

word_embedding

March 29, 2025

```
[ ]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import scipy.sparse.linalg as sp_linalg
```

1 load the co-occurrence matrix and dictionary

```
[ ]: file_name = "co_occur.csv"

df = pd.read_csv(file_name, header=None)
M = df.to_numpy()

M_w = np.log10(M + 1) # normalize the matrix

with open('dictionary.txt', 'r') as f:
    words = f.read().splitlines()
```

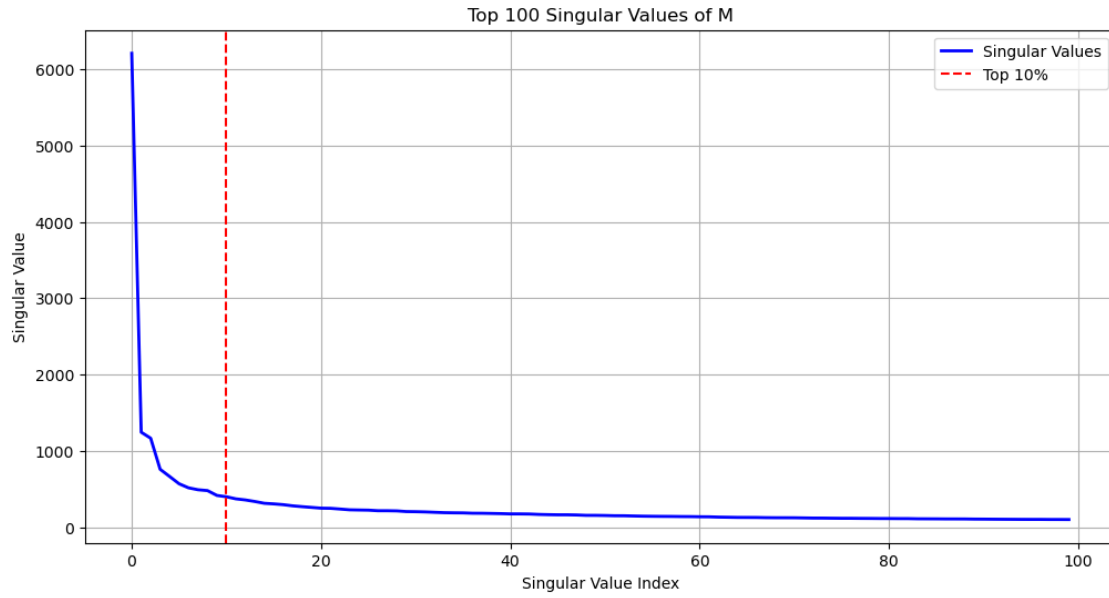
2 Plot of first 100 singular values

```
[4]: # perform SVD for the first 100 singular values
U, s, Vt = sp_linalg.svds(M_w, k=100)
s = s[:-1]

plt.figure(figsize=(12,6))

plt.plot(s, 'b-', linewidth=2, label='Singular Values')
critical_index = int(0.1 * len(s))
plt.axvline(critical_index, color='r', linestyle='--', label='Top 10%')

plt.xlabel('Singular Value Index')
plt.ylabel('Singular Value')
plt.title('Top 100 Singular Values of M')
plt.legend()
plt.grid()
plt.show()
```



3 Try to find out the interpretable dimensions

```
[5]: vec = [3,4,15,24,36]
for i in vec:
    ui = U[:,i]
    index = np.argsort(ui)
    print(i)
    print("largest: ", words[index[-1]])
    print("second largest: ", words[index[-2]])
    print("third largest: ", words[index[-3]])
    print("forth largest: ", words[index[-4]])
    print("fifth largest: ", words[index[-5]])
    print("sixth largest: ", words[index[-6]])
    print("seventh largest: ", words[index[-7]])
    print("eighth largest: ", words[index[-8]])
    print("ninth largest: ", words[index[-9]])
    print("tenth largest: ", words[index[-10]])
    print("-----")
    print("smallest: ", words[index[0]])
    print("second smallest: ", words[index[1]])
    print("third smallest: ", words[index[2]])
    print("forth smallest: ", words[index[3]])
    print("fifth smallest: ", words[index[4]])
    print("sixth smallest: ", words[index[5]])
    print("seventh smallest: ", words[index[6]])
    print("eighth smallest: ", words[index[7]])
```

```
print("ninth smallest: ", words[index[8]])
print("tenth smallest: ", words[index[9]])
print()
```

3

largest: which
second largest: where
third largest: who
forth largest: whom
fifth largest: that
sixth largest: gain
seventh largest: under
eighth largest: taking
ninth largest: here
tenth largest: receiving

smallest: five
second smallest: several
third smallest: six
forth smallest: four
fifth smallest: were
sixth smallest: seven
seventh smallest: eight
eighth smallest: three
ninth smallest: been
tenth smallest: numerous

