

USERGUIDE

OF ELATOOLS (ANISOTROPIC ELASTICITY TOOLS)

FROM ELASTICTOOLS PROJECT V1.6.2

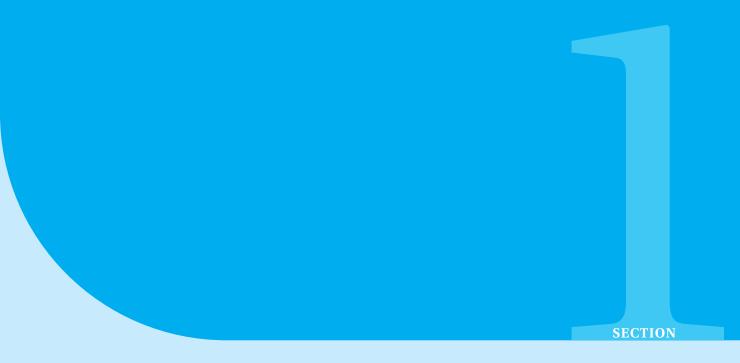
PRODUCED BY:

SHAHRAM YALAMEHA

YALAMEHA93@GMAIL.COM

Table of Contents

1	Features and Change Log of ElATools					
	1.1	Features of ElATools and its comparison with ELATE and ELAM codes				
			2			
	1.2	Change Log	3			
2	The	Theoretical Background				
	2.1	Hooke's law and elastic tensor of crystals	5			
	2.2	2.2. Transformation law and representation surfaces of elastic pro-				
		prieties	6			
	2.3	2.3. Basic proprieties and averaging schemes	9			
3	Wor	kflow of ElATools	12			
4	Gett	ting started	13			
	4.1	How to obtain ElATools	13			
	4.2	How to install ElATools	13			
	4.3	How to use ElATools	14			
	4.4	Run ELATools and Results data	14			
		4.4.1 Calculation Kernel (CK)	15			
		4.4.2 Temporary images	17			
5	Post	t processing	19			
	5.1	dat2wrl	19			
	5.2	dat2gnu	20			
	5.3	dat2agr	22			
19	Re	eferences	25			



Features and Change Log of El*A*Tools

We introduce a computational method and a user-friendly code (ElATools) developed for the analysis of anisotropic elastic properties. ElATools enables facile analysis of the second-order elastic stiffness tensor of two-dimensional (2D) and three-dimensional (3D) crystal systems. It computes and displays the main mechanical properties such as bulk modulus, Young's modulus, shear modulus, p-wave modulus, universal anisotropy index, Chung-Buessem anisotropy index, log-Euclidean anisotropy parameter, Cauchy pressure, Poisson's ratio, and Pugh's ratio, using three averaging schemes of Voigt, Reuss, and Hill. ElATools has a database that contains more than 13,000 elastic stiffness constants for 3D materials available to the user. The program supports output files of the major computational codes IRelat, ElaStic, and AELAS. Three helpful plotting and visualization tools are integrated to conveniently interface with GNUPLOT, XMGRACE, and view3dscene, offering immediate post-processing of the results. ElATools provides reliable means to investigate the mechanical stability based on the calculation of six (three) eigenvalues of the elastic tensor in 3D (2D) materials. It can effectively identify anomalous mechanical properties, such as negative linear compressibility, negative Poisson's ratio, and highlyanisotropic elastic modulus in 2D and 3D materials, which are central properties to design and develop high-performance nanoscale electromechanical devices.

1.1 Features of ElATools and its comparison with ELATE and ELAM codes

• Compute and display the main mechanical properties such as bulk modulus, Young's modulus, shear modulus, p-wave modulus, universal anisotropy index [5], Chung-

Buessem anisotropy index [5], log-Euclidean anisotropy parameter [6], Cauchy pressure, Poisson's ratio, Pugh's ratio, according to the three averaging schemes of Voigt, Reuss, and Hill [7] - Many of these features are included in ELAM and ELATE codes.

- Investigation of mechanical stability using calculation of six (three) eigenvalues of the elastic tensor in 3D (2D) materials This option exists only in ELATE for 3D materials.
- Visualization of the 3D surfaces and 2D projections on any desired plane for shear modulus, Poisson's ratio, linear compressibility, bulk modulus, and Young's modulus in 3D materials ELATE only depicts these features on XY, XZ, and ZY planes. The bulk modulus calculation does not exist in either ELAM or ELATE.
- Visualization of the 2D polar covers for Poisson's ratio, shear modulus, and Young's modulus in 2D materials This option does not exist in the ELATE or ELAM.
- An offline database of more than 13000 elastic tensors taken from Materials API This option is available only online in ELATE.
- Supports various output formats for custom drawing or displaying with different software: ".dat" files for standard plotting, ".wrl" files for visualization of the 3D surfaces by view3dscene software [8], ".agr" files for visualization of the 2D projections that are opened by XMGRACE [9], and ".gpi" script files for visualization of the 3D surfaces, 2D heat maps, and 2D projections that can be run by GNUPLOT [10] ELAM generates only VRML (for 3D visualization) and PS formats (for 2D cut visualization). ELATE provides images online in PNG format only.

1.2 Change Log

- v1.1.0 [14/07/2018] : Add a new funtion to calculate the bulk modulus properties for 3D system.
- v1.1.1 [20/12/2018] : Add a new funtion to check stability conditions for 3D system.
- v.1.2.0 [05/04/2019] : Add dat2gnu lapw to plot by gnuplut.
- v.1.3.0 [12/05/2020] : Add a new funtion to calculate elsetic properties, and check stability conditions for 2D system.
- v.1.4.0 [10/06/2020]: The addition of a database includes more than 13,000 elastic tensors and a function for reading it.
- v.1.5.0 [01/07/2020] : Add a new funtion to calculate the phase and group velocities of the acoustic waves.

