Autoencoder

Prof. Seungchul Lee

Industrial AI Lab.

Autoencoders

- It is like ‘deep learning version’ of unsupervised learning

- Definition
  – An autoencoder is a neural network that is trained to attempt to copy its input to its output
  – The network consists of two parts: an encoder and a decoder that produce a reconstruction

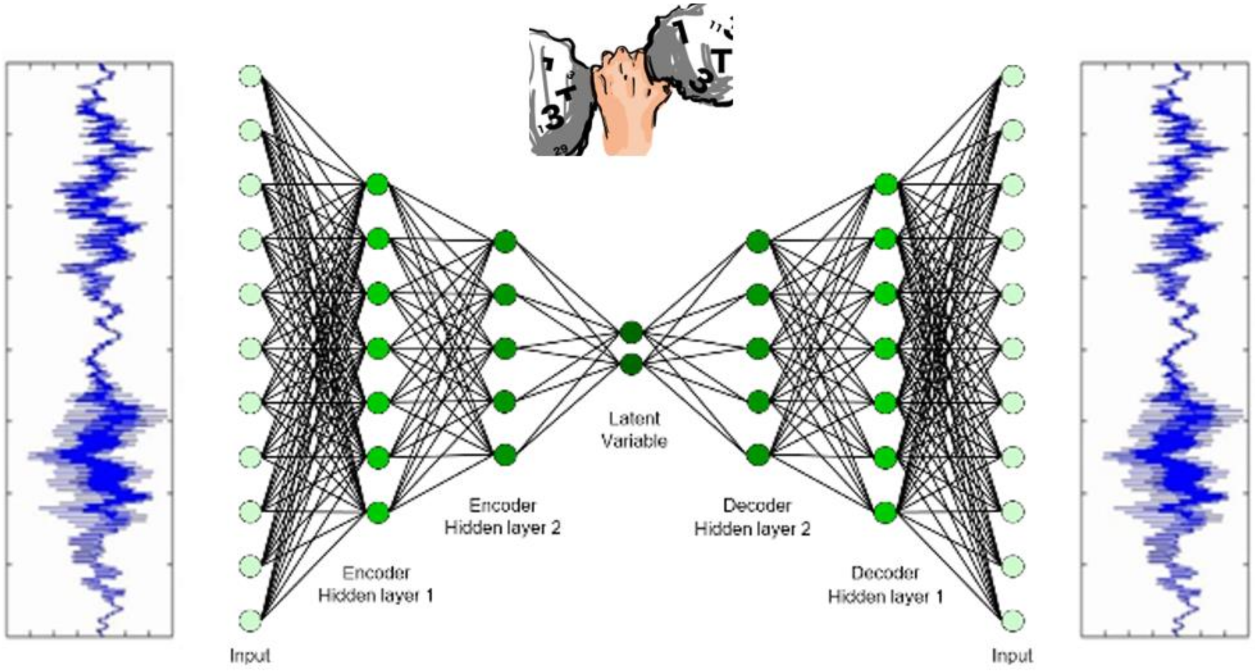
- Encoder and Decoder
  – Encoder function : $z = f(x)$
  – Decoder function : $x = g(z)$
  – We learn to set $g\big(f(x)\big) = x$

Autoencoder

- Dimension reduction
- Recover the input data

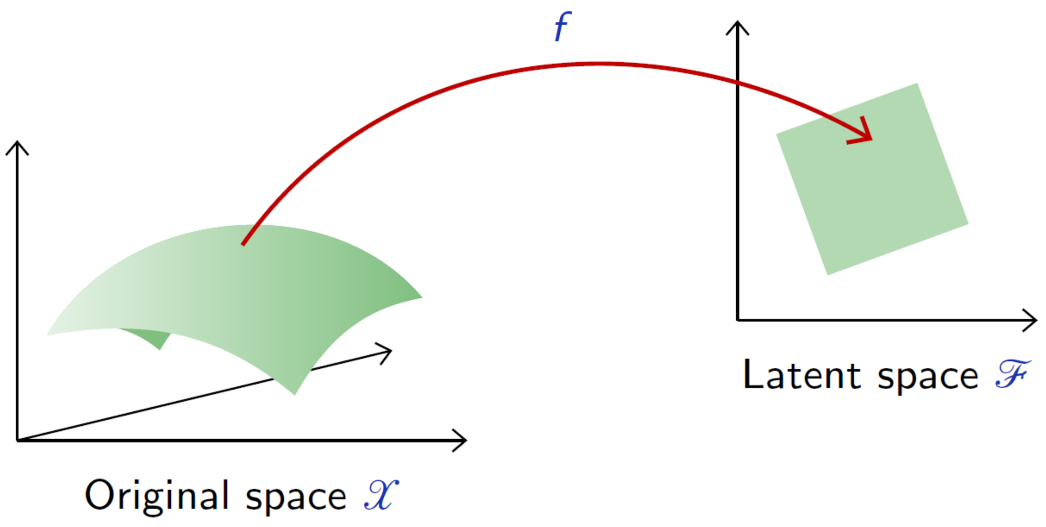
Autoencoder

- Dimension reduction
- Recover the input data
  - Learns an encoding of the inputs so as to recover the original input from the encodings as well as possible



Autoencoder

- Autoencoder combines an encoder f from the original space $\mathcal{X}$ to a latent space $\mathcal{F}$, and a decoder g to map back to $\mathcal{X}$, such that $g \circ f$ is [close to] the identity on the data



