bnpy Documentation

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BNPy (or bnpy) is Bayesian Nonparametric clustering for Python.

Our goal is to make it easy for Python programmers to train state-of-the-art clustering models on large datasets. We focus on nonparametric models based on the Dirichlet process, especially extensions that handle hierarchical and sequential datasets. Traditional parametric counterparts (like finite mixture models) are also supported.

Training a model with **bnpy** requires the user to specify the dataset, the model, and the algorithm to use. Flexible keyword options allow advanced users lots of control, but smart defaults make it simple for beginners. **bnpy**'s modular implementation makes it possible to try many variants of models and algorithms, to find the best fit for the data at hand.

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Example Gallery

You can find many examples of **bnpy** in action in our curated Example Gallery.

These same demos are also directly available as Python scrips inside the project Github repository.

Quick Start

You can use **bnpy** to train a model in two ways: (1) from a command line/terminal, or (2) from within a Python script (of course). Both options require specifying a dataset, an allocation model, an observation model (likelihood), and an algorithm. Optional keyword arguments with reasonable defaults allow control of specific model hyperparameters, algorithm parameters, etc.

Below, we show how to call bnpy to train a 8 component Gaussian mixture model on a default toy dataset stored in a .csv file on disk. In both cases, log information is printed to stdout, and all learned model parameters are saved to disk.

2.1 Training from a terminal

```
python -m bnpy.Run /path/to/my_dataset.csv FiniteMixtureModel Gauss EM --K 8 --output_path
```

2.2 Training via Python

2.3 Featured algorithms

Train a Dirichlet-process Gaussian mixture model (DP-GMM) via full-dataset variational coordinate ascent. This algorithm is often called "VB" for variational Bayes.

```
python -m bnpy.Run /path/to/dataset.csv DPMixtureModel Gauss VB --K 8
```

Train DP-GMM via scalable incremental or "memoized" variational coordinate ascent, with birth and merge moves, with data divided into 10 batches.

python -m bnpy.Run /path/to/dataset.csv DPMixtureModel Gauss memoVB --K 8 --nBatch 10 --mo

Train HDP-HMM model to capture sequential structure in the dataset

2.4 Getting Help

```
# print help message for required arguments
python -m bnpy.Run --help
```

print help message for specific keyword options for Gaussian mixture models
python -m bnpy.Run /path/to/dataset.csv FiniteMixtureModel Gauss EM --kwhelp

Supported allocation models

The following are possible *allocation* models, which is **bnpy**-terminology for a generative model which assigns clusters to structured datasets.

Mixture models

- FiniteMixtureModel: fixed number of clusters
- DPMixtureModel: infinite number of clusters, via the Dirichlet process
- Topic models (aka admixtures models)
 - FiniteTopicModel: fixed number of topics. This is Latent Dirichlet allocation.
 - HDPTopicModel: infinite number of topics, via the hierarchical Dirichlet process
- Hidden Markov models (HMMs)
 - FiniteHMM: Markov sequence model with a fixture number of states
 - HDPHMM: Markov sequence models with an infinite number of states

COMING SOON

- relational models (like the IRM, MMSB, etc.)
- grammar models

Supported observations models

Any of the above allocation models can be combined with one of these *observation* models, which describe how to produce data assigned to a specific cluster.

- Real-valued vector observations (1-dim, 2-dim, ... D-dim)
 - Gauss: Full-covariance Gaussian
 - *DiagGauss*: Diagonal-covariance Gaussian
 - ZeroMeanGauss: Zero-mean, full-covariance
 - AutoRegGauss: first-order auto-regressive Gaussian
- Binary vector observations (1-dim, 2-dim, ... D-dim)
 - Bern: Bernoulli
- Discrete, bag-of-words data (each observation is one of V symbols)
 - *Mult* : Multinomial

Supported algorithms

• Variational methods

- EM: Expectation-maximization
- VB: variational Bayes
- *soVB* : stochastic variational (online)
- *moVB* : memoized variational (online)

COMING SOON

- Gibbs sampling

5.1 Installation

5.1.1 Requirements

bnpy requires Python 2.7+ and the following packages:

- numpy >= 1.11
- scipy >= 0.18
- pandas >= 0.18
- Cython >= 0.25
- joblib >= 0.10
- memory_profiler >= 0.41
- munkres >= 1.0
- numexpr >= 2.6
- psutil >= 5.0
- scikit_learn >= 0.18

For interactivity and visualization, we also recommend:

- ipython >= 5.1
- matplotlib >= 1.5

5.1.2 Easy installation of bnpy

First, make sure you have a working local install of the Anaconda python distribution, which makes managing common Python packages within userspace a breeze.

Then, you can just clone the latest stable version of bnpy via:

```
git clone https://github.com/bnpy/bnpy.git
```

And then install from the cloned source via:

```
cd bnpy/
pip install -e .
```

Verifying correct installation

Within a terminal, you can first verify basic installation with:

```
python -m bnpy.Run --help
```

You can further train a very simple model:

```
python -m bnpy.Run \
DATASET_PATH/faithful/faithful.csv \
FiniteMixtureModel Gauss VB --nLap 1 --K 3
```

To further verify matplotlib installation, enter:

```
from matplotlib import pylab
pylab.plot([1,2,3])
pylab.show()
```

5.1.3 Advanced Installation

Some of bnpy's advanced features require compiling custom C++ source code for fast algorithms. These aren't needed for basic usage, but do come in handy.

Installing with Eigen C++ libraries

The Eigen C++ Matrix template library (>=3.0) is used for:

- fast local step updates for hidden Markov models
- fast local step updates for L-sparse mixtures

If you want these features, go download and install Eigen from http://www.eigen.tuxfamily.org.

To install bnpy with Eigen support, you need to set the following environment variable:

```
export EIGENPATH=/path/to/eigen/
```

You can verify the right location by verifying the following directory exists:

```
ls $EIGENPATH/Eigen/
```

If the \$EIGENPATH env variable is set when you perform **pip install**, the required C++ libraries should be built and useful automatically.

Installing with Boost C++ math libraries

The Boost C++ math library (\geq 1.52) is used for the following features:

• fast local step updates for L-sparse topic models

If you want these features, go download and install boost from http://www.boost.org.

To install bnpy with Boost C++ support, you need to set the following environment variable:

```
export BOOSTMATHPATH=/path/to/boost/include/
```

You can verify the right location by verifying the following directory exists:

```
ls $BOOSTMATHPATH/math/
```

If the \$BOOSTMATHPATH env variable is set when you perform **pip install**, the required C++ libraries should be built and useful automatically.

5.1.4 Common errors with matplotlib

If you try the above and get errors about not having "wx" or "wxpython" or "qt" installed, you need to configure your Matplotlib_backend.

I recommend setting your matplotlibre file to have *backend: TkAgg* for Linux, and *backend: MacOSX* for Mac.

5.2 Example Gallery

5.2.1 Asterisk toy dataset

Training mixture models and DP mixture models on well-separated 2D Gaussian blobs.

Variational coordinate descent for Mixture of Gaussians

How to do Variational Bayes (VB) coordinate descent for GMM.

Here, we train a finite mixture of Gaussians with full covariances.

We'll consider a mixture model with a symmetric Dirichlet prior:

$$\pi \sim \text{Dir}(1/K, 1/K, \dots 1/K)$$

as well as a standard conjugate prior on the mean and covariances, such that

$$\mathbb{E}[\mu_k] = 0$$
$$\mathbb{E}[\Sigma_k] = 0.1I_D$$

We will initialize the approximate variational posterior using K=10 randomly chosen examples ('randexamples' procedure), and then perform coordinate descent updates (alternating local step and global step) until convergence.

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns
# sphinx_gallery_thumbnail_number = 3

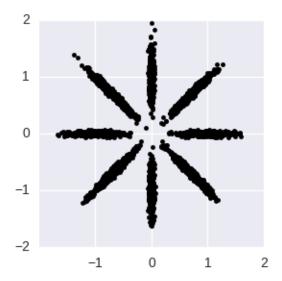
FIG_SIZE = (3, 3)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read bnpy's built-in "AsteriskK8" dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'AsteriskK8')
dataset = bnpy.data.XData.read_npz(
    os.path.join(dataset_path, 'x_dataset.npz'))
```

Make a simple plot of the raw data

```
pylab.plot(dataset.X[:, 0], dataset.X[:, 1], 'k.')
pylab.gca().set_xlim([-2, 2])
pylab.gca().set_ylim([-2, 2])
pylab.tight_layout()
```



Training the model

Let's do one single run of the VB algorithm.

Using 10 clusters and the 'randexamples' initializatio procedure.

```
trained_model, info_dict = bnpy.run(
    dataset, 'FiniteMixtureModel', 'Gauss', 'VB',
    output_path='/tmp/AsteriskK8/helloworld-K=10/',
    nLap=100,
    sF=0.1, ECovMat='eye',
    K=10,
    initname='randexamples')
```

Out:

```
Dataset Summary:
X Data
 num examples: 5000
 num dims: 2
Allocation Model: Finite mixture model. Dir prior param 1.00
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior: Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [ 0. 0.]
 E[covar[k]] =
 [[ 0.1 0. ]
  [ 0.
         0.1]]
Initialization:
 initname = randexamples
 K = 10 (number of clusters)
 seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: VB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
```

ask_output_path: /tm	p/AsteriskK8/h	elloworld-K=10/1			
1/100 after	0 sec.	132.9 MiB K	10 loss	6.582634775e-01	
2/100 after	0 sec.	132.9 MiB K	10 loss	4.350235353e-01	Ndiff
3/100 after	0 sec.	132.9 MiB K	10 loss	3.454096950e-01	Ndiff
4/100 after	0 sec.	132.9 MiB K	10 loss	3.049230819e-01	Ndiff
5/100 after	0 sec.	132.9 MiB K	10 loss	2.732439109e-01	Ndiff
6/100 after	0 sec.	132.9 MiB K	10 loss	2.326372999e-01	Ndiff
7/100 after	0 sec.	132.9 MiB K	10 loss	2.100254570e-01	Ndiff
8/100 after	0 sec.	132.9 MiB K	10 loss	2.097453779e-01	Ndiff
9/100 after	0 sec.	132.9 MiB K	10 loss	2.094741199e-01	Ndiff
10/100 after	0 sec.	132.9 MiB K	10 loss	2.091535256e-01	Ndiff
11/100 after	0 sec.	132.9 MiB K	10 loss	2.087740779e-01	Ndiff
12/100 after	0 sec.	132.9 MiB K	10 loss	2.083262051e-01	Ndiff
13/100 after	0 sec.	132.9 MiB K	10 loss	2.078022512e-01	Ndiff
14/100 after	0 sec.	132.9 MiB K	10 loss	2.072001819e-01	Ndiff
15/100 after	0 sec.	132.9 MiB K	10 loss	2.065288318e-01	Ndiff
16/100 after	0 sec.	132.9 MiB K	10 loss	2.058118708e-01	Ndiff
17/100 after	0 sec.	132.9 MiB K	10 loss	2.050844132e-01	Ndiff
18/100 after	0 sec.	132.9 MiB K	10 loss	2.043795824e-01	Ndiff
19/100 after	0 sec.	132.9 MiB K	10 loss	2.037146182e-01	Ndiff
20/100 after	0 sec.	132.9 MiB K	10 loss	2.030678434e-01	Ndiff
21/100 after	0 sec.	132.9 MiB K	10 loss	2.022621299e-01	Ndiff
22/100 after	0 sec.	132.9 MiB K	10 loss	2.008648784e-01	Ndiff
23/100 after	0 sec.	132.9 MiB K	10 loss	2.002168334e-01	Ndiff
24/100 after	0 sec.	132.9 MiB K	10 loss	1.995420809e-01	Ndiff
25/100 after	1 sec.	132.9 MiB K	10 loss	1.988594991e-01	Ndiff
26/100 after	1 sec.	132.9 MiB K	10 loss	1.982035545e-01	Ndiff
27/100 after	1 sec.	132.9 MiB K	10 loss	1.974254707e-01	Ndiff
28/100 after	1 sec.	132.9 MiB K	10 loss	1.966834121e-01	Ndiff
29/100 after	1 sec.	132.9 MiB K	10 loss	1.964267444e-01	Ndiff
30/100 after	1 sec.	132.9 MiB K	10 loss	1.961250819e-01	Ndiff
31/100 after	1 sec.	132.9 MiB K	10 loss	1.957730227e-01	Ndiff
32/100 after	1 sec.	132.9 MiB K	10 loss	1.953666781e-01	Ndiff
33/100 after	1 sec.	132.9 MiB K	10 loss	1.949058031e-01	Ndiff
34/100 after	1 sec.	132.9 MiB K	10 loss	1.943977009e-01	Ndiff
35/100 after	1 sec.	132.9 MiB K	10 loss	1.938623040e-01	Ndiff
36/100 after	1 sec.	132.9 MiB K	10 loss	1.933345511e-01	Ndiff
37/100 after	1 sec.	132.9 MiB K	10 loss	1.928570776e-01	Ndiff
38/100 after	1 sec.	132.9 MiB K	10 loss	1.924667495e-01	Ndiff
39/100 after	1 sec.	132.9 MiB K	10 loss	1.921899371e-01	Ndiff
40/100 after	1 sec.	132.9 MiB K	10 loss	1.919922352e-01	Ndiff
41/100 after	1 sec.	132.9 MiB K	10 loss	1.916267958e-01	Ndiff
42/100 after	1 sec.	132.9 MiB K	10 loss	1.909787395e-01	Ndiff

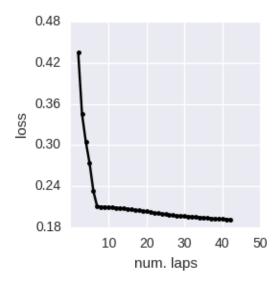
Loss function trace plot

We can plot the value of the loss function over iterations, starting after the first full pass over the dataset (first lap).

As expected, we see monotonic decrease in the loss function's score after every subsequent iteration.

Remember that the VB algorithm for GMMs is *guaranteed* to decrease this loss function after every step.

```
pylab.plot(info_dict['lap_history'][1:], info_dict['loss_history'][1:], 'k.-')
pylab.xlabel('num. laps')
pylab.ylabel('loss')
pylab.tight_layout()
```



Visualization of learned clusters

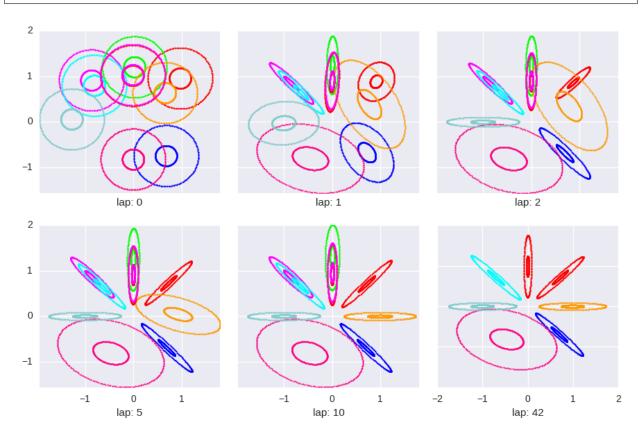
Here's a short function to show the learned clusters over time.

```
def show_clusters_over_time(
       task_output_path=None,
       query_laps=[0, 1, 2, 5, 10, None],
       nrows=2):
    ''' Read model snapshots from provided folder and make visualizations
   Post Condition
    _____
   New matplotlib plot with some nice pictures.
   ncols = int(np.ceil(len(query_laps) // float(nrows)))
   fig_handle, ax_handle_list = pylab.subplots(
       figsize=(FIG_SIZE[0] * ncols, FIG_SIZE[1] * nrows),
       nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for plot_id, lap_val in enumerate(query_laps):
       cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
        # Plot the current model
       cur_ax_handle = ax_handle_list.flatten()[plot_id]
       bnpy.viz.PlotComps.plotCompsFromHModel(
           cur_model, Data=dataset, ax_handle=cur_ax_handle)
       cur_ax_handle.set_xticks([-2, -1, 0, 1, 2])
       cur_ax_handle.set_yticks([-2, -1, 0, 1, 2])
```

```
cur_ax_handle.set_xlabel("lap: %d" % lap_val)
pylab.tight_layout()
```

Show the estimated clusters over time

```
show_clusters_over_time(info_dict['task_output_path'])
```



Out:

SKIPPED 3 comps with size below 0.00

Total running time of the script: (0 minutes 1.969 seconds)

Download Python source code: plot-02-demo=vb_single_run-model=dp_mix+gauss.py

Download Jupyter notebook: plot-02-demo=vb_single_run-model=dp_mix+gauss.ipynb

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Initialization for Mixtures of Gaussians

How to initialize Gaussian observation models.

We demonstrate a few possible initialization procedures for Gaussian observation models (which include Gauss, DiagGauss, ZeroMeanGauss).

Initialization depends on two key user-specified procedures:

- 1. Specifying hyperparameters for the conjugate prior
- 2. Specifying how many clusters are created

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns
# sphinx_gallery_thumbnail_number = 2

FIG_SIZE = (3, 3)
SMALL_FIG_SIZE = (2, 2)
```

Out:

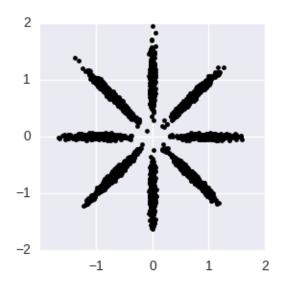
/home/docs/checkouts/readthedocs.org/user_builds/bnpy/envs/latest/local/lib/python2.7/site-

Read bnpy's built-in "AsteriskK8" dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'AsteriskK8')
dataset = bnpy.data.XData.read_npz(
    os.path.join(dataset_path, 'x_dataset.npz'))
```

Make a simple plot of the raw data

```
pylab.figure(figsize=FIG_SIZE)
pylab.plot(dataset.X[:, 0], dataset.X[:, 1], 'k.')
pylab.gca().set_xlim([-2, 2])
pylab.gca().set_ylim([-2, 2])
pylab.tight_layout()
```



Utility function for displaying many random initializations side by side.

```
def show_many_random_initial_models(
        obsPriorArgsDict,
        initArgsDict,
       nrows=1, ncols=6):
    ''' Create plot of many different random initializations
    fig_handle, ax_handle_list = pylab.subplots(
        figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
       nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for trial_id in range(nrows * ncols):
        cur_model = bnpy.make_initialized_model(
            dataset,
            allocModelName='FiniteMixtureModel',
            obsModelName='Gauss',
            algName='VB',
            allocPriorArgsDict=dict(gamma=10.0),
            obsPriorArgsDict=obsPriorArgsDict,
            initArgsDict=initArgsDict,
            seed=int(trial_id),
            )
        # Plot the current model
        cur_ax_handle = ax_handle_list.flatten()[trial_id]
       bnpy.viz.PlotComps.plotCompsFromHModel(
            cur_model, Data=dataset, ax_handle=cur_ax_handle)
       cur_ax_handle.set_xticks([-2, -1, 0, 1, 2])
        cur_ax_handle.set_yticks([-2, -1, 0, 1, 2])
   pylab.tight_layout()
```

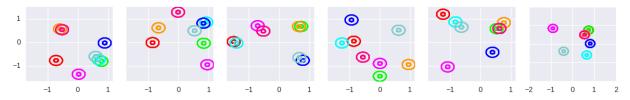
initname: 'randexamples'

This procedure selects K examples uniformly at random. Each cluster is then initialized from one selected example, using a standard global step update.

Example 1: Initialize with 8 clusters, with prior biased towards small covariances

$$\mathbb{E}_{\mathbf{prior}}[\Sigma_k] = 0.01I_D$$

```
show_many_random_initial_models(
    dict(sF=0.01, ECovMat='eye'),
    dict(initname='randexamples', K=8))
```



Example 2: Initialize with 8 clusters, with prior biased towards moderate covariances

$$\mathbb{E}_{\mathbf{prior}}[\Sigma_k] = 0.2I_D$$

```
show_many_random_initial_models(
    dict(sF=0.2, ECovMat='eye'),
    dict(initname='randexamples', K=8))
```

initname: 'bregmankmeans'

This procedure selects K examples using a distance-biased procedure. First, one example is chosen uniformly at random. Next, each successive example is chosen with probability proportional to the distance from the nearest example in the chosen set.

We measure distance using the appropriate Bregman divergence.

Example 1: Initialize with 8 clusters, with prior biased towards small covariances

```
show_many_random_initial_models(
    dict(sF=0.01, ECovMat='eye'),
    dict(initname='bregmankmeans', K=8, init_NiterForBregmankMeans=0))
```

Example 2: Initialize as above, then allow the k-means algorithm to run for 10 iterations to "refine" the initial clustering.

```
show_many_random_initial_models(
    dict(sF=0.01, ECovMat='eye'),
    dict(initname='bregmankmeans', K=8, init_NiterForBregmanKMeans=10))
```

Total running time of the script: (0 minutes 4.934 seconds)

Download Python source code: plot-01-demo=init_methods-model=mix+gauss.py

Download Jupyter notebook: plot-01-demo=init_methods-model=mix+gauss.ipynb

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Variational with birth and merge proposals for DP mixtures of Gaussians

How to train a DP mixture model.

We'll show that despite diverse, poor quality initializations, our proposal moves that insert new clusters (birth) and remove redundant clusters (merge) can consistently recover the same ideal posterior with 8 clusters.

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns
# sphinx_gallery_thumbnail_number = 2

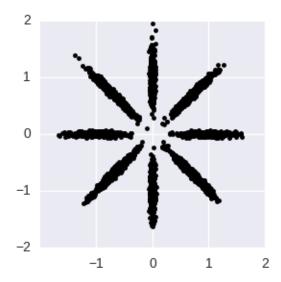
FIG_SIZE = (3, 3)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'AsteriskK8')
dataset = bnpy.data.XData.read_npz(
    os.path.join(dataset_path, 'x_dataset.npz'))
```

Make a simple plot of the raw data

```
pylab.plot(dataset.X[:, 0], dataset.X[:, 1], 'k.')
pylab.gca().set_xlim([-2, 2])
pylab.gca().set_ylim([-2, 2])
pylab.tight_layout()
```



Setup: Function for visualization

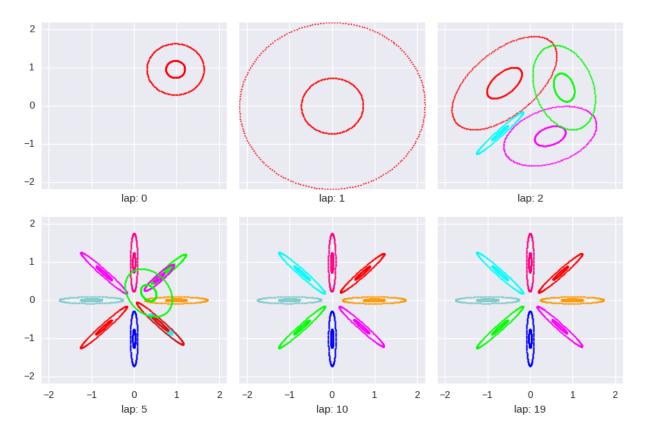
Here's a short function to show the learned clusters over time.

```
def show_clusters_over_time(
        task_output_path=None,
        query_laps=[0, 1, 2, 5, 10, None],
        nrows=2):
    ''' Read model snapshots from provided folder and make visualizations
    Post Condition
    New matplotlib plot with some nice pictures.
   ncols = int(np.ceil(len(query_laps) // float(nrows)))
    fig_handle, ax_handle_list = pylab.subplots(
        figsize=(FIG_SIZE[0] * ncols, FIG_SIZE[1] * nrows),
        nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for plot_id, lap_val in enumerate(query_laps):
        cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
        # Plot the current model
        cur_ax_handle = ax_handle_list.flatten()[plot_id]
        bnpy.viz.PlotComps.plotCompsFromHModel(
            cur_model, Data=dataset, ax_handle=cur_ax_handle)
        cur_ax_handle.set_xticks([-2, -1, 0, 1, 2])
        cur_ax_handle.set_yticks([-2, -1, 0, 1, 2])
        cur_ax_handle.set_xlabel("lap: %d" % lap_val)
   pylab.tight_layout()
```

Training from K=1 cluster

Using 1 initial cluster, with birth and merge proposal moves.

```
K1_trained_model, K1_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Gauss', 'memoVB',
    output_path='/tmp/AsteriskK8/trymoves-K=1/',
    nLap=100, nTask=1, nBatch=1,
    sF=0.1, ECovMat='eye',
    K=1, initname='randexamples',
    moves='birth,merge,shuffle',
    m_startLap=5, b_startLap=2, b_Kfresh=4)
show_clusters_over_time(K1_info_dict['task_output_path'])
```



Out:

```
Dataset Summary:
X Data
 total size: 5000 units
 batch size: 5000 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 1.00
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior: Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [ 0. 0.]
 E[covar[k]] =
 [[ 0.1 0. ]
  [ 0. 0.1]]
Initialization:
 initname = randexamples
 K = 1 (number of clusters)
 seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/AsteriskK8/trymoves-K=1/1
BIRTH @ lap 1.00: Disabled. Waiting for lap >= 2 (--b_startLap).
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent wi
   1.000/100 after 0 sec. | 131.5 MiB | K 1 | loss 1.105578508e+00 |
MERGE @ lap 2.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 2.00 : Added 4 states. 1/1 succeeded. 0/1 failed eval phase. 0/1 failed build
```

```
0 sec. | 131.6 MiB | K 5 | loss 7.390275336e-01 |
   2.000/100 after
MERGE @ lap 3.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 3.00 : Added 12 states. 3/4 succeeded. 1/4 failed eval phase. 0/4 failed build
   3.000/100 after
                    1 sec. | 131.6 MiB | K 17 | loss 2.819339824e-02 |
MERGE @ lap 4.00: Disabled. Waiting for lap \geq 5 (--m startLap).
BIRTH @ lap 4.00 : Added 0 states. 0/12 succeeded. 10/12 failed eval phase. 2/12 failed but
                    2 sec. | 131.6 MiB | K 17 | loss -1.240759022e-02 | Ndiff
   4.000/100 after
BIRTH @ lap 5.000 : None attempted. 0 past failures. 0 too small. 17 too busy.
MERGE @ lap 5.00 : 4/30 accepted. Ndiff 98.67. 10 skipped.
   5.000/100 after 2 sec. | 131.6 MiB | K 13 | loss -2.742336056e-02 | Ndiff
BIRTH @ lap 6.000 : None attempted. 0 past failures. 0 too small. 13 too busy.
MERGE @ lap 6.00 : 3/23 accepted. Ndiff 767.62. 5 skipped.
   6.000/100 after 3 sec. | 131.6 MiB | K 10 | loss -4.626686932e-02 | Ndiff
BIRTH @ lap 7.000 : None attempted. 0 past failures. 0 too small. 10 too busy.
MERGE @ lap 7.00 : 0/18 accepted. Ndiff 0.00. 0 skipped.
   7.000/100 after
                    3 sec. | 131.6 MiB | K 10 | loss -4.686532682e-02 | Ndiff
BIRTH @ lap 8.00 : Added 0 states. 0/2 succeeded. 2/2 failed eval phase. 0/2 failed build
MERGE @ lap 8.00 : 2/2 accepted. Ndiff 0.09. 5 skipped.
   8.000/100 after 3 sec. | 131.6 MiB | K 8 | loss -4.769229049e-02 | Ndiff
BIRTH @ lap 9.00 : Added 0 states. 0/1 succeeded. 1/1 failed eval phase. 0/1 failed build
MERGE @ lap 9.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
   9.000/100 after 3 sec. | 131.6 MiB | K 8 | loss -4.787962424e-02 | Ndiff
BIRTH @ lap 10.000 : None attempted. 0 past failures. 0 too small. 8 too busy.
MERGE @ lap 10.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
   10.000/100 after
                      4 sec. | 131.6 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 11.00 : Added 0 states. 0/1 succeeded. 1/1 failed eval phase. 0/1 failed build
MERGE @ lap 11.00 : 0/5 accepted. Ndiff 0.00. 0 skipped.
  11.000/100 after 4 sec. | 131.6 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 12.00 : Added 0 states. 0/1 succeeded. 1/1 failed eval phase. 0/1 failed build
MERGE @ lap 12.00 : 0/4 accepted. Ndiff 0.00. 0 skipped.
  12.000/100 after 4 sec. | 131.6 MiB | K
                                                 8 | loss -4.787962433e-02 | Ndiff
MERGE @ lap 13.00: No promising candidates, so no attempts.
BIRTH @ lap 13.000 : None attempted. 8 past failures. 0 too small. 0 too busy.
  13.000/100 after 4 sec. | 131.6 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 14.000 : None attempted. 2 past failures. 0 too small. 6 too busy.
MERGE @ lap 14.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
   14.000/100 after 4 sec. | 131.6 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 15.000 : None attempted. 0 past failures. 0 too small. 8 too busy.
MERGE @ lap 15.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  15.000/100 after 4 sec. | 131.6 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 16.000 : None attempted. 1 past failures. 0 too small. 7 too busy.
MERGE @ lap 16.00 : 0/5 accepted. Ndiff 0.00. 0 skipped.
  16.000/100 after 5 sec. | 131.6 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 17.000 : None attempted. 3 past failures. 0 too small. 5 too busy.
MERGE @ lap 17.00 : 0/4 accepted. Ndiff 0.00. 0 skipped.
  17.000/100 after
                    5 sec. | 131.6 MiB | K
                                                 8 | loss -4.787962433e-02 | Ndiff
MERGE @ lap 18.00: No promising candidates, so no attempts.
BIRTH @ lap 18.000 : None attempted. 8 past failures. 0 too small. 0 too busy.
  18.000/100 after 5 sec. | 131.6 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 19.000 : None attempted. 2 past failures. 0 too small. 6 too busy.
MERGE @ lap 19.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
  19.000/100 after 5 sec. | 131.6 MiB | K 8 | loss -4.787962433e-02 | Ndiff
... done. converged.
```

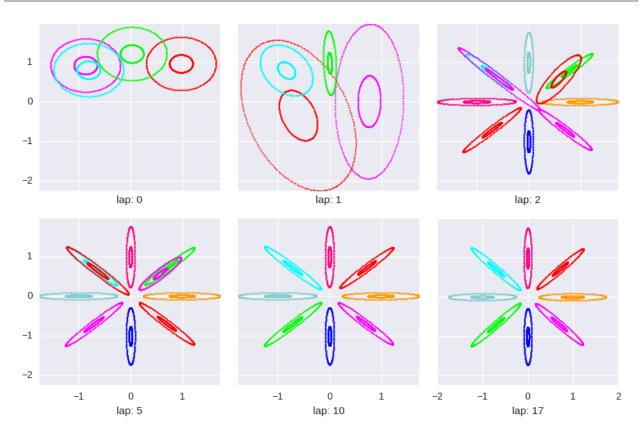
```
SKIPPED 1 comps with size below 0.00
SKIPPED 2 comps with size below 0.00
```

Training from K=4 cluster

Now using 4 initial clusters, with birth and merge proposal moves.

```
K4_trained_model, K4_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Gauss', 'memoVB',
    output_path='/tmp/AsteriskK8/trymoves-K=4/',
    nLap=100, nTask=1, nBatch=1,
    sF=0.1, ECovMat='eye',
    K=4, initname='randexamples',
    moves='birth,merge,shuffle',
    m_startLap=5, b_startLap=2, b_Kfresh=4)

show_clusters_over_time(K4_info_dict['task_output_path'])
```



Out:

```
Dataset Summary:
X Data
total size: 5000 units
batch size: 5000 units
num. batches: 1
```

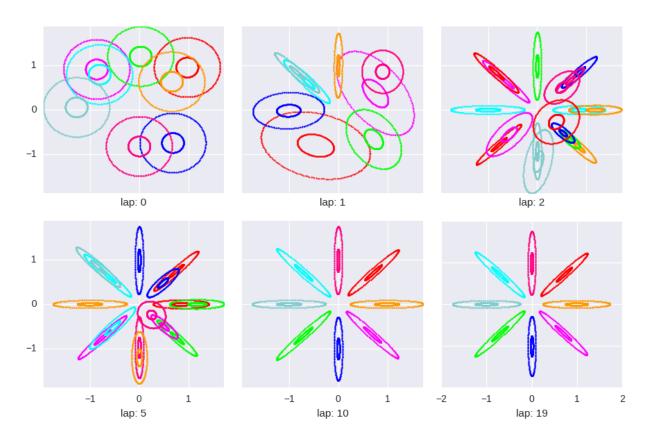
```
Allocation Model: DP mixture with K=0. Concentration gamma0= 1.00
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior: Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [ 0. 0.]
 E[covar[k]] =
 [[ 0.1 0. ]
  [ 0. 0.1]]
Initialization:
 initname = randexamples
 K = 4 (number of clusters)
 seed = 1607680
 elapsed time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/AsteriskK8/trymoves-K=4/1
BIRTH @ lap 1.00: Disabled. Waiting for lap >= 2 (--b_startLap).
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent w
   1.000/100 after
                       0 sec. | 130.2 MiB | K 4 | loss 9.001549009e-01 |
MERGE @ lap 2.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 2.00 : Added 8 states. 2/4 succeeded. 2/4 failed eval phase. 0/4 failed build
                     0 sec. | 130.2 MiB | K 12 | loss 6.597743621e-03 |
    2.000/100 after
MERGE @ lap 3.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 3.00 : Added 0 states. 0/9 succeeded. 9/9 failed eval phase. 0/9 failed build
   3.000/100 after
                     1 sec. | 130.2 MiB | K 12 | loss -2.949554282e-02 | Ndiff
MERGE @ lap 4.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 4.00 : Added 0 states. 0/3 succeeded. 3/3 failed eval phase. 0/3 failed build
    4.000/100 after 2 sec. | 130.2 MiB | K 12 | loss -3.255430235e-02 | Ndiff
BIRTH @ lap 5.000 : None attempted. 0 past failures. 0 too small. 12 too busy.
MERGE @ lap 5.00 : 2/25 accepted. Ndiff 0.00. 5 skipped.
    5.000/100 after
                     2 sec. | 130.2 MiB | K 10 | loss -3.311213517e-02 | Ndiff
BIRTH @ lap 6.000 : None attempted. 1 past failures. 0 too small. 9 too busy.
MERGE @ lap 6.00 : 2/17 accepted. Ndiff 417.46. 3 skipped.
                      2 sec. | 130.2 MiB | K 8 | loss -4.787665915e-02 | Ndiff
    6.000/100 after
BIRTH @ lap 7.000 : None attempted. O past failures. O too small. 8 too busy.
MERGE @ lap 7.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
    7.000/100 after 3 sec. | 130.2 MiB | K 8 | loss -4.787962431e-02 | Ndiff
BIRTH @ lap 8.00 : Added 0 states. 0/1 succeeded. 1/1 failed eval phase. 0/1 failed build
MERGE @ lap 8.00 : 0/2 accepted. Ndiff 0.00. 0 skipped.
   8.000/100 after
                     3 sec. |
                                  130.2 MiB | K
                                                  8 | loss -4.787962433e-02 | Ndiff
MERGE @ lap 9.00: No promising candidates, so no attempts.
BIRTH @ lap 9.00 : Added 0 states. 0/1 succeeded. 1/1 failed eval phase. 0/1 failed build
                        3 sec. | 130.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
    9.000/100 after
BIRTH @ lap 10.000 : None attempted. 1 past failures. 0 too small. 7 too busy.
MERGE @ lap 10.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
   10.000/100 after 3 sec. | 130.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 11.000 : None attempted. 2 past failures. 0 too small. 6 too busy.
MERGE @ lap 11.00 : 0/8 accepted. Ndiff 0.00. 0 skipped.
  11.000/100 after
                      3 sec. | 130.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 12.000 : None attempted. 0 past failures. 0 too small. 8 too busy.
MERGE @ lap 12.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
  12.000/100 after 4 sec. | 130.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 13.000 : None attempted. 5 past failures. 0 too small. 3 too busy.
MERGE @ lap 13.00 : 0/2 accepted. Ndiff 0.00. 0 skipped.
```

```
13.000/100 after
                                   130.2 MiB | K
                                                    8 | loss -4.787962433e-02 | Ndiff
                        4 sec. |
MERGE @ lap 14.00: No promising candidates, so no attempts.
BIRTH @ lap 14.000 : None attempted. 8 past failures. 0 too small. 0 too busy.
                       4 sec. | 130.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
  14.000/100 after
BIRTH @ lap 15.000 : None attempted. 1 past failures. 0 too small. 7 too busy.
MERGE @ lap 15.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
   15.000/100 after 4 sec. | 130.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 16.000 : None attempted. 2 past failures. 0 too small. 6 too busy.
MERGE @ lap 16.00 : 0/8 accepted. Ndiff 0.00. 0 skipped.
  16.000/100 after
                     4 sec. | 130.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 17.000 : None attempted. 0 past failures. 0 too small. 8 too busy.
MERGE @ lap 17.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
  17.000/100 after
                       4 sec. | 130.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
... done. converged.
SKIPPED 2 comps with size below 0.00
```