- v.1.5.1 [20/07/2020] : Add a new funtion to calculate the shear modulus for 2D system.
- v.1.5.2 [10/08/2020] : Add new options of dat2gnu to plot 2D heat maps.
- v.1.6.0 [20/04/2021] : Add new elsetic properties for 3D materials. Lame's first and second parameters, Kleinman parameter, Hardness information.
- v.1.6.1 [04/05/2021] : Add heat map colors (bbry, grv, bbvy, bgyr, bryw) in dat2gnu.x [Properties] [hmap colors]
- v1.6.2[0.5/0.5/2021]: Module wrl-setcolor.f90 added to dat2wrl.x. From now on you can customize the color scheme of case.wrl files.
- v1.6.3 [31/05/2021]: Fixed a number of bugs
- v1.6.4 [01/06/2021]: Add a function to calculate the hardness.

3D and 2D representations of hardness can be plot by dat2gnu.x and dat2wrl.x.

dat2gnu hard: 2D cut of hardness

dat2gnu hmhard: 2D Heat map of hardness

dat2wrl hard: 3D representations of hardness

• v1.6.5 [08/06/2021]: Add advanced option for 2D materials. To enter this option, after selecting the two-dimensional system, select the option related to the elastic tensor Cij-2D.dat.

This option should be used for rectangular, quadratic, and oblique 2D materials. This option has not been tested. Be careful when using.

- v1.6.6 [05/07/2021]: Add Cauchy pressure for Cubic, Hexagonal, Trigonal, Tetragonal, and Orthorhombic symmetries.
- v1.6.7 [09/07/2021]: Add "Back" option in GUI. Fix bug in "Advanced option" of 2D materials.

Theoretical Background

2.1 Hooke's law and elastic tensor of crystals

The shape of a solid material changes when it is subjected to a stress. Provided that the stress is below a specific value, the elastic limit, the strain is recoverable (Fig. 1). This means that the material returns to its original shape when the stress is removed. In this elastic regime, according to Hooke's law, it can be stated that for sufficiently low stresses, the amount of strain is proportional to the magnitude of the applied stress:

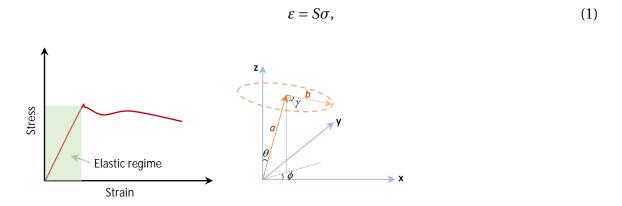


Figure 1: Schematic stress–strain curves and definitions of angles used to describe the directions in the calculations related to ElATools. The elastic regime corresponds to the portion of the diagram where the strain is proportional to the stress.

where *S* is a constant. *S* is called the *elastic compliance constant* (ECC), or the *compliance*. Another form of this equation can be written as follows,

$$\varepsilon = C\sigma, \ E \equiv C = 1/s,$$
 (2)

where *C* is the *elastic stiffness constant* (ESC), or *stiffness*, and E is Young's modulus. The general form of Hooke's law can be rewritten in the form of tensor,

$$\varepsilon_{ij} = S_{ijkl}\sigma_{kl},\tag{3}$$

where S_{ijkl} are the ECCs of the crystal. Also, as an alternative to Eq.(2),

$$\sigma_{ij} = c_{ijkl} \varepsilon_{kl},\tag{4}$$

where C_{ijkl} are the ESCs. Eq.(3) and Eq.(4) stand for nine equations, each with nine terms on the right-hand side. The S_{ijkl} or C_{ijkl} are 4^{th} -rank tensors, and ϵ_{ij} or σ_{ij} are second th -rank tensors. Hence, the C_{ijkl} (S_{ijkl}) consists of 81 *stiffness* (*compliances*) constants of the crystal. Due to the inherent symmetries (translational and rotational symmetries) of ϵ_{ij} , σ_{ij} , and S_{ijkl} or C_{ijkl} , the number of independent coordinates of the 4^{th} -rank tensor reduces to 21 for the least symmetric case. On the other hand, the further reduction resulting from the symmetry of the crystal can be applied to this number: 21 for triclinic, 15 for monoclinic, 9 for orthorhombic, 7 for trigonal, 5 for tetragonal, 5 for hexagonal and 3 for cubic.

2.2 2.2. Transformation law and representation surfaces of elastic proprieties

A 4^{th} -rank tensor is defined (like tensors of lower rank) by its transformation law [11]. We know that the 81 tensor components A_{ijkl} representing a physical quantity are said to form a 4^{th} -rank tensor if they transform on change of axes to A'_{ijkl} , where

$$A'_{ijkl} = a_{im} a_{jn} a_{ko} a_{lp} A_{mnop}.$$
 (5)

It can be shown that 4^{th} -rank tensor S_{ijkl} or C_{ijkl} follows this rule [11]:

$$\begin{cases}
\varepsilon'_{ij} = a_{ik} a_{jl} \varepsilon_{kl}, \\
\varepsilon_{kl} = S_{klmn} \sigma_{mn}, \\
\sigma_{mn} = a_{om} a_{pn} \sigma'_{op},
\end{cases}$$

$$\begin{cases}
\varepsilon'_{ij} = a_{ik} a_{jl} S_{klmn} a_{om} a_{pn} \sigma'_{op}. \\
\varepsilon'_{ij} = a_{ik} a_{jl} S_{klmn} a_{om} a_{pn} \sigma'_{op}.
\end{cases}$$
(6)

