

# 模式识别编程实验报告

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注：本实验所有代码可见

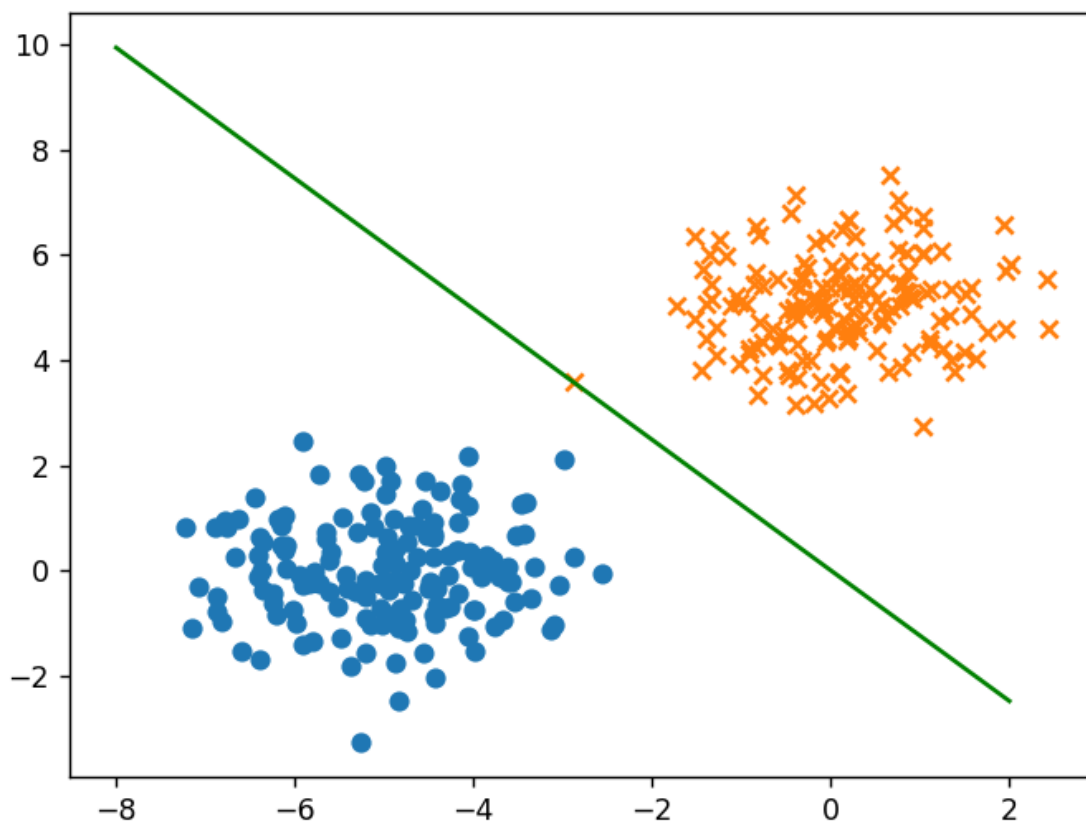
<https://github.com/Hongyuan-Tao/Pattern-Recognition-And-Machine-Learning>

## Lecture2 (感知机算法) :

1、如程序PLAandPocket.py中PLA和Pocket函数所示

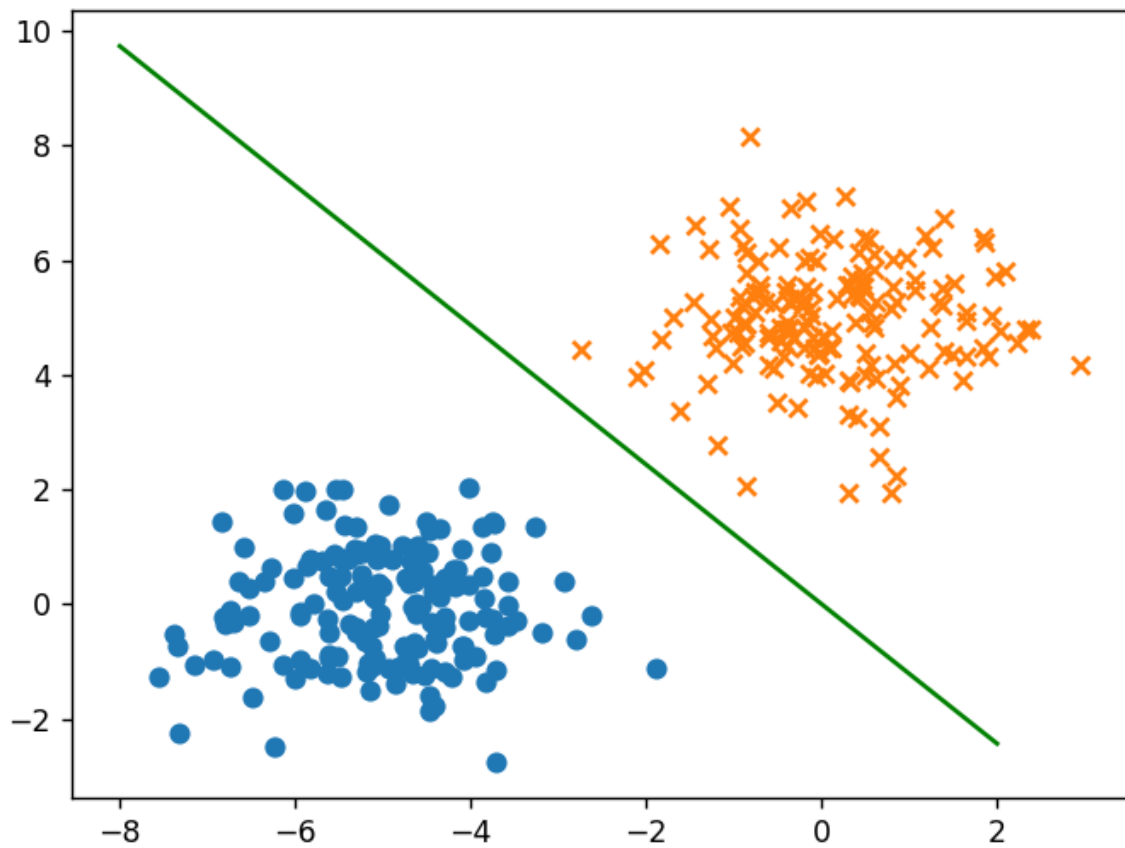
2、PLA:

```
生成数据集: [[-6.38993151 -1.69156339 1.
 [-3.54371144 -0.5830198 1.
 [-4.26765222 -0.69521965 1.
 ...
 [-0.58339504 4.26962143 -1.
 [ 0.26893695 3.86227642 -1.
 [-0.83921265 4.23696374 -1.
 W: [-6.2021366 -4.99212743]
 b: 0.0
 count 2
0.002959012985229492 s
训练集分类准确率: 1.0
测试集分类准确率: 1.0
```



Pocket:

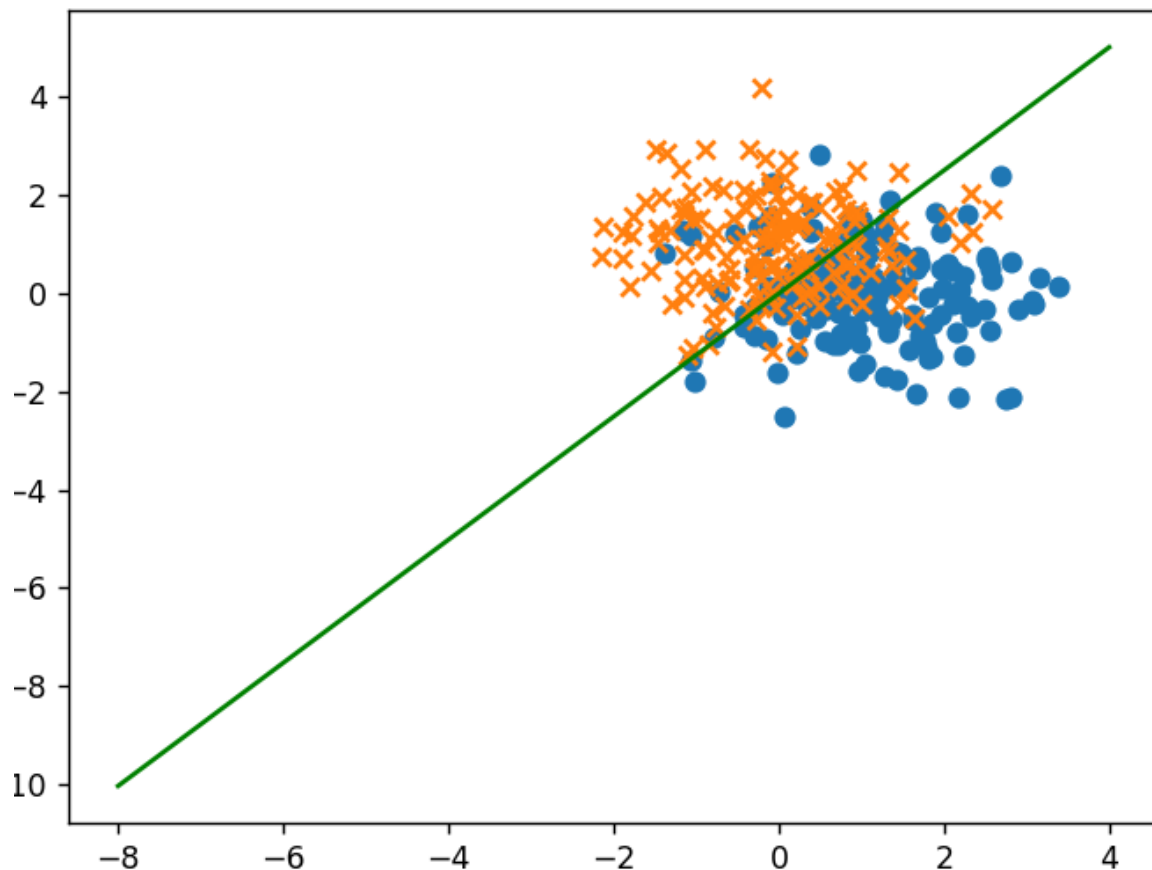
```
生成数据集: [[-5.48511596  0.49605235  1.
 [-4.6405052  0.39200793  1.
 [-5.30438422  0.85997873  1.
 ...
 [ 1.06931431  5.48861631 -1.
 [ 2.06875026  4.6722137  -1.
 [ 0.31130234  1.93929649 -1.
 W: [ 1.41142393 -3.79126822]
 b: -1.0
 0.0059697628021240234 s
 训练集分类准确率: 1.0
 测试集分类准确率: 1.0
```



3、PLA算法无法得出结果

Pocket:

```
生成数据集: [[ 0.68920654  0.28215435  1.
 [ 0.99576377  1.49270854  1.
 [ 1.61096564 -0.55377333  1.
 ...
 [-1.15125378  0.78527363 -1.
 [-0.01157509 -0.64601332 -1.
 [ 0.49904407  1.76670186 -1.
 W: [ 0.90811003 -0.63114889]
 b: 0.0
 0.22539782524108887 s
 训练集分类准确率: 0.775
 测试集分类准确率: 0.7875
```



4、过多增加pocket算法的迭代次数无法提升性能

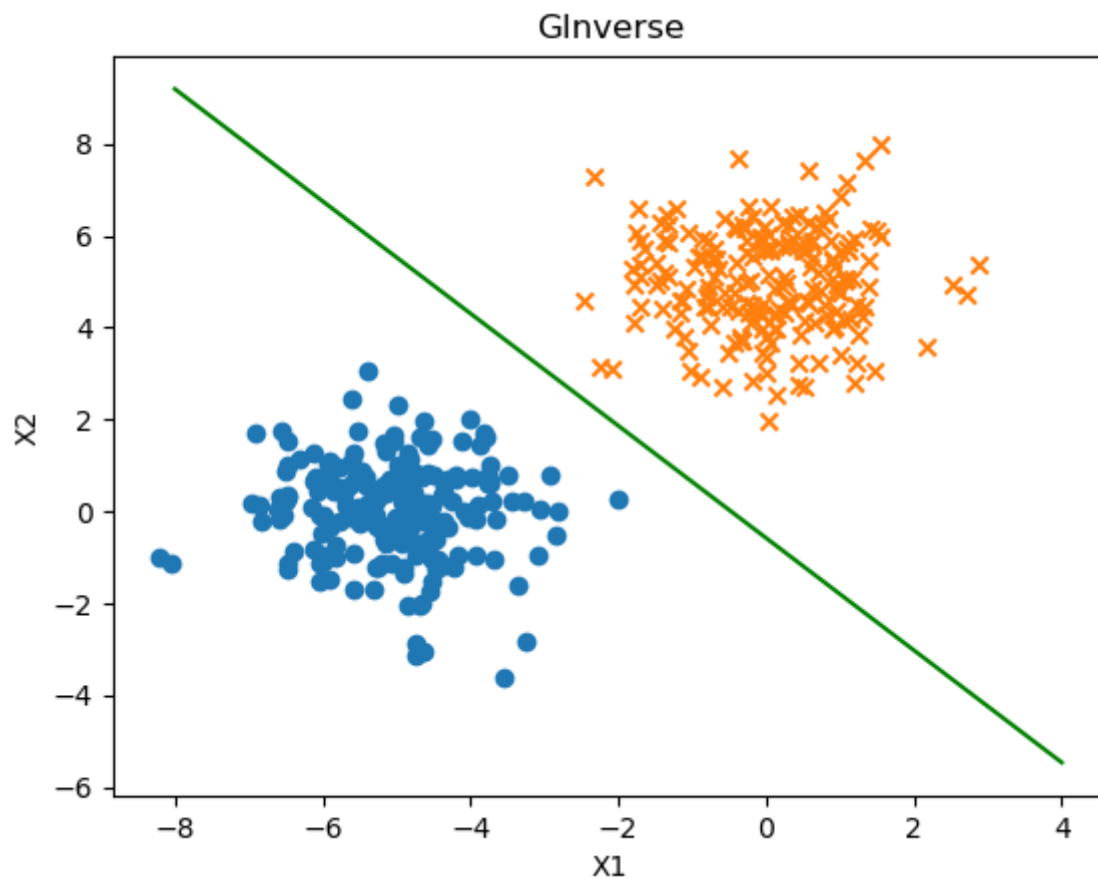
$x_1$ 与 $x_2$ 的均值越分开，同时其协方差越小，其可分性越好

### Lecture3 (线性回归) :

1、见代码文件GradientDescent.py中的函数GInverse()与GD()

