BayesPy Documentation

Release 0.1

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INTRODUCTION

BayesPy provides tools for Bayesian inference with Python. The user constructs a model as a Bayesian network, observes data and runs posterior inference. The goal is to provide a tool which is efficient, flexible and extendable enough for expert use but also accessible for more casual users.

Currently, only variational Bayesian inference for conjugate-exponential family (variational message passing) has been implemented. Future work includes variational approximations for other types of distributions and possibly other approximate inference methods such as expectation propagation, Laplace approximations, Markov chain Monte Carlo (MCMC) and other methods. Contributions are welcome.

It is recommended to use the latest version from the GitHub master branch. The version in PyPI is quite outdated.

1.1 Project information

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BayesPy including the documentation is licensed under Version 3.0 of the GNU General Public License. See LICENSE file for a text of the license or visit http://www.gnu.org/copyleft/gpl.html.

- Documentation:
 - http://bayespy.org
 - PDF file
 - RST format in doc directory
- · Repository: https://github.com/bayespy/bayespy.git
- Bug reports: https://github.com/bayespy/bayespy/issues
- Mailing list: bayespy@googlegroups.com
- IRC: #bayespy @ freenode
- Author: Jaakko Luttinen jaakko.luttinen@iki.fi
- Latest release:
- Build status:
- Unit test coverage:

1.2 Similar projects

VIBES (http://vibes.sourceforge.net/) allows variational inference to be performed automatically on a Bayesian network. It is implemented in Java and released under revised BSD license.

Bayes Blocks (http://research.ics.aalto.fi/bayes/software/) is a C++/Python implementation of the variational building block framework. The framework allows easy learning of a wide variety of models using variational Bayesian learning. It is available as free software under the GNU General Public License.

Infer.NET (http://research.microsoft.com/infernet/) is a .NET framework for machine learning. It provides message-passing algorithms and statistical routines for performing Bayesian inference. It is partly closed source and licensed for non-commercial use only.

PyMC (https://github.com/pymc-devs/pymc) provides MCMC methods in Python. It is released under the Academic Free License.

OpenBUGS (http://www.openbugs.info) is a software package for performing Bayesian inference using Gibbs sampling. It is released under the GNU General Public License.

Dimple (http://dimple.probprog.org/) provides Gibbs sampling, belief propagation and a few other inference algorithms for Matlab and Java. It is released under the Apache License.

Stan (http://mc-stan.org/) provides inference using MCMC with an interface for R and Python. It is released under the New BSD License.

PBNT - Python Bayesian Network Toolbox (http://pbnt.berlios.de/) is Bayesian network library in Python supporting static networks with discrete variables. There was no information about the license.

CHAPTER

TWO

USER GUIDE

2.1 Installation

BayesPy is a Python 3 package and it can be installed from PyPI or the latest development version from GitHub. The instructions below explain how to set up the system by installing required packages, how to install BayesPy and how to compile this documentation yourself. However, if these instructions contain errors or some relevant details are missing, please file a bug report at https://github.com/bayespy/bayespy/issues.

2.1.1 Installing requirements

BayesPy requires Python 3.2 (or later) and the following packages:

- NumPy (>=1.8.0),
- SciPy (>=0.13.0)
- matplotlib (>=1.2)
- h5py

Ideally, a manual installation of these dependencies is not required and you can skip to the next section "Installing Bayespy". However, there are several reasons why the installation of BayesPy as described in the next section won't work because of your system. Thus, this section tries to give as detailed and robust a method of setting up your system such that the installation of BayesPy should work.

A proper installation of the dependencies for Python 3 can be a bit tricky and you may refer to http://www.scipy.org/install.html for more detailed instructions about the SciPy stack. If your system has an older version of any of the packages (NumPy, SciPy or matplotlib) or it does not provide the packages for Python 3, you may set up a virtual environment and install the latest versions there. To create and activate a new virtual environment, run

```
virtualenv -p python3 --system-site-packages ENV
source ENV/bin/activate
```

If you have relevant system libraries installed (C compiler, Python development files, BLAS/LAPACK etc.), you may be able to install the Python packages from PyPI. For instance, on Ubuntu (>= 12.10), you may install the required system libraries for each package as:

```
sudo apt-get build-dep python3-numpy
sudo apt-get build-dep python3-scipy
sudo apt-get build-dep python3-matplotlib
sudo apt-get build-dep python-h5py
```

Then installation/upgrade from PyPI should work:

```
pip install distribute --upgrade
pip install numpy --upgrade
pip install scipy --upgrade
pip install matplotlib --upgrade
pip install h5py
```

Note that Matplotlib requires a quite recent version of Distribute (>=0.6.28). If you have problems installing any of these packages, refer to the manual of that package.

2.1.2 Installing BayesPy

If the system has been properly set up and the virtual environment is activated (optional), latest release of BayesPy can be installed from PyPI simply as

```
pip install bayespy
```

If you want to install the latest development version of BayesPy, use GitHub instead:

```
pip install https://github.com/bayespy/bayespy/archive/master.zip
```

It is recommended to run the unit tests in order to check that BayesPy is working properly. Thus, install Nose and run the unit tests:

```
pip install nose nosetests bayespy
```

2.1.3 Compiling documentation

This documentation can be found at http://bayespy.org/. The documentation source files are readable as such in reStructuredText format in doc/source/ directory. It is possible to compile the documentation into HTML or PDF yourself. In order to compile the documentation, Sphinx is required and a few extensions for it. Those can be installed as:

```
pip install sphinx sphinxcontrib-tikz sphinxcontrib-bayesnet sphinxcontrib-bibtex
```

In addition, the numpydoc extension for Sphinx is required. However, the latest stable release (0.4) does not support Python 3, thus one needs to install the development version:

```
pip install https://github.com/numpy/numpydoc/archive/master.zip
```

In order to visualize graphical models in HTML, you need to have pnmcrop. On Ubuntu, it can be installed as

```
sudo apt-get install netpbm
```

The documentation can be compiled to HTML and PDF by running the following commands in the doc directory:

```
make html
make latexpdf
```

You can also run doctest to test code snippets in the documentation:

```
make doctest
```

or in the docstrings:

```
nosetests --with-doctest bayespy
```

2.2 Quick start guide

This short guide shows the key steps in using BayesPy for variational Bayesian inference by applying BayesPy to a simple problem. The key steps in using BayesPy are the following:

- · Construct the model
- Observe some of the variables by providing the data in a proper format
- · Run variational Bayesian inference
- Examine the resulting posterior approximation

To demonstrate BayesPy, we'll consider a very simple problem: we have a set of observations from a Gaussian distribution with unknown mean and variance, and we want to learn these parameters. In this case, we do not use any real-world data but generate some artificial data. The dataset consists of ten samples from a Gaussian distribution with mean 5 and standard deviation 10. This dataset can be generated with NumPy as follows:

```
>>> import numpy as np
>>> data = np.random.normal(5, 10, size=(10,))
```

2.2.1 Constructing the model

Now, given this data we would like to estimate the mean and the standard deviation as if we didn't know their values. The model can be defined as follows:

$$p(\mathbf{y}|\mu,\tau) = \prod_{n=0}^{9} \mathcal{N}(y_n|\mu,\tau)$$
$$p(\mu) = \mathcal{N}(\mu|0, 10^{-6})$$
$$p(\tau) = \mathcal{G}(\tau|10^{-6}, 10^{-6})$$

where \mathcal{N} is the Gaussian distribution parameterized by its mean and precision (i.e., inverse variance), and \mathcal{G} is the gamma distribution parameterized by its shape and rate parameters. Note that we have given quite uninformative priors for the variables μ and τ . This simple model can also be shown as a directed factor graph: This model can be

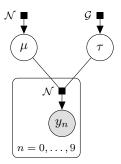


Figure 2.1: Directed factor graph of the example model.

constructed in BayesPy as follows:

```
>>> from bayespy.nodes import GaussianARD, Gamma
>>> mu = GaussianARD(0, 1e-6)
>>> tau = Gamma(1e-6, 1e-6)
>>> y = GaussianARD(mu, tau, plates=(10,))
```

This is quite self-explanatory given the model definitions above. We have used two types of nodes GaussianARD and Gamma to represent Gaussian and gamma distributions, respectively. There are much more distributions in bayespy.nodes so you can construct quite complex conjugate exponential family models. The node y uses keyword argument plates to define the plates $n = 0, \dots, 9$.

2.2.2 Performing inference

Now that we have created the model, we can provide our data by setting y as observed:

```
>>> y.observe(data)
```

Next we want to estimate the posterior distribution. In principle, we could use different inference engines (e.g., MCMC or EP) but currently only variational Bayesian (VB) engine is implemented. The engine is initialized by giving all the nodes of the model:

```
>>> from bayespy.inference import VB
>>> Q = VB(mu, tau, y)
```

The inference algorithm can be run as long as wanted (max. 20 iterations in this case):

```
>>> Q.update(repeat=20)

Iteration 1: loglike=-6.020956e+01 (... seconds)

Iteration 2: loglike=-5.820527e+01 (... seconds)

Iteration 3: loglike=-5.820290e+01 (... seconds)

Iteration 4: loglike=-5.820288e+01 (... seconds)

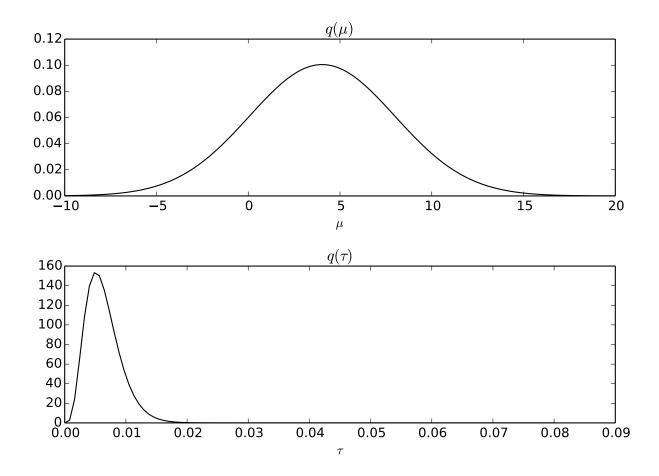
Converged at iteration 4.
```

Now the algorithm converged after four iterations, before the requested 20 iterations. VB approximates the true posterior $p(\mu, \tau | \mathbf{y})$ with a distribution which factorizes with respect to the nodes: $q(\mu)q(\tau)$.

2.2.3 Examining posterior approximation

The resulting approximate posterior distributions $q(\mu)$ and $q(\tau)$ can be examined, for instance, by plotting the marginal probability density functions:

```
>>> import bayespy.plot as bpplt
>>> bpplt.pyplot.subplot(2, 1, 1)
<matplotlib.axes.AxesSubplot object at 0x...>
>>> bpplt.pdf(mu, np.linspace(-10, 20, num=100), color='k', name=r'\mu')
[<matplotlib.lines.Line2D object at 0x...>]
>>> bpplt.pyplot.subplot(2, 1, 2)
<matplotlib.axes.AxesSubplot object at 0x...>
>>> bpplt.pdf(tau, np.linspace(1e-6, 0.08, num=100), color='k', name=r'\tau')
[<matplotlib.lines.Line2D object at 0x...>]
>>> bpplt.pyplot.tight_layout()
>>> bpplt.pyplot.show()
```



This example was a very simple introduction to using BayesPy. The model can be much more complex and each phase contains more options to give the user more control over the inference. The following sections give more details about the phases.

2.3 Constructing the model

In BayesPy, the model is constructed by creating nodes which form a directed network. There are two types of nodes: stochastic and deterministic. A stochastic node corresponds to a random variable (or a set of random variables) from a specific probability distribution. A deterministic node corresponds to a deterministic function of its parents. For a list of built-in nodes, see the *User API*.

2.3.1 Creating nodes

Creating a node is basically like writing the conditional prior distribution of the variable in Python. The node is constructed by giving the parent nodes, that is, the conditioning variables as arguments. The number of parents and their meaning depend on the node. For instance, a Gaussian node is created by giving the mean vector and the precision matrix. These parents can be constant numerical arrays if they are known:

```
>>> from bayespy.nodes import Gaussian
>>> X = Gaussian([2, 5], [[1.0, 0.3], [0.3, 1.0]])
```

or other nodes if they are unknown and given prior distributions:

```
>>> from bayespy.nodes import Gaussian, Wishart
>>> mu = Gaussian([0, 0], [[1e-6, 0], [0, 1e-6]])
>>> Lambda = Wishart(2, [[1, 0], [0, 1]])
>>> X = Gaussian(mu, Lambda)
```

Nodes can also be named by providing name keyword argument:

```
>>> X = Gaussian(mu, Lambda, name='x')
```

The name may be useful when referring to the node using an inference engine.

For the parent nodes, there are two main restrictions: non-constant parent nodes must be conjugate and the parent nodes must be mutually independent in the posterior approximation.

Conjugacy of the parents

In Bayesian framework in general, one can give quite arbitrary probability distributions for variables. However, one often uses distributions that are easy to handle in practice. Quite often this means that the parents are given conjugate priors. This is also one of the limitations in BayesPy: only conjugate family prior distributions are accepted currently. Thus, although in principle one could give, for instance, gamma prior for the mean parameter mu, only Gaussian-family distributions are accepted because of the conjugacy. If the parent is not of a proper type, an error is raised. This conjugacy is checked automatically by BayesPy and NoConverterError is raised if a parent cannot be interpreted as being from a conjugate distribution.

Independence of the parents

Another a bit rarely encountered limitation is that the parents must be mutually independent (in the posterior factorization). Thus, a node cannot have the same stochastic node as several parents without intermediate stochastic nodes. For instance, the following leads to an error:

```
>>> from bayespy.nodes import Dot
>>> Y = Dot(X, X)
Traceback (most recent call last):
...
ValueError: Parent nodes are not independent
```

The error is raised because X is given as two parents for Y, and obviously X is not independent of X in the posterior approximation. Even if X is not given several times directly but there are some intermediate deterministic nodes, an error is raised because the deterministic nodes depend on their parents and thus the parents of Y would not be independent. However, it is valid that a node is a parent of another node via several paths if all the paths or all except one path has intermediate stochastic nodes. This is valid because the intermediate stochastic nodes have independent posterior approximations. Thus, for instance, the following construction does not raise errors:

```
>>> from bayespy.nodes import Dot
>>> Z = Gaussian(X, [[1,0], [0,1]])
>>> Y = Dot(X, Z)
```

This works because there is now an intermediate stochastic node Z on the other path from X node to Y node.

2.3.2 Effects of the nodes on inference

When constructing the network with nodes, the stochastic nodes actually define three important aspects:

- 1. the prior probability distribution for the variables,
- 2. the factorization of the posterior approximation,

3. the functional form of the posterior approximation for the variables.

Prior probability distribution

First, the most intuitive feature of the nodes is that they define the prior distribution. In the previous example, mu was a stochastic GaussianARD node corresponding to μ from the normal distribution, tau was a stochastic Gamma node corresponding to τ from the gamma distribution, and y was a stochastic GaussianARD node corresponding to y from the normal distribution with mean μ and precision τ . If we denote the set of all stochastic nodes by Ω , and by π_X the set of parents of a node X, the model is defined as

$$p(\Omega) = \prod_{X \in \Omega} p(X|\pi_X),$$

where nodes correspond to the terms $p(X|\pi_X)$.

Posterior factorization

Second, the nodes define the structure of the posterior approximation. The variational Bayesian approximation factorizes with respect to nodes, that is, each node corresponds to an independent probability distribution in the posterior approximation. In the previous example, mu and tau were separate nodes, thus the posterior approximation factorizes with respect to them: $q(\mu)q(\tau)$. Thus, the posterior approximation can be written as:

$$p(\tilde{\Omega}|\hat{\Omega}) \approx \prod_{X \in \tilde{\Omega}} q(X),$$

where $\tilde{\Omega}$ is the set of latent stochastic nodes and $\hat{\Omega}$ is the set of observed stochastic nodes. Sometimes one may want to avoid the factorization between some variables. For this purpose, there are some nodes which model several variables jointly without factorization. For instance, GaussianGammaISO is a joint node for μ and τ variables from the normal-gamma distribution and the posterior approximation does not factorize between μ and τ , that is, the posterior approximation is $q(\mu,\tau)$.

Functional form of the posterior

Last, the nodes define the functional form of the posterior approximation. Usually, the posterior approximation has the same or similar functional form as the prior. For instance, Gamma uses gamma distribution to also approximate the posterior distribution. Similarly, GaussianARD uses Gaussian distribution for the posterior. However, the posterior approximation of GaussianARD uses a full covariance matrix although the prior assumes a diagonal covariance matrix. Thus, there can be slight differences in the exact functional form of the posterior approximation but the rule of thumb is that the functional form of the posterior approximation is the same as or more general than the functional form of the prior.

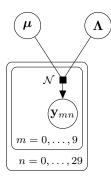
2.3.3 Using plate notation

Defining plates

Stochastic nodes take the optional parameter plates, which can be used to define plates of the variable. A plate defines the number of repetitions of a set of variables. For instance, a set of random variables y_{mn} could be defined as

$$\mathbf{y}_{mn} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Lambda}), \qquad m = 0, \dots, 9, \quad n = 0, \dots, 29.$$

This can also be visualized as a graphical model:



The variable has two plates: one for the index m and one for the index n. In BayesPy, this random variable can be constructed as:

```
>>> y = Gaussian(mu, Lambda, plates=(10,30))
```

Note: The plates are always given as a tuple of positive integers.

Plates also define indexing for the nodes, thus you can use simple NumPy-style slice indexing to obtain a subset of the plates:

```
>>> y_0 = y[0]
>>> y_0.plates
(30,)
>>> y_even = y[:,::2]
>>> y_even.plates
(10, 15)
>>> y_complex = y[:5, 10:20:5]
>>> y_complex.plates
(5, 2)
```

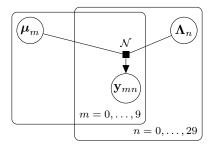
Note that this indexing is for the plates only, not for the random variable dimensions.

Sharing and broadcasting plates

Instead of having a common mean and precision matrix for all y_{mn} , it is also possible to share plates with parents. For instance, the mean could be different for each index m and the precision for each index n:

$$\mathbf{y}_{mn} \sim \mathcal{N}(\boldsymbol{\mu}_m, \boldsymbol{\Lambda}_n), \qquad m = 0, \dots, 9, \quad n = 0, \dots, 29.$$

which has the following graphical representation:



This can be constructed in BayesPy, for instance, as:

```
>>> from bayespy.nodes import Gaussian, Wishart
>>> mu = Gaussian([0, 0], [[1e-6, 0], [0, 1e-6]], plates=(10,1))
>>> Lambda = Wishart(2, [[1, 0], [0, 1]], plates=(1,30))
>>> X = Gaussian(mu, Lambda)
```

There are a few things to notice here. First, the plates are defined similarly as shapes in NumPy, that is, they use similar broadcasting rules. For instance, the plates (10,1) and (1,30) broadcast to (10,30). In fact, one could use plates (10,1) and (30,) to get the broadcasted plates (10,30) because broadcasting compares the plates from right to left starting from the last axis. Second, X is not given plates keyword argument because the default plates are the plates broadcasted from the parents and that was what we wanted so it was not necessary to provide the keyword argument. If we wanted, for instance, plates (20,10,30) for X, then we would have needed to provide plates=(20,10,30).

The validity of the plates between a child and its parents is checked as follows. The plates are compared plate-wise starting from the last axis and working the way forward. A plate of the child is compatible with a plate of the parent if either of the following conditions is met:

- 1. The two plates have equal size
- 2. The parent has size 1 (or no plate)

Table below shows an example of compatible plates for a child node and its two parent nodes:

node	plates							
parent1		3	1	1	1	8	10	
parent2			1	1	5	1	10	
child	5	3	1	7	5	8	10	

Plates in deterministic nodes

Note that plates can be defined explicitly only for stochastic nodes. For deterministic nodes, the plates are defined implicitly by the plate broadcasting rules from the parents. Deterministic nodes do not need more plates than this because there is no randomness. The deterministic node would just have the same value over the extra plates, but it is not necessary to do this explicitly because the child nodes of the deterministic node can utilize broadcasting anyway. Thus, there is no point in having extra plates in deterministic nodes, and for this reason, deterministic nodes do not use plates keyword argument.

Plates in constants

It is useful to understand how the plates and the shape of a random variable are connected. The shape of an array which contains all the plates of a random variable is the concatenation of the plates and the shape of the variable. For instance, consider a 2-dimensional Gaussian variable with plates (3,). If you want the value of the constant mean vector and constant precision matrix to vary between plates, they are given as (3,2)-shape and (3,2,2)-shape arrays, respectively:

```
>>> import numpy as np
\rightarrow \rightarrow mu = [ [0,0], [1,1], [2,2] ]
>>> Lambda = [ [[1.0, 0.0],
                 [0.0, 1.0]],
                 [[1.0, 0.9],
                  [0.9, 1.0]],
                 [[1.0, -0.3],
                  [-0.3, 1.0]]
. . .
>>> X = Gaussian(mu, Lambda)
>>> np.shape(mu)
(3, 2)
>>> np.shape(Lambda)
(3, 2, 2)
>>> X.plates
(3,)
```

Thus, the leading axes of an array are the plate axes and the trailing axes are the random variable axes. In the example above, the mean vector has plates (3,) and shape (2,2), and the precision matrix has plates (3,) and shape (2,2).

Factorization of plates

It is important to undestand the independency structure the plates induce for the model. First, the repetitions defined by a plate are independent a priori given the parents. Second, the repetitions are independent in the posterior approximation, that is, the posterior approximation factorizes with respect to plates. Thus, the plates also have an effect on the independence structure of the posterior approximation, not only prior. If dependencies between a set of variables need to be handled, that set must be handled as a some kind of multi-dimensional variable.

Irregular plates

The handling of plates is not always as simple as described above. There are cases in which the plates of the parents do not map directly to the plates of the child node. The user API should mention such irregularities.

For instance, the parents of a mixture distribution have a plate which contains the different parameters for each cluster, but the variable from the mixture distribution does not have that plate:

```
>>> from bayespy.nodes import Gaussian, Wishart, Categorical, Mixture
>>> mu = Gaussian([[0], [0], [0]], [[[1]], [[1]], [[1]]])
>>> Lambda = Wishart(1, [[[1]], [[1]], [[1]]])
>>> Z = Categorical([1/3, 1/3, 1/3], plates=(100,))
>>> X = Mixture(Z, Gaussian, mu, Lambda)
>>> mu.plates
(3,)
>>> Lambda.plates
(3,)
>>> Z.plates
(100,)
>>> X.plates
(100,)
```

The plates (3,) and (100,) should not broadcast according to the rules mentioned above. However, when validating the plates, Mixture removes the plate which corresponds to the clusters in mu and Lambda. Thus, X has plates which are the result of broadcasting plates () and (100,) which equals (100,).

Also, sometimes the plates of the parents may be mapped to the variable axes. For instance, an automatic relevance determination (ARD) prior for a Gaussian variable is constructed by giving the diagonal elements of the precision matrix (or tensor). The Gaussian variable itself can be a scalar, a vector, a matrix or a tensor. A set of five 4×3 -dimensional Gaussian matrices with ARD prior is constructed as:

```
>>> from bayespy.nodes import GaussianARD, Gamma
>>> tau = Gamma(1, 1, plates=(5,4,3))
>>> X = GaussianARD(0, tau, shape=(4,3))
>>> tau.plates
(5, 4, 3)
>>> X.plates
(5,)
```

Note how the last two plate axes of tau are mapped to the variable axes of X with shape (4,3) and the plates of X are obtained by taking the remaining leading plate axes of tau.

2.3.4 Example model: Principal component analysis

Now, we'll construct a bit more complex model which will be used in the following sections. The model is a probabilistic version of principal component analysis (PCA):

$$\mathbf{Y} = \mathbf{C}\mathbf{X}^T + \text{noise}$$

where \mathbf{Y} is $M \times N$ data matrix, \mathbf{C} is $M \times D$ loading matrix, \mathbf{X} is $N \times D$ state matrix, and noise is isotropic Gaussian. The dimensionality D is usually assumed to be much smaller than M and N.

A probabilistic formulation can be written as:

$$p(\mathbf{Y}) = \prod_{m=0}^{M-1} \prod_{n=0}^{N-1} \mathcal{N}(y_{mn} | \mathbf{c}_m^T \mathbf{x}_n, \tau)$$

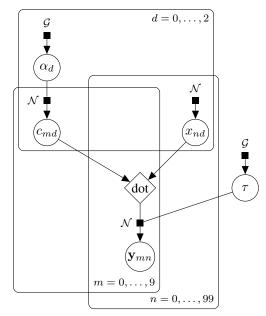
$$p(\mathbf{X}) = \prod_{n=0}^{N-1} \prod_{d=0}^{D-1} \mathcal{N}(x_{nd} | 0, 1)$$

$$p(\mathbf{C}) = \prod_{m=0}^{M-1} \prod_{d=0}^{D-1} \mathcal{N}(c_{md} | 0, \alpha_d)$$

$$p(\boldsymbol{\alpha}) = \prod_{d=0}^{D-1} \mathcal{G}(\alpha_d | 10^{-3}, 10^{-3})$$

$$p(\tau) = \mathcal{G}(\tau | 10^{-3}, 10^{-3})$$

where we have given automatic relevance determination (ARD) prior for C. This can be visualized as a graphical model:



Now, let us construct this model in BayesPy. First, we'll define the dimensionality of the latent space in our model:

```
>>> D = 3
```

Then the prior for the latent states **X**:

```
>>> X = GaussianARD(0, 1,
... shape=(D,),
... plates=(1,100),
... name='X')
```

Note that the shape of X is (D,), although the latent dimensions are marked with a plate in the graphical model and they are conditionally independent in the prior. However, we want to (and need to) model the posterior dependency of the latent dimensions, thus we cannot factorize them, which would happen if we used plates=(1,100,D) and shape=(). The first plate axis with size 1 is given just for clarity.

The prior for the ARD parameters α of the loading matrix:

```
>>> alpha = Gamma(1e-3, 1e-3, ... plates=(D,), ... name='alpha')
```

The prior for the loading matrix C:

```
>>> C = GaussianARD(0, alpha,
... shape=(D,),
... plates=(10,1),
... name='C')
```

Again, note that the shape is the same as for X for the same reason. Also, the plates of alpha, (D,), are mapped to the full shape of the node C, (10, 1, D), using standard broadcasting rules.

The dot product is just a deterministic node:

```
>>> F = Dot(C, X)
```

However, note that Dot requires that the input Gaussian nodes have the same shape and that this shape has exactly one axis, that is, the variables are vectors. This the reason why we used shape (D,) for X and C but from a bit different perspective. The node computes the inner product of D-dimensional vectors resulting in plates (10,100) broadcasted from the plates (1,100) and (10,1):

```
>>> F.plates (10, 100)
```

The prior for the observation noise τ :

```
>>> tau = Gamma(1e-3, 1e-3, name='tau')
```

Finally, the observations are conditionally independent Gaussian scalars:

```
>>> Y = GaussianARD(F, tau, name='Y')
```

Now we have defined our model and the next step is to observe some data and to perform inference.

2.4 Performing inference

Approximation of the posterior distribution can be divided into several steps:

- Observe some nodes
- Choose the inference engine
- Initialize the posterior approximation
- Run the inference algorithm

In order to illustrate these steps, we'll be using the PCA model constructed in the previous section.

2.4.1 Observing nodes

First, let us generate some toy data:

```
>>> c = np.random.randn(10, 2)
>>> x = np.random.randn(2, 100)
>>> data = np.dot(c, x) + 0.1*np.random.randn(10, 100)
```

The data is provided by simply calling observe method of a stochastic node:

```
>>> Y.observe(data)
```

It is important that the shape of the data array matches the plates and shape of the node Y. For instance, if Y was Wishart node for 3×3 matrices with plates (5, 1, 10), the full shape of Y would be (5, 1, 10, 3, 3). The data array should have this shape exactly, that is, no broadcasting rules are applied.

Missing values

It is possible to mark missing values by providing a mask which is a boolean array:

```
>>> Y.observe(data, mask=[[True], [False], [False], [True], [True], ... [False], [True], [True], [True], [False]])
```

True means that the value is observed and False means that the value is missing. The shape of the above mask is (10,1), which broadcasts to the plates of Y, (10,100). Thus, the above mask means that the second, third, sixth and tenth rows of the 10×100 data matrix are missing.

The mask is applied to the *plates*, not to the data array directly. This means that it is not possible to observe a random variable partially, each repetition defined by the plates is either fully observed or fully missing. Thus, the mask is applied to the plates. It is often possible to circumvent this seemingly tight restriction by adding an observable child node which factorizes more.

The shape of the mask is broadcasted to plates using standard NumPy broadcasting rules. So, if the variable has plates (5,1,10), the mask could have a shape (),(1,),(1,1),(1,1,1),(10,),(1,10),(1,10),(5,1,1) or (5,1,10). In order to speed up the inference, missing values are automatically integrated out if they are not needed as latent variables to child nodes. This leads to faster convergence and more accurate approximations.

2.4.2 Choosing the inference method

Inference methods can be found in bayespy.inference package. Currently, only variational Bayesian approximation is implemented (bayespy.inference.VB). The inference engine is constructed by giving the stochastic nodes of the model.

```
>>> from bayespy.inference import VB
>>> Q = VB(Y, C, X, alpha, tau)
```

There is no need to give any deterministic nodes. Currently, the inference engine does not automatically search for stochastic parents and children, thus it is important that all stochastic nodes of the model are given. This should be made more robust in future versions.

A node of the model can be obtained by using the name of the node as a key:

```
>>> Q['X']
<bayespy.inference.vmp.nodes.gaussian.GaussianARD object at 0x...>
```

Note that the returned object is the same as the node object itself:

```
>>> Q['X'] is X True
```

Thus, one may use the object X when it is available. However, if the model and the inference engine are constructed in another function or module, the node object may not be available directly and this feature becomes useful.

2.4.3 Initializing the posterior approximation

The inference engines give some initialization to the stochastic nodes by default. However, the inference algorithms can be sensitive to the initialization, thus it is sometimes necessary to have better control over the initialization. For VB, the following initialization methods are available:

- initialize_from_prior: Use the current states of the parent nodes to update the node. This is the default initialization.
- initialize_from_parameters: Use the given parameter values for the distribution.
- initialize_from_value: Use the given value for the variable.
- initialize_from_random: Draw a random value for the variable. The random sample is drawn from the current state of the node's distribution.

Note that initialize_from_value and initialize_from_random initialize the distribution with a value of the variable instead of parameters of the distribution. Thus, the distribution is actually a delta distribution with a peak on the value after the initialization. This state of the distribution does not have proper natural parameter values nor normalization, thus the VB lower bound terms are np.nan for this initial state.

These initialization methods can be used to perform even a bit more complex initializations. For instance, a Gaussian distribution could be initialized with a random mean and variance 0.1. In our PCA model, this can be obtained by

```
>>> X.initialize_from_parameters(np.random.randn(1, 100, D), 10)
```

Note that the shape of the random mean is the sum of the plates (1, 100) and the variable shape (D,). In addition, instead of variance, GaussianARD uses precision as the second parameter, thus we initialized the variance to $\frac{1}{10}$. This random initialization is important in our PCA model because the default initialization gives C and X zero mean. If the mean of the other variable was zero when the other is updated, the other variable gets zero mean too. This would lead to an update algorithm where both means remain zeros and effectively no latent space is found. Thus, it is important to give non-zero random initialization for X if C is updated before X the first time. It is typical that at least some nodes need be initialized with some randomness.

By default, nodes are initialized with the method initialize_from_prior. The method is not very time consuming but if for any reason you want to avoid that default initialization computation, you can provide initialize=False when creating the stochastic node. However, the node does not have a proper state in that case, which leads to errors in VB learning unless the distribution is initialized using the above methods.

2.4.4 Running the inference algorithm

The approximation methods are based on iterative algorithms, which can be run using update method. By default, it takes one iteration step updating all nodes once:

```
>>> Q.update()
Iteration 1: loglike=-9.305259e+02 (... seconds)
```

The loglike tells the VB lower bound. The order in which the nodes are updated is the same as the order in which the nodes were given when creating Q. If you want to change the order or update only some of the nodes, you can give as arguments the nodes you want to update and they are updated in the given order:

```
>>> Q.update(C, X)
Iteration 2: loglike=-8.818976e+02 (... seconds)
```

It is also possible to give the same node several times:

```
>>> Q.update(C, X, C, tau)
Iteration 3: loglike=-8.071222e+02 (... seconds)
```

Note that each call to update is counted as one iteration step although not variables are necessarily updated. Instead of doing one iteration step, repeat keyword argument can be used to perform several iteration steps:

```
>>> Q.update(repeat=10)

Iteration 4: loglike=-7.167588e+02 (... seconds)

Iteration 5: loglike=-6.827873e+02 (... seconds)

Iteration 6: loglike=-6.259477e+02 (... seconds)

Iteration 7: loglike=-4.725400e+02 (... seconds)

Iteration 8: loglike=-3.270816e+02 (... seconds)

Iteration 9: loglike=-2.208865e+02 (... seconds)

Iteration 10: loglike=-1.658761e+02 (... seconds)

Iteration 11: loglike=-1.469468e+02 (... seconds)

Iteration 12: loglike=-1.420311e+02 (... seconds)

Iteration 13: loglike=-1.405139e+02 (... seconds)
```

The VB algorithm stops automatically if it converges, that is, the relative change in the lower bound is below some threshold:

```
>>> Q.update(repeat=1000)
Iteration 14: loglike=-1.396481e+02 (... seconds)
...
Iteration 488: loglike=-1.224106e+02 (... seconds)
Converged at iteration 488.
```

Now the algorithm stopped before taking 1000 iteration steps because it converged. The relative tolerance can be adjusted by providing tol keyword argument to the update method:

```
>>> Q.update(repeat=10000, tol=1e-6)
Iteration 489: loglike=-1.224094e+02 (... seconds)
...
Iteration 847: loglike=-1.222506e+02 (... seconds)
Converged at iteration 847.
```

Making the tolerance smaller, may improve the result but it may also significantly increase the iteration steps until convergence.

Instead of using update method of the inference engine VB, it is possible to use the update methods of the nodes directly as

```
>>> C.update()
or
>>> Q['C'].update()
```

However, this is not recommended, because the update method of the inference engine VB is a wrapper which, in addition to calling the nodes' update methods, checks for convergence and does a few other useful minor things. But if for any reason these direct update methods are needed, they can be used.

Parameter expansion

Sometimes the VB algorithm converges very slowly. This may happen when the variables are strongly coupled in the true posterior but factorized in the approximate posterior. This coupling leads to zigzagging of the variational parameters which progresses slowly. One solution to this problem is to use parameter expansion. The idea is to add an auxiliary variable which parameterizes the posterior approximation of several variables. Then optimizing this auxiliary variable actually optimizes several posterior approximations jointly leading to faster convergence.

The parameter expansion is model specific. Currently in BayesPy, only state-space models have built-in parameter expansions available. These state-space models contain a variable which is a dot product of two variables (plus some noise):

$$y = \mathbf{c}^T \mathbf{x} + \text{noise}$$

The parameter expansion can be motivated by noticing that we can add an auxiliary variable which rotates the variables \mathbf{c} and \mathbf{x} so that the dot product is unaffected:

$$y = \mathbf{c}^T \mathbf{x} + \text{noise} = \mathbf{c}^T \mathbf{R} \mathbf{R}^{-1} \mathbf{x} + \text{noise} = (\mathbf{R}^T \mathbf{c})^T (\mathbf{R}^{-1} \mathbf{x}) + \text{noise}$$

Now, applying this rotation to the posterior approximations $q(\mathbf{c})$ and $q(\mathbf{x})$, and optimizing the VB lower bound with respect to the rotation leads to parameterized joint optimization of \mathbf{c} and \mathbf{x} .

The available parameter expansion methods are in module transformations:

```
>>> from bayespy.inference.vmp import transformations
```

First, you create the rotation transformations for the two variables:

```
>>> rotX = transformations.RotateGaussianARD(X)
>>> rotC = transformations.RotateGaussianARD(C, alpha)
```

Here, the rotation for C provides the ARD parameters alpha so they are updated simultaneously. In addition to RotateGaussianARD, there are a few other built-in rotations defined, for instance, RotateGaussian and RotateGaussianMarkovChain. It is extremely important that the model satisfies the assumptions made by the rotation class and the user is mostly responsible for this. The optimizer for the rotations is constructed by giving the two rotations and the dimensionality of the rotated space:

```
>>> R = transformations.RotationOptimizer(rotC, rotX, D)
```

Now, calling rotate method will find optimal rotation and update the relevant nodes (X, C and alpha) accordingly:

```
>>> R.rotate()
```

Let us see how our iteration would have gone if we had used this parameter expansion. First, let us re-initialize our nodes and VB algorithm:

```
>>> alpha.initialize_from_prior()
>>> C.initialize_from_prior()
>>> X.initialize_from_parameters(np.random.randn(1, 100, D), 10)
>>> tau.initialize_from_prior()
>>> Q = VB(Y, C, X, alpha, tau)
```

Then, the rotation is set to run after each iteration step:

```
>>> Q.callback = R.rotate
```

Now the iteration converges to the relative tolerance 10^{-6} much faster:

```
>>> Q.update(repeat=1000, tol=1e-6)
Iteration 1: loglike=-9.363500e+02 (... seconds)
...
Iteration 18: loglike=-1.221354e+02 (... seconds)
Converged at iteration 18.
```

The convergence took 18 iterations with rotations and 488 or 847 iterations without the parameter expansion. In addition, the lower bound is improved slightly. One can compare the number of iteration steps in this case because the cost per iteration step with or without parameter expansion is approximately the same. Sometimes the parameter expansion can have the drawback that it converges to a bad local optimum. Usually, this can be solved by updating the nodes near the observations a few times before starting to update the hyperparameters and to use parameter expansion. In any case, the parameter expansion is practically necessary when using state-space models in order to converge to a proper solution in a reasonable time.

2.5 Examining the results

After the results have been obtained, it is important to be able to examine the results easily. The results can be examined either numerically by inspecting numerical arrays or visually by plotting distributions of the nodes. In addition, the posterior distributions can be visualized during the learning algorithm and the results can saved into a file.

2.5.1 Plotting the results

The module plot offers some plotting basic functionality:

```
>>> import bayespy.plot as bpplt
```

The module contains matplotlib.pyplot module if the user needs that. For instance, interactive plotting can be enabled as:

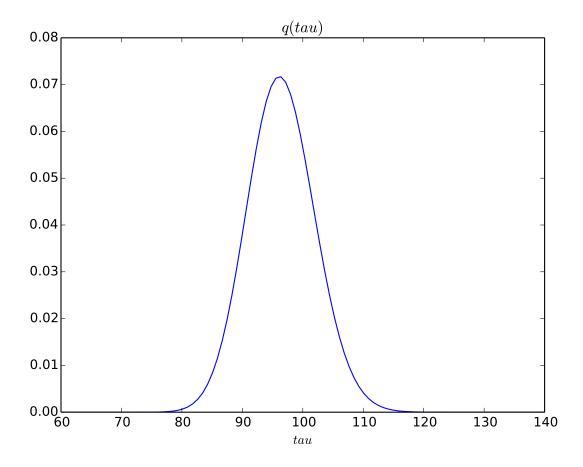
```
>>> bpplt.pyplot.ion()
```

The plot module contains some functions but it is not a very comprehensive collection, thus the user may need to write some problem- or model-specific plotting functions. The current collection is:

- pdf (): show probability density function of a scalar
- contour (): show probability density function of two-element vector
- hinton(): show the Hinton diagram
- plot (): show value as a function

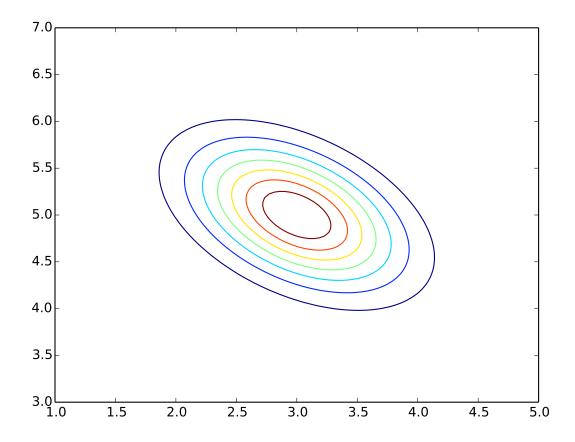
The probability density function of a scalar random variable can be plotted using the function pdf ():

```
>>> bpplt.pyplot.figure()
<matplotlib.figure.Figure object at 0x...>
>>> bpplt.pdf(Q['tau'], np.linspace(60, 140, num=100))
[<matplotlib.lines.Line2D object at 0x...>]
```



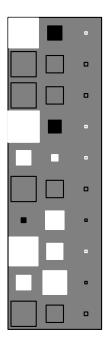
The variable tau models the inverse variance of the noise, for which the true value is $0.1^{-2}=100$. Thus, the posterior captures the true value quite accurately. Similarly, the function contour () can be used to plot the probability density function of a 2-dimensional variable, for instance:

```
>>> V = Gaussian([3, 5], [[4, 2], [2, 5]])
>>> bpplt.pyplot.figure()
<matplotlib.figure.Figure object at 0x...>
>>> bpplt.contour(V, np.linspace(1, 5, num=100), np.linspace(3, 7, num=100))
<matplotlib.contour.QuadContourSet object at 0x...>
```



Both pdf() and contour() require that the user provides the grid on which the probability density function is computed. They also support several keyword arguments for modifying the output, similarly as plot and contour in matplotlib.pyplot. These functions can be used only for stochastic nodes. A few other plot types are also available as built-in functions. A Hinton diagram can be plotted as:

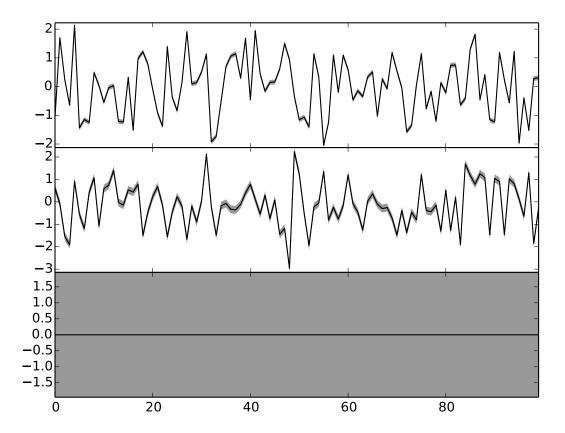
```
>>> bpplt.pyplot.figure()
<matplotlib.figure.Figure object at 0x...>
>>> bpplt.hinton(C)
```



The diagram shows the elements of the matrix C. The size of the filled rectangle corresponds to the absolute value of the element mean, and white and black correspond to positive and negative values, respectively. The non-filled rectangle shows standard deviation. From this diagram it is clear that the third column of C has been pruned out and the rows that were missing in the data have zero mean and column-specific variance. The function $\min()$ is a simple wrapper for node-specific Hinton diagram plotters, such as $\mathtt{gaussian_hinton}()$ and $\mathtt{dirichlet_hinton}()$. Thus, the keyword arguments depend on the node which is plotted.

Another plotting function is plot (), which just plots the values of the node over one axis as a function:

```
>>> bpplt.pyplot.figure()
<matplotlib.figure.Figure object at 0x...>
>>> bpplt.plot(X, axis=-2)
```



Now, the axis is the second last axis which corresponds to $n=0,\ldots,N-1$. As D=3, there are three subplots. For Gaussian variables, the function shows the mean and two standard deviations. The plot shows that the third component has been pruned out, thus the method has been able to recover the true dimensionality of the latent space. It also has similar keyword arguments to plot function in matplotlib.pyplot. Again, plot () is a simple wrapper over node-specific plotting functions, thus it supports only some node classes.

2.5.2 Monitoring during the inference algorithm

It is possible to plot the distribution of the nodes during the learning algorithm. This is useful when the user is interested to see how the distributions evolve during learning and what is happening to the distributions. In order to utilize monitoring, the user must set plotters for the nodes that he or she wishes to monitor. This can be done either when creating the node or later at any time.

