18247 2148152 6374.4
                   1
## + Telephone
                   1
                         12304 2154095 6376.6
## <none>
                               2166399 6379.2
## + Property
                   3
                         13094 2153306 6380.3
## + Dependants
                   1
                            29 2166371 6381.2
## + Job
                   3
                          9807 2156592 6381.5
                   3
## + Residence
                          7629 2158770 6382.4
## + Employment
                          8988 2157411 6383.8
## + Existing
                   3
                           465 2165935 6385.0
## Step: AIC=6349.99
## CreditScore ~ Status + Duration + Purpose + History + Savings +
##
       Personal + Foreign + Plans + OtherParties
##
##
                Df Sum of Sq
                                 RSS
                                         AIC
## + Disposable 3
                       50008 2028366 6336.5
                       35748 2042626 6340.1
## + Housing
                 2
## + Amount
                       21816 2056558 6343.5
                 1
## + Age
                 1
                       18416 2059958 6344.9
## + Telephone
                 1
                       14562 2063811 6346.4
## <none>
                             2078374 6350.0
```

```
## + Property
                       12391 2065983 6351.2
## + Residence
                       12001 2066373 6351.4
                 3
## + Dependants
                1
                          37 2078337 6352.0
                 3
## + Job
                        4996 2073378 6354.1
## + Employment
                 4
                        8935 2069438 6354.5
## + Existing
                 3
                         784 2077590 6355.7
##
## Step: AIC=6336.5
## CreditScore ~ Status + Duration + Purpose + History + Savings +
##
       Personal + Foreign + Plans + OtherParties + Disposable
##
##
                Df Sum of Sq
                                  RSS
                                         AIC
## + Amount
                 1
                       86779 1941587 6303.5
## + Housing
                 2
                       40388 1987978 6324.4
## + Age
                       24730 2003636 6328.7
                 1
## + Telephone
                       13096 2015270 6333.3
## <none>
                              2028366 6336.5
## + Residence
                 3
                       12264 2016102 6337.7
## + Property
                       11206 2017160 6338.1
                 3
## + Dependants
                 1
                         343 2028022 6338.4
## + Employment
                 4
                       15009 2013356 6338.6
## + Job
                 3
                        3274 2025091 6341.2
                        2756 2025610 6341.4
## + Existing
                 3
##
## Step: AIC=6303.52
## CreditScore ~ Status + Duration + Purpose + History + Savings +
##
       Personal + Foreign + Plans + OtherParties + Disposable +
##
       Amount
##
                Df Sum of Sq
                                  RSS
                                         AIC
## + Telephone
                       32709 1908877 6291.9
## + Housing
                 2
                       35743 1905844 6292.7
## + Age
                       28116 1913470 6293.9
## <none>
                              1941587 6303.5
                 3
## + Property
                       14281 1927306 6303.6
## + Dependants
                         492 1941094 6305.3
                1
## + Residence
                 3
                        8724 1932863 6305.9
## + Employment
                 4
                       12631 1928956 6306.3
## + Job
                 3
                        1865 1939722 6308.8
## + Existing
                 3
                        1416 1940170 6308.9
##
## Step: AIC=6291.93
## CreditScore ~ Status + Duration + Purpose + History + Savings +
##
       Personal + Foreign + Plans + OtherParties + Disposable +
##
       Amount + Telephone
##
                Df Sum of Sq
                                  RSS
                                         AIC
## + Housing
                       35313 1873565 6281.0
## + Age
                 1
                       20271 1888606 6285.4
## <none>
                              1908877 6291.9
## + Property
                 3
                       11502 1897375 6293.1
## + Dependants
                         291 1908587 6293.8
                1
## + Residence
                 3
                        8446 1900431 6294.4
## + Employment 4
                       11104 1897774 6295.3
```

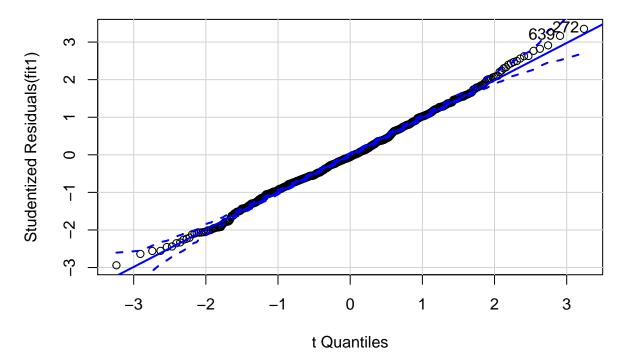
```
## + Existing
                 3
                        2702 1906175 6296.8
## + Job
                 3
                        2121 1906756 6297.0
##
## Step: AIC=6280.99
## CreditScore ~ Status + Duration + Purpose + History + Savings +
       Personal + Foreign + Plans + OtherParties + Disposable +
##
##
       Amount + Telephone + Housing
##
##
                Df Sum of Sq
                                 RSS
                                         AIC
                     14214.8 1859350 6276.9
## + Age
## <none>
                             1873565 6281.0
## + Property
                 3
                     10976.3 1862588 6282.3
## + Dependants
                       314.6 1873250 6282.9
                1
## + Residence
                 3
                      7540.8 1866024 6283.8
## + Employment
                 4
                     11442.0 1862123 6284.1
## + Existing
                 3
                      2572.5 1870992 6285.9
## + Job
                 3
                      2121.5 1871443 6286.1
##
## Step: AIC=6276.9
## CreditScore ~ Status + Duration + Purpose + History + Savings +
##
       Personal + Foreign + Plans + OtherParties + Disposable +
##
       Amount + Telephone + Housing + Age
##
                Df Sum of Sq
##
                                 RSS
## <none>
                              1859350 6276.9
## + Property
                 3
                     12294.3 1847056 6277.6
## + Dependants
                       516.7 1858833 6278.7
                 1
                 3
## + Residence
                      7016.2 1852334 6279.9
## + Existing
                 3
                      3792.5 1855557 6281.3
## + Employment
                 4
                      7638.2 1851712 6281.6
## + Job
                 3
                      1938.2 1857412 6282.1
##
## Call:
## lm(formula = CreditScore ~ Status + Duration + Purpose + History +
       Savings + Personal + Foreign + Plans + OtherParties + Disposable +
       Amount + Telephone + Housing + Age, data = Train)
##
##
## Residuals:
       Min
                1Q Median
                                30
                                        Max
## -139.51 -31.67
                     -2.61
                             32.64 161.55
##
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                         773.15372
                                      39.30008 19.673 < 2e-16 ***
## StatusNegative
                         -50.87728
                                       8.13959
                                               -6.251 6.80e-10 ***
## StatusNone
                          37.58202
                                       7.92566
                                                 4.742 2.53e-06 ***
## StatusSmall
                         -31.32648
                                       8.24029 -3.802 0.000155 ***
## Duration
                         -28.12235
                                       4.57978 -6.141 1.32e-09 ***
                                      17.11427 -1.450 0.147490
## PurposeDomestic
                         -24.81449
## PurposeEducation
                         -52.96452
                                      10.15649
                                                -5.215 2.37e-07 ***
                                      7.37124
                                                 0.021 0.983395
## PurposeFurniture
                           0.15346
## PurposeNewCar
                         -46.23655
                                      7.04418 -6.564 9.69e-11 ***
## PurposeOther
                                      16.57907 -1.199 0.230958
                         -19.87584
```

```
## PurposeRepairs
                         -25.63507
                                      13.45493
                                                -1.905 0.057123 .
## PurposeTelevision
                           2.30334
                                       6.93365
                                                 0.332 0.739832
## PurposeTraining
                          59.37339
                                      21.67226
                                                 2.740 0.006295 **
## PurposeUsedCar
                                      8.21757
                                                 4.612 4.67e-06 ***
                          37.90101
## HistoryB
                          -0.84901
                                      12.38169
                                                -0.069 0.945350
## HistoryC
                          48.63893
                                       9.46070
                                                 5.141 3.47e-07 ***
## HistoryD
                          49.07111
                                      10.79740
                                                 4.545 6.40e-06 ***
## HistoryE
                          82.21082
                                       9.79985
                                                 8.389 2.37e-16 ***
## SavingsLow
                         -13.14080
                                      7.86423
                                                -1.671 0.095140 .
