Homework 3: Actuators

24-775 Robot Design & Experimentation

Name:	Peize	Hong	
	-		

You are designing an electric wheelchair for a friend, and he has asked for you to make one that can win a drag race. To do this you must select the motor and gearbox so that the wheelchair can travel the farthest in 5 seconds. The specifications are:

Mass of wheelchair + occupant: 100 kg

Radius of wheel: 0.5 m Battery voltage: 30 V

You may ignore friction, damping, inductance, thermodynamics, and aerodynamics to only consider the inertial terms. Upload your code or hand calculations with your answers.

- a) Write out the equations of motion for this system, based on the acceleration of the wheelchair and the basic motor model.
- b) Either algebraically, symbolically, or numerically solve for the forward displacement of the wheelchair with the following conditions:

Motor: Maxon EC45-Flat 70W 30V, part # 402685 (data sheet attached)

Gear ratio: 1:1

Initial Conditions: x = 0, dx/dt = 0

How far did the wheelchair travel? You may use Matlab, Python, or other software.

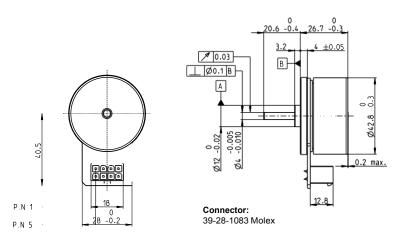
Hint: In Matlab, instructions on solving differential equations symbolically:

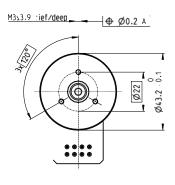
https://www.mathworks.com/help/symbolic/solve-a-single-differential-equation.html and numerically:

https://www.mathworks.com/help/matlab/math/solve-nonstiff-odes.html

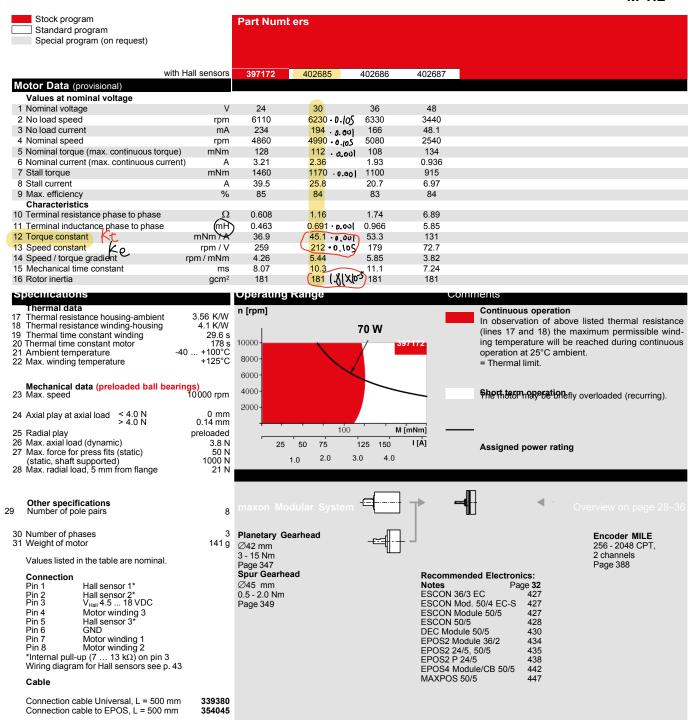
- c) Plot the final displacement for all gear ratios from 1:1 to 100:1. What is the optimal gear ratio?
- d) Now consider the motor selection question. Of the four EC45-Flat 70W motors in the attached datasheet, which will move the wheelchair the farthest in 5 seconds? (Pair each motor with its own optimal gear ratio)
- e) Gears only come in certain ratios. Based on the options for GP 42 C gearboxes in the attached datasheet, what is the optimal motor+gearbox combination?