By comparing Eq.(3) and the recent equation, we have:

$$S'_{ijkl} = a_{im} a_{jn} a_{ko} a_{lp} S_{mnop}, (7)$$

which is the necessary transformation law. To express the anisotropic form of Hooke's law in matrix notation, we use the Voigt notation scheme. In the S'_{ijkl} and S_{mnop} , the first two suffixes are abbreviated into a single one running from 1 to 6, and the last two are abbreviated in the same way, according to the following Voigt scheme:

Therefore, the components of the stress (σ) and the strain (ε) tensors are written in a single suffix running from 1 to 6,

$$\sigma_{ij} = \begin{pmatrix} \sigma_{11} & \sigma_{12} & \sigma_{13} \\ \sigma_{12} & \sigma_{22} & \sigma_{23} \\ \sigma_{13} & \sigma_{23} & \sigma_{33} \end{pmatrix} \text{Voigt scheme} \begin{pmatrix} \sigma_{1} & \sigma_{6} & \sigma_{5} \\ \sigma_{6} & \sigma_{2} & \sigma_{4} \\ \sigma_{5} & \sigma_{4} & \sigma_{3} \end{pmatrix},$$

$$\varepsilon_{ij} = \begin{pmatrix} \varepsilon_{11} & \varepsilon_{12} & \varepsilon_{13} \\ \varepsilon_{12} & \varepsilon_{22} & \varepsilon_{23} \\ \varepsilon_{13} & \varepsilon_{23} & \varepsilon_{33} \end{pmatrix} \text{Voigt scheme} \begin{pmatrix} \varepsilon_{1} & \frac{1}{2}\varepsilon_{6} & \frac{1}{2}\varepsilon_{5} \\ \frac{1}{2}\varepsilon_{6} & \varepsilon_{2} & \frac{1}{2}\varepsilon_{4} \\ \frac{1}{2}\varepsilon_{5} & \frac{1}{2}\varepsilon_{4} & \varepsilon_{3} \end{pmatrix}.$$

$$(9)$$

According to this scheme, we have for the S_{mnop} [11],

 $S_{mnop} = S_{ij}$, when i and j are 1; 2 or 3, $2S_{mnop} = S_{ij}$, when either i or j are 4; 5 or 6, $4S_{mnop} = S_{ij}$ when both i and j are 4; 5; or 6.

Therefore, Eq.(3) takes the shorter form:

$$\varepsilon_i = S_{ij}\sigma_j \ (i, j = 1, 2, ..., 6).$$
 (10)

The Voigt scheme replaces the cumbersome 2^{th} and 4^{th} -rank tensors in a 3-dimensional vector space of vectors and matrices in a 6-dimensional vector space. The reason for introducing the factors of 0.5 in Eq.(9) and the factors of 2 and 4 into the definitions of the S_{ij} is to enable writing Eq.(10) in a compact form.

Using S_{ij} in Eq.(10) and Eq.(5), we can get a general and and straightforward compliance transformation relation for any crystal from the old systems (T') to measurement systems (T):

$$T'_{iikl} = r_{i\alpha} \, r_{i\beta} \, r_{k\gamma} \, r_{l\delta} \, T_{\alpha\beta\gamma\delta}, \tag{11}$$

where the r represents the components of the rotation matrix (or direction cosines). In general, the tension produces not only longitudinal, and lateral strains, but shear strains as well. Therefore, spherical coordinates are suitable for such stresses and the responses that materials give to stresses. We choose $r \equiv a$ to be the first unit vector in the new basis set [3, 4],

$$\boldsymbol{a} = \begin{pmatrix} \sin(\theta)\cos(\varphi) \\ \sin(\theta)\sin(\varphi) \\ \cos(\theta) \end{pmatrix}; \quad 0 \le \theta \le \pi, \quad 0 \le \varphi \le \pi, \tag{12}$$

This unit vector (\boldsymbol{a}) is required to determine Young's modulus (E), linear compressibility (β), and bulk modulus (B). But some elastic properties such as the shear modulus (G) and Poisson's ratio (v) requires another perpendicular direction. Therefore, we define unit vector \boldsymbol{b} , which is perpendicular to \boldsymbol{a} (see Fig. 1), as follows [3, 4]:

$$\boldsymbol{b} \equiv \begin{pmatrix} \cos(\theta)\cos(\varphi)\cos(\gamma) - \sin(\theta)\sin(\gamma) \\ \cos(\theta)\sin(\varphi)\cos(\gamma) - \cos(\theta)\sin(\gamma) \\ -\sin(\theta)\cos(\gamma) \end{pmatrix}, \quad 0 \le \gamma \le 2\pi.0$$
 (13)

Therefore, by defining these two vectors, Eq.(11) is as follows:

$$T'_{\alpha\beta\gamma\delta} = a_{\alpha i} \, a_{\beta j} \, b_{\gamma k} \, b_{\delta l} T_{ijkl}, \tag{14}$$

Using this equation, we can calculate the representation surfaces for elastic properties. For instance, from Eq.(10), we know that Young's modulus can be obtained by using purely normal stress (see Fig. ??(c)),

$$E(\mathbf{a}) \equiv \frac{1}{S'_{1111}} = \sum_{ijkl}^{6} \frac{1}{a_{1i}a_{1j}a_{1k}a_{1l}S_{ijkl}}$$

$$= \frac{1}{S'_{11}} = \frac{1}{a_{i}a_{j}a_{k}a_{l}S_{ijkl}} \text{ (by Einstein's summation rule),}$$
(15)