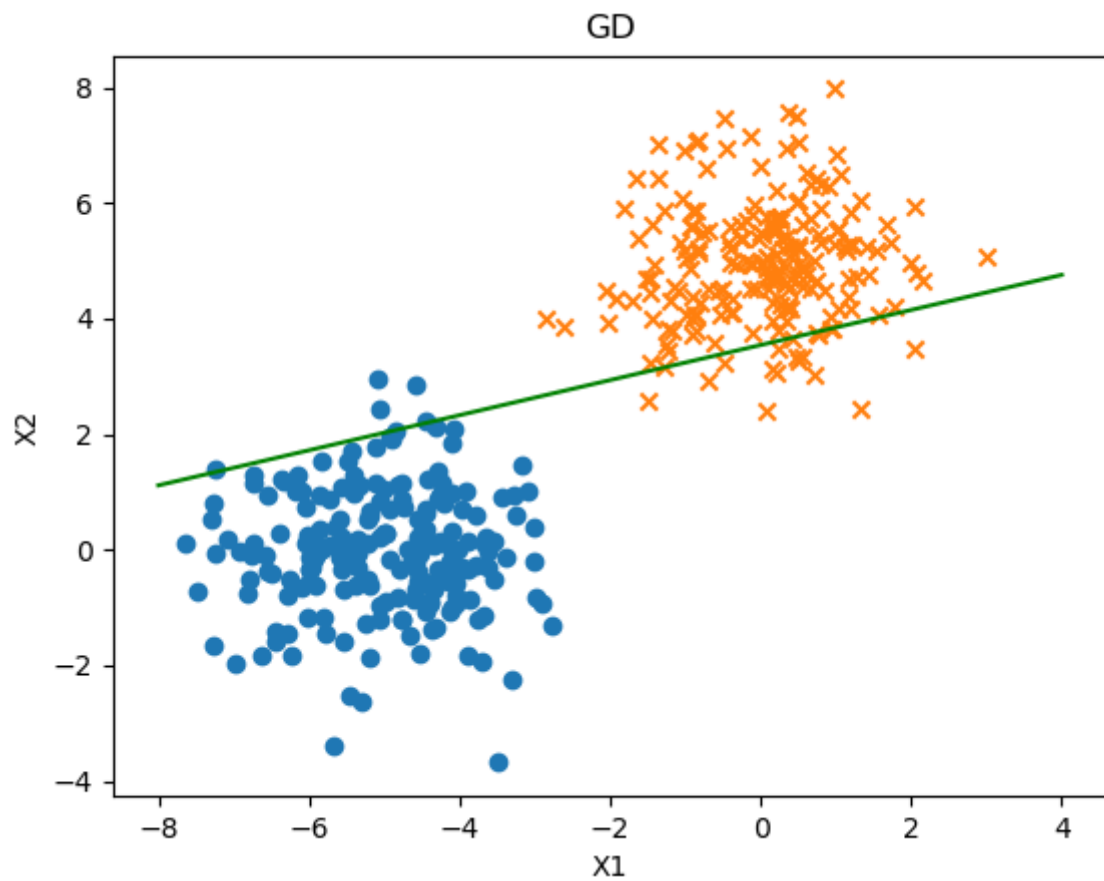
2、广义逆法:

```
生成数据集: [[-6.95675602  0.16948929  1.
 [-5.25301305  0.49213068  1.
 [-3.76502649  0.81173035  1.
 ...
 [ 2.51177111  4.94749949 -1.
 [-0.0268919  5.67736544 -1.
 [ 0.94748708  4.9454531  -1.
 [-0.20277849 -0.16615728 -0.09575341]
耗时: 0.0020301342010498047 s
训练集分类准确率: 1.0
测试集分类准确率: 1.0
```

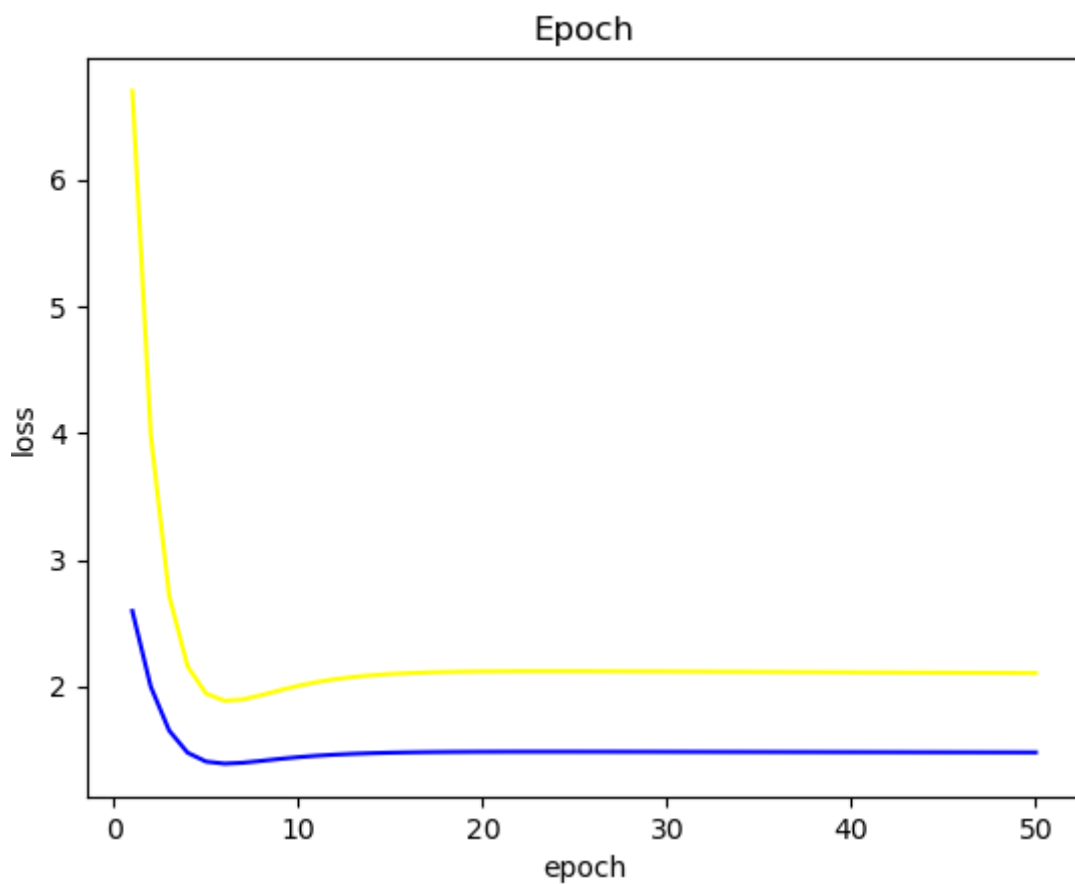


梯度下降法: epoch=50时:

```
W: [ 0.16197141 -0.53337153  1.88999169]
训练集损失函数: 1.487914145613151
测试集损失函数: 1.4839018244978677
耗时: 1.129492998123169 s
训练集分类准确率: 0.940625
测试集分类准确率: 0.9625
```



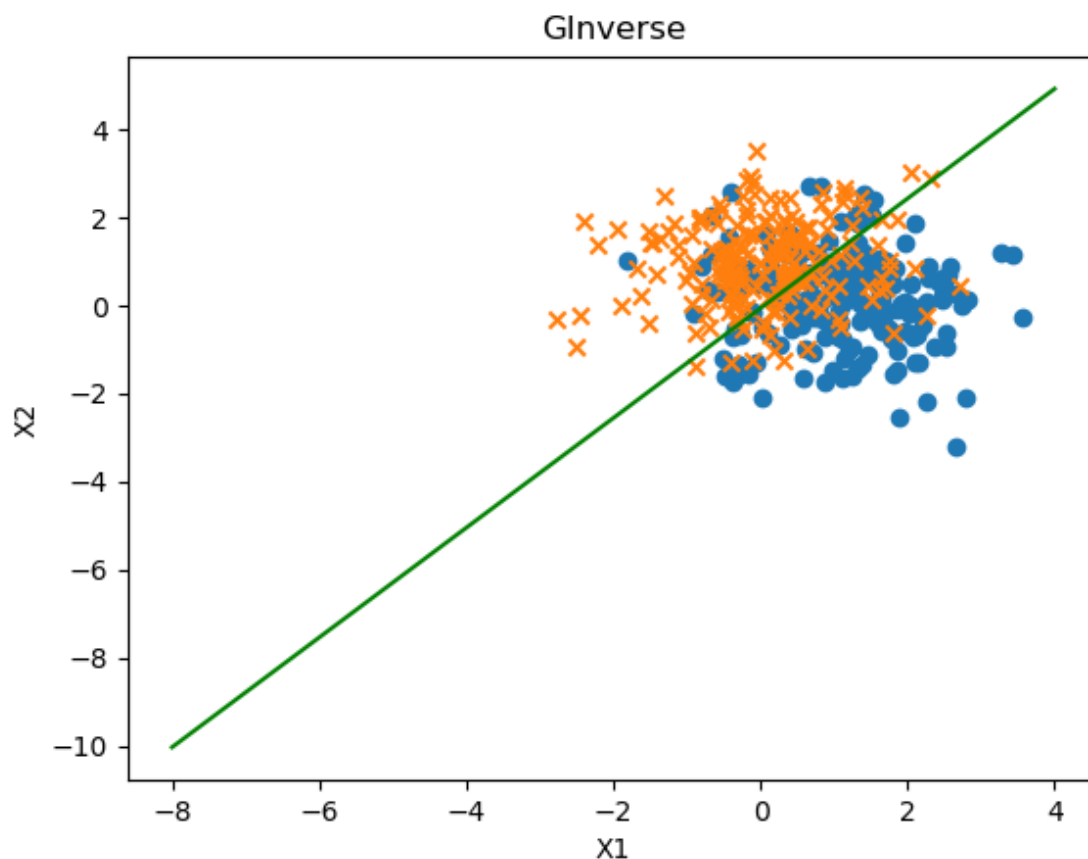
训练集损失与测试集损失随epoch的变化曲线:



  
[image-20231008130558746](C:\Users\DELL\AppData\Roaming\Typora\typora-user-images\image-20231008130558746.png)

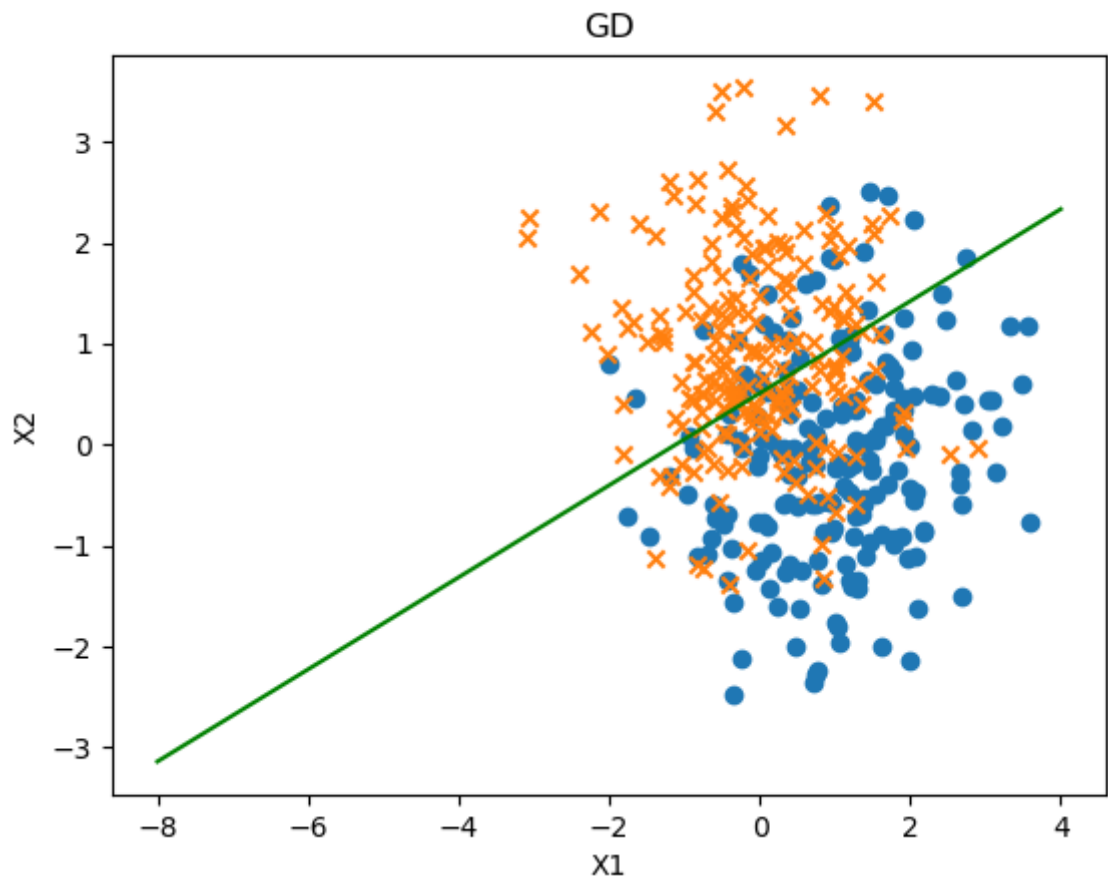
3、广义逆法:

```
生成数据集: [[ 0.70426024 -1.06137361 1.
 [ 1.62252998 0.04296114 1.
 [ 2.80836003 0.12391411 1.
 ...
 [-0.52842288 1.23118205 -1.
 [ 0.37686012 0.21420823 -1.
 [-1.6913932 0.85207638 -1.
 [ 0.37733183 -0.30260107 -0.01837985]
耗时: 0.002002716064453125 s
训练集分类准确率: 0.76875
测试集分类准确率: 0.75
```



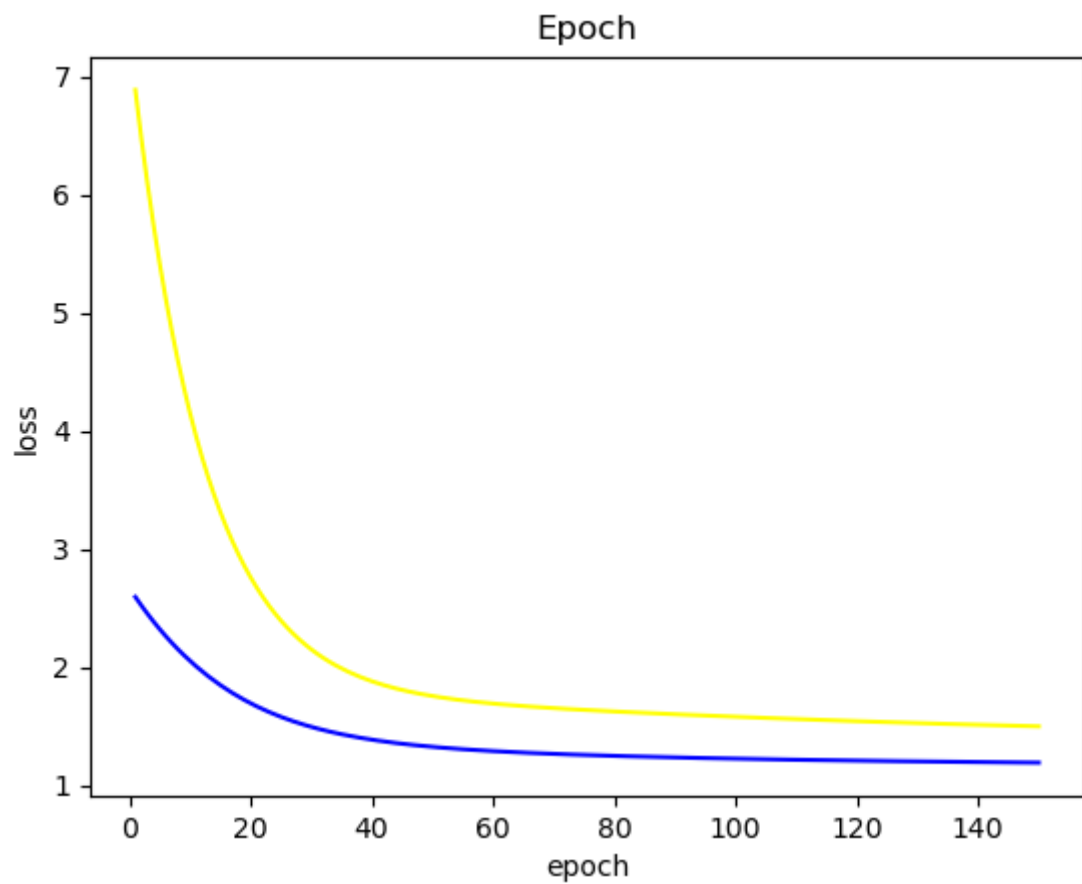
梯度下降法(epoch=150):

```
W: [ 0.20805413 -0.45635146 0.23216762]
训练集损失函数: 1.1819619336373846
测试集损失函数: 1.1432849368471796
耗时: 10.597349405288696 s
训练集分类准确率: 0.7375
测试集分类准确率: 0.7625
```



训练集损失与测试集损失随epoch的变化曲线: ![image-20231003022247548](#)]