## SavingsMedium
                           0.06139
                                       9.28806
                                                 0.007 0.994728
## SavingsUnknown
                          25.83608
                                       8.59536
                                                 3.006 0.002736 **
## SavingsVeryLarge
                          62.47214
                                      11.29406
                                                 5.531 4.37e-08 ***
## PersonalF:Single
                                       6.75865
                                                 1.175 0.240303
                           7.94241
## PersonalM:DivSepMar
                         -13.30743
                                       8.70654
                                                -1.528 0.126818
## PersonalM:Single
                          30.06153
                                       4.33588
                                                 6.933 8.78e-12 ***
## ForeignYes
                         -54.42600
                                       9.65159
                                                -5.639 2.41e-08 ***
## PlansNone
                                       5.16452
                                                 6.250 6.81e-10 ***
                          32.27987
## PlansStores
                          11.89419
                                       9.68139
                                                 1.229 0.219615
## OtherPartiesGuarantor 61.12648
                                      12.15645
                                                 5.028 6.17e-07 ***
## OtherPartiesNone
                          11.94918
                                       8.90652
                                                 1.342 0.180118
## Disposable2
                         -11.97283
                                       6.48331
                                                -1.847 0.065176
## Disposable3
                         -26.72090
                                       6.94964
                                                -3.845 0.000131 ***
## Disposable4
                         -41.89259
                                       6.66438
                                                -6.286 5.48e-10 ***
## Amount
                         -23.88738
                                       3.73000
                                                -6.404 2.64e-10 ***
## TelephoneYes
                          12.64238
                                       3.87933
                                                 3.259 0.001168 **
## HousingRent
                         -16.91325
                                       4.89081
                                                -3.458 0.000574 ***
## HousingRentFree
                                       6.15605
                                                -0.612 0.540658
                          -3.76808
## Age
                          16.27202
                                       6.74177
                                                 2.414 0.016030 *
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 49.4 on 762 degrees of freedom
## Multiple R-squared: 0.7181, Adjusted R-squared: 0.7044
## F-statistic: 52.46 on 37 and 762 DF, p-value: < 2.2e-16
```

We see that the model is the same as fit1, so we just keep fit1 as our chosen best model.

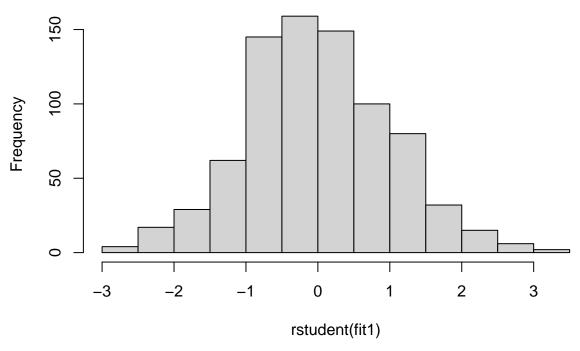
Diagnostic checks

Let's check whether error is normally distributed.



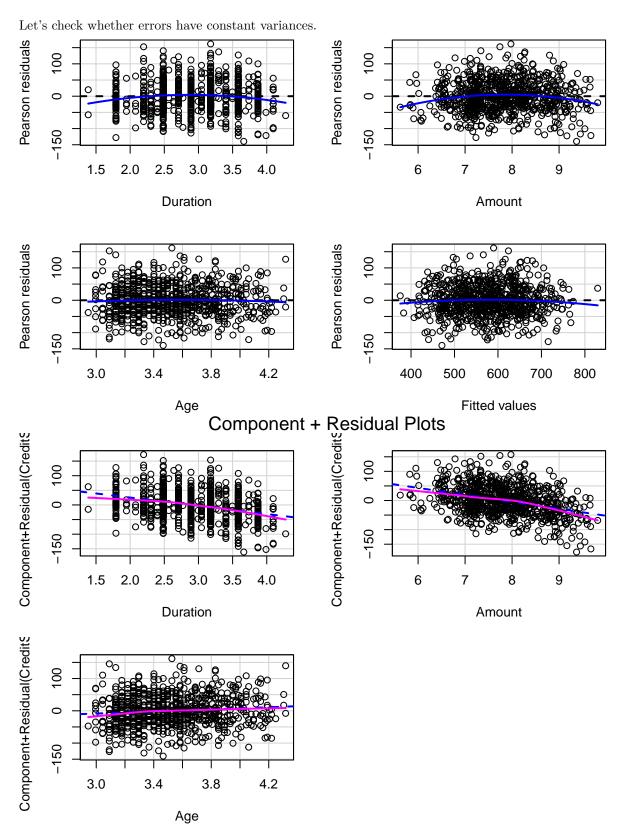
[1] 272 639

Histogram of rstudent(fit1)



Interpretation:

Although the QQ-plot of *fit1* is not completely a straight line, almost all points are inside the confidence interval and the histogram of the residuals is approximately normal distributed. Therefore, the error is approximately normal distributed and the small skewness will not cause much affect to the results. Note that the two outlying data points has been highlighted, *no*.272 and *no*.639, considering the skewness might be caused by outliers, we want to know which in order to see what happens if they are removed later.



${\bf Interpretation:}$

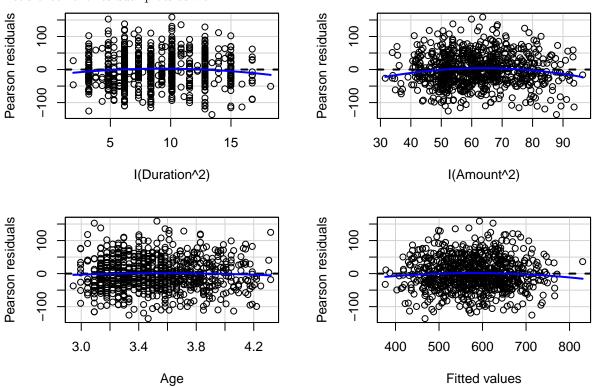
The residual plot for log(Age) is approximately straight line hence the skewness of residual plot for age might

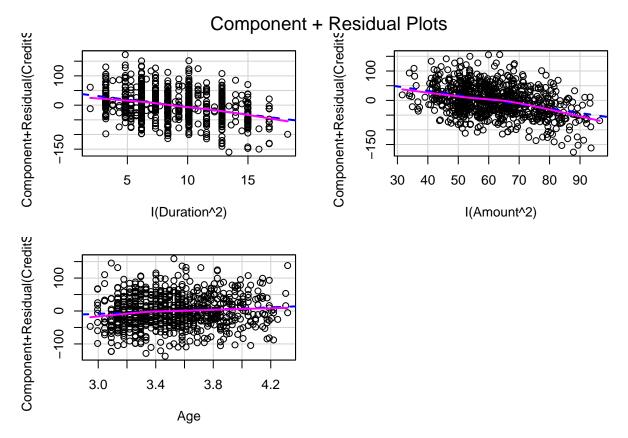
be caused by outliers, while for log(Duration) and log(Amount), plots tends to be downward so the trend is a little bit non-monotonic but it is not too bad. So we just try power transformation for them to see what happen, called model fit2.

 $log(Duration) \rightarrow (log(Duration))^2$

 $log(Amount) \rightarrow (log(Amount))^2$

Let's check the residual plots as well.





We see that the plots become much better and all the Component+Residual Plots are approximately straight lines. Moreover, the residual plots are approximately around 0 and have no clear patterns except some outliers, which is acceptable. Thus, the assumptions for linear regression are satisfied.

So we keep fit2 as our best model and let's check the summary output.