Training from K=8 cluster

Now using 8 initial clusters

```
K8_trained_model, K8_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Gauss', 'memoVB',
    output_path='/tmp/AsteriskK8/trymoves-K=8/',
    nLap=100, nTask=1, nBatch=1,
    sF=0.1, ECovMat='eye',
    K=8, initname='randexamples',
    moves='birth,merge,shuffle',
    m_startLap=5, b_startLap=2, b_Kfresh=4)
show_clusters_over_time(K8_info_dict['task_output_path'])
```



Out:

```
Dataset Summary:
X Data
 total size: 5000 units
 batch size: 5000 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 1.00
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior: Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [ 0. 0.]
 E[covar[k]] =
 [[ 0.1 0. ]
  [ 0. 0.1]]
Initialization:
 initname = randexamples
 K = 8 (number of clusters)
 seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/AsteriskK8/trymoves-K=8/1
BIRTH @ lap 1.00: Disabled. Waiting for lap >= 2 (--b_startLap).
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent wi
   1.000/100 after
                     0 sec. | 132.3 MiB | K 8 | loss 6.479391366e-01 |
MERGE @ lap 2.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 2.00 : Added 12 states. 3/8 succeeded. 5/8 failed eval phase. 0/8 failed build
```

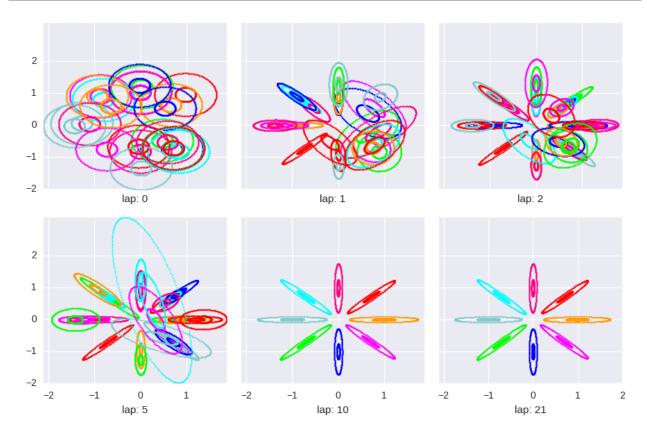
```
2.000/100 after 1 sec. | 132.4 MiB | K 20 | loss 7.345925210e-02 |
MERGE @ lap 3.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 3.00 : Added 0 states. 0/13 succeeded. 8/13 failed eval phase. 5/13 failed bui
                     2 sec. | 132.4 MiB | K 20 | loss 1.384405895e-02 | Ndiff
   3.000/100 after
MERGE @ lap 4.00: Disabled. Waiting for lap \geq 5 (--m startLap).
BIRTH @ lap 4.00 : Added 0 states. 0/12 succeeded. 8/12 failed eval phase. 4/12 failed bui.
                     3 sec. | 132.4 MiB | K 20 | loss 1.057016337e-02 | Ndiff
   4.000/100 after
BIRTH @ lap 5.000 : None attempted. 0 past failures. 0 too small. 20 too busy.
MERGE @ lap 5.00 : 4/41 accepted. Ndiff 635.65. 6 skipped.
   5.000/100 after 4 sec. | 132.4 MiB | K 16 | loss -3.619883330e-03 | Ndiff
BIRTH @ lap 6.000 : None attempted. 0 past failures. 0 too small. 16 too busy.
MERGE @ lap 6.00 : 4/26 accepted. Ndiff 459.69. 10 skipped.
   6.000/100 after 5 sec. | 132.4 MiB | K 12 | loss -2.198388303e-02 | Ndiff
BIRTH @ lap 7.000 : None attempted. 0 past failures. 0 too small. 12 too busy.
MERGE @ lap 7.00 : 3/21 accepted. Ndiff 366.43. 7 skipped.
   7.000/100 after
                    5 sec. | 132.4 MiB | K 9 | loss -4.222694604e-02 | Ndiff
BIRTH @ lap 8.000 : None attempted. 1 past failures. 0 too small. 8 too busy.
MERGE @ lap 8.00 : 1/16 accepted. Ndiff 75.14. 1 skipped.
   8.000/100 after 5 sec. | 132.4 MiB | K 8 | loss -4.787951351e-02 | Ndiff
BIRTH @ lap 9.00 : Added 0 states. 0/1 succeeded. 1/1 failed eval phase. 0/1 failed build
MERGE @ lap 9.00 : 0/7 accepted. Ndiff 0.00. 0 skipped.
   9.000/100 after 6 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 10.00 : Added 0 states. 0/4 succeeded. 4/4 failed eval phase. 0/4 failed build
MERGE @ lap 10.00 : 0/3 accepted. Ndiff 0.00. 0 skipped.
   10.000/100 after 6 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 11.00 : Added 0 states. 0/1 succeeded. 1/1 failed eval phase. 0/1 failed build
MERGE @ lap 11.00 : 0/2 accepted. Ndiff 0.00. 0 skipped.
  11.000/100 after 6 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 12.000 : None attempted. 3 past failures. 0 too small. 5 too busy.
MERGE @ lap 12.00 : 0/5 accepted. Ndiff 0.00. 0 skipped.
  12.000/100 after 6 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 13.000 : None attempted. 1 past failures. 0 too small. 7 too busy.
MERGE @ lap 13.00 : 0/11 accepted. Ndiff 0.00. 0 skipped.
  13.000/100 after 6 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 14.000 : None attempted. 1 past failures. 0 too small. 7 too busy.
MERGE @ lap 14.00 : 0/7 accepted. Ndiff 0.00. 0 skipped.
   14.000/100 after 7 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 15.000 : None attempted. 5 past failures. 0 too small. 3 too busy.
MERGE @ lap 15.00 : 0/3 accepted. Ndiff 0.00. 0 skipped.
  15.000/100 after 7 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 16.000 : None attempted. 5 past failures. 0 too small. 3 too busy.
MERGE @ lap 16.00 : 0/2 accepted. Ndiff 0.00. 0 skipped.
  16.000/100 after 7 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 17.000 : None attempted. 3 past failures. 0 too small. 5 too busy.
MERGE @ lap 17.00 : 0/5 accepted. Ndiff 0.00. 0 skipped.
  17.000/100 after
                    7 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 18.000 : None attempted. 1 past failures. 0 too small. 7 too busy.
MERGE @ lap 18.00 : 0/11 accepted. Ndiff 0.00. 0 skipped.
   18.000/100 after 7 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 19.000 : None attempted. 1 past failures. 0 too small. 7 too busy.
MERGE @ lap 19.00 : 0/7 accepted. Ndiff 0.00. 0 skipped.
  19.000/100 after 7 sec. | 132.4 MiB | K 8 | loss -4.787962433e-02 | Ndiff
... done. converged.
```

```
SKIPPED 3 comps with size below 0.00
SKIPPED 1 comps with size below 0.00
```

Training from K=25 cluster

Now using 25 initial clusters

```
K25_trained_model, K25_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Gauss', 'memoVB',
    output_path='/tmp/AsteriskK8/trymoves-K=25/',
    nLap=100, nTask=1, nBatch=1,
    sF=0.1, ECovMat='eye',
    K=25, initname='randexamples',
    moves='birth,merge,shuffle',
    m_startLap=5, b_startLap=2, b_Kfresh=4)
show_clusters_over_time(K25_info_dict['task_output_path'])
```



Out:

```
Dataset Summary:
X Data
total size: 5000 units
batch size: 5000 units
num. batches: 1
```

```
Allocation Model: DP mixture with K=0. Concentration gamma0= 1.00
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior: Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [ 0. 0.]
 E[covar[k]] =
 [[ 0.1 0. ]
  [ 0. 0.1]]
Initialization:
 initname = randexamples
 K = 25 (number of clusters)
 seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/AsteriskK8/trymoves-K=25/1
BIRTH @ lap 1.00: Disabled. Waiting for lap >= 2 (--b_startLap).
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent w
   1.000/100 after
                     0 sec. | 132.2 MiB | K 25 | loss 4.392317798e-01 |
MERGE @ lap 2.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 2.00 : Added 14 states. 4/18 succeeded. 11/18 failed eval phase. 3/18 failed by
                     2 sec. | 132.2 MiB | K 39 | loss 1.219944497e-01 |
   2.000/100 after
MERGE @ lap 3.00: Disabled. Waiting for lap \geq 5 (--m_startLap).
BIRTH @ lap 3.00 : Added 0 states. 0/15 succeeded. 3/15 failed eval phase. 12/15 failed but
   3.000/100 after
                    3 sec. | 135.2 MiB | K 39 | loss 8.910722771e-02 | Ndiff
MERGE @ lap 4.00: Disabled. Waiting for lap >= 5 (--m_startLap).
BIRTH @ lap 4.00 : Added 0 states. 0/15 succeeded. 9/15 failed eval phase. 6/15 failed bui.
   4.000/100 after 5 sec. | 135.2 MiB | K 39 | loss 8.017398425e-02 | Ndiff
BIRTH @ lap 5.000 : None attempted. 0 past failures. 0 too small. 39 too busy.
MERGE @ lap 5.00 : 8/63 accepted. Ndiff 338.97. 32 skipped.
   5.000/100 after
                   7 sec. | 135.2 MiB | K 31 | loss 5.747324378e-02 | Ndiff
BIRTH @ lap 6.000 : None attempted. 0 past failures. 0 too small. 31 too busy.
MERGE @ lap 6.00 : 10/39 accepted. Ndiff 1032.92. 38 skipped.
   6.000/100 after 8 sec. | 135.2 MiB | K 21 | loss 1.309182046e-02 | Ndiff
BIRTH @ lap 7.000 : None attempted. 0 past failures. 0 too small. 21 too busy.
MERGE @ lap 7.00 : 5/35 accepted. Ndiff 323.06. 14 skipped.
   7.000/100 after
                     9 sec. | 135.2 MiB | K 16 | loss -8.888342290e-03 | Ndiff
BIRTH @ lap 8.000 : None attempted. 0 past failures. 0 too small. 16 too busy.
MERGE @ lap 8.00 : 4/24 accepted. Ndiff 443.50. 12 skipped.
   8.000/100 after
                    9 sec. |
                                135.2 MiB | K 12 | loss -3.261743488e-02 | Ndiff
BIRTH @ lap 9.000 : None attempted. 0 past failures. 0 too small. 12 too busy.
MERGE @ lap 9.00 : 3/22 accepted. Ndiff 185.39. 7 skipped.
   9.000/100 after 10 sec. | 135.2 MiB | K 9 | loss -4.523238984e-02 | Ndiff
BIRTH @ lap 10.00 : Added 0 states. 0/1 succeeded. 1/1 failed eval phase. 0/1 failed build
MERGE @ lap 10.00 : 1/13 accepted. Ndiff 1.72. 1 skipped.
  BIRTH @ lap 11.00 : Added 0 states. 0/3 succeeded. 3/3 failed eval phase. 0/3 failed build
MERGE @ lap 11.00 : 0/4 accepted. Ndiff 0.00. 0 skipped.
  8 | loss -4.787962433e-02 | Ndiff
MERGE @ lap 12.00: No promising candidates, so no attempts.
BIRTH @ lap 12.00 : Added 0 states. 0/3 succeeded. 3/3 failed eval phase. 0/3 failed build
  BIRTH @ lap 13.000 : None attempted. 3 past failures. 0 too small. 5 too busy.
MERGE @ lap 13.00 : 0/4 accepted. Ndiff 0.00. 0 skipped.
```

```
13.000/100 after
                                    135.2 MiB | K
                                                     8 | loss -4.787962433e-02 | Ndiff
                       11 sec. |
BIRTH @ lap 14.000 : None attempted. 2 past failures. 0 too small. 6 too busy.
MERGE @ lap 14.00 : 0/11 accepted. Ndiff 0.00. 0 skipped.
                                    135.2 MiB | K
                       11 sec. |
                                                     8 | loss -4.787962433e-02 | Ndiff
  14.000/100 after
BIRTH @ lap 15.000 : None attempted. 2 past failures. 0 too small. 6 too busy.
MERGE @ lap 15.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
   15.000/100 after
                       11 sec. |
                                   135.2 MiB | K
                                                    8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 16.000 : None attempted. 4 past failures. 0 too small. 4 too busy.
MERGE @ lap 16.00 : 0/4 accepted. Ndiff 0.00. 0 skipped.
                                   135.2 MiB | K
  16.000/100 after
                       11 sec. |
                                                     8 | loss -4.787962433e-02 | Ndiff
MERGE @ lap 17.00: No promising candidates, so no attempts.
BIRTH @ lap 17.000 : None attempted. 8 past failures. 0 too small. 0 too busy.
  17.000/100 after
                       11 sec. |
                                   135.2 MiB | K
                                                     8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 18.000 : None attempted. 3 past failures. 0 too small. 5 too busy.
MERGE @ lap 18.00 : 0/4 accepted. Ndiff 0.00. 0 skipped.
  18.000/100 after
                       11 sec. |
                                   135.2 MiB | K
                                                     8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 19.000 : None attempted. 2 past failures. 0 too small. 6 too busy.
MERGE @ lap 19.00 : 0/11 accepted. Ndiff 0.00. 0 skipped.
   19.000/100 after
                       12 sec. | 135.2 MiB | K
                                                     8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 20.000 : None attempted. 2 past failures. 0 too small. 6 too busy.
MERGE @ lap 20.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
  20.000/100 after
                       12 sec. | 135.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
BIRTH @ lap 21.000 : None attempted. 4 past failures. 0 too small. 4 too busy.
MERGE @ lap 21.00 : 0/4 accepted. Ndiff 0.00. 0 skipped.
   21.000/100 after
                       12 sec. |
                                   135.2 MiB | K 8 | loss -4.787962433e-02 | Ndiff
... done. converged.
SKIPPED 4 comps with size below 0.00
SKIPPED 3 comps with size below 0.00
```

Total running time of the script: (0 minutes 32.509 seconds)

```
Download Python source code: plot-03-demo=vb+proposals-model=dp_mix+gauss.py

Download Jupyter notebook: plot-03-demo=vb+proposals-model=dp_mix+gauss.ipynb

Generated by Sphinx-Gallery
```

5.2.2 Standard Normal dataset

Variational training of DP mixture models on thousands of points from a single 1D Gaussian with mean 0 and variance 1.

Variational with merge and delete proposals for DP mixtures of Gaussians

How delete moves can be more effective than merges.

In this example, we show how merge moves alone may not be enough to reliably escape local optima. Instead, we show that more flexible delete moves can escape from situations where merges alone fail.

```
import bnpy
import numpy as np
import os
```

```
from matplotlib import pylab
import seaborn as sns

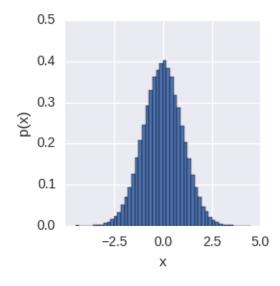
FIG_SIZE = (3, 3)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Create toy dataset of many points drawn from standard normal

```
prng = np.random.RandomState(42)
X = prng.randn(100000, 1)
dataset = bnpy.data.XData(X, name='StandardNormalK1')
```

Make a simple plot of the raw data

```
pylab.hist(dataset.X[:, 0], 50, normed=1)
pylab.xlabel('x')
pylab.ylabel('p(x)')
pylab.tight_layout()
```



Setup: Determine specific settings of the proposals

```
merge_kwargs = dict(
    m_startLap=10,
    m_pair_ranking_procedure='total_size',
    m_pair_ranking_direction='descending',
    )

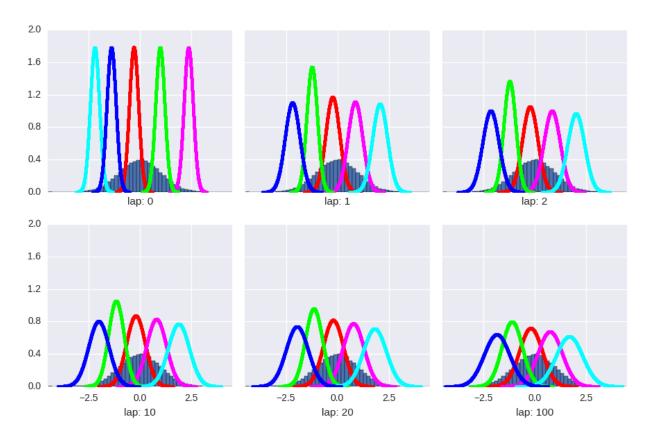
delete_kwargs = dict(
    d_startLap=10,
    d_nRefineSteps=50,
    )
```

Setup: Helper function to display the learned clusters

```
def show_clusters_over_time(
        task_output_path=None,
        query_laps=[0, 1, 2, 10, 20, None],
        nrows=2):
    I = I = I
    ncols = int(np.ceil(len(query_laps) // float(nrows)))
    fig_handle, ax_handle_list = pylab.subplots(
        figsize=(FIG SIZE[0] * ncols, FIG SIZE[1] * nrows),
        nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for plot_id, lap_val in enumerate(query_laps):
        cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
        cur_ax_handle = ax_handle_list.flatten()[plot_id]
        bnpy.viz.PlotComps.plotCompsFromHModel(
            cur_model, dataset=dataset, ax_handle=cur_ax_handle)
        cur_ax_handle.set_xlim([-4.5, 4.5])
        cur_ax_handle.set_xlabel("lap: %d" % lap_val)
   pylab.tight_layout()
```

Run with merge moves only, from K=5 initial clusters

Unfortunately, no pairwise merge is accepted. The model is stuck using 5 clusters when one cluster would do.



```
Dataset Summary:
X Data
 total size: 100000 units
 batch size: 100000 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior: Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [.0.]
 E[covar[k]] =
 [[ 0.1]]
Initialization:
 initname = randexamplesbydist
 K = 5 (number of clusters)
 seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/StandardNormalK1/trymoves-K=5-gamma=5.0-ECovMat=0.1*eye-moves=merge
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent wi
                                                    5 | loss 1.547776525e+00 |
   1.000/100 after
                        0 sec. | 143.8 MiB | K
MERGE @ lap 2.00: Disabled. Waiting for lap >= 10 (--m_startLap).
    2.000/100 after 0 sec. |
                                   143.8 MiB | K
                                                    5 | loss
                                                              1.446186110e+00 | Ndiff 2.
MERGE @ lap 3.00: Disabled. Waiting for lap >= 10 (--m_startLap).
   3.000/100 after
                        0 sec. |
                                   143.8 MiB | K
                                                     5 | loss 1.434177601e+00
                                                                              | Ndiff 1:
```

```
MERGE @ lap 4.00: Disabled. Waiting for lap >= 10 (--m_startLap).
   4.000/100 after 0 sec. | 143.8 MiB | K 5 | loss 1.429642157e+00 | Ndiff
MERGE @ lap 5.00: Disabled. Waiting for lap >= 10 (--m_startLap).
   5.000/100 after 0 sec. | 143.8 MiB | K 5 | loss 1.427329685e+00 | Ndiff
MERGE @ lap 6.00: Disabled. Waiting for lap >= 10 (--m_startLap).
   6.000/100 after 1 sec. | 143.8 MiB | K 5 | loss 1.425951747e+00 | Ndiff
MERGE @ lap 7.00: Disabled. Waiting for lap >= 10 (--m_startLap).
   7.000/100 after 1 sec. | 143.8 MiB | K 5 | loss 1.425047267e+00 | Ndiff
MERGE @ lap 8.00: Disabled. Waiting for lap >= 10 (--m_startLap).
   8.000/100 after 1 sec. | 143.8 MiB | K 5 | loss 1.424412975e+00 | Ndiff
MERGE @ lap 9.00: Disabled. Waiting for lap >= 10 (--m_startLap).
   MERGE @ lap 10.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  10.000/100 after 1 sec. | 143.8 MiB | K 5 | loss 1.423589980e+00 | Ndiff
MERGE @ lap 11.00: No promising candidates, so no attempts.
  11.000/100 after 1 sec. | 143.8 MiB | K 5 | loss
                                                         1.423310120e+00 | Ndiff
MERGE @ lap 12.00: No promising candidates, so no attempts.
  12.000/100 after 1 sec. | 143.8 MiB | K
                                                5 | loss
                                                          1.423085107e+00 | Ndiff
MERGE @ lap 13.00: No promising candidates, so no attempts.
  13.000/100 after 1 sec. | 143.8 MiB | K
                                                 5 | loss 1.422900698e+00 | Ndiff
MERGE @ lap 14.00: No promising candidates, so no attempts.
  14.000/100 after 1 sec. | 143.8 MiB | K 5 | loss 1.422747120e+00 | Ndiff
MERGE @ lap 15.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  15.000/100 after 2 sec. | 143.8 MiB | K
                                              5 | loss
                                                         1.422617464e+00 | Ndiff
MERGE @ lap 16.00: No promising candidates, so no attempts.
  16.000/100 after 2 sec. | 143.8 MiB | K
                                                 5 | loss
                                                         1.422506710e+00 | Ndiff
MERGE @ lap 17.00: No promising candidates, so no attempts.
  17.000/100 after 2 sec. | 143.8 MiB | K
                                                 5 | loss 1.422411133e+00 | Ndiff
MERGE @ lap 18.00: No promising candidates, so no attempts.
  18.000/100 after 2 sec. | 143.8 MiB | K
                                               5 | loss
                                                         1.422327908e+00 | Ndiff
MERGE @ lap 19.00: No promising candidates, so no attempts.
  19.000/100 after 2 sec. | 143.8 MiB | K
                                                 5 | loss
                                                          1.422254864e+00 | Ndiff
MERGE @ lap 20.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  20.000/100 after 2 sec. | 143.8 MiB | K
                                                 5 | loss
                                                          1.422190300e+00 | Ndiff
MERGE @ lap 21.00: No promising candidates, so no attempts.
  21.000/100 after 2 sec. | 143.8 MiB | K
                                                 5 | loss 1.422132869e+00 | Ndiff
MERGE @ lap 22.00: No promising candidates, so no attempts.
  22.000/100 after 2 sec. | 143.8 MiB | K 5 | loss
                                                          1.422081490e+00 | Ndiff
MERGE @ lap 23.00: No promising candidates, so no attempts.
  23.000/100 after 2 sec. | 143.8 MiB | K
                                                 5 | loss
                                                          1.422035287e+00 | Ndiff
MERGE @ lap 24.00: No promising candidates, so no attempts.
  24.000/100 after 3 sec. | 143.8 MiB | K
                                                 5 | loss 1.421993542e+00 | Ndiff
MERGE @ lap 25.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  25.000/100 after 3 sec. | 143.8 MiB | K 5 | loss 1.421955661e+00 | Ndiff
MERGE @ lap 26.00: No promising candidates, so no attempts.
  26.000/100 after 3 sec. | 143.8 MiB | K 5 | loss
                                                          1.421921151e+00 | Ndiff
MERGE @ lap 27.00: No promising candidates, so no attempts.
  27.000/100 after 3 sec. | 143.8 MiB | K
                                                 5 | loss
                                                          1.421889597e+00 | Ndiff
MERGE @ lap 28.00: No promising candidates, so no attempts.
  28.000/100 after 3 sec. | 143.8 MiB | K
                                                 5 | loss 1.421860649e+00 | Ndiff
MERGE @ lap 29.00: No promising candidates, so no attempts.
  29.000/100 after 3 sec. | 143.8 MiB | K 5 | loss 1.421834007e+00 | Ndiff
MERGE @ lap 30.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
```

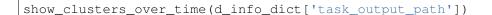
```
30.000/100 after 3 sec. | 143.8 MiB | K 5 | loss 1.421809418e+00 | Ndiff
MERGE @ lap 31.00: No promising candidates, so no attempts.
  31.000/100 after 3 sec. | 143.8 MiB | K
                                                 5 | loss 1.421786661e+00 | Ndiff
MERGE @ lap 32.00: No promising candidates, so no attempts.
  32.000/100 after 4 sec. | 143.8 MiB | K
                                                  5 | loss 1.421765547e+00 | Ndiff
MERGE @ lap 33.00: No promising candidates, so no attempts.
  33.000/100 after 4 sec. | 143.8 MiB | K 5 | loss
                                                           1.421745910e+00 | Ndiff
MERGE @ lap 34.00: No promising candidates, so no attempts.
  34.000/100 after 4 sec. | 143.8 MiB | K
                                                5 | loss
                                                           1.421727607e+00 | Ndiff
MERGE @ lap 35.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  35.000/100 after 4 sec. | 143.8 MiB | K
                                                 5 | loss
                                                           1.421710511e+00 | Ndiff
MERGE @ lap 36.00: No promising candidates, so no attempts.
  36.000/100 after 4 sec. | 143.8 MiB | K
                                                 5 | loss 1.421694512e+00 | Ndiff
MERGE @ lap 37.00: No promising candidates, so no attempts.
  37.000/100 after 4 sec. | 143.8 MiB | K 5 | loss
                                                           1.421679511e+00 | Ndiff
MERGE @ lap 38.00: No promising candidates, so no attempts.
  38.000/100 after 4 sec. | 143.8 MiB | K
                                                 5 | loss
                                                           1.421665422e+00 | Ndiff
MERGE @ lap 39.00: No promising candidates, so no attempts.
  39.000/100 after 4 sec. | 143.8 MiB | K
                                                  5 | loss 1.421652166e+00 | Ndiff
MERGE @ lap 40.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  40.000/100 after 4 sec. | 143.8 MiB | K 5 | loss 1.421639676e+00 | Ndiff
MERGE @ lap 41.00: No promising candidates, so no attempts.
  41.000/100 after 5 sec. | 143.8 MiB | K 5 | loss
                                                           1.421627889e+00 | Ndiff
MERGE @ lap 42.00: No promising candidates, so no attempts.
  42.000/100 after 5 sec. | 143.8 MiB | K
                                                 5 | loss
                                                           1.421616749e+00 | Ndiff
MERGE @ lap 43.00: No promising candidates, so no attempts.
  43.000/100 after 5 sec. | 143.8 MiB | K
                                                 5 | loss 1.421606208e+00 | Ndiff
MERGE @ lap 44.00: No promising candidates, so no attempts.
  44.000/100 after 5 sec. | 143.8 MiB | K 5 | loss 1.421596220e+00 | Ndiff
MERGE @ lap 45.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  45.000/100 after 5 sec. | 143.8 MiB | K 5 | loss
                                                           1.421586745e+00 | Ndiff
MERGE @ lap 46.00: No promising candidates, so no attempts.
  46.000/100 after 5 sec. | 143.8 MiB | K
                                                  5 | loss
                                                           1.421577745e+00 | Ndiff
MERGE @ lap 47.00: No promising candidates, so no attempts.
  47.000/100 after 5 sec. | 143.8 MiB | K
                                                  5 | loss 1.421569187e+00 | Ndiff
MERGE @ lap 48.00: No promising candidates, so no attempts.
  48.000/100 after 5 sec. | 143.8 MiB | K 5 | loss
                                                           1.421561041e+00 | Ndiff
MERGE @ lap 49.00: No promising candidates, so no attempts.
  49.000/100 after 5 sec. | 143.8 MiB | K
                                                5 | loss
                                                           1.421553280e+00 | Ndiff
MERGE @ lap 50.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  50.000/100 after 6 sec. | 143.8 MiB | K
                                                  5 | loss
                                                           1.421545876e+00 | Ndiff
MERGE @ lap 51.00: No promising candidates, so no attempts.
  51.000/100 after 6 sec. | 143.8 MiB | K
                                                 5 | loss 1.421538809e+00 | Ndiff
MERGE @ lap 52.00: No promising candidates, so no attempts.
  52.000/100 after 6 sec. | 143.8 MiB | K 5 | loss
                                                           1.421532055e+00 | Ndiff
MERGE @ lap 53.00: No promising candidates, so no attempts.
                                                 5 | loss
  53.000/100 after 6 sec. | 143.8 MiB | K
                                                           1.421525596e+00 | Ndiff
MERGE @ lap 54.00: No promising candidates, so no attempts.
  54.000/100 after 6 sec. | 143.8 MiB | K
                                                  5 | loss
                                                          1.421519413e+00 | Ndiff
MERGE @ lap 55.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  55.000/100 after 6 sec. | 143.8 MiB | K
                                                 5 | loss 1.421513490e+00 | Ndiff
MERGE @ lap 56.00: No promising candidates, so no attempts.
  56.000/100 after 6 sec. | 143.8 MiB | K 5 | loss 1.421507811e+00 | Ndiff
```

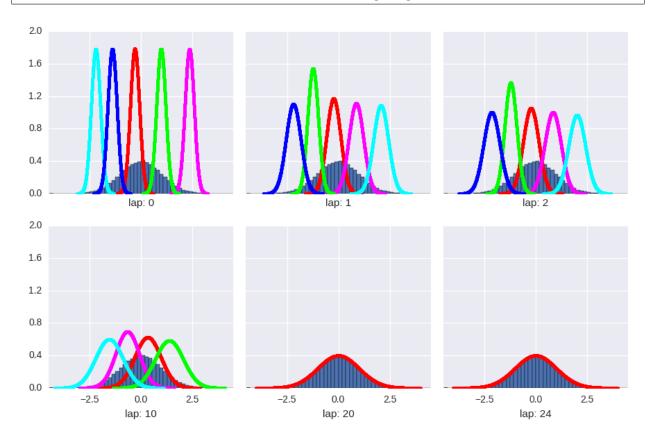
```
MERGE @ lap 57.00: No promising candidates, so no attempts.
  57.000/100 after 6 sec. | 143.8 MiB | K 5 | loss 1.421502363e+00 | Ndiff
MERGE @ lap 58.00: No promising candidates, so no attempts.
  58.000/100 after 6 sec. | 143.8 MiB | K
                                                  5 | loss
                                                           1.421497133e+00 | Ndiff
MERGE @ lap 59.00: No promising candidates, so no attempts.
  59.000/100 after 7 sec. | 143.8 MiB | K
                                                  5 | loss 1.421492107e+00 | Ndiff
MERGE @ lap 60.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  60.000/100 after 7 sec. | 143.8 MiB | K 5 | loss
                                                           1.421487275e+00 | Ndiff
MERGE @ lap 61.00: No promising candidates, so no attempts.
  61.000/100 after 7 sec. | 143.8 MiB | K
                                                  5 | loss
                                                            1.421482626e+00 | Ndiff
MERGE @ lap 62.00: No promising candidates, so no attempts.
  62.000/100 after 7 sec. | 143.8 MiB | K
                                                  5 | loss
                                                           1.421478151e+00 | Ndiff
MERGE @ lap 63.00: No promising candidates, so no attempts.
  63.000/100 after 7 sec. | 143.8 MiB | K
                                                  5 | loss 1.421473840e+00 | Ndiff
MERGE @ lap 64.00: No promising candidates, so no attempts.
  64.000/100 after 7 sec. | 143.8 MiB | K
                                                 5 | loss
                                                           1.421469686e+00 | Ndiff
MERGE @ lap 65.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  65.000/100 after 7 sec. | 143.8 MiB | K
                                                  5 | loss
                                                            1.421465679e+00 | Ndiff
MERGE @ lap 66.00: No promising candidates, so no attempts.
  66.000/100 after 7 sec. | 143.8 MiB | K
                                                  5 | loss 1.421461813e+00 | Ndiff
MERGE @ lap 67.00: No promising candidates, so no attempts.
  67.000/100 after 8 sec. | 143.8 MiB | K 5 | loss 1.421458080e+00 | Ndiff
MERGE @ lap 68.00: No promising candidates, so no attempts.
  68.000/100 after 8 sec. | 143.8 MiB | K
                                                5 | loss
                                                            1.421454475e+00 | Ndiff
MERGE @ lap 69.00: No promising candidates, so no attempts.
  69.000/100 after 8 sec. | 143.8 MiB | K
                                                  5 | loss
                                                           1.421450991e+00 | Ndiff
MERGE @ lap 70.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  70.000/100 after 8 sec. | 143.8 MiB | K
                                                  5 | loss 1.421447622e+00 | Ndiff
MERGE @ lap 71.00: No promising candidates, so no attempts.
  71.000/100 after 8 sec. | 143.8 MiB | K
                                                5 | loss
                                                           1.421444363e+00 | Ndiff
MERGE @ lap 72.00: No promising candidates, so no attempts.
  72.000/100 after 8 sec. | 143.8 MiB | K
                                                  5 | loss
                                                            1.421441210e+00 | Ndiff
MERGE @ lap 73.00: No promising candidates, so no attempts.
  73.000/100 after 8 sec. | 143.8 MiB | K
                                                  5 | loss
                                                            1.421438156e+00 | Ndiff
MERGE @ lap 74.00: No promising candidates, so no attempts.
  74.000/100 after 8 sec. | 143.8 MiB | K
                                                  5 | loss 1.421435198e+00 | Ndiff
MERGE @ lap 75.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  75.000/100 after 9 sec. | 143.8 MiB | K 5 | loss
                                                            1.421432332e+00 | Ndiff
MERGE @ lap 76.00: No promising candidates, so no attempts.
                                                  5 | loss
  76.000/100 after 9 sec. | 143.8 MiB | K
                                                            1.421429553e+00 | Ndiff
MERGE @ lap 77.00: No promising candidates, so no attempts.
  77.000/100 after 9 sec. | 143.8 MiB | K
                                                  5 | loss
                                                           1.421426858e+00 | Ndiff
MERGE @ lap 78.00: No promising candidates, so no attempts.
  78.000/100 after 9 sec. | 143.8 MiB | K
                                                  5 | loss 1.421424243e+00 | Ndiff
MERGE @ lap 79.00: No promising candidates, so no attempts.
  79.000/100 after 9 sec. | 143.8 MiB | K 5 | loss
                                                           1.421421705e+00 | Ndiff
MERGE @ lap 80.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  80.000/100 after 9 sec. | 143.8 MiB | K
                                                  5 | loss
                                                            1.421419241e+00 | Ndiff
MERGE @ lap 81.00: No promising candidates, so no attempts.
  81.000/100 after 9 sec. | 143.8 MiB | K
                                                  5 | loss 1.421416847e+00 | Ndiff
MERGE @ lap 82.00: No promising candidates, so no attempts.
  82.000/100 after 9 sec. | 143.8 MiB | K 5 | loss 1.421414521e+00 | Ndiff
MERGE @ lap 83.00: No promising candidates, so no attempts.
```