4

largest: french
second largest: quebec
third largest: du
forth largest: montreal
fifth largest: le
sixth largest: battalion
seventh largest: fort
eighth largest: la
ninth largest: regiment
tenth largest: pierre

smallest: pp
second smallest: hit
third smallest: vol
forth smallest: orthodox
fifth smallest: ed
sixth smallest: pitcher
seventh smallest: hits
eighth smallest: eds
ninth smallest: isbn

tenth smallest: christian

15

largest: been
second largest: get
third largest: are
forth largest: were
fifth largest: got
sixth largest: gets
seventh largest: themselves
eighth largest: be
ninth largest: can
tenth largest: various

smallest: near
second smallest: within
third smallest: around
forth smallest: in
fifth smallest: he
sixth smallest: into
seventh smallest: across
eighth smallest: she
ninth smallest: through
tenth smallest: due

24

largest: government
second largest: political
third largest: committee
forth largest: law
fifth largest: important
sixth largest: commission
seventh largest: party
eighth largest: policy
ninth largest: army
tenth largest: by

smallest: area
second smallest: river
third smallest: north
forth smallest: road
fifth smallest: near
sixth smallest: south
seventh smallest: park
eighth smallest: east
ninth smallest: water
tenth smallest: island

36

largest: album
second largest: episode
third largest: film
forth largest: song
fifth largest: tv
sixth largest: show
seventh largest: episodes
eighth largest: series
ninth largest: band
tenth largest: movie

smallest: people
second smallest: president
third smallest: government
forth smallest: held
fifth smallest: leader
sixth smallest: minister
seventh smallest: students
eighth smallest: received
ninth smallest: father
tenth smallest: members

3.1 Interpretation

- Dimension 3 separates quantity-related words (e.g., five, six, several) from syntactic function words (e.g., which, where, under, here).
- Dimension 4 separates publishing/abbreviation-related terms (e.g., pp, vol, isbn) from French-associated words (e.g., french, du, le, la, montreal).
- Dimension 15 separates spatial prepositions (e.g., near, within, in) from verbs in different tenses (e.g., been, are, got, get).
- Dimension 24 separates political/government-related terms (e.g., government, political, law) from geographical terms (e.g., river, north, island).
- Dimension 36 separates entertainment-related vocabulary (e.g., album, film, tv, song) from social role-related words (e.g., people, president, student).

4 Map some words into the dimension $V = V_{women} - V_{man}$

```
[6]: rows_norm = np.linalg.norm(U,axis=1,keepdims=True)
    U_normalized = U / rows_norm

    # man: 236 women: 783

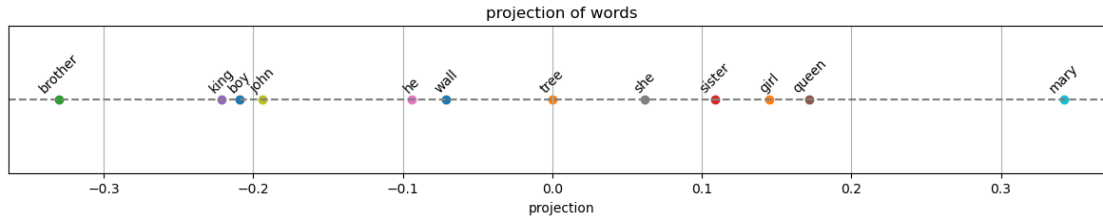
    V1 = U_normalized[783]
    V2 = U_normalized[236]
    V = V1 - V2
    V = V / np.linalg.norm(V)

    w = {
        'boy':1121,
        'girl':996,
        'brother':614,
        'sister':1088,
        'king':240,
        'queen':814,
        'he':12,
        'she':42,
        'john':128,
        'mary':788,
        'wall':1273,
        'tree':1403
    }

    projection = {}
    for word,index in w.items():
        projection[word] = np.dot(V,U_normalized[index])
        projection[word] = round(projection[word],3)

    plt.figure(figsize=(15, 2))
    plt.axhline(0, color='gray', linestyle='--')
    for word, proj in projection.items():
        plt.scatter(proj, 0)
        plt.text(proj, 0.005, word, ha='center', rotation=45)

    plt.title("projection of words")
    plt.xlabel("projection")
    plt.yticks([])
    plt.grid(True, axis='x')
    plt.show()
```



4.1 Interpretation

- Words related to the male gender (such as boy, brother, king) are distributed on the left side of the zero value
- while words related to the female gender (such as queen, sister) are distributed on the right side of the zero value.
- Neutral words like “tree” are exactly at the zero value.