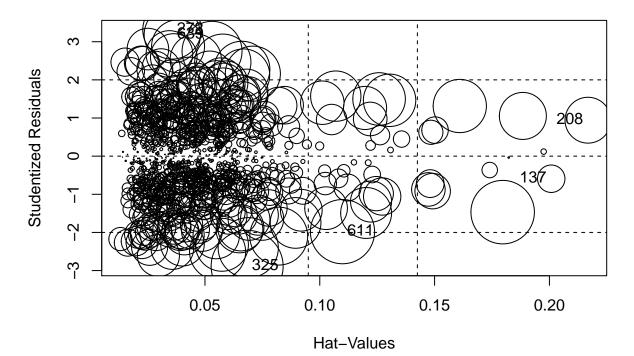
```
##
## Call:
##
   lm(formula = CreditScore ~ Status + I(Duration^2) + History +
       Purpose + I(Amount^2) + Savings + Disposable + Personal +
##
       OtherParties + Age + Plans + Housing + Telephone + Foreign,
##
       data = Train)
##
##
##
  Residuals:
##
        Min
                                              Max
                   1Q
                        Median
                                      3Q
   -136.226
             -30.894
                        -2.888
                                 32.271
                                         158.669
##
##
  Coefficients:
##
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          642.67279
                                      33.25874
                                                 19.323 < 2e-16 ***
## StatusNegative
                          -50.33865
                                        8.09329
                                                 -6.220 8.20e-10 ***
## StatusNone
                                       7.87905
                           37.80254
                                                  4.798 1.93e-06 ***
## StatusSmall
                          -30.63848
                                        8.19473
                                                 -3.739 0.000199 ***
## I(Duration^2)
                           -5.05929
                                        0.79482
                                                 -6.365 3.36e-10 ***
## HistoryB
                           -1.71064
                                      12.30882
                                                 -0.139 0.889505
## HistoryC
                           47.43691
                                       9.41143
                                                  5.040 5.81e-07 ***
## HistoryD
                           48.61100
                                      10.73529
                                                  4.528 6.90e-06 ***
```

```
## HistoryE
                          80.96960
                                       9.74846
                                                 8.306 4.51e-16 ***
## PurposeDomestic
                         -24.04207
                                      17.00420
                                               -1.414 0.157803
## PurposeEducation
                         -53.05132
                                      10.09636
                                                -5.254 1.93e-07 ***
## PurposeFurniture
                                      7.33330
                          -0.65449
                                                -0.089 0.928907
## PurposeNewCar
                         -46.39522
                                      7.00577
                                                -6.622 6.67e-11 ***
## PurposeOther
                         -17.52377
                                      16.49235
                                                -1.063 0.288328
## PurposeRepairs
                         -26.72275
                                      13.38743
                                                -1.996 0.046278 *
## PurposeTelevision
                           2.33951
                                       6.89109
                                                 0.339 0.734328
## PurposeTraining
                          60.86332
                                      21.52967
                                                 2.827 0.004823 **
## PurposeUsedCar
                          37.63425
                                       8.18310
                                                 4.599 4.97e-06 ***
## I(Amount^2)
                          -1.50658
                                       0.23836
                                                -6.321 4.43e-10 ***
## SavingsLow
                         -13.21931
                                       7.81988
                                                -1.690 0.091346
## SavingsMedium
                           0.09274
                                       9.23287
                                                 0.010 0.991988
## SavingsUnknown
                          25.96073
                                       8.54548
                                                 3.038 0.002463 **
## SavingsVeryLarge
                          61.98826
                                      11.23031
                                                 5.520 4.66e-08 ***
## Disposable2
                         -12.53188
                                       6.41867
                                                -1.952 0.051255
## Disposable3
                         -27.68162
                                       6.88491
                                                -4.021 6.38e-05 ***
## Disposable4
                         -42.74550
                                       6.56140
                                                -6.515 1.32e-10 ***
## PersonalF:Single
                           7.66456
                                       6.71791
                                                 1.141 0.254264
## PersonalM:DivSepMar
                         -13.69298
                                       8.65364
                                               -1.582 0.113988
## PersonalM:Single
                          29.91992
                                       4.30413
                                                 6.951 7.78e-12 ***
## OtherPartiesGuarantor
                                      12.08982
                          61.43833
                                                 5.082 4.71e-07 ***
## OtherPartiesNone
                          12.31841
                                       8.85811
                                                 1.391 0.164742
## Age
                          16.45256
                                       6.69879
                                                 2.456 0.014270 *
## PlansNone
                          32.60000
                                       5.13389
                                                 6.350 3.70e-10 ***
## PlansStores
                          12.05621
                                       9.62299
                                                 1.253 0.210643
## HousingRent
                                                -3.515 0.000466 ***
                         -17.08724
                                       4.86161
## HousingRentFree
                          -2.90474
                                       6.12398
                                                -0.474 0.635406
## TelephoneYes
                                                 3.325 0.000928 ***
                          12.83856
                                       3.86178
## ForeignYes
                         -54.70072
                                       9.58834
                                                -5.705 1.67e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 49.11 on 762 degrees of freedom
## Multiple R-squared: 0.7214, Adjusted R-squared:
## F-statistic: 53.32 on 37 and 762 DF, p-value: < 2.2e-16
## [1] "fit2$adj.r.squared = 0.707831"
```

We find that $(log(Duration))^2$ and $(log(Amount)^2$ are still significant at 5% level and R_{adj}^2 has been increased to 0.707831, which shows a good fit of our model fit2.

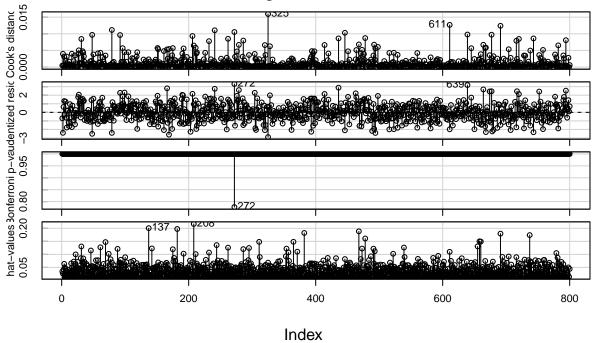
Moreover, we also need to test whether there are unusual or influential observations which could affect the result.

Let's look for outliers and high-leverage points.



StudRes Hat CookD ## 137 -0.5921394 0.20079092 0.002320161 ## 208 0.9425215 0.21679834 0.006472095 ## 272 3.3116139 0.03566543 0.010535907 ## 325 -2.8877540 0.06836724 0.015950606 ## 611 -1.9796145 0.1098883 0.012683133 ## 639 3.1836112 0.03579505 0.009784403

Diagnostic Plots



Interpretation:

From the plots and the output values:

Observations no.272, no.639, no.325 have a high value of |StudRes| > 2 so these three observations are considered as outliers.

Observation no.137 and no.208 have high Hat values much larger than $2p/n = 15 \times 2/800 = 0.0375$ so considered as high-leverage points. However, the CookD of them are very small so these two points are not influential.

Observation no.325 and no.611 have a high value of CookD, so these two observations could be influential.

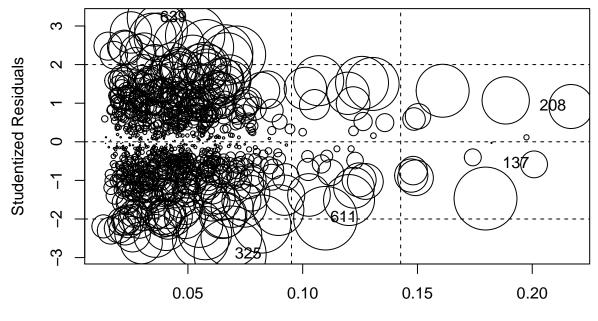
However, the value of CookD don't differ so much and all of them are < 1 so we focus on the StudRes and Hat-Values first.

Let's consider the model with the removal of points:

fit3: model fit2 with the removal of observation no.272, which has the highest value of |StudRes|.

```
## Calls:
## 1: lm(formula = CreditScore ~ Status + I(Duration^2) + History + Purpose +
     I(Amount^2) + Savings + Disposable + Personal + OtherParties + Age + Plans
##
     + Housing + Telephone + Foreign, data = Train)
## 2: lm(formula = fit2, data = Train1)
##
##
                          Model 1 Model 2
## (Intercept)
                              643
                                      639
## StatusNegative
                            -50.3
                                    -51.2
## StatusNone
                             37.8
                                     37.7
## StatusSmall
                            -30.6
                                    -30.9
## I(Duration^2)
                            -5.06
                                    -5.13
## HistoryB
                            -1.71
                                    -1.55
## HistoryC
                             47.4
                                     47.0
## HistoryD
                             48.6
                                     48.5
## HistoryE
                                       81
                               81
## PurposeDomestic
                            -24.0
                                    -23.4
## PurposeEducation
                            -53.1
                                    -52.4
## PurposeFurniture
                           -0.654
                                   -0.361
## PurposeNewCar
                            -46.4
                                    -46.1
## PurposeOther
                            -17.5
                                    -17.1
## PurposeRepairs
                                    -26.4
                            -26.7
## PurposeTelevision
                             2.34
                                     2.43
## PurposeTraining
                             60.9
                                     60.6
## PurposeUsedCar
                             37.6
                                     35.8
## I(Amount^2)
                            -1.51
                                    -1.46
## SavingsLow
                            -13.2
                                    -13.4
## SavingsMedium
                                   0.0765
                           0.0927
## SavingsUnknown
                             26.0
                                     26.1
## SavingsVeryLarge
                               62
                                       62
                                    -13.3
## Disposable2
                            -12.5
## Disposable3
                            -27.7
                                    -27.2
## Disposable4
                            -42.7
                                    -42.3
## PersonalF:Single
                             7.66
                                     7.82
## PersonalM:DivSepMar
                            -13.7
                                    -13.8
## PersonalM:Single
                             29.9
                                     29.6
## OtherPartiesGuarantor
                             61.4
                                     61.7
## OtherPartiesNone
                             12.3
                                     12.3
                             16.5
                                     17.1
## Age
```

```
## PlansNone
                              32.6
                                       32.3
## PlansStores
                              12.1
                                      12.1
## HousingRent
                             -17.1
                                      -16.8
## HousingRentFree
                                       -4.6
                              -2.9
## TelephoneYes
                              12.8
                                      12.2
## ForeignYes
                             -54.7
                                      -54.6
```



```
## StudRes Hat CookD
## 137 -0.5848924 0.20079992 0.002263873
## 208 0.9141369 0.21688358 0.006091623
## 325 -2.9202828 0.06838213 0.016311577
## 611 -1.9798528 0.10990184 0.012687795
## 639 3.2050902 0.03579506 0.009914958
## [1] "fit3$adj.r.squared = 0.710646"
```

After we delete no.272, the CookD for the whole model changed but no.639 still has the largest high |StudtRes|. Notice that R_{adj}^2 has been increased to 0.710646. Let's try removing no.639 to see what happens, called fit4.