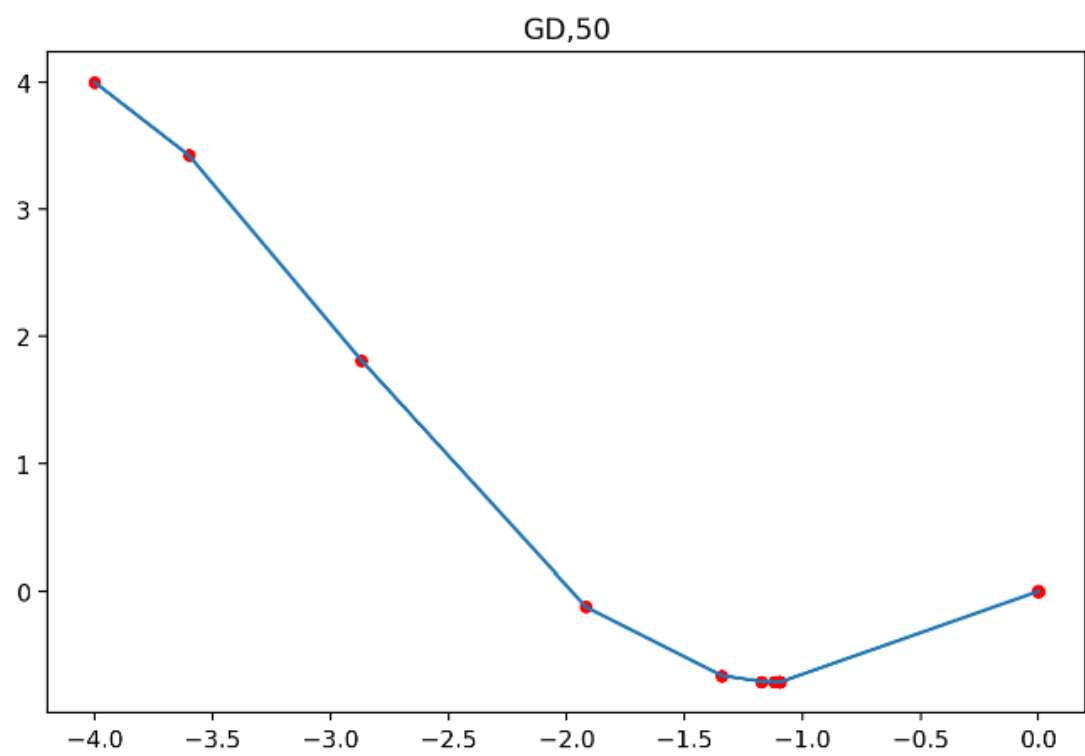
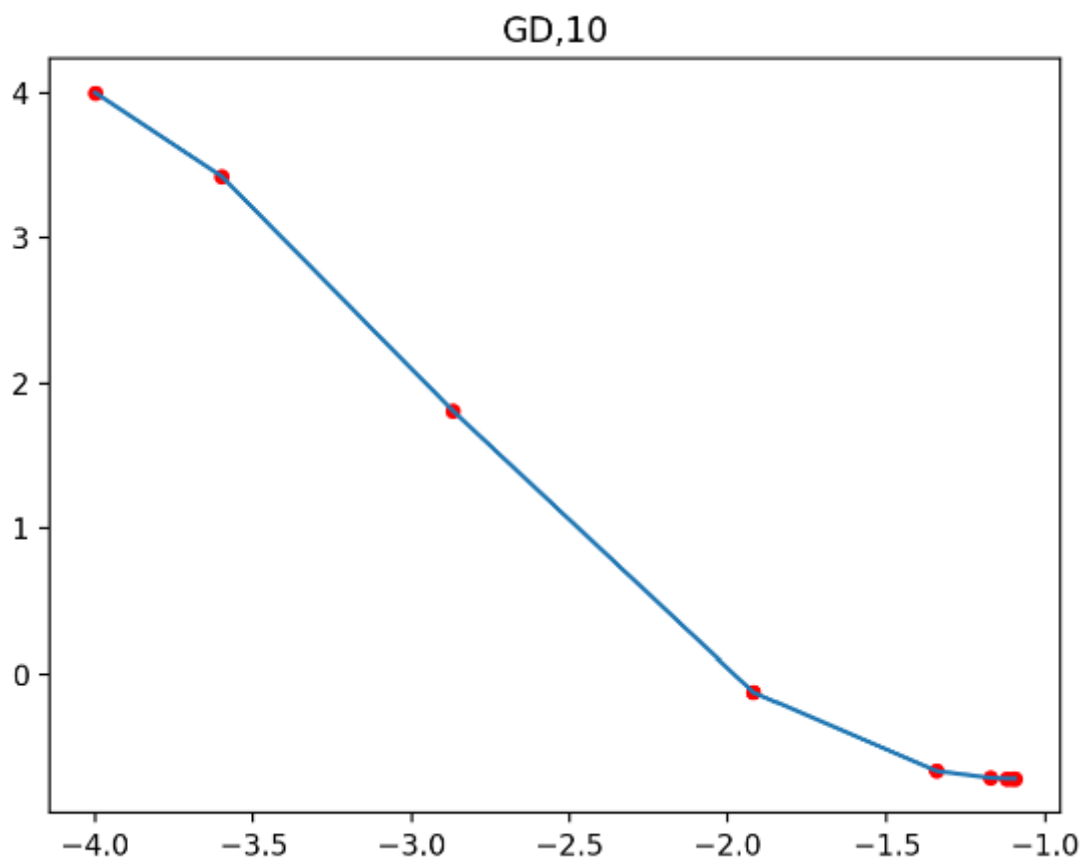
(C:\Users\DELL\AppData\Roaming\Typora\typora-user-images\image-20231003022247548.png



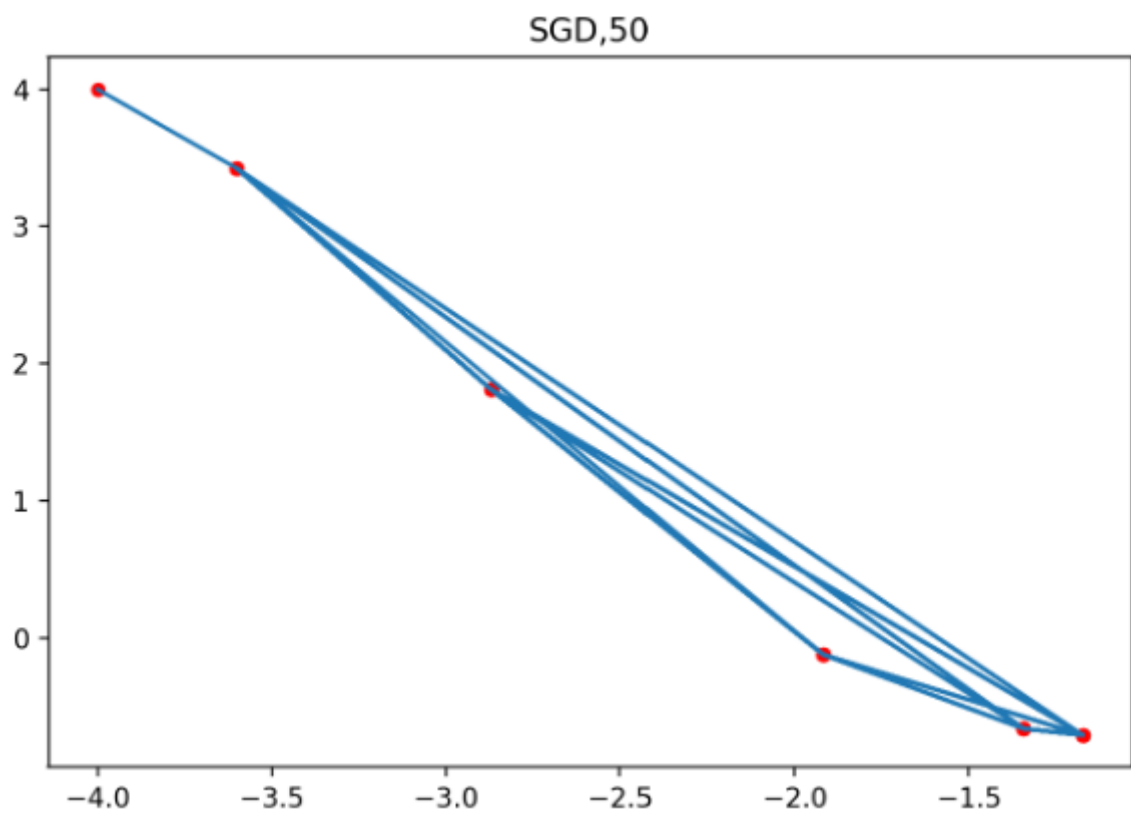
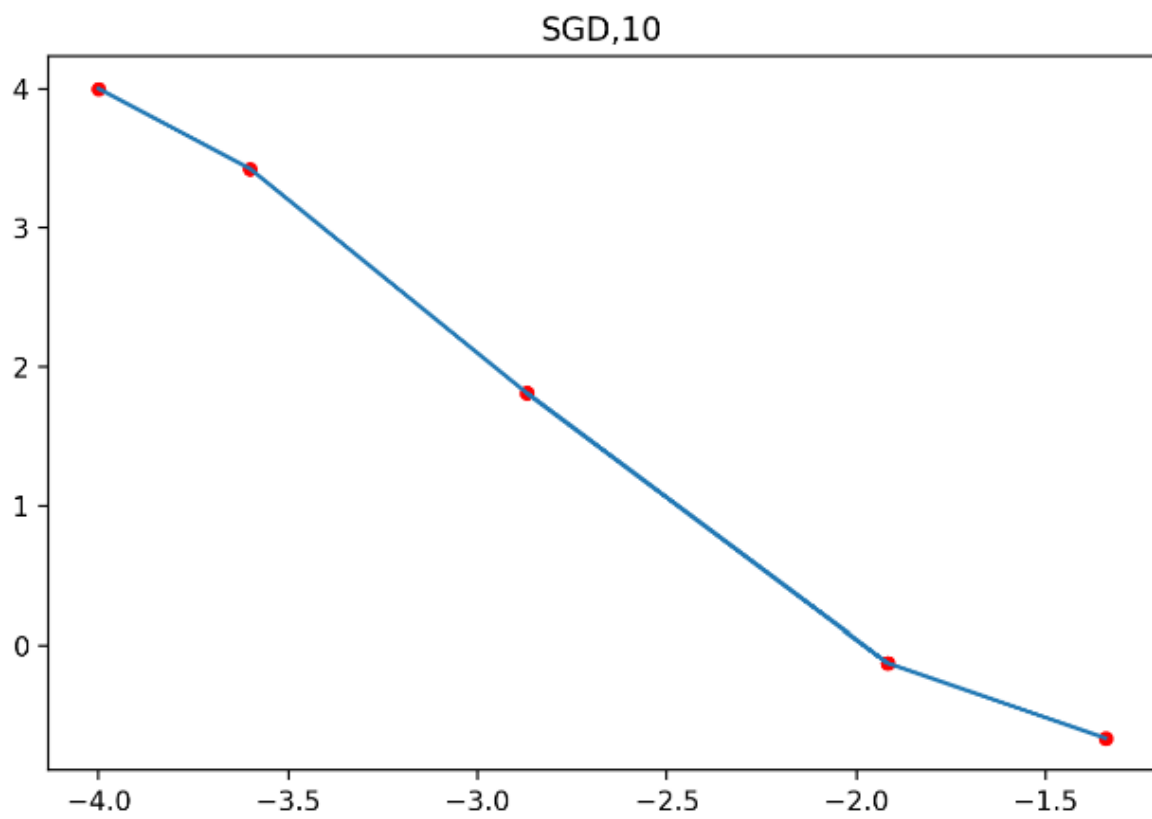
5、不同算法的变化结果：

梯度下降法：

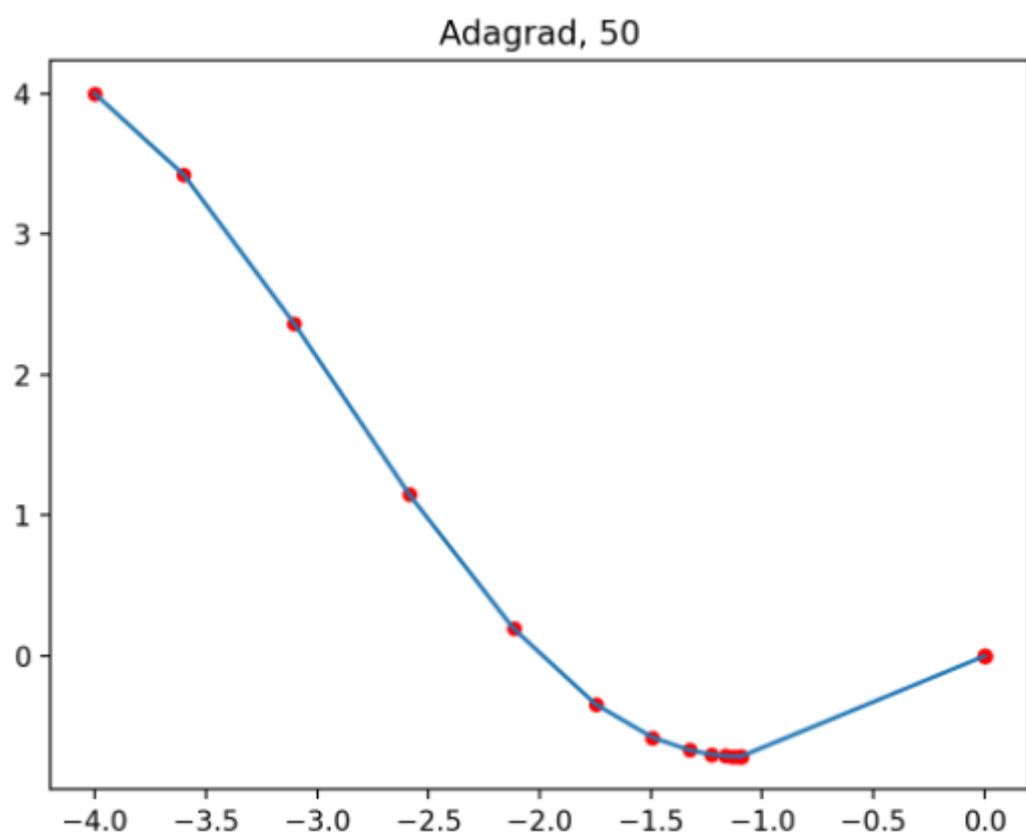
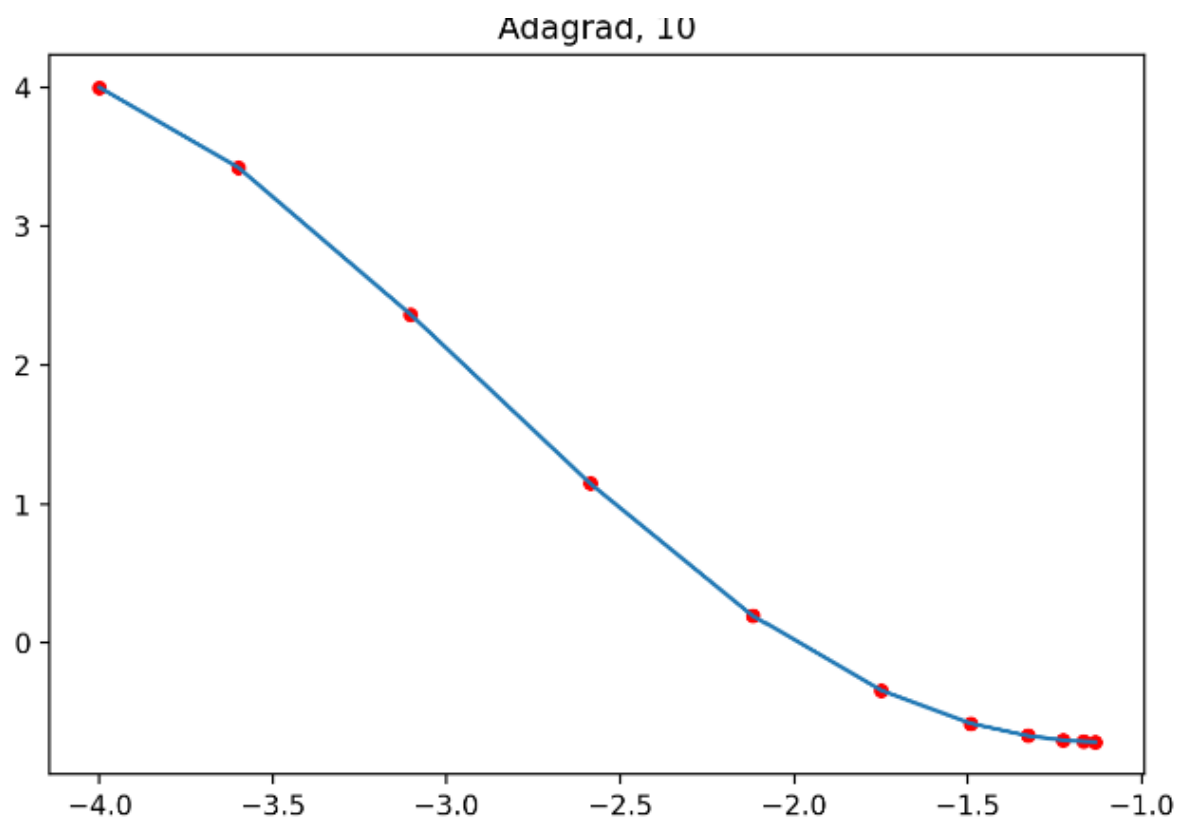