Source: Dr. Francois Fleuret at EPEL

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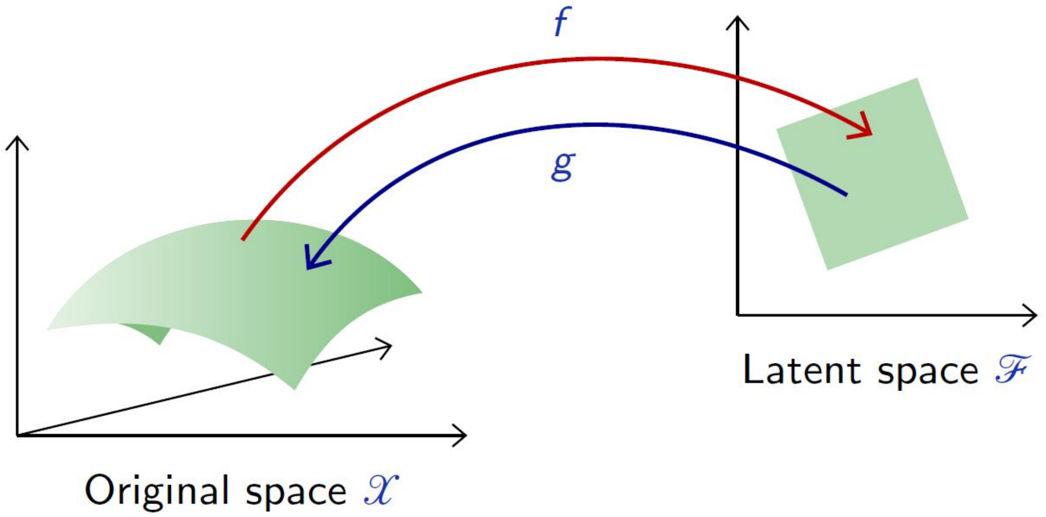


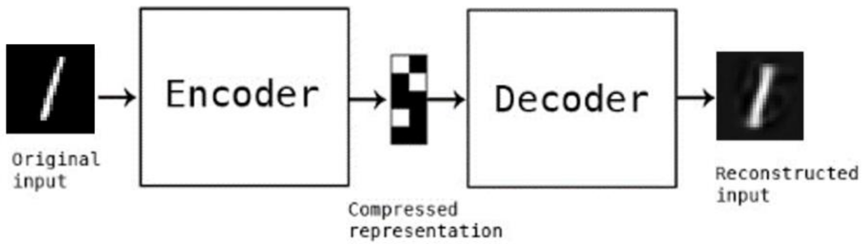
- A proper autoencoder has to capture a "good" parametrization of the signal, and in particular the statistical dependencies between the signal components.

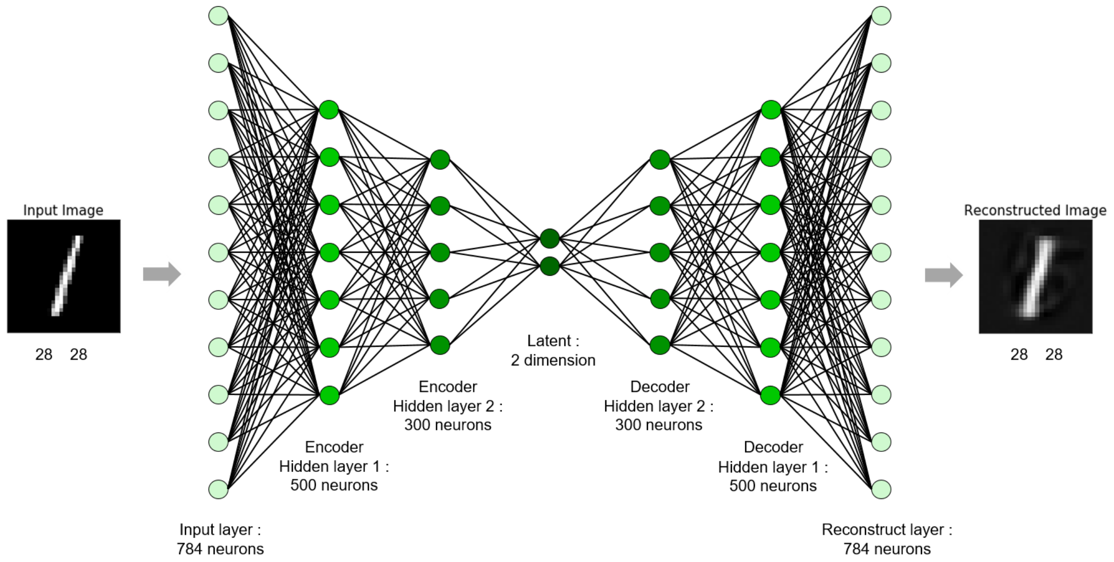
Source: Dr. Francois Fleuret at EPEL

Autoencoder with MNIST

Autoencoder with TensorFlow

- MNIST example
- Use only (1, 5, 6) digits to visualize in 2-D





$$\frac{1}{m}\sum_{i=1}^{m}(t_i - y_i)^2$$

Import Libraries and Load MNIST Data

```python
import numpy as np
import matplotlib.pyplot as plt
%matplotlib inline

from sklearn.neural_network import MLPRegressor
from sklearn.metrics import accuracy_score
```