Hat-Values

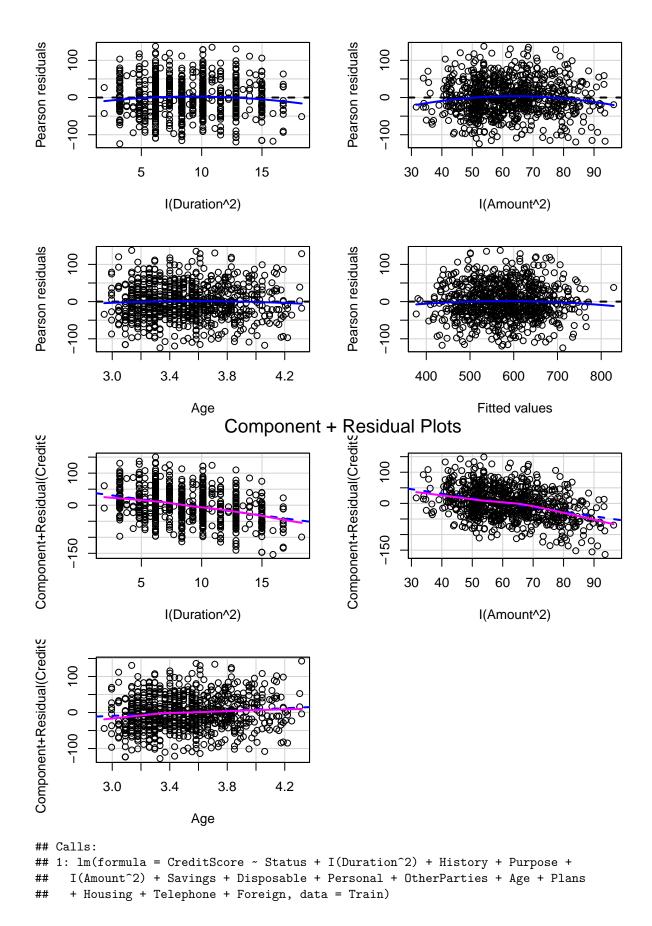
```
## Calls:
## 1: lm(formula = CreditScore ~ Status + I(Duration^2) + History + Purpose +
     I(Amount^2) + Savings + Disposable + Personal + OtherParties + Age + Plans
     + Housing + Telephone + Foreign, data = Train)
## 2: lm(formula = fit2, data = Train1)
## 3: lm(formula = fit2, data = Train2)
##
##
                          Model 1 Model 2 Model 3
## (Intercept)
                              643
                                      639
                                              639
                                    -51.2
                                             -51.3
## StatusNegative
                            -50.3
## StatusNone
                             37.8
                                     37.7
                                             37.1
## StatusSmall
                            -30.6
                                    -30.9
                                            -30.7
## I(Duration^2)
                            -5.06
                                    -5.13
                                            -5.00
## HistoryB
                            -1.71
                                    -1.55
                                            -1.61
```

```
## HistoryC
                             47.4
                                      47.0
                                              46.8
## HistoryD
                                      48.5
                                              48.4
                             48.6
## HistoryE
                               81
                                        81
                                                81
                                              -23.2
## PurposeDomestic
                            -24.0
                                     -23.4
## PurposeEducation
                            -53.1
                                     -52.4
                                              -52.0
                           -0.654
                                    -0.361
                                            -1.242
## PurposeFurniture
## PurposeNewCar
                                     -46.1
                            -46.4
                                              -45.9
                                             -17.6
                                     -17.1
## PurposeOther
                            -17.5
## PurposeRepairs
                            -26.7
                                     -26.4
                                              -26.2
## PurposeTelevision
                             2.34
                                      2.43
                                              2.51
## PurposeTraining
                             60.9
                                      60.6
                                              60.6
## PurposeUsedCar
                             37.6
                                      35.8
                                              36.1
## I(Amount^2)
                            -1.51
                                     -1.46
                                              -1.48
                            -13.2
## SavingsLow
                                     -13.4
                                              -13.4
                           0.0927
                                    0.0765 -2.0019
## SavingsMedium
## SavingsUnknown
                             26.0
                                      26.1
                                              26.1
## SavingsVeryLarge
                             62.0
                                      62.0
                                              61.9
## Disposable2
                            -12.5
                                     -13.3
                                              -14.4
                                     -27.2
                            -27.7
                                              -27.5
## Disposable3
## Disposable4
                            -42.7
                                     -42.3
                                              -42.8
## PersonalF:Single
                             7.66
                                      7.82
                                              8.35
## PersonalM:DivSepMar
                            -13.7
                                     -13.8
                                             -13.2
## PersonalM:Single
                             29.9
                                      29.6
                                              30.0
## OtherPartiesGuarantor
                                      61.7
                                              61.1
                             61.4
## OtherPartiesNone
                             12.3
                                      12.3
                                              11.6
## Age
                             16.5
                                      17.1
                                              17.5
## PlansNone
                             32.6
                                      32.3
                                              32.2
## PlansStores
                             12.1
                                      12.1
                                              12.0
                                     -16.8
## HousingRent
                            -17.1
                                             -17.7
## HousingRentFree
                            -2.90
                                     -4.60
                                              -4.93
## TelephoneYes
                             12.8
                                      12.2
                                              12.5
## ForeignYes
                            -54.7
                                     -54.6
                                              -54.9
##
## Call:
## lm(formula = fit2, data = Train2)
##
## Residuals:
##
        Min
                   1Q
                        Median
                                      3Q
                                              Max
## -134.649 -30.154
                        -2.857
                                  32.584
                                          138.064
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          639.4449
                                       32.8638
                                                19.457 < 2e-16 ***
## StatusNegative
                          -51.2620
                                        7.9966
                                                -6.410 2.55e-10 ***
                                                  4.773 2.17e-06 ***
## StatusNone
                           37.1499
                                        7.7828
## StatusSmall
                          -30.6810
                                        8.0930
                                                 -3.791 0.000162 ***
## I(Duration^2)
                           -5.0032
                                        0.7861
                                                -6.364 3.39e-10 ***
                                                -0.133 0.894422
## HistoryB
                           -1.6137
                                       12.1554
## HistoryC
                           46.7695
                                        9.2952
                                                  5.032 6.08e-07 ***
## HistoryD
                           48.3784
                                       10.6015
                                                  4.563 5.87e-06 ***
## HistoryE
                                        9.6269
                                                  8.415 < 2e-16 ***
                           81.0095
## PurposeDomestic
                          -23.1777
                                       16.7933
                                                -1.380 0.167939
## PurposeEducation
                          -52.0207
                                        9.9731 -5.216 2.36e-07 ***
```

```
## PurposeFurniture
                           -1.2417
                                       7.2476
                                               -0.171 0.864012
## PurposeNewCar
                          -45.9375
                                       6.9191
                                               -6.639 6.00e-11 ***
## PurposeOther
                          -17.6155
                                      16.2881
                                                -1.081 0.279819
## PurposeRepairs
                                      13.2209
                          -26.1998
                                                -1.982 0.047874 *
## PurposeTelevision
                            2.5112
                                       6.8052
                                                0.369 0.712223
## PurposeTraining
                                      21.2613
                                                2.850 0.004488 **
                           60.5980
## PurposeUsedCar
                           36.0965
                                       8.0996
                                                 4.457 9.58e-06 ***
## I(Amount^2)
                           -1.4762
                                       0.2359
                                                -6.258 6.53e-10 ***
## SavingsLow
                          -13.4453
                                       7.7226
                                                -1.741 0.082081 .
