Robert Collins CSE486, Penn State

Lecture 18: Generalized Stereo: Epipolar Geometry

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Generalized Stereo

Key idea: Any two images showing an overlapping view of the world can be treated as a stereo pair...

... we just have to figure out how the two views are related.

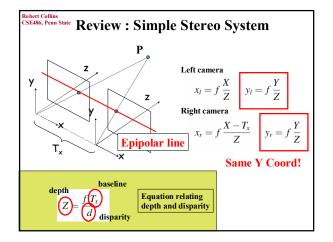
Some of the most "beautiful" math in vision concerns describing how multiple views are related, geometrically.

CSE486, Penn State Recall: Epipolar Constraint

Important Stereo Vision Concept:

Given a point in the left image, we don't have to search the whole right image for a corresponding point.

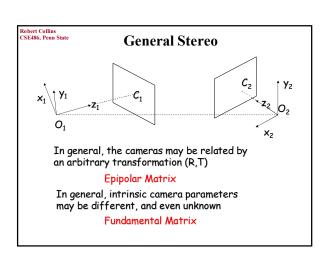
The "epipolar constraint" reduces the search space to a one-dimensional line.



CSE486, Penn State Review: Epipolar Constraint

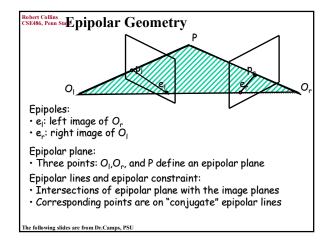


Corresponding features are constrained to lie along conjugate epipolar lines (on the same row in the case of our simple setup).



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EPIPOLAR GEOMETRY



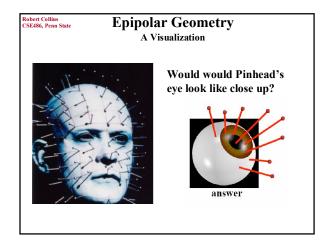
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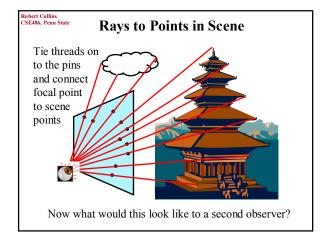
BORING!!!

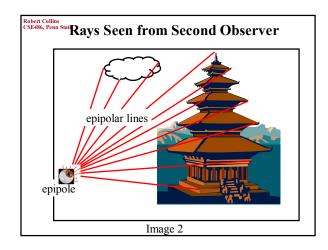
Let's try again...

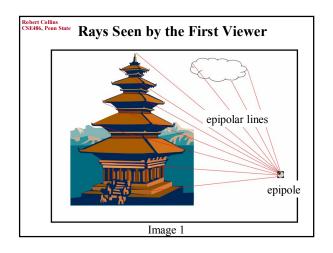
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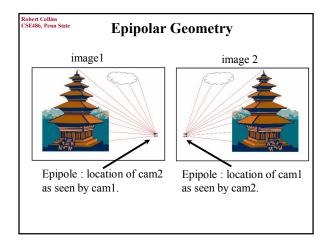
EPIPOLAR GEOMETRY

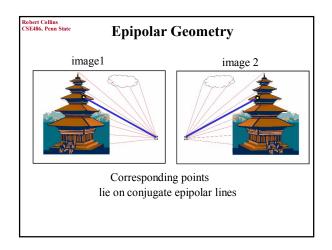


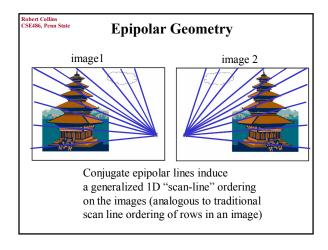


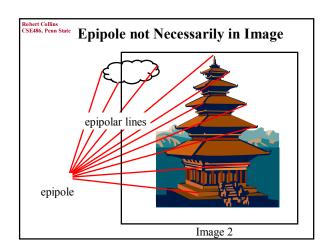


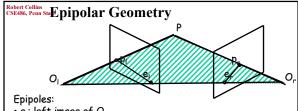










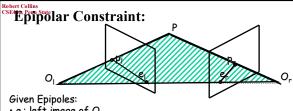


- · e1: left image of Or
- · er: right image of O1

Epipolar plane:

- Three points: O₁,O_r, and P define an epipolar plane
- Epipolar lines and epipolar constraint:
- Intersections of epipolar plane with the image planes
- · Corresponding points are on "conjugate" epipolar lines

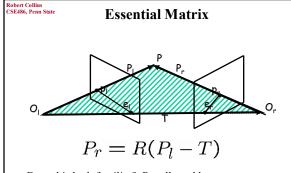
The following slides are from Dr.Camps, PSU



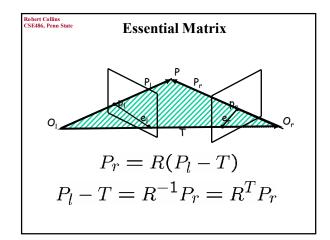
- · e : left image of Or
- · e_r: right image of O

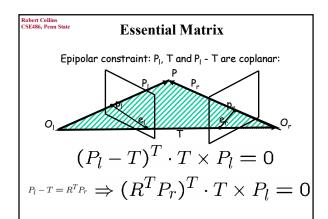
Given pi:

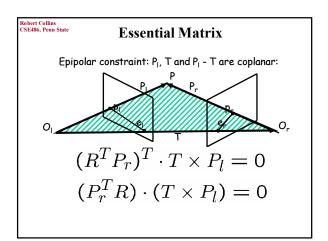
- ·consider its epipolar line: p, e,
- -find epipolar plane: $O_{\rm l}$, $p_{\rm l}$, $e_{\rm l}$ -intersect the epipolar plane with the right image plane
- ·search for pr on the right epipolar line

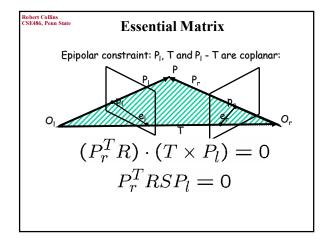


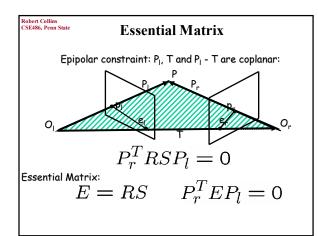
Does this look familiar? Recall world to camera transformation by (R,T). Here, we are transforming from camera to camera.











Robert Collins CSE486, Penn State Essential Matrix Properties

$$E = RS$$

- has rank 2
- depends only on the EXTRINSIC Parameters (R & T)

We will discuss more of the wonderful properties of this matrix next time...