随机梯度下降法:

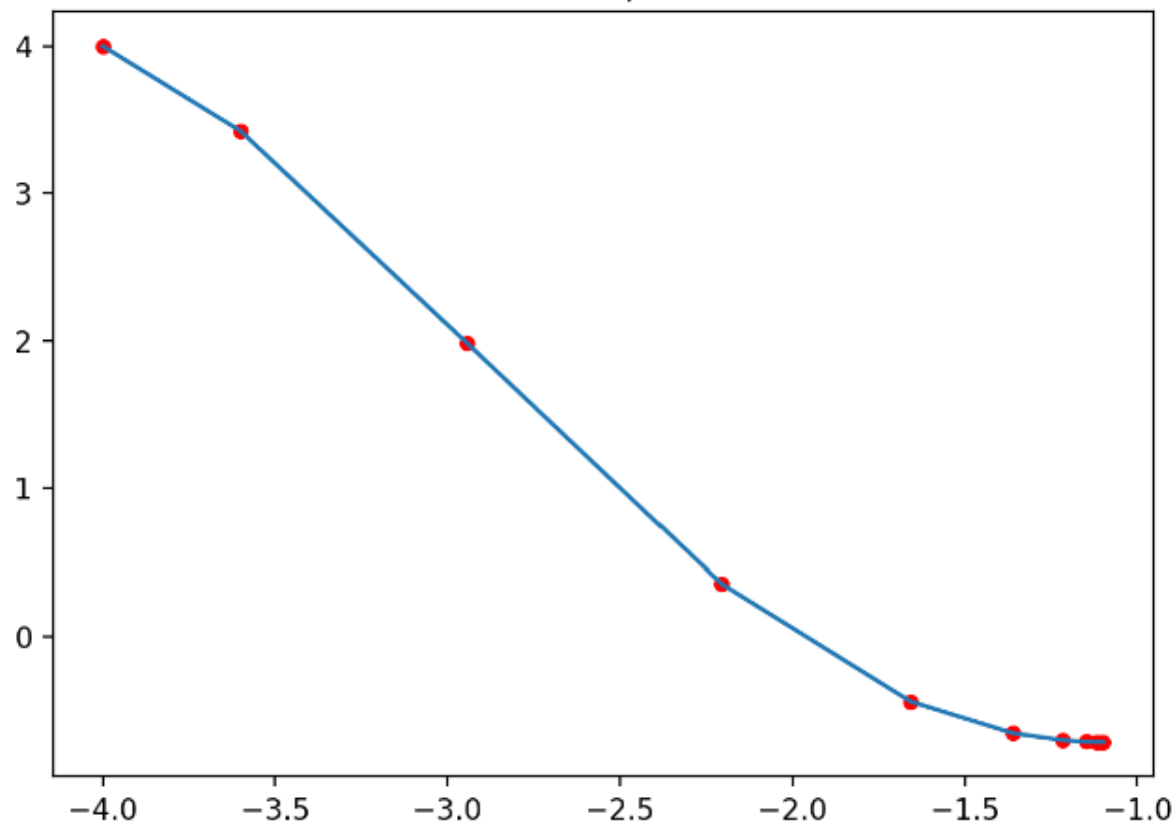


Adagrad:

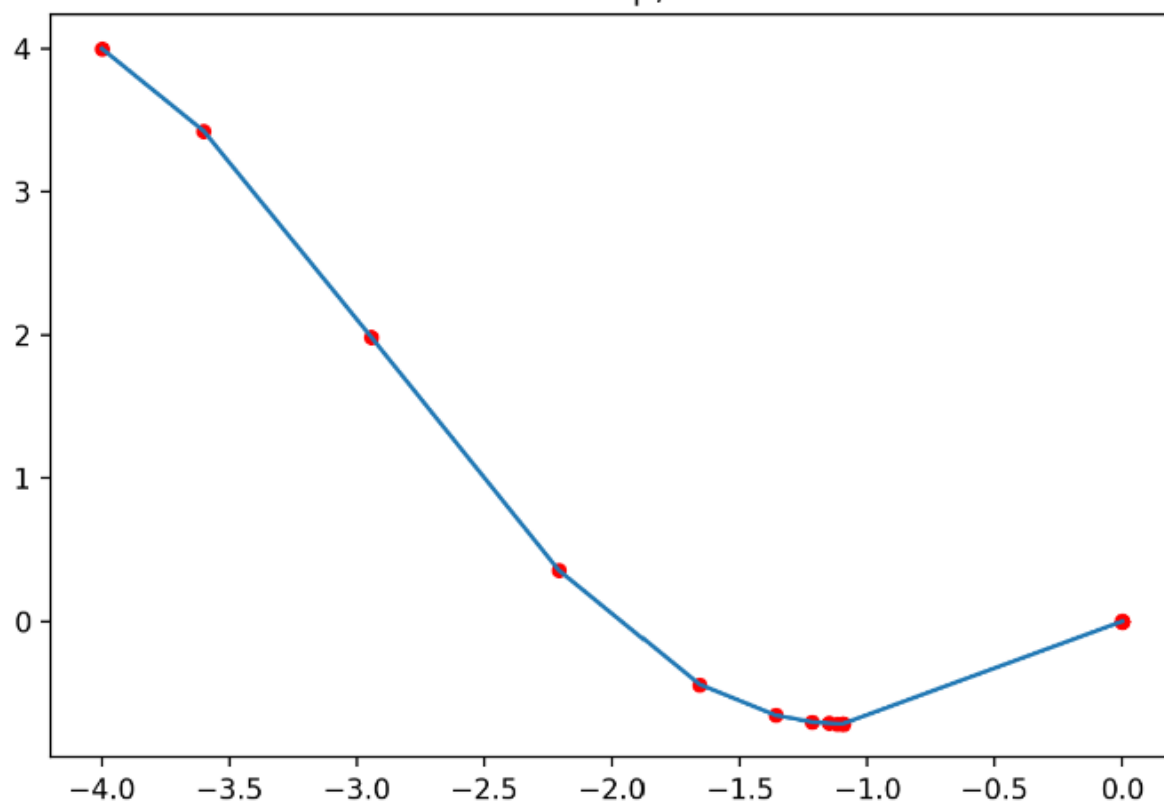


RMSProp:

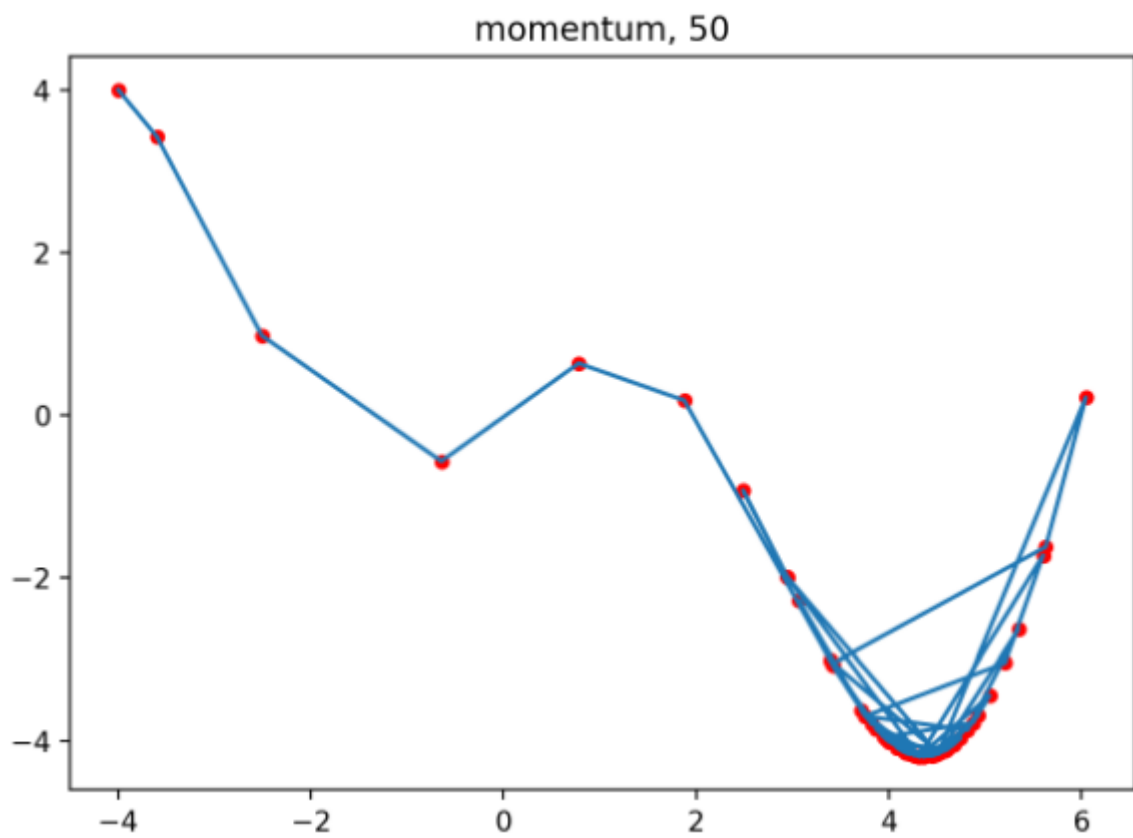
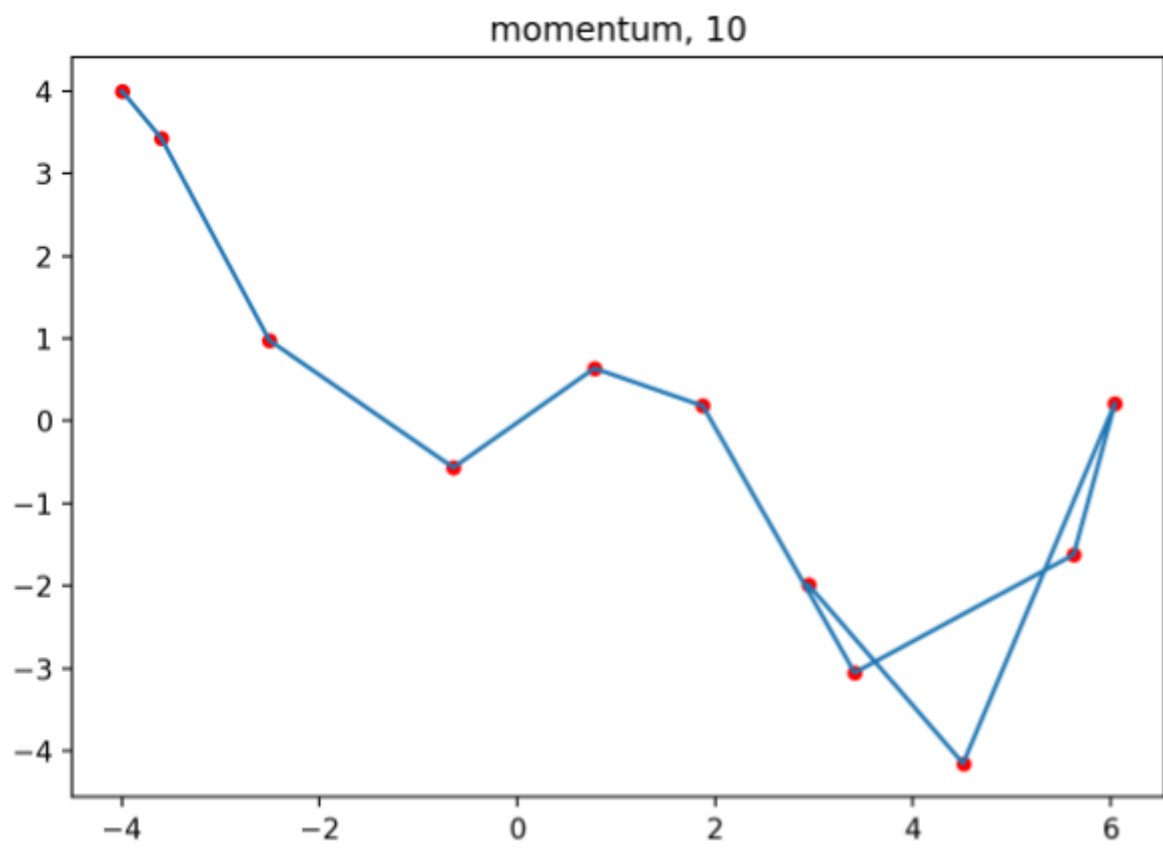
RMSProp, 10



RMSProp, 50

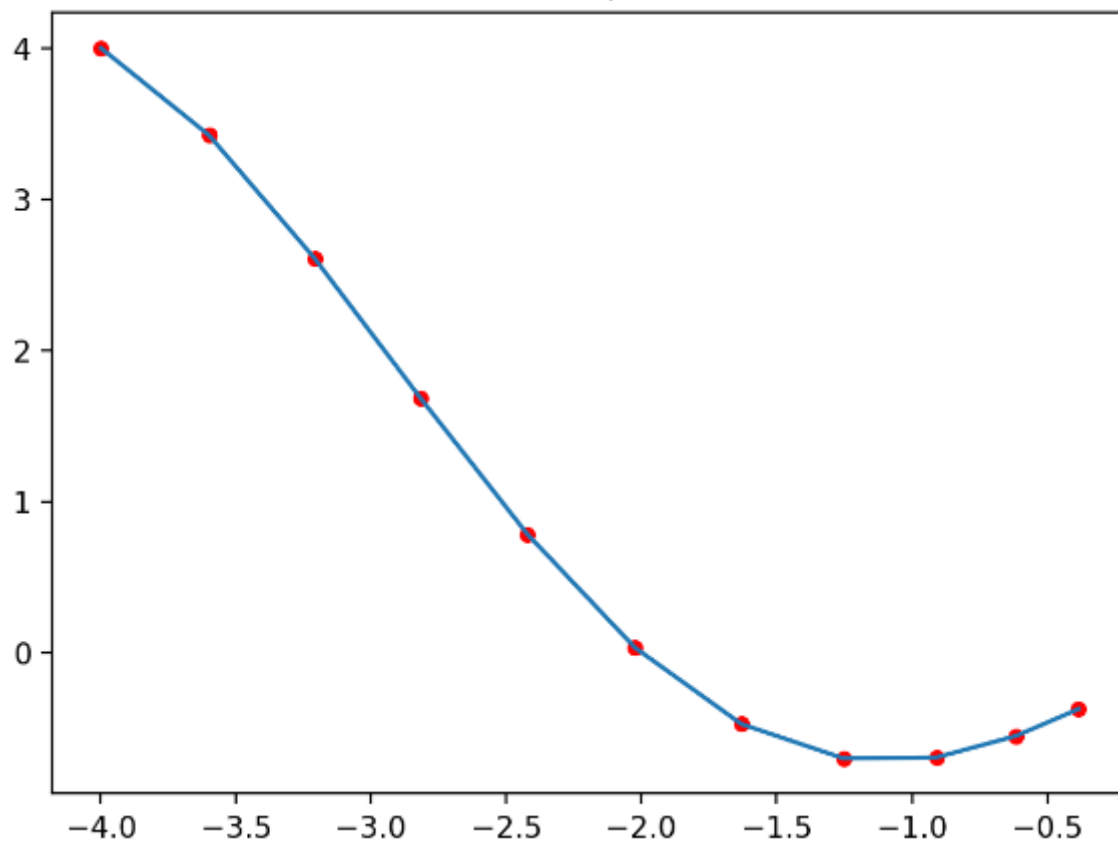


动量法 (Momentum) :