## SavingsMedium
                           -2.0019
                                       9.1407
                                               -0.219 0.826699
## SavingsUnknown
                           26.0741
                                       8.4391
                                                3.090 0.002077 **
  SavingsVeryLarge
                           61.8698
                                      11.0903
                                                5.579 3.37e-08 ***
## Disposable2
                                       6.3525
                                               -2.269 0.023565 *
                          -14.4119
                          -27.4673
## Disposable3
                                       6.8014
                                                -4.038 5.93e-05 ***
## Disposable4
                          -42.7765
                                       6.4829
                                                -6.598 7.79e-11 ***
## PersonalF:Single
                            8.3528
                                       6.6363
                                                 1.259 0.208546
## PersonalM:DivSepMar
                                       8.5475
                                                -1.544 0.122902
                          -13.2010
## PersonalM:Single
                           29.9837
                                       4.2540
                                                7.048 4.07e-12 ***
                          61.1499
## OtherPartiesGuarantor
                                      11.9402
                                                5.121 3.85e-07 ***
## OtherPartiesNone
                           11.6303
                                       8.7502
                                                 1.329 0.184202
                                                2.640 0.008452 **
## Age
                           17.4768
                                       6.6191
## PlansNone
                           32.1997
                                       5.0706
                                                 6.350 3.70e-10 ***
## PlansStores
                                       9.5030
                                                 1.260 0.208137
                           11.9716
## HousingRent
                          -17.6743
                                       4.8084
                                                -3.676 0.000254 ***
## HousingRentFree
                           -4.9283
                                       6.0699
                                                -0.812 0.417094
## TelephoneYes
                           12.5080
                                       3.8186
                                                 3.276 0.001103 **
## ForeignYes
                                               -5.793 1.01e-08 ***
                          -54.8567
                                       9.4691
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 48.5 on 760 degrees of freedom
## Multiple R-squared: 0.7261, Adjusted R-squared: 0.7128
## F-statistic: 54.45 on 37 and 760 DF, p-value: < 2.2e-16
## [1] "fit4$adj.r.squared = 0.712758"
```

According to the comparison and summary, the model changed after deleting the observation no.272 and no.639. Coefficient of log(Age) has been increased by about 6% and log(Age) become more significant by summary output. The R_{adj}^2 has been increased to 0.712758.

Let's remove no.325 to see what happens, called fit5.



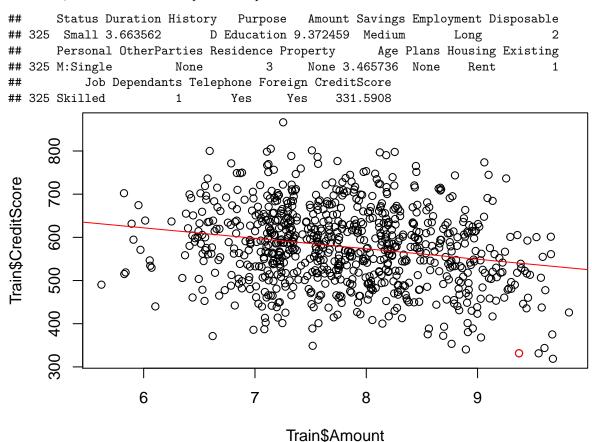
```
## 2: lm(formula = fit2, data = Train1)
## 3: lm(formula = fit2, data = Train2)
## 4: lm(formula = fit2, data = Train3)
##
##
                           Model 1 Model 2 Model 3 Model 4
##
                                        639
                                                639
                                                         635
   (Intercept)
                               643
##
  StatusNegative
                             -50.3
                                      -51.2
                                              -51.3
                                                       -51.2
## StatusNone
                              37.8
                                       37.7
                                               37.1
                                                        37.0
## StatusSmall
                             -30.6
                                      -30.9
                                              -30.7
                                                       -30.3
## I(Duration^2)
                             -5.06
                                      -5.13
                                              -5.00
                                                       -5.01
## HistoryB
                             -1.71
                                      -1.55
                                              -1.61
                                                       -1.48
## HistoryC
                              47.4
                                       47.0
                                               46.8
                                                        46.7
## HistoryD
                              48.6
                                       48.5
                                               48.4
                                                        50.4
## HistoryE
                                81
                                         81
                                                  81
                                                          81
                                                       -22.0
                                      -23.4
                                              -23.2
## PurposeDomestic
                             -24.0
  PurposeEducation
                             -53.1
                                      -52.4
                                              -52.0
                                                       -47.5
                            -0.654
                                    -0.361
                                             -1.242
                                                      -0.473
  PurposeFurniture
  PurposeNewCar
                             -46.4
                                      -46.1
                                              -45.9
                                                       -45.3
  PurposeOther
                             -17.5
                                      -17.1
                                              -17.6
                                                       -17.4
## PurposeRepairs
                             -26.7
                                      -26.4
                                              -26.2
                                                       -25.7
  PurposeTelevision
                              2.34
                                       2.43
                                               2.51
                                                        3.41
## PurposeTraining
                              60.9
                                       60.6
                                               60.6
                                                        62.4
                                               36.1
## PurposeUsedCar
                              37.6
                                       35.8
                                                        36.5
## I(Amount^2)
                             -1.51
                                      -1.46
                                              -1.48
                                                       -1.45
## SavingsLow
                             -13.2
                                      -13.4
                                              -13.4
                                                       -13.7
  SavingsMedium
                            0.0927
                                    0.0765
                                            -2.0019
                                                    -0.7210
   SavingsUnknown
                                               26.1
                                                        25.6
                              26.0
                                       26.1
   SavingsVeryLarge
                              62.0
                                       62.0
                                               61.9
                                                        61.8
   Disposable2
                             -12.5
                                      -13.3
                                              -14.4
                                                       -13.7
## Disposable3
                             -27.7
                                      -27.2
                                              -27.5
                                                       -27.3
## Disposable4
                             -42.7
                                      -42.3
                                              -42.8
                                                       -42.5
  PersonalF:Single
                              7.66
                                      7.82
                                               8.35
                                                        8.49
## PersonalM:DivSepMar
                             -13.7
                                      -13.8
                                              -13.2
                                                       -13.1
                              29.9
                                       29.6
                                               30.0
                                                        30.3
## PersonalM:Single
  OtherPartiesGuarantor
                              61.4
                                       61.7
                                               61.1
                                                        61.4
## OtherPartiesNone
                              12.3
                                       12.3
                                               11.6
                                                        11.9
## Age
                              16.5
                                       17.1
                                               17.5
                                                        17.7
## PlansNone
                              32.6
                                       32.3
                                               32.2
                                                        32.4
## PlansStores
                              12.1
                                       12.1
                                               12.0
                                                        11.8
## HousingRent
                             -17.1
                                      -16.8
                                              -17.7
                                                       -16.6
  HousingRentFree
                             -2.90
                                      -4.60
                                              -4.93
                                                       -5.57
  TelephoneYes
                              12.8
                                       12.2
                                               12.5
                                                        12.8
## ForeignYes
                             -54.7
                                      -54.6
                                              -54.9
                                                       -55.2
   [1] "fit2$adj.r.squared = 0.707831"
   [1] "fit3$adj.r.squared = 0.710646"
   [1] "fit4$adj.r.squared = 0.712758"
## [1] "fit5$adj.r.squared = 0.713202"
```

After deleting no.272, no.639 and no.325, according to the comparison and summary: log(Age) become more significant by summary output. The R_{adj}^2 has been increased to 0.713202. However, the differences are very small so this is further evidence that it is not a clear call, and it is not right or wrong to remove these

observations. Depending on what we want to do with the model (e.g. if we want to make predictions), we could even use both models and see how the outcome differs. According to residual and Component+Residual Plot, the assumption still holds.

If we take a look at the no.325, we find that it has higher Amount but lower CreditScore extremely (the red points shown below). So this observation should be deleted since it may influence the accuracy of prediction for general individuals.

Actually, it is hard to say whether we should remove these three observations, we should be very careful when considering the deletion of observations. This could be discussed separately. We can determine that the observation is an outlier because of data errors in recording or because a protocal wasn't followed. In these cases, deleting the offending observation seems reasonable. However, some observations may have some interesting characteristics, which might give useful insight to our study, which is a subjective judgment. Therefore, we evaluate them in prediction part.



Model Prediction

Summary of current model:

fit2: best model we find:

 $CreditScore \sim Status + (log(Duration))^2 + History + Purpose + (log(Amount))^2 + Savings + Disposable + Personal + Other Parties + log(Age) + Plans + Housing + Telephone + Foreign$

fit3: best model with the removal of no.272.

fit4: best model with the removal of both no.272 and no.639.

fit5: best model with the removal of both no.272,no.639 and no.325.

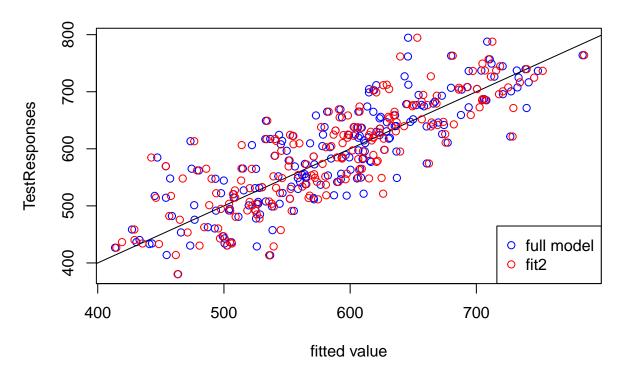
We will use the Test.txt data to predict the responses for individuals.

We use the mean-square error (MSE) as a criterion of the quality for full model, fit2, fit3, fit4 and fit5.

