1. Answer. O) E-step: PLUX, T, B) & PLXL, B) · PLUTY X TPINI (a, Da) PLGITY, Zi = E PINI(a, Da) PCCITY).  $P(C(X), \pi, \theta) = \frac{n}{i!} \frac{p(X)(G, \theta; i) P(G(\pi))}{Z_i}$ In pix |T, O) = = = 200 ln pix, c|T, O) + = 200 ln pix, c) : 9(4) = PLYT, X, O) => = 9(4) = = 1 P(4) xi, T, Day L(π, 0) = = = Eq (h (Xi, Ci)π, O)] + conct. = E = 2 (ci=i) ch postci=i, e) + (n poci=i) Ti) = = = = dici) (h ( thi) dx (1-di) = x1 ] +h [ ] + const, = = = Disj) Ch Go + Achd + (20-85) h cl-9 1 + h T ] + wist. Φίψ = - q((i=i) = - (1) (θi) × (20- χή - θ) (2). M-stp: VO, L = D.

$$\frac{1}{\sum_{i=1}^{N} \frac{1}{\sum_{i=1}^{N} \frac{1}$$

Psedu - code:

Input: Puta X1, ..., Xn. K christas.

Output: parameter  $\pi$ ,  $\theta$ , and cluster distributions  $\theta ij$ .

1. Initialize To, do in some way.

2. for iteration ==1, ..., T.

(a). E - step: for  $i = 1, \dots, n$ ;  $j = 1, \dots, K$ .  $\psi_{i}^{(t)}(j) = \frac{\pi_{i}^{(t-1)} \left(\frac{20}{\pi_{i}^{t}}\right) \left(0, \frac{t}{j}\right)^{x_{i}}}{\left(\frac{20}{\pi_{i}^{t}}\right)^{x_{i}} \left(\frac{20}{\pi_{i}^{t}}\right)^{x_{i}}} \left(\frac{20}{\pi_{i}^{t}}\right)^{1-x_{i}}}$ 

(2)  $M - \text{step}: N_{3}^{t} = \underbrace{\sum_{i=1}^{n} \phi_{i}^{t}(i)}_{20} \cdot XL = \underbrace{\sum_{i=1}^{n} \phi_{i}^{t}(j)}_{20} \cdot XL = \underbrace{\sum_{i=1}^{n} \phi$ 

3. Calculate  $L(\pi, \theta) = \ln p/s/\pi, \theta$ , for each iteration, to access convergence of object function.

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2. Answar:
We first factorize quality = quality quality quality quality
P(X/C, T, D) = ( T. P/XICi, O) PCCITIPIOCO ) POT.
MP(X/C/T/B)= 三三1 (G=j) (Mp(xilBj) + M(Tj)]+ 其(Mp(引)) + Mp(T).
Assume:
QCR) ~ Dirichlet (di', ..., dk).
9(0k) ~ Beta (a', b')
9 cCi) ~ Discote CT)
QCCi=j) & exp { Ex (h p(x, c, x, 0) ]}
       ~ exp {E-g [mp(xi | Ci, O) + ln (ci | TL)]}
       ~ exp { Eq ( h ( G) B; x; L1-B) 20-x; + h = ] }
       ~ exp { xi Eq (h)) + (20-xi) Eq [h(1-0)] + Eq (h)[) }
        9000 × 0xp { E-2 (hprx, c, n, 0) ]}
      ~ exp. { E-g(lm pix/c, 0) + lnp(0)]}
      derp { En [hprxi] (i, bj) thp(bj)]}
      又中分子主(ximbi + co-xijh(l-bj)]) 中p(bj)
      又ep {(三xidill) + ao -1 ) ln Bi + 1 三中山 (20-xi) + bo -1 ) ln (1-Bi) }
       マウィーカントを(1) ナ (1-ひ) かちこいへんから) ナ.
 · 自 = 00十三年的加,的 = 如十三年的 (20 - N)
qui) a exp { Eq Emp (x, C, T, D)]}
    スの中{Er Eh PCCIで thipony]}
スの中{A データにリルで、ナラス (3-1) 加了}
スの中{A データにリルで、ナラス (3-1) 加了}
 が一方十分。
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Pesulo - cole:
   1. Inputs: Puta and definitions 210), 900, 9001, 9001
  2 autputs: parameters O; bi, di for j=1,..., K
        For iteration t=1,..., T
            c). Update 2001 = j) by setting Quis = exp[x2(460),41) -4(0),41+bj,47)]
                                                                                                   + W-xi) (4 (bi,+1) - 4 (0i,+1 + bi,+-1)] + 4 (di,+1) - 4 (\frac{1}{2} \lambda_{\text{t}} \text{ty})
            (2) Update 9(0) by setting 0, t = 0.0 + \frac{1}{2}X(0); bit = bo +\frac{1}{2}(20-8i) 0
            (3). Update 951 by setting 51, t = 20+ 11, 15 = = $\frac{1}{27} \phi(y), +1.
4. Evaluatie L CC, ai, bé, di) to access unvergence
             L = Eq (h pix, c, T, O) - lng(c, T, O)]
                        = E(=== ( m 1 %) + xim & + (20-86) m(1-4),]
                         + 电气温温加户(证=引元]]
                         + Eq Chipery]
                        + for ( ) I hp(0)]
                      · Eq ( 是是 h bid)]
                        - Eq [ H 2(0)]
                        - Eg & mgiT/]
十三年的(1)(1)(1)(1)(1)(1)
                    + (1) -1) 上(4(1),七) - 4(長点七月
                     + = {(a-1) (4(9,+) -4(9,+) -4(9,+)] + (b-1) (4(9,+) -4(0,+) + bi+)]
                    - = = = ( (bis) la (bis)
                   - \{ \(\alpha\) \(\beta\) 
                    - 美 (d) + -1 (4 (d) + ) - 4 (表 ) + 1] -In(B(a))
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3. Answer:

(1). Sompling  $\theta$ :

(2). P(0;1 X, C, 0; )  $\Rightarrow$  p(x|0; C) p(0; D)  $\Rightarrow (x_{ij}^{T}|p(x)|0; D) = p(0) \quad \text{for} \quad y_{ij} > 0.$ (2) If  $y_{ij} < 0$ ,  $p(0; D_{ij}, C_{ij}, D_{ij}) = p(0)$ (2) Sompling C:  $p(C_{ij} = j| X_{ij}, C_{ij}) \Rightarrow p(X_{ij} = j| C_{ij}) = p(0).$ (2) For  $y_{ij}^{T} > 0$ ,  $p(C_{ij} = j| X_{ij}, C_{ij}) \Rightarrow p(X_{ij} = j| C_{ij}) = p(X_{ij} = j| X_{ij}, C_{ij})$ (1) For  $y_{ij}^{T} = 0$ ,  $p(C_{ij} = naw) = p(X_{ij} = j| X_{ij} = j| X_{ij} = p(X_{ij} = j| X_{ij}, C_{ij}) =$ 

$$\int \text{ for } N_j^{-1} > 0, \quad P(G_i = j \mid X, 0, C_i) \propto P(X \mid D_i) S \frac{1}{3+n-1}. \quad ((K \rightarrow 0), \frac{1}{2K} \rightarrow 0)$$

$$\int \text{ for } N_j^{-1} = 0, \quad P(G_i = naw) \times (0, C_i) = \sum_{j: N_j^{-1} = 0} P(G_i = j \mid X, 0, C_i).$$

$$\int \text{ lim } \sum_{k \rightarrow 0} \frac{1}{j: N_j^{-1} = 0} \frac{1}{j! N_j^{-1}} \frac{1}{j! N_j^{-1}} = \frac{1}{3+n-1} \int P(X \mid D_j) \frac{1}{j! N_j^{-1}} \frac{1}{j! N_j^{-1}} = \frac{1}{3+n-1} \int P(X \mid D_j) \frac{1}{j! N_j^{-1}} \frac{1}{j! N_j^{-$$

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Psalu - wde:
 Input: Putu x1, 5-1, 8n.
 Intput - K, parameter & Dis
 1. Initialize in some way. (We can set ci=1 for i=1,...,n), Q, ~p(d).
 2. For iteration +=1,..., T, re-inlex cluster go from 1 to K(+1)
    (w). for i=1,..., n:
         For all i that ni >0,
                    $2 (1) = post (8) 15-2 / (2+n+1).
         For att a now value j',
                      Del') = 3+n+1 Jprs: 10, pros do.
  (b). Harmolise to, and sample the order a from a discrete distribution
      with the posumeter.
  (c) If G=j', generate of ~ p(O(Ki).
3. for j=1, ..., K" generate.
          9; 2p(0) {xi: Ci = j3)
   (K+ = # non-zero clusters that one re-indexed refter completing 2)
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