```
83.000/100 after 9 sec. | 143.8 MiB | K
                                               5 | loss 1.421412261e+00 | Ndiff
MERGE @ lap 84.00: No promising candidates, so no attempts.
  84.000/100 after 9 sec. | 143.8 MiB | K
                                                5 | loss 1.421410063e+00 | Ndiff
MERGE @ lap 85.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  85.000/100 after 10 sec. | 143.8 MiB | K
                                                5 | loss 1.421407925e+00 | Ndiff
MERGE @ lap 86.00: No promising candidates, so no attempts.
  86.000/100 after 10 sec. | 143.8 MiB | K
                                                5 | loss 1.421405845e+00 | Ndiff
MERGE @ lap 87.00: No promising candidates, so no attempts.
  87.000/100 after 10 sec. | 143.8 MiB | K
                                                         1.421403820e+00 | Ndiff
MERGE @ lap 88.00: No promising candidates, so no attempts.
  88.000/100 after 10 sec. | 143.8 MiB | K
                                                5 | loss 1.421401849e+00 | Ndiff
MERGE @ lap 89.00: No promising candidates, so no attempts.
  89.000/100 after 10 sec. | 143.8 MiB | K
                                                5 | loss 1.421399930e+00 | Ndiff
MERGE @ lap 90.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  90.000/100 after 10 sec. | 143.8 MiB | K
                                                5 | loss
                                                         1.421398060e+00 | Ndiff
MERGE @ lap 91.00: No promising candidates, so no attempts.
  91.000/100 after 10 sec. | 143.8 MiB | K
                                                5 | loss 1.421396238e+00 | Ndiff
MERGE @ lap 92.00: No promising candidates, so no attempts.
  92.000/100 after 10 sec. | 143.8 MiB | K
                                                5 | loss 1.421394462e+00 | Ndiff
MERGE @ lap 93.00: No promising candidates, so no attempts.
  5 | loss 1.421392731e+00 | Ndiff
MERGE @ lap 94.00: No promising candidates, so no attempts.
  94.000/100 after 11 sec. | 143.8 MiB | K
                                                5 | loss 1.421391043e+00 | Ndiff
MERGE @ lap 95.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  95.000/100 after 11 sec. | 143.8 MiB | K
                                                5 | loss 1.421389396e+00 | Ndiff
MERGE @ lap 96.00: No promising candidates, so no attempts.
  96.000/100 after 11 sec. | 143.8 MiB | K
                                                5 | loss 1.421387789e+00 | Ndiff
MERGE @ lap 97.00: No promising candidates, so no attempts.
  97.000/100 after 11 sec. | 143.8 MiB | K 5 | loss 1.421386221e+00 | Ndiff
MERGE @ lap 98.00: No promising candidates, so no attempts.
  98.000/100 after 11 sec. | 143.8 MiB | K
                                                5 | loss 1.421384690e+00 | Ndiff
MERGE @ lap 99.00: No promising candidates, so no attempts.
  99.000/100 after 11 sec. | 143.8 MiB | K
                                                5 | loss 1.421383195e+00 | Ndiff
MERGE @ lap 100.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
 5 | loss 1.421381735e+00 | Ndiff
... done. not converged. max laps thru data exceeded.
```

Run with *delete* moves, from K=5 initial clusters

More flexible delete moves are accepted.





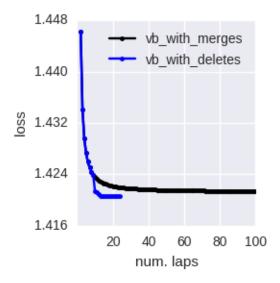
```
Dataset Summary:
X Data
 total size: 100000 units
 batch size: 100000 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior: Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [ 0.]
 E[covar[k]] =
 [[0.1]]
Initialization:
 initname = randexamplesbydist
 K = 5 (number of clusters)
 seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/StandardNormalK1/trymoves-K=5-gamma=5.0-ECovMat=0.1*eye-moves=delete
DELETE @ lap 1.00: Disabled. Cannot delete before first complete lap, because $S that repre
   1.000/100 after 0 sec. | 151.4 MiB | K 5 | loss 1.547776525e+00 |
DELETE @ lap 2.00: Disabled. Waiting for lap >= 10 (--d_startLap).
    2.000/100 after
                        0 sec. | 151.4 MiB | K
                                                     5 | loss 1.446186110e+00 | Ndiff 2.
```

```
DELETE @ lap 3.00: Disabled. Waiting for lap >= 10 (--d_startLap).
   3.000/100 after 0 sec. | 151.4 MiB | K 5 | loss 1.434177601e+00 | Ndiff 1
DELETE @ lap 4.00: Disabled. Waiting for lap >= 10 (--d_startLap).
   4.000/100 after 0 sec. | 151.4 MiB | K 5 | loss 1.429642157e+00 | Ndiff
DELETE @ lap 5.00: Disabled. Waiting for lap \geq 10 (--d_startLap).
   5.000/100 after 0 sec. | 151.4 MiB | K 5 | loss 1.427329685e+00 | Ndiff
DELETE @ lap 6.00: Disabled. Waiting for lap \geq 10 (--d_startLap).
   DELETE @ lap 7.00: Disabled. Waiting for lap >= 10 (--d_startLap).
   7.000/100 after 1 sec. | 151.4 MiB | K 5 | loss 1.425047267e+00 | Ndiff
DELETE @ lap 8.00: Disabled. Waiting for lap >= 10 (--d startLap).
   8.000/100 after 1 sec. | 151.4 MiB | K
                                                5 | loss 1.424412975e+00 | Ndiff
DELETE @ lap 9.00: Disabled. Waiting for lap >= 10 (--d_startLap).
   9.000/100 after 1 sec. | 151.4 MiB | K 5 | loss 1.423946233e+00 | Ndiff
DELETE @ lap 10.00: 1/1 accepted. Ndiff 43526.74.
  10.000/100 after 3 sec. | 151.4 MiB | K
                                                4 | loss 1.421389609e+00 | Ndiff
DELETE @ lap 11.00: 1/1 accepted. Ndiff 49884.65.
  11.000/100 after 5 sec. | 151.4 MiB | K
                                                3 | loss 1.421157450e+00 | Ndiff
DELETE @ lap 12.00: 1/1 accepted. Ndiff 43419.31.
  12.000/100 after 6 sec. | 156.6 MiB | K 2 | loss 1.420888889e+00 | Ndiff
DELETE @ lap 13.00: 1/1 accepted. Ndiff 42527.97.
  13.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 14.00: Ineligible. Did not find >= 2 UIDs in entire model.
  14.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 15.00: Ineligible. Did not find >= 2 UIDs in entire model.
  15.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 16.00: Ineligible. Did not find >= 2 UIDs in entire model.
  16.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 17.00: Ineligible. Did not find >= 2 UIDs in entire model.
  17.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 18.00: Ineligible. Did not find >= 2 UIDs in entire model.
  18.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 19.00: Ineligible. Did not find >= 2 UIDs in entire model.
  19.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 20.00: Ineligible. Did not find >= 2 UIDs in entire model.
  20.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 21.00: Ineligible. Did not find >= 2 UIDs in entire model.
  21.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 22.00: Ineligible. Did not find >= 2 UIDs in entire model.
  22.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 23.00: Ineligible. Did not find >= 2 UIDs in entire model.
  23.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
DELETE @ lap 24.00: Ineligible. Did not find >= 2 UIDs in entire model.
  24.000/100 after 6 sec. | 156.6 MiB | K 1 | loss 1.420559635e+00 | Ndiff
... done. converged.
```

Loss function trace plot

```
pylab.plot(
    m_info_dict['lap_history'][1:],
    m_info_dict['loss_history'][1:], 'k.-',
```

```
label='vb_with_merges')
pylab.plot(
    d_info_dict['lap_history'][1:],
    d_info_dict['loss_history'][1:], 'b.-',
    label='vb_with_deletes')
pylab.legend(loc='upper right')
pylab.xlabel('num. laps')
pylab.ylabel('loss')
pylab.tight_layout()
```



Total running time of the script: (0 minutes 20.276 seconds)

Download Python source code: plot-01-demo=deletes-model=dp_mix+gauss.py

Download Jupyter notebook: plot-01-demo=deletes-model=dp_mix+gauss.ipynb

Generated by Sphinx-Gallery

5.2.3 Old faithful dataset

Variational training of DP mixture models on classic dataset on eruption times from Old Faithful geyser in Yellowstone National Park.

Variational with merge and delete proposals for DP mixtures of Gaussians

How delete moves can be more effective than merges.

In this example, we show how merge moves alone may not be enough to reliably escape local optima. Instead, we show that more flexible delete moves can escape from situations where merges alone fail.

```
import bnpy
import numpy as np
import os
```

```
from matplotlib import pylab
import seaborn as sns

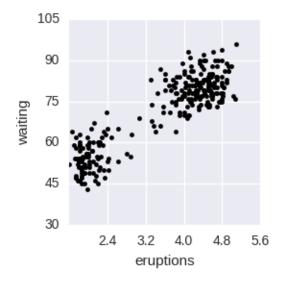
FIG_SIZE = (3, 3)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Load dataset from file

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'faithful')
dataset = bnpy.data.XData.read_csv(
    os.path.join(dataset_path, 'faithful.csv'))
```

Make a simple plot of the raw data

```
pylab.plot(dataset.X[:, 0], dataset.X[:, 1], 'k.')
pylab.xlabel(dataset.column_names[0])
pylab.ylabel(dataset.column_names[1])
pylab.tight_layout()
data_ax_h = pylab.gca()
```



Setup: Determine specific settings of the proposals

```
merge_kwargs = dict(
    m_startLap=10,
    m_pair_ranking_procedure='total_size',
    m_pair_ranking_direction='descending',
)

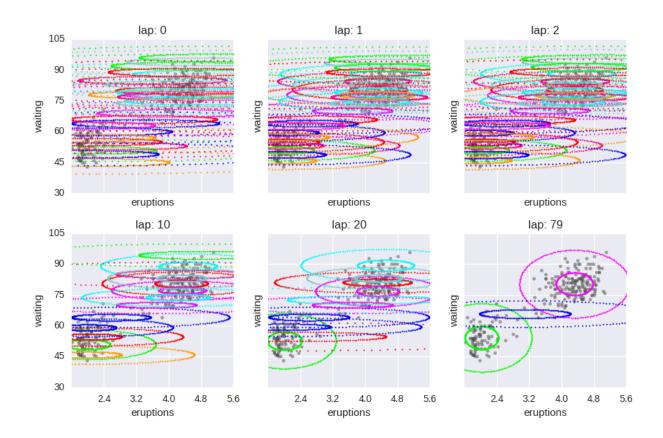
delete_kwargs = dict(
    d_startLap=20,
    d_nRefineSteps=50,
)
```

Setup: Helper function to display the learned clusters

```
def show_clusters_over_time(
       task_output_path=None,
       query_laps=[0, 1, 2, 10, 20, None],
       nrows=2):
    I = I = I
   ncols = int(np.ceil(len(query_laps) // float(nrows)))
   fig_handle, ax_handle_list = pylab.subplots(
        figsize=(FIG SIZE[0] * ncols, FIG SIZE[1] * nrows),
       nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for plot_id, lap_val in enumerate(query_laps):
       cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
       cur_ax_handle = ax_handle_list.flatten()[plot_id]
       bnpy.viz.PlotComps.plotCompsFromHModel(
            cur_model, dataset=dataset, ax_handle=cur_ax_handle)
        cur_ax_handle.set_title("lap: %d" % lap_val)
       cur_ax_handle.set_xlabel(dataset.column_names[0])
       cur_ax_handle.set_ylabel(dataset.column_names[1])
       cur_ax_handle.set_xlim(data_ax_h.get_xlim())
        cur_ax_handle.set_ylim(data_ax_h.get_ylim())
   pylab.tight_layout()
```

DiagGauss observation model, without moves

Start with too many clusters (K=25)



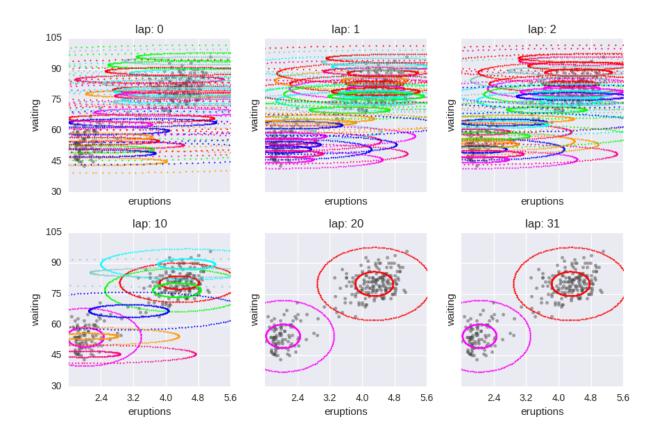
```
Dataset Summary:
X Data
 total size: 272 units
 batch size: 272 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model: Gaussian with diagonal covariance.
Obs. Data Prior:
                  independent Gauss-Wishart prior on each dimension
 Wishart params
   nu = 4
 beta = [10 10]
 Expectations
 E[mean[k]] =
  [ 0 0]
  E[covar[k]] =
  [[ 5. 0.]
  [ 0. 5.]]
Initialization:
  initname = randexamplesbydist
 K = 25 (number of clusters)
  seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/faithful/trymoves-K=25-gamma=5.0-lik=DiagGauss-ECovMat=5.0*eye-move
    1.000/1000 after
                          0 sec. |
                                     153.9 MiB | K
                                                     25 | loss 3.062238769e+00 |
```

2.000/1000 after	0 sec.	153.9 MiB	K	25 loss	3.029485836e+00 Ndiff
3.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.988929671e+00 Ndiff
4.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.934114089e+00 Ndiff
5.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.864320498e+00 Ndiff
6.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.796068518e+00 Ndiff
7.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.755200911e+00 Ndiff
8.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.724352077e+00 Ndiff
9.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.714818175e+00 Ndiff
10.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.710015995e+00 Ndiff
11.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.704686401e+00 Ndiff
12.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.698284253e+00 Ndiff
13.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.684190801e+00 Ndiff
14.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.673906693e+00 Ndiff
15.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.665323886e+00 Ndiff
16.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.654124178e+00 Ndiff
17.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.640063487e+00 Ndiff
18.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.617231862e+00 Ndiff
19.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.586775359e+00 Ndiff
20.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.569671629e+00 Ndiff
21.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.545014854e+00 Ndiff
22.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.525424540e+00 Ndiff
23.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.509251223e+00 Ndiff
24.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.493302635e+00 Ndiff
25.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.488984785e+00 Ndiff
26.000/1000 after	0 sec.	153.9 MiB	l K	25 loss	2.484950693e+00 Ndiff
27.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.480608059e+00 Ndiff
28.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.467505075e+00 Ndiff
29.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.465130737e+00 Ndiff
30.000/1000 after	0 sec.	153.9 MiB	K	25 loss	2.463555210e+00 Ndiff
31.000/1000 after	0 sec.	153.9 MiB	•	25 loss	•
32.000/1000 after	0 sec.	153.9 MiB	•	25 loss	2.459545432e+00 Ndiff
33.000/1000 after	0 sec.	153.9 MiB	•	25 loss	2.456958951e+00 Ndiff
34.000/1000 after	0 sec.	153.9 MiB		25 loss	2.453823064e+00 Ndiff
35.000/1000 after	0 sec.	153.9 MiB		25 loss	2.449961599e+00 Ndiff
36.000/1000 after	0 sec.	153.9 MiB		25 loss	2.445166898e+00 Ndiff
37.000/1000 after	0 sec.	153.9 MiB		25 loss	2.439248319e+00 Ndiff
38.000/1000 after	0 sec.	153.9 MiB		25 loss	2.432174168e+00 Ndiff
39.000/1000 after	0 sec.			25 loss	2.424387029e+00 Ndiff
40.000/1000 after	0 sec.			25 loss	
41.000/1000 after	0 sec.			25 loss	
42.000/1000 after	0 sec.			25 loss	·
43.000/1000 after	0 sec.			25 loss	·
44.000/1000 after	0 sec.			25 loss	2.375964695e+00 Ndiff
45.000/1000 after	0 sec.			25 loss	
46.000/1000 after	1 sec.			25 loss	2.371010870e+00 Ndiff
47.000/1000 after	1 sec.			25 loss	
48.000/1000 after 49.000/1000 after	1 sec.			25 loss 25 loss	·
50.000/1000 after	1 sec.			25 loss 25 loss	
51.000/1000 after	1 sec. 1 sec.			25 1088 25 1088	
52.000/1000 after	1 sec.			25 1088 25 1088	
53.000/1000 after	1 sec.			25 10ss 25 1oss	
54.000/1000 after	1 sec.	153.9 MiB		25 10ss 25 1oss	
51.000/1000 arcer	1 300.	TOO. 7 PILL	1 1/	TO99	2.3301722300.90 Naill

```
25 | loss 2.350192185e+00 | Ndiff
  55.000/1000 after
                         1 sec. |
                                     153.9 MiB | K
  56.000/1000 after
                         1 sec. |
                                     153.9 MiB | K
                                                     25 | loss 2.350192152e+00 | Ndiff
                                                     25 | loss 2.350192136e+00 | Ndiff
  57.000/1000 after
                         1 sec. |
                                     153.9 MiB | K
  58.000/1000 after
                                     153.9 MiB | K
                                                    25 | loss 2.350192129e+00 | Ndiff
                         1 sec. |
                                                    25 | loss 2.350192124e+00 | Ndiff
  59.000/1000 after
                         1 sec. |
                                     153.9 MiB | K
  60.000/1000 after
                                     153.9 MiB | K
                                                     25 | loss 2.350192122e+00 | Ndiff
                         1 sec. |
                                                     25 | loss 2.350192120e+00 | Ndiff
  61.000/1000 after
                         1 sec. |
                                     153.9 MiB | K
  62.000/1000 after
                                                     25 | loss 2.350192119e+00 | Ndiff
                         1 sec. |
                                     153.9 MiB | K
                                                    25 | loss 2.350192119e+00 | Ndiff
  63.000/1000 after
                         1 sec. |
                                    153.9 MiB | K
                                                     25 | loss 2.350192118e+00 | Ndiff
  64.000/1000 after
                         1 sec. |
                                    153.9 MiB | K
  65.000/1000 after
                                     153.9 MiB | K
                                                     25 | loss 2.350192118e+00 | Ndiff
                         1 sec. |
                                                    25 | loss 2.350192117e+00 | Ndiff
  66.000/1000 after
                         1 sec. |
                                    153.9 MiB | K
  67.000/1000 after
                                                    25 | loss 2.350192117e+00 | Ndiff
                         1 sec. |
                                    153.9 MiB | K
  68.000/1000 after
                                                    25 | loss 2.350192117e+00 | Ndiff
                         1 sec. |
                                    153.9 MiB | K
  69.000/1000 after
                                     153.9 MiB | K
                                                    25 | loss 2.350192117e+00 | Ndiff
                         1 sec. |
                                                    25 | loss 2.350192117e+00 | Ndiff
  70.000/1000 after
                        1 \text{ sec.}
                                    153.9 MiB | K
                                                    25 | loss 2.350192116e+00 | Ndiff
  71.000/1000 after
                        1 sec. |
                                   153.9 MiB | K
  72.000/1000 after
                                                    25 | loss 2.350192116e+00 | Ndiff
                         1 sec. |
                                    153.9 MiB | K
                                                    25 | loss 2.350192116e+00 | Ndiff
  73.000/1000 after
                         1 sec. |
                                     153.9 MiB | K
                                                    25 | loss 2.350192116e+00 | Ndiff
  74.000/1000 after
                         1 sec. |
                                    153.9 MiB | K
  75.000/1000 after
                         1 sec. |
                                    153.9 MiB | K
                                                    25 | loss 2.350192116e+00 | Ndiff
                                                     25 | loss 2.350192116e+00 | Ndiff
  76.000/1000 after
                         1 sec. |
                                     153.9 MiB | K
  77.000/1000 after
                                    153.9 MiB | K
                                                    25 | loss 2.350192116e+00 | Ndiff
                         1 sec. |
                                                    25 | loss 2.350192116e+d0 | Ndiff
  78.000/1000 after
                         1 sec. |
                                   153.9 MiB | K
                                   153.9 MiB | K
                                                    25 | loss 2.350192116e+00 | Ndiff
  79.000/1000 after
                         1 sec. |
... done. converged.
SKIPPED 2 comps with size below 0.00
```

DiagGauss observation model

Start with too many clusters (K=25) Use merges and deletes to reduce to a better set.



```
Dataset Summary:
X Data
 total size: 272 units
 batch size: 272 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model: Gaussian with diagonal covariance.
Obs. Data Prior:
                  independent Gauss-Wishart prior on each dimension
 Wishart params
   nu = 4
 beta = [10 10]
 Expectations
 E[mean[k]] =
  [ 0 0]
 E[covar[k]] =
  [[ 5. 0.]
  [ 0. 5.]]
Initialization:
  initname = randexamplesbydist
 K = 25 (number of clusters)
  seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/faithful/trymoves-K=25-gamma=5.0-lik=DiagGauss-ECovMat=5.0*eye-moves
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent wi
```

```
DELETE @ lap 1.00: Disabled. Cannot delete before first complete lap, because $S that repre
   1.000/100 after 0 sec. | 153.9 MiB | K 25 | loss 3.051961291e+00 |
MERGE @ lap 2.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 2.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   2.000/100 after
                       0 sec. | 153.9 MiB | K 25 | loss 3.022209522e+00 | Ndiff
MERGE @ lap 3.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 3.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   3.000/100 after 0 sec. | 153.9 MiB | K 25 | loss 2.984471596e+00 | Ndiff
MERGE @ lap 4.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 4.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   4.000/100 after 0 sec. | 153.9 MiB | K 25 | loss 2.926643058e+00 | Ndiff
MERGE @ lap 5.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 5.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   5.000/100 after
                     0 sec. | 153.9 MiB | K 25 | loss 2.862469660e+00 | Ndiff
MERGE @ lap 6.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 6.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   6.000/100 after 0 sec. | 153.9 MiB | K 25 | loss 2.779705996e+00 | Ndiff
MERGE @ lap 7.00: Disabled. Waiting for lap >= 10 (-m_startLap).
DELETE @ lap 7.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   7.000/100 after
                       0 sec. | 153.9 MiB | K 25 | loss 2.734025386e+00 | Ndiff
MERGE @ lap 8.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 8.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   8.000/100 after 0 sec. | 153.9 MiB | K 25 | loss 2.705925412e+00 | Ndiff
MERGE @ lap 9.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 9.00: Disabled. Waiting for lap \geq 20 (--d_startLap).
   9.000/100 after 0 sec. | 153.9 MiB | K 25 | loss 2.695114165e+00 | Ndiff
DELETE @ lap 10.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 10.00 : 11/21 accepted. Ndiff 96.55. 39 skipped.
  10.000/100 after 0 sec. | 153.9 MiB | K 14 | loss 2.588387948e+00 | Ndiff
DELETE @ lap 11.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 11.00 : 6/10 accepted. Ndiff 57.31. 23 skipped.
  11.000/100 after 0 sec. | 153.9 MiB | K 8 | loss 2.418907387e+00 | Ndiff
DELETE @ lap 12.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 12.00 : 4/5 accepted. Ndiff 24.39. 14 skipped.
   12.000/100 after
                       0 sec. | 153.9 MiB | K
                                                  4 | loss 2.344906523e+00 | Ndiff
DELETE @ lap 13.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 13.00 : 1/4 accepted. Ndiff 0.00. 2 skipped.
  13.000/100 after 0 sec. | 153.9 MiB | K 3 | loss 2.342439735e+00 | Ndiff
MERGE @ lap 14.00: No promising candidates, so no attempts.
DELETE @ lap 14.00: Disabled. Waiting for lap >= 20 (--d_startLap).
  14.000/100 after 0 sec. | 153.9 MiB | K 3 | loss 2.341617749e+00 | Ndiff
DELETE @ lap 15.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 15.00 : 0/2 accepted. Ndiff 0.00. 0 skipped.
  15.000/100 after 0 sec. | 153.9 MiB | K 3 | loss 2.341288596e+00 | Ndiff
DELETE @ lap 16.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 16.00 : 0/1 accepted. Ndiff 0.00. 0 skipped.
  16.000/100 after 0 sec. | 153.9 MiB | K 3 | loss 2.341147153e+00 | Ndiff
DELETE @ lap 17.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 17.00 : 0/2 accepted. Ndiff 0.00. 0 skipped.
  17.000/100 after
                    0 sec. | 153.9 MiB | K 3 | loss 2.341080073e+00 | Ndiff
MERGE @ lap 18.00: No promising candidates, so no attempts.
DELETE @ lap 18.00: Disabled. Waiting for lap >= 20 (--d_startLap).
  18.000/100 after 1 sec. | 153.9 MiB | K 3 | loss 2.341044964e+00 | Ndiff
```

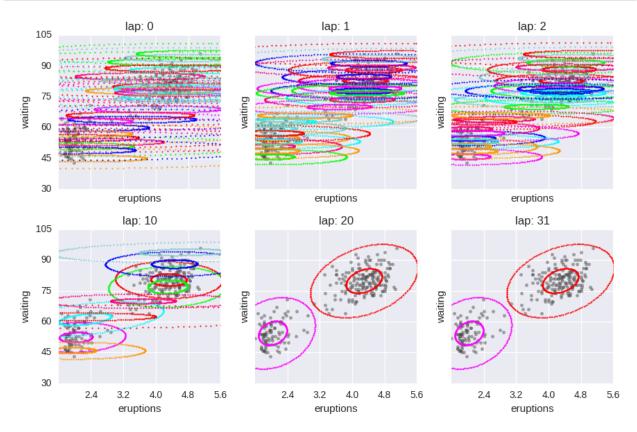
```
DELETE @ lap 19.00: Disabled. Waiting for lap >= 20 (--d startLap).
MERGE @ lap 19.00 : 0/2 accepted. Ndiff 0.00. 0 skipped.
  19.000/100 after
                     1 sec. | 153.9 MiB | K 3 | loss 2.341025070e+00 | Ndiff
MERGE @ lap 20.00: No promising candidates, so no attempts.
DELETE @ lap 20.00: 1/1 accepted. Ndiff 169.12.
  20.000/100 after 1 sec. | 153.9 MiB | K 2 | loss 2.330925760e+00 | Ndiff
DELETE @ lap 21.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 21.00 : 0/1 accepted. Ndiff 0.00. 0 skipped.
                   1 sec. | 153.9 MiB | K 2 | loss 2.330925543e+00 | Ndiff
  21.000/100 after
MERGE @ lap 22.00: No promising candidates, so no attempts.
DELETE @ lap 22.00: 0/1 accepted. Ndiff 0.00.
  22.000/100 after
                      1 sec. | 153.9 MiB | K 2 | loss 2.330925529e+00 | Ndiff
MERGE @ lap 23.00: No promising candidates, so no attempts.
DELETE @ lap 23.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo-
  23.000/100 after 1 sec. | 153.9 MiB | K 2 | loss 2.330925528e+00 | Ndiff
MERGE @ lap 24.00: No promising candidates, so no attempts.
DELETE @ lap 24.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo
                      1 sec. | 153.9 MiB | K 2 | loss 2.330925528e+00 | Ndiff
  24.000/100 after
MERGE @ lap 25.00: No promising candidates, so no attempts.
DELETE @ lap 25.00: Empty plan. O UIDs eligible as delete target. O too busy with other mo
  25.000/100 after 1 sec. | 153.9 MiB | K 2 | loss 2.330925528e+00 | Ndiff
DELETE @ lap 26.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo-
MERGE @ lap 26.00 : 0/1 accepted. Ndiff 0.00. 0 skipped.
  26.000/100 after 1 sec. | 153.9 MiB | K 2 | loss 2.330925528e+00 | Ndiff
MERGE @ lap 27.00: No promising candidates, so no attempts.
DELETE @ lap 27.00: 0/1 accepted. Ndiff 0.00.
  27.000/100 after 1 sec. |
                                                  2 | loss 2.330925528e+00 | Ndiff
                                 153.9 MiB | K
MERGE @ lap 28.00: No promising candidates, so no attempts.
DELETE @ lap 28.00: 0/1 accepted. Ndiff 0.00.
  28.000/100 after
                   1 sec. |
                                 153.9 MiB | K
                                                 2 | loss 2.330925528e+00 | Ndiff
MERGE @ lap 29.00: No promising candidates, so no attempts.
DELETE @ lap 29.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo
  MERGE @ lap 30.00: No promising candidates, so no attempts.
DELETE @ lap 30.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo-
  30.000/100 after 1 sec. | 153.9 MiB | K 2 | loss 2.330925528e+00 | Ndiff
DELETE @ lap 31.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo-
MERGE @ lap 31.00 : 0/1 accepted. Ndiff 0.00. 0 skipped.
  31.000/100 after
                   1 sec. | 153.9 MiB | K 2 | loss 2.330925528e+00 | Ndiff
... done. converged.
```

Gauss observation model

Start with too many clusters (K=25) Use merges and deletes to reduce to a better set.

```
full_trained_model, full_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Gauss', 'memoVB',
    output_path=('/tmp/faithful/' +
        'trymoves-K=%d-gamma=%s-lik-Gauss-ECovMat=%s*eye-moves=merge,delete,shuffle/' % (
            K, gamma, sF)),
    nLap=100, nTask=1, nBatch=1,
    gamma0=gamma, sF=sF, ECovMat='eye',
```

```
K=K, initname='randexamplesbydist',
  moves='merge,delete,shuffle',
  **dict(delete_kwargs.items() + merge_kwargs.items()))
show_clusters_over_time(full_info_dict['task_output_path'])
```



```
Dataset Summary:
X Data
 total size: 272 units
 batch size: 272 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model:
                  Gaussian with full covariance.
                  Gauss-Wishart on mean and covar of each cluster
Obs. Data Prior:
 E[mean[k]] =
  [ 0. 0.]
 E[ covar[k] ] =
  [[ 5. 0.]
  [ 0. 5.]]
Initialization:
  initname = randexamplesbydist
 K = 25 (number of clusters)
  seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
```

```
task_output_path: /tmp/faithful/trymoves-K=25-gamma=5.0-lik-Gauss-ECovMat=5.0*eye-moves=me
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent w
DELETE @ lap 1.00: Disabled. Cannot delete before first complete lap, because $S that repre
                       0 sec. | 155.5 MiB | K 25 | loss 2.959097158e+00 |
   1.000/100 after
MERGE @ lap 2.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 2.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   2.000/100 after
                     0 sec. | 155.5 MiB | K 25 | loss 2.937002302e+00 | Ndiff
MERGE @ lap 3.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 3.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   3.000/100 after
                      0 sec. | 155.5 MiB | K 25 | loss 2.912622033e+00 | Ndiff
MERGE @ lap 4.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 4.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   4.000/100 after
                     0 sec. | 155.5 MiB | K 25 | loss 2.880654959e+00 | Ndiff
MERGE @ lap 5.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 5.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   5.000/100 after
                     0 sec. | 155.5 MiB | K 25 | loss 2.829532053e+00 | Ndiff
MERGE @ lap 6.00: Disabled. Waiting for lap >= 10 (--m startLap).
DELETE @ lap 6.00: Disabled. Waiting for lap >= 20 (--d_startLap).
                       0 sec. | 155.5 MiB | K 25 | loss 2.769025659e+00 | Ndiff
   6.000/100 after
MERGE @ lap 7.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 7.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   7.000/100 after 0 sec. | 155.5 MiB | K 25 | loss 2.725273863e+00 | Ndiff
MERGE @ lap 8.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 8.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   8.000/100 after 0 sec. | 155.5 MiB | K 25 | loss 2.675946971e+00 | Ndiff
MERGE @ lap 9.00: Disabled. Waiting for lap >= 10 (--m_startLap).
DELETE @ lap 9.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   9.000/100 after
                       0 sec. | 155.5 MiB | K 25 | loss 2.647374823e+00 | Ndiff
DELETE @ lap 10.00: Disabled. Waiting for lap >= 20 (--d startLap).
MERGE @ lap 10.00 : 11/18 accepted. Ndiff 107.08. 41 skipped.
   10.000/100 after 1 sec. | 155.5 MiB | K 14 | loss 2.556490112e+00 | Ndiff
DELETE @ lap 11.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 11.00 : 6/7 accepted. Ndiff 88.56. 27 skipped.
  11.000/100 after 1 sec. | 155.6 MiB | K 8 | loss 2.396890018e+00 | Ndiff
DELETE @ lap 12.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 12.00: 4/5 accepted. Ndiff 35.75. 11 skipped.
  12.000/100 after 1 sec. | 155.6 MiB | K 4 | loss 2.315013331e+00 | Ndiff
DELETE @ lap 13.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 13.00 : 2/3 accepted. Ndiff 6.24. 3 skipped.
  13.000/100 after
                    1 sec. | 155.6 MiB | K 2 | loss 2.282002142e+00 | Ndiff
MERGE @ lap 14.00: No promising candidates, so no attempts.
DELETE @ lap 14.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   14.000/100 after 1 sec. | 155.6 MiB | K
                                                   2 | loss 2.268874488e+00 | Ndiff
DELETE @ lap 15.00: Disabled. Waiting for lap >= 20 (--d_startLap).
MERGE @ lap 15.00 : 0/1 accepted. Ndiff 0.00. 0 skipped.
  15.000/100 after
                    1 sec. | 155.6 MiB | K 2 | loss 2.268112275e+00 | Ndiff
MERGE @ lap 16.00: No promising candidates, so no attempts.
DELETE @ lap 16.00: Disabled. Waiting for lap >= 20 (--d_startLap).
   16.000/100 after 1 sec. | 155.6 MiB | K 2 | loss 2.268077838e+00 | Ndiff
MERGE @ lap 17.00: No promising candidates, so no attempts.
DELETE @ lap 17.00: Disabled. Waiting for lap >= 20 (--d startLap).
  17.000/100 after 1 sec. | 155.6 MiB | K 2 | loss 2.268076838e+00 | Ndiff
MERGE @ lap 18.00: No promising candidates, so no attempts.
```

```
DELETE @ lap 18.00: Disabled. Waiting for lap >= 20 (--d startLap).
  18.000/100 after 1 sec. | 155.6 MiB | K 2 | loss 2.268076812e+00 | Ndiff
MERGE @ lap 19.00: No promising candidates, so no attempts.
DELETE @ lap 19.00: Disabled. Waiting for lap >= 20 (--d_startLap).
  19.000/100 after
                       1 sec. | 155.6 MiB | K 2 | loss 2.268076811e+00 | Ndiff
DELETE @ lap 20.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 20.00 : 0/1 accepted. Ndiff 0.00. 0 skipped.
  20.000/100 after
                    1 sec. | 155.6 MiB | K 2 | loss 2.268076811e+00 | Ndiff
MERGE @ lap 21.00: No promising candidates, so no attempts.
DELETE @ lap 21.00: 0/1 accepted. Ndiff 0.00.
  21.000/100 after
                     1 sec. |
                                                  2 | loss 2.268076811e+00 | Ndiff
                                  155.6 MiB | K
MERGE @ lap 22.00: No promising candidates, so no attempts.
DELETE @ lap 22.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo
  22.000/100 after
                    1 sec. | 155.6 MiB | K 2 | loss 2.268076811e+00 | Ndiff
MERGE @ lap 23.00: No promising candidates, so no attempts.
DELETE @ lap 23.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo
  23.000/100 after 1 sec. | 155.6 MiB | K
                                                2 | loss 2.268076811e+00 | Ndiff
MERGE @ lap 24.00: No promising candidates, so no attempts.
DELETE @ lap 24.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other move
  24.000/100 after 1 sec. | 155.6 MiB | K
                                                 2 | loss 2.268076811e+00 | Ndiff
DELETE @ lap 25.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo-
MERGE @ lap 25.00 : 0/1 accepted. Ndiff 0.00. 0 skipped.
  MERGE @ lap 26.00: No promising candidates, so no attempts.
DELETE @ lap 26.00: 0/1 accepted. Ndiff 0.00.
  26.000/100 after 1 sec. | 155.6 MiB | K 2 | loss 2.268076811e+00 | Ndiff
MERGE @ lap 27.00: No promising candidates, so no attempts.
DELETE @ lap 27.00: 0/1 accepted. Ndiff 0.00.
  27.000/100 after 1 sec. | 155.6 MiB | K
                                                 2 | loss 2.268076811e+00 | Ndiff
MERGE @ lap 28.00: No promising candidates, so no attempts.
DELETE @ lap 28.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo-
  28.000/100 after 1 sec. | 155.6 MiB | K 2 | loss 2.268076811e+00 | Ndiff
MERGE @ lap 29.00: No promising candidates, so no attempts.
DELETE @ lap 29.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo
  29.000/100 after
                       1 sec. | 155.6 MiB | K 2 | loss 2.268076811e+00 | Ndiff
DELETE @ lap 30.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo-
MERGE @ lap 30.00 : 0/1 accepted. Ndiff 0.00. 0 skipped.
  30.000/100 after
                   1 sec. | 155.6 MiB | K
                                                 2 | loss 2.268076811e+00 | Ndiff
MERGE @ lap 31.00: No promising candidates, so no attempts.
DELETE @ lap 31.00: Empty plan. 0 UIDs eligible as delete target. 0 too busy with other mo
  31.000/100 after
                   1 sec. | 155.6 MiB | K 2 | loss 2.268076811e+00 | Ndiff
... done. converged.
```

Loss function trace plot

```
pylab.figure()
pylab.plot(
    diag1_info_dict['lap_history'][2:],
    diag1_info_dict['loss_history'][2:], 'r.-',
    label='diag_covar fixed')
pylab.plot(
```

```
diag_info_dict['lap_history'][2:],
    diag_info_dict['loss_history'][2:], 'k.-',
    label='diag_covar + moves')

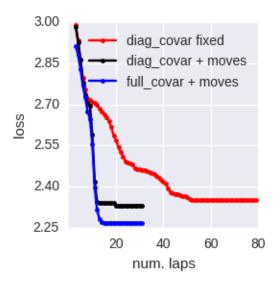
pylab.plot(
    full_info_dict['lap_history'][2:],
    full_info_dict['loss_history'][2:], 'b.-',
    label='full_covar + moves')

pylab.legend(loc='upper right')

pylab.xlabel('num. laps')

pylab.ylabel('loss')

pylab.tight_layout()
```



Total running time of the script: (0 minutes 5.577 seconds)

Download Python source code: plot-02-demo=merge_and_delete-model=dp_mix+gauss.py

Download Jupyter notebook: plot-02-demo=merge_and_delete-model=dp_mix+gauss.ipynb

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Variational training for Mixtures of Gaussians

Showcase of different models and algorithms applied to same dataset.

In this example, we show how bnpy makes it easy to apply different models and algorithms to the same dataset.

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns

SMALL_FIG_SIZE = (2.5, 2.5)
```

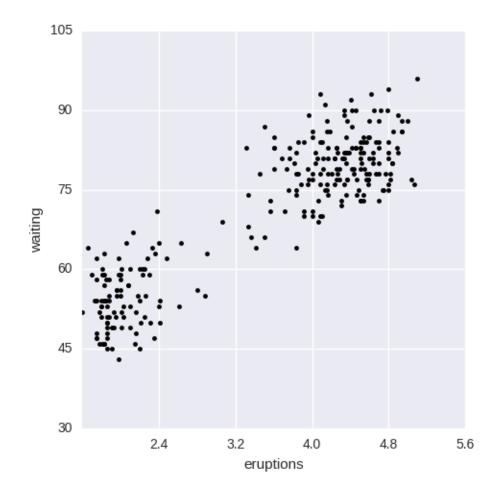
```
FIG_SIZE = (5, 5)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Load dataset from file

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'faithful')
dataset = bnpy.data.XData.read_csv(
    os.path.join(dataset_path, 'faithful.csv'))
```

Make a simple plot of the raw data

```
pylab.plot(dataset.X[:, 0], dataset.X[:, 1], 'k.')
pylab.xlabel(dataset.column_names[0])
pylab.ylabel(dataset.column_names[1])
pylab.tight_layout()
data_ax_h = pylab.gca()
```



Setup: Helper function to display the learned clusters

```
def show_clusters_over_time(
    task_output_path=None,
```

```
query_laps=[0, 1, 2, 10, 20, None],
   nrows=2):
''' Show 2D elliptical contours overlaid on raw data.
I = I = I
ncols = int(np.ceil(len(query_laps) // float(nrows)))
fig_handle, ax_handle_list = pylab.subplots(
    figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
   nrows=nrows, ncols=ncols, sharex=True, sharey=True)
for plot_id, lap_val in enumerate(query_laps):
   cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
    cur_ax_handle = ax_handle_list.flatten()[plot_id]
   bnpy.viz.PlotComps.plotCompsFromHModel(
        cur_model, dataset=dataset, ax_handle=cur_ax_handle)
    cur_ax_handle.set_title("lap: %d" % lap_val)
    cur_ax_handle.set_xlabel(dataset.column_names[0])
   cur_ax_handle.set_ylabel(dataset.column_names[1])
   cur ax handle.set xlim(data ax h.get xlim())
    cur_ax_handle.set_ylim(data_ax_h.get_ylim())
pylab.tight_layout()
```

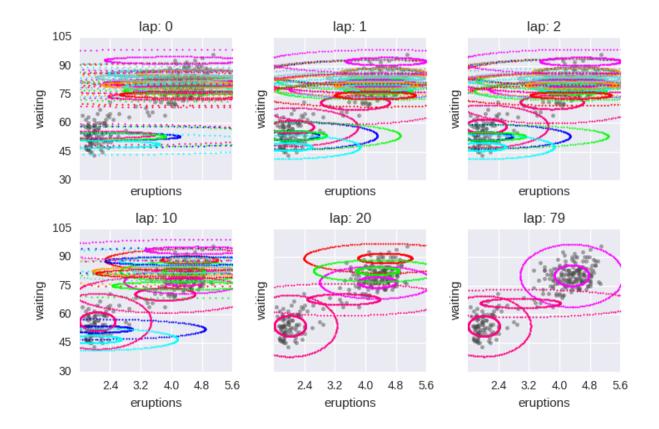
DiagGauss observation model

Assume diagonal covariances.

