

#### INSTITUTE OF TECHNOLOGY OF CAMBODIA

Graduate School of ITC Master of Data Science



# Temporal Graph Learning with Application to Large-Scale Flight Traffic Prediction

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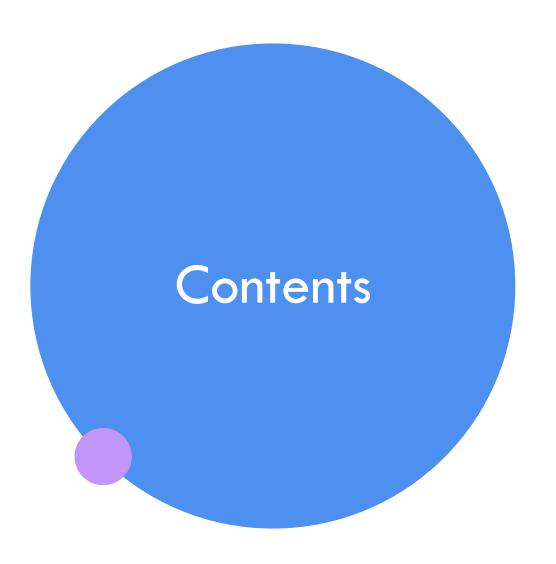
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Dr. HAS Sothea

Dr. NEANG Pheak



2023-2024



Introduction

Literature Reviews

Methodology

Results and Discussions

Conclusions and Future Directions

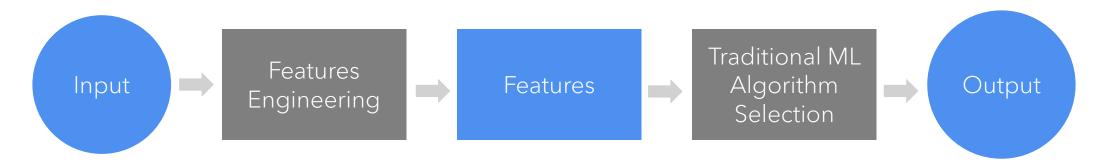
Publication and Acknowledgement

References

# Introduction (1)

Traditional approaches

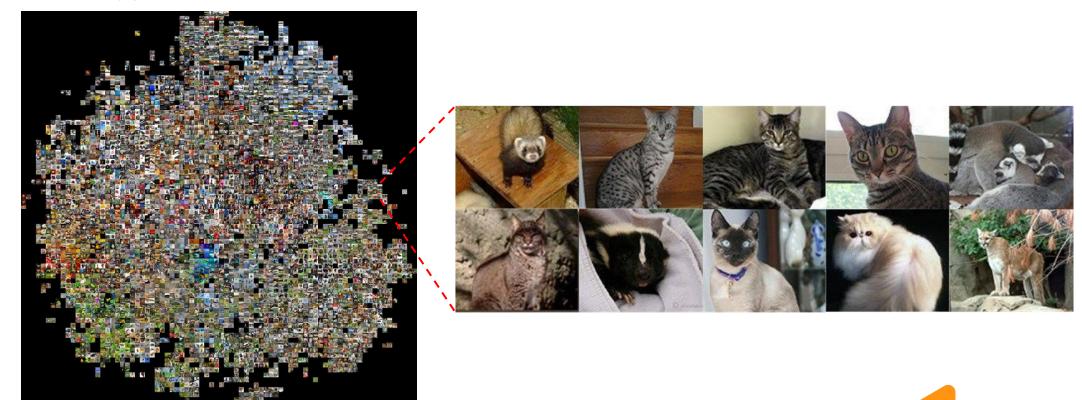
#### Handcrafted Approach:



# Introduction (2)

### The struggle

Handcrafted approach failed:

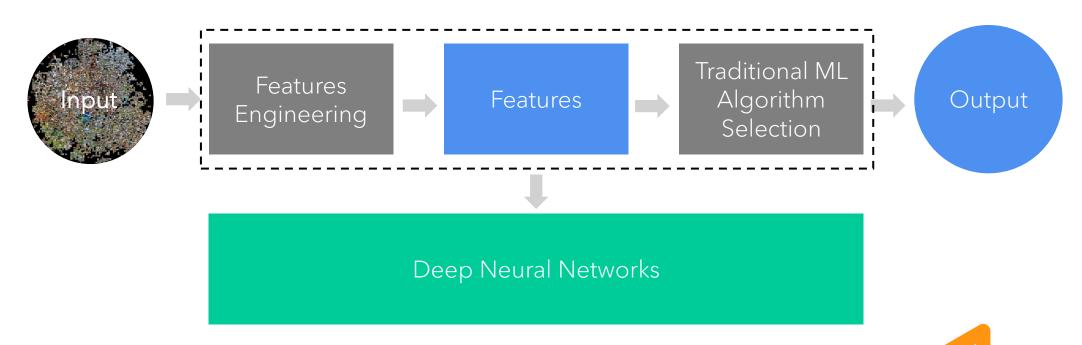


ImageNet [1]
Source: https://cs.stanford.edu/people/karpathy/cnnembed/

# Introduction (3)

The rise of new approaches

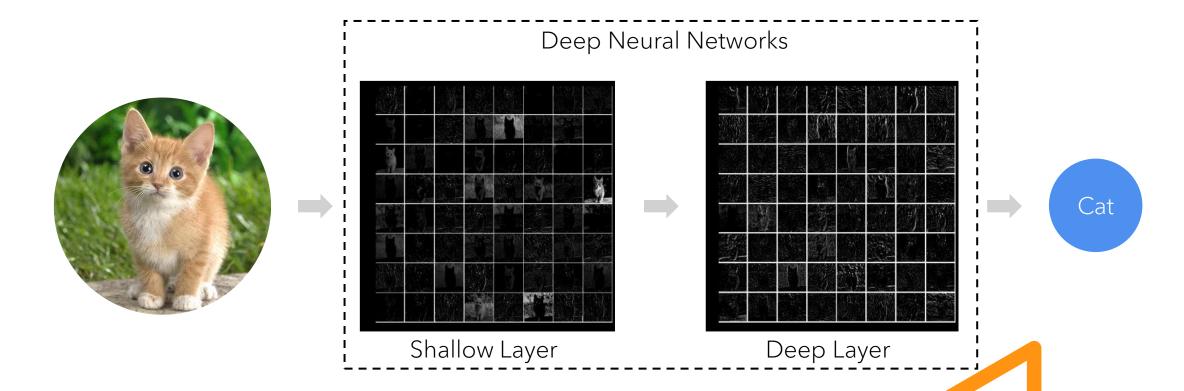
#### Deep Learning Approach:



# Introduction (4)

Into the realm of deep neural network

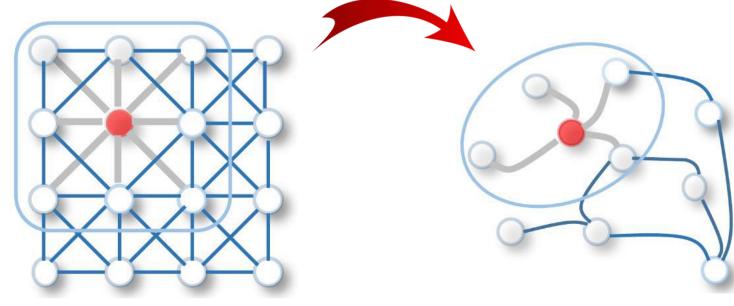
#### Example:



# Introduction (5)

Domain adaptation

### From image to graph:



Source: [2]

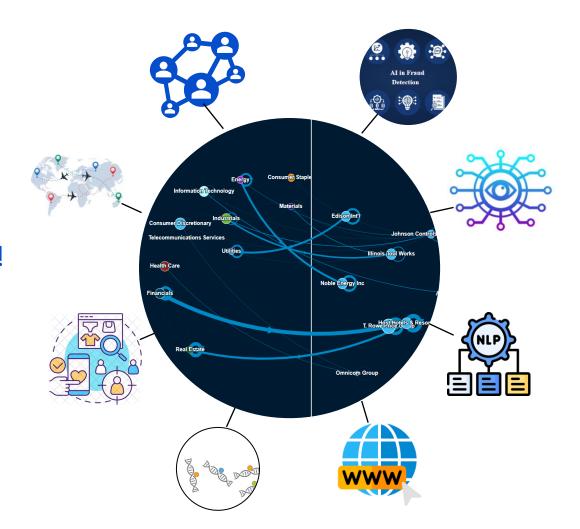
Image Domain (Kernel of CNN)

Graph Domain (Neighborhood of GNN)

# Introduction (6)

Graph applications

Graphs are everywhere!!!



