

# IQR Report

## (Outlier, Replacing)

### Reason of multiplying 1.5 with IQR

- Multiplying 1.5 with the interquartile range (IQR) is a common technique used in statistics to identify outliers using the concept of the “Tukey method” or “Tukey’s fences”.
- The interquartile range is a measure of statistical dispersion, representing the range between the first quartile (25<sup>th</sup> Percentile) and the third quartile (75<sup>th</sup> Percentile) of the dataset.

Tukey’s Fences : Tukey’s fences are thresholds used to define the bounds beyond which data points are considered outliers. These fences are calculated as follows:

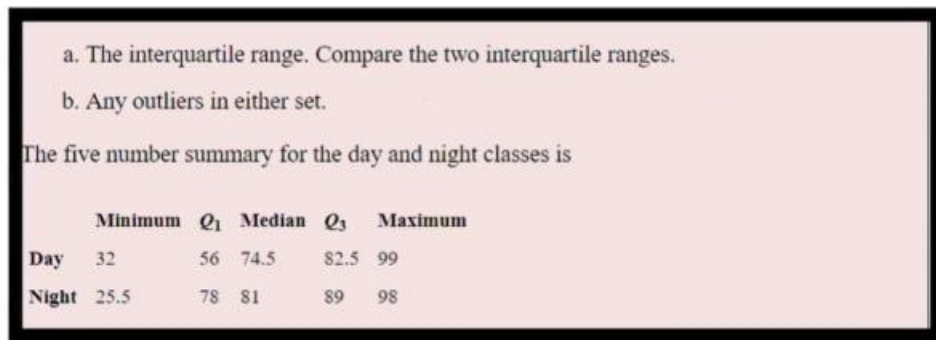
Lower Bound:  $(Q1 - 1.5 * IQR)$

Upper Bound:  $(Q3 + 1.5 * IQR)$

- The choice of 1.5 as the multiplier is somewhat arbitrary but is widely accepted as a balance between detecting genuine outliers and not excessively labelling data points as outliers.
- This value provides a reasonable compromise between sensitivity to potential outliers and the risk of falsely identifying normal data points as outliers.
- John Tukey, a prominent statistician, introduced this method as part of exploratory data analysis. While

other multipliers can be used, 1.5 has become a standard in many statistical analyses due to its effectiveness in identifying potential outliers without overly inflating the outlier count.

Example:



a. The interquartile range. Compare the two interquartile ranges.  
b. Any outliers in either set.

The five number summary for the day and night classes is

	Minimum	$Q_1$	Median	$Q_3$	Maximum
Day	32	56	74.5	82.5	99
Night	25.5	78	81	89	98

Solution:

$$\text{IQR} = Q_3 - Q_1 = 82.5 - 56 = 26.5$$

$$\text{IQR} = 26.5$$

Lesser Range Outlier:

$$Q_1 - 1.5(\text{IQR}) = 16.25$$

Greater Range of Outlier:

$$Q_3 + 1.5(\text{IQR}) = 82.5 + 1.5(26.5)$$

$$= 82.5 + 39.75$$

$$= 122.75$$

$$Q_3 + 1.5(\text{IQR}) = 122.75$$

Conclusion:

Day and Night classes lower than 16.25 are lesser range outliers and classes higher than 122.25 are higher range outliers.