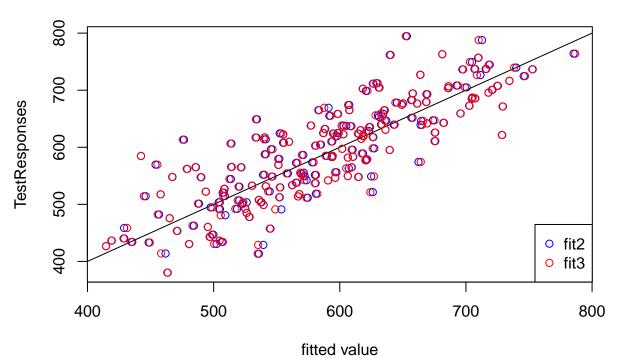
- ## [1] "full_MSE = 2468.280381"
- ## [1] "fit2_MSE = 2443.476907"
- ## [1] "fit3_MSE = 2435.199877"
- ## [1] "fit4_MSE = 2436.308412"
- ## [1] "fit5_MSE = 2425.233652"

Let's also draw the graph for fitted value and True Value for models.

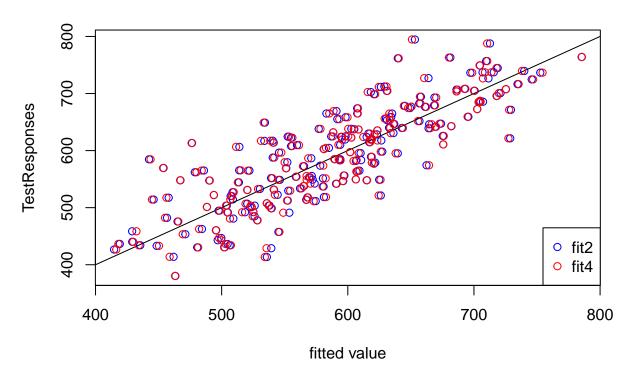
Fitted Value vs True Value for full model and fit2



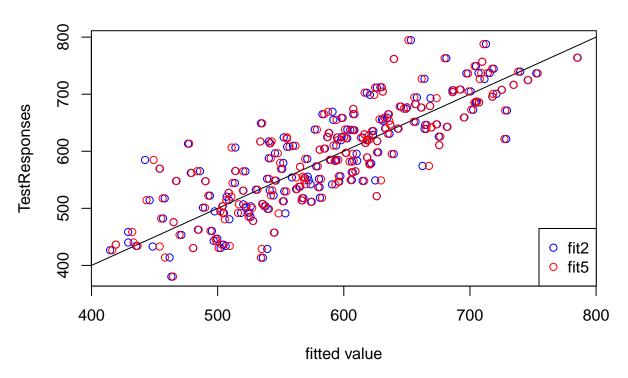
Fitted Value vs True Value for fit2 and fit3



Fitted Value vs True Value for fit2 and fit4



Fitted Value vs True Value for fit2 and fit5



${\bf Interpretation:}$

Compared to full model, our best model fit2 has a lower MSE 2443.477. The plot shows that fit2 is much better than $full\ model\ 2468.28$ since the points concentrate more along the y=x axis.

We see that the MSE tends to decreases as we delete the outliers and fit5 has the lowest MSE 2425.234. So our best model is now fit5.

Let's summarize our data into a data frame and predict:

| ## | | fitted_value | lower_bound | upper_bound | true_value |
|----|----|--------------|-------------|-------------|------------|
| ## | 1 | 477.4090 | 380.6238 | 574.1942 | 613.2571 |
| ## | 2 | 695.1527 | 596.9392 | 793.3662 | 659.2217 |
| ## | 3 | 588.8279 | 492.6674 | 684.9884 | 584.9637 |
| ## | 4 | 643.4013 | 547.7542 | 739.0484 | 639.6288 |
| ## | 5 | 584.3633 | 486.9702 | 681.7564 | 604.7193 |
| ## | 6 | 619.9772 | 522.5292 | 717.4252 | 620.1996 |
| ## | 7 | 533.7640 | 437.5979 | 629.9301 | 617.0603 |
| ## | 8 | 562.1437 | 463.9633 | 660.3240 | 554.1421 |
| ## | 9 | 596.0893 | 500.3294 | 691.8491 | 556.3166 |
| ## | 10 | 606.8638 | 509.9590 | 703.7686 | 637.4851 |
| ## | 11 | 708.8831 | 611.7069 | 806.0593 | 737.1314 |
| ## | 12 | 500.7662 | 402.9024 | 598.6300 | 430.5130 |
| ## | 13 | 490.5075 | 394.8866 | 586.1284 | 547.5392 |
| ## | 14 | 657.1201 | 560.8720 | 753.3682 | 682.7224 |
| ## | 15 | 650.0193 | 552.3720 | 747.6665 | 676.9100 |
| ## | 16 | 701.0991 | 603.3159 | 798.8823 | 672.7252 |
| ## | 17 | 628.3286 | 532.1093 | 724.5479 | 655.9837 |
| ## | 18 | 636.0935 | 538.8844 | 733.3026 | 653.3876 |
| ## | 19 | 624.8229 | 528.6831 | 720.9628 | 711.4867 |
| ## | 20 | 717.5793 | 617.9138 | 817.2447 | 744.6560 |

| | 0.4 | 705 0000 | 600 0075 | 007 0004 | 607 4004 |
|----|----------------|----------|----------|----------|----------|
| ## | | 705.6903 | 603.9975 | 807.3831 | 687.1201 |
| ## | 22 | 703.5347 | 606.5239 | 800.5456 | 685.0312 |
| ## | 23 | 543.3457 | 446.5268 | 640.1645 | 531.5324 |
| ## | 24 | 687.1644 | 589.0400 | 785.2888 | 706.8683 |
| ## | 25 | 489.9192 | 391.2941 | 588.5444 | 501.2033 |
| ## | 26 | 479.2898 | 382.2074 | 576.3722 | 562.0501 |
| ## | 27 | 522.8847 | 424.1405 | 621.6288 | 503.5416 |
| ## | 28 | 634.8224 | 538.3258 | 731.3190 | 630.6475 |
| ## | 29 | 587.5301 | 490.6970 | 684.3632 | 669.1843 |
| ## | 30 | 509.6301 | 412.0774 | 607.1828 | 434.1115 |
| ## | 31 | 673.5630 | 575.9498 | 771.1762 | 692.9877 |
| ## | 32 | 573.8576 | 470.1270 | 677.5883 | 511.4866 |
| ## | 33 | 681.6501 | 585.9872 | 777.3129 | 642.7761 |
| | | | | | |
| ## | 34 | 746.2124 | 650.0412 | 842.3836 | 724.6790 |
| ## | 35 | 514.2817 | 414.7035 | 613.8599 | 565.4501 |
| ## | 36 | 727.3414 | 631.4962 | 823.1865 | 621.4969 |
| ## | 37 | 607.5850 | 510.0289 | 705.1411 | 674.0797 |
| ## | 38 | 607.5529 | 510.6103 | 704.4956 | 636.9924 |
| ## | 39 | 443.6115 | 344.6120 | 542.6111 | 514.2173 |
| ## | 40 | 673.3878 | 576.9957 | 769.7800 | 647.1938 |
| ## | 41 | 570.2727 | 474.5358 | 666.0095 | 542.2178 |
| ## | 42 | 580.8009 | 485.2445 | 676.3574 | 602.7555 |
| ## | 43 | 416.4709 | 317.1830 | 515.7588 | 426.6896 |
| ## | 44 | 595.1849 | 497.8485 | 692.5214 | 619.4148 |
| ## | 45 | 617.4601 | 520.4925 | 714.4276 | 614.6528 |
| ## | 46 | 541.8615 | 444.8110 | 638.9119 | 613.9141 |
| ## | 47 | 676.4960 | 579.2430 | 773.7489 | 625.6636 |
| ## | 48 | 579.3539 | 482.2246 | 676.4832 | 573.5844 |
| | 49 | 569.4618 | 472.7374 | 666.1862 | 586.5229 |
| | 50 | 709.7126 | 611.6384 | 807.7868 | 756.8776 |
| | 51 | 595.1391 | 498.5186 | 691.7596 | 624.1171 |
| ## | 52 | 592.9066 | 497.2736 | 688.5396 | 582.9542 |
| | | | | | |
| | 53 | 503.3138 | 407.2916 | 599.3359 | 436.2796 |
| | 54 | 556.8992 | 459.5225 | 654.2760 | 607.9046 |
| | 55 | 630.1715 | 531.8381 | 728.5048 | 712.2499 |
| ## | 56 | 707.1764 | 609.7955 | 804.5573 | 685.6361 |
| | 57 | 464.5831 | 366.5595 | 562.6067 | 380.3482 |
| | 58 | 480.4624 | 383.2769 | 577.6478 | 430.3903 |
| | 59 | 753.6936 | 655.9392 | 851.4480 | 736.5829 |
| ## | 60 | 593.3173 | 497.1295 | 689.5050 | 541.9331 |
| ## | 61 | 456.3902 | 360.6322 | 552.1481 | 517.4296 |
| ## | 62 | 540.6680 | 442.0177 | 639.3184 | 498.8789 |
| ## | 63 | 520.3144 | 424.7265 | 615.9024 | 564.8867 |
| ## | 64 | 655.4442 | 559.2481 | 751.6403 | 651.6743 |
| ## | 65 | 579.7023 | 483.7132 | 675.6913 | 537.0380 |
| ## | 66 | 564.3485 | 468.2970 | 660.3999 | 537.9019 |
| ## | 67 | 626.3723 | 529.5365 | 723.2081 | 617.7234 |
| ## | 68 | 647.5179 | 551.7839 | 743.2519 | 674.5304 |
| ## | 69 | 638.0141 | 540.3637 | 735.6645 | 595.2126 |
| ## | 70 | 458.2966 | 361.6706 | 554.9225 | 413.8889 |
| ## | 71 | 605.4607 | 509.2270 | 701.6943 | 549.5685 |
| | 72 | 599.1682 | 500.7582 | 697.5783 | 658.3994 |
| | 73 | 520.0244 | 424.2064 | 615.8424 | 531.0190 |
| | 73 74 | 494.3730 | | | 460.4072 |
| ## | / ' | 494.3730 | 398.4272 | 590.3188 | 400.4072 |

| ## | 75 | 616.5445 | 519.1282 | 713.9607 | 702.5505 |
|----|------------|----------------------|----------|----------|----------|
| | 76 | 635.7650 | 539.0089 | 732.5210 | 664.8437 |
| | | | | | |
| | 77 | 633.2539 | 537.7824 | 728.7254 | 639.9483 |
| | 78 | 691.9819 | 594.6167 | 789.3471 | 708.1774 |
| | 79 | 587.2836 | 487.9345 | 686.6327 | 624.8101 |
| ## | 80 | 626.3687 | 529.8652 | 722.8723 | 598.1557 |
| ## | 81 | 668.3728 | 571.4569 | 765.2887 | 679.2970 |
| ## | 82 | 498.9740 | 398.9434 | 599.0046 | 442.9465 |
| ## | 83 | 601.4376 | 505.8594 | 697.0158 | 597.2687 |
| ## | 84 | 535.3456 | 434.7090 | 635.9822 | 649.0334 |
| ## | 85 | 629.4475 | 532.3392 | 726.5558 | 548.9310 |
| ## | 86 | 675.6211 | 579.5005 | 771.7417 | 610.8058 |
| ## | 87 | 604.5626 | 507.3408 | 701.7844 | 581.8715 |
| ## | 88 | 620.0625 | 523.9965 | 716.1284 | 628.3831 |
| ## | 89 | 588.0113 | 490.1754 | 685.8473 | 631.9839 |
| ## | 90 | 686.5627 | 583.3667 | 789.7588 | 703.6629 |
| ## | 91 | 606.1538 | 508.0804 | 704.2273 | 563.2154 |
| ## | 92 | 531.5777 | 434.7543 | 628.4011 | 532.6827 |
