$$\coprod_{g \in \ker_{n}} |\partial \Delta^{n+1}| \xrightarrow{\coprod_{g \in \ker_{n}} |i^{n+1}|} \coprod_{g \in \ker_{n}} |\Delta^{n+1}| 
\downarrow (a_{g})_{g \in \ker_{n}} \downarrow \qquad \qquad \downarrow \downarrow 
K_{n} \longleftrightarrow K'_{n} \downarrow 
f_{n} \longleftrightarrow X$$