The volume compressibility of a crystal is the proportional decrease in volume of a crystal when subjected to unit hydrostatic pressure, but the linear compressibility is the relative decrease in length of a line when the crystal is subjected to unit hydrostatic pressure (HP). Hence, it is obtained by applying isotropic stress (P_{HP}) in a tensor form so that ε_{ij} =-(P_{HP}) S_{ijkk} [3, 11], and by considering that the extension in a direction is $\varepsilon_{ij}a_ia_j$, and for this reason, we have:

$$\beta(\mathbf{a}) = a_i a_j a_k a_k S_{ijkk} = a_i a_j S_{ijkk}; \ a_k. \ a_k = 1$$
 (16)

On the other hand, the relationship between β and B can be expressed as follows [11],

$$B(\mathbf{a}) = \frac{1}{\beta(\mathbf{a})} = \frac{1}{a_i a_j S_{ijkk}}$$
(17)

As mentioned, the G and v are not as straightforward to represent and depend on two directions (\boldsymbol{a} and \boldsymbol{b}). The shear ratio (Poisson's ratio) is obtained by applying a pure shear (Fig. $\ref{Fig. 27}(d)$) (a purely normal) stress in the vector form of Eq.(3), and results in:

$$G(\mathbf{a}, \mathbf{b}) = \frac{1}{4S_{1212}} = \frac{1}{4S_{66}} = \frac{1}{4} \frac{1}{a_i b_i a_k b_l S_{ijkl}},$$
(18)

$$v(\mathbf{a}, \mathbf{b}) = -\frac{S'_{1212}}{S'_{111}} = -\frac{S'_{12}}{S'_{11}} = -\frac{a_i a_j b_k b_l S_{ijkl}}{a_i a_j a_k a_l S_{ijkl}}.$$
 (19)

To better understand these equations, we obtain Young's modulus of a cubic crystal. As for cubic crystal, because of lattice symmetry, there are three independent variables C_{11} , C_{12} , C_{44} in the C_{ij} , and S_{11} , S_{12} , and S_{33} in the S_{ij} . Using Eq.(15) and Eq.(12), we have:

$$S'_{1111} = a_{11}a_{11}a_{11}a_{11}S_{1111} + a_{12}a_{12}a_{12}a_{12}S_{2222} + a_{13}a_{13}a_{13}S_{3333} +$$

$$a_{11}a_{11}a_{12}a_{12}S_{1122} + a_{11}a_{11}a_{13}a_{13}S_{1133} + a_{12}a_{12}a_{13}a_{13}S_{2233} +$$

$$a_{11}a_{11}a_{12}a_{12}S_{2211} + a_{11}a_{11}a_{13}a_{13}S_{3311} + a_{12}a_{12}a_{13}a_{13}S_{3322} +$$

$$\frac{1}{4}[a_{12}a_{13}a_{12}a_{13}S_{2323}] + \frac{1}{4}[a_{13}a_{11}a_{13}a_{11}S_{3131}] + \frac{1}{4}[a_{11}a_{12}a_{11}a_{12}S_{1212}]$$

$$= S_{11}(a_{11}^4 + a_{12}^4 + a_{12}^4) + (\frac{1}{4}S_{44} + 2S_{12})[a_{12}^2a_{12}^2 + a_{11}^2a_{12}^2 + a_{11}^2a_{12}^2],$$
(20)

with further simplification,

$$\frac{1}{E} = S'_{1111} = S_{11} - 2(S_{11} - S_{12} - \frac{1}{2}S_{44})(a_{11}^2 a_{12}^2 + a_{11}^2 a_{13}^2 + a_{12}^2 a_{13}^2)$$
 (21)

To calculate the orientation-dependent Poisson's ratio, shear modulus and Young's modulus in 2D material, Eq.(12) and Eq.(13) are used again and changed as follows:

$$\mathbf{a} = \begin{pmatrix} \cos(\varphi) \\ \sin(\varphi) \\ 0 \end{pmatrix}; \ \mathbf{b} = \begin{pmatrix} -\sin(\varphi) \\ \cos(\varphi) \\ 0 \end{pmatrix}; \quad 0 \le \varphi \le 2\pi.$$
 (22)

For 2D system, according to Hooke's law (Eq.(3) and Eq.(4)), the relationship between σ and the corresponding strain tensor ε can be described using the stiffness tensor C_{ij} , for orthogonal symmetry under plane stress conditions as [12],

$$\begin{pmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{12} \end{pmatrix} = \begin{pmatrix} C_{11} & C_{12} & 0 \\ C_{12} & C_{22} & 0 \\ 0 & 0 & C_{66} \end{pmatrix} \begin{pmatrix} \varepsilon_{11} \\ \varepsilon_{22} \\ 2\varepsilon_{12} \end{pmatrix}, \tag{23}$$

where Voigt notation has been used for C_{ij} . Here C_{11} (S_{11}), C_{22} (S_{22}), C_{12} = C_{21} (S_{12} = S_{21}), and C_{66} (S_{66}) represent C_{1111} (S_{1111}), C_{2222} (S_{2222}), C_{1122} (S_{1122}), and C_{1212} (S_{1212}), respectively. So, using the previous equations, the in-plane Young's modulus, shear modulus, and Poisson's ratio can be defined as:

$$E(\varphi) = \frac{1}{S_{11}\cos^4(\varphi) + S_{22}\sin^4(\varphi) + (2S_{12} + S_{66})\cos^2(\varphi)\sin^2(\varphi)}$$
(24)

$$v(\varphi) = -\frac{[S_{22} - S_{33} + S_{22}]\cos^2(\varphi)\sin^2(\varphi) + S_{12}\cos^4(\varphi) + S_{12}\sin^4(\varphi)}{[2S_{12} + S_{66}]\cos^2(\varphi)\sin^2(\varphi) + S_{11}\cos^4(\varphi) + S_{22}\sin^4(\varphi)}$$
(25)

$$\frac{1}{G(\varphi)} = [S_{11} + S_{22} - 2S_{12}]\cos^2(\varphi)\sin^2(\varphi) + \frac{1}{4}S_{66}[\cos^4(\varphi) + \sin^4(\varphi) - 2\sin^2(\varphi)\cos^2(\varphi)]$$
 (26)

2.3 2.3. Basic proprieties and averaging schemes

From elastic constants, other basic elastic properties, including elastic moduli, can be obtained. The elastic response of an isotropic system is generally described by the *B* and the *G*, which may be obtained by averaging the single-crystal elastic constants. The averaging methods most often used are the Voigt [13], Reuss [14] and Hill [7] bounds. In Voigt's and, Reuss's approximations, the equation takes the following form:

$$B_{V} = \frac{1}{9}([C_{11} + C_{22} + C_{33}] + 2[C_{12} + C_{23} + C_{31}]),$$

$$G_{V} = \frac{1}{15}([C_{11} + C_{22} + C_{33}] - [C_{12} + C_{23} + C_{31}] + 4[C_{44} + C_{55} + C_{66}]),$$

$$B_{R} = \frac{1}{9}([S_{11} + S_{22} + S_{33}] + 2[S_{12} + S_{23} + S_{31}]),$$

$$G_{R} = \frac{1}{15}([S_{11} + S_{22} + S_{33}] - 4[S_{12} + S_{23} + S_{31}] + 3[S_{44} + S_{55} + S_{66}]).$$
(27)

Also, the arithmetic mean of the Voigt and Reuss bounds, termed the Voigt-Reuss-Hill (VRH) average is also found as a better approximation to the actual elastic behavior of a polycrystal material,

$$B_{VRH} = \frac{1}{2}(B_V + B_R),$$

$$G_{VRH} = \frac{1}{2}(G_V + G_R)$$
(28)

The Young's modulus (E), and Poisson's ratio (v) for an isotropic material are given by:

$$E = \frac{9BG}{3B+G}, \quad \nu = \frac{3B-2G}{2(3B+G)}.$$
 (29)

The elastic anisotropy is a crucial measurement of the anisotropy of chemical bonding and can be calculated by elastic constants. For all crystal systems, the bulk response is in general, anisotropic, and one must account for such contributions to quantify the extent of anisotropy accurately. For this purpose, Ranganathan et al. [5] introduce a new universal anisotropy index (A^U) ,

$$A^{U} = 5\frac{G_{V}}{G_{R}} + \frac{B_{V}}{B_{R}} - 6. {30}$$

It is noteworthy that in weakly anisotropic materials, i.e. isotropic material, all such averages lead to similar results for elastic moduli. The mechanical behavior such as ductile or brittle can be represented by the ratio of the G to the B, i.e., the Pugh ratio G/B, by simply considering B as the resistance to fracture and G as the resistance to plastic deformation. The critical value of the Pugh ratio to separate ductile and brittle materials is around 0.57. If G/B < 0.57, the material is more ductile; otherwise, it behaves in a brittle manner [1, 15]. Hence, a higher Pugh ratio indicates more brittleness property. Cauchy pressure (P_c) is another characteristic to describe the brittleness and ductility of the metals and compounds and is defined [16] by:

$$P_c = C_{12} - C_{44} \tag{31}$$

For covalent materials with brittle atomic bonds, the P_c is negative, because in this case, material resistance to shear strain, i.e., C_{44} , is much more than that for volume change, i.e., C_{12} . However, the P_c must be positive for the metallic-like bonding, where the electrons are almost delocalized. For an isotropic crystal, A^U is zero. The departure of A^U from zero defines the extent of the elastic anisotropy.

In this work, the relation among the E, G, v, and elastic stiffness constants for a 2D system are derived as,

$$E_{x} = \frac{C_{11}C_{22} - C_{12}C_{21}}{C_{22}},$$

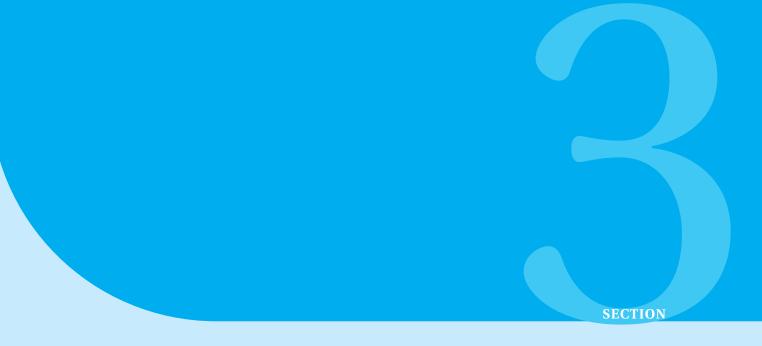
$$E_{y} = \frac{C_{11}C_{22} - C_{12}C_{21}}{C_{11}},$$

$$v_{xy} = \frac{C_{21}}{C_{22}},$$

$$v_{yx} = \frac{C_{12}}{C_{11}},$$

$$G_{xy} = C_{66},$$
(32)

where $E_l = \sigma_l/\varepsilon_l$ is Young's modulus along the axis of l. $v_{lk} = -d\varepsilon_k/d\varepsilon_l$ is the Poisson's ratio with tensile strain applied in the l direction and the response strain in the k direction. G_{xy} is the shear modulus in the xy-plane.