- Only use (1, 5, 6) digits to visualize latent space in 2-D

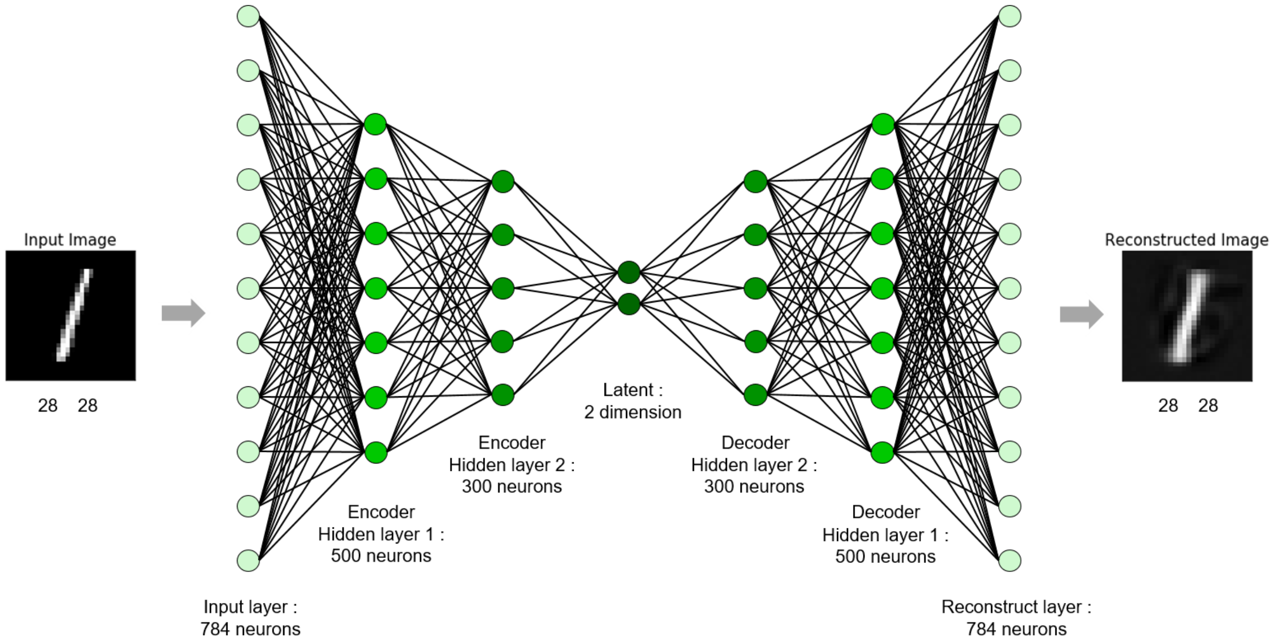
```python
train_x = np.load('./data_files/mnist_train_images.npy')
train_y = np.load('./data_files/mnist_train_labels.npy')
test_x = np.load('./data_files/mnist_test_images.npy')
test_y = np.load('./data_files/mnist_test_labels.npy')

n_train = train_x.shape[0]
n_test = test_x.shape[0]

print ("The number of training images : {}, shape : {}".format(n_train, train_x.shape))
print ("The number of testing images : {}, shape : {}".format(n_test, test_x.shape))
```

```
The number of training images : 16583, shape : (16583, 784)
The number of testing images : 2985, shape : (2985, 784)
```

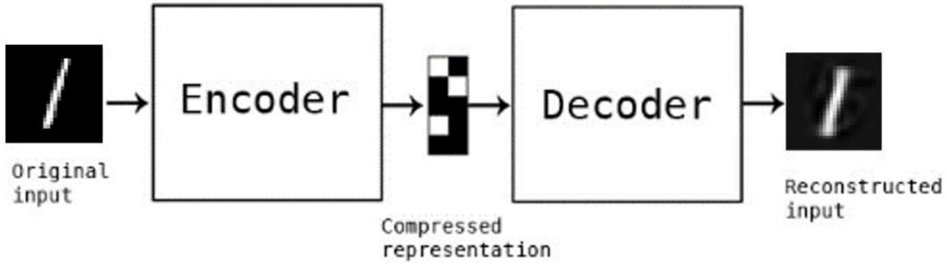
Structure of Autoencoder

- Input shape and latent variable shape
- Encoder shape
- Decoder shape

```
# Shape of input and latent variable

n_input = 28*28

# Encoder structure
n_encoder1 = 500
n_encoder2 = 300

n_latent = 2

# Decoder structure
n_decoder2 = 300
n_decoder1 = 500
```



Build a Model

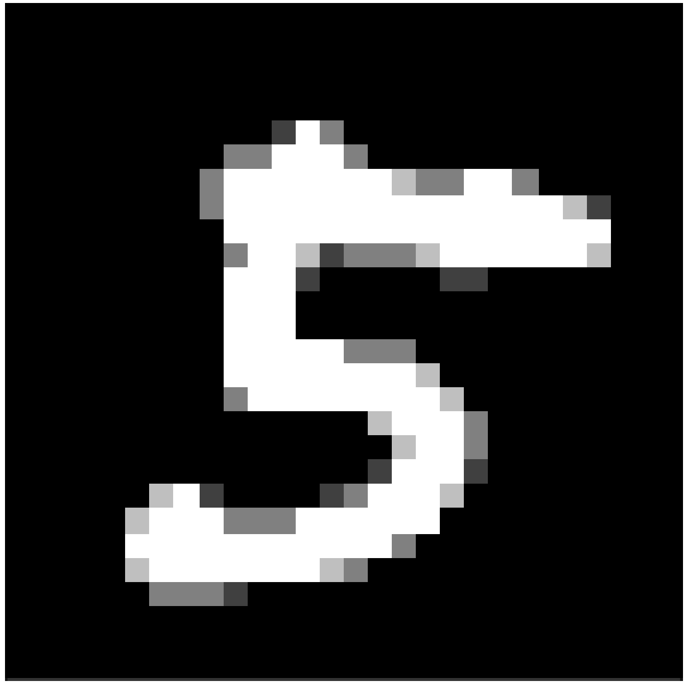



```
reg = MLPRegressor(hidden_layer_sizes = (n_encoder1, n_encoder2, n_latent, n_decoder2, n_decoder1),
                   activation = 'tanh',
                   solver = 'adam',
                   learning_rate_init = 0.0001,
                   max_iter = 20,
                   tol = 0.0000001,
                   verbose = True)
```