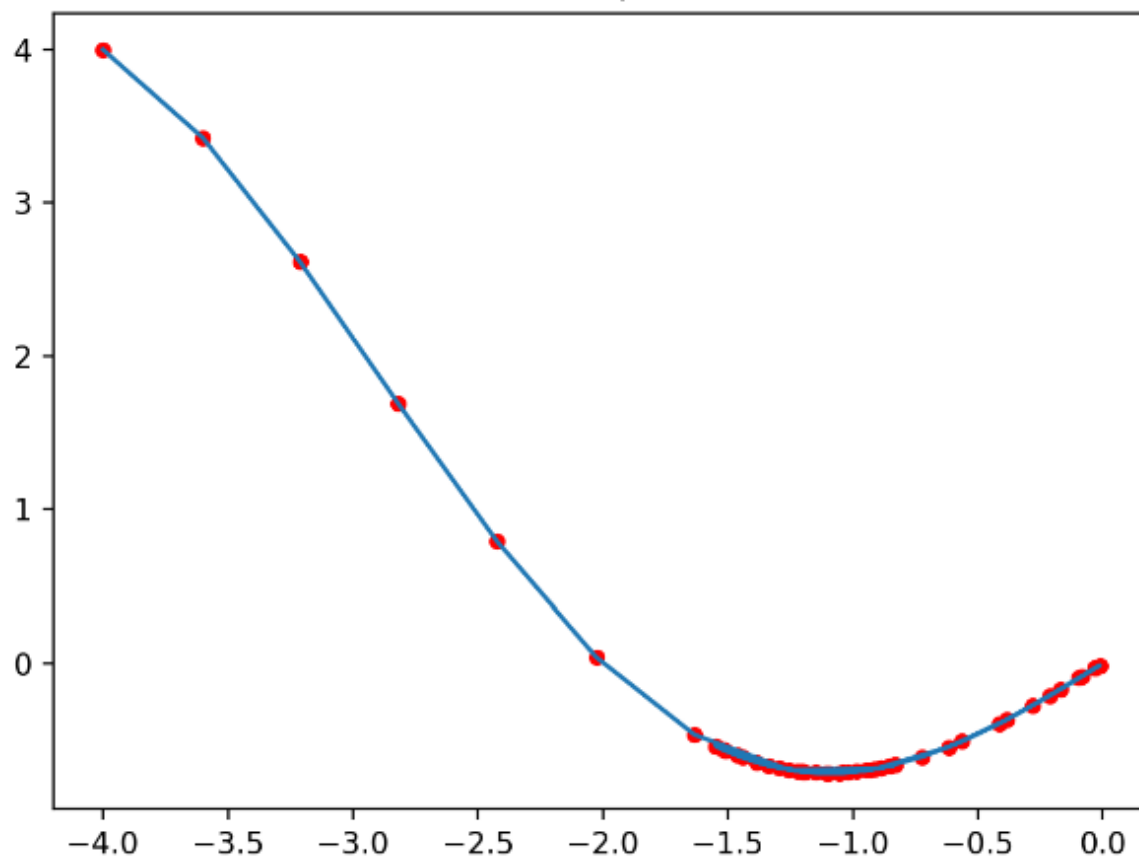


Adam:

Adam, 10



Adam, 50

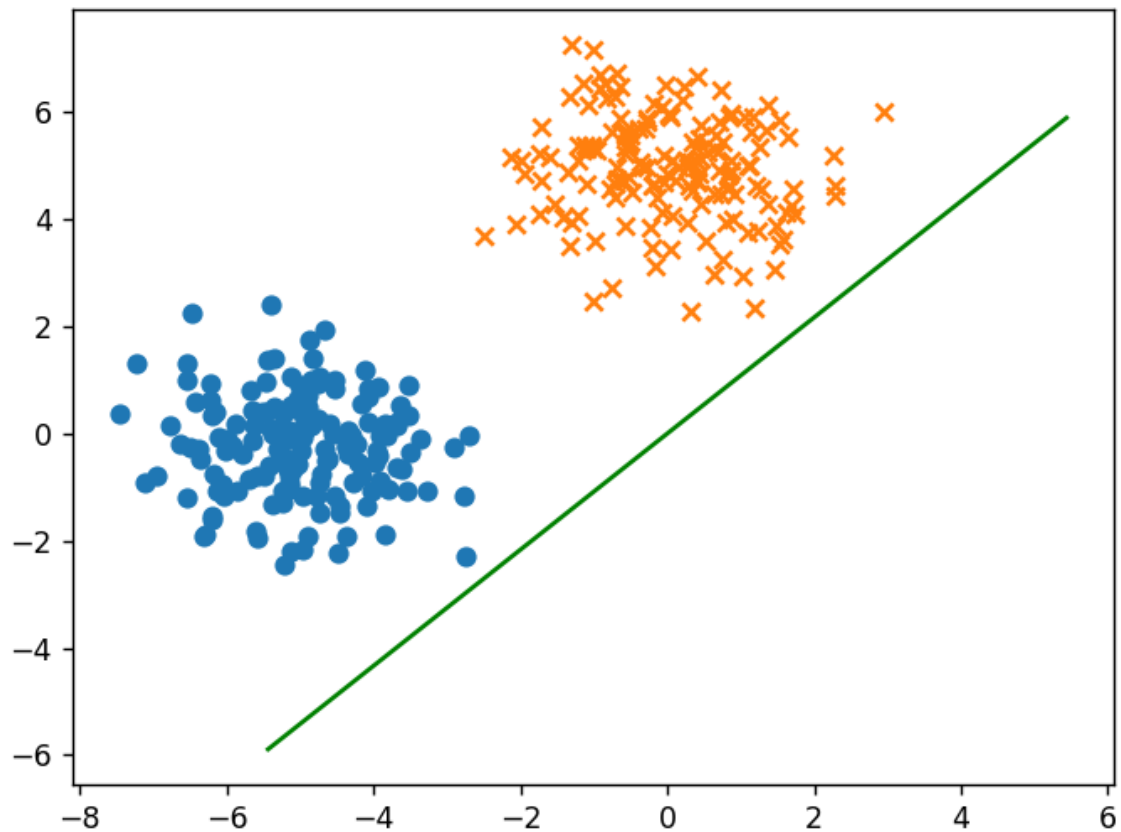


## Lecture4-1 (Fisher线性判别) :

1、见代码文件Fisher.py中的函数fisher()与predict()

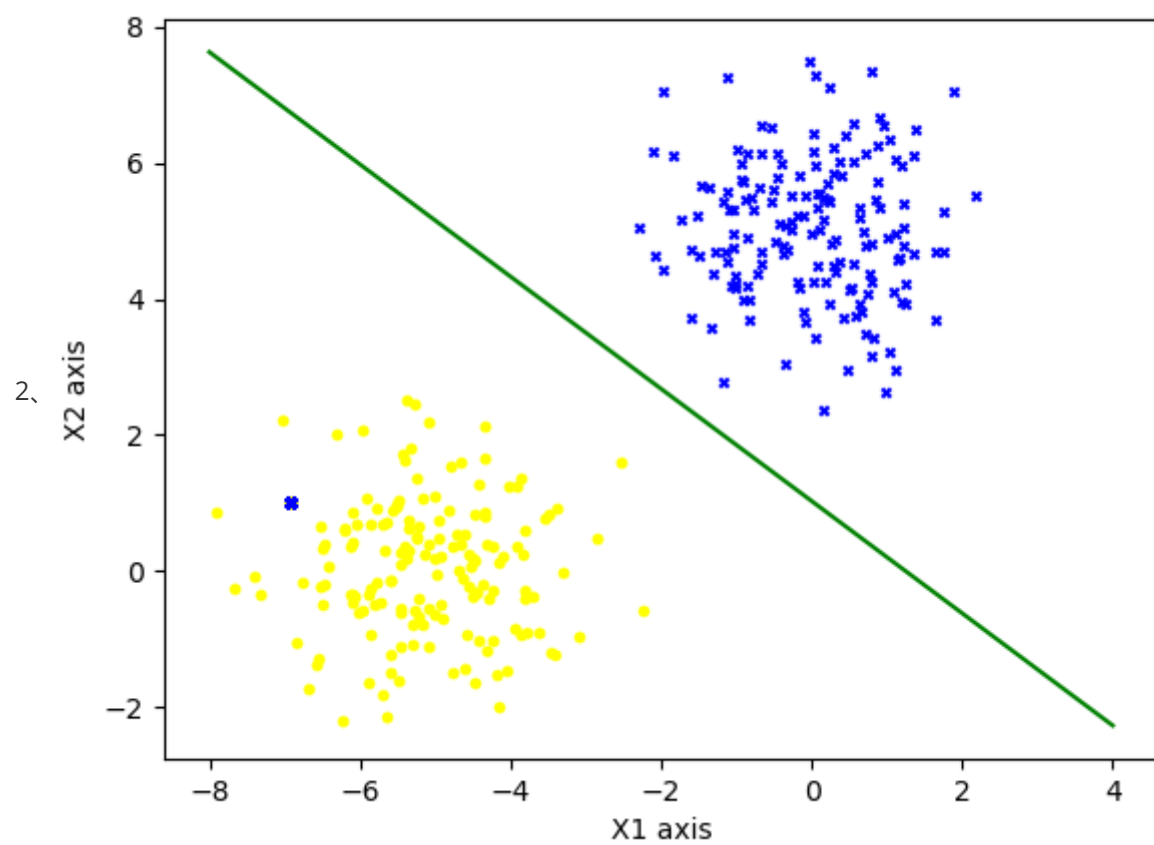
2、

```
生成数据集: [[-6.55299706  0.99846154  1.
 [-5.13744008 -1.04008932  1.
 [-6.17953585 -0.75385586  1.
 ...
 [-1.99574922  5.10808674 -1.
 [-0.56924375  3.89041239 -1.
 [ 1.13969594  5.64476592 -1.
类型:  <class 'numpy.ndarray'>
最佳投影向量: [-0.01812006 -0.01964221]
分类阈值: -0.0014052345016553475
在训练集上的分类准确率为: 1.0
在测试集上的分类准确率为: 1.0
```



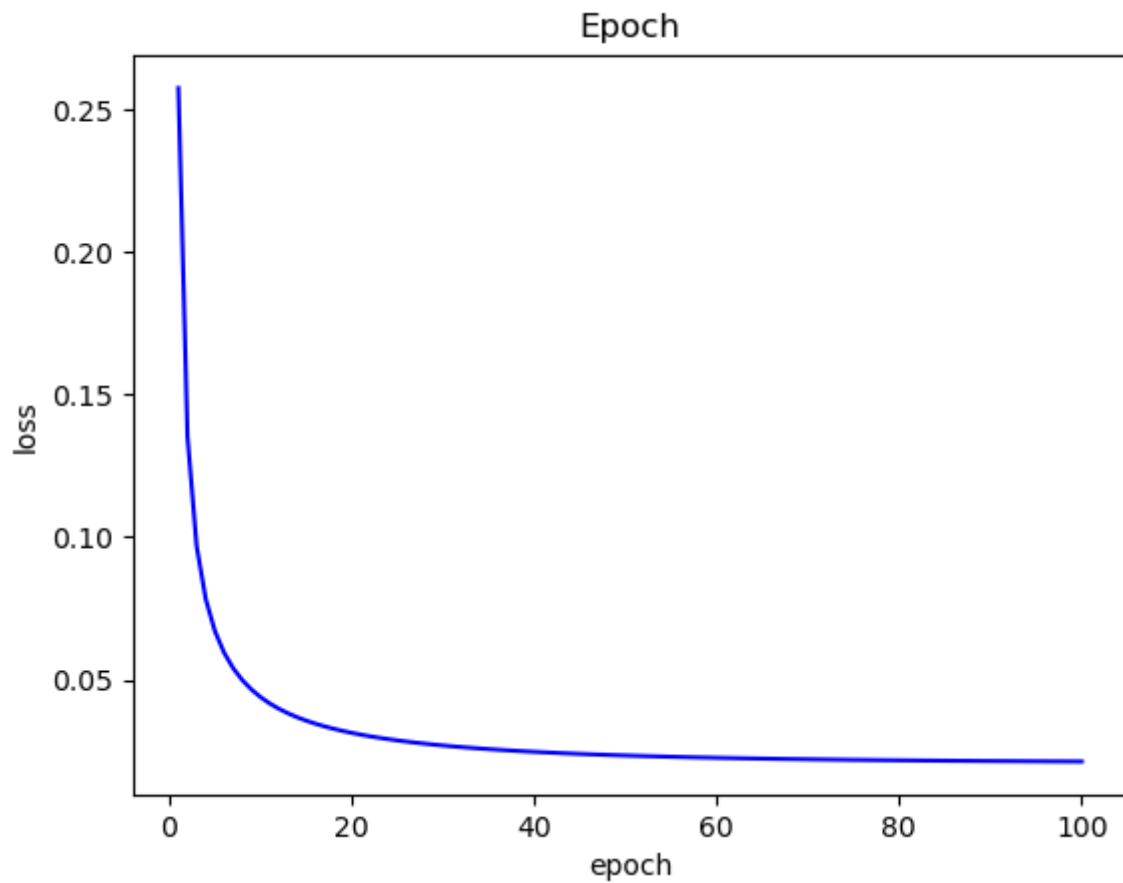
## Lecture4-2 (逻辑斯蒂回归) :