# Introduction (7)

Machine learning on graphs

#### **Graph Modeling**

System of interaction modeled as Graph Networks with entities as nodes and interaction as edges

#### **Graph Machine Learning**

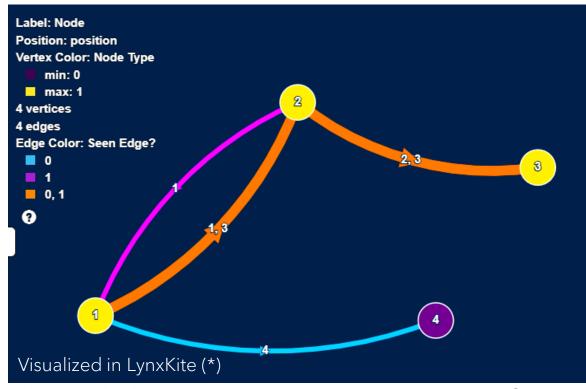
Framework successful in social networks, transportation, recommendation systems

#### Static Assumption Limitation

Existing methods are limited by static assumptions, not applicable to real-world networks

#### Real-World Graphs Example

Directed graph with temporal changes in nodes and edges



# Introduction (8)

**Problem statements** 

#### TGB Dataset<sup>[15]</sup>

67 million edges, a Large-scale crowd-sourced international flight network from 2019 to 2022

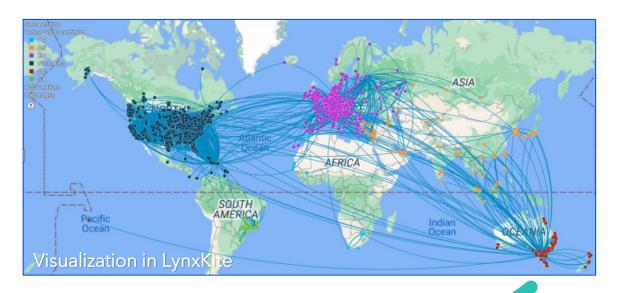
Dataset	#Nodes	#Edges	#Steps
tgbl-flight	18,143	67,169,570	1,385

#### Goals

Future link prediction (Given historical flight routes, predict future flight route)

#### Challenges

High memory and computational requirement.



# Introduction (9)

**Objectives** 

#### Research Questions and Contributions

- [1] How to efficiently analyze large-scale traffic flight prediction?
- [2] Which is the most suitable TGL method? Based on which evaluation method?
- [3] Can we further improve the selected TGL method?
- [4] What is the generalizability of the framework and performance on full dataset?

# Literature Reviews (1)

Static graph Approaches

### GCN<sup>[3]</sup> (Graph Convolutional Network)

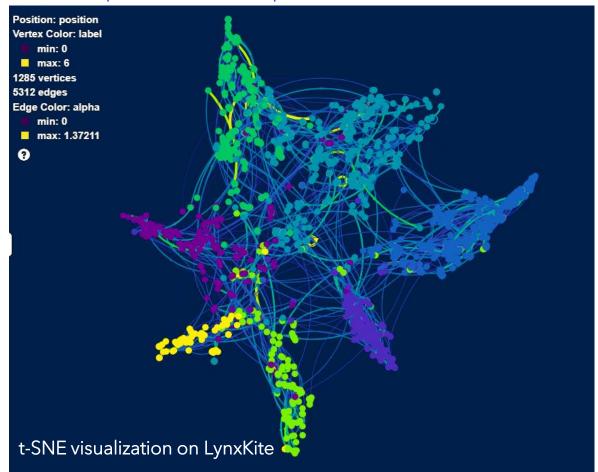
Trasductive learning method by Neighborhood aggregation normalized by node degree.

# GraphSAGE [4] (Sampling and Aggregation)

Generalized GCN to Inductive setting by sampling fixed d-neighbors and aggregating by permutation invariance operator such as mean or max.