Test or Evaluation

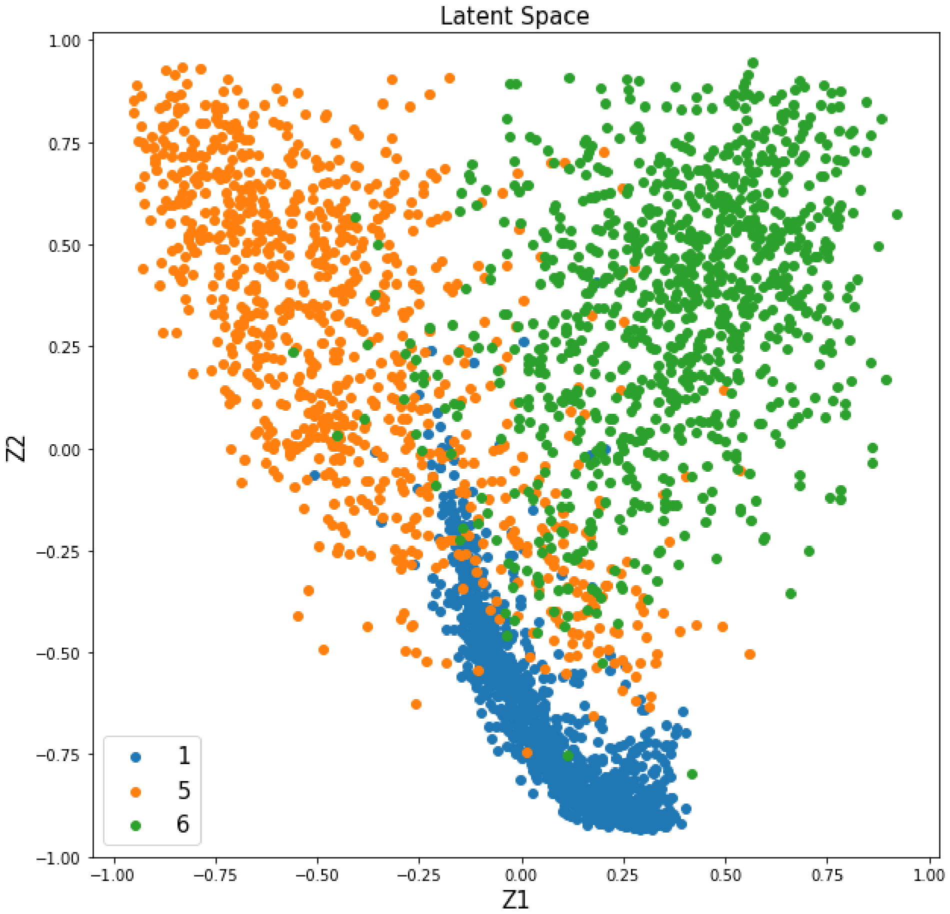
```
idx = np.random.randint(test_x.shape[0])
x_reconst = reg.predict(test_x[idx].reshape(-1,784))
```

Imput Image



Distribution in Latent Space

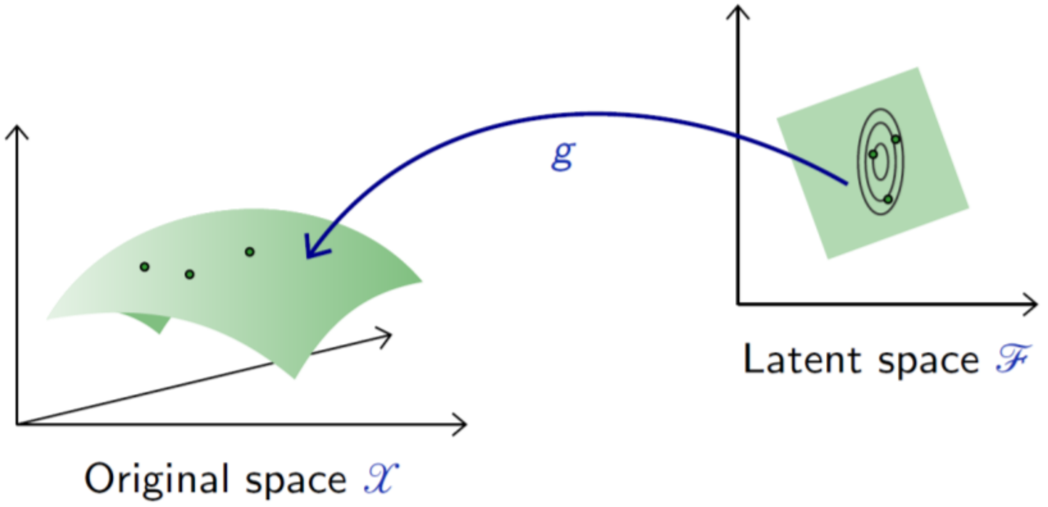
- Make a projection of 784-dim image onto 2-dim latent space