| ## | 93 | 632.2693 | 535.1817 | 729.3570 | 658.7866 |
| ## | 94 | 661.7449 | 565.2655 | 758.2244 | 676.5573 |
| ## | 95 | 714.0289 | 617.4201 | 810.6377 | 737.1775 |
| ## | 96 | 549.5583 | 452.7399 | 646.3767 | 579.5870 |
| ## | 97 | 613.5816 | 515.0295 | 712.1337 | 623.8587 |
| ## | 98 | 548.2882 | 451.9282 | 644.6481 | 491.1756 |
| ## | 99 | 620.2451 | 522.1987 | 718.2916 | 578.8728 |
| ## | 100 | 710.7854 | 612.5917 | 808.9791 | 787.7449 |
| ## | 101 | 511.8170 | 416.2245 | 607.4096 | 544.3827 |
| ## | 102 | 601.0114 | 503.7648 | 698.2581 | 638.1359 |
| ## | 103 | 516.1461 | 420.3210 | 611.9712 | 491.9649 |
| ## | 104 | 727.9118 | 632.0715 | 823.7521 | 671.4428 |
| ## | 105 | 568.7309 | 470.4473 | 667.0145 | 553.3379 |
| ## | 106 | 618.1651 | 520.0165 | 716.3137 | 619.2276 |
| ## | 107 | 554.3621 | 456.0958 | 652.6284 | 529.6569 |
| ## | 107 | 527.3830 | 430.1321 | 624.6340 | 500.8778 |
| ## | 108 | | | 640.2198 | 617.2553 |
| ## | 110 | 542.8536 561.7237 | 445.4874 | | |
| | | | 465.7295 | 657.7179 | 609.5791 |
| ## | 111 112 | 469.7762 | 373.9268 | 565.6256 | 453.4090 |
| ## | | 516.8095 | 420.5075 | 613.1115 | 506.9408 |
| ## | 113 | 584.4868 | 486.7974 | 682.1762 | 664.9839 |
| ## | 114 | 607.1942 | 510.7300 | 703.6584 | 595.6654 |
| ## | 115 | 483.8045 | 387.3163 | 580.2928 | 565.0835 |
| ## | 116 | 591.7949 | 494.7232 | 688.8666 | 610.0330 |
| ## | 117 | 510.8421 | 413.9152 | 607.7690 | 520.4210 |
| ## | 118 | 503.6472 | 404.8051 | 602.4893 | 503.6356 |
| ## | 119 | 595.6850 | 499.6276 | 691.7425 | 546.5841 |
| ## | 120 | 498.3436 | 400.0958 | 596.5914 | 446.8143 |
| ## | 121 | 527.8930 | 430.3598 | 625.4262 | 477.8550 |
| ## | 122 | 651.2346 | 554.4802 | 747.9889 | 794.6505 |
| ## | 123 | 667.5199 | 569.7875 | 765.2524 | 574.2764 |
| ## | 124 | 506.8886 | 411.1048 | 602.6723 | 514.5122 |
| ## | 125 | 601.8366 | 505.5179 | 698.1553 | 622.8158 |
| ## | 126 | 582.7245 | 485.6211 | 679.8279 | 518.5721 |
| ## | 127 | 523.7989 | 427.2724 | 620.3255 | 492.2498 |
| ## | 128 | 542.0710 | 442.8251 | 641.3169 | 587.7238 |
| | | | | | |

| | | | | | 224 2542 |
|----|-----|----------|----------|----------|--------------------|
| | 129 | 600.2313 | 503.8390 | 696.6236 | 624.9519 |
| ## | 130 | 624.1752 | 526.7654 | 721.5851 | 698.7750 |
| ## | 131 | 484.9609 | 387.9287 | 581.9931 | 462.5540 |
| ## | 132 | 620.3361 | 524.8376 | 715.8345 | 577.0902 |
| ## | 133 | 454.2826 | 356.8211 | 551.7442 | 569.5065 |
| ## | 134 | 436.4759 | 337.8355 | 535.1162 | 434.0912 |
| ## | 135 | 734.7323 | 637.9998 | 831.4649 | 716.4410 |
| ## | 136 | 502.1141 | 402.3762 | 601.8520 | 494.6875 |
| | | | | | |
| ## | 137 | 718.3520 | 620.4925 | 816.2115 | 700.6472 |
| ## | 138 | 707.8334 | 610.3692 | 805.2976 | 726.4957 |
| ## | 139 | 432.2765 | 329.6693 | 534.8837 | 458.5903 |
| ## | 140 | 665.4160 | 569.0600 | 761.7720 | 639.1471 |
| ## | 141 | 466.9063 | 367.8732 | 565.9395 | 547.9424 |
| ## | 142 | 540.6983 | 444.1466 | 637.2500 | 551.7520 |
| ## | 143 | 492.6125 | 396.8063 | 588.4187 | 522.1601 |
| ## | 144 | 568.7484 | 471.8633 | 665.6335 | 549.1214 |
| ## | 145 | 698.9073 | 601.4560 | 796.3586 | 704.8164 |
| ## | 146 | 665.8576 | 569.4677 | 762.2475 | 646.1397 |
| ## | 147 | 536.8817 | 441.1911 | 632.5723 | 503.6918 |
| ## | 148 | 567.4952 | 470.9825 | 664.0080 | 555.4639 |
| ## | 149 | 454.0582 | 356.6670 | 551.4495 | 433.0654 |
| ## | 150 | 535.2990 | 438.2442 | 632.3539 | 507.6927 |
| ## | 151 | 616.1485 | 519.1033 | 713.1937 | 548.0493 |
| ## | 152 | 698.5211 | 601.7043 | | 736.3741 |
| | | | | 795.3380 | |
| ## | 153 | 626.0148 | 520.9897 | 731.0400 | 521.3435 |
| ## | 154 | 618.7004 | 521.0646 | 716.3361 | 589.1671 |
| ## | 155 | 703.7080 | 607.3421 | 800.0739 | 749.2599 |
| ## | 156 | 449.2545 | 351.6147 | 546.8943 | 584.7224 |
| ## | 157 | 609.2119 | 512.3566 | 706.0671 | 564.8569 |
| ## | 158 | 550.1804 | 454.0557 | 646.3052 | 569.0468 |
| ## | 159 | 616.3902 | 518.8602 | 713.9201 | 629.8096 |
| ## | 160 | 566.5545 | 470.9402 | 662.1689 | 513.8385 |
| ## | 161 | 508.9498 | 412.6860 | 605.2135 | 527.1536 |
| ## | 162 | 455.2180 | 359.3009 | 551.1351 | 482.2035 |
| ## | 163 | 419.2786 | 321.7618 | 516.7953 | 436.4769 |
| ## | 164 | 636.8767 | 539.0587 | 734.6948 | 646.6033 |
| ## | 165 | 554.8222 | 457.5100 | 652.1344 | 622.5434 |
| ## | 166 | 547.6992 | 448.3446 | 647.0537 | 596.5075 |
| ## | 167 | 608.6173 | 511.6731 | 705.5616 | 665.0947 |
| ## | 168 | 504.1788 | 408.5231 | 599.8345 | 491.6161 |
| ## | 169 | 607.7702 | 510.9684 | 704.5720 | 583.2814 |
| ## | 170 | 511.0990 | 415.3239 | 606.8741 | 606.5028 |
| | | | | | 584.8640 |
| ## | 171 | 595.6453 | 498.0059 | 693.2847 | |
| ## | 172 | 622.3756 | 522.2213 | 722.5299 | 635.3163 |
| ## | 173 | 542.2080 | 445.2812 | 639.1349 | 522.5450 |
| ## | 174 | 644.3270 | 548.3189 | 740.3352 | 678.3172 |
| ## | 175 | 544.5838 | 447.3856 | 641.7819 | 457.4744 |
| ## | 176 | 717.6419 | 621.8523 | 813.4315 | 695.6921 |
| ## | 177 | 784.9967 | 686.4029 | 883.5905 | 764.0372 |
| ## | 178 | 534.3521 | 437.3839 | 631.3203 | 413.4732 |
| ## | 179 | 554.9386 | 458.6314 | 651.2457 | 624.3904 |
| ## | 180 | 669.6159 | 573.7169 | 765.5148 | 641.7423 |
| ## | 181 | 551.6739 | 455.7206 | 647.6271 | 512.4366 |
| ## | 182 | 725.0205 | 628.4656 | 821.5755 | 707.5731 |
| | | | | | - · · - |

```
## 183
           433.3519
                        336.0903
                                     530.6135
                                                440.1676
## 184
           738.3554
                        642.3501
                                     834.3607
                                                739.5392
                                     753.4721
                                                694.3444
## 185
           655.9110
                        558.3499
## 186
           679.9263
                        584.1010
                                     775.7515
                                                763.0419
## 187
           545.2586
                        447.9477
                                     642.5696
                                                548.6716
## 188
           630.9500
                        535.1712
                                     726.7287
                                                704.5717
## 189
           581.8916
                        485.0386
                                     678.7447
                                                551.4120
## 190
                        468.3097
                                     665.9114
