Project 2. Find the Girth of an Undirected Graph

(Due 4/21-28/2018 Sun)

Description:

In this project, we will process an undirected graph, not necessarily connected. The *girth* of a graph is the *length* of a shortest cycle in this graph. After you find the girth, you also need to produce the cycle that corresponds to the girth.

Requirements:

- 1. (*Input*) The input comes from a text file that stores the *adjacency matrix* of a graph. Your program will take the file name of an input as a command-line argument. Then your program will read the content of the file line by line, in which each row corresponds to one row of the adjacency matrix of a graph.
- 2. (Validation) Before we process the graph, we need to validate the data to make sure that the given data corresponds to the adjacency matrix of a graph. Basically we need to check the following items:
 - (Square Matrix)

Each row of the data file has a sequence of integers separated by a space character. Make sure that the number of rows equals the number of columns. Otherwise display an error message.

• (Bit Value Entries)

Check if each entry of the matrix takes the bit value: 0 or 1. If not, display an error message.

• (No Self-Loops)

Since an undirected graph cannot have any self-loop, we need to check that all the diagonal entries must be 0. Otherwise display an error message.

• (Valid Undirected Graph)

In order to make sure that this matrix corresponds to the adjacency matrix of an undirected graph, you need to check if it is *symmetric*. If not, display an error message.

3. (Find the Girth) After you pass the data validation, you design an algorithm to calculate its girth and its corresponding shortest cycle. In this project, the performance of your algorithm is not very important, if only you get a correct answer.

• Hint

You can use the *Breadth-First Search* algorithm to calculate it. You need a way to find the length of the cycle. You may need to modify the original *Breadth-First Search*.

- 4. (Output) After you get the answer, you need to output the girth of the graph. Other than that, you also need to print out this shortest cycle as a sequence of vertex numbers.
- 5. (*Testing*) You need to prepare your own testing files for your project development. I will use my own testing files for grading. (I will post my testing files for your checking.)