The plotters are set by creating a plotter object and providing this object to the node. The plotter is a wrapper of one of the plotting functions mentioned above: PDFPlotter, ContourPlotter, HintonPlotter or FunctionPlotter. Thus, our example model could use the following plotters:

```
>>> tau.set_plotter(bpplt.PDFPlotter(np.linspace(60, 140, num=100)))
>>> C.set_plotter(bpplt.HintonPlotter())
>>> X.set_plotter(bpplt.FunctionPlotter(axis=-2))
```

These could have been given at node creation as a keyword argument plotter:

```
>>> V = Gaussian([3, 5], [[4, 2], [2, 5]],
... plotter=bpplt.ContourPlotter(np.linspace(1, 5, num=100),
... np.linspace(3, 7, num=100)))
```

When the plotter is set, one can use the plot method of the node to perform plotting:

```
>>> V.plot()
<matplotlib.contour.QuadContourSet object at 0x...>
```

Nodes can also be plotted using the plot method of the inference engine:

```
>>> Q.plot('C')
```

This method remembers the figure in which a node has been plotted and uses that every time it plots the same node. In order to monitor the nodes during learning, it is possible to use the keyword argument plot:

```
>>> Q.update(repeat=5, plot=True, tol=np.nan)

Iteration 19: loglike=-1.221354e+02 (... seconds)

Iteration 20: loglike=-1.221354e+02 (... seconds)

Iteration 21: loglike=-1.221354e+02 (... seconds)

Iteration 22: loglike=-1.221354e+02 (... seconds)

Iteration 23: loglike=-1.221354e+02 (... seconds)
```

Each node which has a plotter set will be plotted after it is updated. Note that this may slow down the inference significantly if the plotting operation is time consuming.

2.5.3 Posterior parameters and moments

If the built-in plotting functions are not sufficient, it is possible to use matplotlib.pyplot for custom plotting. Each node has get_moments method which returns the moments and they can be used for plotting. Stochastic exponential family nodes have natural parameter vectors which can also be used. In addition to plotting, it is also possible to just print the moments or parameters in the console.

2.5.4 Saving and loading results

The results of the inference engine can be easily saved and loaded using VB.save() and VB.load() methods:

```
>>> Q.save(filename='tmp.hdf5')
>>> Q.load(filename='tmp.hdf5')
```

The results are stored in a HDF5 file. The user may set an autosave file in which the results are automatically saved regularly. Autosave filename can be set at creation time by autosave_filename keyword argument or later using VB.set_autosave() method. If autosave file has been set, the VB.save() and VB.load() methods use that file by default. In order for the saving to work, all stochastic nodes must have been given (unique) names.

However, note that these methods do *not* save nor load the node definitions. It means that the user must create the nodes and the inference engine and then use VB.load() to set the state of the nodes and the inference engine. If there are any differences in the model that was saved and the one which is tried to update using loading, then loading does not work. Thus, the user should keep the model construction unmodified in a Python file in order to be able to load the results later. Or if the user wishes to share the results, he or she must share the model construction Python file with the HDF5 results file.

CHAPTER

THREE

EXAMPLES

3.1 Regression

3.1.1 Linear regression

```
import numpy as np
k = 2
c = 5
s = 2
x = np.arange(10)
y = k*x + c + s*np.random.randn(10)
from bayespy.nodes import GaussianARD
B = GaussianARD(0, 1e-6, shape=(2,))
X = np.vstack([x, np.ones(len(x))]).T
from bayespy.nodes import SumMultiply
F = SumMultiply('i,i', B, X)
from bayespy.nodes import Gamma
tau = Gamma(1e-3, 1e-3)
Y = GaussianARD(F, tau)
Y.observe(y)
from bayespy.inference import VB
Q = VB(Y, B, tau)
Q.update(repeat=100)
import bayespy.plot as bpplt
# These two lines are needed to enable inline plotting IPython Notebooks
%matplotlib inline
bpplt.pyplot.plot([])
xh = np.linspace(-5, 15, 100)
Xh = np.vstack([xh, np.ones(len(xh))]).T
Fh = SumMultiply('i,i', B, Xh)
bpplt.plot(Fh, x=xh, scale=2)
bpplt.plot(y, x=x, color='r', marker='x', linestyle='None')
bpplt.plot(k*xh+c, x=xh, color='r');
```

```
Iteration 1: loglike=-4.515537e+01 (0.000 seconds)
Iteration 2: loglike=-4.429472e+01 (0.010 seconds)
Iteration 3: loglike=-4.428241e+01 (0.000 seconds)
Iteration 4: loglike=-4.428197e+01 (0.000 seconds)
Iteration 5: loglike=-4.428195e+01 (0.010 seconds)
Converged.
bpplt.pdf(tau, np.linspace(1e-6, 1, 100), color='k')
bpplt.pyplot.axvline(s**(-2), color='r')
# Add labels
bpplt.pyplot.title(r'$q(\tau)$')
bpplt.pyplot.xlabel(r'$\tau$');
bpplt.contour(B, np.linspace(1,3,1000), np.linspace(1,9,1000), n=10, colors='k')
bpplt.plot(c, x=k, color='r', marker='x', linestyle='None', markersize=10, markeredgewidth=2)
# Add labels
bpplt.pyplot.title(r'$q(k,c)$')
bpplt.pyplot.xlabel(r'$k$')
bpplt.pyplot.ylabel(r'$c$');
```

3.1.2 Improving accuracy

```
from bayespy.nodes import GaussianGammaISO
B_tau = GaussianGammaISO(np.zeros(2), 1e-6*np.identity(2), 1e-3, 1e-3)
F_tau = SumMultiply('i,i', B_tau, X)
Y = GaussianARD(F_tau, 1)
Y.observe(y)
from bayespy.inference import VB
Q = VB(Y, B_tau)
Q.update(repeat=10)
Iteration 1: loglike=-4.594957e+01 (0.000 seconds)
Iteration 2: loglike=-4.594957e+01 (0.000 seconds)
Converged.
bpplt.pdf(B_tau.get_marginal_logpdf(gaussian=None, gamma=True),
          np.linspace(1e-6, 1, 100), color='k')
bpplt.pyplot.axvline(s**(-2), color='r')
# Add labels
bpplt.pyplot.title(r'$q(\tau)$')
bpplt.pyplot.xlabel(r'$\tau$');
bpplt.contour(B_tau.get_marginal_logpdf(gaussian=[0,1], gamma=False),
              np.linspace(1,3,100), np.linspace(1,9,100),
              n=10, colors='k')
# Plot the true value
bpplt.plot(c, x=k, color='r', marker='x', linestyle='None', markersize=10, markeredgewidth=2)
# Add labels
bpplt.pyplot.title(r'$q(k,c)$')
bpplt.pyplot.xlabel(r'$k$')
bpplt.pyplot.ylabel(r'$c$');
```

```
bpplt.contour(B_tau.get_marginal_logpdf(gaussian=[0], gamma=True),
             np.linspace(1,3,100), np.linspace(1e-6,1,100),
             n=10, colors='k')
bpplt.plot(s**(-2), x=k, color='r', marker='x', linestyle='None', markersize=10, markeredgewidth=2)
bpplt.pyplot.title(r'$q(k,\tau)$')
bpplt.pyplot.xlabel(r'$k$')
bpplt.pyplot.ylabel(r'$\tau$');
xh = np.linspace(-5, 15, 100)
Xh = np.vstack([xh, np.ones(len(xh))]).T
Fh_tau = SumMultiply('i,i', B_tau, Xh)
bpplt.plot(Fh_tau, x=xh, scale=2)
bpplt.plot(y, x=x, color='r', marker='x', linestyle='None')
bpplt.plot(k*xh+c, x=xh, color='r')
_____
AttributeError
                                         Traceback (most recent call last)
<ipython-input-8-bad1c68bbf3d> in <module>()
      2 Xh = np.vstack([xh, np.ones(len(xh))]).T
     3 Fh_tau = SumMultiply('i,i', B_tau, Xh)
---> 4 bpplt.plot(Fh_tau, x=xh, scale=2)
      5 bpplt.plot(y, x=x, color='r', marker='x', linestyle='None')
      6 bpplt.plot(k*xh+c, x=xh, color='r')
/home/jluttine/workspace/bayespy/bayespy/plot.py in plot(Y, axis, scale, center, **kwargs)
   125
                   return plot_gaussian(Y, axis=axis, scale=scale, center=center, **kwargs)
   126
--> 127
           (mu, var) = Y.get_mean_and_variance()
           std = np.sqrt(var)
   128
   129
AttributeError: 'SumMultiply' object has no attribute 'get_mean_and_variance'
```

3.1.3 Multivariate regression

3.1.4 Non-linear regression

3.2 Gaussian mixture model

This example demonstrates the use of Gaussian mixture model for flexible density estimation, clustering or classification.

3.2.1 Data

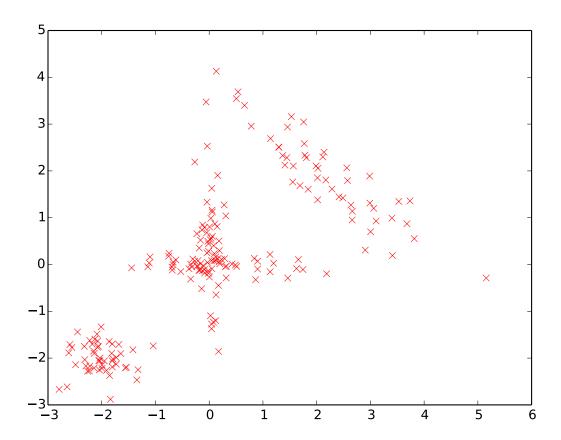
First, let us generate some artificial data for the analysis. The data are two-dimensional vectors from one of the four different Gaussian distributions:

```
>>> import numpy as np
>>> y0 = np.random.multivariate_normal([0, 0], [[2, 0], [0, 0.1]], size=50)
>>> y1 = np.random.multivariate_normal([0, 0], [[0.1, 0], [0, 2]], size=50)
>>> y2 = np.random.multivariate_normal([2, 2], [[2, -1.5], [-1.5, 2]], size=50)
```

```
>>> y3 = np.random.multivariate_normal([-2, -2], [[0.5, 0], [0, 0.5]], size=50)
>>> y = np.vstack([y0, y1, y2, y3])
```

Thus, there are 200 data vectors in total. The data looks as follows:

```
>>> import bayespy.plot as bpplt
>>> bpplt.pyplot.plot(y[:,0], y[:,1], 'rx')
[<matplotlib.lines.Line2D object at 0x...>]
```



3.2.2 **Model**

For clarity, let us denote the number of the data vectors with $\ensuremath{\mathbb{N}}$

```
>>> N = 200
```

and the dimensionality of the data vectors with \mathbb{D} :

```
>>> D = 2
```

We will use a "large enough" number of Gaussian clusters in our model:

```
>>> K = 10
```

Cluster assignments Z and the prior for the cluster assignment probabilities alpha:

```
>>> from bayespy.nodes import Dirichlet, Categorical
>>> alpha = Dirichlet(1e-5*np.ones(K),
... name='alpha')
>>> Z = Categorical(alpha,
... plates=(N,),
... name='z')
```

The mean vectors and the precision matrices of the clusters:

If either the mean or precision should be shared between clusters, then that node should not have plates, that is, plates=(). The data vectors are from a Gaussian mixture with cluster assignments Z and Gaussian component parameters mu and Lambda:

```
>>> from bayespy.nodes import Mixture
>>> Y = Mixture(Z, Gaussian, mu, Lambda,
... name='Y')
>>> Z.initialize_from_random()
>>> from bayespy.inference import VB
>>> Q = VB(Y, mu, Lambda, Z, alpha)
```

3.2.3 Inference

Before running the inference algorithm, we provide the data:

```
>>> Y.observe(y)
```

Then, run VB iteration until convergence:

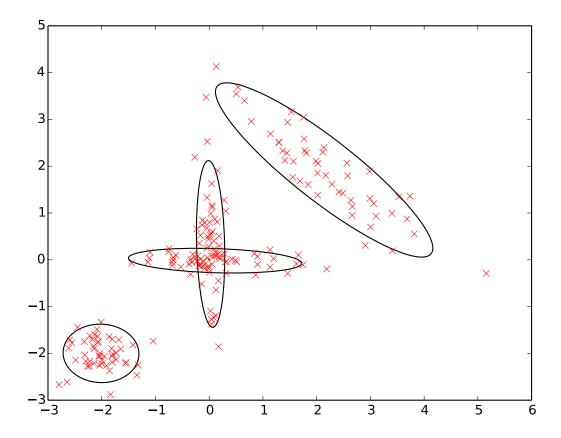
```
>>> Q.update(repeat=1000)
Iteration 1: loglike=-1.401968e+03 (... seconds)
...
Iteration 48: loglike=-1.017893e+03 (... seconds)
Converged at iteration 48.
```

The algorithm converges very quickly. Note that the default update order of the nodes was such that mu and Lambda were updated before Z, which is what we wanted because Z was initialized randomly.

3.2.4 Results

For two-dimensional Gaussian mixtures, the mixture components can be plotted using gaussian mixture ():

```
>>> bpplt.gaussian_mixture(Y, scale=2)
```



The function is called with scale=2 which means that each ellipse shows two standard deviations. From the ten cluster components, the model uses effectively the correct number of clusters (4). These clusters capture the true density accurately.

3.2.5 Next steps

The next step for improving the results could be to use GaussianWishart node for modelling the mean vectors mu and precision matrices Lambda jointly without factorization. This should improve the accuracy of the posterior approximation and the speed of the VB estimation. However, the implementation is a bit more complex.

In addition to clustering and density estimation, this model could also be used for classification by setting the known class assignments as observed.

3.3 Bernoulli mixture model

This example considers data generated from a Bernoulli mixture model. One simple example process could be a questionnaire for election candidates. We observe a set of binary vectors, where each vector represents a candidate in the election and each element in these vectors correspond to a candidate's answer to a yes-or-no question. The goal is to find groups of similar candidates and analyze the answer patterns of these groups.

3.3.1 Data

First, we generate artificial data to analyze. Let us assume that the questionnaire contains ten yes-or-no questions. We assume that there are three groups with similar opinions. These groups could represent parties. These groups have the following answering patterns, which are represented by vectors with probabilities of a candidate answering yes to the questions:

```
>>> p0 = [0.1, 0.9, 0.1, 0.9, 0.1, 0.9, 0.1, 0.9, 0.1, 0.9]
>>> p1 = [0.1, 0.1, 0.1, 0.1, 0.1, 0.9, 0.9, 0.9, 0.9, 0.9]
>>> p2 = [0.9, 0.9, 0.9, 0.9, 0.9, 0.1, 0.1, 0.1, 0.1, 0.1]
```

Thus, the candidates in the first group are likely to answer no to questions 1, 3, 5, 7 and 9, and yes to questions 2, 4, 6, 8, 10. The candidates in the second group are likely to answer yes to the last five questions, whereas the candidates in the third group are likely to answer yes to the first five questions. For convenience, we form a NumPy array of these vectors:

```
>>> import numpy as np
>>> p = np.array([p0, p1, p2])
```

Next, we generate a hundred candidates. First, we randomly select the group for each candidate:

```
>>> from bayespy.utils import random
>>> z = random.categorical([1/3, 1/3, 1/3], size=100)
```

Using the group patterns, we generate yes-or-no answers for the candidates:

```
>>> x = random.bernoulli(p[z])
```

This is our simulated data to be analyzed.

3.3.2 Model

Now, we construct a model for learning the structure in the data. We have a dataset of hundred 10-dimensional binary vectors:

```
>>> N = 100
>>> D = 10
```

We will create a Bernoulli mixture model. We assume that the true number of groups is unknown to us, so we use a large enough number of clusters:

```
>>> K = 10
```

We use the categorical distribution for the group assignments and give the group assignment probabilities an uninformative Dirichlet prior:

```
>>> from bayespy.nodes import Categorical, Dirichlet
>>> R = Dirichlet(K*[1e-5],
... name='R')
>>> Z = Categorical(R,
... plates=(N,1),
... name='Z')
```

Each group has a probability of a yes answer for each question. These probabilities are given beta priors:

```
>>> from bayespy.nodes import Beta
>>> P = Beta([0.5, 0.5],
... plates=(D,K),
... name='P')
```

The answers of the candidates are modelled with the Bernoulli distribution:

```
>>> from bayespy.nodes import Mixture, Bernoulli
>>> X = Mixture(Z, Bernoulli, P)
```

Here, Z defines the group assignments and P the answering probability patterns for each group. Note how the plates of the nodes are matched: Z has plates (N, 1) and P has plates (D, K), but in the mixture node the last plate axis of P is discarded and thus the node broadcasts plates (N, 1) and (D, 1) resulting in plates (N, D) for X.

3.3.3 Inference

In order to infer the variables in our model, we construct a variational Bayesian inference engine:

```
>>> from bayespy.inference import VB
>>> Q = VB(Z, R, X, P)
```

This also gives the default update order of the nodes. In order to find different groups, they must be initialized differently, thus we use random initialization for the group probability patterns:

```
>>> P.initialize_from_random()
```

We provide our simulated data:

```
>>> X.observe(x)
```

Now, we can run inference:

```
>>> Q.update(repeat=1000)
Iteration 1: loglike=-6.872145e+02 (... seconds)
...
Iteration 17: loglike=-5.236921e+02 (... seconds)
Converged at iteration 17.
```

The algorithm converges in 17 iterations.

3.3.4 Results

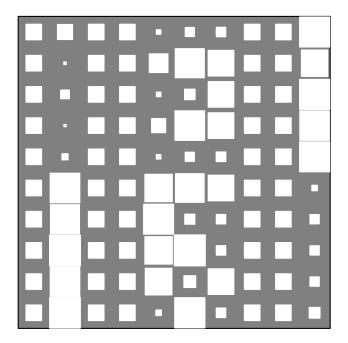
Now we can examine the approximate posterior distribution. First, let us plot the group assignment probabilities:

```
>>> import bayespy.plot as bpplt
>>> bpplt.hinton(R)
```



This plot shows that there are three dominant groups, which is equal to the true number of groups used to generate the data. However, there are still two smaller groups as the data does not give enough evidence to prune them out. The yes-or-no answer probability patterns for the groups can be plotted as:

>>> bpplt.hinton(P)



The three dominant groups have found the true patterns accurately. The patterns of the two minor groups some kind of mixtures of the three groups and they exist because the generated data happened to contain a few samples giving evidence for these groups. Finally, we can plot the group assignment probabilities for the candidates:

>>> bpplt.hinton(Z)



This plot shows the clustering of the candidates. It is possible to use ${\tt HintonPlotter}$ to enable monitoring during the VB iteration by providing ${\tt plotter=HintonPlotter}$ () for Z, P and R when creating the nodes.

3.4 Hidden Markov model

In this example, we will demonstrate the use of hidden Markov model in the case of known and unknown parameters. We will also use two different emission distributions to demonstrate the flexibility of the model construction.

3.4.1 Known parameters

This example follows the one presented in Wikipedia.

Model

Each day, the state of the weather is either 'rainy' or 'sunny'. The weather follows a first-order discrete Markov process. It has the following initial state probabilities

```
>>> a0 = [0.6, 0.4] # p(rainy)=0.6, p(sunny)=0.4
```

and state transition probabilities:

```
>>> A = [[0.7, 0.3], # p(rainy->rainy)=0.7, p(rainy->sunny)=0.3
... [0.4, 0.6]] # p(sunny->rainy)=0.4, p(sunny->sunny)=0.6
```

We will be observing one hundred samples:

```
>>> N = 100
```

The discrete first-order Markov chain is constructed as:

```
>>> from bayespy.nodes import CategoricalMarkovChain
>>> Z = CategoricalMarkovChain(a0, A, states=N)
```

However, instead of observing this process directly, we observe whether Bob is 'walking', 'shopping' or 'cleaning'. The probability of each activity depends on the current weather as follows:

```
>>> P = [[0.1, 0.4, 0.5], ... [0.6, 0.3, 0.1]]
```

where the first row contains activity probabilities on a rainy weather and the second row contains activity probabilities on a sunny weather. Using these emission probabilities, the observed process is constructed as:

```
>>> from bayespy.nodes import Categorical, Mixture
>>> Y = Mixture(Z, Categorical, P)
```

Data

In order to test our method, we'll generate artificial data from the model itself. First, draw realization of the weather process:

```
>>> weather = Z.random()
```

Then, using this weather, draw realizations of the activities:

```
>>> activity = Mixture(weather, Categorical, P).random()
```

Inference

Now, using this data, we set our variable Y to be observed:

```
>>> Y.observe(activity)
```

In order to run inference, we construct variational Bayesian inference engine:

```
>>> from bayespy.inference import VB
>>> Q = VB(Y, Z)
```

Note that we need to give all random variables to VB. In this case, the only random variables were Y and Z. Next we run the inference, that is, compute our posterior distribution:

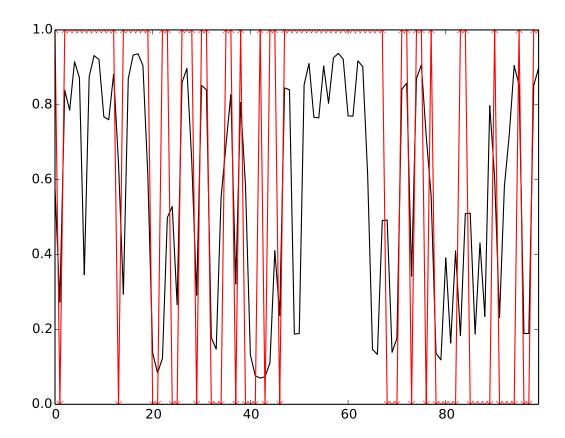
```
>>> Q.update()
Iteration 1: loglike=-1.095883e+02 (... seconds)
```

In this case, because there is only one unobserved random variable, we recover the exact posterior distribution and there is no need to iterate more than one step.

Results

One way to plot a 2-class categorical timeseries is to use the basic plot () function:

```
>>> import bayespy.plot as bpplt
>>> bpplt.plot(Z)
>>> bpplt.plot(1-weather, color='r', marker='x')
```



The black line shows the posterior probability of rain and the red line and crosses show the true state. Clearly, the method is not able to infer the weather very accurately in this case because the activies do not give that much information about the weather.

3.4.2 Unknown parameters

In this example, we consider unknown parameters for the Markov process and different emission distribution.

Data

We generate data from three 2-dimensional Gaussian distributions with different mean vectors and common standard deviation:

```
>>> import numpy as np
>>> mu = np.array([ [0,0], [3,4], [6,0] ])
>>> std = 2.0
```

Thus, the number of clusters is three:

```
>>> K = 3
```

And the number of samples is 200:

```
>>> N = 200
```

Each initial state is equally probable:

```
>>> p0 = np.ones(K) / K
```

State transition matrix is such that with probability 0.9 the process stays in the same state. The probability to move one of the other two states is 0.05 for both of those states.

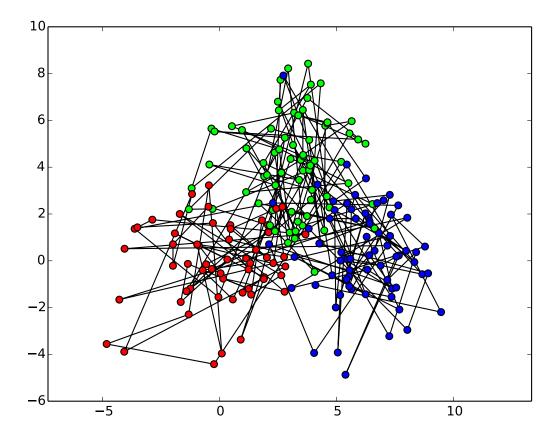
```
>>> q = 0.9
>>> r = (1-q) / (K-1)
>>> P = q*np.identity(K) + r*(np.ones((3,3))-np.identity(3))
```

Simulate the data:

```
>>> y = np.zeros((N,2))
>>> z = np.zeros(N)
>>> for n in range(N):
... z[n] = state
... y[n,:] = std*np.random.randn(2) + mu[state]
... state = np.random.choice(K, p=P[state])
```

Then, let us visualize the data:

```
>>> bpplt.pyplot.figure()
<matplotlib.figure.Figure object at 0x...>
>>> bpplt.pyplot.axis('equal')
(...)
>>> colors = [ [[1,0,0], [0,1,0], [0,0,1]][int(state)] for state in z ]
>>> bpplt.pyplot.plot(y[:,0], y[:,1], 'k-', zorder=-10)
[<matplotlib.lines.Line2D object at 0x...>]
>>> bpplt.pyplot.scatter(y[:,0], y[:,1], c=colors, s=40)
<matplotlib.collections.PathCollection object at 0x...>
```



Consecutive states are connected by a solid black line and the dot color shows the true class.

Model

Now, assume that we do not know the parameters of the process (initial state probability and state transition probabilities). We give these parameters quite non-informative priors, but it is possible to provide more informative priors if such information is available:

```
>>> from bayespy.nodes import Dirichlet
>>> a0 = Dirichlet(1e-3*np.ones(K))
>>> A = Dirichlet(1e-3*np.ones((K,K)))
```

The discrete Markov chain is constructed as:

```
>>> Z = CategoricalMarkovChain(a0, A, states=N)
```

Now, instead of using categorical emission distribution as before, we'll use Gaussian distribution. For simplicity, we use the true parameters of the Gaussian distributions instead of giving priors and estimating them. The known standard deviation can be converted to a precision matrix as:

```
>>> Lambda = std**(-2) * np.identity(2)
```

Thus, the observed process is a Gaussian mixture with cluster assignments from the hidden Markov process 2:

```
>>> from bayespy.nodes import Gaussian
>>> Y = Mixture(Z, Gaussian, mu, Lambda)
```

Note that Lambda does not have cluster plate axis because it is shared between the clusters.

Inference

Let us use the simulated data:

```
>>> Y.observe(y)
```

Because VB takes all the random variables, we need to provide A and a0 also:

```
>>> Q = VB(Y, Z, A, a0)
```

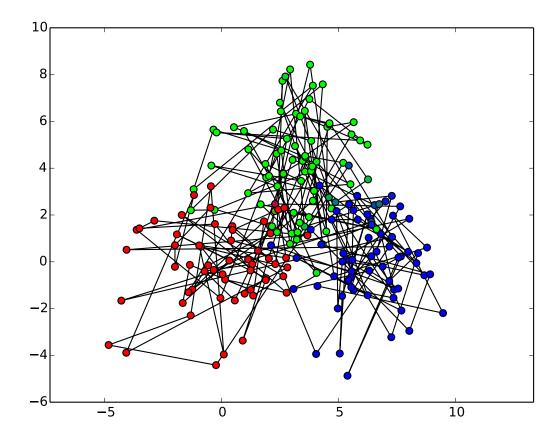
Then, run VB iteration until convergence:

```
>>> Q.update(repeat=1000)
Iteration 1: loglike=-9.963054e+02 (... seconds)
...
Iteration 8: loglike=-9.235053e+02 (... seconds)
Converged at iteration 8.
```

Results

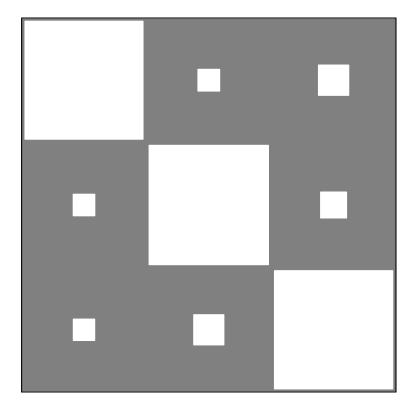
Plot the classification of the data similarly as the data:

```
>>> bpplt.pyplot.figure()
<matplotlib.figure.Figure object at 0x...>
>>> bpplt.pyplot.axis('equal')
(...)
>>> colors = Y.parents[0].get_moments()[0]
>>> bpplt.pyplot.plot(y[:,0], y[:,1], 'k-', zorder=-10)
[<matplotlib.lines.Line2D object at 0x...>]
>>> bpplt.pyplot.scatter(y[:,0], y[:,1], c=colors, s=40)
<matplotlib.collections.PathCollection object at 0x...>
```



The data has been classified quite correctly. Even samples that are more in the region of another cluster are classified correctly if the previous and next sample provide enough evidence for the correct class. We can also plot the state transition matrix:

>>> bpplt.hinton(A)



Clearly, the learned state transition matrix is close to the true matrix. The models described above could also be used for classification by providing the known class assignments as observed data to $\mathbb Z$ and the unknown class assignments as missing data.

3.5 Principal component analysis

This example uses a simple principal component analysis to find a two-dimensional latent subspace in a higher dimensional dataset.

3.5.1 Data

Let us create a Gaussian dataset with latent space dimensionality two and some observation noise:

```
>>> M = 20
>>> N = 100

>>> import numpy as np
>>> x = np.random.randn(N, 2)
>>> w = np.random.randn(M, 2)
>>> f = np.einsum('ik, jk->ij', w, x)
>>> y = f + 0.1*np.random.randn(M, N)
```

3.5.2 Model

We will use 10-dimensional latent space in our model and let it learn the true dimensionality:

```
>>> D = 10
```

Import relevant nodes:

```
>>> from bayespy.nodes import GaussianARD, Gamma, SumMultiply
```

The latent states:

```
>>> X = GaussianARD(0, 1, plates=(1,N), shape=(D,))
```

The loading matrix with automatic relevance determination (ARD) prior:

```
>>> alpha = Gamma(1e-5, 1e-5, plates=(D,))
>>> C = GaussianARD(0, alpha, plates=(M,1), shape=(D,))
```

Compute the dot product of the latent states and the loading matrix:

```
>>> F = SumMultiply('d, d->', X, C)
```

The observation noise:

```
>>> tau = Gamma(1e-5, 1e-5)
```

The observed variable:

```
>>> Y = GaussianARD(F, tau)
```

3.5.3 Inference

Observe the data:

```
>>> Y.observe(y)
```

We do not have missing data now, but they could be easily handled with mask keyword argument. Construct variational Bayesian (VB) inference engine:

```
>>> from bayespy.inference import VB
>>> Q = VB(Y, X, C, alpha, tau)
```

Initialize the latent subspace randomly, otherwise both X and C would converge to zero:

```
>>> C.initialize_from_random()
```

Now we could use VB.update() to run the inference. However, let us first create a parameter expansion to speed up the inference. The expansion is based on rotating the latent subspace optimally. This is optional but will usually improve the speed of the inference significantly, especially in high-dimensional problems:

```
>>> from bayespy.inference.vmp.transformations import RotateGaussianARD
>>> rot_X = RotateGaussianARD(X)
>>> rot_C = RotateGaussianARD(C, alpha)
```

By giving alpha for rot_C, the rotation will also optimize alpha jointly with C. Now that we have defined the rotations for our variables, we need to construct an optimizer:

```
>>> from bayespy.inference.vmp.transformations import RotationOptimizer
>>> R = RotationOptimizer(rot_X, rot_C, D)
```

In order to use the rotations automatically, we need to set it as a callback function:

```
>>> Q.set_callback(R.rotate)
```

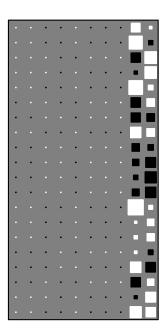
For more information about the rotation parameter expansion, see [2] and [1]. Now we can run the actual inference until convergence:

```
>>> Q.update(repeat=1000)
Iteration 1: loglike=-2.339710e+03 (... seconds)
...
Iteration 23: loglike=6.500608e+02 (... seconds)
Converged at iteration 23.
```

3.5.4 Results

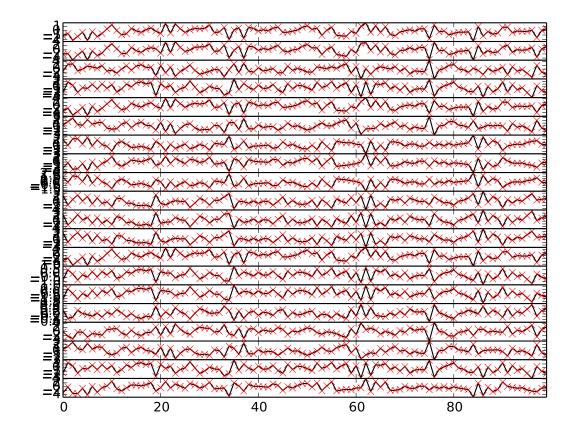
The results can be visualized, for instance, by plotting the Hinton diagram of the loading matrix:

```
>>> import bayespy.plot as bpplt
>>> bpplt.pyplot.figure()
<matplotlib.figure.Figure object at 0x...>
>>> bpplt.hinton(C)
```



The method has been able to prune out unnecessary latent dimensions and keep two components, which is the true number of components.

```
>>> bpplt.pyplot.figure()
<matplotlib.figure.Figure object at 0x...>
>>> bpplt.plot(F)
>>> bpplt.plot(f, color='r', marker='x', linestyle='None')
```



The reconstruction of the noiseless function values are practically perfect in this simple example. Larger noise variance, more latent space dimensions and missing values would make this problem more difficult. The model construction could also be improved by having, for instance, C and tau in the same node without factorizing between them in the posterior approximation. This can be achieved by using GaussianGammaISO node.

3.6 Linear state-space model

3.6.1 Model

In linear state-space models a sequence of M-dimensional observations $\mathbf{Y} = (\mathbf{y}_1, \dots, \mathbf{y}_N)$ is assumed to be generated from latent D-dimensional states $\mathbf{X} = (\mathbf{x}_1, \dots, \mathbf{x}_N)$ which follow a first-order Markov process:

$$\mathbf{x}_n = \mathbf{A}\mathbf{x}_{n-1} + \text{noise},$$

 $\mathbf{y}_n = \mathbf{C}\mathbf{x}_n + \text{noise},$

where the noise is Gaussian, A is the $D \times D$ state dynamics matrix and C is the $M \times D$ loading matrix. Usually, the latent space dimensionality D is assumed to be much smaller than the observation space dimensionality M in order to model the dependencies of high-dimensional observations efficiently.

In order to construct the model in BayesPy, first import relevant nodes:

```
>>> from bayespy.nodes import GaussianARD, GaussianMarkovChain, Gamma, Dot
```

The data vectors will be 30-dimensional:

```
>>> M = 30
```

There will be 400 data vectors:

```
>>> N = 400
```

Let us use 10-dimensional latent space:

```
>>> D = 10
```

The state dynamics matrix **A** has ARD prior:

Note that **A** is a $D \times D$ -dimensional matrix. However, in BayesPy it is modelled as a collection (plates=(D,)) of D-dimensional vectors (shape=(D,)) because this is how the variables factorize in the posterior approximation of the state dynamics matrix in GaussianMarkovChain. The latent states are constructed as

```
>>> X = GaussianMarkovChain(np.zeros(D),
... 1e-3*np.identity(D),
... A,
... np.ones(D),
... n=N,
... name='X')
```

where the first two arguments are the mean and precision matrix of the initial state, the third argument is the state dynamics matrix and the fourth argument is the diagonal elements of the precision matrix of the innovation noise. The node also needs the length of the chain given as the keyword argument n=N. Thus, the shape of this node is (N,D).

The linear mapping from the latent space to the observation space is modelled with the loading matrix which has ARD prior:

```
>>> gamma = Gamma(1e-5,
... 1e-5,
... plates=(D,),
... name='gamma')
>>> C = GaussianARD(0,
... gamma,
... shape=(D,),
... plates=(M,1),
... name='C')
```

Note that the plates for C are (M, 1), thus the full shape of the node is (M, 1, D). The unit plate axis is added so that C broadcasts with X when computing the dot product:

```
>>> F = Dot(C,
... X,
... name='F')
```

This dot product is computed over the D-dimensional latent space, thus the result is a $M \times N$ -dimensional matrix which is now represented with plates (M, N) in BayesPy:

```
>>> F.plates (30, 400)
```

We also need to use random initialization either for C or X in order to find non-zero latent space because by default both C and X are initialized to zero because of their prior distributions. We use random initialization for C and then we must update X the first time before updating C:

```
>>> C.initialize_from_random()
```

The precision of the observation noise is given gamma prior:

```
>>> tau = Gamma(1e-5,
... 1e-5,
... name='tau')
```

The observations are noisy versions of the dot products:

```
>>> Y = GaussianARD(F,
... tau,
... name='Y')
```

The variational Bayesian inference engine is then construced as:

```
>>> from bayespy.inference import VB
>>> Q = VB(X, C, gamma, A, alpha, tau, Y)
```

Note that X is given before C, thus X is updated before C by default.

3.6.2 Data

Now, let us generate some toy data for our model. Our true latent space is four dimensional with two noisy oscillator components, one random walk component and one white noise component.

The true linear mapping is just random:

```
>>> c = np.random.randn(M,4)
```

Then, generate the latent states and the observations using the model equations:

We want to simulate missing values, thus we create a mask which randomly removes 80% of the data:

```
>>> from bayespy.utils import random
>>> mask = random.mask(M, N, p=0.2)
>>> Y.observe(y, mask=mask)
```

3.6.3 Inference

As we did not define plotters for our nodes when creating the model, it is done now for some of the nodes:

```
>>> import bayespy.plot as bpplt
>>> X.set_plotter(bpplt.FunctionPlotter(center=True, axis=-2))
>>> A.set_plotter(bpplt.HintonPlotter())
>>> C.set_plotter(bpplt.HintonPlotter())
>>> tau.set_plotter(bpplt.PDFPlotter(np.linspace(0.02, 0.5, num=1000)))
```

This enables plotting of the approximate posterior distributions during VB learning. The inference engine can be run using VB.update() method:

```
>>> Q.update(repeat=10)
Iteration 1: loglike=-1.439704e+05 (... seconds)
...
Iteration 10: loglike=-1.051441e+04 (... seconds)
```

The iteration progresses a bit slowly, thus we'll consider parameter expansion to speed it up.

Parameter expansion

Section *Parameter expansion* discusses parameter expansion for state-space models to speed up inference. It is based on a rotating the latent space such that the posterior in the observation space is not affected:

$$\mathbf{y}_n = \mathbf{C}\mathbf{x}_n = (\mathbf{C}\mathbf{R}^{-1})(\mathbf{R}\mathbf{x}_n)$$
.

Thus, the transformation is $C \to CR^{-1}$ and $X \to RX$. In order to keep the dynamics of the latent states unaffected by the transformation, the state dynamics matrix A must be transformed accordingly:

$$\mathbf{R}\mathbf{x}_n = \mathbf{R}\mathbf{A}\mathbf{R}^{-1}\mathbf{R}\mathbf{x}_{n-1}$$
,

resulting in a transformation $A \to RAR^{-1}$. For more details, refer to [1] and [2]. In BayesPy, the transformations are available in bayespy.inference.vmp.transformations:

```
>>> from bayespy.inference.vmp import transformations
```

The rotation of the loading matrix along with the ARD parameters is defined as:

```
>>> rotC = transformations.RotateGaussianARD(C, gamma)
```

For rotating X, we first need to define the rotation of the state dynamics matrix:

```
>>> rotA = transformations.RotateGaussianARD(A, alpha)
```

Now we can define the rotation of the latent states:

```
>>> rotX = transformations.RotateGaussianMarkovChain(X, rotA)
```

The optimal rotation for all these variables is found using rotation optimizer:

```
>>> R = transformations.RotationOptimizer(rotX, rotC, D)
```

Set the parameter expansion to be applied after each iteration:

```
>>> Q.callback = R.rotate
```

Now, run iterations until convergence:

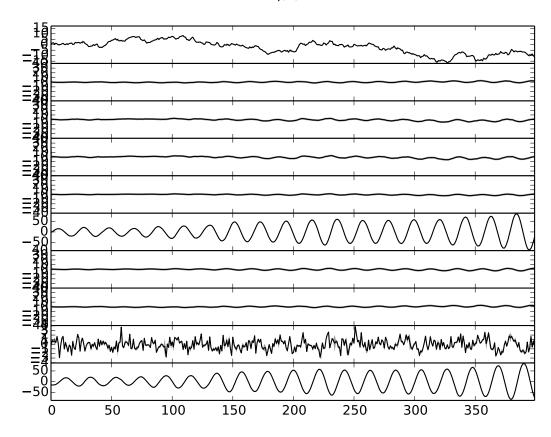
```
>>> Q.update(repeat=1000)
Iteration 11: loglike=-1.010806e+04 (... seconds)
...
Iteration 60: loglike=-8.906224e+03 (... seconds)
Converged at iteration 60.
```

3.6.4 Results

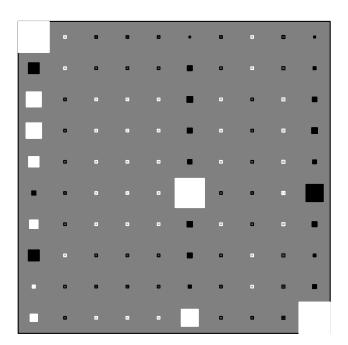
Because we have set the plotters, we can plot those nodes as:

```
>>> Q.plot(X, A, C, tau)
```

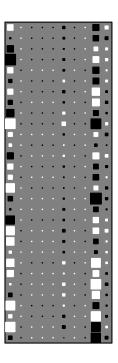


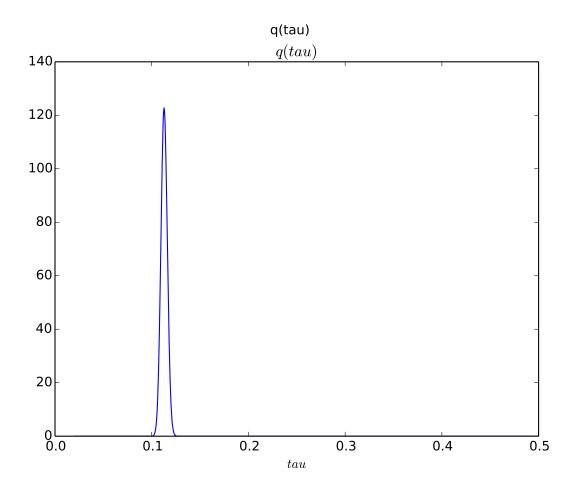


q(A)



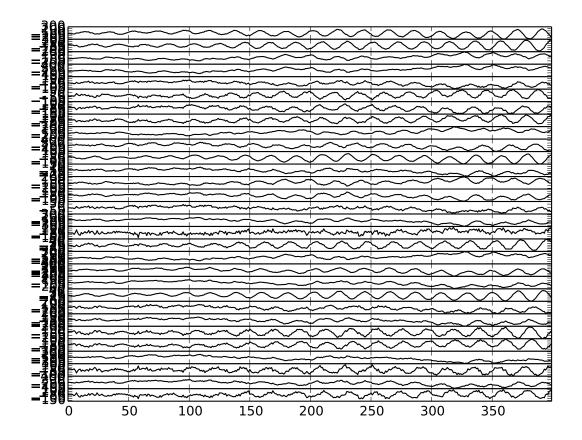
q(C)





There are clearly four effective components in X: random walk (component number 1), random oscillation (7 and 10), and white noise (9). These dynamics are also visible in the state dynamics matrix Hinton diagram. Note that the white noise component does not have any dynamics. Also C shows only four effective components. The posterior of tau captures the true value $3^{-2} \approx 0.111$ accurately. We can also plot predictions in the observation space:

```
>>> bpplt.plot(F, center=True)
```



We can also measure the performance numerically by computing root-mean-square error (RMSE) of the missing values:

```
>>> from bayespy.utils import misc
>>> misc.rmse(y[~mask], F.get_moments()[0][~mask])
5.182592...
```

This is relatively close to the standard deviation of the noise (3), so the predictions are quite good considering that only 20% of the data was used.

DEVELOPER GUIDE

How to document: https://github.com/numpy/numpy/blob/master/doc/HOWTO_DOCUMENT.rst.txt

How to contribute: http://docs.scipy.org/doc/numpy/dev/gitwash/development workflow.html

4.1 Variational message passing

The general update equation for factorized approximation:

$$\log q(\boldsymbol{\theta}) = \langle \log p(\boldsymbol{\theta}|\operatorname{pa}(\boldsymbol{\theta})) \rangle + \sum_{\mathbf{x} \in \operatorname{ch}(\boldsymbol{\theta})} \langle \log p(\mathbf{x}|\operatorname{pa}(\mathbf{x})) \rangle + \operatorname{const}, \tag{4.1}$$

where $pa(\theta)$ and $ch(\theta)$ are the set of parents and children of θ , respectively. The expectations are over the approximate distribution of all other variables than θ . Actually, not all the variables are needed, because the non-constant part uses only the Markov blanket of θ . Thus, the optimization can be done locally using messages from neighbouring nodes.

The messages are simple for conjugate-exponential models. Exponential-family distributions have the form

$$\log p(\mathbf{x}|\mathbf{\Theta}) = \mathbf{u}_{\mathbf{x}}(\mathbf{x})^{\mathrm{T}} \boldsymbol{\phi}_{\mathbf{x}}(\mathbf{\Theta}) + g_{\mathbf{x}}(\mathbf{\Theta}) + f_{\mathbf{x}}(\mathbf{x}), \tag{4.2}$$

where $\Theta = \{\theta_j\}$ is the set of parents. If a parent has a conjugate prior, (4.2) is linear with respect to the parent's natural statistics. Thus, (4.2) can be re-organized with respect to θ_j as

$$\log p(\mathbf{x}|\boldsymbol{\Theta}) = \mathbf{u}_{\boldsymbol{\theta}_j}(\boldsymbol{\theta}_j)^{\mathrm{T}} \boldsymbol{\phi}_{\mathbf{x} \to \boldsymbol{\theta}_j}(\mathbf{x}, \{\boldsymbol{\theta}_k\}_{k \neq j}) + \mathrm{const},$$

where \mathbf{u}_{θ_j} is the natural statistics of θ_j . Thus, the update equation (4.1) can be given as

$$\log q(\boldsymbol{\theta}_j) = \mathbf{u}_{\boldsymbol{\theta}_j}(\boldsymbol{\theta}_j)^{\mathrm{T}} \left(\langle \boldsymbol{\phi}_{\boldsymbol{\theta}_j} \rangle + \sum_{\mathbf{x} \in \mathrm{ch}(\boldsymbol{\theta}_j)} \langle \boldsymbol{\phi}_{\mathbf{x} \to \boldsymbol{\theta}_j} \rangle \right) + f_{\boldsymbol{\theta}_j}(\boldsymbol{\theta}_j) + \mathrm{const},$$

where the summation is over all the child nodes of θ_j . Because of the conjugacy, $\langle \phi_{\theta_j} \rangle$ depends (multi)linearly on the expectations of the parents' natural statistics. Similarly, $\langle \phi_{\mathbf{x} \to \theta_j} \rangle$ depends (multi)linearly on the expectations of the children's and co-parents' natural statistics.