### GAT<sup>[5]</sup> (Graph Attention Network)

Each node give different "importance" to their neighborhood. An Example of Cora Graph Classification:



# Literature Reviews (2)

Dynamic (temporal) graph Approaches

# EdgeBank<sup>[6]</sup>

Pure Memory-based evaluation methods

### JODIE<sup>[7]</sup>

Dynamic projection based on user-items (bipartite) interaction and updated by RNN.

### DyRep<sup>[8]</sup>

Temporal point process-based attention mechanism

#### TGAT<sup>[9]</sup>

Generalize GAT to temporal graph by incorporating learnable relative time encoder derived fom Bochner's theorem.

#### **TGN**[10]

Proposed generic TGL framework consists of

- (1) Message Function (2) Message Aggregator
- (3) Memory Updater (4) Node Embedding
- (5) Predictor

# Literature Reviews (3)

Dynamic (temporal) graph Approaches

### DyGFormer<sup>[11]</sup>

Turn graph learning into sequence-based learning by extracting, aligning, and patching first hop neighborhood and feeding into the Transformer. Incorporating neighbor co-occurrence to capture correlation of the neighborhoods.

#### TCL[12]

Use breadth first search (BFS) to extract node embedding, use two streams of attention mechanism to embed pairs of interaction node. Apply cross-attention to learn joinly between both pair of nodes.

#### **CAWN**[13]

Generalized random walk into inductive setting by anonymized node identities. Using RNN to update the node embedding extracted by graph motif.

### GraphMixer<sup>[14]</sup>

Propose a simple MLP-Mixer based architecture with static time encoding function

# Literature Reviews (4)

TGL methods taxonomy

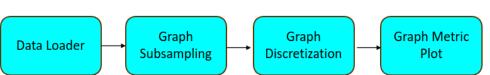
TGL Methods									
	GNN based	Sequence based	graph walk based	None					
Memory Based	JODIE		CAWN	EdgeBank**					
Self-Attention Based	TGAT TCL GAT*	DyGFormer							
Memory and Self- Attention Based	DyREP TGN								
MLP		GraphMixer							
None  (*) Static graph methods. (**)	GraphSAGE* GCN* Purely memory based								

# Methodology (1)

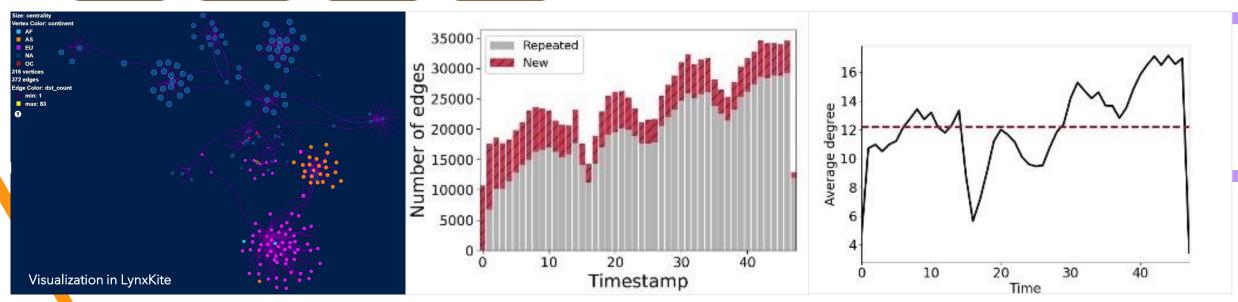
Efficient analysis approach

### Dataset Insight

Perform graph subsampling and timestamp discretization for visualization and Statistics



	Re-occurrence	Novelty	Surprise	Average Degree
Sample Node	0.305	0.36	0.244	12.25



# Methodology (2)

evaluation methods

#### **Traditional Methods**

Binary classification is considered standard

### **Evaluation Tasks**

Link prediction using 50% historical and 50% random negative edges



### TGB Proposal

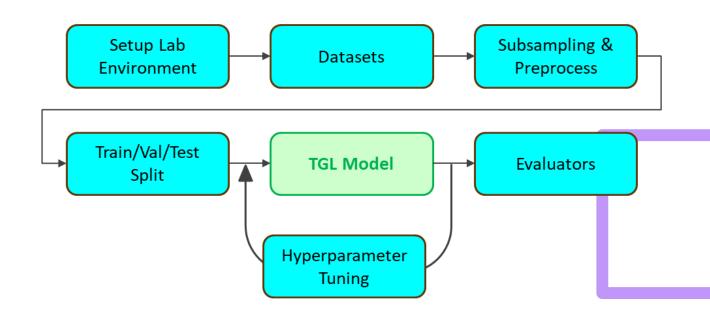
ONE-VS-MANY Rank-based evaluation with Mean Reciprocal Rank (MRR)