1、见代码文件Logistic.py内的函数SGD。





数据点: -5.082438797608212 0.8334802825538884 真实类别: [1.] 计算类别: 1 概率值: 0.9818114951794473  
数据点: -5.772598958776367 0.9458639135274352 真实类别: [1.] 计算类别: 1 概率值: 0.9879196908606043  
数据点: -4.257023999337464 0.7755354896695198 真实类别: [1.] 计算类别: 1 概率值: 0.9683941179802275  
数据点: -4.980955645009449 0.6037761133675454 真实类别: [1.] 计算类别: 1 概率值: 0.9840348885177581  
数据点: -4.635614419537781 -1.3892300205411732 真实类别: [1.] 计算类别: 1 概率值: 0.9965758217447358  
数据点: -5.147365034248389 1.2594196946057206 真实类别: [1.] 计算类别: 1 概率值: 0.9746726745519639  
数据点: -4.972331827619395 0.21331119992917202 真实类别: [1.] 计算类别: 1 概率值: 0.9886781007032581  
数据点: -3.9994636110749804 1.1684312964756562 真实类别: [1.] 计算类别: 1 概率值: 0.9464500325745031  
数据点: -4.041931813733918 -1.5072532462904535 真实类别: [1.] 计算类别: 1 概率值: 0.9952056985530027  
数据点: -4.010596878491258 -0.1314652790900866 真实类别: [1.] 计算类别: 1 概率值: 0.9830726756585872  
数据点: -4.857167670013449 2.4064597628486646 真实类别: [1.] 计算类别: 1 概率值: 0.9160777009890345  
数据点: -4.516803399352791 -0.8700105164065465 真实类别: [1.] 计算类别: 1 概率值: 0.9940151377028733  
数据点: -7.289197522640739 0.5866740767239247 真实类别: [1.] 计算类别: 1 概率值: 0.9971786917199906  
数据点: -5.133941318783918 -1.8031644605371908 真实类别: [1.] 计算类别: 1 概率值: 0.998379380227356  
数据点: -4.9523068344412815 -0.08265155009505408 真实类别: [1.] 计算类别: 1 概率值: 0.9911948498835613  
数据点: -4.174800435402759 0.8284691827769635 真实类别: [1.] 计算类别: 1 概率值: 0.9648562646275112  
数据点: -5.742562488341206 1.3989518545688144 真实类别: [1.] 计算类别: 1 概率值: 0.9814716198233385  
数据点: -2.004842103595118 -0.253377893057851 真实类别: [1.] 计算类别: 1 概率值: 0.9351387561177097  
数据点: -4.406331497057808 -0.40269302412634433 真实类别: [1.] 计算类别: 1 概率值: 0.9900972898414141  
数据点: -4.327822984405973 1.5504172561995564 真实类别: [1.] 计算类别: 1 概率值: 0.9410995989235603  
数据点: -3.519028179373069 1.0975889471287252 真实类别: [1.] 计算类别: 1 概率值: 0.929314546733761  
数据点: -3.134739493168724 -1.0004530330655164 真实类别: [1.] 计算类别: 1 概率值: 0.9851480721920968  
数据点: -7.483330228335294 1.2574782002172955 真实类别: [1.] 计算类别: 1 概率值: 0.995520274252808  
数据点: -5.535501279096166 -0.5707433716517446 真实类别: [1.] 计算类别: 1 概率值: 0.9963321263135214  
数据点: -4.73236581912802 0.6249539386059606 真实类别: [1.] 计算类别: 1 概率值: 0.9804606923707542  
数据点: -6.338440734985751 0.3963170410211942 真实类别: [1.] 计算类别: 1 概率值: 0.9951684970603293  
数据点: -5.544124846877673 -0.457524785778184 真实类别: [1.] 计算类别: 1 概率值: 0.9959623477480174  
数据点: -5.702037726897173 -0.3398048889681044 真实类别: [1.] 计算类别: 1 概率值: 0.9960080828936145  
数据点: -3.709779246197387 1.3722905632051088 真实类别: [1.] 计算类别: 1 概率值: 0.9219837594358352  
数据点: -4.5843138771335195 0.34919262472729323 真实类别: [1.] 计算类别: 1 概率值: 0.9829628314889282  
数据点: -5.7346335714216075 0.6578734081354721 真实类别: [1.] 计算类别: 1 概率值: 0.9904087902399246  
数据点: -6.0832688430780975 1.6597287024543563 真实类别: [1.] 计算类别: 1 概率值: 0.9818052025527166  
数据点: -4.6654040896117825 0.6009756129758765 真实类别: [1.] 计算类别: 1 概率值: 0.9799086696208604  
数据点: -6.1217996635877014 -0.49084471663214047 真实类别: [1.] 计算类别: 1 概率值: 0.9974561253065534  
数据点: -6.369360595711045 -1.937088810900264 真实类别: [1.] 计算类别: 1 概率值: 0.9994312277789209  
数据点: -4.082991962245137 -0.3868008963295351 真实类别: [1.] 计算类别: 1 概率值: 0.9872335096116719  
数据点: -3.705846742289825 -0.8541850637201754 真实类别: [1.] 计算类别: 1 概率值: 0.9889039454668889  
数据点: -4.985484841696257 -0.7232110602786869 真实类别: [1.] 计算类别: 1 概率值: 0.9951820307573562  
数据点: -0.42984840078648745 4.314563206461582 真实类别: [0.] 计算类别: 0 概率值: 0.9733664697807481  
数据点: -0.08786545755948205 5.094055218740585 真实类别: [0.] 计算类别: 0 概率值: 0.9896812061695637  
数据点: 1.1232138797334772 5.255950377726406 真实类别: [0.] 计算类别: 0 概率值: 0.9963838386312939  
数据点: 0.5187954422063538 6.373511255929149 真实类别: [0.] 计算类别: 0 概率值: 0.9979360603947655  
数据点: 0.5030652846302315 3.0457443380525206 真实类别: [0.] 计算类别: 0 概率值: 0.9587157812644288  
数据点: 1.9299682443481663 5.542364688732313 真实类别: [0.] 计算类别: 0 概率值: 0.9984746147963821  
数据点: -0.7049643625664485 4.924606620199083 真实类别: [0.] 计算类别: 0 概率值: 0.9810472081643058  
数据点: -1.1115861110129486 5.2164112374995435 真实类别: [0.] 计算类别: 0 概率值: 0.980293995926454  
数据点: -0.048739481389295396 4.29343041507631 真实类别: [0.] 计算类别: 0 概率值: 0.9794710266051431  
数据点: -0.2941960466828457 5.751183744401182 真实类别: [0.] 计算类别: 0 概率值: 0.9933460379040839  
数据点: -1.198257259215314 5.933998853051266 真实类别: [0.] 计算类别: 0 概率值: 0.9889482649792446  
数据点: 0.06811324897171993 4.323938161941664 真实类别: [0.] 计算类别: 0 概率值: 0.9816665920477476  
数据点: 0.1776216075069517 5.156199818825839 真实类别: [0.] 计算类别: 0 概率值: 0.9919896445160095  
数据点: -1.5527709663507738 4.286521813161135 真实类别: [0.] 计算类别: 0 概率值: 0.9388333591293296  
数据点: -1.7099291137725479 5.450982776551628 真实类别: [0.] 计算类别: 0 概率值: 0.9751905260086414  
数据点: -0.6153105796061 5.872731376076321 真实类别: [0.] 计算类别: 0 概率值: 0.9924266965128594  
数据点: 0.8238882470822332 5.7897149291571175 真实类别: [0.] 计算类别: 0 概率值: 0.9972111267291643



## Lecture5 (支撑向量机) :

1、见代码文件SVM.py中的函数Dual\_SVM、Kernel\_SVM

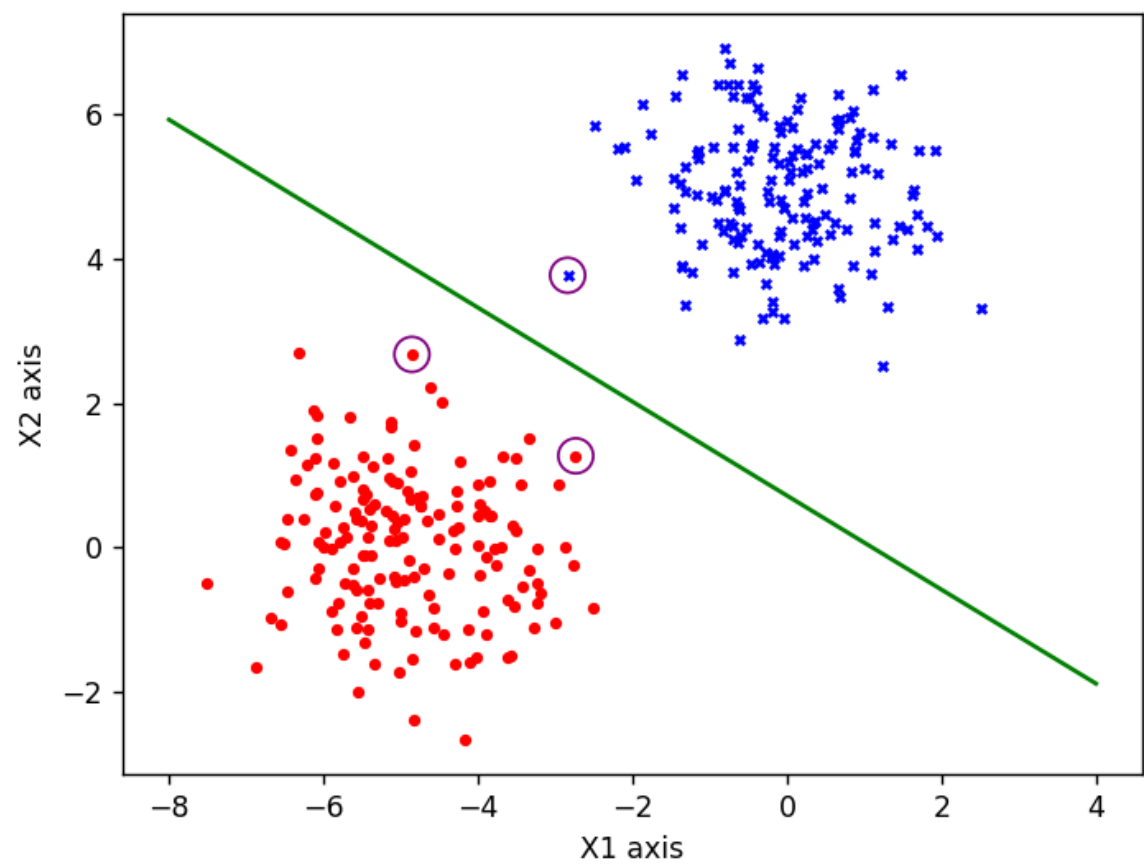
2、数据生成见代码文件SVM.py中的函数DATA

均值向量为(-5,0)(0,5)时:

生成数据集:

```
生成数据集: [[ -5.75633488  0.2780014  1.          ]
 [ -5.5780553   0.39399782  1.          ]
 [ -5.05860219 -0.46664276  1.          ]
 ...
 [ 0.05880747  5.83408442 -1.          ]
 [ 2.05597182  5.13623444 -1.          ]
 [ 0.38309998  4.25561865 -1.          ]]
```

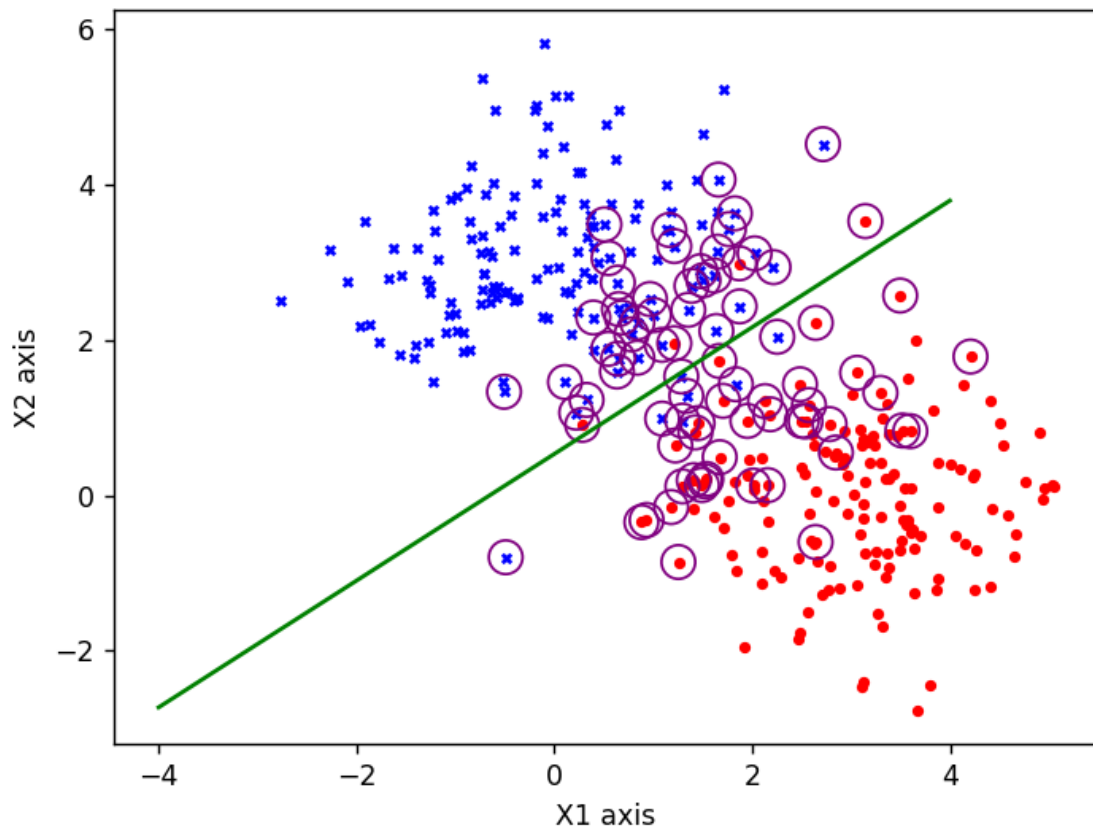
图示：



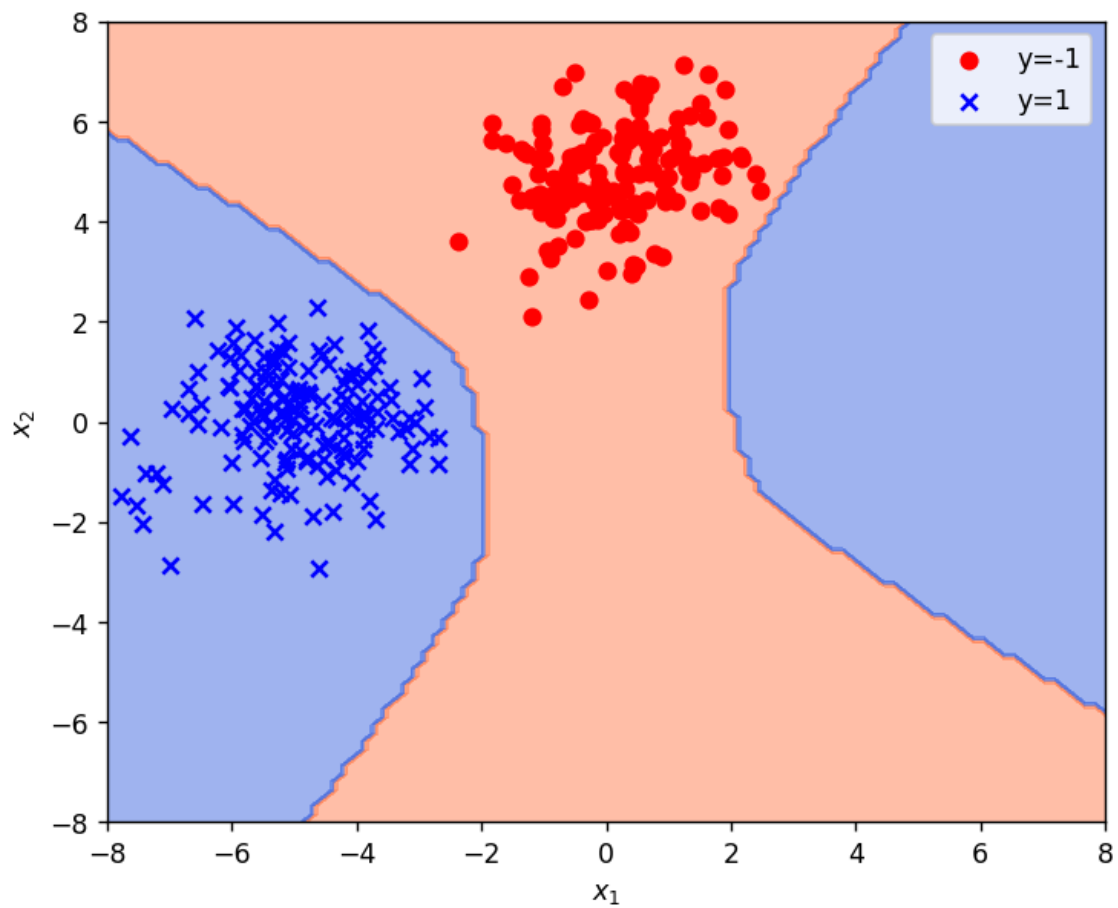
均值向量为(3,0)(0,3)时：

```
生成数据集：[[ -1.56934444  1.12805754  1.
[ -3.74885618 -0.24597254  1.
[ -3.64893547  0.08641762  1.
...
[ -0.58315937  4.13975806 -1.
[ -0.08931694  3.16266402 -1.
[  0.79695897  3.00932367 -1.]]]
```