EC 45 flat Ø42.8 mm, brushless, 70 Watt



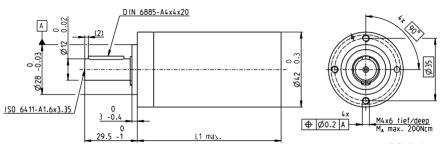


M 1:2



Planetary Gearhead GP 42 C Ø42 mm, 3-15 Nm

Ceramic Version



Technical Data				
Planetary Gearhead		stra	aight t	teeth
Output shaft		stair	nless	steel
Bearing at output	preload			
Radial play, 12 mm from fla		max	. 0.06	i mm
Axial play at axial load	< 5 N			mm (
	> 5 N	ma	ıx. 0.3	
Max. axial load (dynamic)				50 N
Max. force for press fits			3	00 N
Direction of rotation, drive				=
Max. continuous input spee	ed		8000	
Recommended temperature	e range	-40)+10	00°C
Number of stages Max. radial load, 12 mm	1	2	3	4
from flange	120 N 240	N 360	N 36	30 N

M 1:2

Stock program Standard program Special program (on request)			Part Numbers									
			203113		203119	203120		203129				
1	Reduction		3.5:1	12:1	26:1	43:1	81:1	156:1	150:1	285:1	441:1	756:1
2	Absolute reduction		1/2	49/4	26	343/8	2197/27	156	2401/16	15379/54	441	756
10	Mass inertia	gcm ²	14	15	9.1	15	9.4	9.1	15	15	14	14
3	Max. motor shaft diameter	mm	10	10	8	10	8	8	10	10	10	10
	Part Numbers		203114	203116	260552*	203121	203125	260553*	203130	203134	203138	203142
1	Reduction		4.3:1	15:1	36:1	53:1	91:1	216:1	186:1	319:1	488:1	936:1
2	Absolute reduction		13/3	91/6	36/1	637/12	91	216/1	4459/24	637/2	4394/9	936
10	Mass inertia	gcm ²	9.1	15	5.0	15	15	5.0	15	15	9.4	9.1
3	Max. motor shaft diameter	mm	8	10	4	10	10	4	10	10	8	8
	Part Numbers		260551*	203117		203122	203126		203131	203135	203139	260554
1	Reduction		6:1	19:1		66:1	113:1		230:1	353 :1	546:1	1296:1
2	Absolute reduction		%	169/9		1183/18	338/3		8281/36	28561/81	546	1296/1
10	Mass inertia	gcm ²	4.9	9.4		15	9.4		15	9.4	14	5.0
3	Max. motor shaft diameter	mm	4	8		10	8		10	8	10	4
	Part Numbers			203118		203123	203127		203132	203136	203140	
	Reduction			21:1		74:1	126:1		257:1	394:1	676:1	
2	Absolute reduction			21		147/2	126		1029/4	1183/3	676	
10	Mass inertia	gcm ²		14		15	14		15	15	9.1	
3	Max. motor shaft diameter	mm		10		10	10		10	10	8	
4	Number of stages		1	2	2	3	3	3	4	4	4	4
5	Max. continuous torque	Nm	3.0	7.5	7.5	15.0	15.0	15.0	15.0	15.0	15.0	15.0
6	Max. intermittent torque at gear output	Nm	4.5	11.3	11.3	22.5	22.5	22.5	22.5	22.5	22.5	22.5
7	Max. efficiency	%	90	81	81	72	72	72	64	64	64	64
8	Weight	g	260	360	360	460	460	460	560	560	560	560
9	Average backlash no load	0	0.6	0.8	8.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
11	Gearhead length L1** *no combination with EC 45 (150/250 W) and EC-i 40 **for EC 45 flat L1 is -3.6 mm	mm	41.0	55.5	55.5	70.0	70.0	70.0	84.5	84.5	84.5	84.5

