

$$X_n \times |\Delta^n| \xrightarrow{(1, |\Delta^\varphi|)} X_n \times |\Delta^m| \xleftarrow{(X_\varphi, 1)} X_m \times |\Delta^m|$$

$$(a, x) \mapsto \bullet \longleftarrow (b, y)$$