Start with too many clusters (K=20)

```
gamma = 5.0
sF = 5.0
K = 20

diag_trained_model, diag_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'DiagGauss', 'memoVB',
    output_path='/tmp/faithful/showcase-K=20-lik=DiagGauss-ECovMat=5*eye/',
    nLap=1000, nTask=1, nBatch=1, convergeThr=0.0001,
    gamma0=gamma, sF=sF, ECovMat='eye',
    K=K, initname='randexamples',
    )
show_clusters_over_time(diag_info_dict['task_output_path'])
```



```
Dataset Summary:
X Data
 total size: 272 units
 batch size: 272 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model: Gaussian with diagonal covariance.
Obs. Data Prior: independent Gauss-Wishart prior on each dimension
 Wishart params
   nu = 4
 beta = [10 10]
 Expectations
 E[mean[k]] =
  [0 0]
  E[covar[k]] =
  [[ 5. 0.]
  [ 0. 5.]]
Initialization:
  initname = randexamples
 K = 20 (number of clusters)
  seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB \mid task 1/1 \mid alg. seed: 1607680 \mid data order seed: 8541952
task_output_path: /tmp/faithful/showcase-K=20-lik=DiagGauss-ECovMat=5*eye/1
    1.000/1000 after
                          0 sec. |
                                      158.6 MiB | K
                                                     20 | loss 3.002088161e+00
```

2.000	/1000	after	0	sec.		158.6	MiB	K	20	loss	2.966309748e+00	Ndiff
3.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.949498401e+00	Ndiff
4.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.931792100e+00	Ndiff
5.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.910174417e+00	Ndiff
6.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.881973764e+00	Ndiff
7.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.833491488e+00	Ndiff
8.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.793876249e+00	Ndiff
9.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.752249036e+00	Ndiff
10.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.698456106e+00	Ndiff
11.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.651622886e+00	Ndiff
12.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.624108159e+00	Ndiff
13.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.587572334e+00	Ndiff
14.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.560219008e+00	Ndiff
15.000	/1000	after	0	sec.		158.6	MiB	K	20	loss	2.544887510e+00	Ndiff
16.000	/1000	after	0	sec.		158.6	MiB	K	20	loss	2.527562170e+00	Ndiff
17.000	/1000	after	0	sec.		158.6	MiB	K	20	loss	2.513204290e+00	Ndiff
18.000	/1000	after	0	sec.		158.6	MiB	K	20	loss	2.507574530e+00	Ndiff
19.000	/1000	after	0	sec.	1	158.6	MiB	K	20	loss	2.497639081e+00	Ndiff
20.000	/1000	after	0	sec.	1	158.6		K	20	loss	2.497002974e+00	Ndiff
		after	0	sec.	1	158.6		K	20	loss	2.496368366e+00	Ndiff
		after	0	sec.	1	158.6		K	20	loss	2.495732569e+00	Ndiff
		after	0	sec.	1	158.6		K	20	loss	2.495103986e+00	Ndiff
		after		sec.	I	158.6		K	20	loss	2.494497370e+00	Ndiff
		after		sec.	1	158.6		K	20	loss	2.493928089e+00	Ndiff
		after		sec.	1	158.6		K	20	loss	2.493406054e+00	Ndiff
		after		sec.		158.6		K	20	loss	2.492931650e+00	Ndiff
		after		sec.		158.6		K	20	loss	2.492495409e+00	Ndiff
		after		sec.	1	158.6		K	20	loss	2.492081031e+00	Ndiff
		after		sec.	1	158.6		K	20	loss	2.491669505e+00	Ndiff
		after		sec.	1	158.6		K	20	loss	2.491242078e+00	Ndiff
		after		sec.	1	158.6 158.6		K	20	loss	2.490781261e+00	Ndiff
		after after		sec.	1	158.6		K K	20 20	loss loss	2.490270354e+00 2.489692235e+00	Ndiff Ndiff
		after		sec.	1	158.6		K	20	loss	2.489027945e+00	Ndiff
		after		sec.	1	158.6		K	20	loss	2.488255286e+00	Ndiff
		after		sec.	1	158.6		K	20	l loss	2.487347489e+00	Ndiff
		after	0		1	158.6		K	20	loss	2.486272015e+00	Ndiff
		after		sec.	ı	158.6		K	20	loss	2.484989607e+00	Ndiff
		after		sec.		158.6		K	20	loss	2.483453885e+00	
		after		sec.		158.6		K	20	loss	2.481612017e+00	
		after		sec.		158.6		K	20	loss	2.479407351e+00	
		after		sec.		158.6		K	20	loss	2.476785615e+00	
		after		sec.	i	158.6		K	20	loss	2.473707547e+00	
		after		sec.	i	158.6		K	20	loss	2.470173027e+00	
46.000	/1000	after	0	sec.	Ī	158.6		K	20	loss	2.466261998e+00	Ndiff
		after		sec.		158.6		K	20	loss	2.462175093e+00	
48.000	/1000	after	0	sec.		158.6		K	20	loss	2.458145085e+00	Ndiff
49.000	/1000	after	0	sec.		158.6	MiB	K	20	loss	2.453753531e+00	Ndiff
50.000	/1000	after	1	sec.		158.6	MiB	K	20	loss	2.441832238e+00	Ndiff
		after		sec.		158.6		K	20	loss	2.437414963e+00	
		after		sec.		158.6		K	20	loss	2.435586138e+00	
		after		sec.		158.6		K	20	loss	2.433555668e+00	
54.000	/1000	after	1	sec.		158.6	MiB	K	20	loss	2.431430213e+00	Ndiff
1												

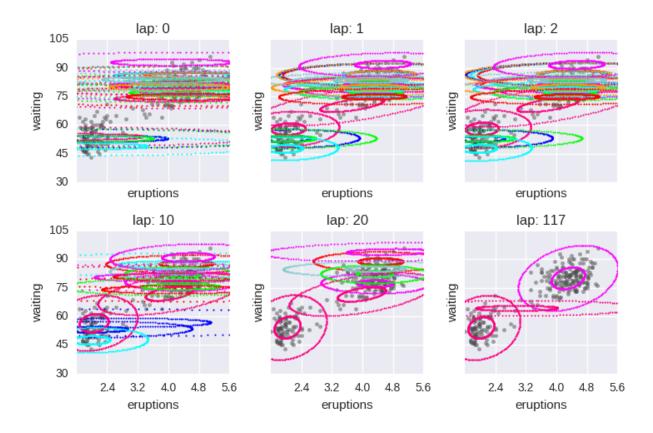
```
20 | loss 2.429483776e+00 | Ndiff
  55.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.428084819e+00 | Ndiff
  56.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.427098172e+00 | Ndiff
  57.000/1000 after
                                     158.6 MiB | K
                         1 sec. |
                                                     20 | loss 2.425535651e+00 | Ndiff
  58.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
  59.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.415976963e+00 | Ndiff
  60.000/1000 after
                                     158.6 MiB | K
                                                     20 | loss 2.412692266e+00 | Ndiff
                         1 sec. |
  61.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.412692093e+00 | Ndiff
  62.000/1000 after
                                     158.6 MiB | K
                                                     20 | loss 2.412692005e+00 | Ndiff
                         1 sec. |
                                                     20 | loss 2.412691958e+00 | Ndiff
  63.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.412691932e+00 | Ndiff
  64.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
  65.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.412691918e+00 | Ndiff
                                                     20 | loss 2.412691910e+00 | Ndiff
  66.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
  67.000/1000 after
                                     158.6 MiB | K
                                                     20 | loss 2.412691906e+00 | Ndiff
                         1 sec. |
                                                     20 | loss 2.412691904e+00 | Ndiff
  68.000/1000 after
                                     158.6 MiB | K
                         1 sec. |
  69.000/1000 after
                                     158.6 MiB | K
                                                     20 | loss 2.412691903e+00 | Ndiff
                         1 sec. |
                                                     20 | loss 2.412691902e+d0 | Ndiff
  70.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                     158.6 MiB | K
                                                     20 | loss 2.412691901e+00 | Ndiff
  71.000/1000 after
                        1 sec. |
                                                     20 | loss 2.412691901e+00 | Ndiff
  72.000/1000 after
                         1 sec. |
                                    158.6 MiB | K
  73.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.412691901e+00 | Ndiff
                                                     20 | loss 2.412691901e+00 | Ndiff
  74.000/1000 after
                                     158.6 MiB | K
                         1 sec. |
                                                     20 | loss 2.412691901e+00 | Ndiff
  75.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.412691901e+00 | Ndiff
  76.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.412691901e+00 | Ndiff
  77.000/1000 after
                         1 sec. |
                                     158.6 MiB | K
                                                     20 | loss 2.412691901e+00 | Ndiff
  78.000/1000 after
                         1 sec. |
                                   158.6 MiB | K
  79.000/1000 after
                         1 sec. |
                                    158.6 MiB | K
                                                     20 | loss 2.412691901e+00 | Ndiff
... done. converged.
```

Gauss observations + VB

Assume full covariances.

Start with too many clusters (K=20)

```
full_trained_model, full_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Gauss', 'VB',
    output_path='/tmp/faithful/showcase-K=20-lik=Gauss-ECovMat=5*eye/',
    nLap=1000, nTask=1, nBatch=1, convergeThr=0.0001,
    gamma0=gamma, sF=sF, ECovMat='eye',
    K=K, initname='randexamples',
    )
show_clusters_over_time(full_info_dict['task_output_path'])
```



```
WARNING: Found unrecognized keyword args. These are ignored.
  --nBatch
Dataset Summary:
X Data
 num examples: 272
 num dims: 2
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model:
                  Gaussian with full covariance.
                  Gauss-Wishart on mean and covar of each cluster
Obs. Data Prior:
 E[mean[k]] =
  [ 0. 0.]
 E[covar[k]] =
  [[ 5. 0.]
  [ 0. 5.]]
Initialization:
  initname = randexamples
 K = 20 (number of clusters)
  seed = 1607680
  elapsed_time: 0.0 sec
Learn Alg: VB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/faithful/showcase-K=20-lik=Gauss-ECovMat=5*eye/1
        1/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 2.904406498e+00 |
        2/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 2.876066302e+00 | Ndiff
        3/1000 after
                                      154.6 MiB | K
                                                      20 | loss 2.864944306e+00 | Ndiff
                          0 sec. |
        4/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss
                                                                2.852026479e+00 | Ndiff
```

5/1000	after	0 sec.	154.6 MiB	K	20	loss	2.836506635e+00	Ndiff
6/1000	after	0 sec.	154.6 MiB	K	20	loss	2.817804673e+00	Ndiff
7/1000	after	0 sec.	154.6 MiB	K	20	loss	2.787080350e+00	Ndiff
8/1000	after	0 sec.	154.6 MiB	K	20	loss	2.743017730e+00	Ndiff
9/1000	after	0 sec.	154.6 MiB	K	20	loss	2.714906517e+00	Ndiff
10/1000	after	0 sec.	154.6 MiB	K	20	loss	2.670842807e+00	Ndiff
11/1000	after	0 sec.	154.6 MiB	K	20	loss	2.640944068e+00	Ndiff
12/1000	after	0 sec.	154.6 MiB	K	20	loss	2.600612644e+00	Ndiff
13/1000	after	0 sec.	154.6 MiB	K	20	loss	2.582832638e+00	Ndiff
14/1000	after	0 sec.	154.6 MiB	K	20	loss	2.569005251e+00	Ndiff
15/1000	after	0 sec.	154.6 MiB	K	20	loss	2.544279312e+00	Ndiff
16/1000	after	0 sec.	154.6 MiB	K	20	loss	2.523247072e+00	Ndiff
17/1000	after	0 sec.	154.6 MiB	K	20	loss	2.511328327e+00	Ndiff
18/1000	after	0 sec.	154.6 MiB	K	20	loss	2.503251361e+00	Ndiff
19/1000	after	0 sec.	154.6 MiB	K	20	loss	2.491852524e+00	Ndiff
20/1000	after	0 sec.	154.6 MiB	K	20	loss	2.490247584e+00	Ndiff
21/1000	after	0 sec.	154.6 MiB	K	20	loss	2.488483904e+00	Ndiff
22/1000		0 sec.	154.6 MiB	K	20	loss	2.486427687e+00	Ndiff
23/1000	after	0 sec.	154.6 MiB	K	20	loss	2.484005616e+00	Ndiff
24/1000		0 sec.	154.6 MiB	K	20	loss	2.481221463e+00	Ndiff
25/1000		0 sec.	154.6 MiB	K	20	loss	2.478177971e+00	Ndiff
26/1000		0 sec.	154.6 MiB	K	20	loss	2.475094563e+00	Ndiff
27/1000		0 sec.	154.6 MiB	K	20	loss	2.471974138e+00	Ndiff
28/1000	after	0 sec.	154.6 MiB	K	20	loss	2.467024647e+00	Ndiff
29/1000	after	0 sec.	154.6 MiB	K	20	loss	2.453713427e+00	Ndiff
30/1000	after	0 sec.	154.6 MiB	K	20	loss	2.445147652e+00	Ndiff
31/1000	after	0 sec.	154.6 MiB	K	20	loss	2.439161802e+00	Ndiff
32/1000		1 sec.	154.6 MiB	K	20 j	loss	2.438783471e+00	Ndiff
33/1000	after	1 sec.	154.6 MiB	K	20	loss	2.438429230e+00	Ndiff
34/1000		1 sec.	154.6 MiB	K	20	loss	2.438098475e+00	Ndiff
35/1000		1 sec.	154.6 MiB	K	20	loss	2.437790556e+00	Ndiff
36/1000	after	1 sec.	154.6 MiB	K	20	loss	2.437503774e+00	Ndiff
37/1000	after	1 sec.	154.6 MiB	K	20	loss	2.437235314e+00	Ndiff
38/1000	after	1 sec.	154.6 MiB	K	20	loss	2.436981439e+00	Ndiff
39/1000	after	1 sec.	154.6 MiB	K	20	loss	2.436737744e+00	Ndiff
40/1000	after	1 sec.	154.6 MiB	K	20	loss	2.436499373e+00	Ndiff
41/1000	after	1 sec.	154.6 MiB	K	20	loss	2.436261156e+00	Ndiff
42/1000	after	1 sec.	154.6 MiB				2.436017666e+00	
43/1000	after	1 sec.	154.6 MiB	K			2.435763198e+00	
44/1000	after	1 sec.	154.6 MiB	K	20	loss	2.435491737e+00	Ndiff
45/1000	after	1 sec.	154.6 MiB	K	20	loss	2.435196931e+00	Ndiff
46/1000	after	1 sec.	154.6 MiB	K	20	loss	2.434872198e+00	Ndiff
47/1000	after	1 sec.	154.6 MiB	K	20	loss	2.434511031e+00	Ndiff
48/1000	after	1 sec.	154.6 MiB	K	20	loss	2.434107639e+00	Ndiff
49/1000			154.6 MiB		20	loss	2.433657974e+00	
50/1000		1 sec.	154.6 MiB		20	loss	2.433161085e+00	
51/1000			154.6 MiB		20	loss	2.432620547e+00	Ndiff
52/1000			154.6 MiB		20	loss	2.432045498e+00	Ndiff
53/1000			154.6 MiB		20	loss	2.431450777e+00	Ndiff
54/1000			154.6 MiB		20	loss	2.430855677e+00	Ndiff
55/1000			154.6 MiB		20	loss		
56/1000	after		154.6 MiB		20	loss	2.429742357e+00	Ndiff
57/1000	after	1 sec.	154.6 MiB	K	20	loss	2.429246005e+00	Ndiff

58/1000	after	1 sec	.	154.6	MiB	K	20	loss	2.428783131e+00	Ndiff
59/1000	after	1 sec	.	154.6	MiB	K	20	loss	2.428335044e+00	Ndiff
60/1000	after	1 sec	.	154.6	MiB	K	20	loss	2.427882144e+00	Ndiff
61/1000	after	1 sec	.	154.6	MiB	K	20	loss	2.427412198e+00	Ndiff
62/1000	after	1 sec	.	154.6	MiB	K	20	loss	2.426923365e+00	Ndiff
63/1000	after	1 sec		154.6		K	20	loss	2.426419184e+00	Ndiff
64/1000		1 sec		154.6		K	20	loss	2.425898789e+00	
65/1000		1 sec		154.6		K	20	loss	2.425353548e+00	
66/1000		1 sec		154.6		K	20	loss	2.424771068e+00	
67/1000		1 sec		154.6		K	20	loss	2.424138280e+00	
68/1000		1 sec		154.6		K	20	loss	2.423441574e+00	
69/1000		1 sec		154.6		K	20	loss	2.422666132e+00	
70/1000		1 sec		154.6		K	20	loss	2.421796837e+00	
71/1000		1 sec		154.6		K	20	loss	2.420824917e+00	
72/1000		1 sec		154.6		K	20	loss	2.419763730e+00	
73/1000		1 sec		154.6		K	20	loss	2.418655856e+00	
74/1000		1 sec		154.6		K	20	loss	2.417536411e+00	
75/1000		1 sec		154.6		K	20	loss	2.416396660e+00	
76/1000		1 sec		154.6		K	20	loss	2.415209641e+00	
77/1000		1 sec		154.6		K	20	loss	2.413957301e+00	
78/1000		1 sec		154.6		K	20	loss	2.412627524e+00	
79/1000		1 sec		154.6		K	20	loss	2.411204929e+00	
80/1000		1 sec		154.6		K	20	loss	2.409665366e+00	
81/1000		1 sec		154.6		K	20	loss	2.407972796e+00	
82/1000		1 sec		154.6		K	20	loss	2.406075452e+00	
83/1000		1 sec		154.6		K	20	loss	2.403897086e+00	
84/1000		1 sec		154.6		K	20	loss	2.401317119e+00	
85/1000		1 sec		154.6		K	20	loss	2.398127190e+00	
86/1000		1 sec		154.6		K	20	loss	2.393870554e+00	
87/1000		1 sec		154.6		K	20	loss	2.385927886e+00	Ndiff
88/1000		1 sec		154.6		K	20	loss	2.373557979e+00	Ndiff
89/1000		1 sec		154.6		K	20	loss	2.370431956e+00	Ndiff
90/1000		1 sec		154.6		K	20	loss	2.361734581e+00	Ndiff
91/1000		1 sec		154.6		K	20	loss	2.356420337e+00	Ndiff
92/1000		1 sec		154.6		K	20	loss	2.356419191e+00	Ndiff
93/1000		1 sec		154.6		K	20	loss	2.356418521e+00	Ndiff
94/1000		1 sec		154.6		K	20 I	loss	2.356418120e+00	Ndiff
95/1000		1 sec			MiB		20	loss		
96/1000		2 sec			MiB		20	loss		
97/1000		2 sec			MiB		20		2.356417640e+00	
98/1000		2 sec			MiB		20	loss		
99/1000		2 sec			MiB		20	loss		
100/1000		2 sec			MiB		20	loss		
101/1000		2 sec			MiB		20	loss		
102/1000		2 sec			MiB		20	loss		
103/1000					MiB					
103/1000		2 sec 2 sec			MiB		20	loss loss		
104/1000		2 sec 2 sec			MiB		20	loss		
106/1000		2 sec 2 sec			MiB		20	loss		
107/1000		2 sec 2 sec			MiB		20	loss		
107/1000		2 sec 2 sec			MiB		20	loss		
109/1000		2 sec 2 sec			MiB		20	loss		
110/1000		2 sec 2 sec			MiB		20	loss		
110/1000	ατι <u>ε</u> τ		· I	104.0		1/	20		Z.JJUHI/HJHETUU	TACTTT

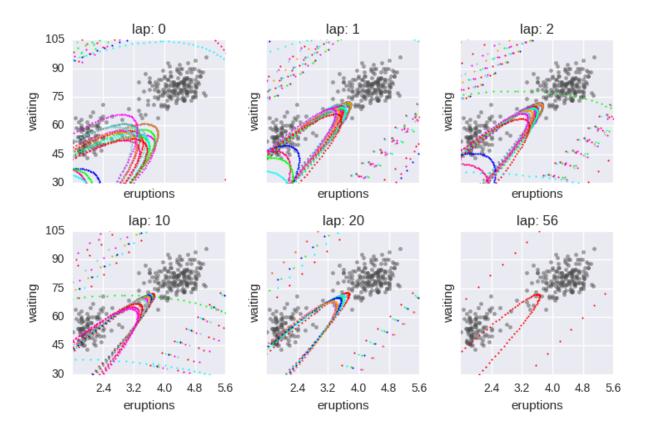
```
111/1000 after
                                                                 2.356417493e+00 | Ndiff
                          2 sec.
                                      154.6 MiB | K
                                                      20 | loss
     112/1000 after
                                                                 2.356417493e+00 | Ndiff
                          2 sec.
                                      154.6 MiB | K
                                                      20 | loss
                                                      20 | loss 2.356417493e+00 | Ndiff
     113/1000 after
                          2 sec.
                                      154.6 MiB | K
     114/1000 after
                                                                 2.356417493e+00 | Ndiff
                          2 sec.
                                      154.6 MiB | K
                                                      20 | loss
     115/1000 after
                          2 sec.
                                      154.6 MiB | K
                                                      20 | loss
                                                                  2.356417493e+00 | Ndiff
     116/1000 after
                          2 sec. |
                                      154.6 MiB | K
                                                      20 | loss
                                                                  2.356417493e+00 | Ndiff
     117/1000 after
                          2 sec.
                                      154.6 MiB | K
                                                      20 | loss
                                                                  2.356417493e+00 | Ndiff
... done. converged.
```

ZeroMeanGauss observations + VB

Assume full covariances and fix all means to zero.

Start with too many clusters (K=20)

```
zm_trained_model, zm_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'ZeroMeanGauss', 'VB',
    output_path='/tmp/faithful/showcase-K=20-lik=ZeroMeanGauss-ECovMat=5*eye/',
    nLap=1000, nTask=1, nBatch=1, convergeThr=0.0001,
    gamma0=gamma, sF=sF, ECovMat='eye',
    K=K, initname='randexamples',
    )
show_clusters_over_time(zm_info_dict['task_output_path'])
```



Out:

64

```
WARNING: Found unrecognized keyword args. These are ignored.
Dataset Summary:
X Data
  num examples: 272
  num dims: 2
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model: Gaussian with fixed zero means, full covariance.
Obs. Data Prior: Wishart on prec matrix Lam
  E[CovMat[k]] =
  [[ 5. 0.]
   [ 0. 5.11
Initialization:
  initname = randexamples
  K = 20 (number of clusters)
  seed = 1607680
  elapsed time: 0.0 sec
Learn Alg: VB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/faithful/showcase-K=20-lik=ZeroMeanGauss-ECovMat=5*eye/1
        1/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 4.019419551e+d0 |
        2/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.989063967e+00 | Ndiff
        3/1000 after
                                                      20 | loss 3.941416771e+00 | Ndiff
                          0 sec. |
                                      154.6 MiB | K
        4/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss
                                                                3.899222162e+00 | Ndiff
                                                      20 | loss 3.876371765e+00 | Ndiff
        5/1000 after
                          0 sec. |
                                      154.6 MiB | K
                          0 sec. |
        6/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.842038547e+00 | Ndiff
                                                      20 | loss 3.808536791e+00 | Ndiff
        7/1000 after
                          0 sec. |
                                      154.6 MiB | K
       8/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.779782054e+00 | Ndiff
                                      154.6 MiB | K
                                                      20 | loss 3.755287922e+00 | Ndiff
        9/1000 after
                          0 sec. |
       10/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.733837701e+00 | Ndiff
                          0 sec. |
       11/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.700117498e+00 | Ndiff
       12/1000 after
                          0 sec. I
                                      154.6 MiB | K
                                                      20 | loss 3.694082693e+00 | Ndiff
                                                      20 | loss 3.686765019e+00 | Ndiff
       13/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.675117147e+00 | Ndiff
       14/1000 after
                          0 sec. I
                                      154.6 MiB | K
       15/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.652297952e+00 | Ndiff
                          0 sec. |
                                                      20 | loss 3.639249110e+00 | Ndiff
       16/1000 after
                          0 sec. |
                                      154.6 MiB | K
       17/1000 after
                                                      20 | loss 3.603588941e+00 | Ndiff
                          0 sec. |
                                      154.6 MiB | K
       18/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.598749399e+00 | Ndiff
                                                      20 | loss 3.592583511e+00 | Ndiff
       19/1000 after
                          0 sec. |
                                      154.6 MiB | K
       20/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.574936974e+00 | Ndiff
       21/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.572459120e+00 | Ndiff
       22/1000 after
                                                      20 | loss 3.570977707e+00 | Ndiff
                          0 sec. |
                                      154.6 MiB | K
                          0 sec. |
       23/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.569306514e+00 | Ndiff
       24/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.567412054e+00 | Ndiff
                          0 sec. |
       25/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.565249330e+00 | Ndiff
       26/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.562749369e+00 | Ndiff
                          0 sec. |
       27/1000 after
                                      154.6 MiB | K
                                                      20 | loss
                                                                3.559772804e+00 | Ndiff
                          0 sec. |
       28/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.555894232e+00 | Ndiff
                          0 sec. |
                                                      20 | loss 3.549078207e+00 | Ndiff
       29/1000 after
                          0 sec. |
                                      154.6 MiB | K
       30/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.531303622e+00 | Ndiff
                          0 sec. |
       31/1000 after
                          0 sec. |
                                      154.6 MiB | K
                                                      20 | loss 3.529382170e+00 | Ndiff
       32/1000 after
                                                      20 | loss 3.527237440e+00 | Ndiff
                          0 sec. |
                                      154.6 MiB | K
                          0 sec. |
       33/1000 after
                                      154.6 MiB | K
                                                      20 | loss 3.524655304e+00 | Ndiff
       34/1000 after
                                                      20 | loss 3.521314832e+00 | Ndiff
                          0 sec. |
                                      154.6 MiB | K
```

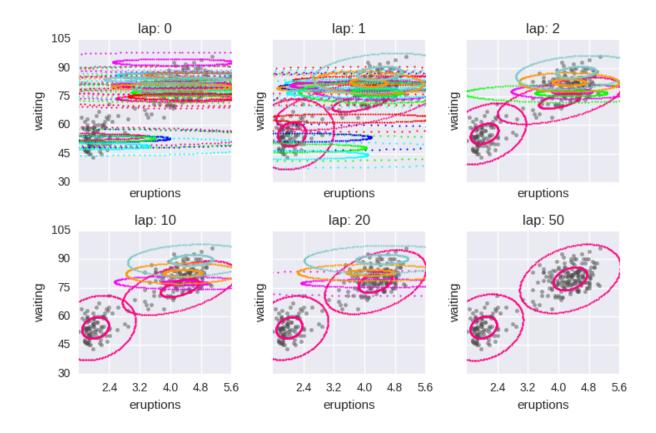
```
20 | loss 3.516111933e+00 | Ndiff
      35/1000 after
                        0 sec. |
                                    154.6 MiB | K
                                                   20 | loss 3.502294322e+00 | Ndiff
      36/1000 after
                        0 sec. |
                                    154.6 MiB | K
      37/1000 after
                                                   20 | loss 3.491586191e+00 | Ndiff
                       0 sec. |
                                    154.6 MiB | K
                                                   20 | loss 3.485039030e+00 | Ndiff
      38/1000 after
                       0 sec. |
                                    154.6 MiB | K
                                                   20 | loss 3.468792370e+00 | Ndiff
      39/1000 after
                        0 sec. I
                                   154.6 MiB | K
      40/1000 after
                        0 sec. |
                                   154.6 MiB | K
                                                   20 | loss 3.467909258e+00 | Ndiff
                                                   20 | loss 3.466944463e+00 | Ndiff
      41/1000 after
                        1 sec. |
                                    154.6 MiB | K
      42/1000 after
                                   154.6 MiB | K
                                                   20 | loss 3.465874350e+00 | Ndiff
                        1 sec. |
                                                   20 | loss 3.464679105e+00 | Ndiff
      43/1000 after
                       1 sec. |
                                   154.6 MiB | K
      44/1000 after
                                  154.6 MiB | K
                                                   20 | loss 3.463333221e+00 | Ndiff
                       1 sec. |
      45/1000 after
                        1 sec. |
                                   154.6 MiB | K
                                                   20 | loss 3.461803293e+00 | Ndiff
                                                   20 | loss 3.460044727e+00 | Ndiff
      46/1000 after
                                   154.6 MiB | K
                       1 sec. |
      47/1000 after
                                   154.6 MiB | K
                                                   20 | loss 3.457996608e+00 | Ndiff
                       1 sec. |
                                                   20 | loss 3.455573178e+00 | Ndiff
      48/1000 after
                        1 sec. |
                                   154.6 MiB | K
      49/1000 after
                                   154.6 MiB | K
                                                   20 | loss 3.452647608e+00 | Ndiff
                        1 sec. |
                                                   20 | loss 3.449011332e+00 | Ndiff
      50/1000 after
                       1 sec. |
                                   154.6 MiB | K
      51/1000 after
                                  154.6 MiB | K
                                                   20 | loss 3.444220039e+00 | Ndiff
                       1 sec. |
                                                   20 | loss 3.436689553e+00 | Ndiff
      52/1000 after
                       1 sec. |
                                  154.6 MiB | K
                                   154.6 MiB | K
      53/1000 after
                        1 sec. |
                                                   20 | loss 3.416217624e+00 | Ndiff
                                                   20 | loss 3.397676918e+00 | Ndiff
      54/1000 after
                                  154.6 MiB | K
                       1 sec. |
      55/1000 after
                        1 sec. |
                                  154.6 MiB | K
                                                   20 | loss 3.395369454e+00 | Ndiff
                                  154.6 MiB | K
                                                   20 | loss 3.395369454e+00 | Ndiff
      56/1000 after
                        1 sec. |
... done. converged.
```

Gauss observations + stochastic VB

Assume full covariances and fix all means to zero.

Start with too many clusters (K=20)

```
stoch_trained_model, stoch_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Gauss', 'soVB',
    output_path=\
        '/tmp/faithful/showcase-K=20-lik=Gauss-ECovMat=5*eye-alg=soVB/',
    nLap=50, nTask=1, nBatch=50,
    rhoexp=0.51, rhodelay=1.0,
    gamma0=gamma, sF=sF, ECovMat='eye',
    K=K, initname='randexamples',
    )
    show_clusters_over_time(stoch_info_dict['task_output_path'])
```



```
Dataset Summary:
X Data
 total size: 272 units
 batch size: 6 units
 num. batches: 50
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior:
                  Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [ 0. 0.]
 E[covar[k]] =
  [[ 5. 0.]
  [ 0. 5.]]
Initialization:
  initname = randexamples
 K = 20 (number of clusters)
  seed = 1607680
  elapsed_time: 0.0 sec
Learn Alg: soVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/faithful/showcase-K=20-lik=Gauss-ECovMat=5*eye-alg=soVB/1
    0.020/50 after
                                                    20 | loss 3.020105590e+01
                        0 sec. |
                                    154.8 MiB | K
    0.040/50 after
                        0 sec. |
                                    154.8 MiB | K
                                                    20 | loss 1.693550049e+01
    0.060/50 after
                        0 sec.
                                    154.8 MiB | K
                                                    20 | loss
                                                               1.182159020e+01
    1.000/50 after
                        1 sec. |
                                                    20 | loss
                                                              1.314590658e+01
                                    154.8 MiB | K
    2.000/50 after
                        1 sec. |
                                    154.8 MiB | K
                                                    20 | loss
                                                              2.522804913e+00
```

1rate 0.

lrate 0.

lrate 0.

lrate 0.

