MTH9845 Risk Management Model Validation report

- · Author: Hongchao Pan, Yu Sun
- Kernel version: Python 3.5
- Packages: numpy, pandas, matplotlib, scipy, math
- · Data:
 - Volatility matrices of EUR/USD and GBP/USD were obtained from Bloomberg
 - Benchmark prices were obtained from Bloomberg pricing model and investing.com
 - Interest rates (foreign and domestic) were obtained from tradingeconomics.com
- · Notes:

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In [1]: # Loading packages
  import pandas as pd
  import numpy as np
  import matplotlib.pyplot as plt
  from scipy.stats import norm
  import math
```

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In [2]: # Get the data from excel file
    df=pd.read_excel(io='Testing-data/Vol-matrix.xlsx',sheetname=0,parse_col
    s="A:F",skiprows=2)
    df['25DC']=df['ATM']+df['25DBF']+0.5*df['25DRR']
    df['25DP']=df['ATM']+df['25DBF']-0.5*df['25DRR']
    df['10DC']=df['ATM']+df['10DBF']+0.5*df['10DRR']
    df['10DP']=df['ATM']+df['10DBF']-0.5*df['10DRR']
    df.iloc[:,1:]=df.iloc[:,1:]/100 # Change the percentage number to decim
    al
    df
```

Out[2]:

	Mid Vol	ATM	25DRR	25DBF	10DRR	10DBF	25DC	25DP	10DC	10
0	EUR/USD	0.071125	0.0009	0.001925	0.001450	0.00570	0.0735	0.0726	0.077550	0.0
1	GBP/USD	0.067125	-0.0028	0.002275	-0.004825	0.00635	0.0680	0.0708	0.071063	0.0

```
In [4]: # Implement the Black-Scholes model in FX derivetives
        # The volatility used for BS is ATM vol
        # Define d1
        def d_1(t,S,K,T,sigma,rd,rf):
            param t: spot time, usually is 0
            param S: spot price: exchange rate
            param K: given strike
            param T: maturity with unit year
            param sigma: volatility
            param rd: domestic interest rate
            param rf: foreign interest rate
            return d1 in BS formula
            return (math.log(S/K)+(rd-rf+0.5*math.pow(sigma,2))*(T-t))/(sigma*ma
        th.sqrt(T-t))
        def BS FX(t,S,K,T,sigma,rd,rf,flag,optflag):
            param t: spot time, usually is 0
            param S: spot price: exchange rate
            param K: given strike
            param T: maturity with unit year
            param sigma: volatility
            param rd: domestic interest rate
            param rf: foreign interest rate
            param flag: call/put indicator
            param optflag: output price or greeks
            d1=d 1(t,S,K,T,sigma,rd,rf)
            d2=d1-sigma*np.sgrt(T-t)
            call price=S*math.exp(-rf*(T-t))*norm.cdf(d1)-K*math.exp(-rd*(T-
        t))*norm.cdf(d2)
            put price=K*math.exp(-rd*(T-t))*norm.cdf(-d2)-S*math.exp(-rf*(T-
        t))*norm.cdf(-d1)
            vega=S*math.exp(-rf*(T-t))*math.sqrt(T-
        t) *math.exp(-0.5*d1*d1)/math.sqrt(2*math.pi)
            if optflag.upper() =='VEGA':
                return vega
            if optflag.upper() == 'PRICE':
                if flag.upper() == 'CALL':
                    return call price
                if flag.upper() == "PUT":
                    return put price
```