The required expectations can be computed locally by using messages from the parents and the children. The message from a parent node θ_i to a child node x is

$$\mathbf{m}_{\boldsymbol{\theta}_{\mathbf{j}} \rightarrow \mathbf{x}} = \langle \mathbf{u}_{\boldsymbol{\theta}_{j}} \rangle = \tilde{\mathbf{u}}_{\boldsymbol{\theta}_{j}} (\tilde{\boldsymbol{\phi}}_{\boldsymbol{\theta}_{\mathbf{j}}}),$$

and the message from a child node x to a parent node θ_i is

$$\mathbf{m}_{\mathbf{x} \rightarrow \boldsymbol{\theta}_j} = \langle \boldsymbol{\phi}_{\mathbf{x} \rightarrow \boldsymbol{\theta}_j} \rangle = \boldsymbol{\phi}_{\mathbf{x} \rightarrow \boldsymbol{\theta}_j} \left(\langle \mathbf{u}_{\mathbf{x}} \rangle, \{ \mathbf{m}_{\boldsymbol{\theta}_k \rightarrow \mathbf{x}} \}_{k \neq j} \right).$$

Using the messages, the natural parameters of $q(\theta)$ can be updated as

$$\tilde{\phi}_{\boldsymbol{\theta}} = \phi_{\boldsymbol{\theta}} \left(\{ \mathbf{m}_{\mathbf{z} \rightarrow \boldsymbol{\theta}} \}_{\mathbf{z} \in \mathrm{pa}(\boldsymbol{\theta})} \right) + \sum_{\mathbf{x} \in \mathrm{ch}(\boldsymbol{\theta})} \mathbf{m}_{\mathbf{x} \rightarrow \boldsymbol{\theta}}.$$

4.2 Implementing nodes

CHAPTER

FIVE

USER API

bayespy.nodes	Package for nodes used to construct the model.
bayespy.inference	Package for Bayesian inference engines
bayespy.plot	Functions for plotting nodes.

5.1 bayespy.nodes

Package for nodes used to construct the model.

5.1.1 Stochastic nodes

Nodes for Gaussian variables:

Gaussian(mu, Lambda, **kwargs)	Node for Gaussian variables.
<pre>GaussianARD(mu, alpha[, ndim, shape])</pre>	Node for Gaussian variables with ARD prior.

bayespy.nodes.Gaussian

class bayespy.nodes.Gaussian (mu, Lambda, **kwargs)

Node for Gaussian variables.

The node represents a *D*-dimensional vector from the Gaussian distribution:

$$\mathbf{x} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Lambda}),$$

where μ is the mean vector and Λ is the precision matrix (i.e., inverse of the covariance matrix).

$$\mathbf{x}, \boldsymbol{\mu} \in \mathbb{R}^D, \quad \boldsymbol{\Lambda} \in \mathbb{R}^{D \times D}, \quad \boldsymbol{\Lambda}$$
 symmetric positive definite

Parameters mu: Gaussian-like node or GaussianGammaISO-like node or GaussianWishart-like node or array

Mean vector

Lambda: Wishart-like node or array

Precision matrix

See also:

Wishart, GaussianARD, GaussianWishart, GaussianGammaARD, GaussianGammaISO

Create Gaussian node

Methods

```
_init__(mu, Lambda, **kwargs)
                                                  Create Gaussian node
add_plate_axis(to_plate)
                                                  Delete this node and the children
delete()
get_mask()
get_moments()
get_shape(ind)
                                                  Return True if the node has a plotter
has plotter()
initialize_from_parameters(mu, Lambda)
initialize from prior()
initialize_from_random()
                                                  Set the variable to a random sample from the current distribution.
initialize from value(x, *args)
                                                  Load the state of the node from a HDF5 file.
load(group)
logpdf(X[, mask])
                                                  Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                                  Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                                  Compute the probability density function of this node.
plot(**kwargs)
                                                  Plot the node distribution using the plotter of the node
                                                  Draw a random sample from the distribution.
random()
rotate(R[, inv, logdet, Q])
rotate_matrix(R1, R2[, inv1, logdet1, inv2, ...])
                                                  The vector is reshaped into a matrix by stacking the row vectors.
                                                  Save the state of the node into a HDF5 file.
save(group)
set_plotter(plotter)
show()
unobserve()
update()
```

Gaussian.__init__ (mu, Lambda, **kwargs) Create Gaussian node bayespy.nodes.Gaussian.add_plate_axis Gaussian.add_plate_axis (to_plate) bayespy.nodes.Gaussian.delete Gaussian.delete() Delete this node and the children

bayespy.nodes.Gaussian.get mask

Gaussian.get_mask()

bayespy.nodes.Gaussian.__init__

Chapter 5. User API

```
bayespy.nodes.Gaussian.get moments
Gaussian.get_moments()
bayespy.nodes.Gaussian.get shape
Gaussian.get_shape (ind)
bayespy.nodes.Gaussian.has_plotter
Gaussian.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.Gaussian.initialize_from_parameters
Gaussian.initialize_from_parameters(mu, Lambda)
bayespy.nodes.Gaussian.initialize from prior
Gaussian.initialize from prior()
bayespy.nodes.Gaussian.initialize_from_random
Gaussian.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Gaussian.initialize_from_value
Gaussian.initialize_from_value(x, *args)
bayespy.nodes.Gaussian.load
Gaussian.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Gaussian.logpdf
Gaussian.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Gaussian.lower_bound_contribution
Gaussian.lower_bound_contribution(gradient=False)
```

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bayespy.nodes.Gaussian.lowerbound

```
Gaussian.lowerbound()
```

bayespy.nodes.Gaussian.move plates

```
Gaussian.move_plates (from_plate, to_plate)
```

bayespy.nodes.Gaussian.observe

```
Gaussian.observe(x, *args, mask=True)
```

Fix moments, compute f and propagate mask.

bayespy.nodes.Gaussian.pdf

```
Gaussian.pdf (X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Gaussian.plot

```
Gaussian.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Gaussian.random

```
Gaussian.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Gaussian.rotate

```
Gaussian.rotate(R, inv=None, logdet=None, Q=None)
```

bayespy.nodes.Gaussian.rotate_matrix

```
Gaussian.rotate_matrix(R1, R2, inv1=None, logdet1=None, inv2=None, logdet2=None, Q=None)
```

The vector is reshaped into a matrix by stacking the row vectors.

Computes R1*X*R2', which is identical to kron(R1,R2)*x (??)

Note that this is slightly different from the standard Kronecker product definition because Numpy stacks row vectors instead of column vectors.

Parameters R1: ndarray

A matrix from the left

R2: ndarray

A matrix from the right

bayespy.nodes.Gaussian.save

```
Gaussian. save (group)

Save the state of the node into a HDF5 file.

group can be the root
```

bayespy.nodes.Gaussian.set plotter

```
Gaussian.set_plotter(plotter)
```

bayespy.nodes.Gaussian.show

```
Gaussian.show()
```

bayespy.nodes.Gaussian.unobserve

```
Gaussian.unobserve()
```

bayespy.nodes.Gaussian.update

```
Gaussian.update()
```

Attributes

```
dims
plates
```

bayespy.nodes.Gaussian.dims

```
Gaussian.dims = None
```

bayespy.nodes.Gaussian.plates

```
Gaussian.plates = None
```

bayespy.nodes.GaussianARD

```
class bayespy.nodes.GaussianARD (mu, alpha, ndim=None, shape=None, **kwargs)
    Node for Gaussian variables with ARD prior.
```

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The node represents a *D*-dimensional vector from the Gaussian distribution:

$$\mathbf{x} \sim \mathcal{N}(\boldsymbol{\mu}, \operatorname{diag}(\boldsymbol{\alpha})),$$

where μ is the mean vector and diag(α) is the diagonal precision matrix (i.e., inverse of the covariance matrix).

$$\mathbf{x}, \boldsymbol{\mu} \in \mathbb{R}^D$$
, $\alpha_d > 0$ for $d = 0, \dots, D-1$

Note: The form of the posterior approximation is a Gaussian distribution with full covariance matrix instead of a diagonal matrix.

Parameters mu: Gaussian-like node or GaussianGammaISO-like node or GaussianGammaARD-like node or array

Mean vector

alpha: gamma-like node or array

Diagonal elements of the precision matrix

See also:

```
Gamma, Gaussian, GaussianGammaARD, GaussianGammaISO, GaussianWishart
```

```
__init__ (mu, alpha, ndim=None, shape=None, **kwargs)
Create GaussianARD node.
```

Methods

```
Create GaussianARD node.
 init (mu, alpha[, ndim, shape])
add_plate_axis(to_plate)
                                                          Delete this node and the children
delete()
get_mask()
get_moments()
get_shape(ind)
has_plotter()
                                                          Return True if the node has a plotter
initialize_from_mean_and_covariance(mu, Cov)
initialize_from_parameters(mu, alpha)
initialize_from_prior()
initialize_from_random()
                                                          Set the variable to a random sample from the current distribution.
initialize from value(x, *args)
load(group)
                                                          Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                                          Compute the log probability density function Q(X) of this node.
lower bound contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                                         Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                                          Compute the probability density function of this node.
plot(**kwargs)
                                                         Plot the node distribution using the plotter of the node
random()
                                                         Draw a random sample from the distribution.
rotate(R[, inv, logdet, axis, Q])
rotate_plates(Q[, plate_axis])
                                                          Approximate rotation of a plate axis.
                                                          Save the state of the node into a HDF5 file.
save(group)
set_plotter(plotter)
show()
unobserve()
update()
```

Chapter 5. User API

```
bayespy.nodes.GaussianARD. init
GaussianARD.__init__(mu, alpha, ndim=None, shape=None, **kwargs)
    Create GaussianARD node.
bayespy.nodes.GaussianARD.add plate axis
GaussianARD.add_plate_axis(to_plate)
bayespy.nodes.GaussianARD.delete
GaussianARD.delete()
    Delete this node and the children
bayespy.nodes.GaussianARD.get_mask
GaussianARD.get_mask()
bayespy.nodes.GaussianARD.get_moments
GaussianARD.get_moments()
bayespy.nodes.GaussianARD.get_shape
GaussianARD.get_shape (ind)
bayespy.nodes.GaussianARD.has_plotter
GaussianARD.has_plotter()
    Return True if the node has a plotter
bayes py. nodes. Gaussian ARD. initialize\_from\_mean\_and\_covariance
GaussianARD.initialize_from_mean_and_covariance (mu, Cov)
bayespy.nodes.GaussianARD.initialize_from_parameters
GaussianARD.initialize from parameters (mu, alpha)
bayespy.nodes.GaussianARD.initialize_from_prior
GaussianARD.initialize_from_prior()
```

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```
bayespy.nodes.GaussianARD.initialize from random
GaussianARD.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.GaussianARD.initialize from value
GaussianARD.initialize_from_value(x, *args)
bayespy.nodes.GaussianARD.load
GaussianARD.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.GaussianARD.logpdf
GaussianARD.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.GaussianARD.lower_bound_contribution
GaussianARD.lower_bound_contribution(gradient=False)
bayespy.nodes.GaussianARD.lowerbound
GaussianARD.lowerbound()
bayespy.nodes.GaussianARD.move_plates
GaussianARD.move_plates (from_plate, to_plate)
bayespy.nodes.GaussianARD.observe
GaussianARD.observe(x, *args, mask=True)
    Fix moments, compute f and propagate mask.
bayespy.nodes.GaussianARD.pdf
GaussianARD.pdf (X, mask=True)
    Compute the probability density function of this node.
```

bayespy.nodes.GaussianARD.plot

```
GaussianARD.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.GaussianARD.random

```
GaussianARD.random()
```

Draw a random sample from the distribution.

bayespy.nodes.GaussianARD.rotate

```
GaussianARD.rotate(R, inv=None, logdet=None, axis=-1, Q=None)
```

bayespy.nodes.GaussianARD.rotate_plates

```
GaussianARD.rotate_plates(Q, plate_axis=-1)
```

Approximate rotation of a plate axis.

Mean is rotated exactly but covariance/precision matrix is rotated approximately.

bayespy.nodes.GaussianARD.save

```
GaussianARD.save (group)

Save the state of the node into a HDF5 file.
```

group can be the root

bayespy.nodes.GaussianARD.set_plotter

```
GaussianARD.set_plotter(plotter)
```

bayespy.nodes.GaussianARD.show

```
GaussianARD.show()
```

bayespy.nodes.GaussianARD.unobserve

```
GaussianARD.unobserve()
```

bayespy.nodes.GaussianARD.update

```
GaussianARD.update()
```

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Attributes

```
dims plates
```

bayespy.nodes.GaussianARD.dims

GaussianARD.dims = None

bayespy.nodes.GaussianARD.plates

```
GaussianARD.plates = None
```

Nodes for precision and scale variables:

Gamma(a, b, **kwargs)	Node for gamma random variables.
Wishart(n, V, **kwargs)	Node for Wishart random variables.
<pre>Exponential(l, **kwargs)</pre>	Node for exponential random variables.

bayespy.nodes.Gamma

```
class bayespy.nodes.Gamma (a, b, **kwargs)
```

Node for gamma random variables.

Parameters a: scalar or array

Shape parameter

b : gamma-like node or scalar or array

Rate parameter

__init__(a, b, **kwargs)

Create gamma random variable node

Methods

init(a, b, **kwargs)	Create gamma random variable node
add_plate_axis(to_plate)	
as_diagonal_wishart()	
delete()	Delete this node and the children
get_mask()	
get_moments()	
get_shape(ind)	
has_plotter()	Return True if the node has a plotter
<pre>initialize_from_parameters(*args)</pre>	
<pre>initialize_from_prior()</pre>	
<pre>initialize_from_random()</pre>	Set the variable to a random sample from the current distribution.
$initialize_from_value(x, *args)$	
load(group)	Load the state of the node from a HDF5 file.
	Continued on next page

Table 5.8 – continued from previous page

```
Compute the log probability density function Q(X) of this node.
logpdf(X[, mask])
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                              Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                               Compute the probability density function of this node.
plot(**kwargs)
                                               Plot the node distribution using the plotter of the node
                                              Draw a random sample from the distribution.
random()
save(group)
                                               Save the state of the node into a HDF5 file.
set_plotter(plotter)
                                              Print the distribution using standard parameterization.
show()
unobserve()
update()
```

```
bayespy.nodes.Gamma. init
Gamma.___init___(a, b, **kwargs)
    Create gamma random variable node
bayespy.nodes.Gamma.add_plate_axis
Gamma.add_plate_axis(to_plate)
bayespy.nodes.Gamma.as diagonal wishart
Gamma.as_diagonal_wishart()
bayespy.nodes.Gamma.delete
Gamma.delete()
    Delete this node and the children
bayespy.nodes.Gamma.get mask
Gamma.get_mask()
bayespy.nodes.Gamma.get_moments
Gamma.get_moments()
bayespy.nodes.Gamma.get_shape
Gamma.get_shape (ind)
```

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```
bayespy.nodes.Gamma.has plotter
Gamma.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.Gamma.initialize from parameters
Gamma.initialize_from_parameters(*args)
bayespy.nodes.Gamma.initialize_from_prior
Gamma.initialize_from_prior()
bayespy.nodes.Gamma.initialize_from_random
Gamma.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Gamma.initialize from value
Gamma.initialize_from_value(x, *args)
bayespy.nodes.Gamma.load
Gamma.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Gamma.logpdf
Gamma.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Gamma.lower bound contribution
Gamma.lower_bound_contribution(gradient=False)
bayespy.nodes.Gamma.lowerbound
Gamma.lowerbound()
bayespy.nodes.Gamma.move_plates
Gamma.move_plates (from_plate, to_plate)
```

bayespy.nodes.Gamma.observe

```
Gamma.observe(x, *args, mask=True)
```

Fix moments, compute f and propagate mask.

bayespy.nodes.Gamma.pdf

```
Gamma.pdf (X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Gamma.plot

```
Gamma.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Gamma.random

```
Gamma.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Gamma.save

```
Gamma.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Gamma.set_plotter

```
Gamma.set_plotter(plotter)
```

bayespy.nodes.Gamma.show

```
Gamma.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Gamma.unobserve

```
Gamma.unobserve()
```

bayespy.nodes.Gamma.update

```
Gamma.update()
```

Attributes

dims	tuple() -> empty tuple
plates	

bayespy.nodes.Gamma.dims

Gamma.dims = ((), ())

bayespy.nodes.Gamma.plates

Gamma.plates = None

bayespy.nodes.Wishart

class bayespy.nodes.Wishart (n, V, **kwargs)

Node for Wishart random variables.

The random variable Λ is a $D \times D$ positive-definite symmetric matrix.

$$p(\mathbf{\Lambda}) = \text{Wishart}(\mathbf{\Lambda}|N, \mathbf{V})$$

Parameters n : scalar or array

N, degrees of freedom, N > D - 1.

V : Wishart-like node or (...,D,D)-array

V, scale matrix.

Methods

70

init(n, V, **kwargs)	Create Wishart node.
<pre>add_plate_axis(to_plate)</pre>	
delete()	Delete this node and the children
get_mask()	
get_moments()	
get_shape(ind)	
has_plotter()	Return True if the node has a plotter
<pre>initialize_from_parameters(*args)</pre>	
<pre>initialize_from_prior()</pre>	
<pre>initialize_from_random()</pre>	Set the variable to a random sample from the current distribution.
<pre>initialize_from_value(x, *args)</pre>	
load(group)	Load the state of the node from a HDF5 file.
logpdf(X[, mask])	Compute the log probability density function $Q(X)$ of this node.
<pre>lower_bound_contribution([gradient])</pre>	
lowerbound()	
<pre>move_plates(from_plate, to_plate)</pre>	
	Continued on next page

Table 5.10 – continued from previous page

```
observe(x, *args[, mask])

pdf(X[, mask])

plot(**kwargs)

random()

save(group)

set_plotter(plotter)

show()

unobserve()

update()

Fix moments, compute f and propagate mask.

Compute the probability density function of this node.

Plot the node distribution using the plotter of the node

Draw a random sample from the distribution.

Save the state of the node into a HDF5 file.
```

```
bayespy.nodes.Wishart.__init__
Wishart.__init__(n, V, **kwargs)
    Create Wishart node.
bayespy.nodes.Wishart.add plate axis
Wishart.add_plate_axis(to_plate)
bayespy.nodes.Wishart.delete
Wishart.delete()
    Delete this node and the children
bayespy.nodes.Wishart.get_mask
Wishart.get_mask()
bayespy.nodes.Wishart.get_moments
Wishart.get_moments()
bayespy.nodes.Wishart.get_shape
Wishart.get_shape(ind)
bayespy.nodes.Wishart.has_plotter
Wishart.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.Wishart.initialize_from_parameters
Wishart.initialize_from_parameters(*args)
```

```
bayespy.nodes.Wishart.initialize from prior
Wishart.initialize_from_prior()
bayespy.nodes.Wishart.initialize from random
Wishart.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Wishart.initialize_from_value
Wishart.initialize_from_value(x, *args)
bayespy.nodes.Wishart.load
Wishart.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Wishart.logpdf
Wishart.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Wishart.lower bound contribution
Wishart.lower_bound_contribution(gradient=False)
bayespy.nodes.Wishart.lowerbound
Wishart.lowerbound()
bayespy.nodes.Wishart.move plates
Wishart.move_plates (from_plate, to_plate)
bayespy.nodes.Wishart.observe
Wishart.observe(x, *args, mask=True)
    Fix moments, compute f and propagate mask.
bayespy.nodes.Wishart.pdf
Wishart.pdf(X, mask=True)
    Compute the probability density function of this node.
```

bayespy.nodes.Wishart.plot

```
Wishart.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Wishart.random

```
Wishart.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Wishart.save

```
Wishart.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Wishart.set_plotter

```
Wishart.set_plotter(plotter)
```

bayespy.nodes.Wishart.show

```
Wishart.show()
```

bayespy.nodes.Wishart.unobserve

```
Wishart.unobserve()
```

bayespy.nodes.Wishart.update

```
Wishart.update()
```

Attributes

dims plates

bayespy.nodes.Wishart.dims

```
Wishart.dims = None
```

bayespy.nodes.Wishart.plates

```
Wishart.plates = None
```

bayespy.nodes.Exponential

```
class bayespy.nodes.Exponential (l, **kwargs)
```

Node for exponential random variables.

Warning: Use Gamma instead of this. *Exponential(l)* is equivalent to *Gamma(1, l)*.

Parameters 1: gamma-like node or scalar or array

Rate parameter

See also:

Gamma, Poisson

Notes

For simplicity, this is just a gamma node with the first parent fixed to one. Note that this is a bit inconsistent with the BayesPy philosophy which states that the node does not only define the form of the prior distribution but more importantly the form of the posterior approximation. Thus, one might expect that this node would have exponential posterior distribution approximation. However, it has a gamma distribution. Also, the moments are gamma moments although only E[x] would be the moment of a exponential random variable. All this was done because: a) gamma was already implemented, so there was no need to implement anything, and b) people might easily use Exponential node as a prior definition and expect to get gamma posterior (which is what happens now). Maybe some day a pure Exponential node is implemented and the users are advised to use Gamma(1,b) if they want to use an exponential prior distribution but gamma posterior approximation.

```
__init__(l, **kwargs)
```

Methods

```
init__(l, **kwargs)
add_plate_axis(to_plate)
as_diagonal_wishart()
                                           Delete this node and the children
delete()
get_mask()
get_moments()
get_shape(ind)
has plotter()
                                          Return True if the node has a plotter
initialize from parameters(*args)
initialize_from_prior()
initialize from random()
                                           Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
load(group)
                                          Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                           Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
                                                                            Continued on next page
```

Table 5.12 – continued from previous page

	 oonanada nom providad pago
observe(x, *args[, mask])	Fix moments, compute f and propagate mask.
pdf(X[, mask])	Compute the probability density function of this node.
plot(**kwargs)	Plot the node distribution using the plotter of the node
random()	Draw a random sample from the distribution.
save(group)	Save the state of the node into a HDF5 file.
set_plotter(plotter)	
show()	Print the distribution using standard parameterization.
unobserve()	-
update()	

```
bayespy.nodes.Exponential.__init__
Exponential.__init__(l, **kwargs)
bayespy.nodes.Exponential.add plate axis
Exponential.add_plate_axis (to_plate)
bayespy.nodes.Exponential.as_diagonal_wishart
Exponential.as_diagonal_wishart()
bayespy.nodes.Exponential.delete
Exponential.delete()
    Delete this node and the children
bayespy.nodes.Exponential.get_mask
Exponential.get_mask()
bayespy.nodes.Exponential.get moments
Exponential.get_moments()
bayespy.nodes.Exponential.get_shape
Exponential.get_shape(ind)
bayespy.nodes.Exponential.has_plotter
Exponential.has_plotter()
```

Return True if the node has a plotter

```
bayespy.nodes.Exponential.initialize from parameters
Exponential.initialize_from_parameters(*args)
bayespy.nodes.Exponential.initialize_from_prior
Exponential.initialize_from_prior()
bayespy.nodes.Exponential.initialize_from_random
Exponential.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Exponential.initialize_from_value
Exponential.initialize_from_value(x, *args)
bayespy.nodes.Exponential.load
Exponential.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Exponential.logpdf
Exponential.logpdf (X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Exponential.lower_bound_contribution
Exponential.lower_bound_contribution(gradient=False)
bayespy.nodes.Exponential.lowerbound
Exponential.lowerbound()
bayespy.nodes.Exponential.move_plates
Exponential.move_plates (from_plate, to_plate)
bayespy.nodes.Exponential.observe
Exponential.observe(x, *args, mask=True)
    Fix moments, compute f and propagate mask.
```

bayespy.nodes.Exponential.pdf

```
Exponential.pdf(X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Exponential.plot

```
Exponential.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Exponential.random

```
Exponential.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Exponential.save

```
Exponential.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Exponential.set_plotter

```
Exponential.set_plotter(plotter)
```

bayespy.nodes.Exponential.show

```
Exponential.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Exponential.unobserve

```
Exponential.unobserve()
```

bayespy.nodes.Exponential.update

```
Exponential.update()

Continued on next page
```

Table 5.13 – continued from previous page

Attributes

dims	tuple() -> empty tuple
plates	

bayespy.nodes.Exponential.dims

```
Exponential.dims = ((), ())
```

bayespy.nodes.Exponential.plates

Exponential.plates = None

Nodes for modelling Gaussian and precision variables jointly (useful as prior for Gaussian nodes):

GaussianGammaISO(*args, **kwargs)	Node for Gaussian-gamma (isotropic) random variables.	
<pre>GaussianGammaARD(mu, alpha, a, b, **kwargs)</pre>	Node for Gaussian and gamma random variables with ARD form.	
<pre>GaussianWishart(*args, **kwargs)</pre>	Node for Gaussian-Wishart random variables.	

bayespy.nodes.GaussianGammalSO

 ${\bf class} \ {\tt bayespy.nodes.GaussianGammaISO} \ (*args, **kwargs)$

Node for Gaussian-gamma (isotropic) random variables.

The prior:

$$p(x, \alpha | \mu, \Lambda, a, b)$$
$$p(x | \alpha, \mu, \Lambda) = \mathcal{N}(x | \mu, \alpha Lambda)$$
$$p(\alpha | a, b) = \mathcal{G}(\alpha | a, b)$$

The posterior approximation $q(x,\alpha)$ has the same Gaussian-gamma form.

Currently, supports only vector variables.

Methods

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Table 5.15 – continued from previous page

```
initialize from parameters(*args)
initialize_from_prior()
initialize_from_random()
                                               Set the variable to a random sample from the current distribution.
initialize\_from\_value(x, *args)
load(group)
                                               Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                               Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                               Fix moments, compute f and propagate mask.
                                               Compute the probability density function of this node.
pdf(X[, mask])
plot(**kwargs)
                                               Plot the node distribution using the plotter of the node
plotmatrix()
                                               Creates a matrix of marginal plots.
random()
                                               Draw a random sample from the distribution.
save(group)
                                               Save the state of the node into a HDF5 file.
set_plotter(plotter)
show()
                                               Print the distribution using standard parameterization.
unobserve()
update()
```

```
bayespy.nodes.GaussianGammalSO. init
GaussianGammaISO.__init__(*args, **kwargs)
bayespy.nodes.GaussianGammalSO.add plate axis
GaussianGammaISO.add_plate_axis(to_plate)
bayespy.nodes.GaussianGammalSO.delete
GaussianGammaISO.delete()
    Delete this node and the children
bayespy.nodes.GaussianGammalSO.get gaussian mean and variance
GaussianGammaISO.get_gaussian_mean_and_variance()
    Return the mean and variance of the distribution
bayespy.nodes.GaussianGammalSO.get marginal logpdf
GaussianGammaISO.get_marginal_logpdf(gaussian=None, gamma=None)
    Get the (marginal) log pdf of a subset of the variables
        Parameters gaussian: list or None
             Indices of the Gaussian variables to keep or None
            gamma: bool or None
             True if keep the gamma variable, otherwise False or None
```

```
Returns function
```

A function which computes log-pdf

```
bayespy.nodes.GaussianGammalSO.get_mask
```

```
GaussianGammaISO.get_mask()
```

bayespy.nodes.GaussianGammalSO.get_moments

```
GaussianGammaISO.get_moments()
```

bayespy.nodes.GaussianGammalSO.get_shape

```
GaussianGammaISO.get_shape (ind)
```

bayespy.nodes.GaussianGammalSO.has plotter

```
GaussianGammaISO.has_plotter()
Return True if the node has a plotter
```

bayespy.nodes.GaussianGammalSO.initialize_from_parameters

```
GaussianGammaISO.initialize_from_parameters(*args)
```

bayespy.nodes.GaussianGammalSO.initialize_from_prior

```
GaussianGammaISO.initialize_from_prior()
```

bayespy.nodes.GaussianGammalSO.initialize from random

```
GaussianGammaISO.initialize_from_random()

Set the variable to a random sample from the current distribution.
```

bayespy.nodes.GaussianGammalSO.initialize from value

```
GaussianGammaISO.initialize_from_value(x, *args)
```

bayespy.nodes.GaussianGammalSO.load

```
GaussianGammaISO.load (group)

Load the state of the node from a HDF5 file.
```

bayespy.nodes.GaussianGammalSO.logpdf

```
GaussianGammaISO.logpdf(X, mask=True)
```

Compute the log probability density function Q(X) of this node.

bayespy.nodes.GaussianGammalSO.lower_bound_contribution

GaussianGammaISO.lower_bound_contribution(gradient=False)

bayespy.nodes.GaussianGammalSO.lowerbound

GaussianGammaISO.lowerbound()

bayespy.nodes.GaussianGammalSO.move_plates

GaussianGammaISO.move_plates (from_plate, to_plate)

bayespy.nodes.GaussianGammalSO.observe

```
GaussianGammaISO.observe(x, *args, mask=True)
```

Fix moments, compute f and propagate mask.

bayespy.nodes.GaussianGammalSO.pdf

```
GaussianGammaISO.pdf (X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.GaussianGammalSO.plot

```
GaussianGammaISO.plot (**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.GaussianGammalSO.plotmatrix

```
GaussianGammaISO.plotmatrix()
```

Creates a matrix of marginal plots.

On diagonal, are marginal plots of each variable. Off-diagonal plot (i,j) shows the joint marginal density of x_i and x_j .

bayespy.nodes.GaussianGammalSO.random

```
GaussianGammaISO.random()
```

Draw a random sample from the distribution.

bayespy.nodes.GaussianGammalSO.save

GaussianGammaISO.save (group)
Save the state of the node into a HDF5 file.
group can be the root

bayespy.nodes.GaussianGammalSO.set_plotter

GaussianGammaISO.set_plotter(plotter)

bayespy.nodes.GaussianGammalSO.show

GaussianGammaISO.show()

Print the distribution using standard parameterization.

bayespy.nodes.GaussianGammalSO.unobserve

GaussianGammaISO.unobserve()

bayespy.nodes.GaussianGammalSO.update

GaussianGammaISO.update()

Attributes

dims plates

bayespy.nodes.GaussianGammalSO.dims

GaussianGammaISO.dims = None

bayespy.nodes.GaussianGammalSO.plates

GaussianGammaISO.plates = None

bayespy.nodes.GaussianGammaARD

class bayespy.nodes.**GaussianGammaARD** (*mu*, *alpha*, *a*, *b*, **kwargs)

Node for Gaussian and gamma random variables with ARD form.

The prior:

$$p(x,\tau|\mu,\alpha,a,b) = p(x|\tau,\mu,\alpha)p(\tau|a,b)$$
$$p(x|\alpha,\mu,\alpha) = \mathcal{N}(x|\mu,\mathrm{diag}(\alpha \tau))$$
$$p(\tau|a,b) = \mathcal{G}(\tau|a,b)$$

The posterior approximation $q(x,\tau)$ has the same Gaussian-gamma form.

Warning: Not yet implemented.

See also:

```
Gaussian, GaussianARD, Gamma, GaussianGammaISO, GaussianWishart
__init__(mu, alpha, a, b, **kwargs)
```

Methods

```
__init___(mu, alpha, a, b, **kwargs)
add_plate_axis(to_plate)
                                             Delete this node and the children
delete()
get_mask()
get_moments()
get_shape(ind)
has_plotter()
                                             Return True if the node has a plotter
initialize_from_parameters(*args)
initialize_from_prior()
initialize from random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
load(group)
                                             Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
                                             Compute the probability density function of this node.
pdf(X[, mask])
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
                                             Draw a random sample from the distribution.
random()
save(group)
                                             Save the state of the node into a HDF5 file.
set_plotter(plotter)
unobserve()
update()
```

bayespy.nodes.GaussianGammaARD.__init__

```
GaussianGammaARD.__init__(mu, alpha, a, b, **kwargs)
```

bayespy.nodes.GaussianGammaARD.add_plate_axis

```
GaussianGammaARD.add_plate_axis(to_plate)
```

bayespy.nodes.GaussianGammaARD.delete

```
GaussianGammaARD.delete()

Delete this node and the children
```

```
bayespy.nodes.GaussianGammaARD.get_mask
GaussianGammaARD.get_mask()
bayespy.nodes.GaussianGammaARD.get moments
GaussianGammaARD.get_moments()
bayespy.nodes.GaussianGammaARD.get_shape
GaussianGammaARD.get_shape(ind)
bayespy.nodes.GaussianGammaARD.has_plotter
GaussianGammaARD.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.GaussianGammaARD.initialize from parameters
GaussianGammaARD.initialize_from_parameters(*args)
bayespy.nodes.GaussianGammaARD.initialize_from_prior
GaussianGammaARD.initialize_from_prior()
bayespy.nodes.GaussianGammaARD.initialize from random
GaussianGammaARD.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.GaussianGammaARD.initialize from value
GaussianGammaARD.initialize_from_value(x, *args)
bayespy.nodes.GaussianGammaARD.load
GaussianGammaARD.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.GaussianGammaARD.logpdf
GaussianGammaARD.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
```

bayespy.nodes.GaussianGammaARD.lower bound contribution

GaussianGammaARD.lower_bound_contribution(gradient=False)

bayespy.nodes.GaussianGammaARD.lowerbound

GaussianGammaARD.lowerbound()

bayespy.nodes.GaussianGammaARD.move_plates

GaussianGammaARD.move_plates (from_plate, to_plate)

bayespy.nodes.GaussianGammaARD.observe

GaussianGammaARD.**observe**(*x*, **args*, *mask=True*) Fix moments, compute f and propagate mask.

bayespy.nodes.GaussianGammaARD.pdf

```
GaussianGammaARD.pdf (X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.GaussianGammaARD.plot

```
GaussianGammaARD.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.GaussianGammaARD.random

```
GaussianGammaARD.random()
```

Draw a random sample from the distribution.

bayespy.nodes.GaussianGammaARD.save

```
GaussianGammaARD.save (group)
Save the state of the node into a HDF5 file.
group can be the root
```

bayespy.nodes.GaussianGammaARD.set_plotter

GaussianGammaARD.set_plotter(plotter)

bayespy.nodes.GaussianGammaARD.unobserve

GaussianGammaARD.unobserve()

bayespy.nodes.GaussianGammaARD.update

GaussianGammaARD.update()

Attributes

dims plates

bayespy.nodes.GaussianGammaARD.dims

GaussianGammaARD.dims = None

bayespy.nodes.GaussianGammaARD.plates

GaussianGammaARD.plates = None

bayespy.nodes.GaussianWishart

class bayespy.nodes.GaussianWishart(*args, **kwargs)

Node for Gaussian-Wishart random variables.

The prior:

$$p(x, \Lambda | \mu, \alpha, V, n)$$

$$p(x | \Lambda, \mu, \alpha) = (N)(x | \mu, \alpha^{-1} Lambda^{-1})$$

$$p(\Lambda | V, n) = (W)(\Lambda | n, V)$$

The posterior approximation $q(x, \Lambda)$ has the same Gaussian-Wishart form.

Currently, supports only vector variables.

Methods

Table 5.19 – continued from previous page

```
initialize_from_parameters(*args)
initialize_from_prior()
initialize_from_random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
load(group)
                                             Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
                                             Compute the probability density function of this node.
pdf(X[, mask])
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
                                             Draw a random sample from the distribution.
random()
                                             Save the state of the node into a HDF5 file.
save(group)
set_plotter(plotter)
                                             Print the distribution using standard parameterization.
show()
unobserve()
update()
```

```
bayespy.nodes.GaussianWishart.__init__

GaussianWishart.__init__(*args, **kwargs)

bayespy.nodes.GaussianWishart.add_plate_axis

GaussianWishart.add_plate_axis(to_plate)

bayespy.nodes.GaussianWishart.delete

GaussianWishart.delete()
    Delete this node and the children

bayespy.nodes.GaussianWishart.get_mask

GaussianWishart.get_mask()

bayespy.nodes.GaussianWishart.get_moments

GaussianWishart.get_moments()

bayespy.nodes.GaussianWishart.get_shape

GaussianWishart.get_shape(ind)
```

```
bayespy.nodes.GaussianWishart.has_plotter
GaussianWishart.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.GaussianWishart.initialize from parameters
GaussianWishart.initialize_from_parameters(*args)
bayespy.nodes.GaussianWishart.initialize_from_prior
GaussianWishart.initialize_from_prior()
bayespy.nodes.GaussianWishart.initialize from random
GaussianWishart.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.GaussianWishart.initialize from value
GaussianWishart.initialize_from_value(x, *args)
bayespy.nodes.GaussianWishart.load
GaussianWishart.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.GaussianWishart.logpdf
GaussianWishart.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.GaussianWishart.lower bound contribution
GaussianWishart.lower_bound_contribution(gradient=False)
bayespy.nodes.GaussianWishart.lowerbound
GaussianWishart.lowerbound()
bayespy.nodes.GaussianWishart.move_plates
GaussianWishart.move_plates (from_plate, to_plate)
```

bayespy.nodes.GaussianWishart.observe

```
GaussianWishart.observe (x, *args, mask=True) Fix moments, compute f and propagate mask.
```

bayespy.nodes.GaussianWishart.pdf

```
GaussianWishart.pdf (X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.GaussianWishart.plot

```
GaussianWishart.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.GaussianWishart.random

```
GaussianWishart.random()
```

Draw a random sample from the distribution.

bayespy.nodes.GaussianWishart.save

```
GaussianWishart.save (group)

Save the state of the node into a HDF5 file.
```

bayespy.nodes.GaussianWishart.set_plotter

```
GaussianWishart.set_plotter(plotter)
```

bayespy.nodes.GaussianWishart.show

```
GaussianWishart.show()
```

group can be the root

Print the distribution using standard parameterization.

bayespy.nodes.GaussianWishart.unobserve

```
GaussianWishart.unobserve()
```

bayespy.nodes.GaussianWishart.update

```
GaussianWishart.update()
```

Attributes

```
dims
plates
```

bayespy.nodes.GaussianWishart.dims

```
GaussianWishart.dims = None
```

bayespy.nodes.GaussianWishart.plates

```
GaussianWishart.plates = None
```

Nodes for discrete count variables:

Bernoulli(p, **kwargs)	Node for Bernoulli random variables.	
Binomial(n, p, **kwargs)	Node for binomial random variables.	
Categorical(p, **kwargs)	Node for categorical random variables.	
<pre>Multinomial(n, p, **kwargs)</pre>	Node for multinomial random variables.	
Poisson(l, **kwargs)	Node for Poisson random variables.	

bayespy.nodes.Bernoulli

```
class bayespy.nodes.Bernoulli(p, **kwargs)
```

Node for Bernoulli random variables.

The node models a binary random variable $z \in \{0,1\}$ with prior probability $p \in [0,1]$ for value one:

```
z \sim \text{Bernoulli}(p).
```

Parameters p: beta-like node

Probability of a successful trial

Examples

Methods

```
_init__(p, **kwargs)
                                             Create Bernoulli node.
add_plate_axis(to_plate)
                                             Delete this node and the children
delete()
get_mask()
get_moments()
get_shape(ind)
has_plotter()
                                             Return True if the node has a plotter
initialize_from_parameters(*args)
initialize from prior()
initialize from random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
                                             Load the state of the node from a HDF5 file.
load(group)
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                             Compute the probability density function of this node.
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
random()
                                             Draw a random sample from the distribution.
save(group)
                                             Save the state of the node into a HDF5 file.
set_plotter(plotter)
                                             Print the distribution using standard parameterization.
show()
unobserve()
update()
```

bayespy.nodes.Bernoulli.__init__

```
Bernoulli.__init__(p, **kwargs)
Create Bernoulli node.
```

bayespy.nodes.Bernoulli.add plate axis

```
Bernoulli.add_plate_axis(to_plate)
```

bayespy.nodes.Bernoulli.delete

```
Bernoulli.delete()

Delete this node and the children
```

bayespy.nodes.Bernoulli.get mask

```
Bernoulli.get_mask()
```

bayespy.nodes.Bernoulli.get_moments

```
Bernoulli.get_moments()
```

```
bayespy.nodes.Bernoulli.get_shape
Bernoulli.get_shape(ind)
bayespy.nodes.Bernoulli.has plotter
Bernoulli.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.Bernoulli.initialize_from_parameters
Bernoulli.initialize_from_parameters(*args)
bayespy.nodes.Bernoulli.initialize_from_prior
Bernoulli.initialize_from_prior()
bayespy.nodes.Bernoulli.initialize from random
Bernoulli.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Bernoulli.initialize_from_value
Bernoulli.initialize_from_value(x, *args)
bayespy.nodes.Bernoulli.load
Bernoulli.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Bernoulli.logpdf
Bernoulli.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Bernoulli.lower bound contribution
Bernoulli.lower_bound_contribution(gradient=False)
bayespy.nodes.Bernoulli.lowerbound
Bernoulli.lowerbound()
```

bayespy.nodes.Bernoulli.move plates

```
Bernoulli.move_plates (from_plate, to_plate)
```

bayespy.nodes.Bernoulli.observe

```
Bernoulli.observe(x, *args, mask=True)
```

Fix moments, compute f and propagate mask.

bayespy.nodes.Bernoulli.pdf

```
Bernoulli.pdf(X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Bernoulli.plot

```
Bernoulli.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Bernoulli.random

```
Bernoulli.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Bernoulli.save

```
Bernoulli.save (group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Bernoulli.set plotter

```
Bernoulli.set_plotter(plotter)
```

bayespy.nodes.Bernoulli.show

```
Bernoulli.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Bernoulli.unobserve

```
Bernoulli.unobserve()
```

bayespy.nodes.Bernoulli.update

```
Bernoulli.update()
```

Attributes

```
dims plates
```

bayespy.nodes.Bernoulli.dims

```
Bernoulli.dims = None
```

bayespy.nodes.Bernoulli.plates

```
Bernoulli.plates = None
```

bayespy.nodes.Binomial

```
{f class} bayespy.nodes.Binomial (n,p,**kwargs)
```

Node for binomial random variables.