                                                517.9553
           567.1105
           578.6743
## 191
                        481.9114
                                     675.4372
                                                638.0033
## 192
           562.8784
                        466.8617
                                     658.8950
                                                533.7296
## 193
           594.3014
                        497.7050
                                     690.8978
                                                655.0662
## 194
           524.6465
                        428.7922
                                     620.5007
                                                484.9591
## 195
           465.0755
                        366.1594
                                     563.9916
                                                475.7100
## 196
           661.7267
                        564.9618
                                     758.4917
                                                727.0107
## 197
           534.8946
                        438.5219
                                     631.2673
                                                428.9199
## 198
           565.3133
                        467.9877
                                     662.6389
                                                572.6965
## 199
           639.8759
                        544.0866
                                     735.6652
                                                761.7539
## 200
           505.7321
                        409.0360
                                     602.4283
                                                480.8677
  'data.frame':
                     191 obs. of
                                  4 variables:
                          695 589 643 584 620 ...
##
    $ fitted value: num
##
    $ lower_bound : num
                          597 493 548 487 523 ...
    $ upper_bound : num
                          793 685 739 682 717 ...
##
    $ true value
                  : num
                          659 585 640 605 620 ...
```

After filtering, we see that 191 of 200 (191/200 = 95.5%) values of CreditScore are in the 95% predictive intervals given by our model *fit5*. We can say that 95.5% individuals lie in the predictive interval, which is a high rate. However, we could not infer causality here.

```
## [1] "num of individual correctly classified = 174.000000"
```

The proportion of individuals who are correctly classified by our model fit5 is 174/200 = 87%.

All in all, our model fit5 is sufficient.

Summary

The model we build is: $CreditScore \sim Status + (log(Duration))^2 + History + Purpose + (log(Amount))^2 + Savings + Disposable + Personal + OtherParties + log(Age) + Plans + Housing + Telephone + Foreign and corresponding coefficients are:$

| ## | (Intercept) | StatusNegative | StatusNone |
|----|------------------------|--------------------------|------------------------|
| ## | 642.67278580 | -50.33864585 | 37.80254324 |
| ## | StatusSmall | <pre>I(Duration^2)</pre> | HistoryB |
| ## | -30.63848211 | -5.05928694 | -1.71064194 |
| ## | ${	t HistoryC}$ | HistoryD | HistoryE |
| ## | 47.43690750 | 48.61099645 | 80.96959777 |
| ## | PurposeDomestic | PurposeEducation | PurposeFurniture |
| ## | -24.04206997 | -53.05132330 | -0.65449404 |
| ## | ${\tt PurposeNewCar}$ | PurposeOther | PurposeRepairs |
| ## | -46.39521729 | -17.52376866 | -26.72275168 |
| ## | PurposeTelevision | PurposeTraining | ${\tt PurposeUsedCar}$ |
| ## | 2.33951122 | 60.86332382 | 37.63425410 |
| ## | <pre>I(Amount^2)</pre> | SavingsLow | ${\tt SavingsMedium}$ |
| ## | -1.50658221 | -13.21931180 | 0.09274299 |

| ## | SavingsUnknown | SavingsVeryLarge | Disposable2 |
|----|---------------------|------------------|---------------------------------|
| ## | 25.96072737 | 61.98825705 | -12.53188250 |
| ## | Disposable3 | Disposable4 | PersonalF:Single |
| ## | -27.68161822 | -42.74550056 | 7.66456101 |
| ## | PersonalM:DivSepMar | PersonalM:Single | ${\tt Other Parties Guarantor}$ |
| ## | -13.69298484 | 29.91992387 | 61.43832784 |
| ## | OtherPartiesNone | Age | PlansNone |
| ## | 12.31840746 | 16.45256118 | 32.60000098 |
| ## | PlansStores | HousingRent | ${\tt HousingRentFree}$ |
| ## | 12.05621218 | -17.08723904 | -2.90474034 |
| ## | TelephoneYes | ForeignYes | |
| ## | 12.83855854 | -54.70072304 | |

We found strong evidence between CreditScore and factors like Status, History, Purpose, Savings, Personal, Disposable, OtherParties, Plans, Housing, Telephone, Foreign. Specifically, applicant with Status (None) or History (E) or Purpose (Training) or Savings (Verylarge) or Disposable (3) or Personal (Single) or OtherParties (Guarantor) or Plans (None) or Housing (Own) or Telephone (Yes) or Foreign (No) has a higher CreditScore, which could be the basis of lending decision. Moreover, we see that applicant who requests lower amount with shorter duration seems to have higher credit score and applicant who requests lower amount with identity of a non-foreign worker has a higher credit score and applicant with worse previous loan history has higher credit score, which might due to correlation between History and Amount, but the causality is to be determined. For continuous variables, Age has a strong negative association with CreditScore while Duration and Amount have strong negative association with CreditScore, but the causality is to be determined.

After prediction, we found our model is much better than the full model by considering the MSE. We also found our 95% predictive intervals contains 191 among 200 samples, which suggests a considerable match. The proportion of the individuals correctly classified is 87%.

In conclusion, Duration, Amount and Age therefore seem the most plausible explanation for differences in CreditScore. We note the significant association between the other variables and CreditScore when considered on their own. Moreover, our model could be improved by considering the correlations between factors and continuous variables, such as Foreign and Duration, History and Amount, Duration and Amount, etc. For instance, adding interactions between variables might increase the accuracy of our model.

Finally, there could be other important variables affecting credit score that we haven't observed and a causal link can not be inferred based on this study alone, more samples and further tests are required.