# Methodology (3)

**Approaches and Processes** 

# Temporal Graph Learning Pipeline

Scale-up environments for large-size datasets, split into training, validation, and test sets



# Methodology (4)

#### **Model Selection**

### Top performance (MRR):

- DyGFormer: 81%

- GraphMixer: 80.57%

- CAWN: 78.47%

- TGN: 71.01%

- JODIE: 68.95%

### Top Efficiency (Speed):

- EdgeBank (No Training)

- JODIE: 2.223s

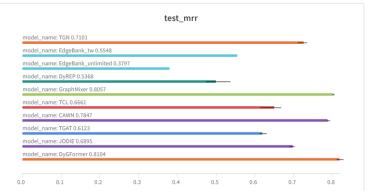
- TGN: 2.649s

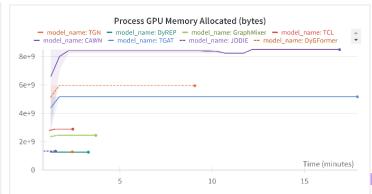
- TCL: 5.586

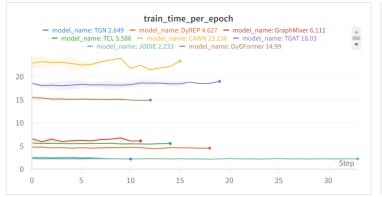
- GraphMixer: 6.111s

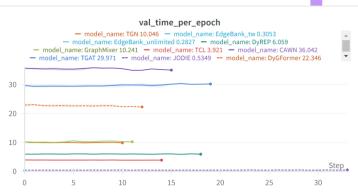
TGN is select to balance the training speed and performance

#### Experiment results of 10 models:









# Methodology (5)

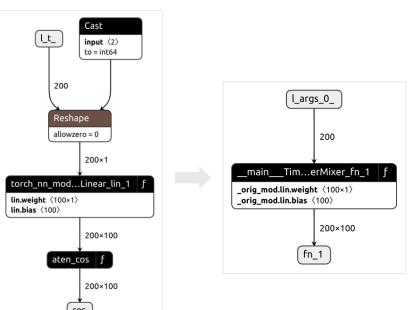
Model insight

#### Model Architecture

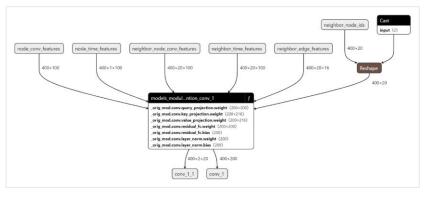
TGN consists of 3 mains modules: Memory Updater, Embedding (b), Decoder (c).

Propose a novel TGN with static time encoder function (a), call TGN-ST. Leverage torch.compile and Introduce vectorize forward pass algorithm.

