

# NMMB430 - DÚ 3

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## 1

We will proceed by calculating  $[2]P, [2]P + [2]P = [4]P$  (doubling) and finally  $[4]P + P = [5]P$  (addition).

$[2]P$ :

$$\begin{aligned}\gamma_1 &= 20, \gamma_2 = 5, \gamma_3 = 8 \\ \implies [2]P &= (20 : 5 : 8)\end{aligned}$$

$[4]P$ :

$$\begin{aligned}\gamma_1 &= 18, \gamma_2 = 4, \gamma_3 = 4 \\ \implies [4]P &= (18 : 4 : 4)\end{aligned}$$

$[4]P + P$ :

$$\begin{aligned}U &= 0, W = 0, V = 26 \\ \implies [5]P &= (0 : -4 : 4)\end{aligned}$$

Since  $4^{-1} = 8$  we get that  $[5]P = (0 : -4 : 4) = (0 : -1 : 1)$  i.e.  $[5]P = (0, -1) = (0, 30)$  in affine coordinates.