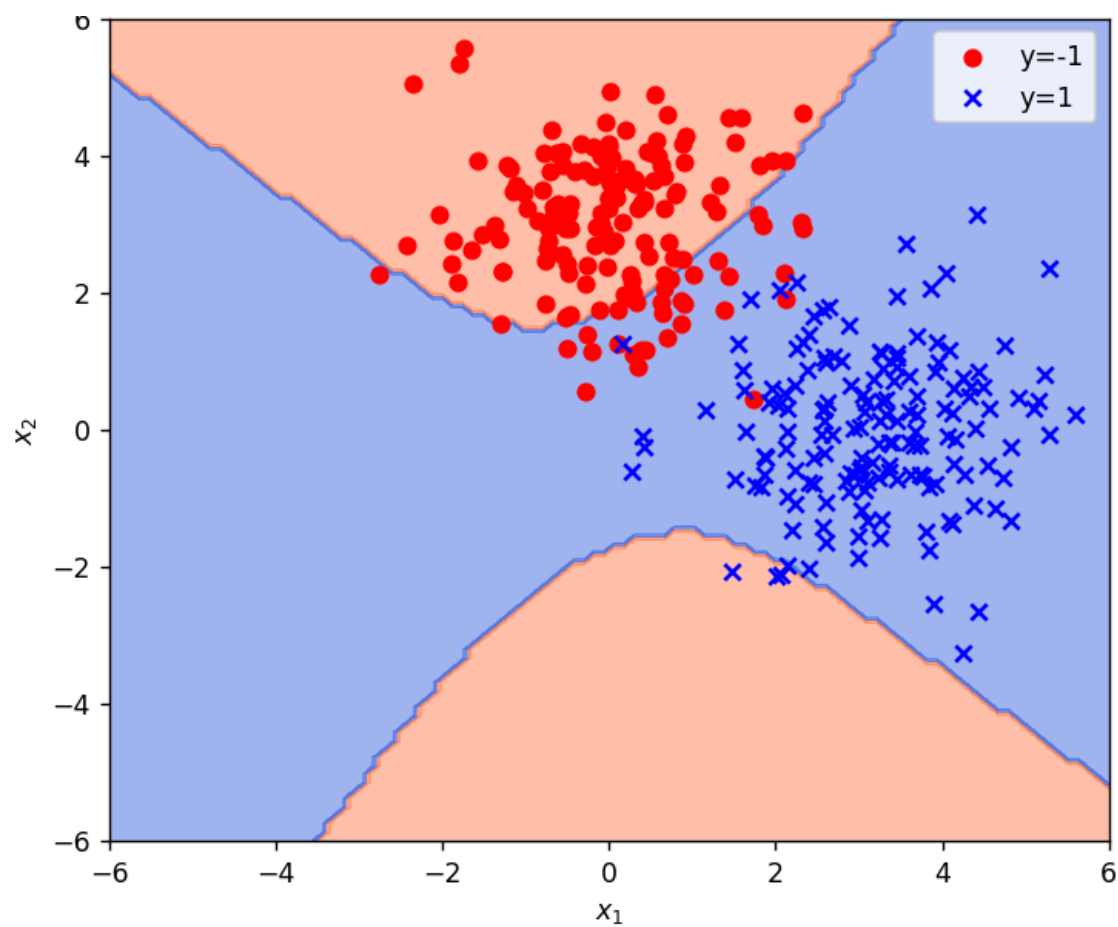
图示：



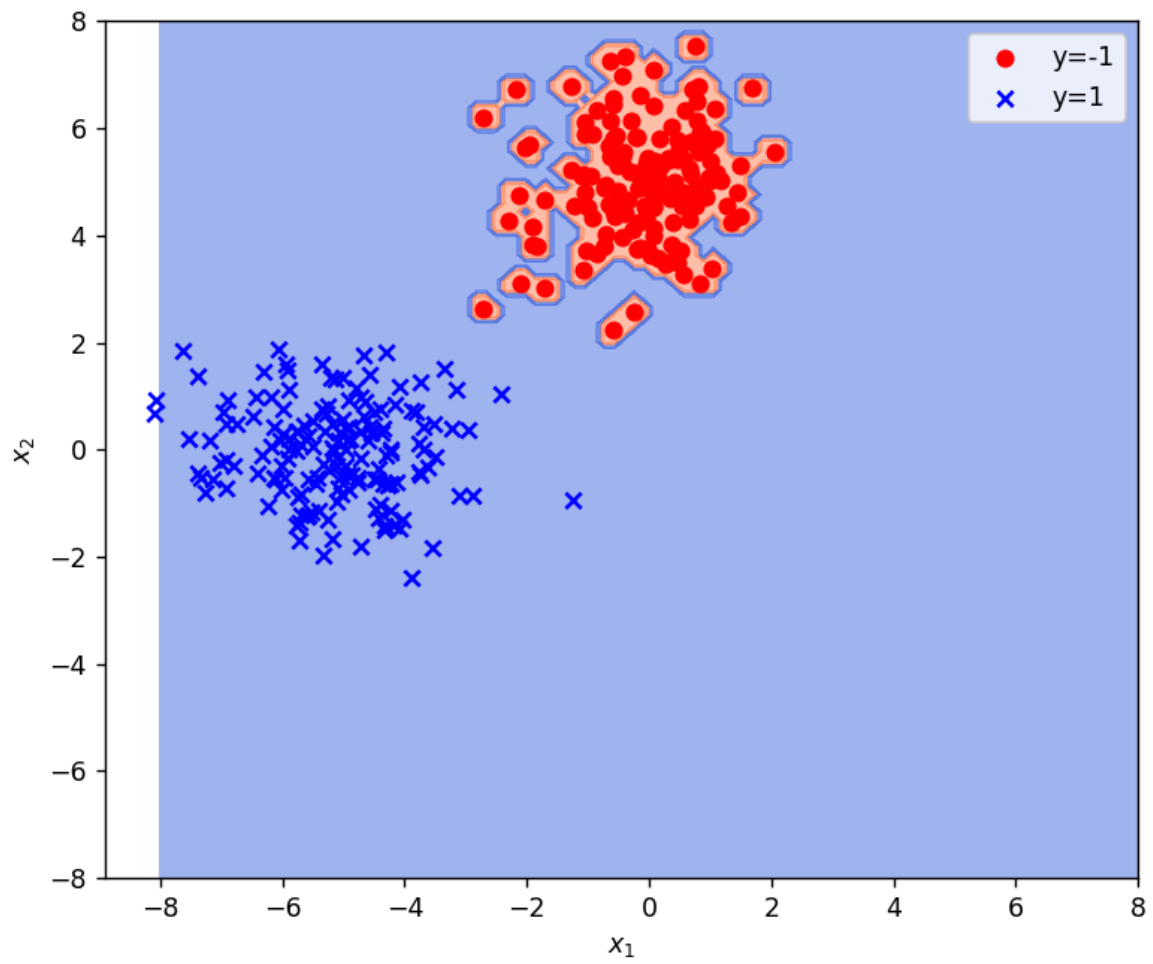
**Kernel-SVM (四次多项式核)**：均值向量为(-5,0)(0,5)时：



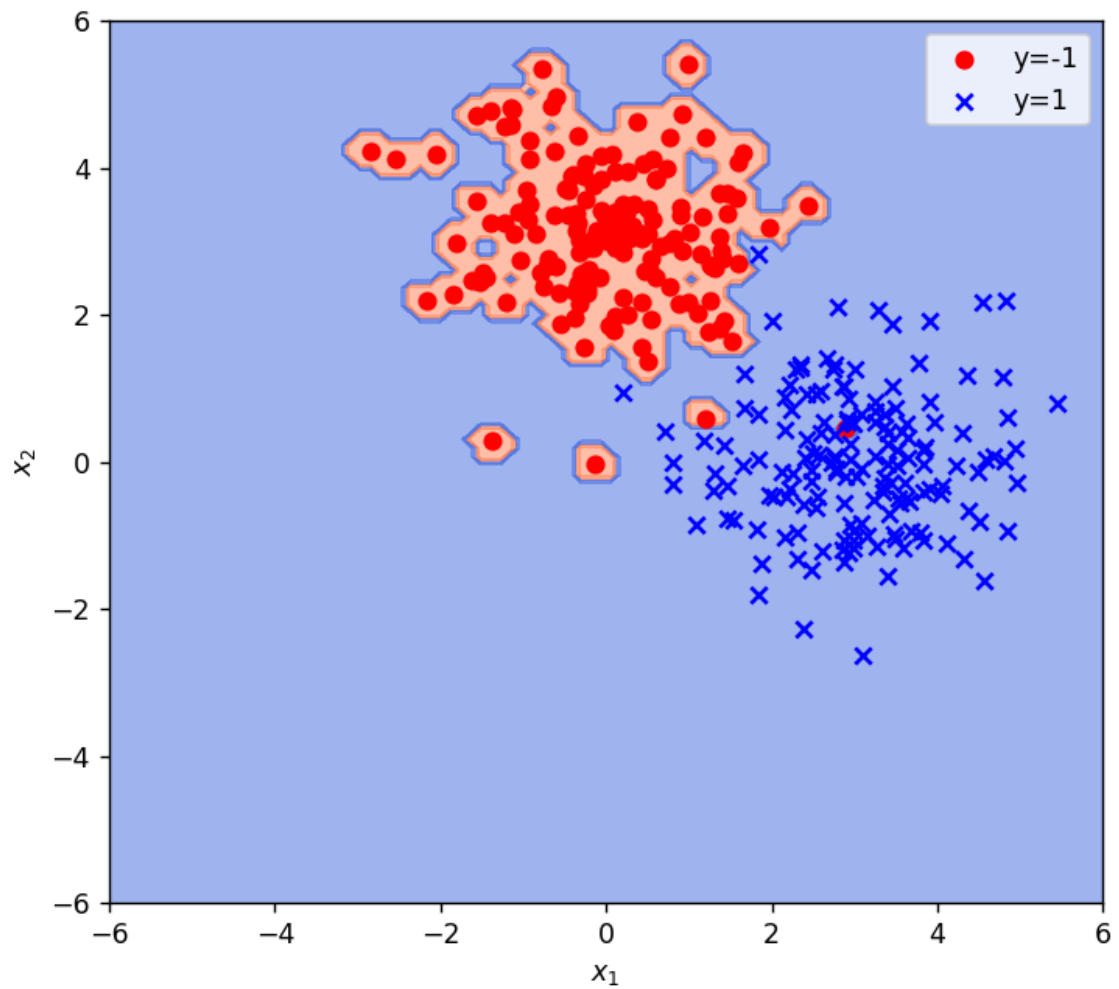
均值向量为(3,0)(0,3)时:



Kernel-SVM (高斯核) : 均值向量为(-5,0)(0,5)时:

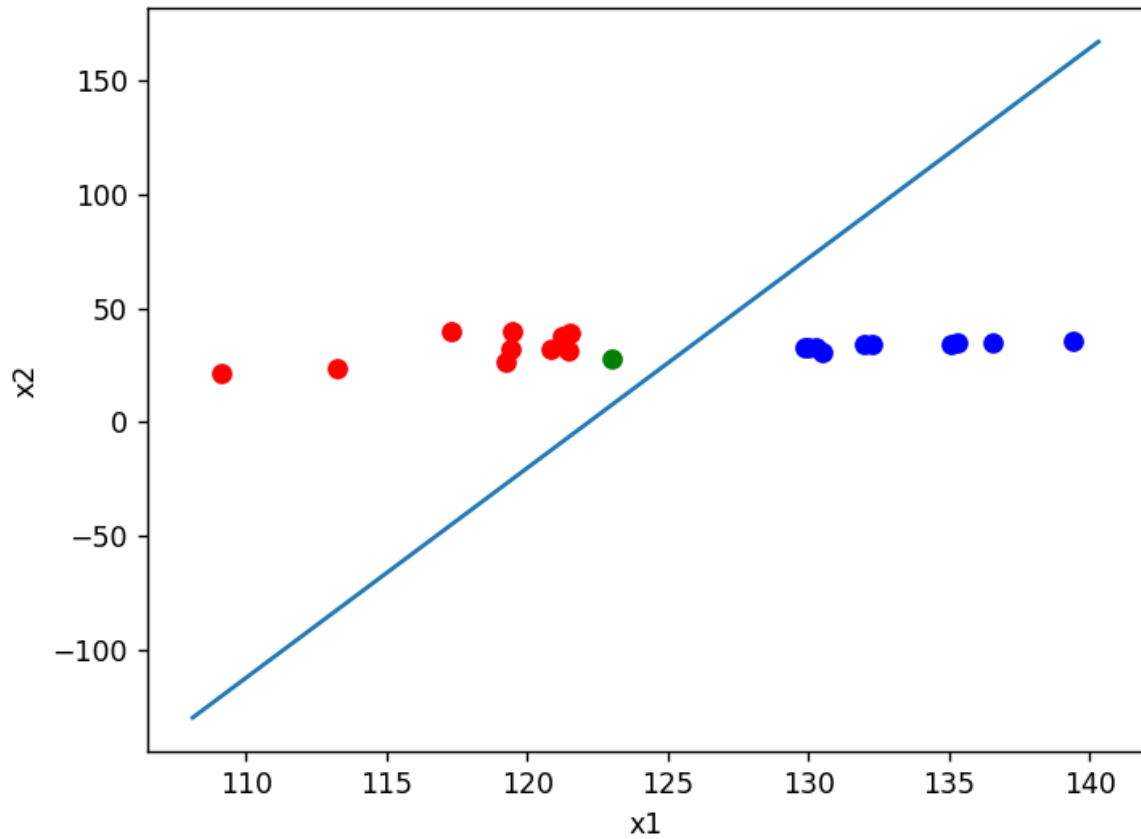


均值向量为(3,0)(0,3)时:



### 3、钓鱼岛：

将对偶支撑向量机的数据改成中日城市数据，训练后，将钓鱼岛数据进行分类，得出钓鱼岛属于中国。如图所示，红色类为中国，蓝色类为日本，绿色点为钓鱼岛：



## Lecture6 (多类分类) :

1、(a):见代码文件OVOPocket.py:

```
PS C:\Users\DELL> & C:/ProgramData/anaconda3/python.exe c:/Users/DELL/Desktop/Pattern-Recognition-And-Machine-Learning/OVOPOCKET.py
W: [ 3.6 11.7 -14.9 -5.6]
b: 1.0
W: [ 2.7 9.7 -11.7 -5.5]
b: 1.0
W: [ 0.4 2. -2.4 -0.2]
b: 0.0
训练集预测准确率为: 0.9111111111111111
测试集预测准确率为: 0.9166666666666666
PS C:\Users\DELL>
```

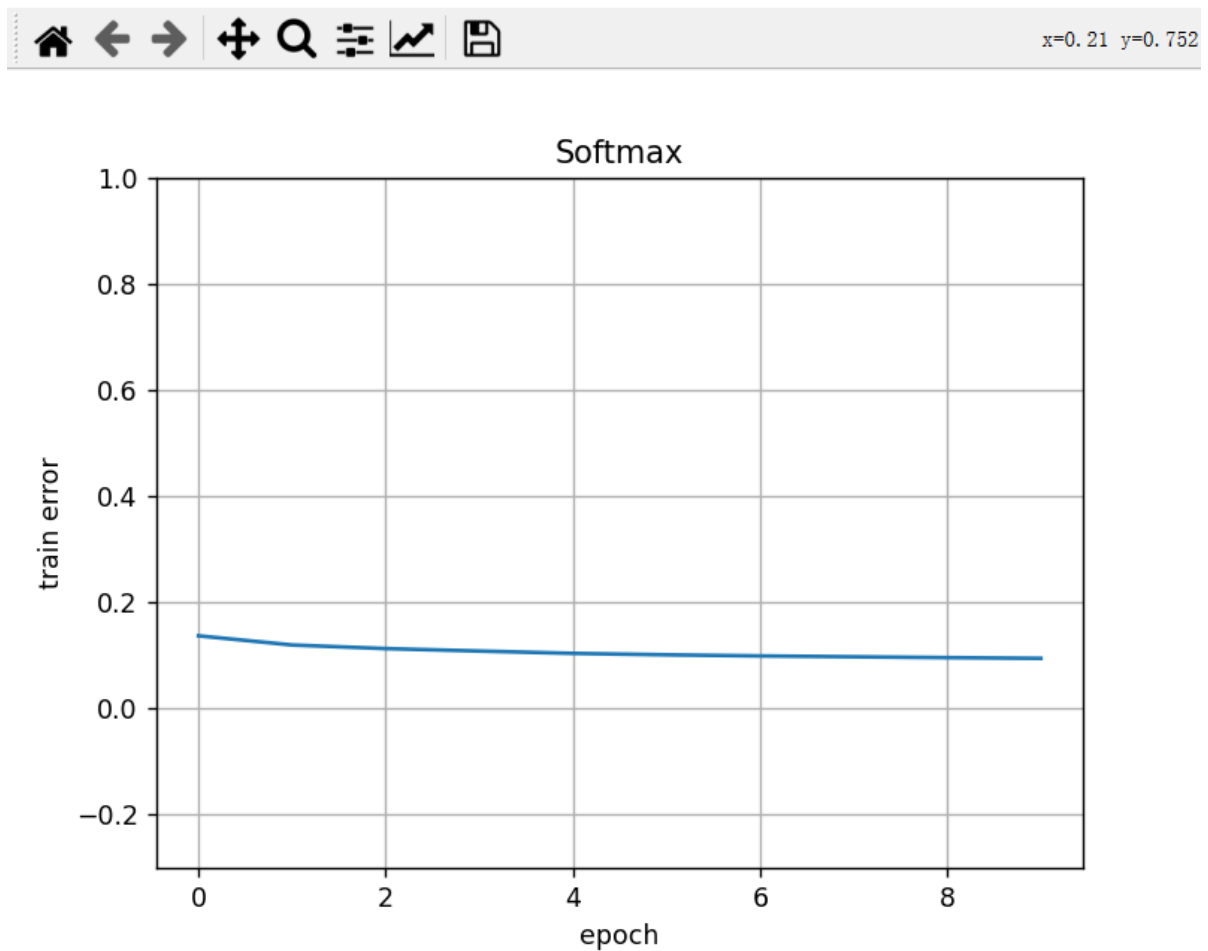
(b):见代码文件Softmax-Iris.py:

```
PS C:\Users\DELL> & C:/ProgramData/anaconda3/python.exe c:/Users/DELL/Desktop/Pattern-Recognition-And-Machine-Learning/Softmax-Iris.py
耗时: 1.8211085796356201 s
[[ [ 1.37727173 2.02183271 -0.37738173 0.35193286]
  [ 1.27737735 0.76316254 1.14230329 0.6867577 ]
  [ 0.34535092 0.21500474 2.23507844 1.96130944]]
训练集测试分类准确率: 0.9777777777777777
测试集测试分类准确率: 0.9666666666666667
```