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In [5]: # Define functions to compute Vanna and Volga
        def Vanna Volga(t,S,K,T,sigma,rd,rf,flag,optflag):
            param t: spot time, usually is 0
            param S: spot price: exchange rate
            param K: given strike
            param T: maturity with unit year
            param sigma: volatility
            param rd: domestic interest rate
            param rf: foreign interest rate
            param flag: call/put indicator
            param optflag: output Vanna or Volga
            d1=d 1(t,S,K,T,sigma,rd,rf)
            d2=d1-sigma*np.sqrt(T-t)
            vega=BS FX(t,S,K,T,sigma,rd,rf,flag,"VEGA")
            vanna=-vega*d2/(S*sigma*np.sgrt(T-t))
            volga= vega*d1*d2/sigma
            if optflag.upper()=="VANNA":
                return vanna
            if optflag.upper()=="VOLGA":
                return volga
```

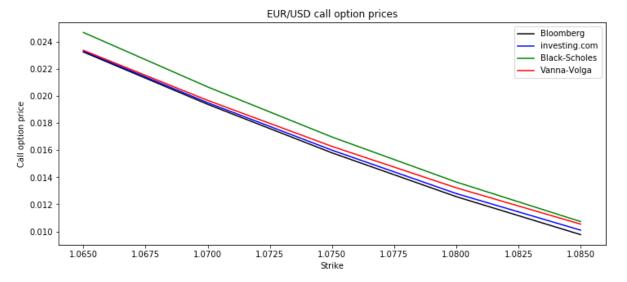
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In [6]: # Define function to compute Kc and Kp
        def K cp(t,S,T,sigma,rd,rf,flag,Delta):
            param t: spot time, usually is 0
            param S: spot price: exchange rate
            param T: maturity with unit year
            param sigma: volatility
            param rd: domestic interest rate
            param rf: foreign interest rate
            param flag: call/put indicator
            param Delta: Delta 0.25 or 0.1
            if flag.upper()=="PUT":
                phi=1
            if flag.upper()=="CALL":
                phi=1
            K=S*np.exp((rd-rf)*T-phi*sigma*np.sqrt(T)*norm.ppf(phi*Delta)+0.5*si
        gma*sigma*T)
             print(S,rd,rf,phi,sigma,T,Delta)
            return K
```

```
# Implement Vanna-Volga model
def VannaVolga Pricing(K ATMs, S0, T, rd, rf, vols):
    param vols: contains vol of ATM, 25DC, 25DP, 10DC, 10DP
    price=[]
    # Compute the K25C, K25P, K10C, K10P
    K25C=K cp(0,S0,T,vols[1],rd,rf,"CALL",0.25)
    K25P=K cp(0,S0,T,vols[2],rd,rf,"PUT",0.25)
    K10C=K_cp(0,S0,T,vols[3],rd,rf,"CALL",0.1)
    K10P=K cp(0,S0,T,vols[4],rd,rf,"PUT",0.1)
    for K in K ATMs:
        BS X=BS FX(0,S0,K,T,vols[0],rd,rf,"CALL","PRICE")
        vanna X=Vanna Volga(0,S0,K,T,vols[0],rd,rf,"CALL","VANNA")
        volga_X=Vanna_Volga(0,S0,K,T,vols[0],rd,rf,"CALL","VOLGA")
        vanna_25=Vanna_Volga(0,S0,K,T,vols[1],rd,rf,"CALL","VANNA")
        volga 25=Vanna Volga(0,S0,K,T,vols[1],rd,rf,"CALL","VOLGA")
        vanna 10=Vanna Volga(0,S0,K,T,vols[2],rd,rf,"CALL","VANNA")
        volga 10=Vanna Volga(0,S0,K,T,vols[2],rd,rf,"CALL","VOLGA")
        BS_25C=BS_FX(0,S0,K25C,T,vols[1],rd,rf,"CALL","PRICE")
        BS_25P=BS_FX(0,S0,K25P,T,vols[2],rd,rf,"PUT","PRICE")
        BS 10C=BS FX(0,S0,K10C,T,vols[3],rd,rf,"CALL","PRICE")
        BS 10P=BS FX(0,S0,K10P,T,vols[4],rd,rf,"PUT","PRICE")
        BS 25CATM=BS FX(0,S0,K25C,T,vols[0],rd,rf,"CALL","PRICE")
        BS_25PATM=BS_FX(0,S0,K25P,T,vols[0],rd,rf,"PUT","PRICE")
        BS 10CATM=BS FX(0,S0,K10C,T,vols[0],rd,rf,"CALL","PRICE")
        BS 10PATM=BS FX(0,S0,K10P,T,vols[0],rd,rf,"PUT","PRICE")
        RR cost25=(BS 25C-BS 25P)-(BS 25CATM-BS 25PATM)
        BF cost25=0.5*(BS 25C+BS 25P)-0.5*(BS 25CATM+BS 25PATM)
        RR cost10=(BS 10C-BS 10P)-(BS 10CATM-BS 10PATM)
        BF cost10=0.5*(BS 10C+BS 10P)-0.5*(BS 10CATM+BS 10PATM)
         print(K10P)
P VV=BS X+vanna X*RR cost25/vanna 25+volga X*BF cost25/volga 25+vanna X*R
R_cost10/vanna_10+volga_X*BF cost10/volga 10
        price.append(P VV)
    return price
```

```
In [8]: # Get the indices of vols
        ind=[1,6,7,8,9]
        vol EURUSD=[df.iloc[0,i] for i in ind ]
        #vol GBPUSD=[df.iloc[1,i] for i in ind ]
        # Get the price of EUR/USD
        price EURUSD=VannaVolga Pricing(K ATMEURUSD,S0s[0],T,rds[0],rfs[0],vol E
        URUSD)
        price EURUSD=[i/S0s[0] for i in price EURUSD]
        # Get the price of GBP/USD
        #price GBPUSD=VannaVolqa Pricing(K ATMGBPUSD,S0s[1],T,rds[1],rfs[1],vol
        GBPUSD)
        #price GBPUSD=[i/S0s[1] for i in price EURUSD]
        # Get the BS price of EUR/USD
        BS EURUSD=
        [BS FX(0,S0s[0],K,T,vol EURUSD[0],rds[0],rfs[0],"CALL","PRICE") for K in
         K ATMEURUSD]
        # Get the BS price of GBP/USD
        #BS GBPUSD=[BS FX(0,S0s[1],K,T,vol GBPUSD[0],rds[1],rfs[1],"CALL","PRIC
        E") for K in K ATMGBPUSD]
```


Out[9]:

	EURUSD Strike	Bloomberg Price	investing.com Price	BS Price	VV Price
0	1.065	0.023241	0.0233	0.024682	0.023363
1	1.070	0.019381	0.0195	0.020663	0.019671
2	1.075	0.015802	0.0160	0.016970	0.016277
3	1.080	0.012571	0.0128	0.013649	0.013224
4	1.085	0.009770	0.0101	0.010733	0.010544



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In [ ]:
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