Workflow of ElATools

For this section, please refer to our paper.

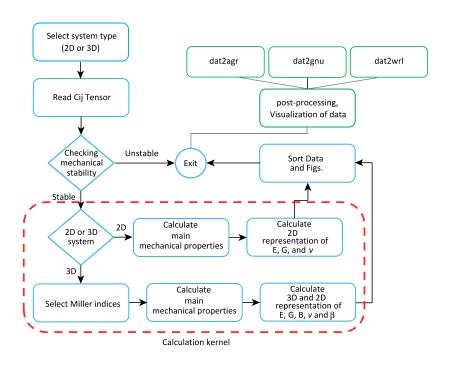


Figure 2: The flowchart of ElATools. The red dashed line represents the Calculation Kernel (CK) block.



Getting started

4.1 How to obtain ElATools

ElATools is an open source code with MIT license and can be downloaded by sending an email to yalameha930gmail.com [Shahram Yalameha]

4.2 How to install ElATools

ElATools is written in Fortran90 and is installed with Intel Fortran (ifort) or gnu fortran (gfortran) compiler. But before the installation of ElATools, the necessary libraries and packages should be installed first: GNUPLOT, LAPACK, and LaTeX libraries. LAPACK libraries are for numerical calculations and are used to calculate elastic compliance constant and so on. LaTeX and GNUPLOT are used to plot temporary figures and the post-processing stages. One of the packages IRelast, Elast, AELAS, and ElaStic can calculate the elastic stiffness constant (C_{ij}). ElaTools supports the output of these packages.

ElATools is distributed in a compressed tar file elatlools_1.**.tar.gz, which uncompresses into several directories: soc, doc, db, and bin. The soc directory contains the f90 files and Makefile. For the compilation, you need to modify Makefile for your system. The doc directory contains a copy of this paper, short userguide, and the examples directory. The db directory contains the elastic constant database file. The path of these files must be specified before installation. For this purpose, you can use run_path.sh script to path these files. This script is located in the soc directory and runs as follows:

chmod +x run_path.sh; ./run_path.sh

Then you need the complete path (example: /home/.../soc/db/) of the elastic constant

database files (Cijs.binery and All_2ID_cop.csv) in the db directory, which is different for the user system.

After installation, which is done with make command, the executable files (EIATools, dat2gnu, dat2agr, and dat2wrl) are saved in bin directory. Finally, the code will run by executing EIATools. You can put this path to the system PATH with

```
export PATH=/home/.../elatools_1.**/bin:$PATH to the .bashrc file in your home directory.
```

4.3 How to use ElATools

You must prepare one of the following files for C_{ij} tensor:

INVELC-matrix: output file of IRelast

elast.output: output file of Elast ELADAT: output file of AELAS

ElaStic_2nd.out: output file of ElaStic

Cij.dat (3D system) or Cij-2D.dat (2D system) file for any other outputs.

After the preparation of these files, you can just run ElATools.

4.4 Run ELATools and Results data

After running El*A*Tools, you must follow the steps below:

1) Welcome

2) Select 2D or 3D crystal system:

If you want to analyze a monolayer, you must have one of files ELADAT or Cij-2D.dat in the executable directory.

If you choose the 3D system, we will have

4) Calculate phase and group velocities.

```
> Want to calculate phase and group velocities? (Y/n)
```

This option has been entered in the code since version 1.5.0. If you select this option we will have:

```
> Want to calculate phase and group velocities? (Y/n)
y
Density of Compound (kg/m^3):
note: If you don't know, enter 0
```

You need to know or calculate the density of compound. If you know the density of the compound, enter its value, otherwise enter the number 0. If you enter the value 0, the program calculates the density of the composition by taking the crystal lattice parameters from you.

4.4.1 Calculation Kernel (CK)

To explain this section, we analyze the GaAs Cubic compound. Cij tensor of this compound (in Cij.dat file) is equal to:

Also, the density of this compound is 5307 kg/m^3 .

Before entering step CK, ElATools examines the mechanical stability condition. As can be seen, it is marked in green color. It then calculates and displays the S_{ij} , calculating the main properties.

After this process, you need to specify the meshes of ϕ and θ angles. We recommend 150 for both angles.

```
> Select the (hkl) Miller indices for 2D cut:
```

After determining the meshing, selecting hkl-plane ((100)-plane was selected as an example) to calculate the 2D projection is the next step. This is the last step in entering the input commands to go to CK.

At the end of CK step, the minimum and maximum value of properties and their coordinates and anisotropic index (A_M) are calculated and displayed. These results are also stored in DATA.dat file.

4.4.2 Temporary images

After passing CK step, you will be asked to plot temporary images.

```
#======#
> Do you want to plot data? (Y/N):
```

By accepting this request, temporary images are plot and stored in a folder called PicFile-hkl (here, hkl is 100). The data files for post processing step are also listed in DatFile-hkl folder, and **END**.