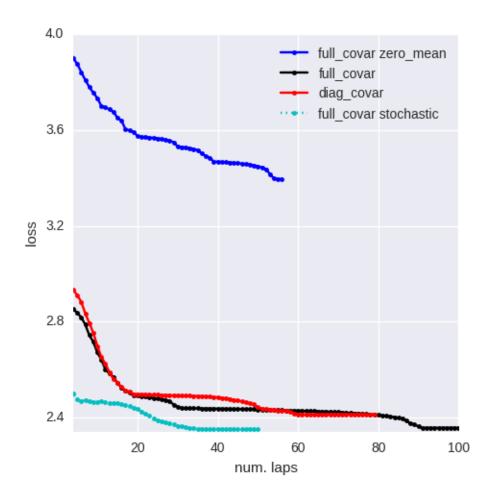
lrate 0.

						_	
3.000/50 after	2 sec.	154.8 MiB K	20	loss	2.507513303e+00	1	lrate
4.000/50 after	3 sec.	154.8 MiB K	20	loss	2.498366509e+00	1	lrate
5.000/50 after	4 sec.	154.8 MiB K	20	loss	2.475120548e+00	1	lrate
6.000/50 after	4 sec.	154.8 MiB K	20	loss	2.469641662e+00	1	lrate
7.000/50 after	5 sec.	154.8 MiB K	20	loss	2.470932762e+00	1	lrate
8.000/50 after	6 sec.	154.8 MiB K	20	loss	2.466158362e+00	1	lrate
9.000/50 after	6 sec.	154.8 MiB K	20	loss	2.465517619e+00	1	lrate
10.000/50 after	7 sec.	154.8 MiB K	20	loss	2.465435382e+00	1	lrate
11.000/50 after	8 sec.	154.8 MiB K	20	loss	2.467696036e+00	1	lrate
12.000/50 after	8 sec.	154.8 MiB K	20	loss	2.461949856e+00	1	lrate
13.000/50 after	9 sec.	154.8 MiB K	20	loss	2.461043110e+00	1	lrate
14.000/50 after	10 sec.	154.8 MiB K	20	loss	2.461264382e+00	1	lrate
15.000/50 after	11 sec.	154.8 MiB K	20	loss	2.458851451e+00	1	lrate
16.000/50 after	11 sec.	154.8 MiB K	20	loss	2.454655643e+00	1	lrate
17.000/50 after	12 sec.	154.8 MiB K	20	loss	2.451234188e+00	1	lrate
18.000/50 after	13 sec.	154.8 MiB K	20	loss	2.446281746e+00	1	lrate
19.000/50 after	13 sec.	154.8 MiB K	20	loss	2.440793273e+00	1	lrate
20.000/50 after	14 sec.	154.8 MiB K	20	loss	2.434143198e+00	1	lrate
21.000/50 after	15 sec.	154.8 MiB K	20	loss	2.423545849e+00	1	lrate
22.000/50 after	15 sec.	154.8 MiB K	20	loss	2.414924985e+00	1	lrate
23.000/50 after	16 sec.	154.8 MiB K	20	loss	2.405741175e+00		lrate
24.000/50 after	17 sec.	154.8 MiB K	20	loss	2.396273286e+00		lrate
25.000/50 after	17 sec.	154.8 MiB K	20	loss	2.388169784e+00	1	lrate
26.000/50 after	18 sec.	154.8 MiB K	20	loss	2.383086462e+00		lrate
27.000/50 after	19 sec.	154.8 MiB K	20	loss	2.378566216e+00		lrate
28.000/50 after	20 sec.	154.8 MiB K	20	loss	2.374468977e+00		lrate
29.000/50 after	20 sec.	154.8 MiB K	20	loss	2.369573743e+00		lrate
30.000/50 after	21 sec.	154.8 MiB K	20	loss	2.365030091e+00		lrate
31.000/50 after	22 sec.	154.8 MiB K	20	loss	2.361840492e+00		lrate
32.000/50 after	22 sec.	154.8 MiB K	20	loss	2.358180297e+00		lrate
33.000/50 after	23 sec.	154.8 MiB K	20	loss	2.355370718e+00	1	lrate
34.000/50 after	24 sec.	154.8 MiB K	20	loss	2.354001069e+00		lrate
35.000/50 after	24 sec.	154.8 MiB K	20	loss	2.352655966e+00		lrate
36.000/50 after	25 sec.	154.8 MiB K	20	loss	2.351706756e+00		lrate
37.000/50 after	26 sec.	154.8 MiB K		loss	2.351346242e+00		lrate
38.000/50 after	27 sec.	154.8 MiB K		loss	2.351470554e+00	1	lrate
39.000/50 after	27 sec.	154.8 MiB K	20	loss	2.351530696e+00	1	lrate
40.000/50 after	28 sec.	154.8 MiB K	20	loss	2.351708300e+00	1	lrate
41.000/50 after	29 sec.	154.8 MiB K	20	loss	2.351489520e+00		lrate
42.000/50 after	29 sec.	154.8 MiB K	20	loss	2.351625569e+00		lrate
43.000/50 after	30 sec.	154.8 MiB K	20	loss	2.351357552e+00		lrate
44.000/50 after	31 sec.	154.8 MiB K	20	loss	2.351536177e+00		lrate
45.000/50 after	32 sec.	154.8 MiB K		loss	2.351543540e+00		lrate
46.000/50 after	32 sec.	154.8 MiB K		loss	2.351346627e+00		lrate
47.000/50 after	33 sec.	154.8 MiB K	20	loss	2.351293738e+00		lrate
48.000/50 after	34 sec.	154.8 MiB K		loss	2.351507196e+00		lrate
49.000/50 after	34 sec.	154.8 MiB K		loss	2.351496294e+00		lrate
50.000/50 after	35 sec.	154.8 MiB K	20	loss	2.351523756e+00	П	lrate
active. not conv	erged.						

0. 0.

Compare loss function traces for all methods

```
pylab.figure()
pylab.plot(
    zm_info_dict['lap_history'],
    zm_info_dict['loss_history'], 'b.-',
    label='full_covar zero_mean')
pylab.plot(
    full_info_dict['lap_history'],
    full_info_dict['loss_history'], 'k.-',
    label='full_covar')
pylab.plot(
    diag_info_dict['lap_history'],
    diag_info_dict['loss_history'], 'r.-',
    label='diag_covar')
pylab.plot(
    stoch_info_dict['lap_history'],
    stoch_info_dict['loss_history'], 'c.:',
    label='full_covar stochastic')
pylab.legend(loc='upper right')
pylab.xlabel('num. laps')
pylab.ylabel('loss')
pylab.xlim([4, 100]) # avoid early iterations
pylab.ylim([2.34, 4.0]) # handpicked
pylab.draw()
pylab.tight_layout()
```



Total running time of the script: (0 minutes 42.505 seconds)

Download Python source code: plot-01-demo=vb_algs-model=mix_gauss.py

Download Jupyter notebook: plot-01-demo=vb_algs-model=mix_gauss.ipynb

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5.2.4 Toy bars dataset: one bar per doc

Variational training of mixture models and topic models with Multinomial likelihoods on simple toy "bars" dataset.

01: Standard variational training for mixture model

How to train a mixture of multinomials.

```
import bnpy
import numpy as np
import os
```

```
from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (3, 3)
SMALL_FIG_SIZE = (1,1)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read toy "bars" dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'bars_one_per_doc')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'))
```

Make a simple plot of the raw data



Let's do one single run of the VB algorithm.

Using 10 clusters and the 'randexamples' initializatio procedure.

```
trained_model, info_dict = bnpy.run(
    dataset, 'FiniteMixtureModel', 'Mult', 'VB',
    output_path='/tmp/bars_one_per_doc/helloworld-K=10/',
    nLap=1000, convergeThr=0.0001,
    K=10, initname='randomlikewang',
    gamma0=50.0, lam=0.1)
```

Out:

```
WARNING: Found unrecognized keyword args. These are ignored.

--gamma0

Dataset Summary:

BagOfWordsData

size: 2000 units (documents)

vocab size: 144

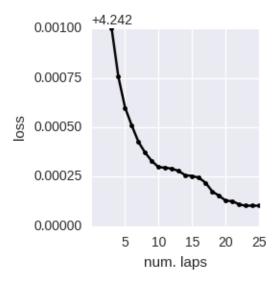
min 5% 50% 95% max
```

```
38
        42
               46
                    51
                          57
                              nUniqueTokensPerDoc
  100
        100
              100
                    100
                         100
                              nTotalTokensPerDoc
Hist of word_count across tokens
            2
                    3
     1
                        <10
                              <100
                                    >=100
         0.29
                0.19
                       0.14
                                 0
   0.38
Hist of unique docs per word type
           < 10
                <100 < 0.10
                             <0.20
                                    <0.50 >=0.50
            0
                   0
                                 0
                                     >.99
Allocation Model: Finite mixture model. Dir prior param 1.00
Obs. Data Model: Multinomial over finite vocabulary.
Obs. Data Prior: Dirichlet over finite vocabulary
  lam = [0.1 0.1] \dots
Initialization:
 initname = randomlikewang
 K = 10 (number of clusters)
  seed = 1607680
  elapsed time: 0.0 sec
Learn Alg: VB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/bars_one_per_doc/helloworld-K=10/1
        1/1000 after
                         0 sec. | 151.2 MiB | K
                                                     10 | loss 4.711444785e+00 |
        2/1000 after
                                                     10 | loss 4.244123622e+00 | Ndiff
                         0 sec. |
                                     151.2 MiB | K
        3/1000 after
                                     151.2 MiB | K
                                                     10 | loss 4.242999256e+00 | Ndiff
                         0 sec. |
        4/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss
                                                                4.242755538e+00 | Ndiff
        5/1000 after
                                                     10 | loss 4.242599251e+d0 | Ndiff
                         0 sec. |
                                     151.2 MiB | K
        6/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242508901e+00 | Ndiff
       7/1000 after
                                                     10 | loss 4.242425981e+00 | Ndiff
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242371327e+00 | Ndiff
       8/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242328843e+00 | Ndiff
        9/1000 after
                         0 sec. |
                                     151.2 MiB | K
       10/1000 after
                                     151.2 MiB | K
                                                     10 | loss 4.242298419e+00 | Ndiff
                         0 sec. |
       11/1000 after
                                     151.2 MiB | K
                                                     10 | loss 4.242296009e+00 | Ndiff
                         0 sec. |
       12/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242290695e+00 | Ndiff
                                                     10 | loss 4.242278821e+00 | Ndiff
       13/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                     151.2 MiB | K
                                                     10 | loss 4.242257185e+00 | Ndiff
      14/1000 after
                       0 sec. |
       15/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242254419e+00 | Ndiff
       16/1000 after
                                                     10 | loss 4.242244922e+00 | Ndiff
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242219919e+00 | Ndiff
       17/1000 after
                         0 sec. |
                                     151.2 MiB | K
                         0 sec. |
       18/1000 after
                                     151.2 MiB | K
                                                     10 | loss 4.242175380e+00 | Ndiff
       19/1000 after
                                                     10 | loss 4.242154460e+00 | Ndiff
                         0 sec. |
                                     151.2 MiB | K
       20/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242128894e+00 | Ndiff
                                                     10 | loss 4.242126836e+00 | Ndiff
       21/1000 after
                         0 sec. |
                                     151.2 MiB | K
       22/1000 after
                                                     10 | loss 4.242109815e+00 | Ndiff
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242103791e+00 | Ndiff
       23/1000 after
                         0 sec. |
                                     151.2 MiB | K
       24/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242103790e+00 | Ndiff
       25/1000 after
                         0 sec. |
                                     151.2 MiB | K
                                                     10 | loss 4.242103790e+00 | Ndiff
... done. converged.
```

First, we can plot the loss function over time We'll skip the first few iterations, since performance is quite bad.

```
pylab.figure(figsize=FIG_SIZE)
pylab.plot(info_dict['lap_history'][2:], info_dict['loss_history'][2:], 'k.-')
pylab.xlabel('num. laps')
pylab.ylabel('loss')
```

pylab.tight_layout()



Setup: Useful function to display learned bar structure over time.

```
def show_bars_over_time(
       task_output_path=None,
        query_laps=[0, 1, 2, 5, None],
        ncols=10):
    , , ,
    nrows = len(query_laps)
    fig_handle, ax_handles_RC = pylab.subplots(
        figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
       nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for row_id, lap_val in enumerate(query_laps):
        cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
        cur_topics_KV = cur_model.obsModel.getTopics()
        # Plot the current model
        cur_ax_list = ax_handles_RC[row_id].flatten().tolist()
        bnpy.viz.BarsViz.show_square_images(
            cur topics KV,
            vmin=0.0, vmax=0.06,
            ax_list=cur_ax_list)
        cur_ax_list[0].set_ylabel("lap: %d" % lap_val)
    pylab.tight_layout()
```

Show the clusters over time

```
show_bars_over_time(info_dict['task_output_path'])
```



Total running time of the script: (0 minutes 5.443 seconds)

Download Python source code: plot-01-demo=vb_single_run-model=mix+mult.py

Download Jupyter notebook: plot-01-demo=vb_single_run-model=mix+mult.ipynb

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05: Training for HDP Topic Model with birth and merge proposals

```
import bnpy
import numpy as np
import os
import sys

from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (3, 3)
SMALL_FIG_SIZE = (1,1)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'bars_one_per_doc')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'))
```

Set the local step algorithmic keyword args

```
local_step_kwargs = dict(
    # Perform at most this many iterations at each document
    nCoordAscentItersLP=100,
```

```
# Stop local iters early when max change in doc-topic counts < this thr
    convThrLP=0.01,
    restartLP=0,
    doMemoizeLocalParams=0,
)

merge_kwargs = dict(
    m_startLap=5,
    m_pair_ranking_procedure='total_size',
    m_pair_ranking_direction='descending',
)

birth_kwargs = dict(
    b_startLap=2,
    b_stopLap=6,
    b_Kfresh=3,
    b_nRefineSteps=5,
)</pre>
```

Setup: Helper function to plot bars at each stage of training

```
def show_bars_over_time(
       task_output_path=None,
       query_laps=[0, 1, 2, 5, None],
       ncols=10):
    1 1 1
   nrows = len(query_laps)
   fig_handle, ax_handles_RC = pylab.subplots(
        figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
       nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for row_id, lap_val in enumerate(query_laps):
       cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
       cur_topics_KV = cur_model.obsModel.getTopics()
        # Plot the current model
       cur_ax_list = ax_handles_RC[row_id].flatten().tolist()
       bnpy.viz.BarsViz.show_square_images(
            cur topics KV,
            vmin=0.0, vmax=0.06,
            ax_list=cur_ax_list)
        cur_ax_list[0].set_ylabel("lap: %d" % lap_val)
   pylab.tight_layout()
```

Training from K=3 with births

Initialization: 3 topics, using random initial guess

```
trained_model, info_dict = bnpy.run(
    dataset, 'HDPTopicModel', 'Mult', 'memoVB',
    output_path='/tmp/bars_one_per_doc/trymoves-model=hdp+mult-K=3-moves=birth, merge, shuff.
    nLap=20, convergeThr=0.001, nBatch=1,
    K=3, initname='randomlikewang',
```

Total running time of the script: (0 minutes 0.000 seconds)

```
Download Python source code: run-05-demo=topic_model_vb+births-model=hdp_topic+multopic+multopic Download Jupyter notebook: run-05-demo=topic_model_vb+births-model=hdp_topic+multopic+multopic Download Sphinx-Gallery
```

04: Training HDP Topic Model with merge proposals

```
import bnpy
import numpy as np
import os
import sys

from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (3, 3)
SMALL_FIG_SIZE = (1,1)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'bars_one_per_doc')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'))
```

Set the local step algorithmic keyword args

```
local_step_kwargs = dict(
    # Perform at most this many iterations at each document
    nCoordAscentItersLP=100,
    # Stop local iters early when max change in doc-topic counts < this thr
    convThrLP=0.001,
    restartLP=0,
    doMemoizeLocalParams=0,
    )

merge_kwargs = dict(
    m_startLap=5,
    m_pair_ranking_procedure='total_size',
    m_pair_ranking_direction='descending',
    )</pre>
```

Run the VB+proposals algorithm with only merges and re-shuffling.

Initialization: 10 topics, using randomlikewang

```
trained_model, info_dict = bnpy.run(
    dataset, 'HDPTopicModel', 'Mult', 'memoVB',
    output_path=
        '/tmp/bars_one_per_doc/' +
        'trymoves-model=hdp+mult-K=10-moves=merge, shuffle/',
    nLap=50, convergeThr=0.001, nBatch=1,
    K=10, initname='randomlikewang',
    alpha=0.5, lam=0.1,
    moves='merge, shuffle',
    **dict(merge_kwargs.items() + local_step_kwargs.items()))
```

```
def show_bars_over_time(
       task_output_path=None,
       query_laps=[0, 1, 2, 5, None],
       ncols=10):
    ''' Show square-image visualization of estimated topics over time.
   Post Condition
   New matplotlib figure with visualization (one row per lap).
   nrows = len(query_laps)
   fig_handle, ax_handles_RC = pylab.subplots(
        figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
       nrows=nrows, ncols=ncols, sharex=True, sharey=True)
   for row_id, lap_val in enumerate(query_laps):
       cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
       cur_topics_KV = cur_model.obsModel.getTopics()
        # Plot the current model
       cur_ax_list = ax_handles_RC[row_id].flatten().tolist()
       bnpy.viz.BarsViz.show_square_images(
            cur_topics_KV,
            vmin=0.0, vmax=0.06,
            ax_list=cur_ax_list)
        cur_ax_list[0].set_ylabel("lap: %d" % lap_val)
   pylab.tight_layout()
```

Examine the bars over time

```
show_bars_over_time(info_dict['task_output_path'])
```

Total running time of the script: (0 minutes 0.000 seconds)

02: Training DP mixture model with birth and merge proposals

How to train a DP mixture of multinomials.

```
import bnpy
import numpy as np
import os

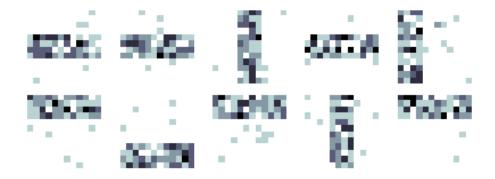
from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (3, 3)
SMALL_FIG_SIZE = (1.5, 1.5)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'bars_one_per_doc')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'))
```

Make a simple plot of the raw data



Setup: Function to show bars from start to end of training run

```
def show_bars_over_time(
          task_output_path=None,
          query_laps=[0, 1, 2, 5, None],
          ncols=10):
          rows = len(query_laps)
          fig_handle, ax_handles_RC = pylab.subplots(
                figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
                nrows=nrows, ncols=ncols, sharex=True, sharey=True)
          for row_id, lap_val in enumerate(query_laps):
                cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
```

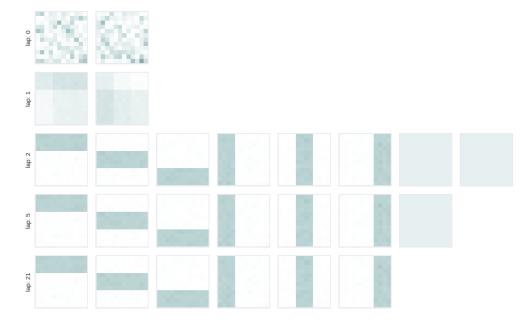
From K=2 initial clusters

Using random initialization

```
initname = 'randomlikewang'
K = 2

K2_trained_model, K2_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Mult', 'memoVB',
    output_path='/tmp/bars_one_per_doc/trymoves-K=%d-initname=%s/' % (
        K, initname),
    nTask=1, nLap=50, convergeThr=0.0001, nBatch=1,
    K=K, initname=initname,
    gamma0=50.0, lam=0.1,
    moves='birth,merge,shuffle,delete',
    b_startLap=2,
    m_startLap=5,
    d_startLap=10)

show_bars_over_time(K2_info_dict['task_output_path'])
```



Out:

```
Dataset Summary:
BagOfWordsData
 total size: 2000 units
 batch size: 2000 units
 num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 50.00
Obs. Data Model: Multinomial over finite vocabulary.
Obs. Data Prior: Dirichlet over finite vocabulary
 lam = [ 0.1 0.1 ] ...
Initialization:
 initname = randomlikewang
 K = 2 (number of clusters)
 seed = 1607680
 elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/bars_one_per_doc/trymoves-K=2-initname=randomlikewang/1
BIRTH @ lap 1.00: Disabled. Waiting for lap >= 2 (--b_startLap).
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent w
DELETE @ lap 1.00: Disabled. Cannot delete before first complete lap, because $S that repre
    1.000/50 after
                       0 sec. | 166.4 MiB | K 2 | loss 4.852914927e+00 |
MERGE @ lap 2.00: Disabled. Waiting for lap >= 5 (--m_startLap).
DELETE @ lap 2.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 2.00 : Added 6 states. 2/2 succeeded. 0/2 failed eval phase. 0/2 failed build
    2.000/50 after
                    0 sec. | 166.4 MiB | K 8 | loss 4.125791748e+00 |
MERGE @ lap 3.00: Disabled. Waiting for lap >= 5 (--m startLap).
DELETE @ lap 3.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 3.00 : Added 0 states. 0/6 succeeded. 0/6 failed eval phase. 6/6 failed build
    3.000/50 after
                      1 sec. | 166.4 MiB | K 8 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 4.00: Disabled. Waiting for lap >= 5 (--m_startLap).
DELETE @ lap 4.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 4.000 : None attempted. 6 past failures. 2 too small. 0 too busy.
   4.000/50 after 1 sec. | 166.4 MiB | K 8 | loss 4.125791567e+00 | Ndiff
DELETE @ lap 5.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 5.000 : None attempted. O past failures. O too small. 8 too busy.
MERGE @ lap 5.00 : 1/16 accepted. Ndiff 0.00. 0 skipped.
    5.000/50 after 1 sec. | 166.4 MiB | K 7 | loss 4.125791567e+00 | Ndiff
DELETE @ lap 6.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 6.000 : None attempted. 1 past failures. 0 too small. 6 too busy.
MERGE @ lap 6.00 : 1/5 accepted. Ndiff 0.00. 0 skipped.
   6.000/50 after 1 sec. | 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
DELETE @ lap 7.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 7.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
MERGE @ lap 7.00 : 0/5 accepted. Ndiff 0.00. 0 skipped.
                                                   6 | loss 4.125791567e+00 | Ndiff
    7.000/50 after
                    1 sec. | 166.4 MiB | K
MERGE @ lap 8.00: No promising candidates, so no attempts.
DELETE @ lap 8.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 8.00 : Added 0 states. 0/1 succeeded. 0/1 failed eval phase. 1/1 failed build
   8.000/50 after
                      2 sec. |
                                 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 9.00: No promising candidates, so no attempts.
DELETE @ lap 9.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 9.000 : None attempted. 6 past failures. 0 too small. 0 too busy.
    9.000/50 after 2 sec. | 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 10.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
```

```
DELETE @ lap 10.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 10.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  10.000/50 after
                       2 sec. |
                                 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 11.00: No promising candidates, so no attempts.
BIRTH @ lap 11.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 11.00: 0/1 accepted. Ndiff 0.00.
  11.000/50 after
                   2 sec. | 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 12.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 12.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 12.00 : 0/5 accepted. Ndiff 0.00. 0 skipped.
   12.000/50 after
                       2 sec. | 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 13.00: No promising candidates, so no attempts.
BIRTH @ lap 13.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 13.00: 0/1 accepted. Ndiff 0.00.
   13.000/50 after
                       2 sec. |
                                 166.4 MiB | K
                                                 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 14.00: No promising candidates, so no attempts.
BIRTH @ lap 14.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 14.00: 0/1 accepted. Ndiff 0.00.
   14.000/50 after
                       2 sec. | 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 15.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 15.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 15.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  15.000/50 after
                   2 sec. | 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 16.00: No promising candidates, so no attempts.
BIRTH @ lap 16.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 16.00: 0/1 accepted. Ndiff 0.00.
   16.000/50 after
                       2 sec. |
                                  166.4 MiB | K
                                                  6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 17.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 17.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 17.00 : 0/5 accepted. Ndiff 0.00. 0 skipped.
   17.000/50 after
                       3 sec. |
                                 166.4 MiB | K
                                                   6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 18.00: No promising candidates, so no attempts.
BIRTH @ lap 18.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 18.00: 0/1 accepted. Ndiff 0.00.
   18.000/50 after
                       3 sec. |
                                   166.4 MiB | K
                                                   6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 19.00: No promising candidates, so no attempts.
BIRTH @ lap 19.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 19.00: 0/1 accepted. Ndiff 0.00.
  19.000/50 after
                      3 sec. |
                                  166.4 MiB | K
                                                 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 20.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 20.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 20.00 : 0/10 accepted. Ndiff 0.00. 0 skipped.
  20.000/50 after
                       3 sec. | 166.4 MiB | K
                                                  6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 21.00: No promising candidates, so no attempts.
BIRTH @ lap 21.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 21.00: 0/1 accepted. Ndiff 0.00.
  21.000/50 after
                      3 sec. | 166.4 MiB | K 6 | loss 4.125791567e+00 | Ndiff
... done. converged.
```

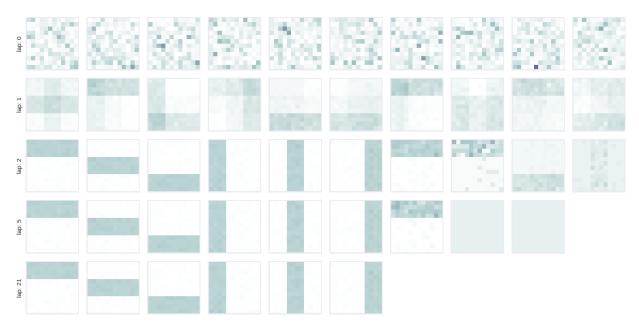
K=10 initial clusters

Using random initialization

```
initname = 'randomlikewang'
K = 10

K10_trained_model, K10_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Mult', 'memoVB',
    output_path='/tmp/bars_one_per_doc/trymoves-K=%d-initname=%s/' % (
        K, initname),
    nTask=1, nLap=50, convergeThr=0.0001, nBatch=1,
    K=K, initname=initname,
    gamma0=50.0, lam=0.1,
    moves='birth,merge,shuffle,delete',
    b_startLap=2,
    m_startLap=5,
    d_startLap=10)

show_bars_over_time(K10_info_dict['task_output_path'])
```



Out:

```
Dataset Summary:
BagOfWordsData
  total size: 2000 units
  batch size: 2000 units
  num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 50.00
Obs. Data Model: Multinomial over finite vocabulary.
Obs. Data Prior: Dirichlet over finite vocabulary
  lam = [ 0.1  0.1] ...
Initialization:
  initname = randomlikewang
  K = 10 (number of clusters)
  seed = 1607680
  elapsed_time: 0.0 sec
```

```
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/bars_one_per_doc/trymoves-K=10-initname=randomlikewang/1
BIRTH @ lap 1.00: Disabled. Waiting for lap >= 2 (--b_startLap).
MERGE @ lap 1.00: Disabled. Cannot plan merge on first lap. Need valid SS that represent w
DELETE @ lap 1.00: Disabled. Cannot delete before first complete lap, because $S that repre
   1.000/50 after
                      0 sec. | 173.4 MiB | K 10 | loss 4.712365207e+00 |
MERGE @ lap 2.00: Disabled. Waiting for lap >= 5 (--m_startLap).
DELETE @ lap 2.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 2.00 : Added 2 states. 1/6 succeeded. 0/6 failed eval phase. 5/6 failed build
    2.000/50 after
                      1 sec. | 174.0 MiB | K 12 | loss 4.128419662e+00 |
MERGE @ lap 3.00: Disabled. Waiting for lap >= 5 (--m_startLap).
DELETE @ lap 3.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 3.00 : Added 0 states. 0/4 succeeded. 0/4 failed eval phase. 4/4 failed build
    3.000/50 after 1 sec. | 174.0 MiB | K 12 | loss 4.127318928e+00 | Ndiff
MERGE @ lap 4.00: Disabled. Waiting for lap >= 5 (--m_startLap).
DELETE @ lap 4.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 4.00 : Added 0 states. 0/2 succeeded. 0/2 failed eval phase. 2/2 failed build
                      1 sec. | 174.0 MiB | K 12 | loss 4.127075221e+00 | Ndiff
    4.000/50 after
                                                                                      1
DELETE @ lap 5.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 5.000 : None attempted. 0 past failures. 0 too small. 12 too busy.
MERGE @ lap 5.00 : 3/18 accepted. Ndiff 0.00. 12 skipped.
    5.000/50 after 2 sec. | 174.0 MiB | K 9 | loss 4.126920998e+00 | Ndiff
DELETE @ lap 6.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 6.000 : None attempted. 1 past failures. 0 too small. 8 too busy.
MERGE @ lap 6.00 : 3/5 accepted. Ndiff 21.29. 10 skipped.
    6.000/50 after
                       2 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
                                                                                      1
DELETE @ lap 7.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 7.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
MERGE @ lap 7.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
    7.000/50 after
                    2 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 8.00: No promising candidates, so no attempts.
DELETE @ lap 8.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 8.00 : Added 0 states. 0/2 succeeded. 0/2 failed eval phase. 2/2 failed build
    8.000/50 after
                      2 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 9.00: No promising candidates, so no attempts.
DELETE @ lap 9.00: Disabled. Waiting for lap >= 10 (--d_startLap).
BIRTH @ lap 9.000 : None attempted. 6 past failures. 0 too small. 0 too busy.
    9.000/50 after 2 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 10.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 10.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 10.00 : 0/6 accepted. Ndiff 0.00. 0 skipped.
   10.000/50 after
                       2 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 11.00: No promising candidates, so no attempts.
BIRTH @ lap 11.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 11.00: 0/1 accepted. Ndiff 0.00.
  11.000/50 after 2 sec. | 174.0 MiB | K
                                                 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 12.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 12.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 12.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
                       3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
   12.000/50 after
MERGE @ lap 13.00: No promising candidates, so no attempts.
BIRTH @ lap 13.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 13.00: 0/1 accepted. Ndiff 0.00.
```

```
13.000/50 after
                      3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 14.00: No promising candidates, so no attempts.
BIRTH @ lap 14.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 14.00: 0/1 accepted. Ndiff 0.00.
  14.000/50 after 3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 15.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 15.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 15.00 : 0/6 accepted. Ndiff 0.00. 0 skipped.
  15.000/50 after 3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 16.00: No promising candidates, so no attempts.
BIRTH @ lap 16.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 16.00: 0/1 accepted. Ndiff 0.00.
  16.000/50 after
                      3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 17.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 17.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 17.00 : 0/9 accepted. Ndiff 0.00. 0 skipped.
  17.000/50 after
                      3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
MERGE @ lap 18.00: No promising candidates, so no attempts.
BIRTH @ lap 18.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 18.00: 0/1 accepted. Ndiff 0.00.
                     3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
  18.000/50 after
MERGE @ lap 19.00: No promising candidates, so no attempts.
BIRTH @ lap 19.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 19.00: 0/1 accepted. Ndiff 0.00.
  19.000/50 after
                      3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
BIRTH @ lap 20.000 : None attempted. 0 past failures. 0 too small. 6 too busy.
DELETE @ lap 20.00: 0/1 accepted. Ndiff 0.00.
MERGE @ lap 20.00: 0/6 accepted. Ndiff 0.00. 0 skipped.
                     3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
  20.000/50 after
MERGE @ lap 21.00: No promising candidates, so no attempts.
BIRTH @ lap 21.000 : None attempted. O past failures. O too small. 6 too busy.
DELETE @ lap 21.00: 0/1 accepted. Ndiff 0.00.
  21.000/50 after
                      3 sec. | 174.0 MiB | K 6 | loss 4.125791567e+00 | Ndiff
... done. converged.
```

Total running time of the script: (0 minutes 15.776 seconds)

Download Python source code: plot-02-demo=vb+proposals-model=dp_mix+mult.py

Download Jupyter notebook: plot-02-demo=vb+proposals-model=dp_mix+mult.ipynb

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03: Standard variational training for topic model

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (3, 3)
```

```
SMALL_FIG_SIZE = (1,1)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'bars_one_per_doc')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'))
```

Make a simple plot of the raw data

Setup: Function to show bars from start to end of training run

```
def show_bars_over_time(
       task_output_path=None,
        query_laps=[0, 1, 2, 5, None],
        ncols=10):
    . . .
    1 1 1
    nrows = len(query_laps)
    fig_handle, ax_handles_RC = pylab.subplots(
        figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
        nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for row_id, lap_val in enumerate(query_laps):
        cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
        cur_topics_KV = cur_model.obsModel.getTopics()
        # Plot the current model
        cur_ax_list = ax_handles_RC[row_id].flatten().tolist()
        bnpy.viz.BarsViz.show_square_images(
            cur_topics_KV,
            vmin=0.0, vmax=0.06,
            ax_list=cur_ax_list)
        cur_ax_list[0].set_ylabel("lap: %d" % lap_val)
    pylab.tight_layout()
```

Train LDA topic model

Using 10 clusters and the 'randexamples' initialization procedure.

```
local_step_kwargs = dict(
    # perform at most this many iterations at each document
    nCoordAscentItersLP=100,
    # stop local iters early when max change in doc-topic counts < this thr
    convThrLP=0.001,
    )
trained_model, info_dict = bnpy.run(</pre>
```

```
dataset, 'FiniteTopicModel', 'Mult', 'VB',
  output_path='/tmp/bars_one_per_doc/helloworld-model=topic+mult-K=10/',
  nLap=100, convergeThr=0.01,
  K=10, initname='randomlikewang',
  alpha=0.5, lam=0.1,
  **local_step_kwargs)
```

First, we can plot the loss function over time We'll skip the first few iterations, since performance is quite bad.

```
pylab.figure(figsize=FIG_SIZE)
pylab.plot(info_dict['lap_history'][1:], info_dict['loss_history'][1:], 'k.-')
pylab.xlabel('num. laps')
pylab.ylabel('loss')
pylab.tight_layout()
```

Show the clusters over time

```
show_bars_over_time(info_dict['task_output_path'])
```

Train LDA topic model with restarts

Using 10 clusters and the 'randexamples' initialization procedure.

```
r_local_step_kwargs = dict(
    # perform at most this many iterations at each document
   nCoordAscentItersLP=100,
   # stop local iters early when max change in doc-topic counts < this thr
   convThrLP=0.001,
    # perform restart proposals at each document
   restartLP=1,
   restartNumItersLP=5,
   restartNumTrialsLP=5,
r_trained_model, r_info_dict = bnpy.run(
   dataset, 'FiniteTopicModel', 'Mult', 'VB',
   output_path='/tmp/bars_one_per_doc/helloworld-model=topic+mult-K=10-localstep=restarts
   nLap=100, convergeThr=0.01,
   K=10, initname='randomlikewang',
   alpha=0.5, lam=0.1,
   **r_local_step_kwargs)
show_bars_over_time(r_info_dict['task_output_path'])
```

Total running time of the script: (0 minutes 0.000 seconds)

```
Download Python source code: run-03-demo=topic_model_vb_single_run-model=hdp_topic_model_vb_single_run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic+run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-model=hdp_topic-run-mod
```

5.2.5 Toy bars dataset: many bars per doc

Variational training of mixture models and topic models with Multinomial likelihoods on toy "bars" dataset with multiple bars per document.

01: Standard variational training for mixture model

How to train a mixture of multinomials.

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (3, 3)
SMALL_FIG_SIZE = (1,1)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read toy "bars" dataset from file.

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'bars_many_per_doc')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'))
```

Make a simple plot of the raw data

```
X_csr_DV = dataset.getSparseDocTypeCountMatrix()
bnpy.viz.BarsViz.show_square_images(
    X_csr_DV[:10].toarray(), vmin=0, vmax=5)
#pylab.colorbar()
#pylab.clabel('word count')
pylab.tight_layout()
```

Let's do one single run of the VB algorithm.