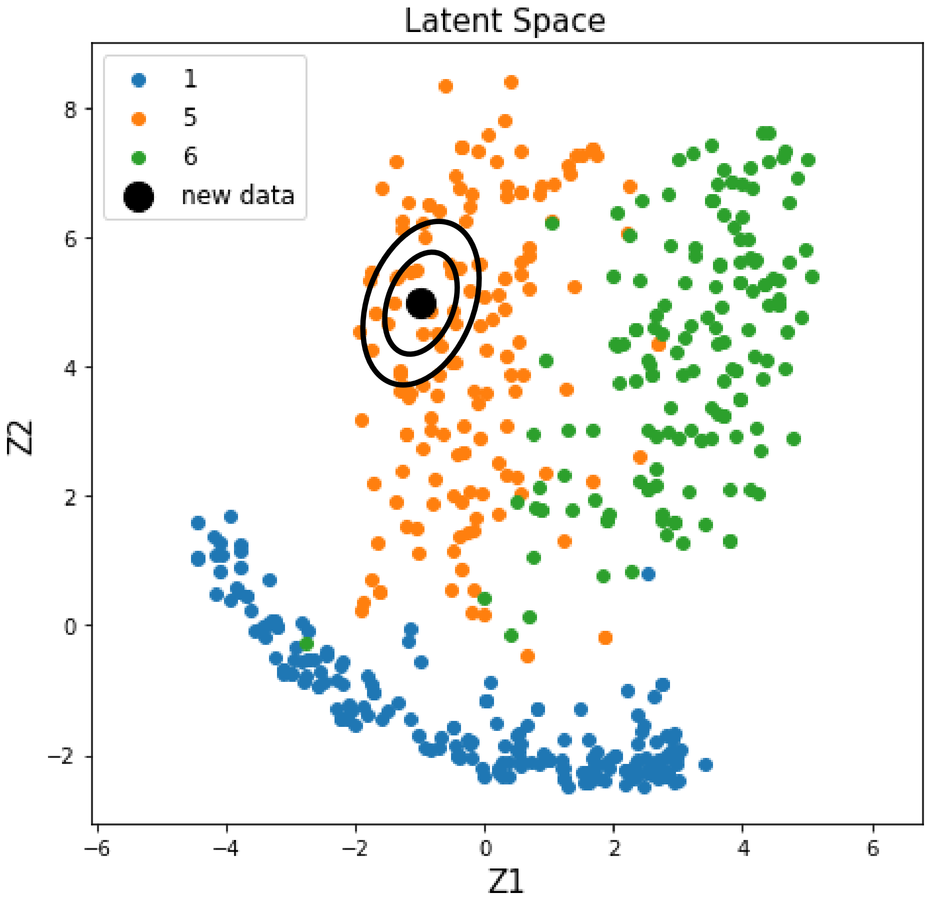
Autoencoder as Generative Model

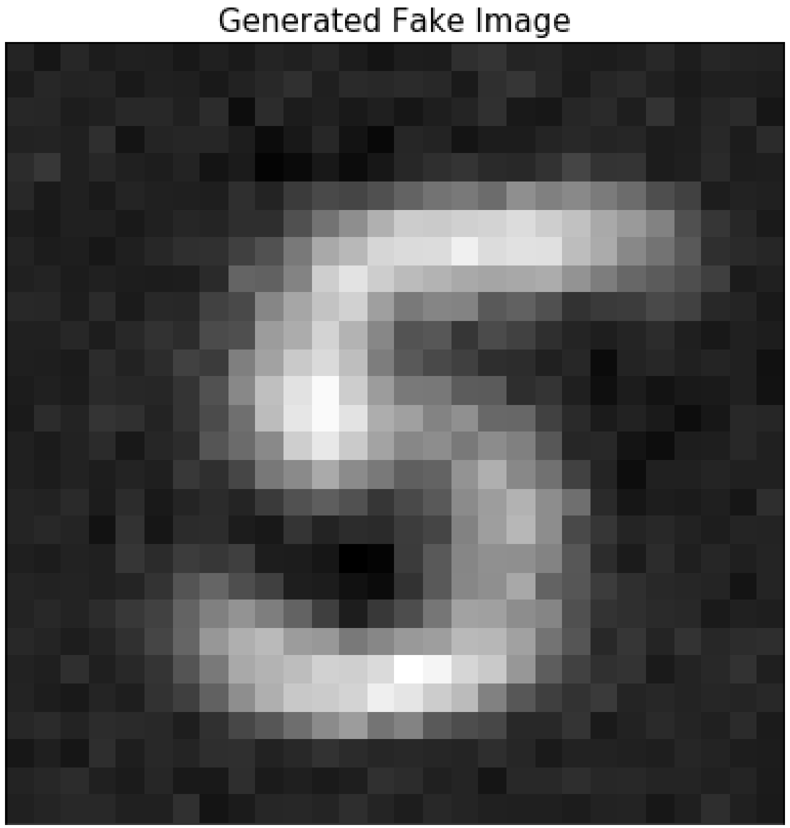
Generative Capabilities

- We can assess the generative capabilities of the decoder g by introducing a [simple] density model q^Z over the latent space $\mathcal{F}$, sample there, and map the samples into the image space $\mathcal{X}$ with g.



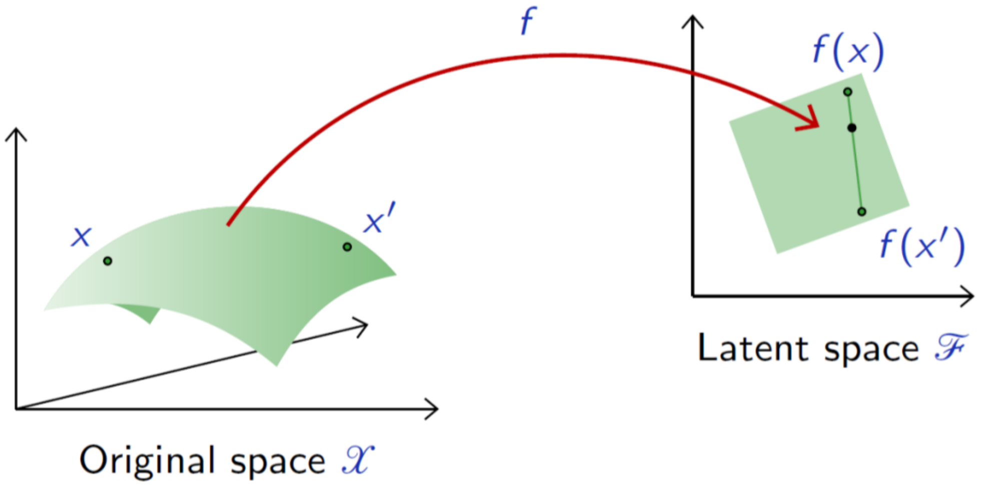
MNIST Example





Latent Representation

- To get an intuition of the latent representation, we can pick two samples x and x' at random and interpolate samples along the line in the latent space