overall length	04	overall length													
maxon Modula + Motor	Page	+ Sensor	Page Br	ake	Page	Overall le	ength [mr	n] = Motor le	ength + gear	head length	+ (sensor/b	orake) + asse	embly parts		
RE 35, 90 W	130					112.1	126.6	126.6	141.1	141.1	141.1	155.6	155.6	155.6	155.6
RE 35, 90 W	130	MR	405			123.5	138.0	138.0	152.5	152.5	152.5	167.0	167.0	167.0	167.0
RE 35, 90 W	130	HED 5540	413/415			132.8	147.3	147.3	161.8	161.8	161.8	176.3	176.3	176.3	176.3
RE 35, 90 W	130	DCT 22	421			130.2	144.7	144.7	159.2	159.2	159.2	173.7	173.7	173.7	173.7
RE 35, 90 W	130			AB 28	458	148.2	162.7	162.7	177.2	177.2	177.2	191.7	191.7	191.7	191.7
RE 35, 90 W	130	HED 5540	413/415	AB 28	458	165.4	179.9	179.9	194.4	194.4	194.4	208.9	208.9	208.9	208.9
RE 40, 150 W	132	_				112.1	126.6	126.6	141.1	141.1	141.1	155.6	155.6	155.6	155.6
RE 40, 150 W	132	MR	405			123.5	138.0	138.0	152.5	152.5	152.5	167.0	167.0	167.0	167.0
RE 40, 150 W	132	HED 5540	413/416			132.8	147.3	147.3	161.8	161.8	161.8	176.3	176.3	176.3	176.3
RE 40, 150 W	132	HEDL 9140	419			166.2	180.7	180.7	195.2	195.2	195.2	209.7	209.7	209.7	209.7
RE 40, 150 W	132			AB 28	458	148.2	162.7	162.7	177.2	177.2	177.2	191.7	191.7	191.7	191.7
RE 40, 150 W	132			AB 28	459	156.2	170.7	170.7	185.2	185.2	185.2	199.7	199.7	199.7	199.7
RE 40, 150 W	132	HED 5540	413/416	AB 28	458	165.4	179.9	179.9	194.4	194.4	194.4	208.9	208.9	208.9	208.9
RE 40, 150 W	132	HEDL 9140	419	AB 28	459	176.7	191.2	191.2	205.7	205.7	205.7	220.2	220.2	220.2	220.2
EC 40, 170 W	219					121.1	135.6	135.6	150.1	150.1	150.1	164.6	164.6	164.6	164.6
EC 40, 170 W	219	HED 5540	414/416			144.5	159.0	159.0	173.5	173.5	173.5	188.0	188.0	188.0	188.0
EC 40, 170 W	219	Res 26	422			148.3	162.8	162.8	177.3	177.3	177.3	191.8	191.8	191.8	191.8
EC 40, 170 W	219			AB 32	460	163.8	178.3	178.3	192.8	192.8	192.8	207.3	207.3	207.3	207.3
EC 40, 170 W	219	HED 5540	414/416	AB 32	460	182.2	196.7	196.7	211.2	211.2	211.2	225.7	225.7	225.7	225.7
EC 45, 150 W	220	_				152.3	166.8	166.8	181.3	181.3	181.3	195.8	195.8	195.8	195.8
EC 45, 150 W	220	HEDL 9140	419			167.9	182.4	182.4	196.9	196.9	196.9	211.4	211.4	211.4	211.4
EC 45, 150 W	220	Res 26	422			152.3	166.8	166.8	181.3	181.3	181.3	195.8	195.8	195.8	195.8
EC 45, 150 W	220			AB 28	459	159.7	174.2	174.2	188.7	188.7	188.7	203.2	203.2	203.2	203.2
EC 45, 150 W	220	HEDL 9140	419	AB 28	459	176.7	191.2	191.2	205.7	205.7	205.7	220.2	220.2	220.2	220.2
EC 45, 250 W	221					185.1	199.6	199.6	214.1	214.1	214.1	228.6	228.6	228.6	228.6
EC 45, 250 W	221	HEDL 9140	419			200.7	215.2	215.2	229.7	229.7	229.7	244.2	244.2	244.2	244.2
EC 45, 250 W	221	Res 26	422			185.1	199.6	199.6	214.1	214.1	214.1	228.6	228.6	228.6	228.6
EC 45, 250 W	221			AB 28	459	192.5	207.0	207.0	221.5	221.5	221.5	236.0	236.0	236.0	236.0
EC 45, 250 W	221	HEDL 9140	419	AB 28	459	209.5	224.0	224.0	238.5	238.5	238.5	253.0	253.0	253.0	253.0