The node models the number of successes $x \in \{0, \dots, n\}$ in n trials with probability p for success:

```
x \sim \text{Binomial}(n, p).
```

Parameters n: scalar or array

Number of trials

p: beta-like node or scalar or array

Probability of a success in a trial

See also:

```
Bernoulli, Multinomial, Beta
```

Examples

Methods

```
_init___(n, p, **kwargs)
                                             Create binomial node
add_plate_axis(to_plate)
                                             Delete this node and the children
delete()
get_mask()
get_moments()
get_shape(ind)
has plotter()
                                             Return True if the node has a plotter
initialize_from_parameters(*args)
initialize_from_prior()
initialize_from_random()
                                             Set the variable to a random sample from the current distribution.
initialize from value(x, *args)
                                             Load the state of the node from a HDF5 file.
load(group)
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                             Compute the probability density function of this node.
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
                                             Draw a random sample from the distribution.
random()
                                             Save the state of the node into a HDF5 file.
save(group)
set_plotter(plotter)
                                             Print the distribution using standard parameterization.
show()
unobserve()
update()
```

bayespy.nodes.Binomial. init

```
Binomial.__init__(n, p, **kwargs)
Create binomial node
```

bayespy.nodes.Binomial.add_plate_axis

```
Binomial.add_plate_axis(to_plate)
```

bayespy.nodes.Binomial.delete

```
Binomial.delete()

Delete this node and the children
```

bayespy.nodes.Binomial.get_mask

Binomial.get_mask()

bayespy.nodes.Binomial.get_moments

Binomial.get_moments()

```
bayespy.nodes.Binomial.get_shape
Binomial.get_shape(ind)
bayespy.nodes.Binomial.has plotter
Binomial.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.Binomial.initialize_from_parameters
Binomial.initialize_from_parameters(*args)
bayespy.nodes.Binomial.initialize_from_prior
Binomial.initialize_from_prior()
bayespy.nodes.Binomial.initialize from random
Binomial.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Binomial.initialize_from_value
Binomial.initialize_from_value(x, *args)
bayespy.nodes.Binomial.load
Binomial.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Binomial.logpdf
Binomial.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Binomial.lower bound contribution
Binomial.lower_bound_contribution(gradient=False)
bayespy.nodes.Binomial.lowerbound
Binomial.lowerbound()
```

bayespy.nodes.Binomial.move plates

```
Binomial.move_plates (from_plate, to_plate)
```

bayespy.nodes.Binomial.observe

```
Binomial.observe(x, *args, mask=True)
```

Fix moments, compute f and propagate mask.

bayespy.nodes.Binomial.pdf

```
Binomial.pdf (X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Binomial.plot

```
Binomial.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Binomial.random

```
Binomial.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Binomial.save

```
Binomial.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Binomial.set plotter

```
Binomial.set_plotter(plotter)
```

bayespy.nodes.Binomial.show

```
Binomial.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Binomial.unobserve

```
Binomial.unobserve()
```

bayespy.nodes.Binomial.update

```
Binomial.update()
```

Attributes

dims plates

bayespy.nodes.Binomial.dims

Binomial.dims = None

bayespy.nodes.Binomial.plates

Binomial.plates = None

bayespy.nodes.Categorical

class bayespy.nodes.Categorical(p, **kwargs)

Node for categorical random variables.

The node models a categorical random variable $x \in \{0, \dots, K-1\}$ with prior probabilities $\{p_0, \dots, p_{K-1}\}$ for each category:

$$p(x = k) = p_k$$
 for $k \in \{0, \dots, K - 1\}$.

Parameters p: Dirichlet-like node or (...,K)-array

Probabilities for each category

See also:

Bernoulli, Multinomial, Dirichlet

Methods

init(p, **kwargs)	Create Categorical node.
add_plate_axis(to_plate)	
delete()	Delete this node and the children
get_mask()	
<pre>get_moments()</pre>	
get_shape(ind)	
has_plotter()	Return True if the node has a plotter
<pre>initialize_from_parameters(*args)</pre>	
initialize_from_prior()	
<pre>initialize_from_random()</pre>	Set the variable to a random sample from the current distribution.
	Continued on next page

Table 5.26 – continued from previous page

```
initialize_from_value(x, *args)
                                              Load the state of the node from a HDF5 file.
load(group)
logpdf(X[, mask])
                                              Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                              Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                              Compute the probability density function of this node.
plot(**kwargs)
                                              Plot the node distribution using the plotter of the node
random()
                                              Draw a random sample from the distribution.
                                              Save the state of the node into a HDF5 file.
save(group)
set plotter(plotter)
show()
                                              Print the distribution using standard parameterization.
unobserve()
update()
```

```
bayespy.nodes.Categorical. init
Categorical.__init__(p, **kwargs)
    Create Categorical node.
bayespy.nodes.Categorical.add_plate_axis
Categorical.add_plate_axis(to_plate)
bayespy.nodes.Categorical.delete
Categorical.delete()
    Delete this node and the children
bayespy.nodes.Categorical.get_mask
Categorical.get_mask()
bayespy.nodes.Categorical.get moments
Categorical.get_moments()
bayespy.nodes.Categorical.get shape
Categorical.get_shape(ind)
bayespy.nodes.Categorical.has plotter
Categorical.has plotter()
```

Return True if the node has a plotter

```
bayespy.nodes.Categorical.initialize from parameters
Categorical.initialize_from_parameters(*args)
bayespy.nodes.Categorical.initialize_from_prior
Categorical.initialize_from_prior()
bayespy.nodes.Categorical.initialize_from_random
Categorical.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Categorical.initialize from value
Categorical.initialize_from_value(x, *args)
bayespy.nodes.Categorical.load
Categorical.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Categorical.logpdf
Categorical.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Categorical.lower_bound_contribution
Categorical.lower_bound_contribution (gradient=False)
bayespy.nodes.Categorical.lowerbound
Categorical.lowerbound()
bayespy.nodes.Categorical.move_plates
Categorical.move_plates (from_plate, to_plate)
bayespy.nodes.Categorical.observe
Categorical.observe(x, *args, mask=True)
    Fix moments, compute f and propagate mask.
```

bayespy.nodes.Categorical.pdf

```
Categorical.pdf(X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Categorical.plot

```
Categorical.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Categorical.random

```
Categorical.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Categorical.save

```
Categorical.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Categorical.set_plotter

```
Categorical.set_plotter(plotter)
```

bayespy.nodes.Categorical.show

```
Categorical.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Categorical.unobserve

```
Categorical.unobserve()
```

bayespy.nodes.Categorical.update

```
Categorical.update()

Continued on next page
```

Table 5.27 – continued from previous page

Attributes

dims plates

bayespy.nodes.Categorical.dims

Categorical.dims = None

bayespy.nodes.Categorical.plates

Categorical.plates = None

bayespy.nodes.Multinomial

class bayespy.nodes.Multinomial(n, p, **kwargs)

Node for multinomial random variables.

Assume there are K categories and N trials each of which leads a success for exactly one of the categories. Given the probabilities p_0, \ldots, p_{K-1} for the categories, multinomial distribution is gives the probability of any combination of numbers of successes for the categories.

The node models the number of successes $x_k \in \{0, ..., n\}$ in n trials with probability p_k for success in K categories.

$$\text{Multinomial}(\mathbf{x}|N,\mathbf{p}) = \frac{N!}{x_0! \cdots x_{K-1}!} p_0^{x_0} \cdots p_{K-1}^{x_{K-1}}$$

Parameters n: scalar or array

N, number of trials

p: Dirichlet-like node or (...,K)-array

p, probabilities of successes for the categories

See also:

```
Dirichlet, Binomial, Categorical
__init__(n, p, **kwargs)
```

Create Multinomial node.

Methods

init(n, p, **kwargs)	Create Multinomial node.	
<pre>add_plate_axis(to_plate)</pre>		
delete()	Delete this node and the children	
get_mask()		
get_moments()		
		Continued on next page

Table 5.28 – continued from previous page

```
get_shape(ind)
has_plotter()
                                             Return True if the node has a plotter
initialize_from_parameters(*args)
initialize_from_prior()
initialize_from_random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
load(group)
                                             Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                             Compute the probability density function of this node.
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
random()
                                             Draw a random sample from the distribution.
                                             Save the state of the node into a HDF5 file.
save(group)
set_plotter(plotter)
                                             Print the distribution using standard parameterization.
show()
unobserve()
update()
```

bayespy.nodes.Multinomial.__init__

```
Multinomial.__init__ (n, p, **kwargs)
Create Multinomial node.
```

bayespy.nodes.Multinomial.add_plate_axis

```
Multinomial.add_plate_axis(to_plate)
```

bayespy.nodes.Multinomial.delete

```
Multinomial.delete()

Delete this node and the children
```

bayespy.nodes.Multinomial.get_mask

```
Multinomial.get_mask()
```

bayespy.nodes.Multinomial.get_moments

Multinomial.get_moments()

bayespy.nodes.Multinomial.get_shape

Multinomial.get_shape(ind)

```
bayespy.nodes.Multinomial.has_plotter
Multinomial.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.Multinomial.initialize from parameters
Multinomial.initialize_from_parameters(*args)
bayespy.nodes.Multinomial.initialize_from_prior
Multinomial.initialize_from_prior()
bayespy.nodes.Multinomial.initialize_from_random
Multinomial.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Multinomial.initialize from value
Multinomial.initialize_from_value(x, *args)
bayespy.nodes.Multinomial.load
Multinomial.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Multinomial.logpdf
Multinomial.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Multinomial.lower bound contribution
Multinomial.lower_bound_contribution(gradient=False)
bayespy.nodes.Multinomial.lowerbound
Multinomial.lowerbound()
bayespy.nodes.Multinomial.move_plates
Multinomial.move_plates (from_plate, to_plate)
```

bayespy.nodes.Multinomial.observe

```
Multinomial.observe(x, *args, mask=True) Fix moments, compute f and propagate mask.
```

bayespy.nodes.Multinomial.pdf

```
Multinomial.pdf (X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Multinomial.plot

```
Multinomial.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Multinomial.random

```
Multinomial.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Multinomial.save

```
Multinomial.save(group)
Save the state of the node into a HDF5 file.
```

group can be the root

bayespy.nodes.Multinomial.set_plotter

```
Multinomial.set_plotter(plotter)
```

bayespy.nodes.Multinomial.show

```
Multinomial.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Multinomial.unobserve

```
Multinomial.unobserve()
```

bayespy.nodes.Multinomial.update

```
Multinomial.update()
```

Attributes

```
dims plates
```

bayespy.nodes.Multinomial.dims

Multinomial.dims = None

bayespy.nodes.Multinomial.plates

Multinomial.plates = None

bayespy.nodes.Poisson

class bayespy.nodes.Poisson(l, **kwargs)

Node for Poisson random variables.

The node uses Poisson distribution:

$$p(x) = Poisson(x|\lambda)$$

where λ is the rate parameter.

Parameters 1: gamma-like node or scalar or array

 λ , rate parameter

See also:

```
Gamma, Exponential
__init__(l, **kwargs)
Create Poisson random variable node
```

Methods

init(l, **kwargs)	Create Poisson random variable node
add_plate_axis(to_plate)	
delete()	Delete this node and the children
get_mask()	
<pre>get_moments()</pre>	
get_shape(ind)	
has_plotter()	Return True if the node has a plotter
<pre>initialize_from_parameters(*args)</pre>	
initialize_from_prior()	
initialize_from_random()	Set the variable to a random sample from the current distribution.
<pre>initialize_from_value(x, *args)</pre>	
load(group)	Load the state of the node from a HDF5 file.
logpdf(X[, mask])	Compute the log probability density function $Q(X)$ of this node.
<pre>lower_bound_contribution([gradient])</pre>	
	Continued on next page

Table 5.30 – continued from previous page

```
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                               Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                               Compute the probability density function of this node.
plot(**kwargs)
                                               Plot the node distribution using the plotter of the node
                                               Draw a random sample from the distribution.
random()
                                               Save the state of the node into a HDF5 file.
save(group)
set_plotter(plotter)
show()
                                               Print the distribution using standard parameterization.
unobserve()
update()
```

```
bayespy.nodes.Poisson.__init__
Poisson.__init__(l, **kwargs)
    Create Poisson random variable node
bayespy.nodes.Poisson.add plate axis
Poisson.add_plate_axis(to_plate)
bayespy.nodes.Poisson.delete
Poisson.delete()
    Delete this node and the children
bayespy.nodes.Poisson.get_mask
Poisson.get_mask()
bayespy.nodes.Poisson.get_moments
Poisson.get_moments()
bayespy.nodes.Poisson.get_shape
Poisson.get_shape(ind)
bayespy.nodes.Poisson.has_plotter
Poisson.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.Poisson.initialize_from_parameters
Poisson.initialize_from_parameters(*args)
```

```
bayespy.nodes.Poisson.initialize from prior
Poisson.initialize_from_prior()
bayespy.nodes.Poisson.initialize from random
Poisson.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Poisson.initialize_from_value
Poisson.initialize_from_value(x, *args)
bayespy.nodes.Poisson.load
Poisson.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Poisson.logpdf
Poisson.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Poisson.lower bound contribution
Poisson.lower_bound_contribution(gradient=False)
bayespy.nodes.Poisson.lowerbound
Poisson.lowerbound()
bayespy.nodes.Poisson.move_plates
Poisson.move_plates (from_plate, to_plate)
bayespy.nodes.Poisson.observe
Poisson.observe(x, *args, mask=True)
    Fix moments, compute f and propagate mask.
bayespy.nodes.Poisson.pdf
Poisson.pdf(X, mask=True)
    Compute the probability density function of this node.
```

bayespy.nodes.Poisson.plot

```
Poisson.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Poisson.random

```
Poisson.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Poisson.save

```
Poisson.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Poisson.set_plotter

```
Poisson.set_plotter(plotter)
```

bayespy.nodes.Poisson.show

```
Poisson.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Poisson.unobserve

```
Poisson.unobserve()
```

bayespy.nodes.Poisson.update

```
Poisson.update()
```

Attributes

dims tuple() -> empty tuple
plates

bayespy.nodes.Poisson.dims

```
Poisson.dims = ((),)
```

bayespy.nodes.Poisson.plates

```
Poisson.plates = None
```

Nodes for probabilities:

Beta(alpha, **kwargs)	Node for beta random variables.
Dirichlet(*args, **kwargs)	Node for Dirichlet random variables.

bayespy.nodes.Beta

```
class bayespy.nodes.Beta(alpha, **kwargs)
```

Node for beta random variables.

The node models a probability variable $p \in [0, 1]$ as

$$p \sim \text{Beta}(a, b)$$

where a and b are prior counts for success and failure, respectively.

Parameters alpha: (...,2)-shaped array

Two-element vector containing a and b

Examples

Methods

```
_init__(alpha, **kwargs)
                                           Create beta node
add_plate_axis(to_plate)
delete()
                                           Delete this node and the children
get_mask()
get_moments()
get_shape(ind)
has_plotter()
                                           Return True if the node has a plotter
initialize_from_parameters(*args)
initialize_from_prior()
                                           Set the variable to a random sample from the current distribution.
initialize_from_random()
initialize_from_value(x, *args)
                                           Load the state of the node from a HDF5 file.
load(group)
                                                                             Continued on next page
```

Table 5.33 – continued from previous page

```
Compute the log probability density function Q(X) of this node.
logpdf(X[, mask])
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                              Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                               Compute the probability density function of this node.
plot(**kwargs)
                                               Plot the node distribution using the plotter of the node
                                              Draw a random sample from the distribution.
random()
save(group)
                                               Save the state of the node into a HDF5 file.
set_plotter(plotter)
                                              Print the distribution using standard parameterization.
show()
unobserve()
update()
```

```
bayespy.nodes.Beta. init
Beta.__init__(alpha, **kwargs)
    Create beta node
bayespy.nodes.Beta.add plate axis
Beta.add_plate_axis(to_plate)
bayespy.nodes.Beta.delete
Beta.delete()
    Delete this node and the children
bayespy.nodes.Beta.get_mask
Beta.get_mask()
bayespy.nodes.Beta.get moments
Beta.get_moments()
bayespy.nodes.Beta.get shape
Beta.get_shape (ind)
bayespy.nodes.Beta.has_plotter
Beta.has_plotter()
    Return True if the node has a plotter
```

```
bayespy.nodes.Beta.initialize from parameters
Beta.initialize_from_parameters(*args)
bayespy.nodes.Beta.initialize_from_prior
Beta.initialize_from_prior()
bayespy.nodes.Beta.initialize_from_random
Beta.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Beta.initialize_from_value
Beta.initialize_from_value(x, *args)
bayespy.nodes.Beta.load
Beta.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Beta.logpdf
Beta.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Beta.lower_bound_contribution
Beta.lower_bound_contribution(gradient=False)
bayespy.nodes.Beta.lowerbound
Beta.lowerbound()
bayespy.nodes.Beta.move_plates
Beta.move_plates (from_plate, to_plate)
bayespy.nodes.Beta.observe
Beta.observe(x, *args, mask=True)
    Fix moments, compute f and propagate mask.
```

bayespy.nodes.Beta.pdf

```
Beta.pdf(X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Beta.plot

```
Beta.plot (**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Beta.random

```
Beta.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Beta.save

```
Beta.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Beta.set_plotter

```
Beta.set_plotter(plotter)
```

bayespy.nodes.Beta.show

```
Beta.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Beta.unobserve

```
Beta.unobserve()
```

bayespy.nodes.Beta.update

```
Beta.update()
```

Continued on next page

Table 5.34 – continued from previous page

Attributes

dims plates

bayespy.nodes.Beta.dims

Beta.dims = None

bayespy.nodes.Beta.plates

Beta.plates = None

bayespy.nodes.Dirichlet

class bayespy.nodes.Dirichlet (*args, **kwargs)

Node for Dirichlet random variables.

The node models a set of probabilities $\{\pi_0,\ldots,\pi_{K-1}\}$ which satisfy $\sum_{k=0}^{K-1}\pi_k=1$ and $\pi_k\in[0,1]$ $\forall k=0,\ldots,K-1$.

$$p(\pi_0, \dots, \pi_{K-1}) = Dirichlet(\alpha_0, \dots, \alpha_{K-1})$$

where α_k are concentration parameters.

The posterior approximation has the same functional form but with different concentration parameters.

Parameters alpha: (...,K)-shaped array

Prior counts α_k

See also:

Beta, Categorical, Multinomial, CategoricalMarkovChain
__init___(*args, **kwargs)

Methods

Table 5.35 – continued from previous page

```
initialize_from_value(x, *args)
                                              Load the state of the node from a HDF5 file.
load(group)
logpdf(X[, mask])
                                              Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                              Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                              Compute the probability density function of this node.
plot(**kwargs)
                                              Plot the node distribution using the plotter of the node
random()
                                              Draw a random sample from the distribution.
                                              Save the state of the node into a HDF5 file.
save(group)
set plotter(plotter)
                                              Print the distribution using standard parameterization.
show()
unobserve()
update()
```

```
bayespy.nodes.Dirichlet. init
Dirichlet.___init___(*args, **kwargs)
bayespy.nodes.Dirichlet.add plate axis
Dirichlet.add_plate_axis(to_plate)
bayespy.nodes.Dirichlet.delete
Dirichlet.delete()
    Delete this node and the children
bayespy.nodes.Dirichlet.get_mask
Dirichlet.get_mask()
bayespy.nodes.Dirichlet.get_moments
Dirichlet.get_moments()
bayespy.nodes.Dirichlet.get_shape
Dirichlet.get_shape(ind)
bayespy.nodes.Dirichlet.has plotter
Dirichlet.has_plotter()
    Return True if the node has a plotter
```

```
bayespy.nodes.Dirichlet.initialize from parameters
Dirichlet.initialize_from_parameters(*args)
bayespy.nodes.Dirichlet.initialize_from_prior
Dirichlet.initialize_from_prior()
bayespy.nodes.Dirichlet.initialize_from_random
Dirichlet.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.Dirichlet.initialize_from_value
Dirichlet.initialize_from_value(x, *args)
bayespy.nodes.Dirichlet.load
Dirichlet.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Dirichlet.logpdf
Dirichlet.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Dirichlet.lower_bound_contribution
Dirichlet.lower_bound_contribution(gradient=False)
bayespy.nodes.Dirichlet.lowerbound
Dirichlet.lowerbound()
bayespy.nodes.Dirichlet.move_plates
Dirichlet.move_plates (from_plate, to_plate)
bayespy.nodes.Dirichlet.observe
Dirichlet.observe(x, *args, mask=True)
    Fix moments, compute f and propagate mask.
```

bayespy.nodes.Dirichlet.pdf

```
Dirichlet.pdf(X, mask=True)
```

Compute the probability density function of this node.

bayespy.nodes.Dirichlet.plot

```
Dirichlet.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Dirichlet.random

```
Dirichlet.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Dirichlet.save

```
Dirichlet.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Dirichlet.set_plotter

```
Dirichlet.set_plotter(plotter)
```

bayespy.nodes.Dirichlet.show

```
Dirichlet.show()
```

Print the distribution using standard parameterization.

bayespy.nodes.Dirichlet.unobserve

```
Dirichlet.unobserve()
```

bayespy.nodes.Dirichlet.update

```
Dirichlet.update()

Continued on next page
```

Table 5.36 – continued from previous page

Attributes

dims plates

bayespy.nodes.Dirichlet.dims

Dirichlet.dims = None

bayespy.nodes.Dirichlet.plates

Dirichlet.plates = None

Nodes for dynamic variables:

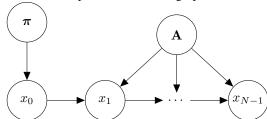
CategoricalMarkovChain(pi, A[, states])	Node for categorical Markov chain random variables.
<pre>GaussianMarkovChain(mu, Lambda, A, nu[, n])</pre>	Node for Gaussian Markov chain random variables.
SwitchingGaussianMarkovChain(mu, Lambda, B,)	Node for Gaussian Markov chain random variables with switching d
VaryingGaussianMarkovChain(mu, Lambda, B, S, nu)	Node for Gaussian Markov chain random variables with time-varyin

bayespy.nodes.CategoricalMarkovChain

class bayespy.nodes.CategoricalMarkovChain(pi, A, states=None, **kwargs)

Node for categorical Markov chain random variables.

The node models a Markov chain which has a discrete set of K possible states and the next state depends only on the previous state and the state transition probabilities. The graphical model is shown below:



where π contains the probabilities for the initial state and **A** is the state transition probability matrix. It is possible to have **A** varying in time.

$$p(x_0, \dots, x_{N-1}) = p(x_0) \prod_{n=1}^{N-1} p(x_n | x_{n-1}),$$

where

$$p(x_0 = k) = \pi_k, \quad \text{for } k \in \{0, \dots, K - 1\},$$

$$p(x_n = j | x_{n-1} = i) = a_{ij}^{(n-1)} \quad \text{for } n = 1, \dots, N - 1, \ i \in \{1, \dots, K - 1\}, \ j \in \{1, \dots, K - 1\}$$

$$a_{ij}^{(n)} = [\mathbf{A}_n]_{ij}$$

This node can be used to construct hidden Markov models by using Mixture for the emission distribution.

```
Parameters pi: Dirichlet-like node or (...,K)-array
```

 π , probabilities for the first state. K-dimensional Dirichlet.

A: Dirichlet-like node or (K,K)-array or (...,1,K,K)-array or (...,N-1,K,K)-array

A, probabilities for state transitions. K-dimensional Dirichlet with plates (K,) or (...,1,K) or (...,N-1,K).

states: int, optional

N, the length of the chain.

See also:

Categorical, Dirichlet, GaussianMarkovChain, Mixture, SwitchingGaussianMarkovChain

__init__ (pi, A, states=None, **kwargs)
Create categorical Markov chain

Methods

```
_init___(pi, A[, states])
                                             Create categorical Markov chain
add_plate_axis(to_plate)
delete()
                                             Delete this node and the children
get mask()
get_moments()
get_shape(ind)
has_plotter()
                                             Return True if the node has a plotter
initialize_from_parameters(*args)
initialize_from_prior()
initialize_from_random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
                                             Load the state of the node from a HDF5 file.
load(group)
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                             Compute the probability density function of this node.
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
                                             Draw a random sample from the distribution.
random()
save(group)
                                             Save the state of the node into a HDF5 file.
set_plotter(plotter)
                                             Print the distribution using standard parameterization.
show()
unobserve()
update()
```

bayespy.nodes.CategoricalMarkovChain.__init__

```
CategoricalMarkovChain.__init__(pi, A, states=None, **kwargs)
Create categorical Markov chain
```

```
bayespy.nodes.CategoricalMarkovChain.add_plate_axis
CategoricalMarkovChain.add_plate_axis(to_plate)
bayespy.nodes.CategoricalMarkovChain.delete
CategoricalMarkovChain.delete()
    Delete this node and the children
bayespy.nodes.CategoricalMarkovChain.get mask
CategoricalMarkovChain.get_mask()
bayespy.nodes.CategoricalMarkovChain.get moments
CategoricalMarkovChain.get_moments()
bayespy.nodes.CategoricalMarkovChain.get_shape
CategoricalMarkovChain.get shape(ind)
bayespy.nodes.CategoricalMarkovChain.has_plotter
CategoricalMarkovChain.has_plotter()
    Return True if the node has a plotter
bayes py. nodes. Categorical Markov Chain. in itialize\_from\_parameters
CategoricalMarkovChain.initialize_from_parameters(*args)
bayespy.nodes.CategoricalMarkovChain.initialize from prior
CategoricalMarkovChain.initialize_from_prior()
bayespy.nodes.CategoricalMarkovChain.initialize_from_random
CategoricalMarkovChain.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.CategoricalMarkovChain.initialize from value
CategoricalMarkovChain.initialize_from_value(x, *args)
```

bayespy.nodes.CategoricalMarkovChain.load

```
CategoricalMarkovChain.load(group)

Load the state of the node from a HDF5 file.
```

bayespy.nodes.CategoricalMarkovChain.logpdf

```
CategoricalMarkovChain.logpdf(X, mask=True)
Compute the log probability density function Q(X) of this node.
```

$bayes py. nodes. Categorical Markov Chain. lower_bound_contribution$

```
CategoricalMarkovChain.lower_bound_contribution(gradient=False)
```

bayespy.nodes.CategoricalMarkovChain.lowerbound

```
CategoricalMarkovChain.lowerbound()
```

bayespy.nodes.CategoricalMarkovChain.move_plates

```
CategoricalMarkovChain.move_plates (from_plate, to_plate)
```

bayespy.nodes.CategoricalMarkovChain.observe

```
CategoricalMarkovChain.observe(x, *args, mask=True) Fix moments, compute f and propagate mask.
```

bayespy.nodes.CategoricalMarkovChain.pdf

```
CategoricalMarkovChain.pdf (X, mask=True)

Compute the probability density function of this node.
```

bayespy.nodes.CategoricalMarkovChain.plot

```
CategoricalMarkovChain.plot (**kwargs)

Plot the node distribution using the plotter of the node
```

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.CategoricalMarkovChain.random

```
CategoricalMarkovChain.random()

Draw a random sample from the distribution.
```

bayespy.nodes.CategoricalMarkovChain.save

```
CategoricalMarkovChain.save (group)
Save the state of the node into a HDF5 file.
group can be the root
```

bayespy.nodes.CategoricalMarkovChain.set_plotter

CategoricalMarkovChain.set_plotter(plotter)

bayespy.nodes.CategoricalMarkovChain.show

```
CategoricalMarkovChain.show()

Print the distribution using standard parameterization.
```

bayespy.nodes.CategoricalMarkovChain.unobserve

CategoricalMarkovChain.unobserve()

bayespy.nodes.CategoricalMarkovChain.update

CategoricalMarkovChain.update()

Attributes

dims plates

bayespy.nodes.CategoricalMarkovChain.dims

 ${\tt Categorical Markov Chain. dims} = None$

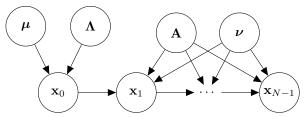
bayes py. nodes. Categorical Markov Chain. plates

CategoricalMarkovChain.plates = None

bayespy.nodes.GaussianMarkovChain

class bayespy.nodes.GaussianMarkovChain (mu, Lambda, A, nu, n=None, **kwargs)
Node for Gaussian Markov chain random variables.

In a simple case, the graphical model can be presented as:



where μ and Λ are the mean and the precision matrix of the initial state, \mathbf{A} is the state dynamics matrix and ν is the precision of the innovation noise. It is possible that \mathbf{A} and/or ν are different for each transition instead of being constant.

The probability distribution is

$$p(\mathbf{x}_0, \dots, \mathbf{x}_{N-1}) = p(\mathbf{x}_0) \prod_{n=1}^{N-1} p(\mathbf{x}_n | \mathbf{x}_{n-1})$$

where

$$\begin{split} p(\mathbf{x}_0) &= \mathcal{N}(\mathbf{x}_0 | \boldsymbol{\mu}, \boldsymbol{\Lambda}) \\ p(\mathbf{x}_n | \mathbf{x}_{n-1}) &= \mathcal{N}(\mathbf{x}_n | \mathbf{A}_{n-1} \mathbf{x}_{n-1}, \operatorname{diag}(\boldsymbol{\nu}_{n-1})). \end{split}$$

Parameters mu: Gaussian-like node or (...,D)-array

 μ , mean of x_0 , D-dimensional with plates (...)

Lambda: Wishart-like node or (...,D,D)-array

 Λ , precision matrix of x_0 , $D \times D$ -dimensional with plates (...)

A: Gaussian-like node or (D,D)-array or (...,1,D,D)-array or (...,N-1,D,D)-array

A, state dynamics matrix, D-dimensional with plates (D,) or (...,1,D) or (...,N-1,D)

nu: gamma-like node or (D,)-array or (...,1,D)-array or (...,N-1,D)-array

 ν , diagonal elements of the precision of the innovation process, plates (D,) or (...,1,D) or (...,N-1,D)

n: int, optional

N, the length of the chain. Must be given if A and ν are constant over time.

See also:

Gaussian, GaussianARD, Wishart, Gamma, SwitchingGaussianMarkovChain, VaryingGaussianMarkovChain, CategoricalMarkovChain

__init__ (mu, Lambda, A, nu, n=None, **kwargs)
Create GaussianMarkovChain node.

Methods

init(mu, Lambda, A, nu[, n])	Create GaussianMarkovChain node.	
<pre>add_plate_axis(to_plate)</pre>		
delete()	Delete this node and the children	
get_mask()		
<pre>get_moments()</pre>		
get_shape(ind)		
has_plotter()	Return True if the node has a plotter	
		Continued on next page

Table 5.40 – continued from previous page

```
initialize_from_parameters(*args)
initialize_from_prior()
initialize_from_random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
load(group)
                                             Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
                                             Compute the probability density function of this node.
pdf(X[, mask])
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
random()
                                             Draw a random sample from the distribution.
rotate(R[, inv, logdet])
save(group)
                                             Save the state of the node into a HDF5 file.
set_plotter(plotter)
show()
unobserve()
update()
```

bayespy.nodes.GaussianMarkovChain. init

```
GaussianMarkovChain.__init__ (mu, Lambda, A, nu, n=None, **kwargs)
Create GaussianMarkovChain node.
```

bayespy.nodes.GaussianMarkovChain.add plate axis

```
GaussianMarkovChain.add_plate_axis(to_plate)
```

bayespy.nodes.GaussianMarkovChain.delete

```
GaussianMarkovChain.delete()

Delete this node and the children
```

bayespy.nodes.GaussianMarkovChain.get mask

```
GaussianMarkovChain.get_mask()
```

bayespy.nodes.GaussianMarkovChain.get_moments

GaussianMarkovChain.get_moments()

bayespy.nodes.GaussianMarkovChain.get_shape

GaussianMarkovChain.get_shape (ind)

```
bayespy.nodes.GaussianMarkovChain.has_plotter
GaussianMarkovChain.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.GaussianMarkovChain.initialize from parameters
GaussianMarkovChain.initialize_from_parameters(*args)
bayespy.nodes.GaussianMarkovChain.initialize_from_prior
GaussianMarkovChain.initialize_from_prior()
bayespy.nodes.GaussianMarkovChain.initialize_from_random
GaussianMarkovChain.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.GaussianMarkovChain.initialize from value
GaussianMarkovChain.initialize_from_value(x, *args)
bayespy.nodes.GaussianMarkovChain.load
GaussianMarkovChain.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.GaussianMarkovChain.logpdf
GaussianMarkovChain.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.GaussianMarkovChain.lower bound contribution
GaussianMarkovChain.lower_bound_contribution(gradient=False)
bayespy.nodes.GaussianMarkovChain.lowerbound
GaussianMarkovChain.lowerbound()
bayespy.nodes.GaussianMarkovChain.move_plates
GaussianMarkovChain.move_plates(from_plate, to_plate)
```

bayespy.nodes.GaussianMarkovChain.observe

```
GaussianMarkovChain.observe(x, *args, mask=True) Fix moments, compute f and propagate mask.
```

bayespy.nodes.GaussianMarkovChain.pdf

```
GaussianMarkovChain.pdf (X, mask=True)

Compute the probability density function of this node.
```

bayespy.nodes.GaussianMarkovChain.plot

```
GaussianMarkovChain.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.GaussianMarkovChain.random

```
GaussianMarkovChain.random()
```

Draw a random sample from the distribution.

bayespy.nodes.GaussianMarkovChain.rotate

```
GaussianMarkovChain.rotate(R, inv=None, logdet=None)
```

bayes py. nodes. Gaussian Markov Chain. save

```
GaussianMarkovChain.save (group)
Save the state of the node into a HDF5 file.
group can be the root
```

bayespy.nodes.GaussianMarkovChain.set plotter

```
GaussianMarkovChain.set_plotter(plotter)
```

bayespy.nodes.GaussianMarkovChain.show

```
GaussianMarkovChain.show()
```

bayespy.nodes.GaussianMarkovChain.unobserve

```
GaussianMarkovChain.unobserve()
```

bayespy.nodes.GaussianMarkovChain.update

GaussianMarkovChain.update()

Attributes

dims plates

bayespy.nodes.GaussianMarkovChain.dims

GaussianMarkovChain.dims = None

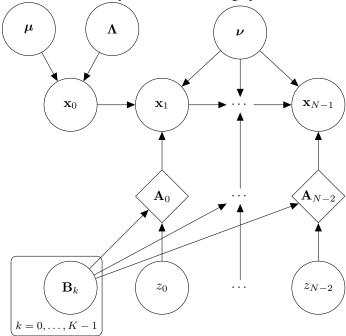
bayespy.nodes.GaussianMarkovChain.plates

GaussianMarkovChain.plates = None

bayespy.nodes.SwitchingGaussianMarkovChain

Node for Gaussian Markov chain random variables with switching dynamics.

The node models a sequence of Gaussian variables :math: $\{x\}_0$, in the factorial Markovian dynamics. The dynamics may change in time, which is obtained by having a set of matrices and at each time selecting one of them as the state dynamics matrix. The graphical model can be presented as:



where μ and Λ are the mean and the precision matrix of the initial state, ν is the precision of the innovation noise, and \mathbf{A}_n are the state dynamics matrix obtained by selecting one of the matrices $\{\mathbf{B}_k\}_{k=0}^{K-1}$ at each time.

The selections are provided by $z_n \in \{0, \dots, K-1\}$. The probability distribution is

$$p(\mathbf{x}_0,\ldots,\mathbf{x}_{N-1}) = p(\mathbf{x}_0) \prod_{n=1}^{N-1} p(\mathbf{x}_n|\mathbf{x}_{n-1})$$

where

$$p(\mathbf{x}_0) = \mathcal{N}(\mathbf{x}_0 | \boldsymbol{\mu}, \boldsymbol{\Lambda})$$

$$p(\mathbf{x}_n | \mathbf{x}_{n-1}) = \mathcal{N}(\mathbf{x}_n | \mathbf{A}_{n-1} \mathbf{x}_{n-1}, \operatorname{diag}(\boldsymbol{\nu})), \quad \text{for } n = 1, \dots, N-1,$$

$$\mathbf{A}_n = \mathbf{B}_{z_n}, \quad \text{for } n = 0, \dots, N-2.$$

Parameters mu: Gaussian-like node or (...,D)-array

 μ , mean of x_0 , D-dimensional with plates (...)

Lambda: Wishart-like node or (...,D,D)-array

 Λ , precision matrix of x_0 , $D \times D$ -dimensional with plates (...)

B: Gaussian-like node or (...,D,D,K)-array

 $\{\mathbf{B}_k\}_{k=0}^{K-1}$, a set of state dynamics matrix, $D \times K$ -dimensional with plates (...,D)

Z: categorical-like node or (...,N-1)-array

 $\{z_0, \ldots, z_{N-2}\}$, time-dependent selection, K-categorical with plates (...,N-1)

nu: gamma-like node or (...,D)-array

 ν , diagonal elements of the precision of the innovation process, plates (...,D)

n: int, optional

N, the length of the chain. Must be given if **Z** does not have plates over the time domain (which would not make sense).

See also:

Gaussian, GaussianARD, Wishart, Gamma, GaussianMarkovChain, VaryingGaussianMarkovChain, Categorical, CategoricalMarkovChain

Notes

Equivalent model block can be constructed with GaussianMarkovChain by explicitly using Gate to select the state dynamics matrix. However, that approach is not very efficient for large datasets because it does not utilize the structure of A_n , thus it explicitly computes huge moment arrays.

```
__init__ (mu, Lambda, B, Z, nu, n=None, **kwargs)
Create SwitchingGaussianMarkovChain node.
```

Methods

Table 5.42 - continued from previous page

```
has plotter()
                                             Return True if the node has a plotter
initialize_from_parameters(*args)
initialize_from_prior()
initialize_from_random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
load(group)
                                             Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                             Compute the probability density function of this node.
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
                                             Draw a random sample from the distribution.
random()
rotate(R[, inv, logdet])
                                             Save the state of the node into a HDF5 file.
save(group)
set_plotter(plotter)
show()
unobserve()
update()
```

bayespy.nodes.SwitchingGaussianMarkovChain.__init__

```
SwitchingGaussianMarkovChain.__init__ (mu, Lambda, B, Z, nu, n=None, **kwargs) Create SwitchingGaussianMarkovChain node.
```

bayespy.nodes.SwitchingGaussianMarkovChain.add_plate_axis

SwitchingGaussianMarkovChain.add_plate_axis(to_plate)

bayespy.nodes.SwitchingGaussianMarkovChain.delete

```
SwitchingGaussianMarkovChain.delete()

Delete this node and the children
```

$bayes py. nodes. Switching Gaussian Markov Chain. get_mask$

SwitchingGaussianMarkovChain.get_mask()

bayespy.nodes.SwitchingGaussianMarkovChain.get_moments

SwitchingGaussianMarkovChain.get_moments()

bayespy.nodes.SwitchingGaussianMarkovChain.get_shape

SwitchingGaussianMarkovChain.get_shape(ind)

```
bayespy.nodes.SwitchingGaussianMarkovChain.has plotter
SwitchingGaussianMarkovChain.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.SwitchingGaussianMarkovChain.initialize_from_parameters
SwitchingGaussianMarkovChain.initialize_from_parameters(*args)
bayespy.nodes.SwitchingGaussianMarkovChain.initialize_from_prior
SwitchingGaussianMarkovChain.initialize_from_prior()
bayespy.nodes.SwitchingGaussianMarkovChain.initialize from random
SwitchingGaussianMarkovChain.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.SwitchingGaussianMarkovChain.initialize from value
SwitchingGaussianMarkovChain.initialize_from_value(x, *args)
bayespy.nodes.SwitchingGaussianMarkovChain.load
SwitchingGaussianMarkovChain.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.SwitchingGaussianMarkovChain.logpdf
SwitchingGaussianMarkovChain.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.SwitchingGaussianMarkovChain.lower_bound_contribution
SwitchingGaussianMarkovChain.lower_bound_contribution(gradient=False)
bayespy.nodes.SwitchingGaussianMarkovChain.lowerbound
SwitchingGaussianMarkovChain.lowerbound()
bayespy.nodes.SwitchingGaussianMarkovChain.move_plates
SwitchingGaussianMarkovChain.move_plates(from_plate, to_plate)
```

bayespy.nodes.SwitchingGaussianMarkovChain.observe

```
SwitchingGaussianMarkovChain.observe(x, *args, mask=True) Fix moments, compute f and propagate mask.
```

bayespy.nodes.SwitchingGaussianMarkovChain.pdf

```
SwitchingGaussianMarkovChain.pdf (X, mask=True)
Compute the probability density function of this node.
```

bayespy.nodes.SwitchingGaussianMarkovChain.plot

```
SwitchingGaussianMarkovChain.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.SwitchingGaussianMarkovChain.random

```
SwitchingGaussianMarkovChain.random()
```

Draw a random sample from the distribution.

bayes py. nodes. Switching Gaussian Markov Chain. rotate

```
SwitchingGaussianMarkovChain.rotate(R, inv=None, logdet=None)
```

bayes py. nodes. Switching Gaussian Markov Chain. save

```
SwitchingGaussianMarkovChain.save (group)
Save the state of the node into a HDF5 file.
group can be the root
```

bayespy.nodes.SwitchingGaussianMarkovChain.set plotter

```
SwitchingGaussianMarkovChain.set_plotter(plotter)
```

bayespy.nodes.SwitchingGaussianMarkovChain.show

SwitchingGaussianMarkovChain.show()

bayespy.nodes.SwitchingGaussianMarkovChain.unobserve

SwitchingGaussianMarkovChain.unobserve()

bayespy.nodes.SwitchingGaussianMarkovChain.update

SwitchingGaussianMarkovChain.update()

Attributes

dims plates

bayespy.nodes.SwitchingGaussianMarkovChain.dims

SwitchingGaussianMarkovChain.dims = None

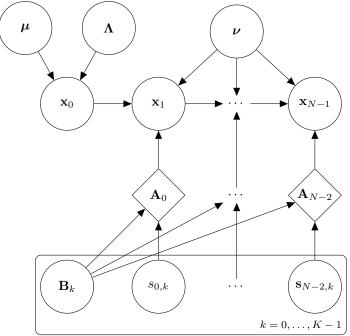
bayespy.nodes.SwitchingGaussianMarkovChain.plates

SwitchingGaussianMarkovChain.plates = None

bayespy.nodes.VaryingGaussianMarkovChain

class bayespy.nodes.**VaryingGaussianMarkovChain** (*mu*, *Lambda*, *B*, *S*, *nu*, *n=None*, **kwargs) Node for Gaussian Markov chain random variables with time-varying dynamics.

The node models a sequence of Gaussian variables $\mathbf{x}_0, \dots, \mathbf{x}_{N-1}$ with linear Markovian dynamics. The time variability of the dynamics is obtained by modelling the state dynamics matrix as a linear combination of a set of matrices with time-varying linear combination weights. The graphical model can be presented as:



where μ and Λ are the mean and the precision matrix of the initial state, ν is the precision of the innovation noise, and A_n are the state dynamics matrix obtained by mixing matrices B_k with weights $s_{n,k}$.

The probability distribution is

$$p(\mathbf{x}_0, \dots, \mathbf{x}_{N-1}) = p(\mathbf{x}_0) \prod_{n=1}^{N-1} p(\mathbf{x}_n | \mathbf{x}_{n-1})$$

where

$$p(\mathbf{x}_0) = \mathcal{N}(\mathbf{x}_0 | \boldsymbol{\mu}, \boldsymbol{\Lambda})$$

$$p(\mathbf{x}_n | \mathbf{x}_{n-1}) = \mathcal{N}(\mathbf{x}_n | \mathbf{A}_{n-1} \mathbf{x}_{n-1}, \operatorname{diag}(\boldsymbol{\nu})), \quad \text{for } n = 1, \dots, N-1,$$

$$\mathbf{A}_n = \sum_{k=0}^{K-1} s_{n,k} \mathbf{B}_k, \quad \text{for } n = 0, \dots, N-2.$$

Parameters mu: Gaussian-like node or (...,D)-array

 μ , mean of x_0 , D-dimensional with plates (...)

Lambda: Wishart-like node or (...,D,D)-array

 Λ , precision matrix of x_0 , $D \times D$ -dimensional with plates (...)

B: Gaussian-like node or (...,D,D,K)-array

 $\{\mathbf{B}_k\}_{k=0}^{K-1},$ a set of state dynamics matrix, $D\times K$ -dimensional with plates (...,D)

S: Gaussian-like node or (...,N-1,K)-array

 $\{s_0, \dots, s_{N-2}\}$, time-varying weights of the linear combination, K-dimensional with plates (...,N-1)

nu: gamma-like node or (...,D)-array

 ν , diagonal elements of the precision of the innovation process, plates (...,D)

n: int, optional

N, the length of the chain. Must be given if **S** does not have plates over the time domain (which would not make sense).

See also:

Gaussian, GaussianARD, Wishart, Gamma, GaussianMarkovChain, SwitchingGaussianMarkovChain

Notes

Equivalent model block can be constructed with GaussianMarkovChain by explicitly using SumMultiply to compute the linear combination. However, that approach is not very efficient for large datasets because it does not utilize the structure of A_n , thus it explicitly computes huge moment arrays.

