## Vlastnosti a slovník Z-transformace

| Obraz   | Předmět                                   |
|---|---|
| $F(z) = \mathcal{Z}[f_n] = \sum_{n=0}^{\infty} \frac{f_n}{z^n}$ | $f_n = \mathcal{L}^{-1}\left[F(z)\right]$ |
| $\frac{1}{z^k}F(z)$   | $f_{n-k}$                                 |
| $z^k F(z) - z^k \sum_{m=0}^{k-1} \frac{f_m}{z^m}$               | $f_{n+k}$                                 |
| $F(\frac{z}{a})$  | $a^n f_n  (a \neq 0)$                     |
| -zF'(z)   | $nf_n$                                    |
| $(z-1)F(z) - zf_0$  | $\Delta f_n$                              |
| $(z-1)^k F(z) - z \sum_{m=0}^{k-1} (z-1)^{k-m-1} \Delta^m f_0$  | $\Delta^k f_n$                            |
| $\frac{F(z)}{z-1}$  | $\sum_{k=0}^{n-1} f_k$                    |
| $\int_{z}^{\infty} \frac{F(\xi)}{\xi} d\xi$                     | $\frac{f_n}{n}$ $(n \ge 1)$               |
| $F(z) \cdot G(z)$   | $f_n * g_n = \sum_{k=0}^n f_k g_{n-k}$    |
| 1   | $\delta_n$                                |
| $\frac{z}{z-1}$   | 1   |
| $\frac{z}{z-a}$   | $a^n$                                     |
| $\frac{z}{(z-1)^2}$   | n   |
| $\frac{az}{(z-a)^2}$  | $n a^n$                                   |
| $\frac{z(z+1)}{(z-1)^3}$  | $n^2$                                     |
| $\frac{z}{z^2+1}$   | $\sin n \frac{\pi}{2}$                    |
| $\frac{z^2}{z^2+1}$   | $\cos n \frac{\pi}{2}$                    |
| $\frac{z\sin b}{z^2 - 2z\cos b + 1}$                            | $\sin bn$                                 |
| $\frac{z(z-\cos b)}{z^2 - 2z\cos b + 1}$                        | $\cos bn$                                 |
| $\frac{az\sin b}{z^2 - 2az\cos b + a^2}$                        | $a^n \sin bn$                             |
| $\frac{z(z-a\cos b)}{z^2 - 2az\cos b + a^2}$                    | $a^n \cos bn$                             |