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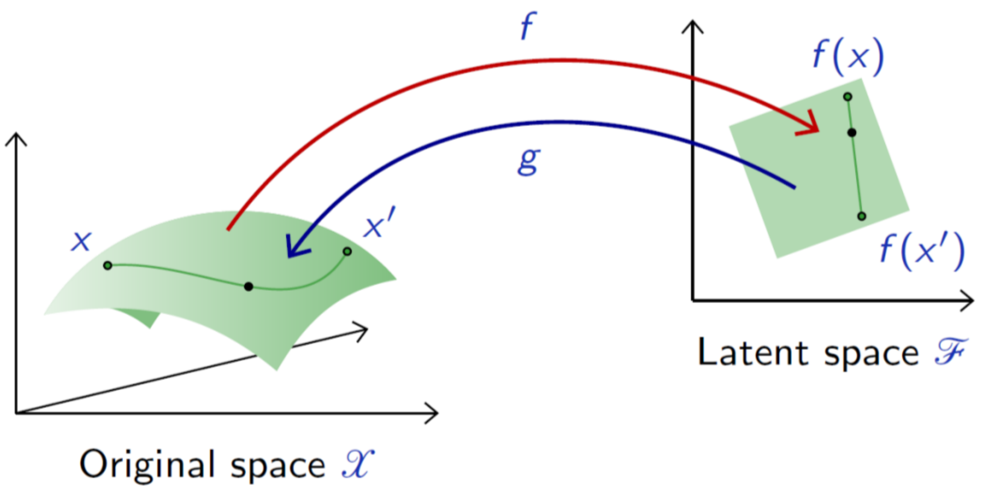
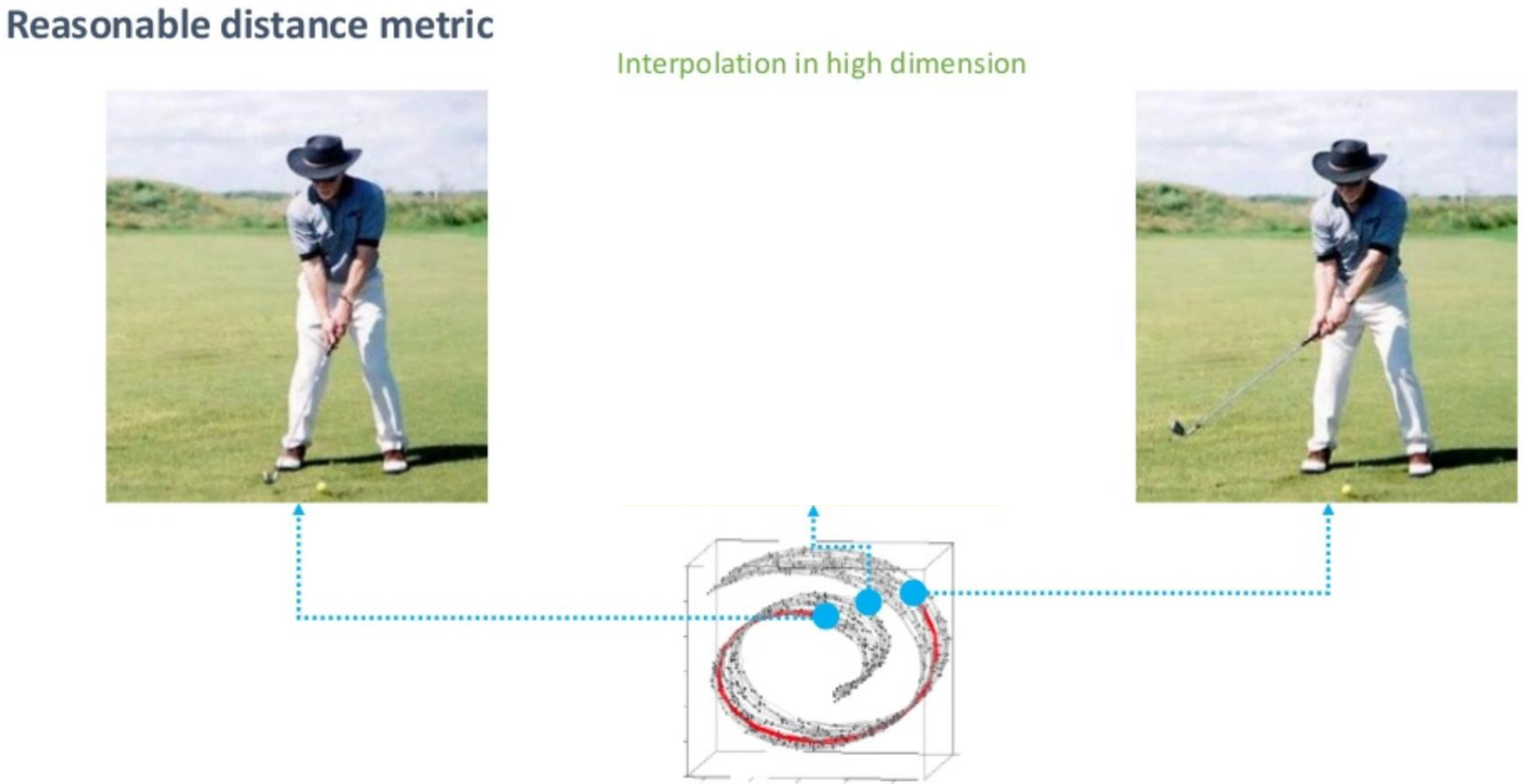
$$g((1-\alpha)f(x) + \alpha f(x'))$$