References

[3]

__init__ (mu, Lambda, B, S, nu, n=None, **kwargs)
Create VaryingGaussianMarkovChain node.

Methods

```
_init__(mu, Lambda, B, S, nu[, n])
                                             Create VaryingGaussianMarkovChain node.
add_plate_axis(to_plate)
                                             Delete this node and the children
delete()
get_mask()
get_moments()
get_shape(ind)
                                             Return True if the node has a plotter
has_plotter()
initialize_from_parameters(*args)
initialize from prior()
initialize from random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
load(group)
                                             Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                             Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                             Compute the probability density function of this node.
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
random()
                                             Draw a random sample from the distribution.
rotate(R[, inv, logdet])
save(group)
                                             Save the state of the node into a HDF5 file.
set_plotter(plotter)
show()
unobserve()
update()
```

bayespy.nodes.VaryingGaussianMarkovChain.__init__

```
VaryingGaussianMarkovChain.__init__ (mu, Lambda, B, S, nu, n=None, **kwargs)
Create VaryingGaussianMarkovChain node.
```

bayespy.nodes.VaryingGaussianMarkovChain.add_plate_axis

 ${\tt Varying Gaussian Markov Chain.add_plate_axis} \ ({\it to_plate})$

bayespy.nodes.VaryingGaussianMarkovChain.delete

```
VaryingGaussianMarkovChain.delete()
Delete this node and the children
```

bayespy.nodes.VaryingGaussianMarkovChain.get mask

VaryingGaussianMarkovChain.get_mask()

bayespy.nodes.VaryingGaussianMarkovChain.get moments

VaryingGaussianMarkovChain.get_moments()

```
bayespy.nodes.VaryingGaussianMarkovChain.get shape
VaryingGaussianMarkovChain.get_shape(ind)
bayespy.nodes.VaryingGaussianMarkovChain.has_plotter
VaryingGaussianMarkovChain.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.VaryingGaussianMarkovChain.initialize from parameters
VaryingGaussianMarkovChain.initialize_from_parameters(*args)
bayespy.nodes.VaryingGaussianMarkovChain.initialize from prior
VaryingGaussianMarkovChain.initialize_from_prior()
bayespy.nodes.VaryingGaussianMarkovChain.initialize from random
VaryingGaussianMarkovChain.initialize from random()
    Set the variable to a random sample from the current distribution.
bayespy.nodes.VaryingGaussianMarkovChain.initialize_from_value
VaryingGaussianMarkovChain.initialize from value(x, *args)
bayespy.nodes.VaryingGaussianMarkovChain.load
VaryingGaussianMarkovChain.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.VaryingGaussianMarkovChain.logpdf
VaryingGaussianMarkovChain.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.VaryingGaussianMarkovChain.lower bound contribution
VaryingGaussianMarkovChain.lower_bound_contribution(gradient=False)
bayespy.nodes.VaryingGaussianMarkovChain.lowerbound
VaryingGaussianMarkovChain.lowerbound()
```

bayespy.nodes.VaryingGaussianMarkovChain.move_plates

VaryingGaussianMarkovChain.move_plates(from_plate, to_plate)

bayespy.nodes.VaryingGaussianMarkovChain.observe

VaryingGaussianMarkovChain.observe (x, *args, mask=True) Fix moments, compute f and propagate mask.

bayespy.nodes.VaryingGaussianMarkovChain.pdf

VaryingGaussianMarkovChain.**pdf** (*X*, *mask=True*) Compute the probability density function of this node.

bayespy.nodes.VaryingGaussianMarkovChain.plot

 ${\tt VaryingGaussianMarkovChain.plot}~(**kwargs)$

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.VaryingGaussianMarkovChain.random

VaryingGaussianMarkovChain.random()

Draw a random sample from the distribution.

bayespy.nodes.VaryingGaussianMarkovChain.rotate

VaryingGaussianMarkovChain.rotate(R, inv=None, logdet=None)

bayespy.nodes.VaryingGaussianMarkovChain.save

VaryingGaussianMarkovChain.save (group)
Save the state of the node into a HDF5 file.
group can be the root

bayespy.nodes.VaryingGaussianMarkovChain.set plotter

VaryingGaussianMarkovChain.set_plotter(plotter)

bayespy.nodes.VaryingGaussianMarkovChain.show

VaryingGaussianMarkovChain.show()

bayespy.nodes.VaryingGaussianMarkovChain.unobserve

VaryingGaussianMarkovChain.unobserve()

bayes py. nodes. Varying Gaussian Markov Chain. update

VaryingGaussianMarkovChain.update()

Attributes

dims plates

bayespy.nodes.VaryingGaussianMarkovChain.dims

VaryingGaussianMarkovChain.dims = None

bayespy.nodes.VaryingGaussianMarkovChain.plates

VaryingGaussianMarkovChain.plates = None

Other stochastic nodes:

Mixture(z, node_class, *params[, cluster_plate]) Node for exponential family mixture variables.

bayespy.nodes.Mixture

class bayespy.nodes.Mixture(z, node_class, *params, cluster_plate=-1, **kwargs)
 Node for exponential family mixture variables.

The node represents a random variable which is sampled from a mixture distribution. It is possible to mix any exponential family distribution. The probability density function is

$$p(x|z=k,\boldsymbol{\theta}_0,\ldots,\boldsymbol{\theta}_{K-1})=\phi(x|\boldsymbol{\theta}_k),$$

where ϕ is the probability density function of the mixed exponential family distribution and $\theta_0, \dots, \theta_{K-1}$ are the parameters of each cluster. For instance, ϕ could be the Gaussian probability density function $\mathcal N$ and $\theta_k = \{\mu_k, \Lambda_k\}$ where μ_k and Λ_k are the mean vector and precision matrix for cluster k.

Parameters z : categorical-like node or array

z, cluster assignment

node_class: stochastic exponential family node class

Mixed distribution

params: types specified by the mixed distribution

Parameters of the mixed distribution. If some parameters should vary between clusters, those parameters' plate axis *cluster_plate* should have a size which equals the number of clusters. For parameters with shared values, that plate axis should have length 1. At least one parameter should vary between clusters.

cluster_plate: int, optional

Negative integer defining which plate axis is used for the clusters in the parameters. That plate axis is ignored from the parameters when considering the plates for this node. By default, mix over the last plate axis.

See also:

Categorical, CategoricalMarkovChain

Examples

A simple 2-dimensional Gaussian mixture model with three clusters for 100 samples can be constructed, for instance, as:

Methods

save(group)

unobserve()
update()

set_plotter(plotter)

```
_init__(z, node_class, *params[, cluster_plate])
add_plate_axis(to_plate)
delete()
                                                   Delete this node and the children
get_mask()
get_moments()
get_shape(ind)
                                                   Return True if the node has a plotter
has plotter()
initialize_from_parameters(*args)
initialize_from_prior()
initialize_from_random()
                                                   Set the variable to a random sample from the current distribution.
initialize from value(x, *args)
                                                   Approximates the posterior predictive pdf int p(x|parents) q(parents) dparent
integrated logpdf from parents(x, index)
load(group)
                                                   Load the state of the node from a HDF5 file.
logpdf(X[, mask])
                                                   Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                                   Fix moments, compute f and propagate mask.
                                                   Compute the probability density function of this node.
pdf(X[, mask])
plot(**kwargs)
                                                   Plot the node distribution using the plotter of the node
random()
                                                   Draw a random sample from the distribution.
```

Save the state of the node into a HDF5 file.

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```
bayespy.nodes.Mixture. init
Mixture.__init__(z, node_class, *params, cluster_plate=-1, **kwargs)
bayespy.nodes.Mixture.add_plate_axis
Mixture.add_plate_axis(to_plate)
bayespy.nodes.Mixture.delete
Mixture.delete()
    Delete this node and the children
bayespy.nodes.Mixture.get_mask
Mixture.get_mask()
bayespy.nodes.Mixture.get_moments
Mixture.get_moments()
bayespy.nodes.Mixture.get_shape
Mixture.get_shape(ind)
bayespy.nodes.Mixture.has plotter
Mixture.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.Mixture.initialize from parameters
Mixture.initialize_from_parameters(*args)
bayespy.nodes.Mixture.initialize_from_prior
Mixture.initialize_from_prior()
bayespy.nodes.Mixture.initialize_from_random
Mixture.initialize_from_random()
    Set the variable to a random sample from the current distribution.
```

```
bayespy.nodes.Mixture.initialize from value
Mixture.initialize_from_value(x, *args)
bayespy.nodes.Mixture.integrated_logpdf_from_parents
Mixture.integrated_logpdf_from_parents(x, index)
    Approximates the posterior predictive pdf int p(x|parents) q(parents) dparents in log-scale as int
    q(parents_i) exp( int q(parents_i) log p(xlparents) dparents_i ) dparents_i.
bayespy.nodes.Mixture.load
Mixture.load(group)
    Load the state of the node from a HDF5 file.
bayespy.nodes.Mixture.logpdf
Mixture.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
bayespy.nodes.Mixture.lower bound contribution
Mixture.lower_bound_contribution(gradient=False)
bayespy.nodes.Mixture.lowerbound
Mixture.lowerbound()
bayespy.nodes.Mixture.move_plates
Mixture.move_plates (from_plate, to_plate)
bayespy.nodes.Mixture.observe
Mixture.observe(x, *args, mask=True)
    Fix moments, compute f and propagate mask.
bayespy.nodes.Mixture.pdf
Mixture.pdf (X, mask=True)
    Compute the probability density function of this node.
```

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bayespy.nodes.Mixture.plot

```
Mixture.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.nodes.Mixture.random

```
Mixture.random()
```

Draw a random sample from the distribution.

bayespy.nodes.Mixture.save

```
Mixture.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.nodes.Mixture.set_plotter

```
Mixture.set_plotter(plotter)
```

bayespy.nodes.Mixture.unobserve

```
Mixture.unobserve()
```

bayespy.nodes.Mixture.update

```
Mixture.update()
```

Attributes

dims plates

bayespy.nodes.Mixture.dims

```
Mixture.dims = None
```

bayespy.nodes.Mixture.plates

Mixture.plates = None

5.1. bayespy.nodes

5.1.2 Deterministic nodes

Dot(*args, **kwargs)	Node for computing inner product of several Gaussian vectors.
<pre>SumMultiply(*args[, iterator_axis])</pre>	Node for computing general products and sums of Gaussian nodes.
<pre>Gate(Z, X[, gated_plate, moments])</pre>	Deterministic gating of one node.

bayespy.nodes.Dot

```
bayespy.nodes.Dot(*args, **kwargs)
```

Node for computing inner product of several Gaussian vectors.

This is a simple wrapper of the much more general SumMultiply. For now, it is here for backward compatibility.

bayespy.nodes.SumMultiply

```
class bayespy.nodes.SumMultiply(*args, iterator_axis=None, **kwargs)
```

Node for computing general products and sums of Gaussian nodes.

The node is similar to *numpy.einsum*, which is a very general function for computing dot products, sums, products and other sums of products of arrays.

For instance, the equivalent of

```
np.einsum('abc,bd,ca->da', X, Y, Z)
would be given as
SumMultiply('abc,bd,ca->da', X, Y, Z)
or
SumMultiply(X, [0,1,2], Y, [1,3], Z, [2,0], [3,0])
```

which is similar to the other syntax of numpy.einsum.

This node operates similarly as numpy.einsum. However, you must use all the elements of each node, that is, an operation like np.einsum('ii->i',X) is not allowed. Thus, for each node, each axis must be given unique id. The id identifies which axes correspond to which axes between the different nodes. Also, Ellipsis ('...') is not yet supported for simplicity. It would also have some problems with constant inputs (because how to determine ndim), so let us just forget it for now.

Each output axis must appear in the input mappings.

The keys must refer to variable dimension axes only, not plate axes.

The input nodes may be Gaussian-gamma (isotropic) nodes.

The output message is Gaussian-gamma (isotropic) if any of the input nodes is Gaussian-gamma.

Notes

This operation can be extremely slow if not used wisely. For large and complex operations, it is sometimes more efficient to split the operation into multiple nodes. For instance, the example above could probably be computed faster by

```
XZ = SumMultiply(X, [0,1,2], Z, [2,0], [0,1])

F = SumMultiply(XZ, [0,1], Y, [1,2], [2,0])
```

because the third axis ('c') could be summed out already in the first operation. This same effect applies also to numpy.einsum in general.

Examples

```
Sum over the rows: 'ij->j'

Inner product of three vectors: 'i,i,i'

Matrix-vector product: 'ij,j->i'

Matrix-matrix product: 'ik,kj->ij'

Outer product: 'i,j->ij'

Vector-matrix-vector product: 'i,ij,j'

__init___(Node1, map1, Node2, map2, ..., NodeN, mapN[, map_out])
```

Methods

bayespy.nodes.SumMultiply. init

```
SumMultiply.__init__(Node1, map1, Node2, map2, ..., NodeN, mapN[, map_out])
```

bayespy.nodes.SumMultiply.add_plate_axis

```
SumMultiply.add_plate_axis(to_plate)
```

bayespy.nodes.SumMultiply.delete

```
SumMultiply.delete()

Delete this node and the children
```

$bayespy.nodes. Sum Multiply.get_mask$

```
SumMultiply.get_mask()
```

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```
bayespy.nodes.SumMultiply.get_moments
SumMultiply.get_moments()
bayespy.nodes.SumMultiply.get_parameters
SumMultiply.get_parameters()
bayespy.nodes.SumMultiply.get_shape
SumMultiply.get_shape(ind)
bayespy.nodes.SumMultiply.has_plotter
SumMultiply.has_plotter()
    Return True if the node has a plotter
bayespy.nodes.SumMultiply.lower bound contribution
SumMultiply.lower_bound_contribution(gradient=False)
bayespy.nodes.SumMultiply.move_plates
SumMultiply.move_plates (from_plate, to_plate)
bayespy.nodes.SumMultiply.plot
SumMultiply.plot(**kwargs)
    Plot the node distribution using the plotter of the node
    Because the distributions are in general very difficult to plot, the user must specify some functions which
    performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is,
    functions that perform plotting for a node.
bayespy.nodes.SumMultiply.set_plotter
SumMultiply.set_plotter(plotter)
Attributes
                         plates
bayespy.nodes.SumMultiply.plates
SumMultiply.plates = None
```

bayespy.nodes.Gate

```
class bayespy.nodes.Gate(Z, X, gated_plate=-1, moments=None, **kwargs)
    Deterministic gating of one node.
```

Gating is performed over one plate axis.

Note: You should not use gating for several variables which parents of a same node if the gates use the same gate assignments. In such case, the results will be wrong. The reason is a general one: A stochastic node may not be a parent of another node via several paths unless at most one path has no other stochastic nodes between them.

```
___init__ (Z, X, gated_plate=-1, moments=None, **kwargs)
```

Methods

bayespy.nodes.Gate.__init__

```
Gate.__init__(Z, X, gated_plate=-1, moments=None, **kwargs)
```

bayespy.nodes.Gate.add_plate_axis

```
Gate.add_plate_axis(to_plate)
```

bayespy.nodes.Gate.delete

```
Gate.delete()
```

Delete this node and the children

$bayespy.nodes. Gate.get_mask$

```
Gate.get_mask()
```

$bayespy.nodes. Gate.get_moments$

```
Gate.get_moments()
```

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```
bayespy.nodes.Gate.get shape
Gate.get_shape(ind)
bayespy.nodes.Gate.has_plotter
Gate.has_plotter()
     Return True if the node has a plotter
bayespy.nodes.Gate.lower_bound_contribution
{\tt Gate.lower\_bound\_contribution}~(\textit{gradient=False})
bayespy.nodes.Gate.move_plates
Gate.move_plates (from_plate, to_plate)
bayespy.nodes.Gate.plot
Gate.plot(**kwargs)
     Plot the node distribution using the plotter of the node
     Because the distributions are in general very difficult to plot, the user must specify some functions which
     performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is,
     functions that perform plotting for a node.
bayespy.nodes.Gate.set plotter
Gate.set_plotter(plotter)
Attributes
                          plates
bayespy.nodes.Gate.plates
Gate.plates = None
```

5.2 bayespy.inference

Package for Bayesian inference engines

5.2.1 Inference engines

VB(*nodes[, tol, autosave_filename, ...]) Variational Bayesian (VB) inference engine

bayespy.inference.VB

Methods

```
_init___(*nodes[, tol, autosave_filename, ...])
compute_lowerbound()
compute_lowerbound_terms(*nodes)
get iteration by nodes()
load(*nodes[, filename])
loglikelihood lowerbound()
                                             Plot the distribution of the given nodes (or all nodes)
plot(*nodes)
plot_iteration_by_nodes()
                                             Plot the cost function per node during the iteration.
save([filename])
set autosave(filename[, iterations])
update(*nodes[, repeat, plot, tol, verbose])
bayespy.inference.VB. init
VB.__init__ (*nodes, tol=1e-05, autosave_filename=None, autosave_iterations=0, callback=None)
bayespy.inference.VB.compute lowerbound
VB.compute lowerbound()
```

```
bayespy.inference.VB.compute lowerbound terms
VB.compute_lowerbound_terms(*nodes)
bayespy.inference.VB.get_iteration_by_nodes
VB.get_iteration_by_nodes()
bayespy.inference.VB.load
VB.load(*nodes, filename=None)
bayespy.inference.VB.loglikelihood lowerbound
VB.loglikelihood_lowerbound()
bayespy.inference.VB.plot
VB.plot(*nodes)
    Plot the distribution of the given nodes (or all nodes)
bayespy.inference.VB.plot_iteration_by_nodes
VB.plot_iteration_by_nodes()
    Plot the cost function per node during the iteration.
    Handy tool for debugging.
bayespy.inference.VB.save
VB.save(filename=None)
bayespy.inference.VB.set_autosave
VB.set_autosave(filename, iterations=None)
bayespy.inference.VB.update
VB.update(*nodes, repeat=1, plot=False, tol=None, verbose=True)
```

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5.2.2 Parameter expansions

```
vmp.transformations.RotationOptimizer(...)Optimizer for rotation parameter expansion in state-spansion in state-spansion for bayespy.nodes.vmp.transformations.RotateGaussianARD(X, *alpha)Rotation parameter expansion for bayespy.nodes.vmp.transformations.RotateGaussianMarkovChain(X, ...)Rotation parameter expansion for bayespy.nodes.vmp.transformations.RotateSwitchingMarkovChain(X, ...)Rotation parameter expansion for bayespy.nodes.vmp.transformations.RotateVaryingMarkovChain(X, ...)Rotation for bayespy.nodes.SwitchingGaussianvmp.transformations.RotateMultiple(*rotators)Rotation for bayespy.nodes.SwitchingGaussian
```

```
class bayespy.inference.vmp.transformations.RotationOptimizer (block1, block2, D)
   Optimizer for rotation parameter expansion in state-space models
   Rotates one model block with R and one model block with R<sup>-1</sup>.

   Parameters block1: rotator object
        The first rotation parameter expansion object
        block2: rotator object
        The second rotation parameter expansion object
        D: int
        Dimensionality of the latent space
References
```

```
[2], [1]
__init___(block1, block2, D)
```

Methods

```
__init__(block1, block2, D)
rotate([maxiter, check_gradient, verbose, ...]) Optimize the rotation of two separate model blocks jointly.
```

bayespy.inference.vmp.transformations.RotationOptimizer.__init__

```
{\tt RotationOptimizer.\_\_init}\_\_(block1, block2, D)
```

bayespy.inference.vmp.transformations.RotationOptimizer.rotate

```
RotationOptimizer.rotate(maxiter=10, check_gradient=False, verbose=False, check_bound=False)

Optimize the rotation of two separate model blocks jointly.
```

If some variable is the dot product of two Gaussians, rotating the two Gaussians optimally can make the inference algorithm orders of magnitude faster.

First block is rotated with \mathbf{R} and the second with \mathbf{R}^{-T} .

Blocks must have methods: bound(U,s,V) and rotate(R).

bayespy.inference.vmp.transformations.RotateGaussian

```
class bayespy.inference.vmp.transformations.RotateGaussian (X)
    Rotation parameter expansion for bayespy.nodes.Gaussian
    __init__(X)
```

Methods

bayespy.inference.vmp.transformations.RotateGaussian. init

```
RotateGaussian.__init__(X)
```

bayes py. in ference. vmp. transformations. Rotate Gaussian. bound

RotateGaussian.bound(R, logdet=None, inv=None)

bayespy.inference.vmp.transformations.RotateGaussian.get_bound_terms

RotateGaussian.get_bound_terms(R, logdet=None, inv=None)

bayespy.inference.vmp.transformations.RotateGaussian.nodes

```
RotateGaussian.nodes()
```

bayespy.inference.vmp.transformations.RotateGaussian.rotate

RotateGaussian.rotate(R, inv=None, logdet=None)

bayespy.inference.vmp.transformations.RotateGaussian.setup

```
RotateGaussian.setup()
```

This method should be called just before optimization.

bayespy.inference.vmp.transformations.RotateGaussianARD

class bayespy.inference.vmp.transformations.RotateGaussianARD (X, *alpha, axis=-1, precompute=False)

Rotation parameter expansion for bayespy.nodes.GaussianARD

The model:
 alpha ~ N(a, b) X ~ N(mu, alpha)

X can be an array (e.g., GaussianARD).

Transform q(X) and q(alpha) by rotating X.

Requirements: * X and alpha do not contain any observed values
 __init__ (X, *alpha, axis=-1, precompute=False)

Precompute tells whether to compute some moments once in the setup function instead of every time in the bound function. However, they are computed a bit differently in the bound function so it can be useful

Methods

```
\begin{tabular}{ll} $\_\_init\_(X, *alpha[, axis, precompute])$ & Precompute tells whether to compute some moments once in the setup function instead bound(R[, logdet, inv, Q]) \\ $\gcd\_bound\_terms(R[, logdet, inv, Q])$ \\ $nodes()$ \\ $rotate(R[, inv, logdet, Q])$ \\ $setup([plate\_axis])$ & This method should be called just before optimization. \\ \end{tabular}
```

too. Precomputation is probably beneficial only when there are large axes that are not rotated (by R nor Q)

and they are not contained in the plates of alpha, and the dimensions for R and Q are quite small.

bayespy.inference.vmp.transformations.RotateGaussianARD.__init__

```
RotateGaussianARD.__init__(X, *alpha, axis=-1, precompute=False)
```

Precompute tells whether to compute some moments once in the setup function instead of every time in the bound function. However, they are computed a bit differently in the bound function so it can be useful too. Precomputation is probably beneficial only when there are large axes that are not rotated (by R nor Q) and they are not contained in the plates of alpha, and the dimensions for R and Q are quite small.

bayespy.inference.vmp.transformations.RotateGaussianARD.bound

RotateGaussianARD.**bound**(*R*, *logdet=None*, *inv=None*, *Q=None*)

bayespy.inference.vmp.transformations.RotateGaussianARD.get bound terms

RotateGaussianARD.get_bound_terms (R, logdet=None, inv=None, Q=None)

bayespy.inference.vmp.transformations.RotateGaussianARD.nodes

RotateGaussianARD.nodes()

bayespy.inference.vmp.transformations.RotateGaussianARD.rotate

```
RotateGaussianARD.rotate(R, inv=None, logdet=None, Q=None)
```

bayespy.inference.vmp.transformations.RotateGaussianARD.setup

```
RotateGaussianARD.setup(plate_axis=None)
```

This method should be called just before optimization.

For efficiency, sum over axes that are not in mu, alpha nor rotation.

If using Q, set rotate_plates to True.

bayespy.inference.vmp.transformations.RotateGaussianMarkovChain

```
{f class} bayespy.inference.vmp.transformations.{f RotateGaussianMarkovChain} ({f X},
```

*args)

 $\textbf{Rotation parameter expansion for } \verb|bayespy.nodes.Gaussian| \verb|MarkovChain| \\$

Assume the following model.

Constant, unit isotropic innovation noise. Unit variance only?

Maybe: Assume innovation noise with unit variance? Would it help make this function more general with respect to A.

TODO: Allow constant A or not rotating A.

A may vary in time.

Shape of A: (N,D,D) Shape of AA: (N,D,D,D)

No plates for X.

```
___init___(X, *args)
```

Methods

```
__init__(X, *args)
bound(R[, logdet, inv])
get_bound_terms(R[, logdet, inv])
nodes()
rotate(R[, inv, logdet])
setup()
This method should be called just before optimization.
```

bayespy.inference.vmp.transformations.RotateGaussianMarkovChain.__init__

```
RotateGaussianMarkovChain.__init__(X, *args)
```

bayespy.inference.vmp.transformations.RotateGaussianMarkovChain.bound

RotateGaussianMarkovChain.bound(R, logdet=None, inv=None)

bayespy.inference.vmp.transformations.RotateGaussianMarkovChain.get bound terms

RotateGaussianMarkovChain.get_bound_terms(R, logdet=None, inv=None)

bayespy.inference.vmp.transformations.RotateGaussianMarkovChain.nodes

RotateGaussianMarkovChain.nodes()

bayespy.inference.vmp.transformations.RotateGaussianMarkovChain.rotate

RotateGaussianMarkovChain.rotate(R, inv=None, logdet=None)

bayespy.inference.vmp.transformations.RotateGaussianMarkovChain.setup

RotateGaussianMarkovChain.setup()

This method should be called just before optimization.

bayespy.inference.vmp.transformations.RotateSwitchingMarkovChain

 $B_rotator)$

Rotation for bayespy.nodes.VaryingGaussianMarkovChain

Assume the following model.

Constant, unit isotropic innovation noise.

$$A_n = B_{z_n}$$

Gaussian B: (..., K, D) x (D) Categorical Z: (..., N-1) x (K) GaussianMarkovChain X: (...) x (N,D)

No plates for X.

___init__ (*X*, *B*, *Z*, *B_rotator*)

Methods

```
__init__(X, B, Z, B_rotator)
bound(R[, logdet, inv])
get_bound_terms(R[, logdet, inv])
nodes()
rotate(R[, inv, logdet])
setup()
This method should be called just before optimization.
```

bayespy.inference.vmp.transformations.RotateSwitchingMarkovChain.__init__

RotateSwitchingMarkovChain. $_$ init $_$ ($X, B, Z, B_$ rotator)

bayespy.inference.vmp.transformations.RotateSwitchingMarkovChain.bound

RotateSwitchingMarkovChain.bound(R, logdet=None, inv=None)

bayespy.inference.vmp.transformations.RotateSwitchingMarkovChain.get bound terms

RotateSwitchingMarkovChain.get_bound_terms (R, logdet=None, inv=None)

bayespy.inference.vmp.transformations.RotateSwitchingMarkovChain.nodes

RotateSwitchingMarkovChain.nodes()

bayespy.inference.vmp.transformations.RotateSwitchingMarkovChain.rotate

RotateSwitchingMarkovChain.rotate(R, inv=None, logdet=None)

bayespy.inference.vmp.transformations.RotateSwitchingMarkovChain.setup

RotateSwitchingMarkovChain.setup()

This method should be called just before optimization.

bayespy.inference.vmp.transformations.RotateVaryingMarkovChain

class bayespy.inference.vmp.transformations.RotateVaryingMarkovChain(X, B, S, B rotator)

Rotation for bayespy.nodes.SwitchingGaussianMarkovChain

Assume the following model.

Constant, unit isotropic innovation noise.

$$A_n = \sum_k B_k s_{kn}$$

Gaussian B: (1,D) x (D,K) Gaussian S: (N,1) x (K) MC X: () x (N+1,D)

No plates for X.

Methods

```
__init__(X, B, S, B_rotator)
bound(R[, logdet, inv])
get_bound_terms(R[, logdet, inv])
nodes()
rotate(R[, inv, logdet])
setup()
This method should be called just before optimization.
```

```
bayespy.inference.vmp.transformations.RotateVaryingMarkovChain. init
     RotateVaryingMarkovChain.__init__(X, B, S, B_rotator)
     bayespy.inference.vmp.transformations.RotateVaryingMarkovChain.bound
     RotateVaryingMarkovChain.bound(R, logdet=None, inv=None)
     bayespy.inference.vmp.transformations.RotateVaryingMarkovChain.get_bound_terms
     RotateVaryingMarkovChain.get_bound_terms(R, logdet=None, inv=None)
     bayespy.inference.vmp.transformations.RotateVaryingMarkovChain.nodes
     RotateVaryingMarkovChain.nodes()
     bayespy.inference.vmp.transformations.RotateVaryingMarkovChain.rotate
     RotateVaryingMarkovChain.rotate(R, inv=None, logdet=None)
     bayespy.inference.vmp.transformations.RotateVaryingMarkovChain.setup
     RotateVaryingMarkovChain.setup()
         This method should be called just before optimization.
bayespy.inference.vmp.transformations.RotateMultiple
class bayespy.inference.vmp.transformations.RotateMultiple(*rotators)
     Identical parameter expansion for several nodes simultaneously
     Performs the same rotation for multiple nodes and combines the cost effect.
     ___init___(*rotators)
     Methods
                               _init__(*rotators)
                             bound(R[, logdet, inv])
                             get_bound_terms(R[, logdet, inv])
                             nodes()
                             rotate(R[, inv, logdet])
                             setup()
     bayespy.inference.vmp.transformations.RotateMultiple.__init__
     RotateMultiple. init (*rotators)
```

bayespy.inference.vmp.transformations.RotateMultiple.bound

RotateMultiple.bound(R, logdet=None, inv=None)

$bayes py. inference. vmp. transformations. Rotate Multiple.get_bound_terms$

RotateMultiple.get_bound_terms (R, logdet=None, inv=None)

bayespy.inference.vmp.transformations.RotateMultiple.nodes

```
RotateMultiple.nodes()
```

bayespy.inference.vmp.transformations.RotateMultiple.rotate

RotateMultiple.rotate(R, inv=None, logdet=None)

bayespy.inference.vmp.transformations.RotateMultiple.setup

RotateMultiple.setup()

5.3 bayespy.plot

Functions for plotting nodes.

5.3.1 Functions

pdf(Z, x, *args[, name])	Plot probability density function of a scalar variable.
contour(Z, x, y[, n])	Plot 2-D probability density function of a 2-D variable.
plot(Y[, axis, scale, center])	Plot a variable or an array as 1-D function with errorbars
hinton(X, **kwargs)	Plot the Hinton diagram of a node
$gaussian_mixture(X[, scale, fill])$	Plot Gaussian mixture as ellipses in 2-D

bayespy.plot.pdf

bayespy.plot.pdf (Z, x, *args, name=None, **kwargs)Plot probability density function of a scalar variable.

Parameters Z: node or function

Stochastic node or log pdf function

x: array

Grid points

bayespy.plot.contour

```
bayespy.plot.contour (Z, x, y, n=None, **kwargs) Plot 2-D probability density function of a 2-D variable.
```

Parameters **Z**: node or function

Stochastic node or log pdf function

x: array

Grid points on x axis

y: array

Grid points on y axis

bayespy.plot.plot

```
bayespy.plot.plot (Y, axis=-1, scale=2, center=False, **kwargs)
Plot a variable or an array as 1-D function with errorbars
```

bayespy.plot.hinton

```
bayespy.plot.hinton(X, **kwargs)

Plot the Hinton diagram of a node
```

The keyword arguments depend on the node type. For some node types, the diagram also shows uncertainty with non-filled rectangles. Currently, beta-like, Gaussian-like and Dirichlet-like nodes are supported.

Parameters X : node

bayespy.plot.gaussian mixture

```
bayespy.plot.gaussian_mixture (X, scale=1, fill=False, **kwargs)
Plot Gaussian mixture as ellipses in 2-D
```

5.3.2 Plotters

Plotter(plotter, *args, **kwargs)	Wrapper for plotting functions and base class for node plotters
PDFPlotter(x_grid, **kwargs)	Plotter of probability density function of a scalar node
ContourPlotter(x1_grid, x2_grid, **kwargs)	Plotter of probability density function of a two-dimensional node
HintonPlotter(**kwargs)	Plotter of the Hinton diagram of a node
FunctionPlotter(**kwargs)	Plotter of a node as a 1-dimensional function
<pre>GaussianTimeseriesPlotter(**kwargs)</pre>	Plotter of a Gaussian node as a timeseries
CategoricalMarkovChainPlotter(**kwargs)	Plotter of a Categorical timeseries

bayespy.plot.Plotter

```
class bayespy.plot.Plotter (plotter, *args, **kwargs)
Wrapper for plotting functions and base class for node plotters
```

The purpose of this class is to collect all the parameters needed by a plotting function and provide a callable interface which needs only the node as the input.

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Plotter instances are callable objects that plot a given node using a specified plotting function.

```
Parameters plotter: function
```

Plotting function to use

args: defined by the plotting function

Additional inputs needed by the plotting function

kwargs: defined by the plotting function

Additional keyword arguments supported by the plotting function

Examples

First, create a gamma variable:

```
>>> import numpy as np
>>> from bayespy.nodes import Gamma
>>> x = Gamma(4, 5)
```

The probability density function can be plotted as:

```
>>> import bayespy.plot as bpplt
>>> bpplt.pdf(x, np.linspace(0.1, 10, num=100))
[<matplotlib.lines.Line2D object at 0x...>]
```

However, this can be problematic when one needs to provide a plotting function for the inference engine as the inference engine gives only the node as input. Thus, we need to create a simple plotter wrapper:

```
>>> p = bpplt.Plotter(bpplt.pdf, np.linspace(0.1, 10, num=100))
```

Now, this callable object p needs only the node as the input:

```
>>> p(x)
[<matplotlib.lines.Line2D object at 0x...>]
```

Thus, it can be given to the inference engine to use as a plotting function:

```
>>> x = Gamma(4, 5, plotter=p)
>>> x.plot()
[<matplotlib.lines.Line2D object at 0x...>]
__init__(plotter, *args, **kwargs)
```

Methods

```
__init__(plotter, *args, **kwargs)
```

bayespy.plot.Plotter. init

```
Plotter.__init__(plotter, *args, **kwargs)
```

bayespy.plot.PDFPlotter

```
class bayespy.plot.PDFPlotter (x_grid, **kwargs)
     Plotter of probability density function of a scalar node
          Parameters x_grid: array
                  Numerical grid on which the density function is computed and plotted
     See also:
     pdf
     ___init___(x_grid, **kwargs)
     Methods
                                  _init___(x_grid, **kwargs)
     bayespy.plot.PDFPlotter.__init__
     PDFPlotter.__init__(x_grid, **kwargs)
bayespy.plot.ContourPlotter
class bayespy.plot.ContourPlotter(x1_grid, x2_grid, **kwargs)
     Plotter of probability density function of a two-dimensional node
          Parameters x1_grid : array
                  Grid for the first dimension
              x2_grid: array
                  Grid for the second dimension
     See also:
     contour
     ___init__ (x1_grid, x2_grid, **kwargs)
     Methods
                                          _(x1_grid, x2_grid, **kwargs)
                                  init_
     bayespy.plot.ContourPlotter.__init__
     ContourPlotter.__init__(x1_grid, x2_grid, **kwargs)
bayespy.plot.HintonPlotter
class bayespy.plot.HintonPlotter(**kwargs)
     Plotter of the Hinton diagram of a node
```

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```
See also:
     hinton
     __init__ (**kwargs)
     Methods
                               init
                                     _(**kwargs)
     bayespy.plot.HintonPlotter.__init__
     HintonPlotter.__init__(**kwargs)
bayespy.plot.FunctionPlotter
class bayespy.plot.FunctionPlotter(**kwargs)
     Plotter of a node as a 1-dimensional function
     See also:
     plot
     __init__(**kwargs)
     Methods
                                      (**kwargs)
                               init__
     bayespy.plot.FunctionPlotter.__init__
     FunctionPlotter.__init__(**kwargs)
bayespy.plot.GaussianTimeseriesPlotter
class bayespy.plot.GaussianTimeseriesPlotter(**kwargs)
     Plotter of a Gaussian node as a timeseries
     __init__(**kwargs)
     Methods
                                      (**kwargs)
                               init
     bayespy.plot.GaussianTimeseriesPlotter.__init__
     GaussianTimeseriesPlotter.__init__(**kwargs)
```

bayespy.plot.CategoricalMarkovChainPlotter

```
class bayespy.plot.CategoricalMarkovChainPlotter(**kwargs)
    Plotter of a Categorical timeseries
    __init__(**kwargs)

Methods

__init__(**kwargs)

bayespy.plot.CategoricalMarkovChainPlotter.__init__

CategoricalMarkovChainPlotter.__init__(**kwargs)
```

5.3. bayespy.plot

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CHAPTER

SIX

DEVELOPER API

This chapter contains API specifications which are relevant to BayesPy developers and contributors.

6.1 Developer nodes

get_moments()

The following base classes are useful if writing new nodes:

```
node.Node(*parents, **kwargs)
stochastic.Stochastic(*args[, initialize, dims])
expfamily.ExponentialFamily(*args, **kwargs)
deterministic.Deterministic(*args, **kwargs)

Base class for all nodes.

Base class for nodes that are stochastic.

A base class for nodes using natural parameterization phi.

Base class for deterministic nodes.
```

6.1.1 bayespy.inference.vmp.nodes.node.Node

```
class bayespy.inference.vmp.nodes.node.Node(*parents, **kwargs)
     Base class for all nodes.
     mask dims plates parents children name
     Sub-classes must implement: 1. For computing the message to children:
          get_moments(self):
        2.For computing the message to parents: _get_message_and_mask_to_parent(self, index)
     Sub-classes may need to re-implement: 1. If they manipulate plates:
          _compute_mask_to_parent(index, mask) _plates_to_parent(self, index) _plates_from_parent(self,
          index)
      ___init___(*parents, **kwargs)
     Methods
          __init__(*parents, **kwargs)
          add_plate_axis(to_plate)
                                               Delete this node and the children
          delete()
          get_mask()
```

Continued on next page

Table 6.2 – continued from previous page

```
get_shape(ind)
has_plotter()
move_plates(from_plate, to_plate)
plot(**kwargs)
set_plotter(plotter)

Return True if the node has a plotter

Plot the node distribution using the plotter of the node
```

bayespy.inference.vmp.nodes.node.Node.__init__

```
Node.__init__(*parents, **kwargs)
```

bayespy.inference.vmp.nodes.node.Node.add_plate_axis

```
Node.add_plate_axis(to_plate)
```

bayespy.inference.vmp.nodes.node.Node.delete

```
Node.delete()
```

Delete this node and the children

bayespy.inference.vmp.nodes.node.Node.get_mask

```
Node.get_mask()
```

bayespy.inference.vmp.nodes.node.Node.get moments

```
Node.get_moments()
```

bayespy.inference.vmp.nodes.node.Node.get shape

```
Node.get_shape(ind)
```

bayespy.inference.vmp.nodes.node.Node.has plotter

```
Node.has_plotter()
```

Return True if the node has a plotter

bayespy.inference.vmp.nodes.node.Node.move_plates

```
Node.move_plates (from_plate, to_plate)
```

bayespy.inference.vmp.nodes.node.Node.plot

```
Node.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.node.Node.set_plotter

```
Node.set_plotter(plotter)
```

Attributes

```
plates
```

bayespy.inference.vmp.nodes.node.Node.plates

```
Node.plates = None
```

6.1.2 bayespy.inference.vmp.nodes.stochastic.Stochastic

Base class for nodes that are stochastic.

u observed

Sub-classes must implement: _compute_message_to_parent(parent, index, u_self, *u_parents) _up-date_distribution_and_lowerbound(self, m, *u) lowerbound(self) _compute_dims initialize_from_prior()

If you want to be able to observe the variable: _compute_fixed_moments_and_f

Sub-classes may need to re-implement: 1. If they manipulate plates:

```
_compute_mask_to_parent(index, mask) _plates_to_parent(self, index) _plates_from_parent(self, index)
```

```
___init___(*args, initialize=True, dims=None, **kwargs)
```

Methods

```
_init___(*args[, initialize, dims])
add_plate_axis(to_plate)
delete()
                                      Delete this node and the children
get mask()
get_moments()
get shape(ind)
                                      Return True if the node has a plotter
has_plotter()
load(group)
                                      Load the state of the node from a HDF5 file.
lowerbound()
move_plates(from_plate, to_plate)
observe(x[, mask])
                                      Fix moments, compute f and propagate mask.
plot(**kwargs)
                                      Plot the node distribution using the plotter of the node
                                      Draw a random sample from the distribution.
random()
                                      Save the state of the node into a HDF5 file.
save(group)
set_plotter(plotter)
unobserve()
update()
```

```
bayespy.inference.vmp.nodes.stochastic. Stochastic. init
Stochastic.__init__(*args, initialize=True, dims=None, **kwargs)
bayespy.inference.vmp.nodes.stochastic.Stochastic.add plate axis
Stochastic.add_plate_axis(to_plate)
bayespy.inference.vmp.nodes.stochastic.Stochastic.delete
Stochastic.delete()
    Delete this node and the children
bayespy.inference.vmp.nodes.stochastic.Stochastic.get_mask
Stochastic.get_mask()
bayespy.inference.vmp.nodes.stochastic.Stochastic.get moments
Stochastic.get_moments()
bayespy.inference.vmp.nodes.stochastic.Stochastic.get shape
Stochastic.get_shape(ind)
bayespy.inference.vmp.nodes.stochastic.Stochastic.has_plotter
Stochastic.has_plotter()
    Return True if the node has a plotter
bayespy.inference.vmp.nodes.stochastic.Stochastic.load
Stochastic.load(group)
    Load the state of the node from a HDF5 file.
bayespy.inference.vmp.nodes.stochastic.Stochastic.lowerbound
Stochastic.lowerbound()
bayespy.inference.vmp.nodes.stochastic.Stochastic.move plates
Stochastic.move_plates (from_plate, to_plate)
bayespy.inference.vmp.nodes.stochastic.Stochastic.observe
Stochastic.observe(x, mask=True)
    Fix moments, compute f and propagate mask.
```

bayespy.inference.vmp.nodes.stochastic.Stochastic.plot

```
Stochastic.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.stochastic.Stochastic.random

```
Stochastic.random()
```

Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.stochastic.Stochastic.save

```
Stochastic.save(group)
```

Save the state of the node into a HDF5 file.

group can be the root

bayespy.inference.vmp.nodes.stochastic.Stochastic.set_plotter

```
Stochastic.set_plotter(plotter)
```

bayespy.inference.vmp.nodes.stochastic.Stochastic.unobserve

```
Stochastic.unobserve()
```

bayespy.inference.vmp.nodes.stochastic.Stochastic.update

```
Stochastic.update()
```

Attributes

plates

bayespy.inference.vmp.nodes.stochastic.Stochastic.plates

Stochastic.plates = None

6.1.3 bayespy.inference.vmp.nodes.expfamily.ExponentialFamily

```
class bayespy.inference.vmp.nodes.expfamily.ExponentialFamily(*args, **kwargs)
    A base class for nodes using natural parameterization phi.
```

phi

```
Sub-classes must implement the following static methods: _compute_message_to_parent(index, u_self, *u_parents) _compute_phi_from_parents(*u_parents, mask) _compute_moments_and_cgf(phi, mask) _compute_fixed_moments_and_f(x, mask=True)

Sub-classes may need to re-implement: 1. If they manipulate plates:
    _compute_mask_to_parent(index, mask) _plates_to_parent(self, index) _plates_from_parent(self, index)
    __init___(*args, **kwargs)
```

Methods

```
_init__(*args, **kwargs)
add plate axis(to plate)
delete()
                                            Delete this node and the children
get_mask()
get_moments()
get shape(ind)
has plotter()
                                            Return True if the node has a plotter
initialize_from_parameters(*args)
initialize_from_prior()
initialize_from_random()
                                             Set the variable to a random sample from the current distribution.
initialize_from_value(x, *args)
                                             Load the state of the node from a HDF5 file.
load(group)
logpdf(X[, mask])
                                             Compute the log probability density function Q(X) of this node.
lower_bound_contribution([gradient])
lowerbound()
move_plates(from_plate, to_plate)
observe(x, *args[, mask])
                                            Fix moments, compute f and propagate mask.
pdf(X[, mask])
                                             Compute the probability density function of this node.
plot(**kwargs)
                                             Plot the node distribution using the plotter of the node
random()
                                            Draw a random sample from the distribution.
save(group)
                                             Save the state of the node into a HDF5 file.
set_plotter(plotter)
unobserve()
update()
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily. init

```
ExponentialFamily.__init__(*args, **kwargs)
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.add_plate_axis

```
ExponentialFamily.add_plate_axis(to_plate)
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.delete

```
ExponentialFamily.delete()

Delete this node and the children
```

```
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.get mask
ExponentialFamily.get_mask()
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.get moments
ExponentialFamily.get_moments()
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.get shape
ExponentialFamily.get_shape (ind)
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.has_plotter
ExponentialFamily.has_plotter()
    Return True if the node has a plotter
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.initialize from parameters
ExponentialFamily.initialize_from_parameters(*args)
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.initialize from prior
ExponentialFamily.initialize_from_prior()
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.initialize from random
ExponentialFamily.initialize_from_random()
    Set the variable to a random sample from the current distribution.
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.initialize from value
ExponentialFamily.initialize_from_value(x, *args)
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.load
ExponentialFamily.load(group)
    Load the state of the node from a HDF5 file.
bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.logpdf
ExponentialFamily.logpdf(X, mask=True)
    Compute the log probability density function Q(X) of this node.
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.lower bound contribution

ExponentialFamily.lower_bound_contribution(gradient=False)

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.lowerbound

```
ExponentialFamily.lowerbound()
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.move plates

```
ExponentialFamily.move_plates (from_plate, to_plate)
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.observe

```
ExponentialFamily.observe(x, *args, mask=True) Fix moments, compute f and propagate mask.
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.pdf

```
ExponentialFamily.pdf (X, mask=True)

Compute the probability density function of this node.
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.plot

```
ExponentialFamily.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.random

```
ExponentialFamily.random()
```

Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.save

```
ExponentialFamily.save (group)
Save the state of the node into a HDF5 file.
group can be the root
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.set plotter

```
ExponentialFamily.set_plotter(plotter)
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.unobserve

```
ExponentialFamily.unobserve()
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.update

```
ExponentialFamily.update()
```

Attributes

```
dims
plates
```

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.dims

ExponentialFamily.dims = None

bayespy.inference.vmp.nodes.expfamily.ExponentialFamily.plates

ExponentialFamily.plates = None

6.1.4 bayespy.inference.vmp.nodes.deterministic.Deterministic

Sub-classes must implement: 1. For implementing the deterministic function:

```
_compute_moments(self, *u)
```

2.One of the following options: a) Simple methods:

```
_compute_message_to_parent(self, index, m, *u) not? _compute_mask_to_parent(self, index, mask)
```

```
(a)More control with: _compute_message_and_mask_to_parent(self, index, m, *u)
```

Sub-classes may need to re-implement: 1. If they manipulate plates:

```
\_compute\_mask\_to\_parent(index, \ mask) \ \_plates\_to\_parent(self, \ index) \ \_plates\_from\_parent(self, \ index)
```

```
___init___(*args, **kwargs)
```

Methods

```
__init__(*args, **kwargs)
add_plate_axis(to_plate)
delete()
get_mask()
get_moments()
get_shape(ind)
has_plotter()
lower_bound_contribution([gradient])

Delete this node and the children

Return True if the node has a plotter
```

Table 6.8 – continued from previous page

move_plates(from_plate, to_plate)
plot(**kwargs)
Plot the node distribution using the plotter of the node
set_plotter(plotter)

bayespy.inference.vmp.nodes.deterministic.Deterministic. init

Deterministic. init (*args, **kwargs)

bayespy.inference.vmp.nodes.deterministic.Deterministic.add plate axis

Deterministic.add_plate_axis(to_plate)

bayespy.inference.vmp.nodes.deterministic.Deterministic.delete

Deterministic.delete()

Delete this node and the children

bayespy.inference.vmp.nodes.deterministic.Deterministic.get_mask

Deterministic.get_mask()

bayespy.inference.vmp.nodes.deterministic.Deterministic.get_moments

Deterministic.get moments()

bayespy.inference.vmp.nodes.deterministic.Deterministic.get_shape

Deterministic.get_shape(ind)

bayespy.inference.vmp.nodes.deterministic.Deterministic.has_plotter

Deterministic.has_plotter()
Return True if the node has a plotter

bayespy.inference.vmp.nodes.deterministic.Deterministic.lower bound contribution

Deterministic.lower_bound_contribution(gradient=False)

bayespy.inference.vmp.nodes.deterministic.Deterministic.move_plates

Deterministic.move_plates (from_plate, to_plate)

bayespy.inference.vmp.nodes.deterministic.Deterministic.plot

```
Deterministic.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.deterministic.Deterministic.set_plotter

```
Deterministic.set_plotter(plotter)
```

Attributes

plates

bayespy.inference.vmp.nodes.deterministic.Deterministic.plates

Deterministic.plates = None

The following nodes are examples of special nodes that remain hidden for the user although they are often implicitly used:

```
constant.Constant(moments, x, **kwargs)

gaussian.GaussianToGaussianGammaISO(X, **kwargs)

gaussian.GaussianGammaISOToGaussianGammaARD(X, ...)

gaussian.WrapToGaussianGammaARD(mu_alpha, ...)

gaussian.WrapToGaussianGammaARD(mu_alpha, ...)

gaussian.WrapToGaussianWishart(X, Lambda, ...)