SECTION

Post processing

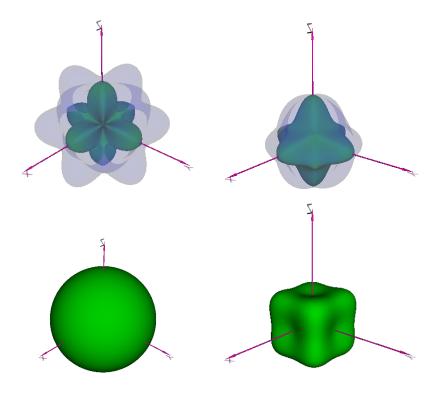
In the post-processing, three powerful program dat2gnu, dat2agr and dat2wrl are designed to visualize these results, which produce files in gpi, agr and wrl formats, respectively.

5.1 dat2wrl

dat2wrl is prepared for 3D graphical representations of elastic properties, capable of producing files in "wrl" format. This format can be visualized and explored with a VRML capable browser, such as View3dscene [8]. Input commands and output files for this program:

Input command to run	Properties	Ouput file	
dat2wrl poi	Poisson's ratio	Poisson.wrl	
dat2wrl shear	Shear modulus	Shear.wrl	
dat2wrl young	Young's modulus	Young.wrl	
dat2wrl bulk	Bulk modulus	Bulk.gpi	
dat2wrl comp	Linear compressibility	Compress.wrl	
dat2wrl pp	Phase velocity: P-mode	Phase-P.wrl	
dat2wrl ps	Phase velocity: Slow-mode	Phase-Slow.wrl	
dat2wrl pf	Phase velocity: Fast-mode	Phase-Fast.wrl	
dat2wrl gp	Group velocity: P-mode	Group-P.wrl	
dat2wrl gs	Group velocity: Slow-mode	Group-Slow.wrl	
dat2wrl gf	Group velocity: Fast-mode	Group-Fast.wrl	
dat2wrl pfp	Power Flow angle (PFA): P-mode	Power-Flow-P.wrl	
dat2wrl pfs	Power Flow angle: Slow-mode	Power-Flow-Slow.wrl	
dat2wrl pff	Group velocity: Fast-mode	Power-Flow-Fast.wrl	

Some output files are displayed by View3dscene software:



5.2 dat2gnu

dat2gnu is responsible for generating files for 2D projections and 2D heat mapes representations of elastic properties, and generate files in "gpi" format, which can be run by

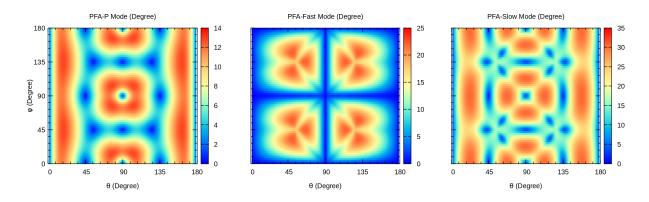
GNUPLOT program. Input commands and output files this program for 3D materials:

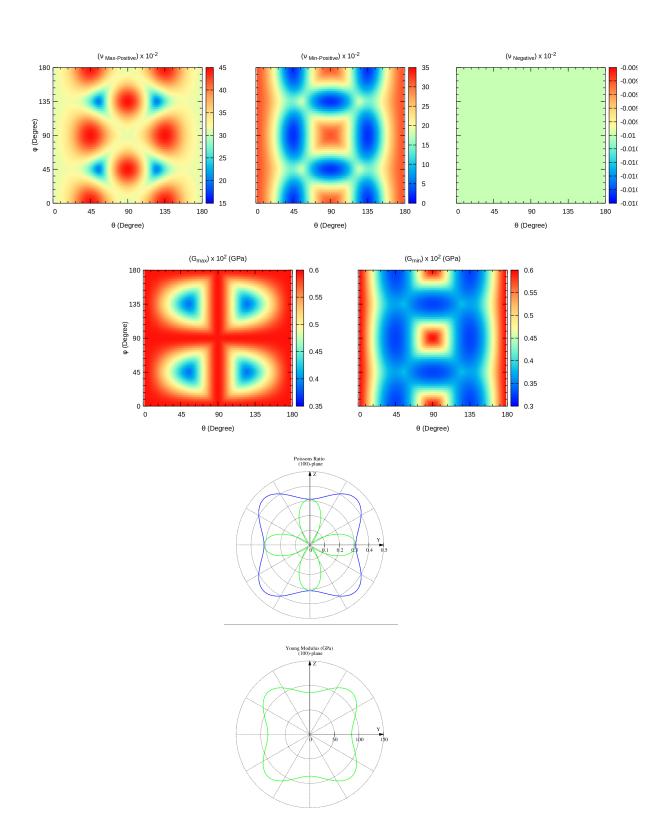
Input command to run	Properties	Ouput file	
dat2gnu poi	Poisson's ratio	poissons.gpi	
dat2gnu shear	Shear modulus	shear.gpi	
dat2gnu young	Young's modulus	young.gpi	
dat2gnu bulk	Bulk modulus	bulk.gpi	
dat2gnu comp	Linear compressibility	compressibiliy.gpi	
dat2gnu pp	Phase velocity: P-mode	phase-p.gpi	
dat2gnu ps	Phase velocity: Slow-mode	phase-slow.gpi	
dat2gnu pf	Phase velocity: Fast-mode	phase-fast.gpi	
dat2gnu gp	Group velocity: P-mode	group-p.gpi	
dat2gnu gs	Group velocity: Slow-mode	group-p.gpi	
dat2gnu gf	Group velocity: Fast-mode	grouphase-p.gpi	
dat2gnu pall	Phase and PFA: all-mode	phase.gpi	
dat2gnu gall	Group and PFA all-mode	group.gpi	
dat2gnu hmpoi	2D heat mape of Poisson's ratio	poissons_smap.gpi	
dat2gnu hmcomp	2D heat mape of Linear compressibility	compressibiliy_smap.gpi	
dat2gnu hmshear	2D heat mape of Shear modulus	shear_smap.gpi	
dat2gnu hmbulk	2D heat mape of Bulk modulus	bulk_smap.gpi	
dat2gnu hmyoung	2D heat mape of Young's modulus	young_smap.gpi	
dat2gnu hmpall	2D heat mape of Phase velocity: all-mode	phase_smap.gpi	
dat2gnu hmgall	2D heat mape of Group velocity: all-mode	group_smap.gpi	
dat2gnu hmpfall	2D heat mape of PFA: all-mode	powerflow_smap.gpi	