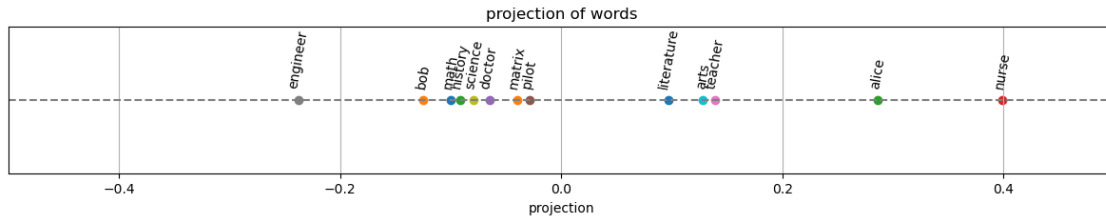
```
[7]: # math, matrix, history, nurse, doctor, pilot, teacher, engineer, science,
    ↪ arts, literature, bob, alice
w_2 = {
    'math': 5304,
    'matrix': 4361,
    'history': 98,
    'nurse': 5777,
    'doctor': 1361,
    'pilot': 1713,
    'teacher': 1569,
    'engineer': 1668,
    'science': 406,
    'arts': 533,
    'literature': 1120,
    'bob': 1401,
    'alice': 3397
}

projection_2 = {}
for word, index in w_2.items():
    projection_2[word] = np.dot(V, U_normalized[index])
    projection_2[word] = round(projection_2[word], 3)

plt.figure(figsize=(15, 2))
plt.axhline(0, color='gray', linestyle='--')
for word, proj in projection_2.items():
    plt.scatter(proj, 0)
    plt.text(proj, 0.01, word, ha='center', rotation=80)

plt.xlim(-0.5, 0.5)
```

```
plt.title("projection of words")
plt.xlabel("projection")
plt.yticks([])
plt.grid(True, axis='x')
plt.show()
```



4.2 Interpretation

- It can be seen that certain professions exhibit significant differences in terms of gender representation
- For example, professions such as engineers and pilots tend to skew male, while teachers and nurses tend to skew female, which may also lead to some bias issues

5 Find out “the most similar word”

- The similarity is measured by cosine-similarity
- use “montreal” and “apple” as examples

```
[8]: def find_closest_by_vec(vec,omit):
    sim=[]
    for i in range(10000):
        if i in omit:
            sim.append(0)
            continue
        sim.append(np.dot(vec,U_normalized[i]))

    sim = np.array(sim)
    index = np.argsort(sim)
    return index

index_montreal = 2207
montreal_vec = U_normalized[index_montreal]
omit = [index_montreal]

print(f"most similar words to {words[index_montreal]}:")
index = find_closest_by_vec(montreal_vec,omit)
for i in range(5):
    print(words[index[-(i+1)]],end=" ")

index_apple = 3370
apple_vec = U_normalized[index_apple]
omit_apple = [index_apple]
print(f"\nmost similar words to {words[index_apple]}:")
index = find_closest_by_vec(apple_vec,omit_apple)
for i in range(5):
    print(words[index[-(i+1)]],end=" ")
```

```
most similar words to montreal:
vancouver toronto ottawa winnipeg calgary
most similar words to apple:
microsoft ibm linux palm os
```

5.1 Interpretation

- It can also be observed here that similar technology companies or tech-related terms are associated with Apple
- indicating that in the training data, Apple is more likely to refer to Apple Inc, rather than the fruit

6 Import test data

- This part will solve word analogy tasks
- For example:
 - “man is to women as king is to ?”
 - the goal is to fill in the ? by a proper word
 - in this case, is “queen”

```
[10]: test=[]
with open("analogy_task.txt",'r') as f:
    for line in f:
        test.append(line.strip().split(" "))

dict_words={}
for i in range(len(words)):
    current_word = words[i]
    dict_words[current_word] = i
```

7 Perform analogy test and calculate the correct rate

```
[11]: correct = 0
over_5=[]
count = 0
mylist=[]
for i in test:
    count+=1
    omit = []
    for j in range(3):
        omit.append(dict_words[i[j]])
    ans = i[3]
    v_diff = U_normalized[dict_words[i[1]]] - U_normalized[dict_words[i[0]]] +
    ↪U_normalized[dict_words[i[2]]]
    v_diff = v_diff/np.linalg.norm(v_diff)
    index = find_closest_by_vec(v_diff,omit)
    if words[index[-1]] == ans:
        correct+=1
print(f"correct: {correct}")
print(f"total: {len(test)}")
print(f"accuracy: {correct/len(test)}")
```

```
correct: 3071
total: 5585
accuracy: 0.5498657117278425
```