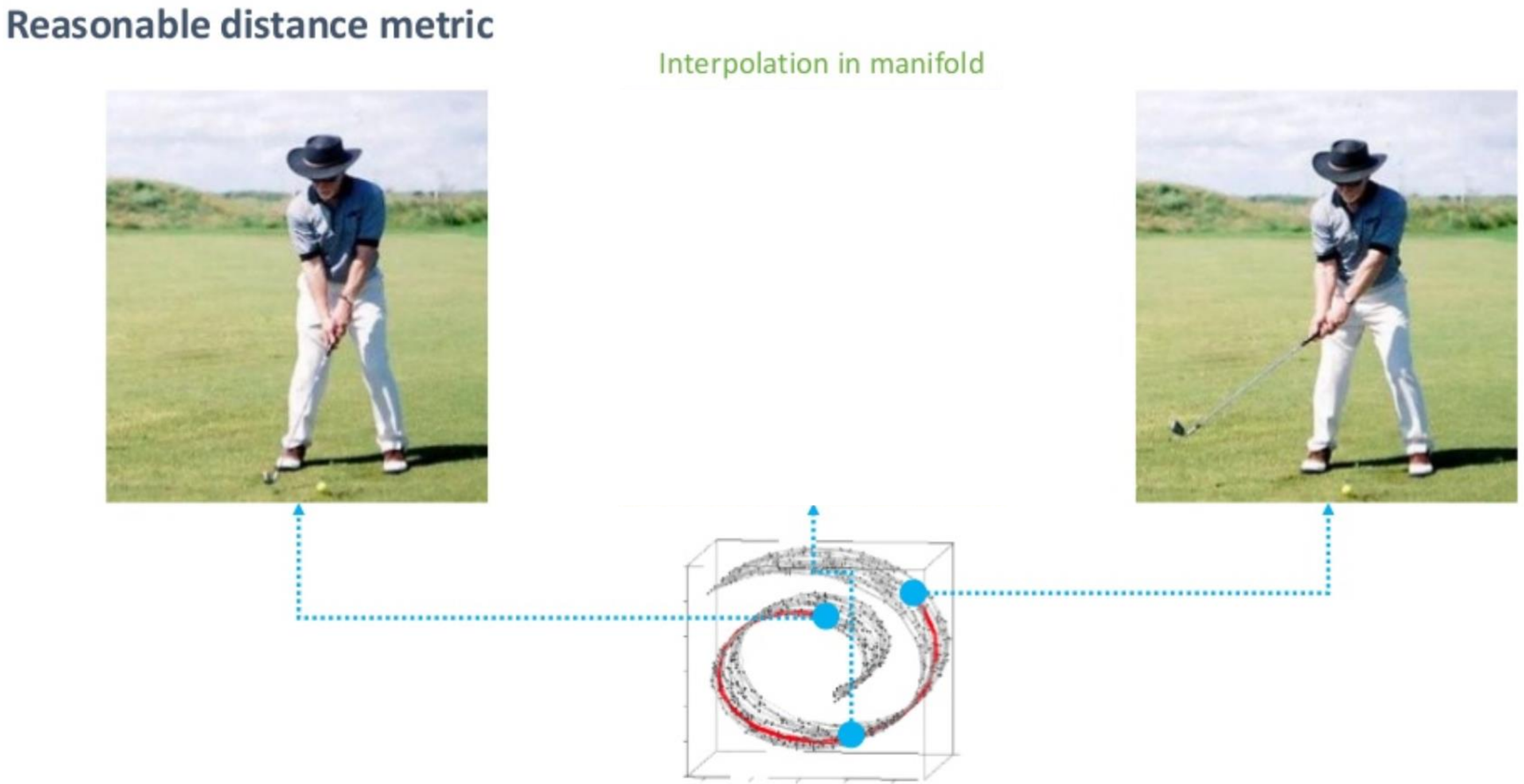


Interpolation in High Dimension



https://www.cs.cmu.edu/~efros/courses/AP06/presentations/ThompsonDimensionalityReduction.pdf