Figure 1



下面随机抽取MNIST中的十个数据，观察分类结果：

第 37471 个手写字符的真实值是：7	预测值是：7 ;
第 24168 个手写字符的真实值是：1	预测值是：1 ;
第 2095 个手写字符的真实值是：7	预测值是：7 ;
第 2881 个手写字符的真实值是：7	预测值是：7 ;
第 35432 个手写字符的真实值是：0	预测值是：0 ;
第 59259 个手写字符的真实值是：4	预测值是：4 ;
第 56652 个手写字符的真实值是：7	预测值是：7 ;
第 25687 个手写字符的真实值是：1	预测值是：1 ;
第 40109 个手写字符的真实值是：3	预测值是：3 ;
第 30476 个手写字符的真实值是：5	预测值是：5 ;

## Lecture7 (神经网络与深度学习) :

1、见代码文件NN-Iris.py:

网络1：设计了一个两层的神经网络进行分类，第一层使用ReLU函数做激活函数，两层网络的大小分别为(4,10)、(10,3)，最后一层使用Softmax函数做激活函数，学习率为0.02，num\_epochs=100，下面展示分类效果：

```
耗时: 4.130415678024292 s
第一层网络参数为: OrderedDict([('weight', tensor([[[-0.4725, -0.3978, 0.1171, -0.1366],
[-0.3732, -0.5735, 1.1813, 2.1240],
[-0.2485, -0.4724, -0.1900, -0.1538],
[ 1.8978, 2.4894, -2.5734, -3.5348],
[ 0.1669, -0.1456, -0.4103, -0.2964],
[ 0.5205, 1.1156, -0.9817, -0.9971],
[-0.1879, -0.4565, -0.1521, 0.1314],
[ 0.0192, -0.0374, 0.2314, -0.1045],
[-0.3120, -0.0141, -0.2300, 0.2974],
[-0.6111, -0.4328, 1.2196, 1.5446]]])), ('bias', tensor([ 0.3226, -0.9810, 0.2884, 1.1039, -0.0201, 0.4511, 0.0706, -0.2951,
0.4725, -0.0951]))])第二层网络参数为: OrderedDict([('weight', tensor([[ 0.1048, -1.6729, -0.1307, 0.9818, -0.2552, 0.2736, -0.2051, -0.2173,
0.2373, -1.3679],
[ 0.1043, 0.4174, -0.1280, 0.4751, 0.2866, -0.0059, 0.1946, 0.2574,
0.1584, 0.3057],
[-0.1434, 1.2874, -0.1769, -1.0684, 0.2727, -0.6116, -0.2264, 0.3091,
0.1993, 0.9359]]])), ('bias', tensor([-0.3965, 1.3936, -1.6447]))])
预测准确率为: 0.9666666666666667
```

网络2: 设计了一个三层的神经网络进行分类, 第一层使用ReLU函数做激活函数, 两层网络的大小分别为(4,10),(10,20),(10,3), 最后一层使用Softmax函数做激活函数, 学习率为0.02, num\_epochs=100, 下面展示分类效果:

```
PS C:\Users\DELL> & C:\ProgramData\anaconda3\python.exe c:\Users\DELL\Desktop\Pattern-Recognition-And-Machine-Learning\MN-Iris.py
2023-11-17 13:16:54.760916: I tensorflow/core/platform/cpu_feature_guard.cc:182] This TensorFlow binary is optimized to use available CPU instructions in performance-critical operations.
To enable the following instructions: SSE SSE2 SSE3 SSE4.1 SSE4.2 AVX AVX2 FMA, in other operations, rebuild TensorFlow with the appropriate compiler flags.
source Control (Ctrl+Shift+G) 147 s
网络参数为: OrderedDict([('weight', tensor([[ 0.1068, -0.3759, -0.2028, -0.4079],
[-0.2531, 0.4481, -0.4444, -0.3960],
[-0.3973, 0.4424, 0.1850, -0.2623],
[-0.6421, -0.6999, 1.4910, 2.0585],
[-0.2987, 0.3924, -0.2685, 0.1422],
[ 1.8071, 2.5937, -2.6898, -3.2684],
[ 1.0638, 0.4638, -1.2590, -1.0143],
[-0.1298, -0.2473, -0.2800, 0.0848],
[-0.2634, 0.0162, 0.2360, -0.0361],
[-0.8227, -1.0881, 1.3967, 1.9871]]])), ('bias', tensor([ 0.4595, 0.3813, 0.0696, -0.1351, -0.2214, 1.2405, -0.0145, -0.4693,
0.2447, -0.5552]))), ('2.weight', tensor([[[-0.1143, 0.0961, -0.2936, -0.2689, 0.2225, -0.2365, -0.0085, -0.0286,
0.0866, 0.0771],
[-0.1269, 0.1830, 0.0988, -0.3024, 0.2629, 0.1411, 0.0446, 0.2423,
-0.0230, 0.0954],
[-0.0988, -0.2918, -0.1534, -0.1309, -0.1427, -0.1866, 0.0093, -0.1222,
0.0652, 0.1849],
[ 0.0099, 0.1682, 0.2717, -0.1760, 0.2874, 0.1639, 0.1446, 0.1667,
-0.1806, 0.1205],
[ 0.0334, 0.2979, -0.2014, -0.0827, -0.3081, -0.1413, 0.2517, 0.1764,
0.0621, -0.1495],
[ 0.2428, -0.2213, 0.1988, 0.2627, 0.2095, -0.4707, -0.1964, -0.2411,
0.0959, -0.1507],
[ 0.2186, -0.0164, 0.2274, -0.5168, -0.2799, 0.5217, 0.3356, -0.1873,
-0.1511, 0.0717],
[-0.2026, -0.1786, -0.2973, -0.2929, -0.2550, 0.9016, 0.3695, 0.3065,
-0.1327, -0.3356],
[ 0.2212, -0.2713, -0.0082, -0.7617, 0.2876, 0.2932, 0.2346, -0.1560,
0.1409, 0.2902],
[ 0.1466, 0.2838, 0.2978, -0.2439, 0.2863, 0.0693, -0.2556, -0.1263,
0.0614, -0.1696],
[ 0.1576, 0.0866, 0.0233, -0.3829, -0.0480, 0.8338, 0.1351, 0.0430,
0.2925, -0.3247],
[-0.1333, 0.1000, -0.2032, 0.4141, 0.1844, -0.6699, -0.0195, 0.2673,
-0.2075, 0.3556],
[-0.1929, -0.2071, 0.2955, 0.0083, 0.0315, 0.2922, 0.2897, 0.2194,
-0.1622, -0.4601],
[ 0.0623, 0.1972, -0.0001, -0.1250, 0.2189, -0.0436, -0.0710, -0.1913,
0.1314, 0.2680],
[-0.2292, 0.3400, 0.2964, -0.6694, 0.2664, 0.3290, 0.0840, -0.0582,
-0.1816, -0.1291],
[ 0.0744, -0.1961, -0.1031, -0.1307, -0.1794, -0.0457, -0.5498, -0.5144,
-0.2220, 0.1017, -0.5331, 0.2478, 0.0031, 0.0339, -0.3572, 0.2423,
0.1824, 0.9257, 0.0648, -0.1170]]])), ('4.bias', tensor([-0.6372, 1.2775, -0.2294]))])
预测准确率为: 0.9666666666666667
```

网络3: 将网络2中的激活函数由ReLU()换成Sigmoid(), 下面展示分类效果:

```
PS C:\Users\DELL> & C:\ProgramData\anaconda3\python.exe c:\Users\DELL\Desktop\Pattern-Recognition-And-Machine-Learning\MN-Iris.py
2023-11-17 13:19:08.665959: I tensorflow/core/platform/cpu_feature_guard.cc:182] This TensorFlow binary is optimized to use available CPU instructions in performance-critical operations.
To enable the following instructions: SSE SSE2 SSE3 SSE4.1 SSE4.2 AVX AVX2 FMA, in other operations, rebuild TensorFlow with the appropriate compiler flags.
耗时: 5.118422985076904 s
网络参数为: OrderedDict([('weight', tensor([[ 0.3153, -0.6293, 0.0924, 0.4473],
[-0.7426, -1.1196, 1.2403, 1.6521],
[ 0.5374, 0.8568, -1.2865, -0.6488],
[ 0.5741, 1.1938, -1.2619, -1.2188],
[ 0.0259, -1.3203, 1.2286, 0.4208],
[ 0.2027, 0.9715, -0.7127, -1.2979],
[ 0.8382, 0.9260, -1.2135, -1.7290],
[-0.5396, -0.2993, 0.6882, 1.1940],
[ 0.3932, -0.1456, 0.1603, -0.0352],
[-0.3266, 0.5611, -0.3233, 0.1699]]])), ('0.bias', tensor([-0.3704, -0.6529, 0.3360, 0.6110, 0.1602, 0.0722, 0.6428, -0.0313,
-0.0283, -0.3129]))), ('2.weight', tensor([[[-0.3505, -1.2179, 1.1527, 1.2997, -0.4480, 0.9223, 1.4081, -0.6179,
0.1428, 0.2119],
[-0.1358, -0.5245, 0.3453, 0.5615, -0.5754, 0.5938, 0.4264, -0.2672,
-0.3147, 0.2980],
[ 0.3647, 0.5989, -0.6318, -0.2368, 0.4967, -0.0997, -0.7605, 0.4022,
0.1104, -0.3456],
[-0.0054, 0.4940, -0.4405, -0.4324, 0.0925, -0.0840, -0.6423, 0.4360,
0.1512, 0.2034],
[-0.0546, 0.0671, -0.1249, -0.2900, 0.5271, -0.2336, -0.3820, 0.1008,
-0.1243, -0.1034],
[ 0.0645, 0.4963, -0.5545, -0.3185, 0.6040, -0.4813, -0.1950, 0.2783,
-0.0788, 0.0386],
[ 0.2227, 0.5120, -0.0155, -0.4372, 0.2256, -0.1175, -0.2571, 0.4121,
0.0404, -0.2226],
[ 0.3331, 1.0502, -0.5040, -0.8245, 1.2205, -0.6668, -0.7179, 0.5148,
0.2431, -0.2154],
[-0.2160, -1.0383, 0.6946, 0.9580, -0.3739, 0.8365, 1.0756, -0.5538,
0.2292, -0.0511],
[ 0.0604, 0.9743, -0.7505, -0.8740, 1.1365, -0.4900, -0.6446, 0.7709,
0.5401, -0.3607],
[-0.2261, -0.2412, 0.1801, 0.4079, -0.5749, -0.0221, 0.0615, -0.2113,
0.1621, 0.0837],
[-0.0037, -0.1339, -0.1858, -0.3290, -0.1812, 0.0438, 0.2462, 0.1627,
0.2104, 0.1627],
[ 0.0739, 0.6445, -0.7183, -0.7726, 0.9509, -0.7329, -0.8232, 0.4266,
0.1237, -0.1777],
[ 0.2187, 0.1439, -0.3131, -0.2680, -0.0217, -0.1211, -0.1664, -0.1150,
-0.2605, -0.3156],
[ 0.0223, -0.6735, 0.3079, 0.2264, -0.5833, 0.3042, 0.1851, -0.0693,
0.1080, -0.2163],
[-0.1730, -0.9192, 1.0475, 1.0648, -0.7305, 0.6765, 0.9044, -0.4374,
```

```

-0.1793, -0.0344],
[-0.1488, 0.4601, -0.1614, -0.1630, 0.6186, -0.5162, -0.6177, 0.1988,
0.1031, -0.1721],
[0.0365, -0.6953, 0.1798, 0.6183, -0.5007, 0.4094, 0.8413, -0.4076,
0.1049, 0.3416],
[0.1838, 0.3848, -0.0732, -0.3041, -0.0713, 0.0624, -0.1542, 0.1854,
-0.1977, 0.0751],
[0.0057, 0.0523, -0.6062, -0.4062, 0.6986, -0.4085, -0.4352, 0.3375,
0.1785, 0.2820]], ('2.bias', tensor([0.0048, 0.0143, 0.1717, -0.2072, -0.0243, 0.0569, -0.3576, 0.3044,
-0.0216, -0.0062, -0.0451, 0.0174, 0.2039, -0.2277, -0.2187, 0.2006,
-0.0458, 0.1436, -0.0481, 0.3308])), ('4.weight', tensor([[-1.9910, 1.0211, -1.1351, -0.6906, -0.5127, -0.9262, -0.6190, -2.1861,
1.2397, -2.1896, 0.6708, -0.2199, -1.6025, -0.2541, 0.5766, 1.7615,
-0.8351, 0.8893, -0.1504, -0.8916],
[0.7866, -0.0975, 0.2724, -0.1824, 0.1731, 0.0358, -0.0348, 0.5510,
0.5415, 0.4115, -0.1512, 0.1003, 0.1140, 0.1378, -0.1042, 0.3830,
0.0385, 0.3946, 0.0328, 0.4882],
[-2.6260, -1.0420, 0.7551, 0.7236, 0.4020, 0.6522, 0.4822, 1.6732,
-2.0639, 1.6744, -0.3238, -0.2684, 1.6791, 0.2961, -0.7846, -2.0670,
0.6993, -1.2231, 0.3412, 0.7651]])), ('4.bias', tensor([0.1767, 0.1364, -0.5173])))
预测准确率为: 0.9833333333333333

```

可以观察到，从网络1到网络3，分类准确率不断提升

2、见代码文件LeNet-MNIST.py,代码调用GPU运算：

结果如图所示：

```

PS C:\Users\DELL> & C:/ProgramData/anaconda3/python.exe c:/Users/DELL/Desktop/Pattern-Recognition-And-Machine-Learning/LeNet-MNIST.py
2023-11-17 13:46:09.101996: I tensorflow/core/platform/cpu_feature_guard.cc:182] This TensorFlow binary is optimized to use available CPU instructions in performance-critical operations.
To enable the following instructions: SSE SSE2 SSE3 SSE4.1 SSE4.2 AVX AVX2 FMA, in other operations, rebuild TensorFlow with the appropriate compiler flags.
cc train: 0.1065 | 0/10 [00:00<, ?it/s]a
10% | 1/10 [00:18<02:43, 18.12s/it]a
cc train: 0.1109 | 2/10 [00:34<02:16, 17.05s/it]a
20% | 3/10 [00:50<01:55, 16.49s/it]a
cc train: 0.23450666666666667 | 4/10 [01:06<01:37, 16.25s/it]a
30% | 5/10 [01:22<01:21, 16.25s/it]a
cc train: 0.7403166666666666 | 6/10 [01:38<01:04, 16.11s/it]a
40% | 7/10 [01:53<00:47, 15.90s/it]a
cc train: 0.9317333333333333 | 8/10 [02:09<00:31, 15.72s/it]a
50% | 9/10 [02:24<00:15, 15.69s/it]a
cc train: 0.9504833333333334 | 10/10 [02:40<00:00, 16.03s/it]a
60% | 
cc train: 0.9068166666666667 | 
70% | 
cc train: 0.9696666666666667 | 
80% | 
cc train: 0.9748666666666667 | 
90% | 
cc train: 0.9782333333333333 | 
100% | 
耗时: 160.33472394943237 s

```