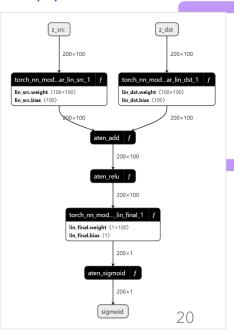
(a) Time Encoder



(b) embedding



(c) decoder



# Methodology (6)

### Model efficiency optimization

Algorithm 1. TGN forward pass			Algorithm 2. TGN-ST forward pass					
1 Input: $X \in \mathbb{R}^{2 \times N \times D}$	; $NS \in \mathbb{R}^{N \times S}$	$\triangleright S$ size of neighbors; <b>D</b> input size	1 Ir	put: $X \in \mathbb{R}^{2 \times N \times D}$ ; $NS \in \mathbb{R}^{N \times S}$	$\triangleright S$ size of neighbors; $D$ i	nput size		
2 Output: $Y \in \mathbb{R}^{N \times 1}$	$MRR \in \mathbb{R}$	▶ N total number of edges	2 C	Output: $Y \in \mathbb{R}^{N \times 1}$ ; $MRR \in \mathbb{R}$	⊳ N total number of edge	es		
3 Initialization: <i>mem</i>	_udater, embedding, link_predictor		3 Initialization: mem_updater, torch.compile({embedding, link_predictor})					
4 For each batch $X_i$	∈ <b>X</b> do		4 F	or each batch $X_i \in X$ do				
5 <b>NS</b> <sub>i</sub> ← Query	negative dst node corresponds to eac		5	$\textit{NS}_i \leftarrow \text{Query negative dst node corresponds to}$	$X_i \qquad \rhd X_i = \left[ X_{src_i}, X_{dst_i} \right]$			
6 For each $x_i \in$	$X_i$ contrasts $ns_i \in \mathit{NS}_i$ do			$\textit{NBR}_i \leftarrow \text{Query the neighbor of } \{X_i, NS_i\}$				
7 $NBR_i \leftarrow$	Query the neighbor of $\{x_i, ns_i\}$		7	$Z_i \leftarrow mem\_updater(X_i, NBR_i)$	⊳ implicit static time enco	der		
8 $Z_i \leftarrow mer$	$n\_updater(\{x_i, NBR_i\})$	⊳ implicit learnable time encoder	8	$\mathbf{Z}_i \leftarrow embedding(\mathbf{Z}_i)$				
9 $Z_i \leftarrow emb$	edding $(oldsymbol{Z_i})$		9	$Y_i \leftarrow link\_predictor\big(\big[\mathbf{Z}_{src_i} \in \mathbf{Z}_i, \mathbf{Z}_{dst_i} \in \mathbf{Z}_i\big]\big)$	$ hd Z_{src_i}$ embedding of so	urce nodes		
10 $Y_i \leftarrow link$	_predictor $\left(\mathbf{Z}_{src_i} \in \mathbf{Z}_i, \mathbf{Z}_{dst_i} \in \mathbf{Z}_i\right)$	$ ightharpoonup Z_{src_i}$ embedding of source nodes	10	For each $x_i \in X_i$ contrasts $ns_i \in NS_i$ do				
11 $MRR_i \leftarrow$	Compute the metrics MRR		11	$MRR_i \leftarrow \text{Compute the metrics MRR}$				
12 End For			12	End For				
13 End For			13 E	nd For				
14 Retu <b>rn Y, MRR</b>			14 R	eturn <b>Y, MRR</b>				

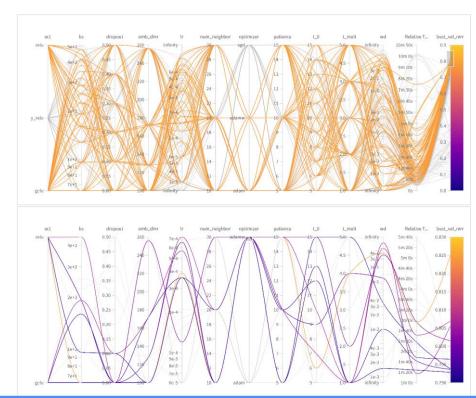
# Methodology (7)

Model performance optimization

### Hyperparameter Tuning

Perform 200 random search experiments:

- -SGD is the worst optimizer
- -Leaky\_relu activation function should be avoid
- -AdamW with cosine annealing is the best training strategy.
- -Batch size & patience number directly impact the training speed.



		Act	bs	dropout	emb_dim	lr	num_neig hbor	optimizer	patien ce	t_0	$t_{mult}$	wd
	distributio n	rand_sel	q_log_uniform _values	int_unifo rm	rand_sel	q_log_uniform _values	rand_sel	rand_sel	rand_s el	int_unifo rm	int_unifo rm	q_log_uniform _values
	range	[relu, leaky_relu, gelu]	[32,512]	[0,0.5]	[100,172, 256]	[0.00001, 0.0001]	[10,20,30]	[sgd, adam, adamw]	[5,10,1 5]	[5,15]	[1,5]	[0.0001, 1]
	step	-	32	0.1	-	0.00003	-	-	-	1	1	0.0005
	final s <mark>el</mark> ection	ReLU	288	0.1	100	0.00072	10	AdamW	5	14	4	0.01292

# Results and Discussions

**Findings** 

### Sample Dataset Result

- -25% faster training time
- -4x Validation time

### **Full Dataset Result**

- -TGN-ST gains 7.25 improvement TGN-ST sets new state-of-the-art result with 72.49% MRR
  - 15% faster training time
  - 5x Validation time

### **Implication**

Consistent improvement on both dataset provide evident for the generalizability of the pipeline and TGN-ST forward pass algorithm.