Interpolation in Manifold



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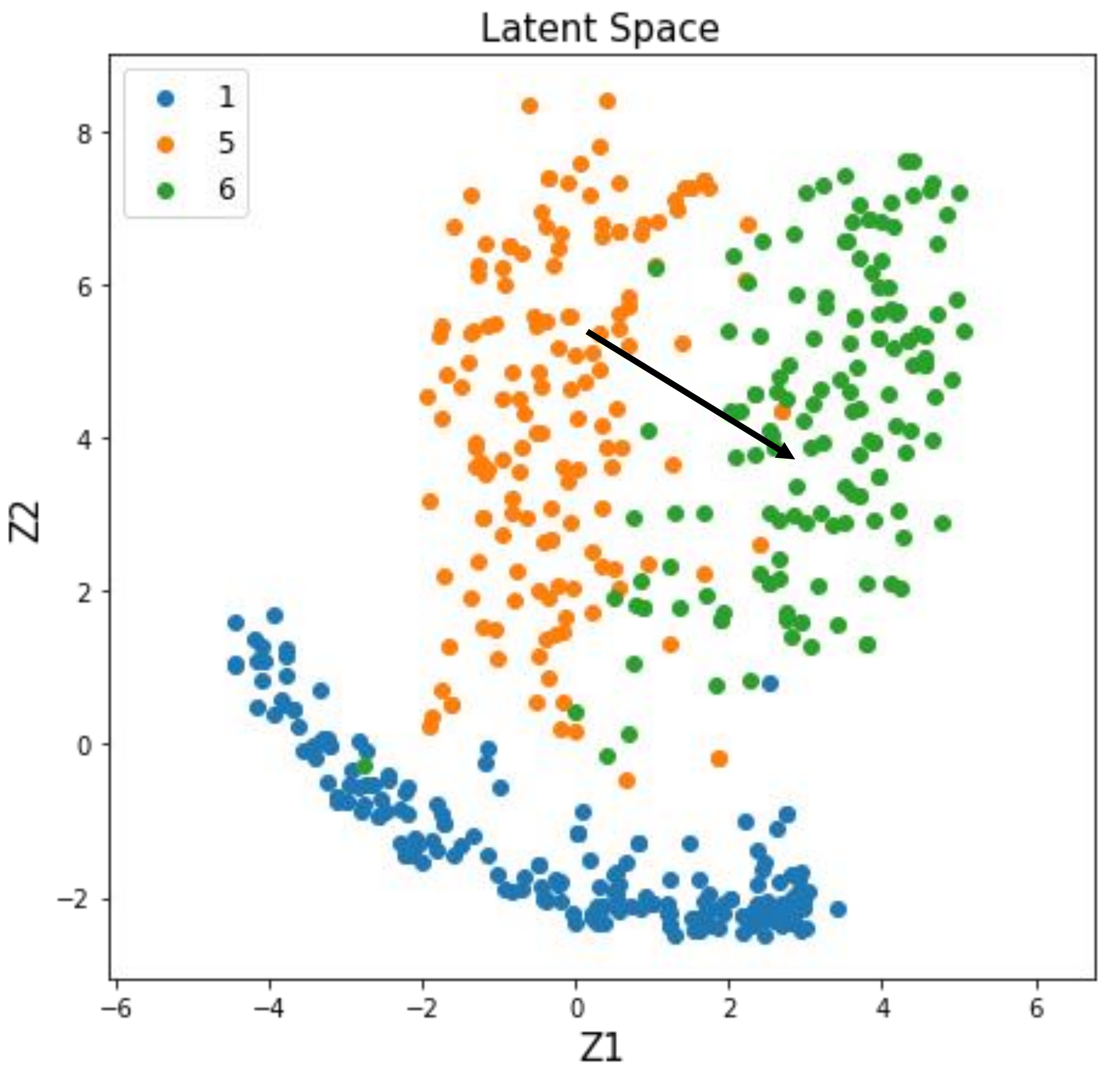
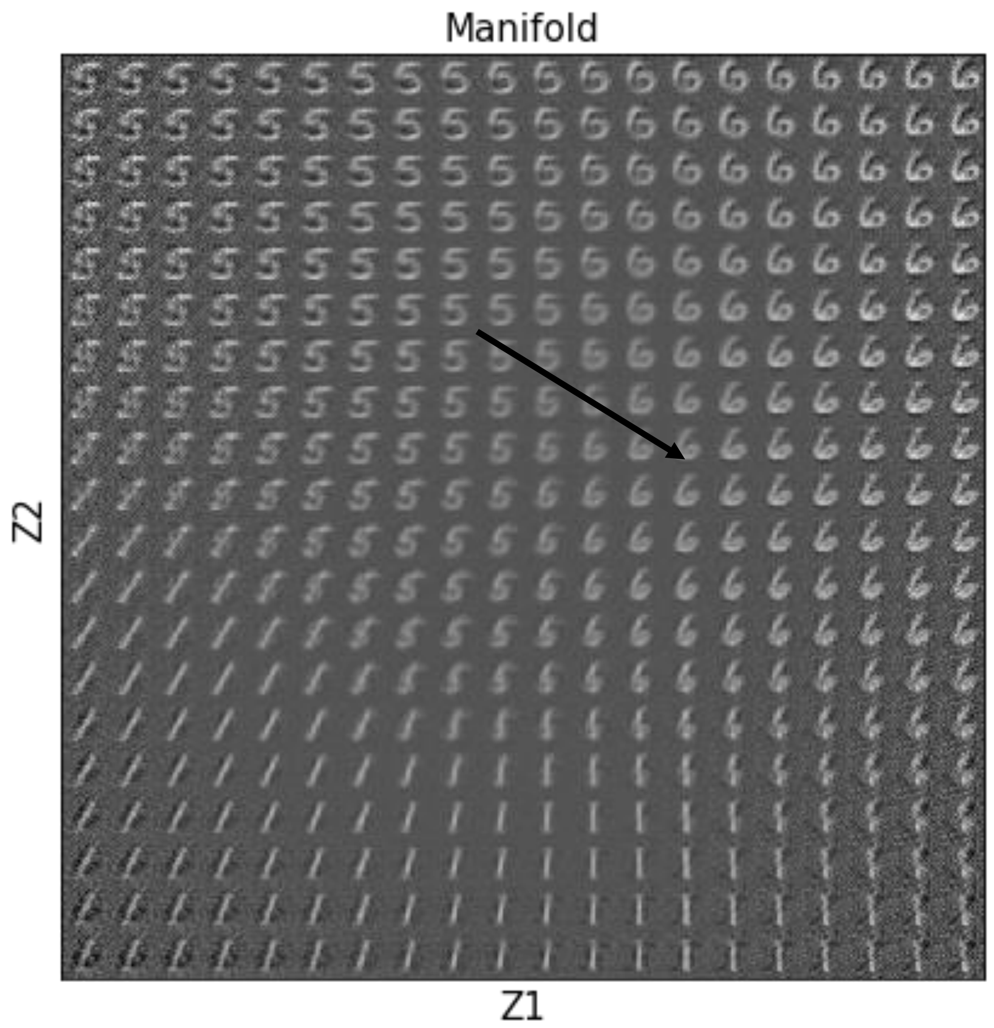
MNIST Example: Walk in the Latent Space





Generative Models

- It generates something that makes sense.

- These results are unsatisfying, because the density model used on the latent space $\mathcal{F}$ is too simple and inadequate.

- Building a "good" model amounts to our original problem of modeling an empirical distribution, although it may now be in a lower dimension space.

- This is a motivation to VAE or GAN.