Wraps Gaussian tvalues.

Converter for Gaussian moments to Gaussian-gamma ISO moments to Gaussian-gamma ISO
```

6.1.5 bayespy.inference.vmp.nodes.constant.Constant

```
class bayespy.inference.vmp.nodes.constant.Constant(moments, x, **kwargs)
    Node for presenting constant values.
```

The node wraps arrays into proper node type.

```
__init__ (moments, x, **kwargs)
```

Methods

Table 6.11 – continued from previous page

has_plotter()	Return True if the node has a plotter
<pre>move_plates(from_plate, to_plate)</pre>	
plot(**kwargs)	Plot the node distribution using the plotter of the node
set_plotter(plotter)	

bayespy.inference.vmp.nodes.constant.Constant.__init__

```
Constant.__init__(moments, x, **kwargs)
```

bayespy.inference.vmp.nodes.constant.Constant.add_plate_axis

```
Constant.add_plate_axis(to_plate)
```

bayespy.inference.vmp.nodes.constant.Constant.delete

```
Constant.delete()
```

Delete this node and the children

bayespy.inference.vmp.nodes.constant.Constant.get_mask

```
Constant.get_mask()
```

bayespy.inference.vmp.nodes.constant.Constant.get moments

```
Constant.get_moments()
```

bayespy.inference.vmp.nodes.constant.Constant.get shape

```
Constant.get_shape (ind)
```

bayespy.inference.vmp.nodes.constant.Constant.has plotter

```
Constant.has_plotter()
```

Return True if the node has a plotter

bayespy.inference.vmp.nodes.constant.Constant.move_plates

```
Constant.move plates (from plate, to plate)
```

bayespy.inference.vmp.nodes.constant.Constant.plot

```
Constant.plot(**kwargs)
```

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.constant.Constant.set_plotter

Constant.set_plotter(plotter)

Attributes

plates

bayespy.inference.vmp.nodes.constant.Constant.plates

Constant.plates = None

6.1.6 bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO

 ${f class}$ bayespy.inference.vmp.nodes.gaussian. ${f GaussianToGaussianGammaISO}$ (X,

**kwargs)

Converter for Gaussian moments to Gaussian-gamma isotropic moments

Combines the Gaussian moments with gamma moments for a fixed value 1.

Methods

bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO. init

GaussianToGaussianGammaISO.__init__(X, **kwargs)

bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.add plate axis

GaussianToGaussianGammaISO.add_plate_axis(to_plate)

bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.delete

GaussianToGaussianGammaISO.delete()

Delete this node and the children

bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.get_mask
GaussianToGaussianGammaISO.get_mask()
bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.get_moments
<pre>GaussianToGaussianGammaISO.get_moments()</pre>
bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.get_shape
${\tt GaussianToGaussianGammaISO.get_shape}~(ind)$
bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.has_plotter
GaussianToGaussianGammaISO.has_plotter() Return True if the node has a plotter
bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.lower_bound_contribution
${\tt GaussianToGaussianGammaISO.} \textbf{lower_bound_contribution} \ (\textit{gradient=False})$
bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.move_plates
GaussianToGaussianGammaISO.move_plates (from_plate, to_plate)
bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.plot
GaussianToGaussianGammaISO.plot (**kwargs) Plot the node distribution using the plotter of the node
Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.
bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.set_plotter
GaussianToGaussianGammaISO. set_plotter (plotter)
Attributes
plates
bayespy.inference.vmp.nodes.gaussian.GaussianToGaussianGammalSO.plates

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 ${\tt GaussianToGaussianGammaISO.plates = None}$

6.1.7 bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD

Methods

init(X, **kwargs)	
<pre>add_plate_axis(to_plate)</pre>	
delete()	Delete this node and the children
get_mask()	
<pre>get_moments()</pre>	
get_shape(ind)	
has_plotter()	Return True if the node has a plotter
<pre>lower_bound_contribution([gradient])</pre>	
<pre>move_plates(from_plate, to_plate)</pre>	
plot(**kwargs)	Plot the node distribution using the plotter of the node
set_plotter(plotter)	

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.__init__

GaussianGammaISOToGaussianGammaARD.__init__(X, **kwargs)

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.add_plate_axis

GaussianGammaISOToGaussianGammaARD.add_plate_axis(to_plate)

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.delete

GaussianGammaISOToGaussianGammaARD.**delete**()

Delete this node and the children

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.get mask

GaussianGammaISOToGaussianGammaARD.get_mask()

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.get moments

GaussianGammaISOToGaussianGammaARD.get_moments()

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.get shape

 ${\tt GaussianGammaISOToGaussianGammaARD.} \textbf{get_shape} \ (ind)$

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.has_plotter

GaussianGammaISOToGaussianGammaARD.has_plotter()
Return True if the node has a plotter

$bayes py. inference. vmp. nodes. gaussian. Gaussian Gammal SOTo Gaussian Gamma ARD. lower_bound_contributed for the contributed for the contribu$

GaussianGammaISOToGaussianGammaARD.lower_bound_contribution(gradient=False)

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.move plates

GaussianGammaISOToGaussianGammaARD.move_plates(from_plate, to_plate)

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.plot

GaussianGammaISOToGaussianGammaARD.plot (**kwargs)
Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

$bayes py. inference. vmp. nodes. gaussian. Gaussian Gammal SOTo Gaussian Gamma ARD. set_plotter$

GaussianGammaISOToGaussianGammaARD.set_plotter(plotter)

Attributes

plates

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOToGaussianGammaARD.plates

GaussianGammaISOToGaussianGammaARD.plates = None

6.1.8 bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart

 ${\bf class} \ {\bf bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart} \ (X_alpha, \\ **kwargs)$

```
___init___(X_alpha, **kwargs)
```

Methods

__init__(X_alpha, **kwargs)
add_plate_axis(to_plate)
delete()

Delete this node and the children

Continued on next page

Table 6.17 – continued from previous page

```
get_mask()
get_moments()
get_shape(ind)
has_plotter()
lower_bound_contribution([gradient])
move_plates(from_plate, to_plate)
plot(**kwargs)
set_plotter(plotter)
Return True if the node has a plotter
Plot the node distribution using the plotter of the node
set_plotter(plotter)
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.__init__

GaussianGammaARDToGaussianWishart.__init__(X_alpha, **kwargs)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.add plate axis

GaussianGammaARDToGaussianWishart.add_plate_axis(to_plate)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.delete

GaussianGammaARDToGaussianWishart.delete()
 Delete this node and the children

$bayes py. inference. vmp. nodes. gaussian. Gaussian Gamma ARD To Gaussian Wishart. get_mask$

GaussianGammaARDToGaussianWishart.get_mask()

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.get moments

GaussianGammaARDToGaussianWishart.get_moments()

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.get_shape

GaussianGammaARDToGaussianWishart.get_shape (ind)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.has_plotter

GaussianGammaARDToGaussianWishart.has_plotter()
Return True if the node has a plotter

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.lower_bound_contribution

GaussianGammaARDToGaussianWishart.lower_bound_contribution(gradient=False)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.move plates

GaussianGammaARDToGaussianWishart.move_plates(from_plate, to_plate)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.plot

GaussianGammaARDToGaussianWishart.plot(**kwargs)

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.set_plotter

GaussianGammaARDToGaussianWishart.set_plotter(plotter)

Attributes

plates

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDToGaussianWishart.plates

GaussianGammaARDToGaussianWishart.plates = None

6.1.9 bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO

__init__(*parents, **kwargs)

Methods

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.__init__

WrapToGaussianGammaISO.__init__(*parents, **kwargs)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.add_plate_axis

WrapToGaussianGammaISO.add_plate_axis(to_plate)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.delete

WrapToGaussianGammaISO.delete()

Delete this node and the children

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.get mask

WrapToGaussianGammaISO.get_mask()

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.get moments

WrapToGaussianGammaISO.get_moments()

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.get_shape

WrapToGaussianGammaISO.get_shape (ind)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.has plotter

WrapToGaussianGammaISO.has_plotter()
Return True if the node has a plotter

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.lower_bound_contribution

WrapToGaussianGammaISO.lower_bound_contribution(gradient=False)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.move plates

WrapToGaussianGammaISO.move_plates (from_plate, to_plate)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.plot

WrapToGaussianGammaISO.plot(**kwargs)

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.set plotter

WrapToGaussianGammaISO.set_plotter(plotter)

Attributes

plates		

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammalSO.plates

WrapToGaussianGammaISO.plates = None

6.1.10 bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD

```
{\bf class} \ {\bf bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD} \ ({\it mu\_alpha, tau, **kwargs})
```

```
__init__ (mu_alpha, tau, **kwargs)
```

Methods

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD. init

```
WrapToGaussianGammaARD.__init__ (mu_alpha, tau, **kwargs)
```

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.add plate axis

WrapToGaussianGammaARD.add_plate_axis(to_plate)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.delete

```
WrapToGaussianGammaARD.delete()

Delete this node and the children
```

$bayes py. inference. vmp. nodes. gaussian. Wrap To Gaussian Gamma ARD. get_mask$

```
WrapToGaussianGammaARD.get_mask()
```

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.get_moments

WrapToGaussianGammaARD.get_moments()

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.get_shape

WrapToGaussianGammaARD.get_shape (ind)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.has_plotter

WrapToGaussianGammaARD.has_plotter()
Return True if the node has a plotter

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.lower_bound_contribution

WrapToGaussianGammaARD.lower_bound_contribution(gradient=False)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.move_plates

WrapToGaussianGammaARD.move_plates (from_plate, to_plate)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.plot

WrapToGaussianGammaARD.plot(**kwargs)

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.set_plotter

WrapToGaussianGammaARD.set_plotter(plotter)

Attributes

plates

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianGammaARD.plates

WrapToGaussianGammaARD.plates = None

6.1.11 bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart

The following node combinations can be wrapped:

- · Gaussian and Wishart
- Gaussian-gamma and Wishart
- · Gaussian-Wishart and gamma

```
__init__(X, Lambda, **kwargs)
```

Methods

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.__init__

```
WrapToGaussianWishart.__init__(X, Lambda, **kwargs)
```

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.add plate axis

WrapToGaussianWishart.add_plate_axis(to_plate)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.delete

```
WrapToGaussianWishart.delete()

Delete this node and the children
```

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.get_mask

```
WrapToGaussianWishart.get_mask()
```

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.get_moments

```
WrapToGaussianWishart.get_moments()
```

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.get shape

```
WrapToGaussianWishart.get_shape(ind)
```

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.has_plotter

WrapToGaussianWishart.has_plotter()
Return True if the node has a plotter

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.lower_bound_contribution

WrapToGaussianWishart.lower_bound_contribution(gradient=False)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.move_plates

WrapToGaussianWishart.move_plates (from_plate, to_plate)

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.plot

WrapToGaussianWishart.plot(**kwargs)

Plot the node distribution using the plotter of the node

Because the distributions are in general very difficult to plot, the user must specify some functions which performs the plotting as wanted. See, for instance, bayespy.plot.plotting for available plotters, that is, functions that perform plotting for a node.

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.set_plotter

WrapToGaussianWishart.set_plotter(plotter)

Attributes

plates

bayespy.inference.vmp.nodes.gaussian.WrapToGaussianWishart.plates

WrapToGaussianWishart.plates = None

6.2 Moments

node.Moments	Base class for defining the expectation of the s
gaussian.GaussianMoments(ndim)	Class for the moments of Gaussian variables.
gaussian_markov_chain.GaussianMarkovChainMoments	
gaussian.GaussianGammaISOMoments(ndim)	Class for the moments of Gaussian-gamma-IS
gaussian.GaussianGammaARDMoments(ndim)	Class for the moments of Gaussian-gamma-Al-
gaussian.GaussianWishartMoments	Class for the moments of Gaussian-Wishart va
gamma.GammaMoments	Class for the moments of gamma variables.
wishart.WishartMoments	
beta.BetaMoments	Class for the moments of beta variables.
dirichlet.DirichletMoments	Class for the moments of Dirichlet variables.

Continu

Table 6.25 – continued from previous page

bernoulli.BernoulliMoments()	Class for the moments of Bernoulli variables.
$\verb binomial.BinomialMoments (N) $	Class for the moments of binomial variables
categorical.CategoricalMoments(categories)	Class for the moments of categorical variables
categorical_markov_chain.CategoricalMarkovChainMoments()	Class for the moments of categorical Markov of
multinomial.MultinomialMoments	Class for the moments of multinomial variable
poisson.PoissonMoments	Class for the moments of Poisson variables

6.2.1 bayespy.inference.vmp.nodes.node.Moments

class bayespy.inference.vmp.nodes.node.Moments

Base class for defining the expectation of the sufficient statistics.

The benefits:

- •Write statistic-specific features in one place only. For instance, covariance from Gaussian message.
- •Different nodes may have identically defined statistic so you need to implement related features only once. For instance, Gaussian and GaussianARD differ on the prior but the moments are the same.
- •General processing nodes which do not change the type of the moments may "inherit" the features from the parent node. For instance, slicing operator.
- •Conversions can be done easily in both of the above cases if the message conversion is defined in the moments class. For instance, GaussianMarkovChain to Gaussian and VaryingGaussianMarkovChain to Gaussian.

```
__init__()
Initialize self. See help(type(self)) for accurate signature.
```

Methods

```
add_converter(moments_to, converter)
compute_dims_from_values(x)
compute_fixed_moments(x)
get_converter(moments_to)
Finds conversion to another moments type if possible.
```

bayespy.inference.vmp.nodes.node.Moments.add_converter

classmethod Moments . add_converter (moments_to, converter)

bayespy.inference.vmp.nodes.node.Moments.compute dims from values

Moments.compute_dims_from_values(x)

bayespy.inference.vmp.nodes.node.Moments.compute_fixed_moments

Moments.compute_fixed_moments (x)

bayespy.inference.vmp.nodes.node.Moments.get_converter

```
Moments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.2 bayespy.inference.vmp.nodes.gaussian.GaussianMoments

```
class bayespy.inference.vmp.nodes.gaussian.GaussianMoments (ndim)
    Class for the moments of Gaussian variables.
```

Methods

___init___(ndim)

init(ndim)	
<pre>add_converter(moments_to, converter)</pre>	
$compute_dims_from_values(x)$	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.gaussian.GaussianMoments.__init__

```
GaussianMoments.__init__(ndim)
```

bayespy.inference.vmp.nodes.gaussian.GaussianMoments.add converter

```
GaussianMoments.add_converter (moments_to, converter)
```

bayespy.inference.vmp.nodes.gaussian.GaussianMoments.compute dims from values

```
GaussianMoments.compute_dims_from_values (x)
Return the shape of the moments for a fixed value.
```

bayespy.inference.vmp.nodes.gaussian.GaussianMoments.compute_fixed_moments

```
GaussianMoments.compute_fixed_moments(x)
Compute the moments for a fixed value
```

bayespy.inference.vmp.nodes.gaussian.GaussianMoments.get_converter

```
GaussianMoments.get_converter (moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.3 bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainMoments

class bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainMoments

```
__init___()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

```
add_converter(moments_to, converter)
compute_dims_from_values(x)
compute_fixed_moments(x)
get_converter(moments_to)
Finds conversion to another moments type if possible.
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainMoments.add_converter

GaussianMarkovChainMoments.add converter (moments to, converter)

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Gaussian Markov Chain Moments. compute_dims_from_chain. Gaussian Markov Chain Markov Chain Moments. Compute_dims_from_chain. Gaussian Markov Chain Markov Chain$

 ${\tt Gaussian Markov Chain Moments.} \textbf{compute_dims_from_values} \ (x)$

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Gaussian Markov Chain Moments. compute_fixed_moments. co$

GaussianMarkovChainMoments.compute_fixed_moments(x)

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainMoments.get_converter

```
GaussianMarkovChainMoments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.4 bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOMoments

class bayespy.inference.vmp.nodes.gaussian.GaussianGammaISOMoments (ndim)
 Class for the moments of Gaussian-gamma-ISO variables.

```
___init___(ndim)
```

Create moments object for Gaussian-gamma isotropic variables

ndim=0: scalar ndim=1: vector ndim=2: matrix ...

Methods

init(ndim)	Create moments object for Gaussian-gamma isotropic variables
<pre>add_converter(moments_to, converter)</pre>	
<pre>compute_dims_from_values(x, alpha)</pre>	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x, alpha)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOMoments.__init__

```
GaussianGammaISOMoments.__init__(ndim)
Create moments object for Gaussian-gamma isotropic variables
ndim=0: scalar ndim=1: vector ndim=2: matrix ...
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOMoments.add converter

GaussianGammaISOMoments.add_converter (moments_to, converter)

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOMoments.compute dims from values

```
GaussianGammaISOMoments.compute_dims_from_values (x, alpha)
Return the shape of the moments for a fixed value.
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOMoments.compute fixed moments

```
GaussianGammaISOMoments.compute_fixed_moments(x, alpha)
Compute the moments for a fixed value

x is a mean vector. alpha is a precision scale
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSOMoments.get converter

```
GaussianGammaISOMoments.get_converter(moments_to)
Finds conversion to another moments type if possible.
```

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.5 bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDMoments

```
___init___(ndim)
```

Create moments object for Gaussian-gamma isotropic variables

ndim=0: scalar ndim=1: vector ndim=2: matrix ...

Methods

init(ndim)	Create moments object for Gaussian-gamma isotropic variables
<pre>add_converter(moments_to, converter)</pre>	
<pre>compute_dims_from_values(x, alpha)</pre>	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x, alpha)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDMoments. init

```
GaussianGammaARDMoments.__init__(ndim)
Create moments object for Gaussian-gamma isotropic variables
ndim=0: scalar ndim=1: vector ndim=2: matrix ...
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDMoments.add converter

GaussianGammaARDMoments.add_converter (moments_to, converter)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDMoments.compute dims from values

```
GaussianGammaARDMoments.compute_dims_from_values (x, alpha)
Return the shape of the moments for a fixed value.
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDMoments.compute_fixed_moments

```
GaussianGammaARDMoments.compute_fixed_moments (x, alpha)
Compute the moments for a fixed value

x is a mean vector. alpha is a precision scale
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDMoments.get_converter

GaussianGammaARDMoments.get_converter (moments_to)

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.6 bayespy.inference.vmp.nodes.gaussian.GaussianWishartMoments

class bayespy.inference.vmp.nodes.gaussian.GaussianWishartMoments
 Class for the moments of Gaussian-Wishart variables.

```
__init__()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

add_converter(moments_to, converter)	
<pre>compute_dims_from_values(x, Lambda)</pre>	Return the shape of the moments for a fixed value.
<pre>compute_fixed_moments(x, Lambda)</pre>	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.gaussian.GaussianWishartMoments.add_converter

GaussianWishartMoments.add_converter (moments_to, converter)

bayespy.inference.vmp.nodes.gaussian.GaussianWishartMoments.compute dims from values

```
GaussianWishartMoments.compute_dims_from_values (x, Lambda)
Return the shape of the moments for a fixed value.
```

bayespy.inference.vmp.nodes.gaussian.GaussianWishartMoments.compute fixed moments

```
GaussianWishartMoments.compute_fixed_moments (x, Lambda)
Compute the moments for a fixed value

x is a vector. Lambda is a precision matrix
```

bayespy.inference.vmp.nodes.gaussian.GaussianWishartMoments.get converter

```
GaussianWishartMoments.get_converter (moments_to) Finds conversion to another moments type if possible.
```

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.7 bayespy.inference.vmp.nodes.gamma.GammaMoments

```
class bayespy.inference.vmp.nodes.gamma.GammaMoments
    Class for the moments of gamma variables.
```

```
init ()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

add_converter(moments_to, converter)	
$compute_dims_from_values(x)$	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.gamma.GammaMoments.add converter

```
GammaMoments.add_converter (moments_to, converter)
```

bayespy.inference.vmp.nodes.gamma.GammaMoments.compute dims from values

```
{\tt GammaMoments.compute\_dims\_from\_values}\ (x)
```

Return the shape of the moments for a fixed value.

bayespy.inference.vmp.nodes.gamma.GammaMoments.compute fixed moments

```
GammaMoments.compute_fixed_moments (x)
Compute the moments for a fixed value
```

bayespy.inference.vmp.nodes.gamma.GammaMoments.get_converter

```
GammaMoments.get_converter (moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.8 bayespy.inference.vmp.nodes.wishart.WishartMoments

class bayespy.inference.vmp.nodes.wishart.WishartMoments

```
___init___()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

add_converter(moments_to, converter)	
$compute_dims_from_values(x)$	Compute the dimensions of phi and u.
<pre>compute_fixed_moments(Lambda)</pre>	Compute moments for fixed x.
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.wishart.WishartMoments.add_converter

WishartMoments.add_converter (moments_to, converter)

bayespy.inference.vmp.nodes.wishart.WishartMoments.compute_dims_from_values

```
WishartMoments.compute_dims_from_values (x) Compute the dimensions of phi and u.
```

bayespy.inference.vmp.nodes.wishart.WishartMoments.compute fixed moments

```
WishartMoments.compute_fixed_moments(Lambda)
Compute moments for fixed x.
```

bayespy.inference.vmp.nodes.wishart.WishartMoments.get_converter

```
WishartMoments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.9 bayespy.inference.vmp.nodes.beta.BetaMoments

Methods

add_converter(moments_to, converter)	
<pre>compute_dims_from_values(p)</pre>	Return the shape of the moments for a fixed value.
<pre>compute_fixed_moments(p)</pre>	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.beta.BetaMoments.add converter

BetaMoments.add_converter (moments_to, converter)

bayespy.inference.vmp.nodes.beta.BetaMoments.compute_dims_from_values

```
BetaMoments.compute_dims_from_values (p)
Return the shape of the moments for a fixed value.
```

bayespy.inference.vmp.nodes.beta.BetaMoments.compute fixed moments

```
BetaMoments.compute_fixed_moments(p)
Compute the moments for a fixed value
```

bayespy.inference.vmp.nodes.beta.BetaMoments.get converter

```
BetaMoments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.10 bayespy.inference.vmp.nodes.dirichlet.DirichletMoments

```
class bayespy.inference.vmp.nodes.dirichlet.DirichletMoments
    Class for the moments of Dirichlet variables.
```

```
__init__()
Initialize self. See help(type(self)) for accurate signature.
```

Methods

add_converter(moments_to, converter)	
$compute_dims_from_values(x)$	Return the shape of the moments for a fixed value.
<pre>compute_fixed_moments(p)</pre>	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.dirichlet.DirichletMoments.add_converter

```
DirichletMoments.add_converter (moments_to, converter)
```

bayespy.inference.vmp.nodes.dirichlet.DirichletMoments.compute_dims_from_values

```
DirichletMoments.compute_dims_from_values (x)
Return the shape of the moments for a fixed value.
```

bayespy.inference.vmp.nodes.dirichlet.DirichletMoments.compute_fixed_moments

```
DirichletMoments.compute_fixed_moments(p)

Compute the moments for a fixed value
```

bayespy.inference.vmp.nodes.dirichlet.DirichletMoments.get converter

```
DirichletMoments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.11 bayespy.inference.vmp.nodes.bernoulli.BernoulliMoments

```
{\bf class} \; {\tt bayespy.inference.vmp.nodes.bernoulli.BernoulliMoments} \\ Class \; {\tt for} \; {\tt the} \; {\tt moments} \; {\tt of} \; {\tt Bernoullivariables}.
```

```
___init___()
```

Methods

```
__init__()
add_converter(moments_to, converter)
compute_dims_from_values(x)
compute_fixed_moments(x)
get_converter(moments_to)

Return the shape of the moments for a fixed value.
Compute the moments for a fixed value
Finds conversion to another moments type if possible.
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliMoments. init

```
BernoulliMoments.__init__()
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliMoments.add converter

BernoulliMoments.add_converter(moments_to, converter)

bayespy.inference.vmp.nodes.bernoulli.BernoulliMoments.compute_dims_from_values

```
BernoulliMoments.compute_dims_from_values(x)
```

Return the shape of the moments for a fixed value.

The realizations are scalars, thus the shape of the moment is ().

bayespy.inference.vmp.nodes.bernoulli.BernoulliMoments.compute_fixed_moments

```
{\tt BernoulliMoments.compute\_fixed\_moments}\,(x)
```

Compute the moments for a fixed value

bayespy.inference.vmp.nodes.bernoulli.BernoulliMoments.get_converter

```
BernoulliMoments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.12 bayespy.inference.vmp.nodes.binomial.BinomialMoments

```
class bayespy.inference.vmp.nodes.binomial.BinomialMoments(N)
```

Class for the moments of binomial variables

```
___init___(N)
```

Methods

init(N)	
<pre>add_converter(moments_to, converter)</pre>	
$compute_dims_from_values(x)$	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.binomial.BinomialMoments. init

```
BinomialMoments.__init__(N)
```

bayespy.inference.vmp.nodes.binomial.BinomialMoments.add converter

BinomialMoments.add_converter(moments_to, converter)

bayespy.inference.vmp.nodes.binomial.BinomialMoments.compute_dims_from_values

```
BinomialMoments.compute_dims_from_values(x)
```

Return the shape of the moments for a fixed value.

The realizations are scalars, thus the shape of the moment is ().

bayespy.inference.vmp.nodes.binomial.BinomialMoments.compute_fixed_moments

```
BinomialMoments.compute_fixed_moments(x)
```

Compute the moments for a fixed value

bayespy.inference.vmp.nodes.binomial.BinomialMoments.get_converter

```
BinomialMoments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.13 bayespy.inference.vmp.nodes.categorical.CategoricalMoments

```
__init__(categories)
```

Create moments object for categorical variables

Methods

init(categories)	Create moments object for categorical variables
<pre>add_converter(moments_to, converter)</pre>	
$compute_dims_from_values(x)$	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.categorical.CategoricalMoments.__init__

```
Categorical Moments.__init__(categories)

Create moments object for categorical variables
```

bayespy.inference.vmp.nodes.categorical.CategoricalMoments.add converter

CategoricalMoments.add_converter (moments_to, converter)

bayespy.inference.vmp.nodes.categorical.CategoricalMoments.compute_dims_from_values

CategoricalMoments.compute_dims_from_values(x)

Return the shape of the moments for a fixed value.

The observations are scalar.

bayespy.inference.vmp.nodes.categorical.CategoricalMoments.compute_fixed_moments

```
Categorical Moments.compute_fixed_moments (x)
```

Compute the moments for a fixed value

bayespy.inference.vmp.nodes.categorical.CategoricalMoments.get_converter

CategoricalMoments.get_converter(moments_to)

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.14 bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainMome

class bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainMoments(categorical Markov chain variables.

```
___init___(categories)
```

Create moments object for categorical Markov chain variables.

Methods

init(categories) Create moments object for categorical Markov chain vari	
<pre>add_converter(moments_to, converter)</pre>	
$ exttt{compute_dims_from_values}(\mathbf{x})$	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainMoments.__init__

```
Create moments chiest for categories | Markov chain variables
```

Create moments object for categorical Markov chain variables.

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainMoments.add_converter

CategoricalMarkovChainMoments.add_converter(moments_to, converter)

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainMoments.compute_dims_f

```
CategoricalMarkovChainMoments.compute_dims_from_values (x) Return the shape of the moments for a fixed value.
```

$bayes py. inference. vmp. nodes. categorical_markov_chain. Categorical Markov Chain Moments. compute_fixed_nodes. Categorical_markov_chain. Categorical_markov_chai$

```
CategoricalMarkovChainMoments.compute_fixed_moments(x)
    Compute the moments for a fixed value
```

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainMoments.get_converter

```
CategoricalMarkovChainMoments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.15 bayespy.inference.vmp.nodes.multinomial.MultinomialMoments

class bayespy.inference.vmp.nodes.multinomial.MultinomialMoments
 Class for the moments of multinomial variables.

```
__init__()
Initialize self. See help(type(self)) for accurate signature.
```

Methods

add_converter(moments_to, converter)	
$compute_dims_from_values(x)$	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.multinomial.MultinomialMoments.add_converter

```
MultinomialMoments.add_converter (moments_to, converter)
```

bayespy.inference.vmp.nodes.multinomial.MultinomialMoments.compute_dims_from_values

```
MultinomialMoments.compute_dims_from_values (x)
Return the shape of the moments for a fixed value.
```

bayespy.inference.vmp.nodes.multinomial.MultinomialMoments.compute_fixed_moments

```
MultinomialMoments.compute_fixed_moments (x)
Compute the moments for a fixed value

x must be a vector of counts.
```

bayespy.inference.vmp.nodes.multinomial.MultinomialMoments.get_converter

```
MultinomialMoments.get_converter(moments_to)
Finds conversion to another moments type if possible.
```

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.2.16 bayespy.inference.vmp.nodes.poisson.PoissonMoments

Methods

add_converter(moments_to, converter)	
$compute_dims_from_values(x)$	Return the shape of the moments for a fixed value.
$compute_fixed_moments(x)$	Compute the moments for a fixed value
<pre>get_converter(moments_to)</pre>	Finds conversion to another moments type if possible.

bayespy.inference.vmp.nodes.poisson.PoissonMoments.add converter

```
PoissonMoments.add_converter (moments_to, converter)
```

bayespy.inference.vmp.nodes.poisson.PoissonMoments.compute_dims_from values

```
PoissonMoments.compute_dims_from_values (x)
Return the shape of the moments for a fixed value.
```

The realizations are scalars, thus the shape of the moment is ().

bayespy.inference.vmp.nodes.poisson.PoissonMoments.compute_fixed_moments

```
PoissonMoments.compute_fixed_moments(x)
Compute the moments for a fixed value
```

bayespy.inference.vmp.nodes.poisson.PoissonMoments.get_converter

```
PoissonMoments.get_converter(moments_to)
```

Finds conversion to another moments type if possible.

Note that a conversion from moments A to moments B may require intermediate conversions. For instance: A->C->D->B. This method finds the path which uses the least amount of conversions and returns that path as a single conversion. If no conversion path is available, an error is raised.

The search algorithm starts from the original moments class and applies all possible converters to get a new list of moments classes. This list is extended by adding recursively all parent classes because their converters are applicable. Then, all possible converters are applied to this list to get a new list of current moments classes. This is iterated until the algorithm hits the target moments class or its subclass.

6.3 Distributions

_		
	stochastic.Distribution	A base class for the VMP for
	expfamily.ExponentialFamilyDistribution	Sub-classes implement distr
	gaussian.GaussianDistribution	Class for the VMP formulas
	gaussian.GaussianARDDistribution(shape, ndim_mu)	
	gaussian.GaussianGammaISODistribution	Class for the VMP formulas
	gaussian.GaussianGammaARDDistribution()	
	gaussian.GaussianWishartDistribution	Class for the VMP formulas
	gaussian_markov_chain. $ ext{GaussianMarkovChainDistribution}(ext{N}, ext{D})$	Sub-classes implement distr
	$\verb gaussian_markov_chain.SwitchingGaussianMarkovChainDistribution (N, D, K) $	Sub-classes implement distr
	$ ext{gaussian_markov_chain.VaryingGaussianMarkovChainDistribution}(N, D)$	Sub-classes implement distr
	gamma.GammaDistribution	Class for the VMP formulas
	wishart.WishartDistribution	Sub-classes implement distr
	beta.BetaDistribution	Class for the VMP formulas
	dirichlet.DirichletDistribution	Class for the VMP formulas
	bernoulli.BernoulliDistribution()	Class for the VMP formulas
	binomial.BinomialDistribution(N)	Class for the VMP formulas
	categorical.CategoricalDistribution(categories)	Class for the VMP formulas
	categorical_markov_chain.CategoricalMarkovChainDistribution()	Class for the VMP formulas
	multinomial.MultinomialDistribution(trials)	Class for the VMP formulas
	poisson.PoissonDistribution	Class for the VMP formulas
-		

6.3.1 bayespy.inference.vmp.nodes.stochastic.Distribution

Initialize self. See help(type(self)) for accurate signature.

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Methods

<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index,)</pre>	Compute the message to a parent node.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*params[, plates])	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.stochastic.Distribution.compute mask to parent

```
Distribution.compute_mask_to_parent(index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.stochastic.Distribution.compute_message_to_parent

```
Distribution.compute_message_to_parent (parent, index, u_self, *u_parents)

Compute the message to a parent node.
```

bayespy.inference.vmp.nodes.stochastic.Distribution.plates_from_parent

```
Distribution.plates_from_parent (index, plates)
Resolve the plate mapping from a parent.
```

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.stochastic.Distribution.plates to parent

```
Distribution.plates_to_parent (index, plates)
Resolves the plate mapping to a parent.
```

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.stochastic.Distribution.random

Initialize self. See help(type(self)) for accurate signature.

```
Distribution.random(*params, plates=None)
Draw a random sample from the distribution.
```

6.3.2 bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution

```
class bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution
    Sub-classes implement distribution specific computations.
    init___()
```

Methods

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.compute_cgf_from_parents

ExponentialFamilyDistribution.compute_cgf_from_parents(*u_parents)

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.compute_fixed_moments_and_f

ExponentialFamilyDistribution.compute_fixed_moments_and_f(x, mask=True)

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.compute logpdf

ExponentialFamilyDistribution.compute_logpdf (u, phi, g, f, ndims)Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.compute mask to parent

ExponentialFamilyDistribution.compute_mask_to_parent(index, mask)

Maps the mask to the plates of a parent.

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.compute message to parent

ExponentialFamilyDistribution.compute_message_to_parent (parent, index, u_self, *u_parents)

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.compute_moments_and_cgf

ExponentialFamilyDistribution.compute_moments_and_cqf(phi, mask=True)

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.compute phi from parents

ExponentialFamilyDistribution.compute_phi_from_parents(*u_parents, mask=True)

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bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.plates_from_parent

ExponentialFamilyDistribution.plates_from_parent (index, plates)

Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.plates_to_parent

ExponentialFamilyDistribution.plates_to_parent (index, plates)

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.expfamily.ExponentialFamilyDistribution.random

ExponentialFamilyDistribution.random(*params, plates=None)

Draw a random sample from the distribution.

6.3.3 bayespy.inference.vmp.nodes.gaussian.GaussianDistribution

class bayespy.inference.vmp.nodes.gaussian.GaussianDistribution
 Class for the VMP formulas of Gaussian variables.

Currently, supports only vector variables.

Notes

Message passing equations:

$$\mathbf{x} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Lambda}),$$

 $\mathbf{x}, \boldsymbol{\mu} \in \mathbb{R}^D$, $\boldsymbol{\Lambda} \in \mathbb{R}^{D \times D}$, $\boldsymbol{\Lambda}$ symmetric positive definite

$$\log \mathcal{N}(\mathbf{x}|\boldsymbol{\mu},\boldsymbol{\Lambda}) = -\frac{1}{2}\mathbf{x}^{\mathrm{T}}\boldsymbol{\Lambda}\mathbf{x} + \mathbf{x}^{\mathrm{T}}\boldsymbol{\Lambda}\boldsymbol{\mu} - \frac{1}{2}\boldsymbol{\mu}^{\mathrm{T}}\boldsymbol{\Lambda}\boldsymbol{\mu} + \frac{1}{2}\log|\boldsymbol{\Lambda}| - \frac{D}{2}\log(2\pi)$$

$$\begin{aligned} \mathbf{u}(\mathbf{x}) &= \begin{bmatrix} \mathbf{x} \\ \mathbf{x} \mathbf{x}^T \end{bmatrix} \\ \boldsymbol{\phi}(\boldsymbol{\mu}, \boldsymbol{\Lambda}) &= \begin{bmatrix} \boldsymbol{\Lambda} \boldsymbol{\mu} \\ -\frac{1}{2} \boldsymbol{\Lambda} \end{bmatrix} \\ \boldsymbol{\phi}_{\boldsymbol{\mu}}(\mathbf{x}, \boldsymbol{\Lambda}) &= \begin{bmatrix} \boldsymbol{\Lambda} \mathbf{x} \\ -\frac{1}{2} \boldsymbol{\Lambda} \end{bmatrix} \\ \boldsymbol{\phi}_{\boldsymbol{\Lambda}}(\mathbf{x}, \boldsymbol{\mu}) &= \begin{bmatrix} -\frac{1}{2} \mathbf{x} \mathbf{x}^T + \frac{1}{2} \mathbf{x} \boldsymbol{\mu}^T + \frac{1}{2} \boldsymbol{\mu} \mathbf{x}^T - \frac{1}{2} \boldsymbol{\mu} \boldsymbol{\mu}^T \end{bmatrix} \\ g(\boldsymbol{\mu}, \boldsymbol{\Lambda}) &= -\frac{1}{2} \operatorname{tr}(\boldsymbol{\mu} \boldsymbol{\mu}^T \boldsymbol{\Lambda}) + \frac{1}{2} \log |\boldsymbol{\Lambda}| \\ g_{\boldsymbol{\phi}}(\boldsymbol{\phi}) &= \frac{1}{4} \boldsymbol{\phi}_1^T \boldsymbol{\phi}_2^{-1} \boldsymbol{\phi}_1 + \frac{1}{2} \log |\boldsymbol{-2} \boldsymbol{\phi}_2| \\ f(\mathbf{x}) &= -\frac{D}{2} \log(2\pi) \\ \overline{\mathbf{u}}(\boldsymbol{\phi}) &= \begin{bmatrix} -\frac{1}{2} \boldsymbol{\phi}_2^{-1} \boldsymbol{\phi}_1 \\ \frac{1}{4} \boldsymbol{\phi}_2^{-1} \boldsymbol{\phi}_1 \boldsymbol{\phi}_1^T \boldsymbol{\phi}_2^{-1} - \frac{1}{2} \boldsymbol{\phi}_2^{-1} \end{bmatrix} \end{aligned}$$

__init__()

Initialize self. See help(type(self)) for accurate signature.

Methods

compute_cgf_from_parents(u_mu_Lambda)	Compute $E_{q(p)}[g(p)]$
$compute_fixed_moments_and_f(x[, mask])$	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index, u,)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_mu_Lambda[, mask])</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*phi[, plates])	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.compute_cgf_from_parents

```
\label{eq:compute_cgf_from_parents} \textbf{GaussianDistribution.compute\_cgf\_from\_parents} \ (\textit{u\_mu\_Lambda}) \\ \textbf{Compute} \ \mathbf{E}_{q(p)}[g(p)]
```

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.compute_fixed_moments_and_f

```
GaussianDistribution.compute_fixed_moments_and_f (x, mask=True)
Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.compute logpdf

```
GaussianDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

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bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.compute_mask_to_parent

GaussianDistribution.compute_mask_to_parent (index, mask)

Maps the mask to the plates of a parent.

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.compute message to parent

GaussianDistribution.compute_message_to_parent (parent, index, u, u_mu_Lambda) Compute the message to a parent node.

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.compute_moments_and_cgf

GaussianDistribution.compute_moments_and_cgf (phi, mask=True)

Compute the moments and $g(\phi)$.

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.compute_phi_from_parents

GaussianDistribution.compute_phi_from_parents (u_mu_Lambda, mask=True)

Compute the natural parameter vector given parent moments.

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.plates_from_parent

GaussianDistribution.plates_from_parent (index, plates)

Passive the plate mapping from a parent

Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.plates to parent

GaussianDistribution.plates_to_parent (index, plates)
Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianDistribution.random

GaussianDistribution.random(*phi, plates=None)
Draw a random sample from the distribution.

6.3.4 bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution

Log probability density function:

$$\log p(x|\mu,\alpha) = -\frac{1}{2}x^T \operatorname{diag}(\alpha)x + x^T \operatorname{diag}(\alpha)\mu - \frac{1}{2}\mu^T \operatorname{diag}(\alpha)\mu + \frac{1}{2}\sum_i \log \alpha_i - \frac{D}{2}\log(2\pi)$$

Parent has moments:

$$\begin{bmatrix} \alpha \circ \mu \\ \alpha \circ \mu \circ \mu \\ \alpha \\ \log(\alpha) \end{bmatrix}$$

```
___init___(shape, ndim_mu)
```

Methods

```
_init___(shape, ndim_mu)
compute_cqf_from_parents(u_mu_alpha)
                                                     Compute the value of the cumulant generating function.
                                                     Compute u(x) and f(x) for given x.
compute_fixed_moments_and_f(x[, mask])
compute_logpdf(u, phi, g, f, ndims)
                                                     Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f].
                                                     Maps the mask to the plates of a parent.
compute_mask_to_parent(index, mask)
compute_message_to_parent(parent, index, u, ...)
compute_moments_and_cqf(phi[, mask])
compute_phi_from_parents(u_mu_alpha[, mask])
plates_from_parent(index, plates)
                                                     Resolve the plate mapping from a parent.
                                                     Resolves the plate mapping to a parent.
plates_to_parent(index, plates)
random(*phi[, plates])
                                                     Draw a random sample from the Gaussian distribution.
```

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution. init

```
GaussianARDDistribution.__init__(shape, ndim_mu)
```

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.compute cgf from parents

```
GaussianARDDistribution.compute_cgf_from_parents(u_mu_alpha)
Compute the value of the cumulant generating function.
```

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.compute fixed moments and f

```
GaussianARDDistribution.compute_fixed_moments_and_f (x, mask=True)
Compute u(x) and f(x) for given x.
```

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.compute_logpdf

```
GaussianARDDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.compute_mask_to_parent

```
GaussianARDDistribution.compute_mask_to_parent(index, mask) Maps the mask to the plates of a parent.
```

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bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.compute message to parent

 $\texttt{GaussianARDDistribution.compute_message_to_parent} \ (\textit{parent}, \textit{index}, \textit{u}, \textit{u_mu_alpha})$

$$m = \begin{bmatrix} x \\ \left[-\frac{1}{2}, \dots, -\frac{1}{2}\right] \\ -\frac{1}{2} \operatorname{diag}(xx^T) \\ \left[\frac{1}{2}, \dots, \frac{1}{2}\right] \end{bmatrix}$$

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.compute_moments_and_cgf

GaussianARDDistribution.compute_moments_and_cgf(phi, mask=True)

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.compute_phi_from_parents

GaussianARDDistribution.compute_phi_from_parents(u_mu_alpha, mask=True)

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.plates from parent

GaussianARDDistribution.plates_from_parent (index, plates)

Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.plates_to_parent

GaussianARDDistribution.plates_to_parent (index, plates)

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianARDDistribution.random

 ${\tt Gaussian ARDDistribution.random\,(*phi,plates=None)}$

Draw a random sample from the Gaussian distribution.

6.3.5 bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution

class bayespy.inference.vmp.nodes.gaussian.GaussianGammaISODistribution
 Class for the VMP formulas of Gaussian-Gamma-ISO variables.

Currently, supports only vector variables.

__init__()

Initialize self. See help(type(self)) for accurate signature.

Methods

```
Compute E_{q(p)}[g(p)]
compute_cgf_from_parents(u_mu_Lambda, u_a, u_b)
compute_fixed_moments_and_f(x, alpha[, mask])
                                                          Compute the moments and f(x) for a fixed value.
compute_logpdf(u, phi, g, f, ndims)
                                                          Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f].
                                                          Maps the mask to the plates of a parent.
compute_mask_to_parent(index, mask)
compute_message_to_parent(parent, index, u, ...)
                                                          Compute the message to a parent node.
compute_moments_and_cgf(phi[, mask])
                                                          Compute the moments and g(\phi).
compute_phi_from_parents(u_mu_Lambda, u_a, u_b)
                                                          Compute the natural parameter vector given parent moments.
                                                          Resolve the plate mapping from a parent.
plates_from_parent(index, plates)
plates_to_parent(index, plates)
                                                          Resolves the plate mapping to a parent.
                                                          Draw a random sample from the distribution.
random(*params[, plates])
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.compute_cgf_from_parents

```
GaussianGammaISODistribution.compute_cgf_from_parents(u\_mu\_Lambda, u\_a, u\_b)

Compute E_{q(p)}[g(p)]
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.compute_fixed_moments_and_f

```
GaussianGammaISODistribution.compute_fixed_moments_and_f(x, alpha, mask=True)

Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.compute_logpdf

```
GaussianGammaISODistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.compute_mask_to_parent

```
GaussianGammaISODistribution.compute_mask_to_parent (index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.compute message to parent

```
GaussianGammaISODistribution.compute_message_to_parent (parent, index, u, u_mu_Lambda, u_a, u_b)
```

Compute the message to a parent node.