Using 10 clusters and the 'randexamples' initializatio procedure.

```
trained_model, info_dict = bnpy.run(
    dataset, 'FiniteMixtureModel', 'Mult', 'VB',
    output_path='/tmp/bars_many_per_doc/helloworld-K=10/',
    nLap=1000, convergeThr=0.0001,
    K=10, initname='randomlikewang',
    gamma0=50.0, lam=0.1)
```

First, we can plot the loss function over time We'll skip the first few iterations, since performance is quite bad.

```
pylab.figure(figsize=FIG_SIZE)
pylab.plot(info_dict['lap_history'][2:], info_dict['loss_history'][2:], 'k.-')
pylab.xlabel('num. laps')
```

```
pylab.ylabel('loss')
pylab.tight_layout()
```

Setup: Useful function to display learned bar structure over time.

```
def show_bars_over_time(
       task_output_path=None,
       query_laps=[0, 1, 2, 5, None],
       ncols=10):
   nrows = len(query_laps)
   fig_handle, ax_handles_RC = pylab.subplots(
       figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
       nrows=nrows, ncols=ncols, sharex=True, sharey=True)
   for row_id, lap_val in enumerate(query_laps):
       cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
       cur_topics_KV = cur_model.obsModel.getTopics()
        # Plot the current model
       cur_ax_list = ax_handles_RC[row_id].flatten().tolist()
       bnpy.viz.BarsViz.show_square_images(
            cur_topics_KV,
            vmin=0.0, vmax=0.06,
            ax_list=cur_ax_list)
       cur_ax_list[0].set_ylabel("lap: %d" % lap_val)
   pylab.tight_layout()
```

Show the clusters over time

```
show_bars_over_time(info_dict['task_output_path'])
```

Total running time of the script: (0 minutes 0.000 seconds)

```
Download Python source code: run-01-demo=vb_single_run-model=mix+mult.py

Download Jupyter notebook: run-01-demo=vb_single_run-model=mix+mult.ipynb

Generated by Sphinx-Gallery
```

5.2.6 we8there bag-of-words text dataset

Text from some restaurant reviews (Taddy 2012). Variational training of mixture models and topic models with Multinomial likelihoods.

VB coordinate descent for Mixture of Multinomials

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns
```

```
FIG_SIZE = (3, 3)
SMALL_FIG_SIZE = (1,1)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read text dataset from file

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'we8there', 'raw')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'),
    vocabfile=os.path.join(dataset_path, 'x_csc_colnames.txt'))

# Filter out documents with less than 20 words
doc_ids = np.flatnonzero(
    dataset.getDocTypeCountMatrix().sum(axis=1) >= 20)
dataset = dataset.make_subset(docMask=doc_ids, doTrackFullSize=False)
```

Make a simple plot of the raw data

```
bnpy.viz.PrintTopics.plotCompsFromWordCounts(
    dataset.getDocTypeCountMatrix()[:10],
    dataset.vocabList,
    prefix='doc',
    Ktop=10)
```

Train with birth and merge proposals

Take the best of 1 initializations

Ideally, we'd run this longer, but this is convenient for rapid inspection.

```
merge kwargs = dict(
   m_startLap=5,
    m_pair_ranking_procedure='elbo',
    m_pair_ranking_direction='descending',
    m_pair_ranking_do_exclude_by_thr=1,
    m pair ranking exclusion thr=-0.0005,
    )
trained_model, info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Mult', 'memoVB',
    output_path='/tmp/we8there/helloworld-model=dp_mix+mult-K=30/',
    nLap=15, convergeThr=0.0001, nTask=1, nBatch=1,
    K=30, initname='bregmankmeans+lam1+iter1',
    gamma0=50.0, lam=0.1,
    moves='birth, merge, shuffle',
    b_startLap=2, b_Kfresh=5, b_stopLap=10,
    **merge_kwargs)
bnpy.viz.PrintTopics.plotCompsFromHModel(
    trained model,
    vocabList=dataset.vocabList,
    Ktop=10)
```

Total running time of the script: (0 minutes 0.000 seconds)

Download Python source code: run-02-demo=mix_vb+proposals-model=dp_mix+mult.py

Download Jupyter notebook: run-02-demo=mix_vb+proposals-model=dp_mix+mult.ipynb

Generated by Sphinx-Gallery

VB coordinate descent for Mixture of Multinomials

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (3, 3)
SMALL_FIG_SIZE = (1,1)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Read text dataset from file

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'we8there', 'raw')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'),
    vocabfile=os.path.join(dataset_path, 'x_csc_colnames.txt'))

# Filter out documents with less than 20 words
doc_ids = np.flatnonzero(
    dataset.getDocTypeCountMatrix().sum(axis=1) >= 20)
dataset = dataset.make_subset(docMask=doc_ids, doTrackFullSize=False)
```

Make a simple plot of the raw data

```
bnpy.viz.PrintTopics.plotCompsFromWordCounts(
   dataset.getDocTypeCountMatrix()[:10],
   dataset.vocabList,
   prefix='doc',
   Ktop=10)
```

Train with K=1 cluster

This is a simple baseline.

```
trained_model, info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Mult', 'VB',
    output_path='/tmp/we8there/helloworld-model=dp_mix+mult-K=1/',
    nLap=1000, convergeThr=0.0001, nTask=1,
    K=1, initname='bregmankmeans+lam1+iter1',
    gamma0=50.0, lam=0.1)
```

```
bnpy.viz.PrintTopics.plotCompsFromHModel(
    trained_model,
    vocabList=dataset.vocabList,
    Ktop=10)
```

Train with K=3 clusters

Take the best of 10 initializations

```
trained_model, info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Mult', 'VB',
    output_path='/tmp/we8there/helloworld-model=dp_mix+mult-K=3/',
    nLap=1000, convergeThr=0.0001, nTask=10,
    K=3, initname='bregmankmeans+lam1+iter1',
    gamma0=50.0, lam=0.1)

bnpy.viz.PrintTopics.plotCompsFromHModel(
    trained_model,
    vocabList=dataset.vocabList,
    Ktop=10)
```

Train with K=10 clusters

Take the best of 10 initializations

```
trained_model, info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Mult', 'VB',
    output_path='/tmp/we8there/helloworld-model=dp_mix+mult-K=10/',
    nLap=1000, convergeThr=0.0001, nTask=10,
    K=10, initname='bregmankmeans+lam1+iter1',
    gamma0=50.0, lam=0.1)

bnpy.viz.PrintTopics.plotCompsFromHModel(
    trained_model,
    vocabList=dataset.vocabList,
    Ktop=10)
```

Train with K=30 clusters

Take the best of 10 initializations

```
trained_model, info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'Mult', 'VB',
    output_path='/tmp/we8there/helloworld-model=dp_mix+mult-K=30/',
    nLap=1000, convergeThr=0.0001, nTask=10,
    K=30, initname='bregmankmeans+lam1+iter1',
    gamma0=50.0, lam=0.1)
bnpy.viz.PrintTopics.plotCompsFromHModel(
```

```
trained_model,
vocabList=dataset.vocabList,
Ktop=10)
```

Total running time of the script: (0 minutes 0.000 seconds)

Download Python source code: run-01-demo=mix_vb_single_run-model=mix+mult.py

Download Jupyter notebook: run-01-demo=mix_vb_single_run-model=mix+mult.ipynb

Generated by Sphinx-Gallery

Standard variational training for topic model

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (2, 2)
SMALL_FIG_SIZE = (1.5, 1.5)
```

Read text dataset from file

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'we8there', 'raw')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'),
    vocabfile=os.path.join(dataset_path, 'x_csc_colnames.txt'))

# Filter out documents with less than 20 words
doc_ids = np.flatnonzero(
    dataset.getDocTypeCountMatrix().sum(axis=1) >= 20)
dataset = dataset.make_subset(docMask=doc_ids, doTrackFullSize=False)
```

Train LDA topic model

Using 10 clusters and a random initialization procedure.

```
local_step_kwargs = dict(
    # perform at most this many iterations at each document
    nCoordAscentItersLP=100,
    # stop local iters early when max change in doc-topic counts < this thr
    convThrLP=0.001,
    )

trained_model, info_dict = bnpy.run(
    dataset, 'FiniteTopicModel', 'Mult', 'VB',
    output_path='/tmp/we8there/helloworld-model=topic+mult-K=10/',
    nLap=10, convergeThr=0.01,</pre>
```

```
K=10, initname='randomlikewang',
alpha=0.5, lam=0.1,
**local_step_kwargs)
```

First, we can plot the loss function over time We'll skip the first few iterations, since performance is quite bad.

```
pylab.figure(figsize=FIG_SIZE)
pylab.plot(info_dict['lap_history'][1:], info_dict['loss_history'][1:], 'k.-')
pylab.xlabel('num. laps')
pylab.ylabel('loss')
pylab.tight_layout()
```

Setup: Helper function to plot bars at each stage of training

```
def show_top_words_over_time(
        task_output_path=None,
       vocabList=None,
        query_laps=[0, 1, 2, 5, None],
        ncols=10):
    1 1 1
   nrows = len(query_laps)
    fig_handle, ax_handles_RC = pylab.subplots(
        figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
        nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for row_id, lap_val in enumerate(query_laps):
        cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
        # Plot the current model
        cur_ax_list = ax_handles_RC[row_id].flatten().tolist()
        bnpy.viz.PrintTopics.plotCompsFromHModel(
            cur_model,
            vocabList=vocabList,
            fontsize=9,
            Ktop=7,
            ax_list=cur_ax_list)
        cur_ax_list[0].set_ylabel("lap: %d" % lap_val)
   pylab.subplots_adjust(
        wspace=0.04, hspace=0.1,
        left=0.01, right=0.99, top=0.99, bottom=0.1)
    pylab.tight_layout()
```

Show the topics over time

```
show_top_words_over_time(
   info_dict['task_output_path'], vocabList=dataset.vocabList)
```

Total running time of the script: (0 minutes 0.000 seconds)

```
Download Python source code: run-03-demo=topic_vb_single_run-model=hdp_topic+mult.pownload Jupyter notebook: run-03-demo=topic_vb_single_run-model=hdp_topic+mult.ip
Generated by Sphinx-Gallery
```

Birth and merge variational training for topic model

```
import bnpy
import numpy as np
import os

from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (2, 2)
SMALL_FIG_SIZE = (1.5, 1.5)
```

Read text dataset from file

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'we8there', 'raw')
dataset = bnpy.data.BagOfWordsData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'),
    vocabfile=os.path.join(dataset_path, 'x_csc_colnames.txt'))

# Filter out documents with less than 20 words
doc_ids = np.flatnonzero(
    dataset.getDocTypeCountMatrix().sum(axis=1) >= 20)
dataset = dataset.make_subset(docMask=doc_ids, doTrackFullSize=False)
```

Train LDA topic model

Using 10 clusters and a random initialization procedure.

```
local_step_kwargs = dict(
    # perform at most this many iterations at each document
   nCoordAscentItersLP=100,
   # stop local iters early when max change in doc-topic counts < this thr
    convThrLP=0.001,
merge_kwargs = dict(
   m_startLap=5,
birth_kwargs = dict(
   b_startLap=2,
   b_stopLap=20,
   b_Kfresh=5)
trained_model, info_dict = bnpy.run(
    dataset, 'HDPTopicModel', 'Mult', 'memoVB',
    output_path='/tmp/we8there/trymoves-model=hdp_topic+mult-K=5/',
   nLap=20, convergeThr=0.01, nBatch=1,
   K=5, initname='randomlikewang',
   gamma=50.0, alpha=0.5, lam=0.1,
   moves='birth, merge, shuffle',
    **dict(local_step_kwargs.items() +
        merge_kwargs.items() +
        birth_kwargs.items()))
```

Setup: Helper function to plot topics at each stage of training

```
def show_top_words_over_time(
       task_output_path=None,
       vocabList=None,
       query_laps=[0, 1, 2, 5, None],
       ncols=10):
    . . .
   1 1 1
   nrows = len(query_laps)
   fig_handle, ax_handles_RC = pylab.subplots(
       nrows=nrows, ncols=ncols, sharex=True, sharey=True)
   for row_id, lap_val in enumerate(query_laps):
       cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
       # Plot the current model
       cur_ax_list = ax_handles_RC[row_id].flatten().tolist()
       bnpy.viz.PrintTopics.plotCompsFromHModel(
           cur model,
           vocabList=vocabList,
           fontsize=9,
           Ktop=7,
           ax_list=cur_ax_list)
       cur_ax_list[0].set_ylabel("lap: %d" % lap_val)
   pylab.subplots_adjust(
       wspace=0.04, hspace=0.1,
       left=0.01, right=0.99, top=0.99, bottom=0.1)
   pylab.tight_layout()
```

Show the topics over time

```
show_top_words_over_time(
  info_dict['task_output_path'], vocabList=dataset.vocabList)
```

Total running time of the script: (0 minutes 0.000 seconds)

```
Download Python source code: run-04-demo=topic_vb+proposals-model=hdp_topic+mult.pDownload Jupyter notebook: run-04-demo=topic_vb+proposals-model=hdp_topic+mult.ipy
Generated by Sphinx-Gallery
```

5.2.7 Small wikipedia bag-of-words text dataset

Text from a few thousand wikipedia articles. Variational training of mixture models and topic models with Multinomial likelihoods.

Birth and merge variational training for topic model

```
import bnpy
import numpy as np
import os
```

```
from matplotlib import pylab
import seaborn as sns

FIG_SIZE = (2, 2)
SMALL_FIG_SIZE = (1.5, 1.5)
```

Read text dataset from file

```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'wiki')
dataset = bnpy.data.BagOfWordsData.LoadFromFile_ldac(
    os.path.join(dataset_path, 'train.ldac'),
    vocabfile=os.path.join(dataset_path, 'vocab.txt'))

# Filter out the first 1000 documents with less than 50 words
doc_ids = np.flatnonzero(np.logical_and(
    dataset.getDocTypeCountMatrix().sum(axis=1) >= 50,
    dataset.getDocTypeCountMatrix().sum(axis=1) < 500))[:1000]
dataset = dataset.make_subset(docMask=doc_ids, doTrackFullSize=False)</pre>
```

Train LDA topic model

Using 10 clusters and a random initialization procedure.

```
local_step_kwargs = dict(
    # perform at most this many iterations at each document
    nCoordAscentItersLP=100,
    # stop local iters early when max change in doc-topic counts < this thr
    convThrLP=0.01,
merge kwargs = dict(
   m_startLap=5,
birth_kwargs = dict(
   b_startLap=4,
   b_stopLap=10,
   b_Kfresh=5)
trained_model, info_dict = bnpy.run(
    dataset, 'HDPTopicModel', 'Mult', 'memoVB',
    output_path='/tmp/wiki/trymoves-model=hdp_topic+mult-K=5/',
    nLap=20, convergeThr=0.01, nBatch=5,
    K=5, initname='randomlikewang',
    gamma=50.0, alpha=0.5, lam=0.1,
    moves='birth, merge, shuffle',
    **dict(local_step_kwargs.items() +
        merge_kwargs.items() +
        birth kwarqs.items()))
```

Setup: Helper function to plot topics at each stage of training

```
def show_top_words_over_time(
       task_output_path=None,
        vocabList=None,
        query_laps=[0, 1, 2, 5, None],
       ncols=10):
    . . .
   nrows = len(query_laps)
    fig_handle, ax_handles_RC = pylab.subplots(
        figsize=(SMALL_FIG_SIZE[0] * ncols, SMALL_FIG_SIZE[1] * nrows),
        nrows=nrows, ncols=ncols, sharex=True, sharey=True)
    for row_id, lap_val in enumerate(query_laps):
        cur_model, lap_val = bnpy.load_model_at_lap(task_output_path, lap_val)
        # Plot the current model
        cur_ax_list = ax_handles_RC[row_id].flatten().tolist()
        bnpy.viz.PrintTopics.plotCompsFromHModel(
            cur model,
            vocabList=vocabList,
            fontsize=9,
            Ktop=7,
            ax_list=cur_ax_list)
        cur_ax_list[0].set_ylabel("lap: %d" % lap_val)
   pylab.subplots_adjust(
        wspace=0.04, hspace=0.1,
        left=0.01, right=0.99, top=0.99, bottom=0.1)
    pylab.tight_layout()
```

Show the topics over time

```
show_top_words_over_time(
   info_dict['task_output_path'], vocabList=dataset.vocabList)
```

Total running time of the script: (0 minutes 0.000 seconds)

```
Download Python source code: run-01-demo=topic_vb+proposals-model=hdp_topic+mult.pdownload Jupyter notebook: run-01-demo=topic_vb+proposals-model=hdp_topic+mult.ipg

Generated by Sphinx-Gallery
```

5.2.8 Small dataset of 6 motion-capture sequences

Variational training of mixture models and HMM models with various Gaussian observation models.

Comparing models for sequential data

How to train mixtures and HMMs with various observation models on the same dataset.

```
import bnpy
import numpy as np
import os
```

```
from matplotlib import pylab
import seaborn as sns

SMALL_FIG_SIZE = (2.5, 2.5)
FIG_SIZE = (5, 5)
pylab.rcParams['figure.figsize'] = FIG_SIZE
```

Load dataset from file

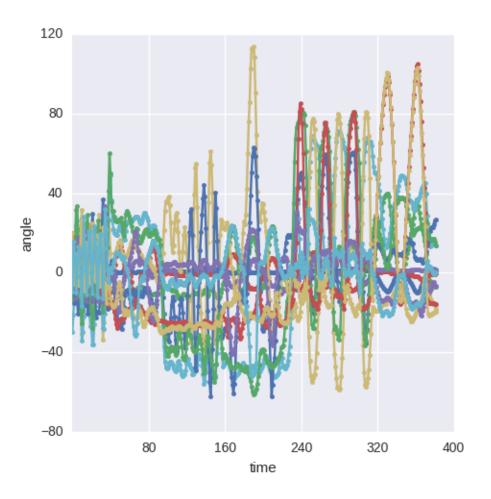
```
dataset_path = os.path.join(bnpy.DATASET_PATH, 'mocap6')
dataset = bnpy.data.GroupXData.read_npz(
    os.path.join(dataset_path, 'dataset.npz'))
```

Setup: Function to make a simple plot of the raw data

```
def show_single_sequence(seq_id):
    start = dataset.doc_range[seq_id]
    stop = dataset.doc_range[seq_id + 1]
    for dim in xrange(12):
        X_seq = dataset.X[start:stop]
        pylab.plot(X_seq[:, dim], '.-')
    pylab.xlabel('time')
    pylab.ylabel('angle')
    pylab.tight_layout()
```

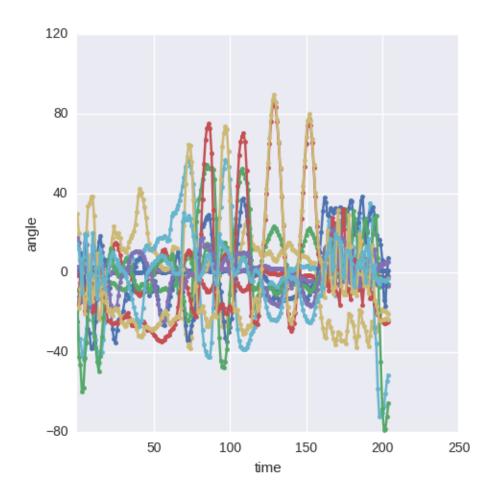
Visualization of the first sequence

```
show_single_sequence(0)
```



Visualization of the second sequence

show_single_sequence(1)



Setup: hyperparameters

```
alpha = 0.5
gamma = 5.0
sF = 1.0
K = 20
```

DP mixture with *DiagGauss* observation model

```
mixdiag_trained_model, mixdiag_info_dict = bnpy.run(
    dataset, 'DPMixtureModel', 'DiagGauss', 'memoVB',
    output_path='/tmp/mocap6/showcase-K=20-model=DP+DiagGauss-ECovMat=1*eye/',
    nLap=50, nTask=1, nBatch=1, convergeThr=0.0001,
    alpha=alpha, gamma=gamma, sF=sF, ECovMat='eye',
    K=K, initname='randexamples',
    )
```

Out:

```
WARNING: Found unrecognized keyword args. These are ignored.
Dataset Summary:
GroupXData
 total size: 6 units
 batch size: 6 units
  num. batches: 1
Allocation Model: DP mixture with K=0. Concentration gamma0= 5.00
Obs. Data Model: Gaussian with diagonal covariance.
Obs. Data Prior: independent Gauss-Wishart prior on each dimension
  Wishart params
    nu = 14 \dots
 beta = [ 12 12]
  Expectations
  E[mean[k]] =
  [ 0 0] ...
  E[covar[k]] =
  [[ 1. 0.]
   [ 0. 1.]] ...
Initialization:
  initname = randexamples
  K = 20 (number of clusters)
  seed = 1607680
  elapsed_time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/mocap6/showcase-K=20-model=DP+DiagGauss-ECovMat=1*eye/1
    1.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.845424399e+00
    2.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.756537185e+00 | Ndiff
    3.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.723105766e+00 | Ndiff
                                                    20 | loss 3.703275957e+00 | Ndiff
    4.000/50 after
                       0 sec. |
                                    178.8 MiB | K
    5.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.689932307e+00 | Ndiff
                                                    20 | loss 3.681432839e+00 | Ndiff
    6.000/50 after
                       0 sec. |
                                    178.8 MiB | K
    7.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.676243541e+00 | Ndiff
                                                    20 | loss 3.672159855e+00 | Ndiff
    8.000/50 after
                       0 sec. |
                                    178.8 MiB | K
    9.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.669045283e+00 | Ndiff
   10.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.665208654e+00 | Ndiff
   11.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.661952478e+00 | Ndiff
   12.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.658115620e+00 | Ndiff
   13.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.655058982e+00 | Ndiff
   14.000/50 after
                                    178.8 MiB | K
                                                    20 | loss 3.653853641e+00 | Ndiff
                       0 sec. |
                                                    20 | loss 3.652570589e+00 | Ndiff
  15.000/50 after
                       0 sec. |
                                    178.8 MiB | K
   16.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.651988134e+00 | Ndiff
   17.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.651566377e+00 | Ndiff
   18.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.651133556e+00 | Ndiff
   19.000/50 after
                                                    20 | loss 3.650800669e+00 | Ndiff
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.650523019e+00 | Ndiff
   20.000/50 after
                       0 sec. |
                                    178.8 MiB | K
   21.000/50 after
                                    178.8 MiB | K
                                                    20 | loss 3.650284547e+00 | Ndiff
                       0 sec. |
   22.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.650075236e+00 | Ndiff
                                                    20 | loss 3.649874747e+00 | Ndiff
   23.000/50 after
                       0 sec. |
                                    178.8 MiB | K
   24.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.649684370e+00 | Ndiff
   25.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.649503048e+00 | Ndiff
   26.000/50 after
                                    178.8 MiB | K
                                                    20 | loss 3.649287038e+00 | Ndiff
                       0 sec. |
   27.000/50 after
                       0 sec. |
                                    178.8 MiB | K
                                                    20 | loss 3.648992642e+00 | Ndiff
```

2

2

1

2

2

21

1

1.

1

1

1:

```
20 | loss 3.648274600e+00 | Ndiff
  28.000/50 after
                      1 sec. |
                                  178.8 MiB | K
  29.000/50 after
                     1 sec. |
                                  178.8 MiB | K
                                                 20 | loss 3.647520307e+00 | Ndiff
                                                 20 | loss 3.647350990e+00 | Ndiff
  30.000/50 after
                      1 sec. |
                                  178.8 MiB | K
  31.000/50 after
                      1 sec. |
                                  178.8 MiB | K
                                                 20 | loss 3.647242457e+00 | Ndiff
  32.000/50 after
                     1 sec. |
                                  178.8 MiB | K
                                                20 | loss 3.647171899e+00 | Ndiff
  33.000/50 after
                     1 sec. |
                                  178.8 MiB | K
                                                 20 | loss 3.647125709e+00 | Ndiff
  34.000/50 after
                      1 sec. |
                                  178.8 MiB | K
                                                 20 | loss 3.647094615e+00 | Ndiff
  35.000/50 after
                                                 20 | loss 3.647072676e+00 | Ndiff
                     1 sec. |
                                  178.8 MiB | K
  36.000/50 after
                     1 sec. |
                                  178.8 MiB | K
                                                20 | loss 3.647056795e+00 | Ndiff
  37.000/50 after
                                                 20 | loss 3.647045269e+00 | Ndiff
                     1 sec. |
                                  178.8 MiB | K
  38.000/50 after
                      1 sec. |
                                  178.8 MiB | K
                                                 20 | loss 3.647036962e+00 | Ndiff
  39.000/50 after
                     1 sec. |
                                                 20 | loss 3.647031023e+00 | Ndiff
                                  178.8 MiB | K
  40.000/50 after
                                                20 | loss 3.647026801e+00 | Ndiff
                     1 sec. |
                                  178.8 MiB | K
                                                 20 | loss 3.647023808e+00 | Ndiff
  41.000/50 after
                                  178.8 MiB | K
                     1 sec. |
  42.000/50 after
                                  178.8 MiB | K
                                                 20 | loss 3.647021689e+00 | Ndiff
                      1 sec. |
  43.000/50 after
                     1 sec. |
                                  178.8 MiB | K
                                                20 | loss 3.647020187e+00 | Ndiff
                                                20 | loss 3.647019120e+00 | Ndiff
  44.000/50 after
                     1 sec. |
                                  178.8 MiB | K
                                                 20 | loss 3.647018361e+00 | Ndiff
                     1 \text{ sec.}
  45.000/50 after
                                  178.8 MiB | K
                                                 20 | loss 3.647017819e+00 | Ndiff
  46.000/50 after
                     1 sec. |
                                  178.8 MiB | K
                                                20 | loss 3.647017432e+00 | Ndiff
  47.000/50 after
                     1 sec. |
                                  178.8 MiB | K
  48.000/50 after
                     1 sec. |
                                  178.8 MiB | K 20 | loss 3.647017154e+00 | Ndiff
                                                20 | loss 3.647016955e+00 | Ndiff
  49.000/50 after
                      1 sec. |
                                  178.8 MiB | K
  50.000/50 after
                                  178.8 MiB | K 20 | loss 3.647016811e+00 | Ndiff
                     1 sec. |
... done. not converged. max laps thru data exceeded.
```

HDP-HMM with *DiagGauss* observation model

Assume diagonal covariances.

Start with too many clusters (K=20)

```
hmmdiag_trained_model, hmmdiag_info_dict = bnpy.run(
     dataset, 'HDPHMM', 'DiagGauss', 'memoVB',
     output_path='/tmp/mocap6/showcase-K=20-model=HDPHMM+DiagGauss-ECovMat=1*eye/',
     nLap=50, nTask=1, nBatch=1, convergeThr=0.0001,
     alpha=alpha, gamma=gamma, sF=sF, ECovMat='eye',
     K=K, initname='randexamples',
    )
```

Out:

```
WARNING: Found unrecognized keyword args. These are ignored.

--alpha
Dataset Summary:
GroupXData
total size: 6 units
batch size: 6 units
num. batches: 1
Allocation Model: None
Obs. Data Model: Gaussian with diagonal covariance.
Obs. Data Prior: independent Gauss-Wishart prior on each dimension
Wishart params
```

```
nu = 14
  beta = [12 12]
  Expectations
  E[mean[k]] =
  [ 0 0] ...
  E[ covar[k]] =
  [[ 1. 0.]
   [ 0. 1.]] ...
Initialization:
  initname = randexamples
  K = 20 (number of clusters)
  seed = 1607680
  elapsed time: 0.0 sec
Learn Alg: memoVB | task
                         1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/mocap6/showcase-K=20-model=HDPHMM+DiagGauss-ECovMat=1*eye/1
    1.000/50 after
                        0 sec. |
                                     180.1 MiB | K
                                                     20 | loss 3.717124121e+00
    2.000/50 after
                        0 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.612329446e+00
    3.000/50 after
                                                     20 | loss
                        1 sec. |
                                     179.0 MiB | K
                                                                 3.580489903e+00
                                                                                 | Ndiff
    4.000/50 after
                        1 sec.
                                     179.0 MiB | K
                                                     20 | loss
                                                                 3.565890757e+00
                                                                                 | Ndiff
    5.000/50 after
                                                     20 | loss
                        1 sec. |
                                     179.0 MiB | K
                                                                3.552817867e+00 | Ndiff
    6.000/50 after
                        1 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.547626693e+00
    7.000/50 after
                        1 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.545715575e+00
                                                                                 | Ndiff
    8.000/50 after
                        2 sec.
                                     179.0 MiB | K
                                                     20
                                                        | loss
                                                                3.542710111e+00
                                                                                 | Ndiff
                                                                3.534107178e+00 | Ndiff
                                                     20 | loss
    9.000/50 after
                        2 sec. |
                                     179.0 MiB | K
   10.000/50 after
                        2 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.530991441e+00
                                                                                 | Ndiff
                        2 sec. |
                                                     20 | loss
   11.000/50 after
                                     179.0 MiB | K
                                                                3.527520848e+00
                                                                                 | Ndiff
   12.000/50 after
                        2 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                 3.525056000e+00 | Ndiff
   13.000/50 after
                        3 sec. |
                                     179.0 MiB | K
                                                     20 | loss 3.523781079e+00 | Ndiff
   14.000/50 after
                        3 sec. I
                                     179.0 MiB | K
                                                     20 | loss 3.521694790e+00 | Ndiff
                                                     20 | loss
   15.000/50 after
                        3 sec.
                                     179.0 MiB | K
                                                                3.518502897e+00
                                                                                 | Ndiff
   16.000/50 after
                        3 sec. I
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517515182e+00
                                                                                 | Ndiff
                        3 sec. |
                                                     20 | loss 3.517412339e+00 | Ndiff
   17.000/50 after
                                     179.0 MiB | K
   18.000/50 after
                        3 sec. |
                                     179.0 MiB | K
                                                     20 | loss 3.517396038e+00
                                                                                 | Ndiff
                                                     20 | loss
   19.000/50 after
                        4 sec. |
                                     179.0 MiB | K
                                                                 3.517386711e+00
                                                                                 | Ndiff
   20.000/50 after
                        4 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517380000e+00 | Ndiff
   21.000/50 after
                        4 sec. |
                                     179.0 MiB | K
                                                     20 | loss 3.517375098e+00 | Ndiff
   22.000/50 after
                        4 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517371095e+00
                                                                                 | Ndiff
                                                                                 | Ndiff
   23.000/50 after
                        4 sec.
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517367640e+00
   24.000/50 after
                        5 sec. |
                                     179.0 MiB | K
                                                     20 | loss 3.517364400e+00
                                                                                 | Ndiff
   25.000/50 after
                        5 sec. |
                                     179.0 MiB | K
                                                     20 | loss 3.517361220e+00
                                                                                 | Ndiff
   26.000/50 after
                        5 sec. |
                                                     20 | loss
                                                                3.517357862e+00
                                                                                 | Ndiff
                                     179.0 MiB | K
   27.000/50 after
                        5 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517353576e+00
                                                                                 | Ndiff
                        5 sec. |
   28.000/50 after
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517347351e+00 | Ndiff
   29.000/50 after
                        5 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517338850e+00 | Ndiff
   30.000/50 after
                                                     20 | loss
                        6 sec.
                                     179.0 MiB | K
                                                                3.517329011e+00 | Ndiff
                                                     20 | loss
   31.000/50 after
                        6 sec. |
                                     179.0 MiB | K
                                                                3.517319213e+00
                                                                                 | Ndiff
   32.000/50 after
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517310197e+00 | Ndiff
                        6 sec. |
   33.000/50 after
                        6 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517301719e+00
                                                                                 | Ndiff
   34.000/50 after
                        6 sec.
                               179.0 MiB | K
                                                     20 | loss
                                                                3.517293335e+00
                                                                                 | Ndiff
   35.000/50 after
                        6 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517285024e+00
                                                                                 | Ndiff
   36.000/50 after
                        7 sec. |
                                     179.0 MiB | K
                                                     20 | loss 3.517277155e+00
                                                                                 | Ndiff
   37.000/50 after
                        7 sec. |
                                     179.0 MiB | K
                                                     20 | loss 3.517270251e+00 | Ndiff
   38.000/50 after
                        7 sec. |
                                     179.0 MiB | K
                                                     20 | loss
                                                                3.517264770e+00
                                                                                 | Ndiff
```

1

```
179.0 MiB | K 20 | loss 3.517260855e+00 | Ndiff
  39.000/50 after
                     7 sec. |
  40.000/50 after
                     7 sec. |
                                 179.0 MiB | K 20 | loss 3.517258241e+00 | Ndiff
                                 179.0 MiB | K 20 | loss 3.517256507e+00 | Ndiff
  41.000/50 after
                     7 sec. |
  42.000/50 after
                     7 sec. |
                                 179.0 MiB | K 20 | loss 3.517255300e+00 | Ndiff
  43.000/50 after
                    8 sec. |
                                 179.0 MiB | K 20 | loss 3.517254394e+00 | Ndiff
  44.000/50 after
                     8 sec. |
                                 179.0 MiB | K 20 | loss 3.517253647e+00 | Ndiff
  45.000/50 after
                     8 sec. |
                                 179.0 MiB | K
                                              20 | loss 3.517252964e+00 | Ndiff
  46.000/50 after
                                              20 | loss 3.517252267e+00 | Ndiff
                     8 sec. |
                                 179.0 MiB | K
  47.000/50 after
                     8 sec. |
                                179.0 MiB | K
                                              20 | loss 3.517251461e+00 | Ndiff
  48.000/50 after
                     8 sec. |
                                              20 | loss 3.517250379e+00 | Ndiff
                                179.0 MiB | K
  49.000/50 after
                     9 sec. |
                                179.0 MiB | K
                                              20 | loss 3.517248618e+00 | Ndiff
  50.000/50 after 9 sec. |
                                179.0 MiB | K 20 | loss 3.517244801e+00 | Ndiff
... done. not converged. max laps thru data exceeded.
```

HDP-HMM with *Gauss* observation model

Assume full covariances.

Start with too many clusters (K=20)

```
hmmfull_trained_model, hmmfull_info_dict = bnpy.run(
     dataset, 'HDPHMM', 'Gauss', 'memoVB',
     output_path='/tmp/mocap6/showcase-K=20-model=HDPHMM+Gauss-ECovMat=1*eye/',
     nLap=50, nTask=1, nBatch=1, convergeThr=0.0001,
     alpha=alpha, gamma=gamma, sF=sF, ECovMat='eye',
     K=K, initname='randexamples',
    )
```

Out:

```
WARNING: Found unrecognized keyword args. These are ignored.
 --alpha
Dataset Summary:
GroupXData
 total size: 6 units
 batch size: 6 units
 num. batches: 1
Allocation Model: None
Obs. Data Model: Gaussian with full covariance.
Obs. Data Prior: Gauss-Wishart on mean and covar of each cluster
 E[mean[k]] =
  [ 0. 0.] ...
 E[covar[k]] =
 [[ 1. 0.]
  [ 0. 1.]] ...
Initialization:
 initname = randexamples
 K = 20 (number of clusters)
 seed = 1607680
 elapsed_time: 0.0 sec
Learn Alq: memoVB | task 1/1 | alq. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/mocap6/showcase-K=20-model=HDPHMM+Gauss-ECovMat=1*eye/1
```

3: 2: 1: 2:

| 1.000/50 after | 1 000/50 6 | 0 | 170 0 11'D | | 0.0 | | 2 452700240 .00 | 1. |
|--|-----------------|----------------|---------------|-------|-----|------|-----------------|-------|
| 3.000/50 after | 1.000/50 after | 0 sec. | 179.0 MiB | K | 20 | loss | 3.453792348e+00 | Mate |
| 4.000/50 after | | | | | | | | |
| 5.000/50 after | | | | | | | | |
| 6.000/50 after | | | | | | | | |
| 7.000/50 after | | | | | | | | |
| 8.000/50 after 2 sec. 179.0 MiB K 20 loss 3.198209231e+00 Ndiff 10.000/50 after 2 sec. 179.0 MiB K 20 loss 3.1960056e+00 Ndiff 11.000/50 after 2 sec. 179.0 MiB K 20 loss 3.194049899e+00 Ndiff 12.000/50 after 3 sec. 179.0 MiB K 20 loss 3.19238495e+00 Ndiff 12.000/50 after 3 sec. 179.0 MiB K 20 loss 3.19338614e+00 Ndiff 14.000/50 after 3 sec. 179.0 MiB K 20 loss 3.188801039e+00 Ndiff 14.000/50 after 3 sec. 179.0 MiB K 20 loss 3.1878025e+00 Ndiff 15.000/50 after 3 sec. 179.0 MiB K 20 loss 3.1878025e+00 Ndiff 16.000/50 after 3 sec. 179.0 MiB K 20 loss 3.18767197e+00 Ndiff 16.000/50 after 4 sec. 179.0 MiB K 20 loss 3.18760195e+00 Ndiff 17.000/50 after 4 sec. 179.0 MiB K 20 loss 3.18610458e+00 Ndiff 18.000/50 after 4 sec. 179.0 MiB K 20 loss 3.186639962e+00 Ndiff 18.000/50 after 4 sec. 179.0 MiB K 20 loss 3.186639962e+00 Ndiff 12.000/50 after 4 sec. 179.0 MiB K 20 loss 3.18657978e+00 Ndiff 12.000/50 after 5 sec. 179.0 MiB K 20 loss 3.18597378e+00 Ndiff 22.000/50 after 5 sec. 179.0 MiB K 20 loss 3.185973787e+00 Ndiff 22.000/50 after 5 sec. 179.0 MiB K 20 loss 3.185973787e+00 Ndiff 22.000/50 after 5 sec. 179.0 MiB K 20 loss 3.18263233e+00 Ndiff 24.000/50 after 5 sec. 179.0 MiB K 20 loss 3.18264094e+00 Ndiff 24.000/50 after 5 sec. 179.0 MiB K 20 loss 3.18264094e+00 Ndiff 26.000/50 after 6 sec. 179.0 MiB K 20 loss 3.181947079e+00 Ndiff 26.000/50 after 6 sec. 179.0 MiB K 20 loss 3.18199580e+00 Ndiff 27.000/50 after 6 sec. 179.0 MiB K 20 loss 3.181938950e+00 Ndiff 27.000/50 after 6 sec. 179.0 MiB K 20 loss 3.18193709e+00 Ndiff 27.000/50 after 6 sec. 179.0 MiB K 20 loss 3.1819338e+00 Ndiff 27.000/50 after 7 sec. 179.0 MiB K 20 loss 3.18183395e+00 Ndiff 27.000/50 after 7 sec. 179.0 MiB K 20 loss 3.18183395e+00 Ndiff 27.000/50 after 8 sec. 179.0 MiB K 20 loss 3.1818338e+00 Ndiff 27.000/50 after 9 sec. 17 | | | | | | | | |
| 9.000/50 after 2 sec. 179.0 MiB K 20 loss 3.196602056e400 Ndiff 10.000/50 after 2 sec. 179.0 MiB K 20 loss 3.194049899e100 Ndiff 11.000/50 after 3 sec. 179.0 MiB K 20 loss 3.192384953e+00 Ndiff 12.000/50 after 3 sec. 179.0 MiB K 20 loss 3.193786164e+00 Ndiff 13.000/50 after 3 sec. 179.0 MiB K 20 loss 3.18881039e+00 Ndiff 14.000/50 after 3 sec. 179.0 MiB K 20 loss 3.18881039e+00 Ndiff 15.000/50 after 3 sec. 179.0 MiB K 20 loss 3.187267197e+00 Ndiff 15.000/50 after 4 sec. 179.0 MiB K 20 loss 3.187104503e+00 Ndiff 17.000/50 after 4 sec. 179.0 MiB K 20 loss 3.186039962e+00 Ndiff 18.000/50 after 4 sec. 179.0 MiB K 20 loss 3.18603962e+00 Ndiff 19.000/50 after 4 sec. 179.0 MiB K 20 loss 3.18603962e+00 Ndiff 19.000/50 after 4 sec. 179.0 MiB K 20 loss 3.186039786e+00 Ndiff 20.000/50 after 4 sec. 179.0 MiB K 20 loss 3.185973787e+00 Ndiff 22.000/50 after 5 sec. 179.0 MiB K 20 loss 3.185973787e+00 Ndiff 22.000/50 after 5 sec. 179.0 MiB K 20 loss 3.185973787e+00 Ndiff 22.000/50 after 5 sec. 179.0 MiB K 20 loss 3.18230313e+00 Ndiff 24.000/50 after 5 sec. 179.0 MiB K 20 loss 3.18230313e+00 Ndiff 24.000/50 after 5 sec. 179.0 MiB K 20 loss 3.18230313e+00 Ndiff 24.000/50 after 5 sec. 179.0 MiB K 20 loss 3.182300590e+00 Ndiff 25.000/50 after 6 sec. 179.0 MiB K 20 loss 3.181200505e+00 Ndiff 26.000/50 after 6 sec. 179.0 MiB K 20 loss 3.181200505e+00 Ndiff 27.000/50 after 6 sec. 179.0 MiB K 20 loss 3.1813338e+00 Ndiff 31.000/50 after 7 sec. 179.0 MiB K 20 loss 3.1813338e+00 Ndiff 33.000/50 after 6 sec. 179.0 MiB K 20 loss 3.1813338e+00 Ndiff 33.000/50 after 7 sec. 179.0 MiB K 20 loss 3.181813395e+00 Ndiff 34.000/50 after 7 sec. 179.0 MiB K 20 loss 3.18181338e+00 Ndiff 34.000/50 after 8 sec. 179.0 MiB K 20 loss 3.18181338e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.18181338e+00 Ndiff 44.000/50 after 9 s | | | | | | | | |
| 10.000/50 after | | | | | | | | |
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| 35.000/50 after 7 sec. 179.0 MiB K 20 loss 3.181813438e+00 Ndiff 36.000/50 after 7 sec. 179.0 MiB K 20 loss 3.181813408e+00 Ndiff 37.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813395e+00 Ndiff 38.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813388e+00 Ndiff 39.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813388e+00 Ndiff 40.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813383e+00 Ndiff 41.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 42.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 43.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | 7 sec. | | | | loss | | |
| 36.000/50 after 7 sec. 179.0 MiB K 20 loss 3.181813408e+00 Ndiff 37.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813395e+00 Ndiff 38.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813388e+00 Ndiff 39.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813385e+00 Ndiff 40.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813383e+00 Ndiff 41.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 42.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 43.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | 7 sec. | | K | | loss | | |
| 37.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813395e+00 Ndiff 38.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813388e+00 Ndiff 40.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813383e+00 Ndiff 41.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813383e+00 Ndiff 42.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 43.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | 7 sec. | | | | | | |
| 38.000/50 after | | 7 sec. | | | | | | |
| 39.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813385e+00 Ndiff 40.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813383e+00 Ndiff 41.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 42.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 43.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | • | | K | | | | |
| 40.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813383e+00 Ndiff 41.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 42.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 43.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | · | | | | | | |
| 41.000/50 after 8 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 42.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 43.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | | | | | |
| 42.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813382e+00 Ndiff 43.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | | | | | |
| 43.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | | | | | |
| 44.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | K | 20 | | | |
| 45.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | K | 20 | | | |
| 46.000/50 after 9 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | | | | | |
| 47.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | 179.0 MiB | K | 20 | loss | | Ndiff |
| 48.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | K | 20 | | | |
| 49.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | K | 20 | | | |
| 50.000/50 after 10 sec. 179.0 MiB K 20 loss 3.181813381e+00 Ndiff | | | | | 20 | | | |
| | | | 179.0 MiB | K | 20 | | | Ndiff |
| done. not converged. max laps thru data exceeded. | | | | | | loss | 3.181813381e+00 | Ndiff |
| | done. not conve | rged. max laps | thru data exc | ceede | ed. | | | |

HDP-HMM with *AutoRegGauss* observation model

Assume full covariances.

Start with too many clusters (K=20)

```
hmmar_trained_model, hmmar_info_dict = bnpy.run(
    dataset, 'HDPHMM', 'AutoRegGauss', 'memoVB',
    output_path='/tmp/mocap6/showcase-K=20-model=HDPHMM+AutoRegGauss-ECovMat=1*eye/',
    nLap=50, nTask=1, nBatch=1, convergeThr=0.0001,
    alpha=alpha, gamma=gamma, sF=sF, ECovMat='eye',
    K=K, initname='randexamples',
    )
```

Out:

```
WARNING: Found unrecognized keyword args. These are ignored.
Dataset Summary:
GroupXData
 total size: 6 units
 batch size: 6 units
 num. batches: 1
Allocation Model: None
Obs. Data Model: Auto-Regressive Gaussian with full covariance.
Obs. Data Prior: MatrixNormal-Wishart on each mean/prec matrix pair: A, Lam
 E[ A ] =
 [[ 1. 0.]
  [ 0. 1.]] ...
 E[Sigma] =
  [[ 1. 0.]
  [ 0. 1.]] ...
Initialization:
 initname = randexamples
 K = 20 (number of clusters)
 seed = 1607680
 elapsed time: 0.0 sec
Learn Alg: memoVB | task 1/1 | alg. seed: 1607680 | data order seed: 8541952
task_output_path: /tmp/mocap6/showcase-K=20-model=HDPHMM+AutoRegGauss-ECovMat=1/*eye/1
   1.000/50 after 0 sec. | 179.0 MiB | K 20 | loss 2.908127656e+00 |
   2.000/50 after
                                  179.0 MiB | K 20 | loss 2.712797722e+00 | Ndiff
                     1 sec. |
   3.000/50 after
                     1 sec. |
                                  179.0 MiB | K
                                                20 | loss 2.623844667e+00 | Ndiff
                                                20 | loss 2.579060900e+00 | Ndiff
   4.000/50 after
                      1 sec. |
                                  179.0 MiB | K
                                                20 | loss 2.548616789e+00 | Ndiff
   5.000/50 after
                                  179.0 MiB | K
                     1 sec. |
   6.000/50 after
                     2 sec. |
                                  179.0 MiB | K
                                                20 | loss 2.518588127e+00 | Ndiff
                                                20 | loss 2.504804864e+00 | Ndiff
   7.000/50 after
                     2 sec. |
                                  179.0 MiB | K
   8.000/50 after
                      2 sec. |
                                  179.0 MiB | K 20 | loss 2.496420689e+00 | Ndiff
   9.000/50 after
                     2 sec. |
                                  179.0 MiB | K 20 | loss 2.492445130e+00 | Ndiff
  10.000/50 after
                      3 sec. |
                                  179.0 MiB | K
                                               20 | loss 2.490165194e+00 | Ndiff
                                                20 | loss 2.485730707e+00 | Ndiff
  11.000/50 after
                      3 sec. |
                                  179.0 MiB | K
                                                20 | loss 2.484287434e+00 | Ndiff
  12.000/50 after
                      3 sec. |
                                  179.0 MiB | K
  13.000/50 after
                     3 sec. |
                                  179.0 MiB | K 20 | loss 2.482746506e+00 | Ndiff
                    4 sec. |
                                  179.0 MiB | K 20 | loss 2.480880306e+00 | Ndiff
  14.000/50 after
                                 179.0 MiB | K 20 | loss 2.480467067e+00 | Ndiff
  15.000/50 after 4 sec. |
```

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```
16.000/50 after
                                                    20 | loss 2.479991235e+00
                                                                               | Ndiff
                       4 sec. |
                                   179.0 MiB | K
  17.000/50 after
                       5 sec. |
                                    179.0 MiB | K
                                                    20 | loss 2.479792583e+00
                                                                               | Ndiff
  18.000/50 after
                       5 sec. |
                                    179.0 MiB | K
                                                    20 | loss 2.478520054e+00
                                                                               | Ndiff
                       5 sec. |
  19.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.477365552e+00 | Ndiff
  20.000/50 after
                       5 sec. I
                                    179.0 MiB | K
                                                    20 | loss 2.476525301e+00 | Ndiff
  21.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.476119048e+00 | Ndiff
                       6 sec. |
  22.000/50 after
                       6 sec.
                                    179.0 MiB | K
                                                    20 | loss 2.474839041e+00 | Ndiff
  23.000/50 after
                                                    20 | loss 2.473186959e+00 | Ndiff
                       6 sec. |
                                   179.0 MiB | K
  24.000/50 after
                       6 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.471452324e+00 | Ndiff
  25.000/50 after
                       7 sec. |
                                                    20 | loss 2.471162626e+00
                                   179.0 MiB | K
                                                                               | Ndiff
  26.000/50 after
                       7 sec. |
                                   179.0 MiB | K
                                                    20 | loss
                                                              2.470983405e+00 | Ndiff
  27.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.470774342e+00 | Ndiff
                       7 sec. |
  28.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.469880859e+00 | Ndiff
                       7 sec. |
  29.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.468970839e+00 | Ndiff
                       8 sec. |
  30.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.467972189e+00 | Ndiff
                       8 sec. |
  31.000/50 after
                       8 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.467661612e+00 | Ndiff
                                                    20 | loss 2.467483397e+00 | Ndiff
  32.000/50 after
                       9 sec. I
                                   179.0 MiB | K
                       9 sec. |
                                                    20 | loss 2.467450274e+00 | Ndiff
  33.000/50 after
                                   179.0 MiB | K
  34.000/50 after
                       9 sec. I
                                   179.0 MiB | K
                                                    20 | loss 2.467407757e+00 | Ndiff
  35.000/50 after
                       9 sec. |
                                                    20 | loss 2.467292085e+00 | Ndiff
                                   179.0 MiB | K
  36.000/50 after
                      10 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.467236037e+00 | Ndiff
  37.000/50 after
                      10 sec.
                                   179.0 MiB | K
                                                    20 | loss 2.467197165e+00 | Ndiff
                      10 sec. |
  38.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.467112796e+00 | Ndiff
  39.000/50 after
                      10 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.466989563e+00 | Ndiff
  40.000/50 after
                                                    20 | loss 2.466727224e+00 | Ndiff
                      11 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.466587267e+00 | Ndiff
  41.000/50 after
                      11 sec. |
                                   179.0 MiB | K
  42.000/50 after
                      11 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.466255511e+00 | Ndiff
  43.000/50 after
                      11 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.466170740e+00 | Ndiff
  44.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.466133408e+00 | Ndiff
                      12 sec. |
  45.000/50 after
                      12 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.466086219e+00 | Ndiff
  46.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.466016271e+00 | Ndiff
                      12 sec. |
  47.000/50 after
                      12 sec. |
                                   179.0 MiB | K
                                                    20 | loss 2.465964032e+00 | Ndiff
  48.000/50 after
                                                    20 | loss 2.465914037e+00 | Ndiff
                      13 sec. |
                                   179.0 MiB | K
  49.000/50 after
                                   179.0 MiB | K
                                                    20 | loss 2.465798065e+00 | Ndiff
                      13 sec. |
                      13 sec. |
  50.000/50 after
                                    179.0 MiB | K
                                                    20 | loss 2.465630615e+00 | Ndiff
... done. not converged. max laps thru data exceeded.
```

Compare loss function traces for all methods

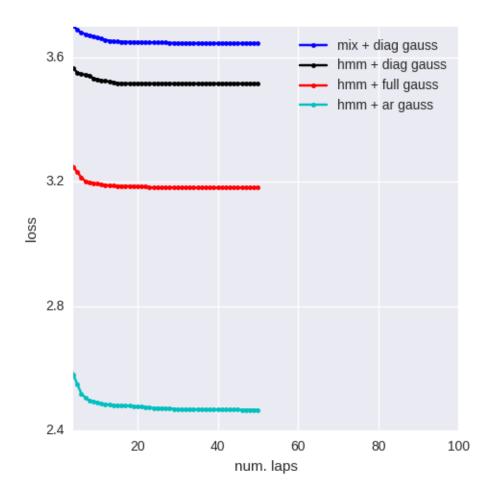
```
pylab.figure()

pylab.plot(
    mixdiag_info_dict['lap_history'],
    mixdiag_info_dict['loss_history'], 'b.-',
    label='mix + diag gauss')

pylab.plot(
    hmmdiag_info_dict['lap_history'],
    hmmdiag_info_dict['loss_history'], 'k.-',
    label='hmm + diag gauss')

pylab.plot(
    hmmfull_info_dict['lap_history'],
```

```
hmmfull_info_dict['loss_history'], 'r.-',
    label='hmm + full gauss')
pylab.plot(
    hmmar_info_dict['lap_history'],
    hmmar_info_dict['loss_history'], 'c.-',
    label='hmm + ar gauss')
pylab.legend(loc='upper right')
pylab.xlabel('num. laps')
pylab.ylabel('loss')
pylab.xlim([4, 100]) # avoid early iterations
pylab.ylim([2.4, 3.7]) # handpicked
pylab.draw()
pylab.tight_layout()
```



Total running time of the script: (0 minutes 33.511 seconds)

Download Python source code: plot-01-demo=many_models_same_data.py

Download Jupyter notebook: plot-01-demo=many_models_same_data.ipynb

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Download all examples in Python source code: examples_python.zip

Download all examples in Jupyter notebooks: examples_jupyter.zip Generated by Sphinx-Gallery

5.3 Allocation Model Guide

5.3.1 What is an allocation model?

Within **bnpy**, every hierarchical model we support has two pieces: an allocation model and an observation model. We use the label "allocation model" to describe the generative process that allocates cluster assignments to individual data points.

TODO ILLUSTRATION

In this document, we give a high-level overview of how we define an allocation model and how variational inference works. We also define the essential variational inference API functions that any concrete allocation model (an instance of the abstract AllocModel class) should support.

5.3.2 Quick Links

Here are some quick links to documentation for each of the possible allocation models supported by bnpy.

- Mixture models
- Topic models
- · Hidden Markov models

5.3.3 Generative model

An allocation model defines a probabilistic generative process for assigning (aka allocating) clusters to data atoms. There are two types of variables involved: cluster probability vectors \$pi_j\$, and discrete assignments \$z\$ n\$ at each data aton indexed by \$n\$. Each allocation model defines a joint distribution

$$\log p(\pi, z) = \log p(\pi) + \log p(z|\pi)$$

First, we generate a set of global cluster probabilities \$pi_0\$.

$$\pi_0 \sim \operatorname{Dir}_K(\frac{\alpha_0}{K})$$

Depending on the model, we may next generate several more cluster probability vectors \$pi_i\$.

Second, we draw cluster assignment variables \$z_n\$ at each data atom \$n\$.

$$z_n \sim \operatorname{Cat}(\pi_{j1}, \dots \pi_{jK})$$

Example: Mixture model

For example, consider a simple finite mixture model with \$K\$ clusters. The complete allocation model would be:

$$\pi_0 \sim \operatorname{Dir}_K(\alpha_0 \frac{1}{K})$$
 $z_n \sim \operatorname{Cat}(\pi_{01}, \dots \pi_{0K})$

To extend this to a Dirichlet process mixture model, we simply use a stick-breaking distribution instead:

$$\pi_0 \sim \operatorname{Stick}(\alpha_0)$$
 $z_n \sim \operatorname{Cat}(\pi_{01}, \dots \pi_{0K}, \dots)$

5.3.4 Variational Inference

Variational inference for allocation models tries to optimize an approximate posterior:

$$\log q(\pi, z) = \log q(\pi|\theta) + \log q(z|r)$$

The optimization objective is to make this approximate posterior as close to the true posterior as possible. Remember that this objective incorporates terms from the observation model as well. The optimization finds values for the free parameters – pseudo-counts theta and assignments r – that make the objective function as large as possible.

$$= \mathcal{L}_{alloc}(r, theta) + (r, ...)$$

Expanding the allocation model terms, we have

$$egin{aligned} \mathcal{L}_{ ext{alloc}}(r, theta) &= +\mathcal{L}_{ ext{entropy}} \ &= \mathbb{E}_q[\log p(z) + rac{\log p(\pi)}{\log q(\pi)}] \ \mathcal{L}_{ ext{entropy}} &= -\mathbb{E}_q[\log q(z)] \ \log p(z|lpha) &\geq \end{aligned}$$

Every variational algorithm proceeds by iteratively improving this objective function by cycling through four concrete steps:

- Local step: optimize the local assignments r and any local theta values.
- Summary step: compute summary statistics from the local parameters.
- Global step:
- Objective function evaluation step

5.3.5 Variational API

Within **bnpy**, each possible allocation model is a subclass of the general-purpose abstract base class: AllocModel. Each AllocModel instance has both state and behaviors. The *state* represents two key values: the hyperparameters that define the prior and the global variational parameters that define the approximate posterior. The *behaviors* are the four fundamental steps of inference, as well as some auxiliary functions.

Attributes

For any generative model in our framework, the hyperparameters of an allocation model are just the set of concentration parameters \$alpha_j\$ that parameterize the generative story for each \$pi_j\$ probability vector. Thus, each allocation model will hold one or more *alpha* values as attributes.

Each AllocModel subclass will have model-specific global parameters, which are represented as instance attributes. For example, a FiniteMixtureModel has a vector of Dirichlet pseudo-counts called *theta*, while a DPMixtureModel instance has a vector of Beta pseudo-counts called *eta*.

Each of the four conceptual steps of the variational inference – local step, summary step, global step, and objective step – is associated with a single instance-level function of an AllocModel object. The general abstract interface for using these functions is documented below. Each subclass will provide an actual implementation of these functions.

Local step

The local step, specified by calc_local_params, finds local parameters for the dataset.

class bnpy.allocmodel.AllocModel(inferType)

```
calc local params (Data, LP)
```

Compute local parameters for each data item and component.

This is the E-step of EM algorithm.

Returned LP contains optimal values of local parameters specific to the provided dataset. Updated values computed using current global parameter attributes.

Possible keyword arguments control model-specific computations.

Parameters

- Data (DataObj) Dataset to compute local parameters for.
- LP (dict) Must contain cond. likelihoods in field 'E_log_soft_ev', a 2D array that is N x K provided by the observation model.

Returns LP (*dict*) – Contains updated fields for all K clusters in current model. * 'resp': N x K 2D array, soft assignments for each data atom.

Summary step

The summary step, specified by get_global_suff_stats, summarizes a dataset Data and its associated local parameters LP. It produces a bag of sufficient statistics SS.

class bnpy.allocmodel.AllocModel(inferType)

```
get_global_suff_stats(Data, SS, LP, **kwargs)
```

Compute low-dim summaries for provided local params.

Returned sufficient statistics are deterministic given Data, LP.

Possible keyword arguments control model-specific computations.

Parameters

- Data (DataObj) Dataset to be summarized.
- **SS** (SuffStatBag) If present, all summaries will be added to this bag. If None, new bag will be created and returned.
- LP (dict) Holds valid local params for K' clusters and all atoms in Data.

Returns SS (SuffStatBag) – Updated fields for each of K' clusters represented in LP

Global step

The global step, performed by update_global_params,

class bnpy.allocmodel.AllocModel(inferType)

```
get_global_suff_stats (Data, SS, LP, **kwargs)
```

Compute low-dim summaries for provided local params.

Returned sufficient statistics are deterministic given Data, LP.

Possible keyword arguments control model-specific computations.

Parameters

- Data (DataObj) Dataset to be summarized.
- **SS** (SuffStatBag) If present, all summaries will be added to this bag. If None, new bag will be created and returned.
- LP (dict) Holds valid local params for K' clusters and all atoms in Data.

Returns SS (SuffStatBag) – Updated fields for each of K' clusters represented in LP

Objective evaluation step

During inference, we need to verify that each step is working as expected. Thus, we need to be able to compute the scalar value of the objective given any current set of global parameters (stored in self) and local parameters (summarized in SS).

class bnpy.allocmodel.AllocModel(inferType)

calc_evidence (Data, SS, LP, todict=0, **kwargs)

Calculate ELBO objective function value for provided state.

Parameters

- Data (optional,) If not provided, relies exclusively on summaries in SS
- **SS** (SuffStatBag) Contains valid summaries for desired dataset.
- LP (optional, dict) If not provided, relies exclusively on summaries in SS If provided, used in place of summaries in SS when possible.

Keyword Arguments todict (*boolean*) – If True, return a dict with different ELBO terms

under named keys like 'Ldata' and 'Lentropy'

If False [default], return scalar value equal to sum of terms.

Returns L (*float*) – Represents sum of all terms in optimization objective. Will be a dict if todict option is True.

Mixture Models

bnpy supports two kinds of mixture models: *FiniteMixtureModel* and *DPMixtureModel*.

FiniteMixtureModel The finite mixture has the following generative representation as an allocation model. There is a single top-level vector of cluster probabilities π_0 . Each data atom's assignment is drawn i.i.d. according to the probabilities in this vector.

$$[\pi_{01},\pi_{02},\dots\pi_{0K}] \sim \mathrm{Dir}_K(rac{lpha_0}{K})$$
 for $n\in 1,\dots N:$ $z_n \sim \mathrm{Cat}_K(\pi_{01},\pi_{0K})$

Here, $\alpha_0 > 0$ is the uniform concentration parameter. TODO interpret.

DPMixtureModel The Dirichlet Process (DP) mixture has the following generative representation as an allocation model. It modifies the finite mixture by using the StickBreaking process to K active weights and a remainder weight, all inside \$pi_0\$.

$$[\pi_{01},\pi_{02},\dots\pi_{0K},\pi_{0,>K}]\sim ext{StickBreaking}_K(\pi_0)$$
 for $n\in 1,\dots N:$ $z_n\sim ext{Cat}_K(\pi_{01},\pi_{0K})$

If we take the limit as K grows to infinity, these two generative models are equivalent.

Using mixtures with other bnpy modules As usual, to train a hierarchical model whose allocation is done by FiniteMixtureModel,

Supported DataObj Types Mixture models can apply to almost all data formats available in bnpy. Any data suitable for topic models or sequence models can also be fit with a basic mixture model.

The only formats that do not apply are those based on GraphData, which require the subclass of mixture models (TBD).

Supported Learning Algorithms Currently, the practical differences are:

- FiniteMixtureModel supports EM, VB, soVB, moVB
- *DPMixtureModel* supports VB, soVB, and moVB.
- - with birth/merge/delete moves for moVB

EM (MAP) inference for the DPMixtureModel is possible, but just not implemented yet.

Common tasks with mixtures

Accessing learned cluster assignments Given a dataset of interest Data (a DataObj), and an hmodel (an instance of HModel) properly initialized with K active clusters, we simply perform a local step.

```
>>> LP = hmodel.calc_local_params(Data)
>>> resp = LP['resp']
```

Here, resp is a 2D array of size N x K. Each entry resp[n, k] gives the probability that data atom n is assigned to cluster k under the posterior. Thus, each entry resp[n,k] must be a value within the interval [0,1]. The sum of every row must equal one.

```
>>> assert resp[n, k] >= 0.0
>>> assert resp[n, k] <= 1.0
>>> assert np.allclose(np.sum(resp[n,:]), 1.0)
```

To convert to hard assignments

```
>>> Z = resp.argmax(axis=1)
```

Here, Z is a 1D array of size N, where entry Z[n] is an integer in the set $\{0, 1, 2, ..., K-1, K\}$.

Accessing learned cluster probabilities

```
>>> pi0 = hmodel.allocModel.get_active_cluster_probs()
>>> assert pi0.ndim == 1
>>> assert pi0.size == hmodel.allocModel.K
```

Global update summaries For a global update, mixture models require only one sufficient statistic: an expected count value for each cluster k. This value gives the expected number of data atoms assigned to k throughout the dataset.

• Count N_k Expected assignments to state k across all data items.

```
>>> LP = hmodel.calc_local_params(Data)
>>> SS = hmodel.get_global_suff_stats(Data, LP)
>>> Nvec = SS.N # or SS.getCountVec()
>>> assert Nvec.size == hmodel.allocModel.K
[ ... TODO ... ]
```

ELBO summaries To compute the ELBO, mixture models require only one non-linear summary statistic: the entropy of the learned assignment parameters *resp*.

$$= +\mathcal{L}_{\text{alloc}} - E[\log q(z)]$$
$$-E[\log q(z)] = \sum_{k=1}^{K} H_k$$
$$H_k = -\sum_{n=1}^{N} r_{nk} \log r_{nk}$$

You can compute this by enabling the correct keyword flag when calling the summary step function.

```
>>> LP = hmodel.calc_local_params(Data)
>>> SS = hmodel.get_global_suff_stats(Data, LP, doPrecompEntropy=1)
>>> Hresp = SS.getELBOTerm('Hresp')
>>> assert Hresp.ndim == 1
>>> assert Hresp.size == SS.K
[ ... TODO ... ]
```

Topic Models

Supported Data Formats Topic models can be applied to any dataset that has group structure.

Supported Learning Algorithms

- FiniteTopicModel supports VB, soVB, moVB
- HDPTopicModel supports VB, soVB, and moVB. * with birth/merge/delete moves for moVB

Possible Implementations

- FiniteTopicModel: stuff here
- HDPTopicModel: more stuff here

There are two types of mixture model supported. Both define the model in terms of a global parameter vector β , where β_k gives the probability of topic k, and local assignments z, where z_n indicates which state $\{1, 2, 3, ... K\}$ is assigned to data item n.

The FiniteMixtureModel has a generative process:

$$[\beta_1, \beta_2, \dots \beta_K] \sim \text{Dir}(\gamma, \gamma, \dots \gamma)$$

 $z_n \sim \text{Discrete}(\beta)$

while the *DPMixtureModel* has generative process:

$$[\beta_1, \beta_2, \dots \beta_K \dots] \sim \text{StickBreaking}(\gamma_0)$$

 $z_n \sim \text{Discrete}(\beta)$

If we let K grow to infinity, these two models converge if $\gamma = \gamma_0/K$.

TOC

5.4 Observation Models

All observation models define a *likelihood* for producing data x_n from some cluster-specific density with parameter ϕ_k :

$$p(x|\phi, z) = \prod_{n=1}^{N} p(x_n|\phi_k)^{\delta_k(z_n)}$$

Supported Bayesian methods require specifying a (conjugate) prior:

$$p(\phi) = \prod_{k=1}^{K} p(\phi_k)$$

5.4.1 Variational methods for observation models

The links below describe the mathematical and computational details for performing standard variational optimization for supported observation models:

Zero-mean full-covariance Gaussian observation model: Variational Methods

TODO update this page

Generative model

The diagonal Gaussian observation model generates each data vector x_n of length D from a multivariate Gaussian with mean $\mu_k \in \mathbb{R}^D$ and a diagonal covariance matrix:

Global Random Variables The global random variables are the cluster-specific means and precisions (inverse variances).

For each cluster k, we have the following global random variables:

$$\mu_{k1}, \mu_{k2}, \dots \mu_{kD}$$
 $\mu_{kd} \in \mathbb{R}$
 $\lambda_{k1}, \lambda_{k2}, \dots \lambda_{kD}$ $\lambda_{kd} \in (0, +\infty)$

Local Random Variables Each dataset observation at index *n* has its own cluster assignment:

$$z_n \in \{1, 2, \dots K\}$$

The generative model and approximate posterior for z_n is determined by an allocation model. For all computations needed by our current observation model, we'll assume either a point estimate or an approximate posterior for z_n is known.

Normal Wishart prior

Each dimension d has a mean μ_{kd} and variance λ_{kd} which have a joint univariate Normal-Wishart prior with scalar hyperparameters $\bar{\nu}$, $\bar{\beta}_d$ for the Wishart prior and then \bar{m}_d , $\bar{\kappa}$ for the Normal prior:

$$\lambda_{kd} \sim \mathcal{W}_1(\bar{\nu}, \bar{\beta}_d)$$
$$\mu_{kd} \sim \mathcal{N}_1(\bar{m}_d, \bar{\kappa}^{-1} \lambda_{kd}^{-1})$$

These are represented by the following numpy array attributes of the Prior parameter bag:

- nu [float] degrees of freedom
- beta [1D array, size D] scale parameters that set mean of lambda
- m [1D array, size D] mean of the parameter mu
- kappa [float] scalar precision of mu

Several keyword arguments can be used to determine the values of the prior hyperparameters when calling bnpy.run

- --nu [float] Sets value of $\bar{\nu}$. Defaults to D + 2.
- **--kappa** [float] Sets value of $\bar{\kappa}$. Defaults to ???.
- --ECovMat [str] Determines the expected value of data covariance under the prior. Possible values include 'eye' and 'diagcovdata'. TODO
- **--sF** [float] These two options set the value of $\bar{\beta}$. TODO.
- TODO set m??

Approximate posterior

We assume the following factorized approximate posterior family for variational optimization:

$$q(z, \mu, \lambda) = \prod_{n=1}^{N} q(z_n) \cdot \prod_{k=1}^{K} (\mu_k, \lambda_k)$$

The specific forms of the global and local factors are given below.

Posterior for local assignments For each observation vector at index n, we assume an independent approximate posterior over the assigned cluster indicator $z_n \in \{1, 2, ... K\}$.

$$q(z) = \prod_{n=1}^{N} q(z_n | \hat{r}_n)$$

$$= \prod_{n=1}^{N} \operatorname{Discrete}(z_n | \hat{r}_{n1}, \hat{r}_{n2}, \dots \hat{r}_{nK})$$

Thus, for this observation model the only local variational parameter is the assignment responsibility array $\hat{r} = \{\{\hat{r}_{nk}\}_{k=1}^K\}_{n=1}^N$.

Inside the *LP* dict, this is represented by the *resp* numpy array:

• resp [2D array, size N x K] Parameters of approximate posterior q(z) over cluster assignments. resp[n,k] = probability observation n is assigned to component k.

Remember, all computations required by our observation model assume that the resp array is given. The actual values of resp are updated by an allocation model.

Posterior for global parameters The goal of variational optimization is to find the best approximate posterior distribution for the mean and precision parameters of each cluster *k*:

$$q(\mu, \lambda) = \prod_{k=1}^{K} \prod_{d=1}^{D} q(\mu_{kd}, \lambda_{kd})$$

$$= \prod_{k=1}^{K} \prod_{d=1}^{D} \mathcal{W}_{1}(\lambda_{kd} | \hat{\nu}_{k}, \hat{\beta}_{kd}) \mathcal{N}_{1}(\mu_{kd} | \hat{m}_{kd}, \hat{\kappa}_{k}^{-1} \lambda_{kd}^{-1})$$

This approximate posterior is represented by the *Post* attribute of the *DiagGaussObsModel*. This is a Param-Bag with the following attributes:

- K [int] number of active clusters
- nu [1D array, size K] Defines $\hat{\nu}_k$ for each cluster
- beta [2D array, size K x D] Defines $\hat{\beta}_{kd}$ for each cluster and dimension
- m [2D array, size K x D] Defines \hat{m}_{kd} for each cluster and dimension
- **kappa** [2D array, size K] Defines $\hat{\kappa}_k$ for each cluster

Objective function Variational optimization will find the approximate posterior parameters that maximize the following objective function, given a fixed observed dataset $x = \{x_1, \dots x_N\}$ and fixed prior hyparpa-

rameters $\bar{\nu}, \bar{\beta}, \bar{m}, \bar{\kappa}$.

$$\mathcal{L}^{\text{DiagGauss}}(\hat{\nu}, \hat{\beta}, \hat{m}, \hat{\kappa}) = \sum_{k=1}^{K} \sum_{d=1}^{D} c_{1,1}^{\text{NW}}(\hat{\nu}_{k}, \hat{\beta}_{kd}, \hat{m}_{kd}, \hat{\kappa})_{k} - c_{1,1}^{\text{NW}}(\bar{\nu}, \bar{\beta}_{d}, \bar{m}_{d}, \bar{\kappa})$$

$$+ \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} (N_{k}(\hat{r}) + \bar{\nu} - \hat{\nu}_{k}) \, \mathbb{E}_{q}[\log \lambda_{kd}]$$

$$- \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} (N_{k}(\hat{r}) + \bar{\kappa} - \hat{\kappa}_{k}) \, \mathbb{E}_{q}[\lambda_{kd}]$$

$$+ \sum_{k=1}^{K} \sum_{d=1}^{D} (S_{kd}^{x}(x, \hat{r}) + \bar{\kappa} \bar{m}_{d} - \hat{\kappa}_{k} \hat{m}_{kd}) \, \mathbb{E}_{q}[\lambda_{kd} \mu_{kd}]$$

$$- \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} \left(S_{kd}^{x^{2}}(x, \hat{r}) + \bar{\beta}_{d} + \bar{\kappa} \bar{m}_{d}^{2} - \hat{\beta}_{kd} - \hat{\kappa}_{k} \hat{m}_{kd}^{2} \right) \, \mathbb{E}_{q}[\lambda_{kd} \mu_{kd}]$$

This objective function is computed by calling the Python function calc_evidence.