	Model and Gains	Test MRR (%)	Training Time per Epoch (s)	Validation Time per Epoch (s)
100 Sample	Vanilla TGN	72.94	2.3743	9.8546
	TGN-ST	80.19	1.7763	2.2687
Nodes	Gain	7.25	0.598 (25%)	7.586 (4.34x)
	Vanilla TGN	70.50 (*)	2800 (**)	9485 (**)
Full Dataset	TGN-ST	72.49	2366	1887
	Gain	1.99	434 (15%)	7598 (5.02x)

<sup>(\*)</sup> Result obtained from TGB leaderboard. (https://tgb.complexdatalab.com/docs/leader\_linkprop/)

<sup>(\*\*)</sup> Result obtained by running & averaging first few epochs

# Conclusions and Future Directions

#### Summary and Future Work

#### Scalable Framework

Established scalable framework, performed graph subsampling, visualization, hyperparameter tuning

#### Model Improvement

Proposed TGN-ST model with new state-of-the-art results and with significant training speed and evaluation speed improvement.

#### **Future Direction**

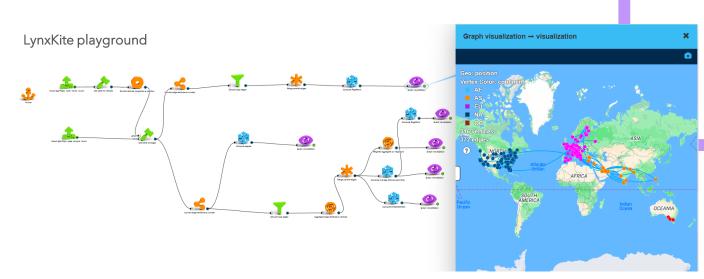
- [1] Explore different graph sampling strategy such as random walk sampling
- [2] Apply framework to other TGB datasets
- [3] Model parallelism and scale further to multi-GPU or multi-node cluster
- [4] Apply more complex neighborhood aggregation method and long-range dependency memory updater such as Selective State-Space Model (S6) or xLSTM

# **Publication**

Hang H., Sokhey P., Gabor B. Sothea H., and Pheak N. Temporal Graph Learning with Application to Large-Scale Traffic Flight Prediction. In Techno-SRJ (under review), 2024.

# Acknowledgement

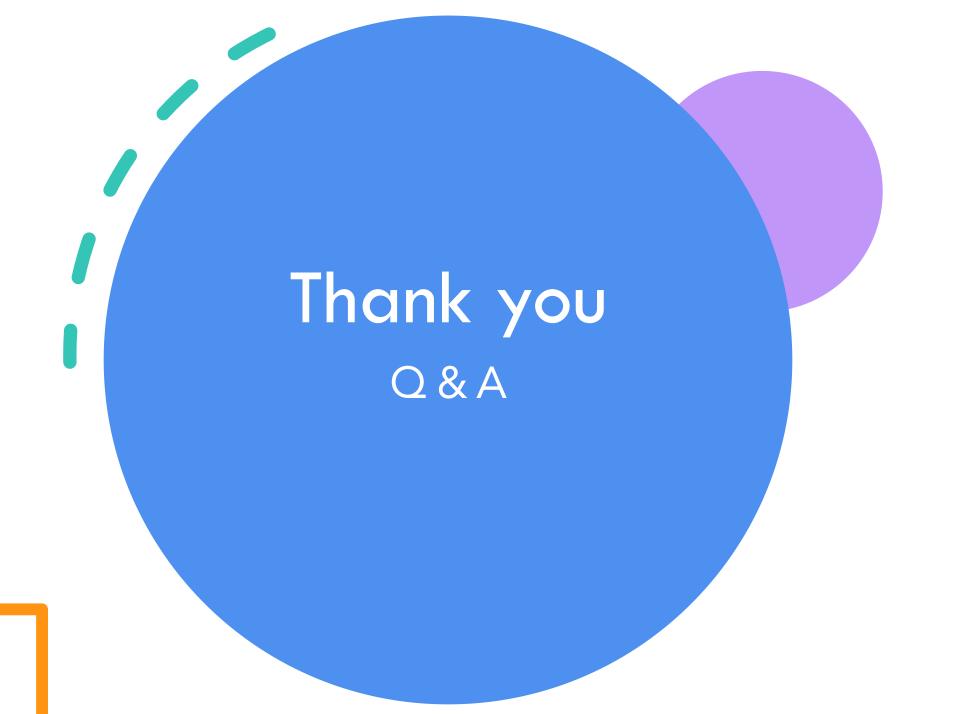
- Dr. Gabor's guides on graph visualization on Lynxkite
- Lynx Analytics' funded Lynx azure cluster