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.compute moments and cgf

```
GaussianGammaISODistribution.compute_moments_and_cgf (phi, mask=True) Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.compute phi from parents

```
GaussianGammaISODistribution.compute_phi_from_parents (u\_mu\_Lambda, u\_a, u\_b, mask=True)

Compute the natural parameter vector given parent moments.
```

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bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.plates_from_parent

```
GaussianGammaISODistribution.plates_from_parent (index, plates)
Resolve the plate mapping from a parent.
```

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.plates to parent

```
GaussianGammaISODistribution.plates_to_parent (index, plates)
Resolves the plate mapping to a parent.
```

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianGammalSODistribution.random

```
GaussianGammaISODistribution.random(*params, plates=None)
Draw a random sample from the distribution.
```

6.3.6 bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution

class bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution

```
___init___()
```

Methods

```
init ()
compute_cgf_from_parents(*u_parents)
compute fixed moments and f(x[, mask])
                                                   Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f].
compute_logpdf(u, phi, g, f, ndims)
compute_mask_to_parent(index, mask)
                                                   Maps the mask to the plates of a parent.
compute_message_to_parent(parent, index, ...)
compute_moments_and_cgf(phi[, mask])
compute_phi_from_parents(*u_parents[, mask])
plates_from_parent(index, plates)
                                                   Resolve the plate mapping from a parent.
                                                   Resolves the plate mapping to a parent.
plates_to_parent(index, plates)
random(*params[, plates])
                                                   Draw a random sample from the distribution.
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.__init__

```
GaussianGammaARDDistribution.__init__()
```

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.compute_cgf_from_parents

GaussianGammaARDDistribution.compute_cgf_from_parents(*u_parents)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.compute_fixed_moments_and_f

GaussianGammaARDDistribution.compute_fixed_moments_and_f(x, mask=True)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.compute logpdf

GaussianGammaARDDistribution.compute_logpdf (u, phi, g, f, ndims)Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.compute_mask_to_parent

GaussianGammaARDDistribution.compute_mask_to_parent (index, mask)

Maps the mask to the plates of a parent.

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.compute message to parent

GaussianGammaARDDistribution.compute_message_to_parent(parent, index, u_self, *u_parents)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.compute moments and cgf

GaussianGammaARDDistribution.compute_moments_and_cgf(phi, mask=True)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.compute phi from parents

GaussianGammaARDDistribution.compute_phi_from_parents(*u_parents, mask=True)

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.plates from parent

GaussianGammaARDDistribution.plates_from_parent (index, plates)
Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianGammaARDDistribution.plates to parent

GaussianGammaARDDistribution.plates_to_parent (index, plates)
Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayes py. inference. vmp. nodes. gaussian. Gaussian Gamma ARD Distribution. random

GaussianGammaARDDistribution.random(*params, plates=None)
Draw a random sample from the distribution.

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6.3.7 bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution

class bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution
 Class for the VMP formulas of Gaussian-Wishart variables.

Currently, supports only vector variables.

```
__init___()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

compute_cgf_from_parents(u_mu_alpha, u_V, u_n)	Compute $E_{q(p)}[g(p)]$
<pre>compute_fixed_moments_and_f(x, Lambda[, mask])</pre>	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index, u,)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_mu_alpha, u_V, u_n)</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*params[, plates])	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.compute cgf from parents

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.compute fixed moments and f

```
GaussianWishartDistribution.compute_fixed_moments_and_f(x, Lambda, mask=True)

Compute the moments and f(x) for a fixed value.
```

$bayes py. inference. vmp. nodes. gaussian. Gaussian Wishart Distribution. compute_log pdf$

```
GaussianWishartDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.compute_mask_to_parent

```
GaussianWishartDistribution.compute_mask_to_parent (index, mask) Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.compute message to parent

Compute the message to a parent node.

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.compute_moments_and_cgf

```
GaussianWishartDistribution.compute_moments_and_cgf (phi, mask=True) Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.compute phi from parents

```
GaussianWishartDistribution.compute_phi_from_parents(u_mu_alpha, u_v, u_n, mask=True)

Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.plates from parent

```
GaussianWishartDistribution.plates_from_parent (index, plates)
Resolve the plate mapping from a parent.
```

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.plates_to_parent

```
GaussianWishartDistribution.plates_to_parent (index, plates)
Resolves the plate mapping to a parent.
```

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.gaussian.GaussianWishartDistribution.random

```
GaussianWishartDistribution.random(*params, plates=None)
Draw a random sample from the distribution.
```

6.3.8 bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainDistribution

```
\underline{\hspace{1cm}}init\underline{\hspace{1cm}}(N, D)
```

Methods

```
__init__(N, D)

compute_cgf_from_parents(u_mu, u_Lambda, ...)

compute_fixed_moments_and_f(x[, mask])

compute_logpdf(u, phi, g, f, ndims)

compute_mask_to_parent(index, mask)

compute_message_to_parent(parent, index, u, ...)

compute_moments_and_cgf(phi[, mask])

compute_phi_from_parents(u_mu, u_Lambda, ...)

Compute CGF using the moments of the parents.

Compute u(x) and f(x) for given x.

Compute E[log p(X)] given E[u], E[phi], E[g] and E[f].

Compute a message to a parent.

Compute a message to a parent.

Compute the moments and the cumulant-generating function.

Compute the natural parameters using parents' moments.
```

Table 6.50 – continued from previous page

<pre>plates_from_parent(index, plates)</pre>	Compute the plates using information of a parent node.
<pre>plates_to_parent(index, plates)</pre>	Computes the plates of this node with respect to a parent.
<pre>random(*params[, plates])</pre>	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainDistribution.__init__

```
GaussianMarkovChainDistribution. init (N, D)
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainDistribution.compute_cgf_from

```
GaussianMarkovChainDistribution.compute_cgf_from_parents(u_mu, u_Lambda, u_LA, u_LV)
```

Compute CGF using the moments of the parents.

 $bayes py. inference. vmp. nodes. gaussian_markov_chain. Gaussian Markov Chain Distribution. compute_fixed_models and the property of the pro$

```
GaussianMarkovChainDistribution.compute_fixed_moments_and_f (x, mask=True)
Compute u(x) and f(x) for given x.
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainDistribution.compute logpdf

```
GaussianMarkovChainDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

 $bayes py. inference. vmp. nodes. gaussian_markov_chain. Gaussian Markov Chain Distribution. compute_mask_torus and the properties of the$

```
GaussianMarkovChainDistribution.compute_mask_to_parent(index, mask)
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainDistribution.compute_message

```
GaussianMarkovChainDistribution.compute_message_to_parent (parent, index, u, u_mu, u_Lambda, u_A, u_v)
```

Compute a message to a parent.

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainDistribution.compute_moments

```
GaussianMarkovChainDistribution.compute_moments_and_cgf (phi, mask=True)

Compute the moments and the cumulant-generating function.
```

This basically performs the filtering and smoothing for the variable.

Parameters phi

Returns u

g

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainDistribution.compute_phi_from

```
GaussianMarkovChainDistribution.compute_phi_from_parents(u_mu, u_Lambda, u_LA, u_Lv, mask=True)
```

Compute the natural parameters using parents' moments.

Parameters u_parents: list of list of arrays

List of parents' lists of moments.

Returns phi: list of arrays

Natural parameters.

dims: tuple

Shape of the variable part of phi.

bayespy.inference.vmp.nodes.gaussian_markov_chain.GaussianMarkovChainDistribution.plates_from_parer

```
GaussianMarkovChainDistribution.plates_from_parent (index, plates)
```

Compute the plates using information of a parent node.

If the plates of the parents are: mu: (...) Lambda: (...) A: (...,N-1,D) v: (...,N-1,D) N: ()

the resulting plates of this node are (...)

Parameters index: int

Index of the parent to use.

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Gaussian Markov Chain Distribution. plates_to_parent$

```
GaussianMarkovChainDistribution.plates_to_parent(index, plates)
```

Computes the plates of this node with respect to a parent.

If this node has plates (...), the latent dimensionality is D and the number of time instances is N, the plates with respect to the parents are:

```
mu: (...) Lambda: (...) A: (...,N-1,D) v: (...,N-1,D)
```

bayespy.inference.vmp.nodes.gaussian markov chain.GaussianMarkovChainDistribution.random

```
GaussianMarkovChainDistribution.random(*params, plates=None)
Draw a random sample from the distribution.
```

6.3.9 bayespy.inference.vmp.nodes.gaussian_markov_chain.SwitchingGaussianMarkovChainDclass bayespy.inference.vmp.nodes.gaussian_markov_chain.SwitchingGaussianMarkovChainDistribut

Sub-classes implement distribution specific computations.

```
\_init\_(N, D, K)
```

Methods

```
_{\text{init}}_{\text{(N, D, K)}}
compute_cgf_from_parents(u_mu, u_Lambda, ...)
                                                       Compute CGF using the moments of the parents.
                                                       Compute u(x) and f(x) for given x.
compute_fixed_moments_and_f(x[, mask])
compute_logpdf(u, phi, g, f, ndims)
                                                       Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f].
compute_mask_to_parent(index, mask)
compute_message_to_parent(parent, index, u, ...)
                                                       Compute a message to a parent.
compute_moments_and_cgf(phi[, mask])
                                                       Compute the moments and the cumulant-generating function.
compute_phi_from_parents(u_mu, u_Lambda, ...)
                                                       Compute the natural parameters using parents' moments.
plates_from_parent(index, plates)
                                                       Compute the plates using information of a parent node.
plates to parent(index, plates)
                                                       Computes the plates of this node with respect to a parent.
random(*params[, plates])
                                                       Draw a random sample from the distribution.
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.SwitchingGaussianMarkovChainDistribution.__init_

```
SwitchingGaussianMarkovChainDistribution. \_ init\_ (N, D, K)
```

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Switching Gaussian Markov Chain Distribution. compute the property of the property o$

```
SwitchingGaussianMarkovChainDistribution.compute_cgf_from_parents(u\_mu, u\_Lambda, u\_B, u\_Z, u\_v)
```

Compute CGF using the moments of the parents.

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Switching Gaussian Markov Chain Distribution. compute the property of the property o$

```
\label{lem:compute_fixed_moments_and_f} Switching \textit{Gaussian} \textit{MarkovChainDistribution.} \textbf{compute\_fixed\_moments\_and\_f} \ (x, \\ \textit{mask=True}) \\ Compute \ \textit{u}(x) \ \text{and} \ \textit{f}(x) \ \text{for given } x.
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.SwitchingGaussianMarkovChainDistribution.compute

```
SwitchingGaussianMarkovChainDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Switching Gaussian Markov Chain Distribution. compute the property of the property o$

```
SwitchingGaussianMarkovChainDistribution.compute_mask_to_parent (index, mask)
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.SwitchingGaussianMarkovChainDistribution.compute

Compute a message to a parent.

bayespy.inference.vmp.nodes.gaussian_markov_chain.SwitchingGaussianMarkovChainDistribution.compute

```
SwitchingGaussianMarkovChainDistribution.compute_moments_and_cgf (phi, mask=True)

Compute the moments and the cumulant-generating function.
```

This basically performs the filtering and smoothing for the variable.

```
Parameters phi
Returns u
```

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Switching Gaussian Markov Chain Distribution. compute the property of the property o$

```
SwitchingGaussianMarkovChainDistribution.compute_phi_from_parents (u\_mu, u\_Lambda, u\_B, u\_Z, u\_v, mask=True)
```

Compute the natural parameters using parents' moments.

```
Parameters u_parents: list of list of arrays

List of parents' lists of moments.

Returns phi: list of arrays

Natural parameters.

dims: tuple
```

Shape of the variable part of phi.

$bayes py. in ference. vmp. nodes. gaussian_markov_chain. Switching Gaussian Markov Chain Distribution. plates_fine the contraction of the contra$

```
SwitchingGaussianMarkovChainDistribution.plates_from_parent (index, plates)
Compute the plates using information of a parent node.

If the plates of the parents are: mu: (...) Lambda: (...) B: (...,D) S: (...,N-1) v: (...,N-1,D) N: ()
the resulting plates of this node are (...)

Parameters index: int
```

Index of the parent to use.

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Switching Gaussian Markov Chain Distribution. plates_tolerance and the property of t$

```
SwitchingGaussianMarkovChainDistribution.plates_to_parent (index, plates)

Computes the plates of this node with respect to a parent.
```

If this node has plates (...), the latent dimensionality is D and the number of time instances is N, the plates with respect to the parents are:

```
mu: (...) Lambda: (...) A: (...,N-1,D) v: (...,N-1,D)
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.SwitchingGaussianMarkovChainDistribution.random

SwitchingGaussianMarkovChainDistribution.random(*params, plates=None)

Draw a random sample from the distribution.

6.3.10 bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDis

 ${\bf class} \ {\tt bayespy.inference.vmp.nodes.gaussian_markov_chain.Varying Gaussian Markov Chain Distribution of the contraction of the contractio$

Sub-classes implement distribution specific computations.

```
__init__(N, D)
```

Methods

init (N, D)	
compute_cgf_from_parents(u_mu, u_Lambda,)	Compute CGF using the moments of the parents.
compute_fixed_moments_and_f(x[, mask])	Compute $u(x)$ and $f(x)$ for given x.
compute_logpdf(u, phi, g, f, ndims)	Compute $E[log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	
<pre>compute_message_to_parent(parent, index, u,)</pre>	Compute a message to a parent.
compute_moments_and_cgf(phi[, mask])	Compute the moments and the cumulant-generating function.
compute_phi_from_parents(u_mu, u_Lambda,)	Compute the natural parameters using parents' moments.
<pre>plates_from_parent(index, plates)</pre>	Compute the plates using information of a parent node.
<pre>plates_to_parent(index, plates)</pre>	Computes the plates of this node with respect to a parent.
random(*params[, plates])	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.__init__

```
VaryingGaussianMarkovChainDistribution.\_init\_(N, D)
```

bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.compute_c

```
\label{lem:compute_cgf_from_parents} Varying \textit{Gaussian} \textit{MarkovChainDistribution.} \textbf{compute\_cgf\_from\_parents} (u\_mu, \\ u\_Lambda, \\ u\_B, u\_S, \\ u\_v) Compute CGF using the moments of the parents.
```

```
mask=True)
    Compute u(x) and f(x) for given x.
bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.compute_le
VaryingGaussianMarkovChainDistribution.compute_logpdf(u, phi, g, f, ndims)
    Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.compute_r
VaryingGaussianMarkovChainDistribution.compute_mask_to_parent(index,
bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.compute_n
VaryingGaussianMarkovChainDistribution.compute_message_to_parent(parent,
                                                                              dex, u,
                                                                              u mu,
                                                                              u_Lambda,
                                                                              u\_B,
                                                                              u\_S,
                                                                              u_v)
    Compute a message to a parent.
bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.compute_r
VaryingGaussianMarkovChainDistribution.compute_moments_and_cgf (phi,
                                                                           mask=True)
    Compute the moments and the cumulant-generating function.
    This basically performs the filtering and smoothing for the variable.
        Parameters phi
        Returns u
           g
bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.compute_p
VaryingGaussianMarkovChainDistribution.compute_phi_from_parents(u_mu,
                                                                             u_Lambda,
                                                                             u\_B.
                                                                             u_S, u_v,
                                                                             mask=True)
    Compute the natural parameters using parents' moments.
```

bayespy.inference.vmp.nodes.gaussian markov chain.VaryingGaussianMarkovChainDistribution.compute f

VaryingGaussianMarkovChainDistribution.compute_fixed_moments_and_f(x,

Parameters u_parents: list of list of arrays

List of parents' lists of moments.

```
Returns phi: list of arrays
```

Natural parameters.

dims: tuple

Shape of the variable part of phi.

bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.plates_from

```
VaryingGaussianMarkovChainDistribution.plates_from_parent (index, plates)

Compute the plates using information of a parent node.
```

```
If the plates of the parents are: mu: (...) Lambda: (...) B: (...,D) S: (...,N-1) v: (...,N-1,D) N: ()
```

the resulting plates of this node are (...)

Parameters index: int

Index of the parent to use.

bayespy.inference.vmp.nodes.gaussian_markov_chain.VaryingGaussianMarkovChainDistribution.plates_to_i

```
VaryingGaussianMarkovChainDistribution.plates_to_parent(index, plates)
```

Computes the plates of this node with respect to a parent.

If this node has plates (...), the latent dimensionality is D and the number of time instances is N, the plates with respect to the parents are:

```
mu: (...) Lambda: (...) A: (...,N-1,D) v: (...,N-1,D)
```

$bayes py. inference. vmp. nodes. gaussian_markov_chain. Varying Gaussian Markov Chain Distribution. random the property of t$

```
VaryingGaussianMarkovChainDistribution.random(*params, plates=None)

Draw a random sample from the distribution.
```

6.3.11 bayespy.inference.vmp.nodes.gamma.GammaDistribution

```
class bayespy.inference.vmp.nodes.gamma.GammaDistribution
    Class for the VMP formulas of gamma variables.
```

```
__init__()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

```
compute_cgf_from_parents(*u_parents)
                                                    Compute E_{q(p)}[g(p)]
compute fixed moments and f(x[, mask])
                                                    Compute the moments and f(x) for a fixed value.
                                                    Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f].
compute_logpdf(u, phi, g, f, ndims)
                                                    Maps the mask to the plates of a parent.
compute_mask_to_parent(index, mask)
compute_message_to_parent(parent, index, ...)
                                                    Compute the message to a parent node.
compute_moments_and_cgf(phi[, mask])
                                                    Compute the moments and g(\phi).
compute_phi_from_parents(*u_parents[, mask])
                                                    Compute the natural parameter vector given parent moments.
                                                    Resolve the plate mapping from a parent.
plates_from_parent(index, plates)
                                                                                   Continued on next page
```

Table 6.53 – continued from previous page

<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
<pre>random(*phi[, plates])</pre>	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.gamma.GammaDistribution.compute_cgf_from_parents

```
GammaDistribution.compute_cgf_from_parents (*u_parents) Compute \mathrm{E}_{q(p)}[g(p)]
```

bayespy.inference.vmp.nodes.gamma.GammaDistribution.compute fixed moments and f

```
GammaDistribution.compute_fixed_moments_and_f (x, mask=True)
Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.gamma.GammaDistribution.compute logpdf

```
GammaDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.gamma.GammaDistribution.compute_mask_to_parent

```
GammaDistribution.compute_mask_to_parent(index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.gamma.GammaDistribution.compute_message_to_parent

```
GammaDistribution.compute_message_to_parent (parent, index, u_self, *u_parents)

Compute the message to a parent node.
```

bayespy.inference.vmp.nodes.gamma.GammaDistribution.compute moments and cgf

```
GammaDistribution.compute_moments_and_cgf (phi, mask=True)

Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.gamma.GammaDistribution.compute phi from parents

```
GammaDistribution.compute_phi_from_parents (*u_parents, mask=True)

Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.gamma.GammaDistribution.plates from parent

```
GammaDistribution.plates_from_parent (index, plates)
Resolve the plate mapping from a parent.
```

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.gamma.GammaDistribution.plates_to_parent

```
GammaDistribution.plates_to_parent (index, plates)
```

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.gamma.GammaDistribution.random

```
{\tt GammaDistribution.random\,(*phi,plates=None)}
```

Draw a random sample from the distribution.

6.3.12 bayespy.inference.vmp.nodes.wishart.WishartDistribution

```
class bayespy.inference.vmp.nodes.wishart.WishartDistribution
    Sub-classes implement distribution specific computations.
```

```
___init___()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

<pre>compute_cgf_from_parents(*u_parents)</pre>	
<pre>compute_fixed_moments_and_f(Lambda[, mask])</pre>	Compute $u(x)$ and $f(x)$ for given x.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index,)</pre>	
<pre>compute_moments_and_cgf(phi[, mask])</pre>	
<pre>compute_phi_from_parents(*u_parents[, mask])</pre>	
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*params[, plates])	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.wishart.WishartDistribution.compute cgf from parents

```
WishartDistribution.compute_cgf_from_parents(*u_parents)
```

bayespy.inference.vmp.nodes.wishart.WishartDistribution.compute fixed moments and f

```
WishartDistribution.compute_fixed_moments_and_f (Lambda, mask=True)
Compute u(x) and f(x) for given x.
```

bayespy.inference.vmp.nodes.wishart.WishartDistribution.compute_logpdf

```
WishartDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.wishart.WishartDistribution.compute_mask_to_parent

WishartDistribution.compute_mask_to_parent(index, mask)

Maps the mask to the plates of a parent.

bayespy.inference.vmp.nodes.wishart.WishartDistribution.compute message to parent

WishartDistribution.compute_message_to_parent(parent, index, u_self, *u_parents)

bayespy.inference.vmp.nodes.wishart.WishartDistribution.compute moments and cgf

WishartDistribution.compute_moments_and_cqf(phi, mask=True)

bayespy.inference.vmp.nodes.wishart.WishartDistribution.compute_phi_from_parents

WishartDistribution.compute_phi_from_parents(*u_parents, mask=True)

bayespy.inference.vmp.nodes.wishart.WishartDistribution.plates_from_parent

WishartDistribution.plates_from_parent (index, plates)

Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.wishart.WishartDistribution.plates_to_parent

```
WishartDistribution.plates_to_parent (index, plates)
```

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.wishart.WishartDistribution.random

```
WishartDistribution.random(*params, plates=None)
Draw a random sample from the distribution.
```

6.3.13 bayespy.inference.vmp.nodes.beta.BetaDistribution

class bayespy.inference.vmp.nodes.beta.BetaDistribution
 Class for the VMP formulas of beta variables.

Although the realizations are scalars (probability p), the moments is a two-dimensional vector: [log(p), log(1-p)].

```
___init___()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

```
Compute E_{q(p)}[g(p)]
compute_cgf_from_parents(u_alpha)
                                                   Compute the moments and f(x) for a fixed value.
compute_fixed_moments_and_f(p[, mask])
compute_logpdf(u, phi, g, f, ndims)
                                                   Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f].
                                                   Maps the mask to the plates of a parent.
compute_mask_to_parent(index, mask)
compute_message_to_parent(parent, index, ...)
                                                   Compute the message to a parent node.
compute_moments_and_cgf(phi[, mask])
                                                   Compute the moments and q(\phi).
compute_phi_from_parents(u_alpha[, mask])
                                                   Compute the natural parameter vector given parent moments.
plates_from_parent(index, plates)
                                                   Resolve the plate mapping from a parent.
plates_to_parent(index, plates)
                                                   Resolves the plate mapping to a parent.
                                                   Draw a random sample from the distribution.
random(*phi[, plates])
```

bayespy.inference.vmp.nodes.beta.BetaDistribution.compute_cgf_from_parents

```
BetaDistribution.compute_cgf_from_parents (u\_alpha) Compute \mathbf{E}_{q(p)}[g(p)]
```

bayespy.inference.vmp.nodes.beta.BetaDistribution.compute_fixed_moments_and_f

```
BetaDistribution.compute_fixed_moments_and_f (p, mask=True)
Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.beta.BetaDistribution.compute logpdf

```
BetaDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.beta.BetaDistribution.compute mask to parent

```
BetaDistribution.compute_mask_to_parent(index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.beta.BetaDistribution.compute message to parent

```
BetaDistribution.compute_message_to_parent (parent, index, u_self, u_alpha) Compute the message to a parent node.
```

bayespy.inference.vmp.nodes.beta.BetaDistribution.compute moments and cgf

```
BetaDistribution.compute_moments_and_cgf (phi, mask=True)
Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.beta.BetaDistribution.compute phi from parents

```
BetaDistribution.compute_phi_from_parents (u_alpha, mask=True)
Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.beta.BetaDistribution.plates_from_parent

```
BetaDistribution.plates_from_parent (index, plates)
```

Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.beta.BetaDistribution.plates_to_parent

```
BetaDistribution.plates_to_parent(index, plates)
```

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.beta.BetaDistribution.random

```
BetaDistribution.random(*phi, plates=None)
```

Draw a random sample from the distribution.

6.3.14 bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution

```
class bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution
    Class for the VMP formulas of Dirichlet variables.
```

```
init ()
```

Initialize self. See help(type(self)) for accurate signature.

Methods

compute_cgf_from_parents(u_alpha)	Compute $E_{q(p)}[g(p)]$
$compute_fixed_moments_and_f(x[, mask])$	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index,)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_alpha[, mask])</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*phi[, plates])	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.compute_cgf_from_parents

```
\label{eq:compute_cgf_from_parents} \begin{tabular}{ll} $\operatorname{Compute} \to \operatorname{Compute} (u\_alpha)$ \\ &\operatorname{Compute} \to \operatorname{E}_{q(p)}[g(p)] \end{tabular}
```

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.compute fixed moments and f

```
DirichletDistribution.compute_fixed_moments_and_f(x, mask=True)
    Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.compute logpdf

```
DirichletDistribution.compute_logpdf(u, phi, g, f, ndims)
     Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.compute mask to parent

```
DirichletDistribution.compute_mask_to_parent(index, mask)
    Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.compute_message_to_parent

```
DirichletDistribution.compute_message_to_parent (parent, index, u_self, u_alpha)
    Compute the message to a parent node.
```

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.compute moments and cgf

```
DirichletDistribution.compute_moments_and_cgf(phi, mask=True)
    Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.compute_phi_from_parents

```
DirichletDistribution.compute_phi_from_parents(u_alpha, mask=True)
    Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.plates_from_parent

```
DirichletDistribution.plates_from_parent (index, plates)
    Resolve the plate mapping from a parent.
```

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.plates to parent

```
DirichletDistribution.plates_to_parent (index, plates)
```

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.dirichlet.DirichletDistribution.random

```
DirichletDistribution.random(*phi, plates=None)
    Draw a random sample from the distribution.
```

6.3.15 bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution

```
{\bf class} \ {\tt bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution} \\ {\bf Class} \ {\tt for} \ {\tt the} \ {\tt VMP} \ {\tt formulas} \ {\tt of} \ {\tt Bernoulli} \ {\tt variables}.
```

```
___init___()
```

Methods

init()	
<pre>compute_cgf_from_parents(u_p)</pre>	Compute $E_{q(p)}[g(p)]$
$compute_fixed_moments_and_f(x[, mask])$	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index,)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_p[, mask])</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*phi)	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution. init

```
BernoulliDistribution.__init__()
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.compute_cgf_from_parents

```
BernoulliDistribution.compute_cgf_from_parents (u\_p) Compute \mathbf{E}_{a(p)}[g(p)]
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.compute fixed moments and f

```
BernoulliDistribution.compute_fixed_moments_and_f (x, mask=True)
Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.compute logpdf

```
BernoulliDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.compute_mask_to_parent

```
BernoulliDistribution.compute_mask_to_parent(index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.compute message to parent

```
BernoulliDistribution.compute_message_to_parent (parent, index, u_self, u_p) Compute the message to a parent node.
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.compute_moments_and_cgf

```
BernoulliDistribution.compute_moments_and_cgf (phi, mask=True)

Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.compute_phi_from_parents

```
BernoulliDistribution.compute_phi_from_parents (u_p, mask=True)

Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.plates_from_parent

```
BernoulliDistribution.plates_from_parent (index, plates)
```

Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.plates_to_parent

```
BernoulliDistribution.plates_to_parent (index, plates)
```

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.bernoulli.BernoulliDistribution.random

```
BernoulliDistribution.random(*phi)
```

Draw a random sample from the distribution.

6.3.16 bayespy.inference.vmp.nodes.binomial.BinomialDistribution

```
class bayespy.inference.vmp.nodes.binomial.BinomialDistribution (N) Class for the VMP formulas of binomial variables.
```

```
init (N)
```

Methods

init(N)	
$compute_cgf_from_parents(u_p)$	Compute $E_{q(p)}[g(p)]$
$compute_fixed_moments_and_f(x[, mask])$	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index,)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_p[, mask])</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
	Continued on next page

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plates_to_parent(index, plates)	Resolves the plate mapping to a parent.
random(*phi)	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.__init__

```
BinomialDistribution.__init__(N)
```

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.compute_cgf_from_parents

```
BinomialDistribution.compute_cgf_from_parents (u\_p)
Compute \mathrm{E}_{q(p)}[g(p)]
```

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.compute_fixed_moments_and_f

```
BinomialDistribution.compute_fixed_moments_and_f (x, mask=True)
Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.compute_logpdf

```
BinomialDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.compute_mask_to_parent

```
BinomialDistribution.compute_mask_to_parent (index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.compute message to parent

```
BinomialDistribution.compute_message_to_parent (parent, index, u\_self, u\_p)

Compute the message to a parent node.
```

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.compute moments and cgf

```
BinomialDistribution.compute_moments_and_cgf (phi, mask=True)

Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.compute phi from parents

```
BinomialDistribution.compute_phi_from_parents (u_p, mask=True)

Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.plates_from_parent

```
BinomialDistribution.plates_from_parent (index, plates)
```

Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.plates to parent

```
BinomialDistribution.plates_to_parent(index, plates)
```

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.binomial.BinomialDistribution.random

```
BinomialDistribution.random(*phi)
```

Draw a random sample from the distribution.

6.3.17 bayespy.inference.vmp.nodes.categorical.CategoricalDistribution

```
__init__(categories)
```

Create VMP formula node for a categorical variable

categories is the total number of categories.

Methods

init(categories)	Create VMP formula node for a categorical variable
compute_cgf_from_parents(u_p)	Compute $E_{q(p)}[g(p)]$
$compute_fixed_moments_and_f(x[, mask])$	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index, u, u_p)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_p[, mask])</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*phi[, plates])	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution. init

```
CategoricalDistribution.__init__(categories)
```

Create VMP formula node for a categorical variable

categories is the total number of categories.

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.compute_cgf_from_parents

```
CategoricalDistribution.compute_cgf_from_parents (u\_p) Compute \mathbf{E}_{q(p)}[g(p)]
```

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.compute fixed moments and f

```
CategoricalDistribution.compute_fixed_moments_and_f (x, mask=True)
Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.compute_logpdf

```
CategoricalDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.compute_mask_to_parent

```
CategoricalDistribution.compute_mask_to_parent(index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.compute message to parent

```
CategoricalDistribution.compute_message_to_parent (parent, index, u, u_p)

Compute the message to a parent node.
```

$bayes py. inference. vmp. nodes. categorical. Categorical Distribution. compute_moments_and_cgf$

```
CategoricalDistribution.compute_moments_and_cgf (phi, mask=True) Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.compute phi from parents

```
CategoricalDistribution.compute_phi_from_parents (u_p, mask=True)
Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.plates from parent

```
CategoricalDistribution.plates_from_parent (index, plates)
Resolve the plate mapping from a parent.
```

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.plates_to_parent

```
CategoricalDistribution.plates_to_parent (index, plates)
Resolves the plate mapping to a parent.
```

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.categorical.CategoricalDistribution.random

CategoricalDistribution.random(*phi, plates=None)
Draw a random sample from the distribution.

6.3.18 bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainDistrik

 ${\bf class} \; {\tt bayespy.inference.vmp.nodes.categorical_markov_chain. \textbf{CategoricalMarkovChainDistribution} \\$

Class for the VMP formulas of categorical Markov chain variables.

___init___(categories, states)

Create VMP formula node for a categorical variable

categories is the total number of categories. states is the length of the chain.

Methods

init(categories, states)	Create VMP formula node for a categorical variable
$ exttt{compute_cgf_from_parents}(u_p0,u_P)$	Compute $E_{q(p)}[g(p)]$
<pre>compute_fixed_moments_and_f(x[, mask])</pre>	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index, u,)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_p0, u_P[, mask])</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*phi[, plates])	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainDistribution.__init__

```
CategoricalMarkovChainDistribution.__init__(categories, states)

Create VMP formula node for a categorical variable
```

categories is the total number of categories. states is the length of the chain.

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainDistribution.compute_cgf_

bayespy.inference.vmp.nodes.categorical markov chain.CategoricalMarkovChainDistribution.compute fixed

```
\label{lem:compute_fixed_moments_and_f} \textbf{CategoricalMarkovChainDistribution.compute\_fixed\_moments\_and\_f} \ (x, \\ mask=True)
```

Compute the moments and f(x) for a fixed value.

bayespy.inference.vmp.nodes.categorical markov chain.CategoricalMarkovChainDistribution.compute logp

```
CategoricalMarkovChainDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[\log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainDistribution.compute_mas

```
CategoricalMarkovChainDistribution.compute_mask_to_parent (index, mask)

Maps the mask to the plates of a parent.
```

$bayes py. inference. vmp. nodes. categorical_markov_chain. Categorical Markov Chain Distribution. compute_mession and the property of the pr$

```
CategoricalMarkovChainDistribution.compute_message_to_parent (parent, index, u, u\_p0, u\_P)
```

Compute the message to a parent node.

$bayes py. inference. vmp. nodes. categorical_markov_chain. Categorical Markov Chain Distribution. compute_moments and the property of the compute for the property of the pr$

```
\label{lem:compute_moments_and_cgf} \mbox{CategoricalMarkovChainDistribution.} \mbox{compute\_moments\_and\_cgf} \ (phi, \\ mask=True) \mbox{Compute the moments and} \ g(\phi).
```

$bayes py. inference. vmp. nodes. categorical_markov_chain. Categorical Markov Chain Distribution. compute_phi_inference. vmp. nodes. categorical Markov Chain Distribution. categorical Markov$

```
\label{lem:compute_phi_from_parents} \begin{tabular}{ll} $(u\_p0, & u\_P, \\ & mask=True) \end{tabular} Compute the natural parameter vector given parent moments.
```

$bayes py. inference. vmp. nodes. categorical_markov_chain. Categorical Markov Chain Distribution. plates_from_parkov_chain. Categorical Markov Chain Distribution. Categorical Markov Chain Distributi$

```
CategoricalMarkovChainDistribution.plates_from_parent (index, plates)
Resolve the plate mapping from a parent.
```

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainDistribution.plates_to_pare

```
CategoricalMarkovChainDistribution.plates_to_parent (index, plates)
Resolves the plate mapping to a parent.
```

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.categorical_markov_chain.CategoricalMarkovChainDistribution.random

```
CategoricalMarkovChainDistribution.random(*phi, plates=None)
Draw a random sample from the distribution.
```

6.3.19 bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution

__init__(trials)

Create VMP formula node for a multinomial variable

trials is the total number of trials.

Methods

init(trials)	Create VMP formula node for a multinomial variable
compute_cgf_from_parents(u_p)	Compute $E_{q(p)}[g(p)]$
<pre>compute_fixed_moments_and_f(x[, mask])</pre>	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
<pre>compute_mask_to_parent(index, mask)</pre>	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index, u, u_p)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_p[, mask])</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*phi)	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.__init_

```
MultinomialDistribution.__init__(trials)
```

Create VMP formula node for a multinomial variable

trials is the total number of trials.

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.compute cgf from parents

```
MultinomialDistribution.compute_cgf_from_parents (u_p) Compute \mathrm{E}_{q(p)}[g(p)]
```

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.compute fixed moments and f

```
MultinomialDistribution.compute_fixed_moments_and_f (x, mask=True) Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.compute_logpdf

```
MultinomialDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.compute_mask_to_parent

```
MultinomialDistribution.compute_mask_to_parent (index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.compute_message_to_parent

```
MultinomialDistribution.compute_message_to_parent (parent, index, u, u_p) Compute the message to a parent node.
```

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.compute_moments_and_cgf

```
MultinomialDistribution.compute_moments_and_cgf (phi, mask=True)

Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.compute_phi_from_parents

```
MultinomialDistribution.compute_phi_from_parents (u_p, mask=True) Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.plates_from_parent

```
MultinomialDistribution.plates_from_parent (index, plates)
Resolve the plate mapping from a parent.
```

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

$bayes py. inference. vmp. nodes. multinomial. Multinomial Distribution. plates_to_parent$

```
MultinomialDistribution.plates_to_parent (index, plates)
Resolves the plate mapping to a parent.
```

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.multinomial.MultinomialDistribution.random

```
MultinomialDistribution.random(*phi)

Draw a random sample from the distribution.
```

6.3.20 bayespy.inference.vmp.nodes.poisson.PoissonDistribution

Methods

compute_cgf_from_parents(u_lambda)	Compute $E_{q(p)}[g(p)]$
<pre>compute_fixed_moments_and_f(x[, mask])</pre>	Compute the moments and $f(x)$ for a fixed value.
<pre>compute_logpdf(u, phi, g, f, ndims)</pre>	Compute $E[\log p(X)]$ given $E[u]$, $E[phi]$, $E[g]$ and $E[f]$.
	Continued on next page

Table 6.62 – continued from previous page

compute_mask_to_parent(index, mask)	Maps the mask to the plates of a parent.
<pre>compute_message_to_parent(parent, index, u,)</pre>	Compute the message to a parent node.
<pre>compute_moments_and_cgf(phi[, mask])</pre>	Compute the moments and $g(\phi)$.
<pre>compute_phi_from_parents(u_lambda[, mask])</pre>	Compute the natural parameter vector given parent moments.
<pre>plates_from_parent(index, plates)</pre>	Resolve the plate mapping from a parent.
<pre>plates_to_parent(index, plates)</pre>	Resolves the plate mapping to a parent.
random(*phi)	Draw a random sample from the distribution.

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.compute_cgf_from_parents

```
PoissonDistribution.compute_cgf_from_parents (u\_lambda) Compute \mathbf{E}_{q(p)}[g(p)]
```

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.compute_fixed_moments_and_f

```
PoissonDistribution.compute_fixed_moments_and_f(x, mask=True)
Compute the moments and f(x) for a fixed value.
```

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.compute logpdf

```
PoissonDistribution.compute_logpdf (u, phi, g, f, ndims)
Compute E[log p(X)] given E[u], E[phi], E[g] and E[f]. Does not sum over plates.
```

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.compute mask to parent

```
PoissonDistribution.compute_mask_to_parent(index, mask)

Maps the mask to the plates of a parent.
```

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.compute_message_to_parent

PoissonDistribution.compute_message_to_parent (parent, index, u, u_lambda) Compute the message to a parent node.

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.compute moments and cgf

```
PoissonDistribution.compute_moments_and_cgf (phi, mask=True)
Compute the moments and g(\phi).
```

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.compute phi from parents

```
PoissonDistribution.compute_phi_from_parents(u_lambda, mask=True)
Compute the natural parameter vector given parent moments.
```

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.plates_from_parent

PoissonDistribution.plates_from_parent (index, plates)

Resolve the plate mapping from a parent.

Given the plates of a parent's moments, this method returns the plates that the moments has for this distribution.

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.plates_to_parent

```
PoissonDistribution.plates_to_parent (index, plates)
```

Resolves the plate mapping to a parent.

Given the plates of the node's moments, this method returns the plates that the message to a parent has for the parent's distribution.

bayespy.inference.vmp.nodes.poisson.PoissonDistribution.random

PoissonDistribution.random(*phi)

Draw a random sample from the distribution.

6.4 Utility functions

linalg	General numerical functions and methods.
random	General functions random sampling and distributions.
optimize	
misc	General numerical functions and methods.

6.4.1 bayespy.utils.linalg

General numerical functions and methods.

Functions

block_banded_solve(A, B, y)	Invert symmetric, banded, positive-definite matrix.
chol(C)	
${ t chol_inv}({ t U})$	
${ t chol_logdet}({ t U})$	
$chol_solve(U, b[, out, matrix])$	
dot(*arrays)	Compute matrix-matrix product.
<pre>inner(*args[, ndim])</pre>	Compute inner product.
inv(A[, ndim])	General array inversion.
$logdet_chol(U)$	
logdet_cov(C)	
$logdet_tri(R)$	Logarithm of the absolute value of the determinant of a triangular matrix.
$m_dot(A,b)$	
$\operatorname{mmdot}(A,B)$	Compute matrix-matrix product.
mvdot(A, b)	Compute matrix-vector product.
	Continued on next page

6.4. Utility functions

Table 6.64 – continued from previous page

outer(A, B[, ndim])	Computes outer product over the last axes of A and B.
<pre>solve_triangular(U, B, **kwargs)</pre>	
tracedot(A,B)	Computes trace(A*B).

bayespy.utils.linalg.block_banded_solve

```
bayespy.utils.linalg.block_banded_solve (A, B, y)
```

Invert symmetric, banded, positive-definite matrix.

A contains the diagonal blocks.

B contains the superdiagonal blocks (their transposes are the subdiagonal blocks).

Shapes: A: (..., N, D, D) B: (..., N-1, D, D) y: (..., N, D)

The algorithm is basically LU decomposition.

Computes only the diagonal and super-diagonal blocks of the inverse. The true inverse is dense, in general.

Assume each block has the same size.

Return: * inverse blocks * solution to the system * log-determinant

bayespy.utils.linalg.chol

```
bayespy.utils.linalg.chol(C)
```

bayespy.utils.linalg.chol_inv

```
bayespy.utils.linalg.chol_inv(U)
```

bayespy.utils.linalg.chol_logdet

```
bayespy.utils.linalg.chol_logdet(U)
```

bayespy.utils.linalg.chol_solve

```
bayespy.utils.linalg.chol_solve(U, b, out=None, matrix=False)
```

bayespy.utils.linalg.dot

```
bayespy.utils.linalg.dot(*arrays)
```

Compute matrix-matrix product.

You can give multiple arrays, the dot product is computed from left to right: A1*A2*A3*...*AN. The dot product is computed over the last two axes of each arrays. All other axes must be broadcastable.

bayespy.utils.linalg.inner

```
bayespy.utils.linalg.inner(*args, ndim=1)
```

Compute inner product.

The number of arrays is arbitrary. The number of dimensions is arbitrary.

bayespy.utils.linalg.inv

```
bayespy.utils.linalg.inv(A, ndim=1)
General array inversion.
```

Supports broadcasting and inversion of multidimensional arrays. For instance, an array with shape (4,3,2,3,2) could mean that there are four (3*2) x (3*2) matrices to be inverted. This can be done by inv(A, ndim=2). For inverting scalars, ndim=0. For inverting matrices, ndim=1.

bayespy.utils.linalg.logdet_chol

```
bayespy.utils.linalg.logdet_chol(U)
```

bayespy.utils.linalg.logdet cov

```
bayespy.utils.linalg.logdet_cov(C)
```

bayespy.utils.linalg.logdet_tri

```
bayespy.utils.linalg.logdet_tri(R)
```

Logarithm of the absolute value of the determinant of a triangular matrix.

bayespy.utils.linalg.m_dot

```
bayespy.utils.linalg.m_dot(A, b)
```

bayespy.utils.linalg.mmdot

```
bayespy.utils.linalg.mmdot (A, B)
Compute matrix-matrix product.
```

Applies broadcasting.

bayespy.utils.linalg.mvdot

```
\verb|bayespy.utils.linalg.mvdot|(A,b)|
```

Compute matrix-vector product.

Applies broadcasting.

bayespy.utils.linalg.outer

```
bayespy.utils.linalg.outer(A, B, ndim=1)
```

Computes outer product over the last axes of A and B.

The other axes are broadcasted. Thus, if A has shape (..., N) and B has shape (..., M), then the result has shape (..., N, M).

Using the argument *ndim* it is possible to change that how many axes trailing axes are used for the outer product. For instance, if ndim=3, A and B have shapes (...,N1,N2,N3) and (...,M1,M2,M3), the result has shape (...,N1,M1,N2,M2,N3,M3).

bayespy.utils.linalg.solve_triangular

```
bayespy.utils.linalg.solve_triangular(U, B, **kwargs)
```

bayespy.utils.linalg.tracedot

```
bayespy.utils.linalg.tracedot (A, B)
Computes trace(A*B).
```

6.4.2 bayespy.utils.random

General functions random sampling and distributions.

Functions

alpha_beta_recursion(logp0, logP)	Compute alpha-beta recursion for Markov chain
bernoulli(p[, size])	Draw random samples from the Bernoulli distribution.
<pre>categorical(p[, size])</pre>	Draw random samples from a categorical distribution.
correlation(D)	Draw a random correlation matrix.
covariance(D[, size])	Draw a random covariance matrix.
dirichlet(alpha[, size])	Draw random samples from the Dirichlet distribution.
gamma_entropy(a, log_b, gammaln_a, psi_a,)	Entropy of $\mathcal{G}(a,b)$.
<pre>gamma_logpdf(bx, logx, a_logx, a_logb, gammaln_a)</pre>	Log-density of $\mathcal{G}(x a,b)$.
<pre>gaussian_entropy(logdet_V, D)</pre>	Compute the entropy of a Gaussian distribution.
<pre>gaussian_gamma_to_t(mu, Cov, a, b[, ndim])</pre>	Integrates gamma distribution to obtain parameters of t distribution
<pre>gaussian_logpdf(yVy, yVmu, muVmu, logdet_V, D)</pre>	Log-density of a Gaussian distribution.
<pre>intervals(N, length[, amount, gap])</pre>	Return random non-overlapping parts of a sequence.
$invwishart_rand(nu, V)$	
mask(*shape[, p])	Return a boolean array of the given shape.
orth(D)	Draw random orthogonal matrix.
sphere([N])	Draw random points uniformly on a unit sphere.
svd(s)	Draw a random matrix given its singular values.
t_logpdf(z2, logdet_cov, nu, D)	
wishart_rand (nu, V)	Draw a random sample from the Wishart distribution.

bayespy.utils.random.alpha_beta_recursion

```
bayespy.utils.random.alpha_beta_recursion(logp0, logP)
```

Compute alpha-beta recursion for Markov chain

Initial state log-probabilities are in p0 and state transition log-probabilities are in P. The probabilities do not need to be scaled to sum to one, but they are interpreted as below:

```
logp0 = log P(z_0) + log P(y_0|z_0) logP[...,n,;;] = log P(z_{n+1}|z_n) + log P(y_{n+1}|z_n+1)
```

bayespy.utils.random.bernoulli

```
bayespy.utils.random.bernoulli (p, size=None)

Draw random samples from the Bernoulli distribution.
```

bayespy.utils.random.categorical

```
bayespy.utils.random.categorical(p, size=None)

Draw random samples from a categorical distribution.
```

bayespy.utils.random.correlation

```
bayespy.utils.random.correlation(D)

Draw a random correlation matrix.
```

bayespy.utils.random.covariance

```
\verb|bayespy.utils.random.covariance|(D, size=())|
```

Draw a random covariance matrix.

Draws from inverse-Wishart distribution. The distribution of each element is independent of the dimensionality of the matrix.