Sufficient statistics The sufficient statistics of this observation model are functions of the local parameters \hat{r} and the observed data x.

$$N_k(\hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk}$$

$$S_{kd}^x(x, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk} x_{nd}^2$$

$$S_{kd}^{x^2}(x, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk} x_{nd}^2$$

These fields are stored within the sufficient statistics parameter bag SS as the following fields:

- SS.N [1D array, size K] SS.N[k] = N_k
- SS.x [2D array, size K x D] SS.x[k,d] = $S_{kd}^x(x,\hat{r})$
- SS.xx [2D array, size K x D] SS.xx[k,d] = $S_{kd}^{x^2}(x,\hat{r})$

Cumulant function The cumulant function of the univariate Normal-Wishart is evaluated for each dimension *d* separately. The function takes 4 scalar input arguments and produces a scalar output.

$$c_{1,1}^{\text{NW}}(\nu,\beta_d,m_d,\kappa) = -\frac{1}{2}\log 2\pi + \frac{1}{2}\log \kappa + \frac{\nu}{2}\log \frac{\beta_d}{2} - \log \Gamma\left(\frac{\nu}{2}\right)$$

Coordinate Ascent Updates

Local step update As with all observation models, the local step computes the *expected* log conditional probability of assigning each observation to each cluster:

$$\mathbb{E}[\log p(x_n|\mu_k, \lambda_k)] = -\frac{D}{2}\log 2\pi + \frac{1}{2}\sum_{d=1}^{D}\mathbb{E}[\log \lambda_{kd}] - \frac{1}{2}\sum_{d=1}^{D}\mathbb{E}[\lambda_{kd}(x_{nd} - \mu_{kd})^2]$$

where the elementary expectations required are:

$$\mathbb{E}[\log \lambda_{kd}] = \psi\left(\frac{\hat{\nu}_k}{2}\right) - \log\frac{\hat{\beta}_{kd}}{2}$$

$$\mathbb{E}_q\left[\lambda_{kd}(x_{nd} - \mu_{kd})^2\right] = \frac{1}{\hat{\kappa}_k} + \frac{\hat{\nu}_k}{\hat{\beta}_{kd}}(x_{nd} - \hat{m}_{kd})^2$$

In our implementation, this is done via the function calc_local_params, which computes the following arrays and places them inside the local parameter dict LP.

• **E_log_soft_ev** [2D array, N x K] log probability of assigning each observation n to each cluster

Global step update The global step update produces an updated approximate posterior over the global random variables. Concretely, this means updated values for each field of the Post ParamBag attribute of the DiagGaussObsModel.

$$\hat{\nu}_k \leftarrow N_k(\hat{r}) + \bar{\nu}$$

$$\hat{\kappa}_k \leftarrow N_k(\hat{r}) + \bar{\kappa}$$

$$\hat{m}_{kd} \leftarrow \frac{1}{\hat{\kappa}_k} \left(S_k^x(x, \hat{r}) + \bar{\kappa} \bar{m}_d \right)$$

$$\hat{\beta}_{kd} \leftarrow S_{kd}^{x^2}(x, \hat{r}) + \bar{\beta}_d + \bar{\kappa} \bar{m}_d^2 - \hat{\kappa}_k \hat{m}_{kd}^2$$

Our implementation performs this update when calling the function update_global_params.

Initialization

Initialization creates valid values of the parameters which define the approximate posterior over the global random variables. Concretely, this means it creates a valid setting of the Post attribute of the DiagGaussObsModel object.

TODO

Diagonal-covariance Gaussian observation model: Variational Bayesian Methods

Generative model

The diagonal Gaussian observation model generates each data vector x_n of length D from a multivariate Gaussian with mean $\mu_k \in \mathbb{R}^D$ and a diagonal covariance matrix:

$$\begin{array}{cccc}
x_{n1} & & & \\
x_{n2} & & & \\
\vdots & & & \\
x_{nD} & & & \\
\end{array} \sim \mathcal{N} \begin{pmatrix} \mu_{k1} & \lambda_{k1}^{-1} & & \\
\mu_{k2} & & \lambda_{k2}^{-1} & & \\
\vdots & & & \ddots & \\
\mu_{kD} & & & & \lambda_{kD}^{-1} \end{pmatrix}$$

Global Random Variables The global random variables are the cluster-specific means and precisions (inverse variances).

For each cluster k, we have the following global random variables:

$$\mu_{k1}, \mu_{k2}, \dots \mu_{kD}$$
 $\mu_{kd} \in \mathbb{R}$
 $\lambda_{k1}, \lambda_{k2}, \dots \lambda_{kD}$ $\lambda_{kd} \in (0, +\infty)$

Local Random Variables Each dataset observation at index *n* has its own cluster assignment:

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The generative model and approximate posterior for z_n is determined by an allocation model. For all computations needed by our current observation model, we'll assume either a point estimate or an approximate posterior for z_n is known.

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Each dimension d has a mean μ_{kd} and variance λ_{kd} which have a joint univariate Normal-Wishart prior with scalar hyperparameters $\bar{\nu}$, $\bar{\beta}_d$ for the Wishart prior and then \bar{m}_d , $\bar{\kappa}$ for the Normal prior:

$$\lambda_{kd} \sim \mathcal{W}_1(\bar{\nu}, \bar{\beta}_d)$$
$$\mu_{kd} \sim \mathcal{N}_1(\bar{m}_d, \bar{\kappa}^{-1} \lambda_{kd}^{-1})$$

These are represented by the following numpy array attributes of the Prior parameter bag:

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- **--sF** [float] These two options set the value of $\bar{\beta}$. TODO.
- TODO set m??

Approximate posterior

We assume the following factorized approximate posterior family for variational optimization:

$$q(z, \mu, \lambda) = \prod_{n=1}^{N} q(z_n) \cdot \prod_{k=1}^{K} (\mu_k, \lambda_k)$$

The specific forms of the global and local factors are given below.

Posterior for local assignments For each observation vector at index n, we assume an independent approximate posterior over the assigned cluster indicator $z_n \in \{1, 2, ... K\}$.

$$q(z) = \prod_{n=1}^{N} q(z_n | \hat{r}_n)$$

$$= \prod_{n=1}^{N} \operatorname{Discrete}(z_n | \hat{r}_{n1}, \hat{r}_{n2}, \dots \hat{r}_{nK})$$

Thus, for this observation model the only local variational parameter is the assignment responsibility array $\hat{r} = \{\{\hat{r}_{nk}\}_{k=1}^K\}_{n=1}^N$.

Inside the *LP* dict, this is represented by the *resp* numpy array:

• resp [2D array, size N x K] Parameters of approximate posterior q(z) over cluster assignments. resp[n,k] = probability observation n is assigned to component k.

Remember, all computations required by our observation model assume that the resp array is given. The actual values of resp are updated by an allocation model.

Posterior for global parameters The goal of variational optimization is to find the best approximate posterior distribution for the mean and precision parameters of each cluster k:

$$q(\mu, \lambda) = \prod_{k=1}^{K} \prod_{d=1}^{D} q(\mu_{kd}, \lambda_{kd})$$

$$= \prod_{k=1}^{K} \prod_{d=1}^{D} \mathcal{W}_{1}(\lambda_{kd} | \hat{\nu}_{k}, \hat{\beta}_{kd}) \mathcal{N}_{1}(\mu_{kd} | \hat{m}_{kd}, \hat{\kappa}_{k}^{-1} \lambda_{kd}^{-1})$$

This approximate posterior is represented by the *Post* attribute of the *DiagGaussObsModel*. This is a Param-Bag with the following attributes:

- K [int] number of active clusters
- nu [1D array, size K] Defines $\hat{\nu}_k$ for each cluster
- beta [2D array, size K x D] Defines $\hat{\beta}_{kd}$ for each cluster and dimension
- m [2D array, size K x D] Defines \hat{m}_{kd} for each cluster and dimension
- **kappa** [2D array, size K] Defines $\hat{\kappa}_k$ for each cluster

Objective function Variational optimization will find the approximate posterior parameters that maximize the following objective function, given a fixed observed dataset $x = \{x_1, \dots x_N\}$ and fixed prior hyparparameters $\bar{\nu}, \bar{\beta}, \bar{m}, \bar{\kappa}$.

$$\begin{split} \mathcal{L}^{\text{DiagGauss}}(\hat{\nu}, \hat{\beta}, \hat{m}, \hat{\kappa}) &= -\frac{ND}{2} \log 2\pi \\ &+ \sum_{k=1}^{K} \sum_{d=1}^{D} c_{1,1}^{\text{NW}}(\hat{\nu}_{k}, \hat{\beta}_{kd}, \hat{m}_{kd}, \hat{\kappa})_{k} - c_{1,1}^{\text{NW}}(\bar{\nu}, \bar{\beta}_{d}, \bar{m}_{d}, \bar{\kappa}) \\ &+ \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} \left(N_{k}(\hat{r}) + \bar{\nu} - \hat{\nu}_{k} \right) \mathbb{E}_{q}[\log \lambda_{kd}] \\ &- \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} \left(N_{k}(\hat{r}) + \bar{\kappa} - \hat{\kappa}_{k} \right) \mathbb{E}_{q}[\lambda_{kd}] \\ &+ \sum_{k=1}^{K} \sum_{d=1}^{D} \left(S_{kd}^{x}(x, \hat{r}) + \bar{\kappa} \bar{m}_{d} - \hat{\kappa}_{k} \hat{m}_{kd} \right) \mathbb{E}_{q}[\lambda_{kd} \mu_{kd}] \\ &- \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} \left(S_{kd}^{x^{2}}(x, \hat{r}) + \bar{\beta}_{d} + \bar{\kappa} \bar{m}_{d}^{2} - \hat{\beta}_{kd} - \hat{\kappa}_{k} \hat{m}_{kd}^{2} \right) \mathbb{E}_{q}[\lambda_{kd} \mu_{kd}] \end{split}$$

This objective function is computed by calling the Python function calc_evidence.

Sufficient statistics The sufficient statistics of this observation model are functions of the local parameters \hat{r} and the observed data x.

$$N_k(\hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk}$$

$$S_{kd}^x(x, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk} x_{nd}^2$$

$$S_{kd}^{x^2}(x, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk} x_{nd}^2$$

These fields are stored within the sufficient statistics parameter bag SS as the following fields:

- SS.N [1D array, size K] SS.N[k] = N_k
- SS.x [2D array, size K x D] SS.x[k,d] = $S_{kd}^x(x,\hat{r})$
- SS.xx [2D array, size K x D] SS.xx[k,d] = $S_{kd}^{x^2}(x,\hat{r})$

Cumulant function The cumulant function of the univariate Normal-Wishart is evaluated for each dimension *d* separately. The function takes 4 scalar input arguments and produces a scalar output.

$$c_{1,1}^{\text{NW}}(\nu, \beta_d, m_d, \kappa) = \frac{1}{2} \log 2\pi - \frac{1}{2} \log \kappa - \frac{\nu}{2} \log \frac{\beta_d}{2} + \log \Gamma\left(\frac{\nu}{2}\right)$$

Coordinate Ascent Updates

Local step update As with all observation models, the local step computes the *expected* log conditional probability of assigning each observation to each cluster:

$$\mathbb{E}[\log p(x_n|\mu_k, \lambda_k)] = -\frac{D}{2}\log 2\pi + \frac{1}{2}\sum_{d=1}^{D}\mathbb{E}[\log \lambda_{kd}] - \frac{1}{2}\sum_{d=1}^{D}\mathbb{E}[\lambda_{kd}(x_{nd} - \mu_{kd})^2]$$

where the elementary expectations required are:

$$\mathbb{E}[\log \lambda_{kd}] = \psi\left(\frac{\hat{\nu}_k}{2}\right) - \log\frac{\hat{\beta}_{kd}}{2}$$

$$\mathbb{E}_q\left[\lambda_{kd}(x_{nd} - \mu_{kd})^2\right] = \frac{1}{\hat{\kappa}_k} + \frac{\hat{\nu}_k}{\hat{\beta}_{kd}}(x_{nd} - \hat{m}_{kd})^2$$

In our implementation, this is done via the function <code>calc_local_params</code>, which computes the following arrays and places them inside the local parameter dict LP.

• $\texttt{E_log_soft_ev}$ [2D array, N x K] log probability of assigning each observation n to each cluster k

Global step update The global step update produces an updated approximate posterior over the global random variables. Concretely, this means updated values for each field of the Post ParamBag attribute of the DiagGaussObsModel.

$$\hat{\nu}_k \leftarrow N_k(\hat{r}) + \bar{\nu}$$

$$\hat{\kappa}_k \leftarrow N_k(\hat{r}) + \bar{\kappa}$$

$$\hat{m}_{kd} \leftarrow \frac{1}{\hat{\kappa}_k} \left(S_k^x(x, \hat{r}) + \bar{\kappa} \bar{m}_d \right)$$

$$\hat{\beta}_{kd} \leftarrow S_{kd}^{x^2}(x, \hat{r}) + \bar{\beta}_d + \bar{\kappa} \bar{m}_d^2 - \hat{\kappa}_k \hat{m}_{kd}^2$$

Our implementation performs this update when calling the function update_qlobal_params.

Initialization

Initialization creates valid values of the parameters which define the approximate posterior over the global random variables. Concretely, this means it creates a valid setting of the Post attribute of the DiagGaussObsModel object.

TODO

Full-covariance Gaussian observation model: Variational Bayesian Methods

TODO revise this!

Generative model

The diagonal Gaussian observation model generates each data vector x_n of length D from a multivariate Gaussian with mean $\mu_k \in \mathbb{R}^D$ and a diagonal covariance matrix:

Global Random Variables The global random variables are the cluster-specific means and precisions (inverse variances).

For each cluster k, we have the following global random variables:

$$\mu_{k1}, \mu_{k2}, \dots \mu_{kD}$$
 $\mu_{kd} \in \mathbb{R}$
 $\lambda_{k1}, \lambda_{k2}, \dots \lambda_{kD}$ $\lambda_{kd} \in (0, +\infty)$

Local Random Variables Each dataset observation at index *n* has its own cluster assignment:

$$z_n \in \{1, 2, \dots K\}$$

The generative model and approximate posterior for z_n is determined by an allocation model. For all computations needed by our current observation model, we'll assume either a point estimate or an approximate posterior for z_n is known.

Normal Wishart prior

Each dimension d has a mean μ_{kd} and variance λ_{kd} which have a joint univariate Normal-Wishart prior with scalar hyperparameters $\bar{\nu}$, $\bar{\beta}_d$ for the Wishart prior and then \bar{m}_d , $\bar{\kappa}$ for the Normal prior:

$$\lambda_{kd} \sim \mathcal{W}_1(\bar{\nu}, \bar{\beta}_d)$$
$$\mu_{kd} \sim \mathcal{N}_1(\bar{m}_d, \bar{\kappa}^{-1} \lambda_{kd}^{-1})$$

These are represented by the following numpy array attributes of the Prior parameter bag:

- nu [float] degrees of freedom
- beta [1D array, size D] scale parameters that set mean of lambda
- m [1D array, size D] mean of the parameter mu
- kappa [float] scalar precision of mu

Several keyword arguments can be used to determine the values of the prior hyperparameters when calling bnpy.run

- --nu [float] Sets value of $\bar{\nu}$. Defaults to D + 2.
- --kappa [float] Sets value of $\bar{\kappa}$. Defaults to ???.
- --ECovMat [str] Determines the expected value of data covariance under the prior. Possible values include 'eye' and 'diagcovdata'. TODO
- **--sF** [float] These two options set the value of $\bar{\beta}$. TODO.
- TODO set m??

Approximate posterior

We assume the following factorized approximate posterior family for variational optimization:

$$q(z, \mu, \lambda) = \prod_{n=1}^{N} q(z_n) \cdot \prod_{k=1}^{K} (\mu_k, \lambda_k)$$

The specific forms of the global and local factors are given below.

Posterior for local assignments For each observation vector at index n, we assume an independent approximate posterior over the assigned cluster indicator $z_n \in \{1, 2, ... K\}$.

$$q(z) = \prod_{n=1}^{N} q(z_n | \hat{r}_n)$$

= $\prod_{n=1}^{N} \mathrm{Discrete}(z_n | \hat{r}_{n1}, \hat{r}_{n2}, \dots \hat{r}_{nK})$

Thus, for this observation model the only local variational parameter is the assignment responsibility array $\hat{r} = \{\{\hat{r}_{nk}\}_{k=1}^K\}_{n=1}^N$.

Inside the *LP* dict, this is represented by the *resp* numpy array:

• resp [2D array, size N x K] Parameters of approximate posterior q(z) over cluster assignments. resp[n,k] = probability observation n is assigned to component k.

Remember, all computations required by our observation model assume that the resp array is given. The actual values of resp are updated by an allocation model.

Posterior for global parameters The goal of variational optimization is to find the best approximate posterior distribution for the mean and precision parameters of each cluster *k*:

$$q(\mu, \lambda) = \prod_{k=1}^{K} \prod_{d=1}^{D} q(\mu_{kd}, \lambda_{kd})$$

$$= \prod_{k=1}^{K} \prod_{d=1}^{D} \mathcal{W}_{1}(\lambda_{kd} | \hat{\nu}_{k}, \hat{\beta}_{kd}) \mathcal{N}_{1}(\mu_{kd} | \hat{m}_{kd}, \hat{\kappa}_{k}^{-1} \lambda_{kd}^{-1})$$

This approximate posterior is represented by the *Post* attribute of the *DiagGaussObsModel*. This is a Param-Bag with the following attributes:

- K [int] number of active clusters
- nu [1D array, size K] Defines $\hat{\nu}_k$ for each cluster
- beta [2D array, size K x D] Defines $\hat{\beta}_{kd}$ for each cluster and dimension
- m [2D array, size K x D] Defines \hat{m}_{kd} for each cluster and dimension
- **kappa** [2D array, size K] Defines $\hat{\kappa}_k$ for each cluster

Objective function Variational optimization will find the approximate posterior parameters that maximize the following objective function, given a fixed observed dataset $x = \{x_1, \dots x_N\}$ and fixed prior hyparparameters $\bar{\nu}, \bar{\beta}, \bar{m}, \bar{\kappa}$.

$$\mathcal{L}^{\text{DiagGauss}}(\hat{\nu}, \hat{\beta}, \hat{m}, \hat{\kappa}) = \sum_{k=1}^{K} \sum_{d=1}^{D} c_{1,1}^{\text{NW}}(\hat{\nu}_{k}, \hat{\beta}_{kd}, \hat{m}_{kd}, \hat{\kappa})_{k} - c_{1,1}^{\text{NW}}(\bar{\nu}, \bar{\beta}_{d}, \bar{m}_{d}, \bar{\kappa})$$

$$+ \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} (N_{k}(\hat{r}) + \bar{\nu} - \hat{\nu}_{k}) \, \mathbb{E}_{q}[\log \lambda_{kd}]$$

$$- \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} (N_{k}(\hat{r}) + \bar{\kappa} - \hat{\kappa}_{k}) \, \mathbb{E}_{q}[\lambda_{kd}]$$

$$+ \sum_{k=1}^{K} \sum_{d=1}^{D} (S_{kd}^{x}(x, \hat{r}) + \bar{\kappa} \bar{m}_{d} - \hat{\kappa}_{k} \hat{m}_{kd}) \, \mathbb{E}_{q}[\lambda_{kd} \mu_{kd}]$$

$$- \frac{1}{2} \sum_{k=1}^{K} \sum_{d=1}^{D} \left(S_{kd}^{x^{2}}(x, \hat{r}) + \bar{\beta}_{d} + \bar{\kappa} \bar{m}_{d}^{2} - \hat{\beta}_{kd} - \hat{\kappa}_{k} \hat{m}_{kd}^{2} \right) \, \mathbb{E}_{q}[\lambda_{kd} \mu_{kd}]$$

This objective function is computed by calling the Python function calc_evidence.

Sufficient statistics The sufficient statistics of this observation model are functions of the local parameters \hat{r} and the observed data x.

$$N_k(\hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk}$$

$$S_{kd}^x(x, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk} x_{nd}^2$$

$$S_{kd}^{x^2}(x, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk} x_{nd}^2$$

These fields are stored within the sufficient statistics parameter bag SS as the following fields:

- SS.N [1D array, size K] SS.N[k] = N_k
- SS.x [2D array, size K x D] SS.x[k,d] = $S_{kd}^x(x,\hat{r})$
- SS.xx [2D array, size K x D] SS.xx[k,d] = $S_{kd}^{x^2}(x,\hat{r})$

Cumulant function The cumulant function of the univariate Normal-Wishart is evaluated for each dimension *d* separately. The function takes 4 scalar input arguments and produces a scalar output.

$$c_{1,1}^{\text{NW}}(\nu, \beta_d, m_d, \kappa) = -\frac{1}{2}\log 2\pi + \frac{1}{2}\log \kappa + \frac{\nu}{2}\log \frac{\beta_d}{2} - \log \Gamma\left(\frac{\nu}{2}\right)$$

Coordinate Ascent Updates

Local step update As with all observation models, the local step computes the *expected* log conditional probability of assigning each observation to each cluster:

$$\mathbb{E}[\log p(x_n|\mu_k, \lambda_k)] = -\frac{D}{2}\log 2\pi + \frac{1}{2}\sum_{d=1}^{D}\mathbb{E}[\log \lambda_{kd}] - \frac{1}{2}\sum_{d=1}^{D}\mathbb{E}[\lambda_{kd}(x_{nd} - \mu_{kd})^2]$$

where the elementary expectations required are:

$$\mathbb{E}[\log \lambda_{kd}] = \psi\left(\frac{\hat{\nu}_k}{2}\right) - \log\frac{\hat{\beta}_{kd}}{2}$$

$$\mathbb{E}_q\left[\lambda_{kd}(x_{nd} - \mu_{kd})^2\right] = \frac{1}{\hat{\kappa}_k} + \frac{\hat{\nu}_k}{\hat{\beta}_{kd}}(x_{nd} - \hat{m}_{kd})^2$$

In our implementation, this is done via the function <code>calc_local_params</code>, which computes the following arrays and places them inside the local parameter dict LP.

• $\texttt{E_log_soft_ev}$ [2D array, N x K] log probability of assigning each observation n to each cluster k

Global step update The global step update produces an updated approximate posterior over the global random variables. Concretely, this means updated values for each field of the Post ParamBag attribute of the DiagGaussObsModel.

$$\hat{\nu}_k \leftarrow N_k(\hat{r}) + \bar{\nu}$$

$$\hat{\kappa}_k \leftarrow N_k(\hat{r}) + \bar{\kappa}$$

$$\hat{m}_{kd} \leftarrow \frac{1}{\hat{\kappa}_k} \left(S_k^x(x, \hat{r}) + \bar{\kappa} \bar{m}_d \right)$$

$$\hat{\beta}_{kd} \leftarrow S_{kd}^{x^2}(x, \hat{r}) + \bar{\beta}_d + \bar{\kappa} \bar{m}_d^2 - \hat{\kappa}_k \hat{m}_{kd}^2$$

Our implementation performs this update when calling the function update_global_params.

Initialization

Initialization creates valid values of the parameters which define the approximate posterior over the global random variables. Concretely, this means it creates a valid setting of the Post attribute of the DiagGaussObsModel object.

TODO

Gaussian Regression observation model: Variational Bayesian Methods

Generative model

The Gaussian regression observation model explains a observed collection of input/output data pairs $\{x_n, y_n\}_{n=1}^N$. Each input observation x_n is a vector of length D, while each output observation y_n is a scalar

In this document, we assume that the observed input data x are fixed and focus on a generative model for the output data y which depends on x. Various generative models, such as the diagonal-covariance Gaussian, are possible for the observed data x. These can be straight-forwardly combined with the model here to produce a joint model for both x and y.

Each cluster *k* produces the output values according to the following standard Bayesian linear regression model:

$$y_n \sim \mathcal{N}\left(b_k + \sum_{d=1}^D w_{kd} x_{nd}, \delta_k^{-1}\right)$$

Here, the cluster-specific parameters are a weight vector w_k , an intercept weight b_k , and a precision scalar δ_k . These are the global random variables of this observation model.

Alternatively, if we define an *expanded* input data vector $\tilde{x}_n = [x_{n1}x_{n2} \dots x_{nD} \ 1]$, we can write the generative model more simply as:

$$y_n \sim \mathcal{N}\left(\sum_{d=1}^{D+1} w_{kd}\tilde{x}_{nd}, \delta_k^{-1}\right)$$

Global Random Variables The global random variables are the cluster-specific weights and precisions. For each cluster k, we have

$$w_k \in \mathbb{R}^D$$
, $w_k = [w_{k1}, w_{k2}, \dots w_{kD} w_{kD+1}]$
 $\delta_k \in (0, +\infty)$

For convenience, let E denote the size of this expanded representation, where E = D + 1.

Local Random Variables Each dataset observation at index *n* has its own cluster assignment:

$$z_n \in \{1, 2, \dots K\}$$

The generative model and approximate posterior for z_n is determined by an allocation model. For all computations needed by our current observation model, we'll assume either a point estimate or an approximate posterior for z_n is known.

Normal-Wishart prior

We assume that the weights w_k and the precision δ_k have a joint Normal-Wishart prior with hyperparameters:

• $\bar{\nu}$ [positive scalar] count parameter of the Wishart prior on precision

- $\bar{\tau}$ [positive scalar] location parameter of the Wishart prior on precision
- \bar{w} [vector of size E] mean value of the Normal prior on cluster weights
- \bar{P} [positive definite E x E matrix] precision matrix for the Normal prior on cluster weights

Mathematically, we have:

$$\delta_k \sim \mathcal{W}_1(\bar{\nu}, \bar{\tau})$$

$$w_k \sim \mathcal{N}_E(\bar{w}, \delta_k^{-1} \bar{P}^{-1})$$

Under this prior, here are some useful expectations for the precision random variable:

$$\mathbb{E}_{\text{prior}}[\delta_k] = \frac{\bar{\nu}}{\bar{\tau}}$$

$$\mathbb{E}_{\text{prior}}[\delta_k^{-1}] = \frac{\bar{\tau}}{\bar{\nu} - 2}$$

$$\text{Var}_{\text{prior}}[\delta_k] = \frac{\bar{\nu}}{\bar{\tau}^2}$$

Likewise, here are some useful prior expectations for the weight vector random variable:

$$\mathbb{E}_{\text{prior}}[w_k] = \bar{w}$$

$$\text{Cov}_{\text{prior}}[w_k] = \frac{\bar{\tau}}{\bar{\nu} - 2}\bar{P}^{-1}$$

And some useful joint expectations:

$$\mathbb{E}_{\text{prior}}[\delta_k w_k] = \frac{\bar{\nu}}{\bar{\tau}} \bar{w}$$

$$\mathbb{E}_{\text{prior}}[\delta_k w_k w_k^T] = \bar{P}^{-1} + \frac{\bar{\nu}}{\bar{\tau}} \bar{w} \bar{w}^T$$

In our Python implementation of the GaussRegressYFromFixedXObsModel class, these quantities are represented by the following numpy array attributes of the Prior parameter bag:

- pnu [float] value of $\bar{\nu}$
- ptau [float] value of $\bar{\tau}$
- w_E [1D array, size E] value of \bar{w}
- P_EE [2D array, size E x E] value of \bar{P}

Several keyword arguments can be used to determine the values of the prior hyperparameters when calling bnpy.run

- **--pnu** [float] Sets value of $\bar{\nu}$. Defaults to 1.
- --ptau [float] Sets value of $\bar{\tau}$. Defaults to 1.
- --w_E [float or 1D array] Sets value of the vector \bar{w} . If float is provided, the whole vector is filled with that value. Defaults to 0.
- --P_diag_val [float or 1D array] Sets \bar{P} to diagonal matrix with specified values. Defaults to 1e-6

Approximate posterior

We assume the following factorized approximate posterior family for variational optimization:

$$q(z, w, \delta) = \prod_{n=1}^{N} q(z_n) \cdot \prod_{k=1}^{K} (w_k, \delta_k)$$

The specific forms of the global and local factors are given below.

Posterior for local assignments For each observation vector at index n, we assume an independent approximate posterior over the assigned cluster indicator $z_n \in \{1, 2, ... K\}$.

$$q(z) = \prod_{n=1}^{N} q(z_n | \hat{r}_n)$$

$$= \prod_{n=1}^{N} \text{Discrete}(z_n | \hat{r}_{n1}, \hat{r}_{n2}, \dots \hat{r}_{nK})$$

Thus, for this observation model the only local variational parameter is the assignment responsibility array $\hat{r} = \{\{\hat{r}_{nk}\}_{k=1}^K\}_{n=1}^N$.

Inside the *LP* dict, this is represented by the *resp* numpy array:

• resp [2D array, size N x K] Parameters of approximate posterior q(z) over cluster assignments. resp[n,k] = probability observation n is assigned to component k.

Remember, all computations required by our observation model assume that the resp array is given. The actual values of resp are updated by an allocation model.

Posterior for global parameters The goal of variational optimization is to find the best approximate posterior distribution for the mean and precision parameters of each cluster *k*:

$$q(w,\delta) = \prod_{k=1}^{K} \mathcal{W}_1(\delta_k|\hat{\nu}_k, \hat{\tau}_k) \mathcal{N}_E(w_k|\hat{w}_k, \delta_k^{-1} \hat{P}_k^{-1})$$

Within our Python implementation in the class GaussRegressYFromFixedXObsModel, this approximate posterior is represented within the *Post* attribute. This attribute is a ParamBag object containing the following numpy arrays:

- K [int] number of active clusters
- pnu_K [1D array, size K] Defines $\hat{\nu}_k$ for each cluster
- **ptau_K** [1D array, size K] Defines $\hat{\tau}_k$ for each cluster
- w_KE [2D array, size K x E] Defines \hat{w}_{ke} for each cluster and expanded dimension
- P_KEE [2D array, size K x E x E] Defines precision matrix \hat{P}_k for each cluster

Objective function Variational optimization will find the approximate posterior parameters that maximize the following objective function, given a fixed observed dataset $x = \{x_1, \dots x_N\}$ and fixed prior hyparparameters $\bar{\nu}, \bar{\tau}, \bar{w}, \bar{P}$.

$$\begin{split} \mathcal{L}^{\text{Gaussian Regression}}(y,x,\hat{\nu},\hat{\tau},\hat{w},\hat{P}) &= -\frac{N}{2}\log 2\pi \\ &+ \sum_{k=1}^K \sum_{d=1}^D c_{1,E}^{\text{NW}}(\hat{\nu}_k,\hat{\tau}_k,\hat{w}_k,\hat{P}_k) - c_{1,E}^{\text{NW}}(\bar{\nu},\bar{\tau},\bar{w},\bar{P}) \\ &- \frac{1}{2} \sum_{k=1}^K \left(N_k(\hat{r}) + \bar{\nu} - \hat{\nu}_k \right) \mathbb{E}_q[\log \delta_k] \\ &- \frac{1}{2} \sum_{k=1}^K \left(S_k^{yy}(y,\hat{r}) + \bar{\tau} + \bar{w}\bar{P}\bar{w} - \hat{\tau}_k - \hat{w}_k\hat{P}_k\hat{w}_k \right) \mathbb{E}_q[\delta_k] \\ &+ \sum_{k=1}^K \left(S_k^{yx}(x,y,\hat{r}) + \bar{P}\bar{w} - \hat{P}_k\hat{w}_k \right)^T \mathbb{E}_q[\delta_k w_k] \\ &- \frac{1}{2} \sum_{k=1}^K \operatorname{trace} \left(\left(S_k^{xx^T}(x,\hat{r}) + \bar{P} - \hat{P}_k \right) \mathbb{E}_q[\delta_k w_k w_k^T] \right) \end{split}$$

This objective function is computed by calling the Python function calc_evidence.

We can directly interpret this function as a lower bound on the marginal evidence:

$$\log p(y|x, \bar{\nu}, \bar{\tau}, \bar{w}, \bar{P}) \ge \mathcal{L}^{\text{Gaussian Regression}}(y, x, \hat{\nu}, \hat{\tau}, \hat{w}, \hat{P})$$

Sufficient statistics The sufficient statistics of this observation model are functions of the local parameters \hat{r} , the observed input data x, and the observed output data y.

$$N_{k}(\hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk}$$

$$S_{k}^{y^{2}}(y, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk}y_{n}^{2}$$

$$S_{k}^{yx}(x, y, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk}y_{n}x_{n}$$

$$S_{k}^{xx^{T}}(x, \hat{r}) = \sum_{n=1}^{N} \hat{r}_{nk}x_{n}x_{n}^{T}$$

These fields are stored within the sufficient statistics parameter bag SS as the following fields:

- SS.N [1D array, size K] SS.N[k] = N_k
- SS.yy_K [1D array, size K] SS.yy[k] = $S_k^{y^2}(y,\hat{r})$
- SS.yx [2D array, size K x E] SS.yx[k] = $S_k^{yx}(x,y,\hat{r})$
- SS.xxT [3D array, size K x E x E] SS.xxT[k] = $S_k^{xx^T}(x,\hat{r})$

Cumulant function The cumulant function of the Normal-Wishart produces a scalar output from 4 input arguments:

$$c_{1,E}^{\mathrm{NW}}(\nu,\tau,w,P) = \frac{E}{2}\log 2\pi - \frac{1}{2}\log |P| - \frac{\nu}{2}\log\frac{\tau}{2} + \log\Gamma\left(\frac{\nu}{2}\right)$$

where $\Gamma(\cdot)$ is the gamma function, and $\log |P|$ is the log determinant of the E x E matrix P.

Coordinate Ascent Updates

Local step update As with all observation models, the local step computes the *expected* log conditional probability of assigning each observation to each cluster:

$$\mathbb{E}_q[\log p(y_n|x_n, w_k, \delta_k)] = -\frac{1}{2}\log 2\pi + \frac{1}{2}\mathbb{E}[\log \delta_k] - \frac{1}{2}\mathbb{E}[\delta_k(y_n - w_k^T \tilde{x}_n)^2]$$

where the elementary expectations required are:

$$\mathbb{E}_{q}[\log \delta_{k}] = -\log \frac{\hat{\tau}_{k}}{2} + \psi \left(\frac{\hat{\nu}_{k}}{2}\right)$$

$$\mathbb{E}_{q}\left[\delta_{k} \left(y_{n} - w_{k}^{T} \tilde{x}_{n}\right)^{2}\right] = \tilde{x}_{n}^{T} \hat{P}_{k}^{-1} \tilde{x}_{n} + \frac{\hat{\nu}_{k}}{\hat{\tau}_{k}} (y_{n} - \bar{w}_{k}^{T} \tilde{x}_{n})^{2}$$

The above operations can be efficiently computed via smart vectorized calculations on modern cpus.

In our implementation, this is done via the function <code>calc_local_params</code>, which computes the following arrays and places them inside the local parameter dict LP.

• **E_log_soft_ev** [2D array, N x K] log probability of assigning each observation n to each cluster k

Global step update The global step update produces an updated approximate posterior over the global random variables. Concretely, this means updated values for each of the four parameters which define each cluster-specific Normal-Wishart:

$$\hat{\nu}_k \leftarrow N_k(\hat{r}) + \bar{\nu}$$

$$\hat{P}_k \leftarrow \bar{P}_k + S_k^{xx^T}(x, \hat{r})$$

$$\hat{w}_k \leftarrow \hat{P}_k^{-1} \left(\bar{P}\bar{w} + S_k^{yx}(x, y, \hat{r}) \right)$$

$$\hat{\tau}_k \leftarrow \bar{\tau} + S_k^{y^2}(y, \hat{r}) + \bar{w}^T \bar{P}\bar{w} - \hat{w}_k^T \hat{P}_k \hat{w}_k$$

Our implementation performs this update when calling the function update_global_params.

Initialization

Initialization creates valid values of the parameters which define the approximate posterior over the global random variables. Concretely, this means it creates a valid setting of the Post attribute of the GaussRegressYFromFixedXObsModel object.

TODO

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