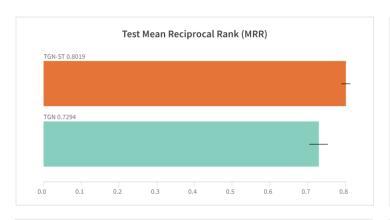
# References

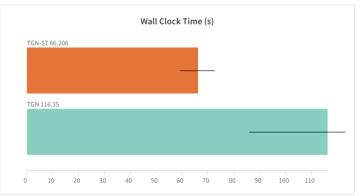
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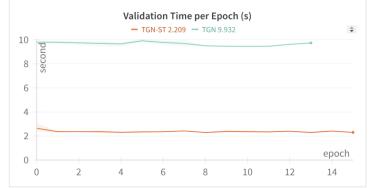
# Appendix 1. TGN-ST vs TGN Benchmarking

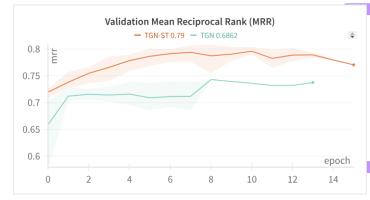




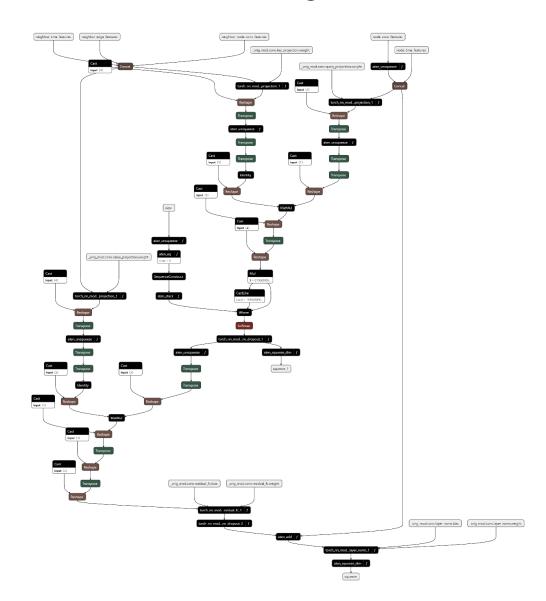








# Appendix 2. TGN embedding module's FX Graph



# Appendix 3. Experimental Setups

- Hardware and Software Requirements:
  - Main computing machine
    - Operating System: Ubuntu 22.04
    - Python Version: 3.10 or higher
    - CPU: Intel Core i7 14700k @3.4GHz with 20 cores (8 P-cores + 12 E-cores).
    - GPU: NVIDIA RTX 4080 Super (320 tensor cores) with 16GB memory.
  - Additional computing machine (Lynx Azure cluster provided by Lynx Analytics)
    - Operating System: Ubuntu 22.04
    - Python Version: 3.10 or higher
    - Cluster: Standard NC4as T4 v3 (4 vcpus, 28 GiB memory)
    - CPU: AMD EPYC 7V12(Rome) CPUs
    - GPU: Nvidia Tesla T4 with 16GB memory
- Main Software Libraries:
  - PyTorch (version 2.0 or higher)
  - PyTorch Geometric (version 2.5 or higher)
  - Wandb (<a href="https://wandb.ai/">https://wandb.ai/</a>)
- Graph visualization and FX graph capture tools:
  - Lynxkite by Lynx Analytics (<a href="https://try.lynxkite.com/">https://try.lynxkite.com/</a>)
  - Onnx export (<a href="https://onnx.ai/">https://onnx.ai/</a>)