```
C \sim Inv-W(I, D)
```

Parameters D: int

Dimensionality of the covariance matrix.

bayespy.utils.random.dirichlet

```
bayespy.utils.random.dirichlet (alpha, size=None)
Draw random samples from the Dirichlet distribution.
```

bayespy.utils.random.gamma_entropy

```
bayespy.utils.random.gamma_entropy (a, log\_b, gammaln\_a, psi\_a, a\_psi\_a)
Entropy of \mathcal{G}(a, b).
```

If you want to get the gradient, just let each parameter be a gradient of that term.

```
Parameters \mathbf{a}: ndarray a \log_{\mathbf{b}}: ndarray
```

gammaln_a : ndarray

 $\log \Gamma(a)$

 $\log(b)$

psi_a : ndarray

 $\psi(a)$

a_psi_a : ndarray

 $a\psi(a)$

bayespy.utils.random.gamma_logpdf

```
bayespy.utils.random.gamma_logpdf(bx, logx, a_logx, a_logb, gammaln_a)
      Log-density of \mathcal{G}(x|a,b).
      If you want to get the gradient, just let each parameter be a gradient of that term.
           Parameters bx: ndarray
                    bx
                logx: ndarray
                    \log(x)
                a_logx: ndarray
                    a \log(x)
                a_logb: ndarray
                    a \log(b)
                gammaln_a: ndarray
                    \log \Gamma(a)
bayespy.utils.random.gaussian entropy
bayespy.utils.random.gaussian_entropy(logdet_V, D)
      Compute the entropy of a Gaussian distribution.
      If you want to get the gradient, just let each parameter be a gradient of that term.
           Parameters logdet_V: ndarray or double
                    The log-determinant of the precision matrix.
                D: int
                    The dimensionality of the distribution.
bayespy.utils.random.gaussian gamma to t
bayespy.utils.random.gaussian_gamma_to_t (mu, Cov, a, b, ndim=1)
      Integrates gamma distribution to obtain parameters of t distribution
bayespy.utils.random.gaussian logpdf
bayespy.utils.random.gaussian_logpdf(yVy, yVmu, muVmu, logdet_V, D)
      Log-density of a Gaussian distribution.
      \mathcal{G}(\mathbf{y}|\boldsymbol{\mu}, \mathbf{V}^{-1})
           Parameters yVy: ndarray or double
                    \mathbf{y}^T \mathbf{V} \mathbf{y}
                yVmu: ndarray or double
                    \mathbf{y}^T \mathbf{V} \boldsymbol{\mu}
                muVmu: ndarray or double
```

```
\mu^T \mathbf{V} \mu
```

logdet_V: ndarray or double

Log-determinant of the precision matrix, $\log |\mathbf{V}|$.

D: int

Dimensionality of the distribution.

bayespy.utils.random.intervals

```
bayespy.utils.random.intervals(N, length, amount=1, gap=0)
```

Return random non-overlapping parts of a sequence.

For instance, N=16, length=2 and amount=4: [0, |1, 2|, 3, 4, 5, |6, 7|, 8, 9, |10, 11|, |12, 13|, 14, 15] that is, [1,2,6,7,10,11,12,13]

However, the function returns only the indices of the beginning of the sequences, that is, in the example: [1,6,10,12]

bayespy.utils.random.invwishart_rand

```
bayespy.utils.random.invwishart_rand(nu, V)
```

bayespy.utils.random.mask

```
bayespy.utils.random.mask(*shape, p=0.5)
```

Return a boolean array of the given shape.

Parameters d0, d1, ..., dn: int

Shape of the output.

p: value in range [0,1]

A probability that the elements are *True*.

bayespy.utils.random.orth

```
bayespy.utils.random.orth(D)
```

Draw random orthogonal matrix.

bayespy.utils.random.sphere

```
bayespy.utils.random.sphere (N=1)
```

Draw random points uniformly on a unit sphere.

Returns (latitude,longitude) in degrees.

bayespy.utils.random.svd

```
bayespy.utils.random.svd(s)
```

Draw a random matrix given its singular values.

bayespy.utils.random.t_logpdf

```
bayespy.utils.random.t_logpdf(z2, logdet_cov, nu, D)
```

bayespy.utils.random.wishart rand

```
bayespy.utils.random.wishart_rand (nu, V)
Draw a random sample from the Wishart distribution.
```

Parameters nu: int

6.4.3 bayespy.utils.optimize

Functions

$check_gradient(f, x0[, verbose])$	Simple wrapper for SciPy's gradient checker.
<pre>minimize(f, x0[, maxiter, verbose])</pre>	Simple wrapper for SciPy's optimize.

bayespy.utils.optimize.check_gradient

```
bayespy.utils.optimize.check_gradient(f, x0, verbose=True)
```

Simple wrapper for SciPy's gradient checker.

The given function must return a tuple: (value, gradient).

Returns relative

bayespy.utils.optimize.minimize

```
bayespy.utils.optimize.minimize (f, x0, maxiter=None, verbose=False)
Simple wrapper for SciPy's optimize.
```

The given function must return a tuple: (value, gradient).

6.4.4 bayespy.utils.misc

General numerical functions and methods.

Functions

```
 \begin{array}{c} \text{T}(X) & \text{Transpose the matrix.} \\ \text{add\_axes}(X[, \text{num, axis}]) & \\ \text{add\_leading\_axes}(x, n) & \\ \text{add\_trailing\_axes}(x, n) & \\ \text{array\_to\_scalar}(x) & \\ \text{atleast\_nd}(X, d) & \\ \text{axes\_to\_collapse}(\text{shape\_x, shape\_to}) & \\ \text{block\_banded}(D, B) & \text{Construct a symmetric block-banded matrix.} \\ \hline \\ \text{Continued on next page} \\ \end{array}
```

Table 6.67 – continued from previous page

```
broadcasted shape(*shapes)
                                                  Computes the resulting broadcasted shape for a given set of shapes.
                                                  Computes the resulting broadcasted shape for a given set of arrays.
broadcasted_shape_from_arrays(*arrays)
ceildiv(a, b)
                                                  Compute a divided by b and rounded up.
check\_gradient(x0, f, df, eps)
chol(C)
chol_inv(U)
chol_logdet(U)
chol_solve(U, b)
cholesky(K)
composite_function(function_list)
                                                  Construct a function composition from a list of functions.
                                                  Create a diagonal array given the diagonal elements.
diag(X[, ndim])
diagonal(A)
dist haversine(c1, c2[, radius])
first(L)
gaussian_logpdf(y_invcov_y, y_invcov_mu, ...)
                                                  Get the diagonal of an array.
get_diag(X[, ndim])
grid(x1, x2)
                                                  Returns meshgrid as a (M*N,2)-shape array.
identity(*shape)
is_callable(f)
is numeric(a)
is_shape_subset(sub_shape, full_shape)
is_string(s)
isinteger(x)
kalman_filter(y, U, A, V, mu0, Cov0[, out])
                                                  Perform Kalman filtering to obtain filtered mean and covariance.
logdet_chol(U)
logsumexp(X[, axis, keepdims])
                                                  Compute log(sum(exp(X))) in a numerically stable way
m_{chol}(C)
m_{chol_inv}(U)
m_chol_logdet(U)
m chol solve(U, B[, out])
m digamma(a, d)
m_{dot}(A, b)
m_outer(A, B)
m_solve_triangular(U, B, **kwargs)
make_equal_length(*shapes)
                                                  Make tuples equal length.
                                                  Add trailing unit axes so that arrays have equal ndim
make_equal_ndim(*arrays)
mean(X[, axis, keepdims])
                                                  Compute the mean, ignoring NaNs.
moveaxis(A, axis_from, axis_to)
                                                  Move the axis axis_from to position axis_to.
multiply_shapes(*shapes)
                                                  Compute element-wise product of lists/tuples.
nans([size])
nested iterator(max inds)
remove whitespace(s)
repeat_to_shape(A, s)
rmse(y1, y2[, axis])
rts_smoother(mu, Cov, A, V[, removethis])
                                                  Perform Rauch-Tung-Striebel smoothing to obtain the posterior.
squeeze(X)
                                                  Remove leading axes that have unit length.
squeeze_to_dim(X, dim)
sum multiply(*args[, axis, sumaxis, keepdims])
sum_product(*args[, axes_to_keep, ...])
                                                  Sum leading axes of A such that A has dim dimensions.
sum_to_dim(A, dim)
sum_to_shape(X, s)
                                                  Sum axes of the array such that the resulting shape is as given.
symm(X)
                                                  Make X symmetric.
                                                                                      Continued on next page
```

Table 6.67 – continued from previous page

```
tempfile([prefix, suffix])
trues(shape)
unique(l)
vb_optimize(x0, set_values, lowerbound[, ...])
vb_optimize_nodes(*nodes)
write_to_hdf5(group, data, name)
zipper_merge(*lists)

Remove duplicate items from a list while preserving order.

Writes the given array into the HDF5 file.
Combines lists by alternating elements from them.
```

bayespy.utils.misc.T

```
bayespy.utils.misc.\mathbf{T}(X)
Transpose the matrix.
```

bayespy.utils.misc.add axes

```
bayespy.utils.misc.add axes (X, num=1, axis=0)
```

bayespy.utils.misc.add_leading_axes

```
bayespy.utils.misc.add_leading_axes (x, n)
```

bayespy.utils.misc.add_trailing_axes

```
bayespy.utils.misc.add_trailing_axes (x, n)
```

bayespy.utils.misc.array_to_scalar

```
bayespy.utils.misc.array_to_scalar(x)
```

bayespy.utils.misc.atleast nd

```
bayespy.utils.misc.atleast_nd(X, d)
```

bayespy.utils.misc.axes to collapse

```
bayespy.utils.misc.axes_to_collapse(shape_x, shape_to)
```

bayespy.utils.misc.block banded

```
\verb|bayespy.utils.misc.block_banded|(D,B)
```

Construct a symmetric block-banded matrix.

D contains square diagonal blocks. B contains super-diagonal blocks.

The resulting matrix is:

bayespy.utils.misc.broadcasted_shape

```
bayespy.utils.misc.broadcasted_shape(*shapes)
```

Computes the resulting broadcasted shape for a given set of shapes.

Uses the broadcasting rules of NumPy. Raises an exception if the shapes do not broadcast.

bayespy.utils.misc.broadcasted_shape_from_arrays

```
bayespy.utils.misc.broadcasted_shape_from_arrays(*arrays)
```

Computes the resulting broadcasted shape for a given set of arrays.

Raises an exception if the shapes do not broadcast.

bayespy.utils.misc.ceildiv

```
bayespy.utils.misc.ceildiv(a, b)
```

Compute a divided by b and rounded up.

bayespy.utils.misc.check_gradient

```
bayespy.utils.misc.check_gradient (x0, f, df, eps)
```

bayespy.utils.misc.chol

```
bayespy.utils.misc.chol(C)
```

bayespy.utils.misc.chol inv

```
bayespy.utils.misc.chol_inv(U)
```

bayespy.utils.misc.chol_logdet

```
bayespy.utils.misc.chol_logdet(U)
```

bayespy.utils.misc.chol_solve

```
\verb|bayespy.utils.misc.chol_solve|(U,b)|
```

bayespy.utils.misc.cholesky

```
bayespy.utils.misc.cholesky(K)
```

bayespy.utils.misc.composite_function

```
bayespy.utils.misc.composite_function(function_list)
```

Construct a function composition from a list of functions.

Given a list of functions [f,g,h], constructs a function $h \circ g \circ f$. That is, returns a function z, for which z(x) = h(g(f(x))).

bayespy.utils.misc.diag

```
bayespy.utils.misc.diag(X, ndim=1)
```

Create a diagonal array given the diagonal elements.

The diagonal array can be multi-dimensional. By default, the last axis is transformed to two axes (diagonal matrix) but this can be changed using ndim keyword. For instance, an array with shape (K,L,M,N) can be transformed to a set of diagonal 4-D tensors with shape (K,L,M,N,M,N) by giving ndim=2. If ndim=3, the result has shape (K,L,M,N,L,M,N), and so on.

Diagonality means that for the resulting array Y holds: $Y[...,i_1,i_2,...,i_n\dim,j_1,j_2,...,j_n\dim]$ is zero if $i_n!=j_n$ for any n.

bayespy.utils.misc.diagonal

```
bayespy.utils.misc.diagonal(A)
```

bayespy.utils.misc.dist haversine

```
bayespy.utils.misc.dist haversine(c1, c2, radius=6372795)
```

bavespv.utils.misc.first

```
bayespy.utils.misc.first(L)
```

bayespy.utils.misc.gaussian_logpdf

```
bayespy.utils.misc.gaussian_logpdf(y_invcov_y, y_invcov_mu, mu_invcov_mu, logdetcov, D)
```

bayespy.utils.misc.get diag

```
bayespy.utils.misc.get_diag(X, ndim=1)
```

Get the diagonal of an array.

If ndim>1, take the diagonal of the last 2*ndim axes.

bayespy.utils.misc.grid

```
bayespy.utils.misc.grid(x1, x2)
```

Returns meshgrid as a (M*N,2)-shape array.

bayespy.utils.misc.identity

bayespy.utils.misc.identity(*shape)

bayespy.utils.misc.is_callable

bayespy.utils.misc.is_callable(f)

bayespy.utils.misc.is numeric

bayespy.utils.misc.is_numeric(a)

bayespy.utils.misc.is_shape_subset

bayespy.utils.misc.is_shape_subset(sub_shape,full_shape)

bayespy.utils.misc.is string

bayespy.utils.misc.is_string(s)

bayespy.utils.misc.isinteger

bayespy.utils.misc.isinteger(x)

bayespy.utils.misc.kalman_filter

bayespy.utils.misc.kalman_filter(y, U, A, V, mu0, Cov0, out=None)

Perform Kalman filtering to obtain filtered mean and covariance.

The parameters of the process may vary in time, thus they are given as iterators instead of fixed values.

Parameters y : (N,D) array

"Normalized" noisy observations of the states, that is, the observations multiplied by the precision matrix U (and possibly other transformation matrices).

U: (N,D,D) array or N-list of (D,D) arrays

Precision matrix (i.e., inverse covariance matrix) of the observation noise for each time instance.

A: (N-1,D,D) array or (N-1)-list of (D,D) arrays

Dynamic matrix for each time instance.

V: (N-1,D,D) array or (N-1)-list of (D,D) arrays

Covariance matrix of the innovation noise for each time instance.

Returns mu: array

Filtered mean of the states.

Cov: array

Filtered covariance of the states.

```
See also:
```

```
rts smoother
```

bayespy.utils.misc.logdet chol

```
bayespy.utils.misc.logdet_chol(U)
```

bayespy.utils.misc.logsumexp

```
bayespy.utils.misc.logsumexp(X, axis=None, keepdims=False)
Compute log(sum(exp(X))) in a numerically stable way
```

bayespy.utils.misc.m_chol

```
bayespy.utils.misc.m_chol(C)
```

bayespy.utils.misc.m_chol_inv

```
bayespy.utils.misc.m_chol_inv(U)
```

bayespy.utils.misc.m chol logdet

```
bayespy.utils.misc.m_chol_logdet(U)
```

bayespy.utils.misc.m chol solve

```
bayespy.utils.misc.m_chol_solve(U, B, out=None)
```

bayespy.utils.misc.m digamma

```
\verb|bayespy.utils.misc.m_digamma| (a,d)
```

bayespy.utils.misc.m_dot

```
bayespy.utils.misc.m_dot(A, b)
```

bayespy.utils.misc.m_outer

```
bayespy.utils.misc.m_outer(A, B)
```

bayespy.utils.misc.m solve triangular

```
bayespy.utils.misc.m_solve_triangular(U, B, **kwargs)
```

bayespy.utils.misc.make_equal_length

```
bayespy.utils.misc.make_equal_length(*shapes)
Make tuples equal length.
```

Add leading 1s to shorter tuples.

bayespy.utils.misc.make_equal_ndim

```
bayespy.utils.misc.make_equal_ndim(*arrays)

Add trailing unit axes so that arrays have equal ndim
```

bayespy.utils.misc.mean

```
bayespy.utils.misc.mean (X, axis=None, keepdims=False)
Compute the mean, ignoring NaNs.
```

bayespy.utils.misc.moveaxis

```
bayespy.utils.misc.moveaxis(A, axis_from, axis_to)
Move the axis axis_from to position axis_to.
```

bayespy.utils.misc.multiply shapes

```
bayespy.utils.misc.multiply_shapes(*shapes)
Compute element-wise product of lists/tuples.
```

Shorter lists are concatenated with leading 1s in order to get lists with the same length.

bayespy.utils.misc.nans

```
bayespy.utils.misc.nans(size=())
```

bayespy.utils.misc.nested iterator

```
bayespy.utils.misc.nested_iterator(max_inds)
```

bayespy.utils.misc.remove_whitespace

```
bayespy.utils.misc.remove_whitespace(s)
```

bayespy.utils.misc.repeat_to_shape

```
bayespy.utils.misc.repeat_to_shape (A, s)
```

bayespy.utils.misc.rmse

```
bayespy.utils.misc.rmse(y1, y2, axis=None)
```

bayespy.utils.misc.rts smoother

```
bayespy.utils.misc.rts_smoother(mu, Cov, A, V, removethis=None)
```

Perform Rauch-Tung-Striebel smoothing to obtain the posterior.

The function returns the posterior mean and covariance of each state. The parameters of the process may vary in time, thus they are given as iterators instead of fixed values.

Parameters mu: (N,D) array

Mean of the states from Kalman filter.

Cov: (N,D,D) array

Covariance of the states from Kalman filter.

A: (N-1,D,D) array or (N-1)-list of (D,D) arrays

Dynamic matrix for each time instance.

V: (N-1,D,D) array or (N-1)-list of (D,D) arrays

Covariance matrix of the innovation noise for each time instance.

Returns mu: array

Posterior mean of the states.

Cov: array

Posterior covariance of the states.

See also:

kalman_filter

bayespy.utils.misc.squeeze

```
bayespy.utils.misc.squeeze(X)
```

Remove leading axes that have unit length.

For instance, a shape (1,1,4,1,3) will be reshaped to (4,1,3).

bayespy.utils.misc.squeeze to dim

```
bayespy.utils.misc.squeeze_to_dim(X, dim)
```

bayespy.utils.misc.sum multiply

```
bayespy.utils.misc.sum_multiply(*args, axis=None, sumaxis=True, keepdims=False)
```

bayespy.utils.misc.sum_product

```
bayespy.utils.misc.sum_product(*args, axes_to_keep=None, axes_to_sum=None, keep-dims=False)
```

bayespy.utils.misc.sum_to_dim

```
bayespy.utils.misc.sum_to_dim(A, dim)
Sum leading axes of A such that A has dim dimensions.
```

bayespy.utils.misc.sum_to_shape

```
bayespy.utils.misc.sum_to_shape (X, s)
```

Sum axes of the array such that the resulting shape is as given.

Thus, the shape of the result will be s or an error is raised.

bayespy.utils.misc.symm

bayespy.utils.misc.tempfile

```
bayespy.utils.misc.tempfile(prefix='', suffix='')
```

bayespy.utils.misc.trues

```
bayespy.utils.misc.trues(shape)
```

bayespy.utils.misc.unique

```
bayespy.utils.misc.unique(l)
```

Remove duplicate items from a list while preserving order.

bayespy.utils.misc.vb_optimize

```
bayespy.utils.misc.vb_optimize(x0, set_values, lowerbound, gradient=None)
```

bayespy.utils.misc.vb_optimize_nodes

```
bayespy.utils.misc.vb_optimize_nodes(*nodes)
```

bayespy.utils.misc.write_to_hdf5

```
bayespy.utils.misc.write_to_hdf5 (group, data, name)
Writes the given array into the HDF5 file.
```

bayespy.utils.misc.zipper_merge

```
bayespy.utils.misc.zipper_merge(*lists)
```

Combines lists by alternating elements from them.

Combining lists [1,2,3], ['a','b','c'] and [42,666,99] results in [1,'a',42,2,'b',666,3,'c',99]

The lists should have equal length or they are assumed to have the length of the shortest list.

This is known as alternating merge or zipper merge.

Classes

bayespy.utils.misc.CholeskyDense

```
{f class} bayespy.utils.misc.CholeskyDense(K)
```

```
___init___(K)
```

Methods

```
__init__(K)
logdet()
solve(b)
trace_solve_gradient(dK)
```

bayespy.utils.misc.CholeskyDense. init

```
CholeskyDense.__init__(K)
```

bayespy.utils.misc.CholeskyDense.logdet

```
CholeskyDense.logdet()
```

bayespy.utils.misc.CholeskyDense.solve

```
CholeskyDense.solve(b)
```

bayespy.utils.misc.CholeskyDense.trace solve gradient

```
CholeskyDense.trace_solve_gradient(dK)
```

bayespy.utils.misc.CholeskySparse

```
{f class} bayespy.utils.misc.CholeskySparse(K)
```

```
___init___(K)
```

Methods

```
__init__(K)
logdet()
solve(b)
trace_solve_gradient(dK)
```

bayespy.utils.misc.CholeskySparse. init

```
CholeskySparse.__init__(K)
```

bayespy.utils.misc.CholeskySparse.logdet

```
CholeskySparse.logdet()
```

bayespy.utils.misc.CholeskySparse.solve

```
CholeskySparse.solve(b)
```

bayespy.utils.misc.CholeskySparse.trace solve gradient

```
CholeskySparse.trace_solve_gradient(dK)
```

bayespy.utils.misc.TestCase

```
class bayespy.utils.misc.TestCase(methodName='runTest')
```

Simple base class for unit testing.

Adds NumPy's features to Python's unittest.

```
__init__ (methodName='runTest')
```

Create an instance of the class that will use the named test method when executed. Raises a ValueError if the instance does not have a method with the specified name.

Methods

init([methodName])	Create an instance of the class that will use the named test method when
addCleanup(function, *args, **kwargs)	Add a function, with arguments, to be called when the test is completed.
addTypeEqualityFunc(typeobj, function)	Add a type specific assertEqual style function to compare a type.
<pre>assertAllClose(A, B[, msg, rtol, atol])</pre>	

```
assertAlmostEqual(first, second[, places, ...])
                                                         Fail if the two objects are unequal as determined by their difference round
assertAlmostEquals(*args, **kwargs)
assertArrayEqual(A, B[, msg])
assertCountEqual(first, second[, msg])
                                                         An unordered sequence comparison asserting that the same elements, reg
assertDictContainsSubset(subset, dictionary)
                                                         Checks whether dictionary is a superset of subset.
assertDictEqual(d1, d2[, msg])
assertEqual(first, second[, msg])
                                                         Fail if the two objects are unequal as determined by the '==' operator.
assertEquals(*args, **kwargs)
assertFalse(expr[, msg])
                                                         Check that the expression is false.
assertGreater(a, b[, msg])
                                                         Just like self.assertTrue(a > b), but with a nicer default message.
assertGreaterEqual(a, b[, msg])
                                                         Just like self.assertTrue(a \ge b), but with a nicer default message.
                                                         Just like self.assertTrue(a in b), but with a nicer default message.
assertIn(member, container[, msg])
assertIs(expr1, expr2[, msg])
                                                         Just like self.assertTrue(a is b), but with a nicer default message.
assertIsInstance(obj, cls[, msg])
                                                         Same as self.assertTrue(isinstance(obj, cls)), with a nicer default message
assertIsNone(obj[, msg])
                                                         Same as self.assertTrue(obj is None), with a nicer default message.
assertIsNot(expr1, expr2[, msg])
                                                         Just like self.assertTrue(a is not b), but with a nicer default message.
assertIsNotNone(obj[, msg])
                                                         Included for symmetry with assertIsNone.
assertLess(a, b[, msg])
                                                         Just like self.assertTrue(a < b), but with a nicer default message.
                                                         Just like self.assertTrue(a \le b), but with a nicer default message.
assertLessEqual(a, b[, msg])
assertListEqual(list1, list2[, msg])
                                                         A list-specific equality assertion.
assertLogs([logger, level])
                                                         Fail unless a log message of level level or higher is emitted on logger_na.
assertMessage(M1, M2)
assertMessageToChild(X, u)
assertMultiLineEqual(first, second[, msg])
                                                         Assert that two multi-line strings are equal.
assertNotAlmostEqual(first, second[, ...])
                                                         Fail if the two objects are equal as determined by their difference rounded
assertNotAlmostEquals(*args, **kwargs)
assertNotEqual(first, second[, msg])
                                                         Fail if the two objects are equal as determined by the '!=' operator.
assertNotEquals(*args, **kwargs)
assertNotIn(member, container[, msg])
                                                         Just like self.assertTrue(a not in b), but with a nicer default message.
assertNotIsInstance(obj, cls[, msg])
                                                         Included for symmetry with assertIsInstance.
assertNotRegex(text, unexpected_regex[, msg])
                                                         Fail the test if the text matches the regular expression.
assertRaises(excClass[, callableObj])
                                                         Fail unless an exception of class excClass is raised by callableObj when i
assertRaisesRegex(expected_exception, ...[, ...])
                                                         Asserts that the message in a raised exception matches a regex.
assertRaisesRegexp(*args, **kwargs)
assertRegex(text, expected_regex[, msg])
                                                         Fail the test unless the text matches the regular expression.
assertRegexpMatches(*args, **kwargs)
assertSequenceEqual(seq1, seq2[, msg, seq_type])
                                                         An equality assertion for ordered sequences (like lists and tuples).
assertSetEqual(set1, set2[, msg])
                                                         A set-specific equality assertion.
assertTrue(expr[, msg])
                                                         Check that the expression is true.
assertTupleEqual(tuple1, tuple2[, msg])
                                                         A tuple-specific equality assertion.
assertWarns(expected_warning[, callable_obj])
                                                         Fail unless a warning of class warnClass is triggered by callable_obj whe
                                                         Asserts that the message in a triggered warning matches a regexp.
assertWarnsRegex(expected_warning, ...[, ...])
assert_(*args, **kwargs)
countTestCases()
                                                         Run the test without collecting errors in a TestResult
debug()
defaultTestResult()
                                                         Execute all cleanup functions.
doCleanups()
fail([msg])
                                                         Fail immediately, with the given message.
failIf(*args, **kwargs)
failIfAlmostEqual(*args, **kwargs)
failIfEqual(*args, **kwargs)
failUnless(*args, **kwargs)
```

```
failUnlessAlmostEqual(*args, **kwargs)
failUnlessEqual(*args, **kwargs)
failUnlessRaises(*args, **kwargs)
id()
run([result])
setUp()
                                                         Hook method for setting up the test fixture before exercising it.
setUpClass()
                                                         Hook method for setting up class fixture before running tests in the class.
                                                         Returns a one-line description of the test, or None if no description has be
shortDescription()
skipTest(reason)
                                                         Skip this test.
subTest([msg])
                                                         Return a context manager that will return the enclosed block of code in a
tearDown()
                                                         Hook method for deconstructing the test fixture after testing it.
                                                         Hook method for deconstructing the class fixture after running all tests in
tearDownClass()
```

bayespy.utils.misc.TestCase. init

```
TestCase. init (methodName='runTest')
```

Create an instance of the class that will use the named test method when executed. Raises a ValueError if the instance does not have a method with the specified name.

bayespy.utils.misc.TestCase.addCleanup

```
TestCase.addCleanup (function, *args, **kwargs)
```

Add a function, with arguments, to be called when the test is completed. Functions added are called on a LIFO basis and are called after tearDown on test failure or success.

Cleanup items are called even if setUp fails (unlike tearDown).

bayespy.utils.misc.TestCase.addTypeEqualityFunc

```
TestCase.addTypeEqualityFunc (typeobj, function)
```

Add a type specific assertEqual style function to compare a type.

This method is for use by TestCase subclasses that need to register their own type equality functions to provide nicer error messages.

Args

typeobj: The data type to call this function on when both values are of the same type in assertE-qual().

function: The callable taking two arguments and an optional msg= argument that raises self.failureException with a useful error message when the two arguments are not equal.

bayespy.utils.misc.TestCase.assertAllClose

TestCase.assertAllClose (A, B, msg='Arrays not almost equal', rtol=0.0001, atol=0)

bayespy.utils.misc.TestCase.assertAlmostEqual

```
TestCase.assertAlmostEqual (first, second, places=None, msg=None, delta=None)
```

Fail if the two objects are unequal as determined by their difference rounded to the given number of decimal

places (default 7) and comparing to zero, or by comparing that the between the two objects is more than the given delta.

Note that decimal places (from zero) are usually not the same as significant digits (measured from the most significant digit).

If the two objects compare equal then they will automatically compare almost equal.

bayespy.utils.misc.TestCase.assertAlmostEquals

```
TestCase.assertAlmostEquals(*args, **kwargs)
```

bayespy.utils.misc.TestCase.assertArrayEqual

```
TestCase.assertArrayEqual (A, B, msg='Arrays not equal')
```

bayespy.utils.misc.TestCase.assertCountEqual

```
TestCase.assertCountEqual (first, second, msg=None)
```

An unordered sequence comparison asserting that the same elements, regardless of order. If the same element occurs more than once, it verifies that the elements occur the same number of times.

self.assertEqual(Counter(list(first)), Counter(list(second)))

Example:

- [0, 1, 1] and [1, 0, 1] compare equal.
- [0, 0, 1] and [0, 1] compare unequal.

bayespy.utils.misc.TestCase.assertDictContainsSubset

```
\texttt{TestCase.} \textbf{assertDictContainsSubset} \ (\textit{subset}, \textit{dictionary}, \textit{msg} = None)
```

Checks whether dictionary is a superset of subset.

bayespy.utils.misc.TestCase.assertDictEqual

```
TestCase.assertDictEqual(d1, d2, msg=None)
```

bayespy.utils.misc.TestCase.assertEqual

```
TestCase.assertEqual (first, second, msg=None)
```

Fail if the two objects are unequal as determined by the '==' operator.

bayespy.utils.misc.TestCase.assertEquals

```
TestCase.assertEquals(*args, **kwargs)
```

bayespy.utils.misc.TestCase.assertFalse

TestCase.assertFalse(expr, msg=None)

Check that the expression is false.

bayespy.utils.misc.TestCase.assertGreater

TestCase.assertGreater (a, b, msg=None)

Just like self.assertTrue(a > b), but with a nicer default message.

bayespy.utils.misc.TestCase.assertGreaterEqual

TestCase.assertGreaterEqual (a, b, msg=None)

Just like self.assertTrue($a \ge b$), but with a nicer default message.

bayespy.utils.misc.TestCase.assertIn

TestCase.assertIn (member, container, msg=None)

Just like self.assertTrue(a in b), but with a nicer default message.

bayespy.utils.misc.TestCase.assertls

TestCase.assertIs (expr1, expr2, msg=None)

Just like self.assertTrue(a is b), but with a nicer default message.

bayespy.utils.misc.TestCase.assertIsInstance

TestCase.assertIsInstance(obj, cls, msg=None)

Same as self.assertTrue(isinstance(obj, cls)), with a nicer default message.

bayespy.utils.misc.TestCase.assertIsNone

TestCase.assertIsNone(obj, msg=None)

Same as self.assertTrue(obj is None), with a nicer default message.

bayespy.utils.misc.TestCase.assertIsNot

TestCase.assertIsNot (expr1, expr2, msg=None)

Just like self.assertTrue(a is not b), but with a nicer default message.

bayespy.utils.misc.TestCase.assertIsNotNone

TestCase.assertIsNotNone(obj, msg=None)

Included for symmetry with assertIsNone.

bayespy.utils.misc.TestCase.assertLess

```
TestCase.assertLess(a, b, msg=None)
```

Just like self.assertTrue(a < b), but with a nicer default message.

bayespy.utils.misc.TestCase.assertLessEqual

```
TestCase.assertLessEqual (a, b, msg=None)
```

Just like self.assertTrue(a <= b), but with a nicer default message.

bayespy.utils.misc.TestCase.assertListEqual

```
TestCase.assertListEqual (list1, list2, msg=None)
```

A list-specific equality assertion.

Args: list1: The first list to compare. list2: The second list to compare. msg: Optional message to use on failure instead of a list of

differences.

bayespy.utils.misc.TestCase.assertLogs

```
TestCase.assertLogs(logger=None, level=None)
```

Fail unless a log message of level *level* or higher is emitted on *logger_name* or its children. If omitted, *level* defaults to INFO and *logger* defaults to the root logger.

This method must be used as a context manager, and will yield a recording object with two attributes: *output* and *records*. At the end of the context manager, the *output* attribute will be a list of the matching formatted log messages and the *records* attribute will be a list of the corresponding LogRecord objects.

Example:

bayespy.utils.misc.TestCase.assertMessage

```
TestCase.assertMessage (M1, M2)
```

bayespy.utils.misc.TestCase.assertMessageToChild

```
TestCase.assertMessageToChild (X, u)
```

bayespy.utils.misc.TestCase.assertMultiLineEqual

```
TestCase.assertMultiLineEqual (first, second, msg=None)
```

Assert that two multi-line strings are equal.

bayespy.utils.misc.TestCase.assertNotAlmostEqual

TestCase.assertNotAlmostEqual (first, second, places=None, msg=None, delta=None)

Fail if the two objects are equal as determined by their difference rounded to the given number of decimal places (default 7) and comparing to zero, or by comparing that the between the two objects is less than the given delta.

Note that decimal places (from zero) are usually not the same as significant digits (measured from the most significant digit).

Objects that are equal automatically fail.

bayespy.utils.misc.TestCase.assertNotAlmostEquals

```
TestCase.assertNotAlmostEquals(*args, **kwargs)
```

bayespy.utils.misc.TestCase.assertNotEqual

```
TestCase.assertNotEqual (first, second, msg=None)
```

Fail if the two objects are equal as determined by the '!=' operator.

bayespy.utils.misc.TestCase.assertNotEquals

```
TestCase.assertNotEquals(*args, **kwargs)
```

bayespy.utils.misc.TestCase.assertNotIn

```
TestCase.assertNotIn (member, container, msg=None)
```

Just like self.assertTrue(a not in b), but with a nicer default message.

bayespy.utils.misc.TestCase.assertNotIsInstance

```
TestCase.assertNotIsInstance(obj, cls, msg=None)
```

Included for symmetry with assertIsInstance.

bayespy.utils.misc.TestCase.assertNotRegex

```
TestCase.assertNotRegex (text, unexpected_regex, msg=None)
```

Fail the test if the text matches the regular expression.

bayespy.utils.misc.TestCase.assertRaises

```
TestCase.assertRaises (excClass, callableObj=None, *args, **kwargs)
```

Fail unless an exception of class excClass is raised by callableObj when invoked with arguments args and keyword arguments kwargs. If a different type of exception is raised, it will not be caught, and the test case will be deemed to have suffered an error, exactly as for an unexpected exception.

If called with callableObj omitted or None, will return a context object used like this:

```
with self.assertRaises(SomeException):
    do_something()
```

An optional keyword argument 'msg' can be provided when assertRaises is used as a context object.

The context manager keeps a reference to the exception as the 'exception' attribute. This allows you to inspect the exception after the assertion:

```
with self.assertRaises(SomeException) as cm:
    do_something()
the_exception = cm.exception
self.assertEqual(the_exception.error_code, 3)
```

bayespy.utils.misc.TestCase.assertRaisesRegex

```
TestCase.assertRaisesRegex (expected_exception, expected_regex, callable_obj=None, *args, **kwargs)
```

Asserts that the message in a raised exception matches a regex.

Args: expected_exception: Exception class expected to be raised. expected_regex: Regex (re pattern object or string) expected

to be found in error message.

callable_obj: Function to be called. msg: Optional message used in case of failure. Can only be used when assertRaisesRegex is used as a context manager.

args: Extra args. kwargs: Extra kwargs.

bayespy.utils.misc.TestCase.assertRaisesRegexp

```
TestCase.assertRaisesRegexp(*args, **kwargs)
```

bayespy.utils.misc.TestCase.assertRegex

```
TestCase.assertRegex (text, expected_regex, msg=None)
Fail the test unless the text matches the regular expression.
```

bayespy.utils.misc.TestCase.assertRegexpMatches

```
TestCase.assertRegexpMatches(*args, **kwargs)
```

bayespy.utils.misc.TestCase.assertSequenceEqual

```
TestCase.assertSequenceEqual (seq1, seq2, msg=None, seq_type=None)
```

An equality assertion for ordered sequences (like lists and tuples).

For the purposes of this function, a valid ordered sequence type is one which can be indexed, has a length, and has an equality operator.

Args: seq1: The first sequence to compare. seq2: The second sequence to compare. seq_type: The expected datatype of the sequences, or None if no

datatype should be enforced.

msg: Optional message to use on failure instead of a list of differences.

bayespy.utils.misc.TestCase.assertSetEqual

```
TestCase.assertSetEqual (set1, set2, msg=None)
```

A set-specific equality assertion.

Args: set1: The first set to compare. set2: The second set to compare. msg: Optional message to use on failure instead of a list of

differences.

assertSetEqual uses ducktyping to support different types of sets, and is optimized for sets specifically (parameters must support a difference method).

bayespy.utils.misc.TestCase.assertTrue

```
TestCase.assertTrue(expr, msg=None)
```

Check that the expression is true.

bayespy.utils.misc.TestCase.assertTupleEqual

```
TestCase.assertTupleEqual (tuple1, tuple2, msg=None)
```

A tuple-specific equality assertion.

Args: tuple1: The first tuple to compare. tuple2: The second tuple to compare. msg: Optional message to use on failure instead of a list of

differences.

bayespy.utils.misc.TestCase.assertWarns

```
TestCase.assertWarns (expected_warning, callable_obj=None, *args, **kwargs)
```

Fail unless a warning of class warnClass is triggered by callable_obj when invoked with arguments args and keyword arguments kwargs. If a different type of warning is triggered, it will not be handled: depending on the other warning filtering rules in effect, it might be silenced, printed out, or raised as an exception.

If called with callable_obj omitted or None, will return a context object used like this:

```
with self.assertWarns(SomeWarning):
    do_something()
```

An optional keyword argument 'msg' can be provided when assertWarns is used as a context object.

The context manager keeps a reference to the first matching warning as the 'warning' attribute; similarly, the 'filename' and 'lineno' attributes give you information about the line of Python code from which the warning was triggered. This allows you to inspect the warning after the assertion:

```
with self.assertWarns(SomeWarning) as cm:
    do_something()
the_warning = cm.warning
self.assertEqual(the_warning.some_attribute, 147)
```

bayespy.utils.misc.TestCase.assertWarnsRegex

Asserts that the message in a triggered warning matches a regexp. Basic functioning is similar to assertWarns() with the addition that only warnings whose messages also match the regular expression are considered successful matches.

Args: expected_warning: Warning class expected to be triggered. expected_regex: Regex (re pattern object or string) expected

to be found in error message.

callable_obj: Function to be called. msg: Optional message used in case of failure. Can only be used when assertWarnsRegex is used as a context manager.

args: Extra args. kwargs: Extra kwargs.

bayespy.utils.misc.TestCase.assert

```
TestCase.assert_(*args, **kwargs)
```

bayespy.utils.misc.TestCase.countTestCases

```
TestCase.countTestCases()
```

bayespy.utils.misc.TestCase.debug

```
TestCase.debug()
```

Run the test without collecting errors in a TestResult

bayespy.utils.misc.TestCase.defaultTestResult

```
TestCase.defaultTestResult()
```

bayespy.utils.misc.TestCase.doCleanups

```
TestCase.doCleanups()
```

Execute all cleanup functions. Normally called for you after tearDown.

bayespy.utils.misc.TestCase.fail

```
TestCase.fail (msg=None)
```

Fail immediately, with the given message.

bayespy.utils.misc.TestCase.faillf

```
TestCase.failIf(*args, **kwargs)
```

```
TestCase.failIfAlmostEqual(*args, **kwargs)
bayespy.utils.misc.TestCase.failIfEqual
TestCase.failIfEqual(*args, **kwargs)
bayespy.utils.misc.TestCase.failUnless
TestCase.failUnless(*args, **kwargs)
bayespy.utils.misc.TestCase.failUnlessAlmostEqual
TestCase.failUnlessAlmostEqual(*args, **kwargs)
bayespy.utils.misc.TestCase.failUnlessEqual
TestCase.failUnlessEqual(*args, **kwargs)
bayespy.utils.misc.TestCase.failUnlessRaises
TestCase.failUnlessRaises(*args, **kwargs)
bayespy.utils.misc.TestCase.id
TestCase.id()
bayespy.utils.misc.TestCase.run
TestCase.run (result=None)
bayespy.utils.misc.TestCase.setUp
TestCase.setUp()
    Hook method for setting up the test fixture before exercising it.
bayespy.utils.misc.TestCase.setUpClass
TestCase.setUpClass()
    Hook method for setting up class fixture before running tests in the class.
```

bayespy.utils.misc.TestCase.failIfAlmostEqual

bayespy.utils.misc.TestCase.shortDescription

```
TestCase.shortDescription()
```

Returns a one-line description of the test, or None if no description has been provided.

The default implementation of this method returns the first line of the specified test method's docstring.

bayespy.utils.misc.TestCase.skipTest

```
TestCase.skipTest (reason)
Skip this test.
```

bayespy.utils.misc.TestCase.subTest

```
TestCase.subTest (msg=None, **params)
```

Return a context manager that will return the enclosed block of code in a subtest identified by the optional message and keyword parameters. A failure in the subtest marks the test case as failed but resumes execution at the end of the enclosed block, allowing further test code to be executed.

bayespy.utils.misc.TestCase.tearDown

```
TestCase.tearDown()
```

Hook method for deconstructing the test fixture after testing it.

bayespy.utils.misc.TestCase.tearDownClass

```
TestCase.tearDownClass()
```

Hook method for deconstructing the class fixture after running all tests in the class.

Attributes

oool
integer

bayespy.utils.misc.TestCase.longMessage

```
TestCase.longMessage = True
```

bayespy.utils.misc.TestCase.maxDiff

```
TestCase.maxDiff = 640
```

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