May 2017 edition / subject to change maxon gear 345

Option
With Cable and Connector
(Ambient temperature -20 ... +100°C)

 (α)

maxon EC motor 2007

Vs: source voltage Vx: resistance voltage i: current Kv: Speed Constant J: MoI r=wheel radius Ve: E.M.F voltage T: Input to rque w: Rotatoral speed Kt: torque constant R: Resistance Tt: Output torque [Le: electric constant

EOM Electrical:

Eom Mechanical

(b)
$$\begin{cases} \frac{1}{4} - 4 & k_{V} = 212 \\ \frac{1}{4} - 212 & k_{V} = 212 \end{cases}$$

$$\begin{cases} k_{e} = 0.0449 \\ k_{V} = 0.045 \end{cases}$$

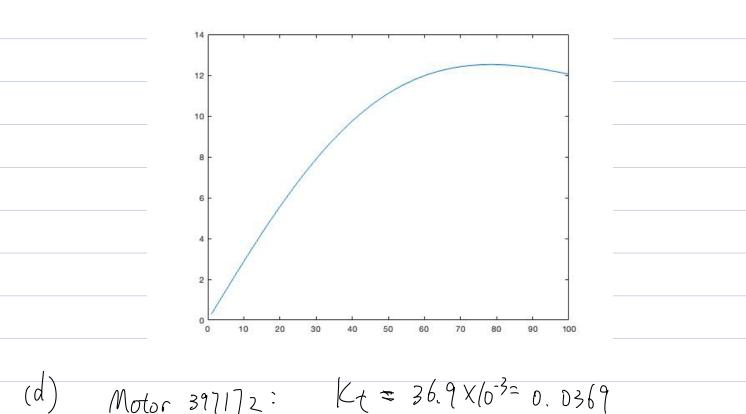
$$\begin{cases} 0.045 \cdot 30 & 0.045 \cdot 0.0449 \end{cases}$$

$$\frac{0.045| \cdot 30}{(18|x|0^{-1}+25) \cdot 1.16} = \frac{0.045| \cdot 0.0449}{(18|x|0^{-1}+25) \cdot 1.16} \theta = \theta$$

$$\begin{cases} \chi(0) = 0 \\ \dot{\chi}(0) = 0 \end{cases}$$

$$0.0466 - 6.98 \times 10^{5} 0 = 0$$

 $t = 5 \times 9.2916 m$



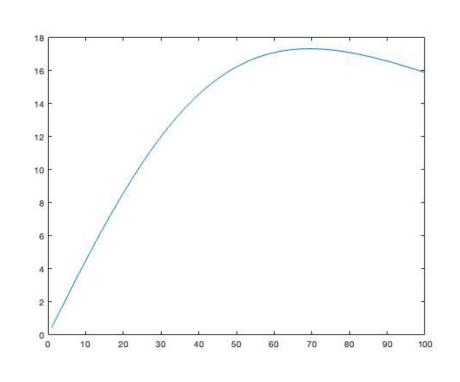
(d) Motor 397172:
$$K_{t} = 36.9 \times 10^{-3} = 0.0369$$

 $K_{e} = \frac{1}{259 \cdot 0.105} = 0.0368 2 \text{ Kt}$

R = 0.608

Optimal N= 69

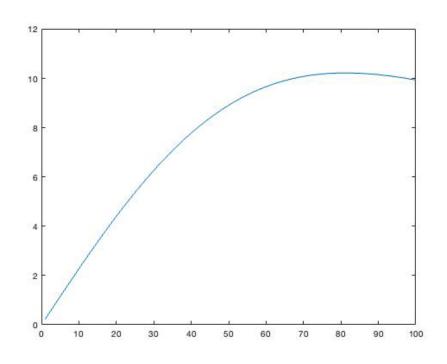
Max dist = 17.31m



Motor 402686 Kt=0.0533 Ke=Kt=0.0533 R= 1.74

Optimal N=81

Max-dist = 10.22m



Motor 40268] Kt=0-13/=Ke R=6.89 Opt N = 66 Max dist = 5.13m