Input commands and output files this program for 2D materials:

Input command to run	Properties	Ouput file
dat2gnu 2dpoi	Poisson's ratio	2Dpoissons.gpi
dat2gnu 2dyoung	Young's modulus	2Dyoung.gpi
dat2gnu 2dshear	Shear modulus	2Dshear.gpi
dat2gnu 2d	Generate all propreites	2Dshear/2Dyoung/2Dpoissons.gpi

Some output files are displayed by GNUPLOT software:



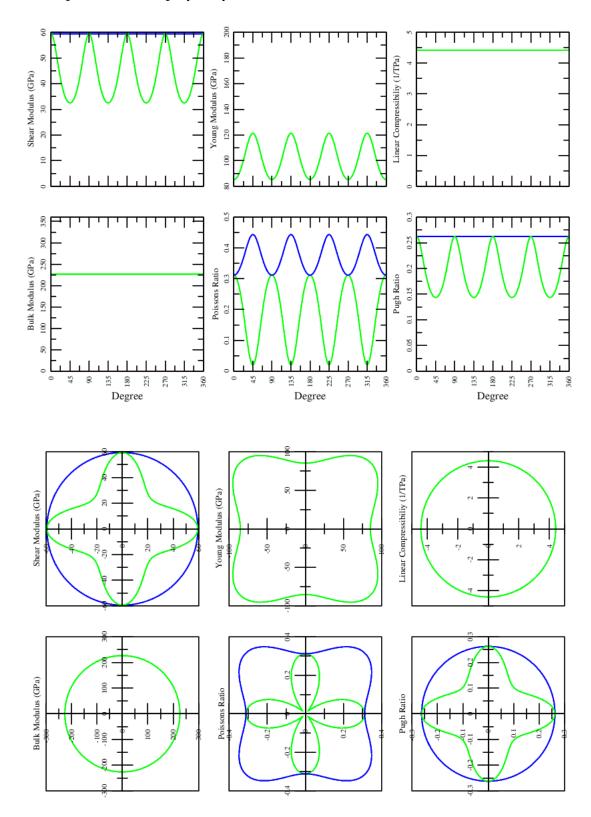


5.3 dat2agr

dat2agr is responsible for generating files for 2D projections representations of elastic properties, and generate files in "agr" format, which can be run by XMGRACE program. Input commands and output files this program for 3D materials:

Input command to run	Properties	Ouput file	
dat2agr box	All elastic properties in Cartesian coordinates	2Dbox.agr	
dat2agr polar	All elastic properties in polar coordinates	2Dpolar.agr	

Two output files are displayed by XMGRACE software:



SECTION

References

- [1] P. Saeidi, S. Yalameha, and Z. Nourbakhsh, Physics Letters A 383, 221 (2019).
- [2] A. Jain, S. P. Ong, G. Hautier, W. Chen, W. D. Richards, S. Dacek, S. Cholia, D. Gunter, D. Skinner, G. Ceder, et al., Apl Materials 1, 011002 (2013).
- [3] A. Marmier, Z. A. Lethbridge, R. I. Walton, C. W. Smith, S. C. Parker, and K. E. Evans, Computer Physics Communications 181, 2102 (2010).
- [4] R. Gaillac, P. Pullumbi, and F.-X. Coudert, Journal of Physics: Condensed Matter 28, 275201 (2016).
- [5] S. I. Ranganathan and M. Ostoja-Starzewski, Physical Review Letters 101, 055504 (2008).
- [6] C. M. Kube, AIP Advances 6, 095209 (2016).
- [7] R. Hill, Proceedings of the Physical Society. Section A 65, 349 (1952).
- [8] M. Kamburelis and other Castle Game Engine developers, View3dscene (2020), URL https://castle-engine.io/view3dscene.php.
- [9] G. D. Team, Grace (2008), URL https://plasma-gate.weizmann.ac.il/Grace/.
- [10] P. K. Janert, Gnuplot in action: understanding data with graphs (Manning, 2010).
- [11] J. F. Nye et al., Physical properties of crystals: their representation by tensors and matrices (Oxford university press, 1985).

- [12] T. Zhao, S. Zhang, Y. Guo, and Q. Wang, Nanoscale 8, 233 (2016).
- [13] W. Voigt et al., Lehrbuch der kristallphysik, vol. 962 (Teubner Leipzig, 1928).
- [14] A. Reuss, Z. Angew. Math. Mech 9, 49 (1929).
- [15] S. Pugh, The London, Edinburgh, and Dublin Philosophical Magazine and Journal of Science 45, 823 (1954).
- [16] D. Pettifor, Materials science and technology 8, 345 (1992).