

CS4160

COMPUTER GRAPHICS

class 2

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1

today's class

rendering architecture overview
mathematical preliminaries

<break>

light & images
the OpenEXR image format

2

2

sep 22: class reschedule

apologies!

choices:

wednesday (sep 21) 6:30-8 pm

or thursday (sep 22) 8-9:30am

3

3

TA office hours

He: T 3:00 - 5:00

Justin: W 4:00 - 6:00

Ray: T/Th 1:00-2:00

[in 122A Mudd]

[changes will be broadcast]

4

4

courseworks/canvas - set to “notify”

make sure you are getting broadcast msgs

check in every once in a while!

5

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getting help

1 - try to solve the problem! (notes/book/canvas)

2 - is it coding?

- if YES: have you used the debugger?
(if not, go to step 1)

3 - post to canvas - include the words “I used the debugger,
and the result was...”, and include image if possible.

4 - go to TA office hours

5 - if the above fails to solve your problem, contact me

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renderer architectures for 3d graphics : an overview

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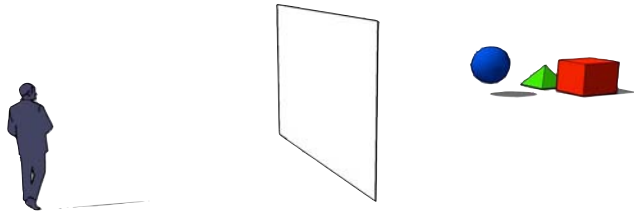
rendering



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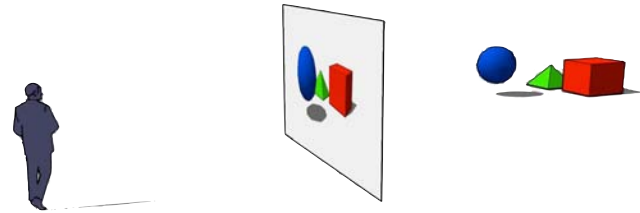
rendering



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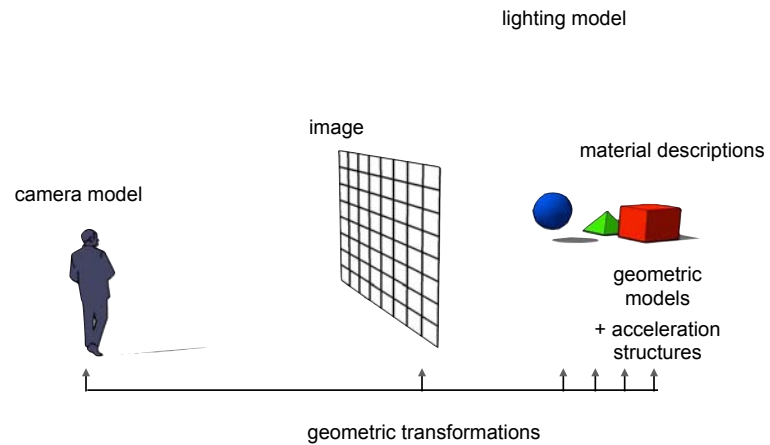
rendering



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rendering overview



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rendering

2 common methods:

- raytracing

examples: Mental Ray, Blue Sky's CGISudio, etc. etc.

- pipeline rendering

called "object-order rendering" in the book

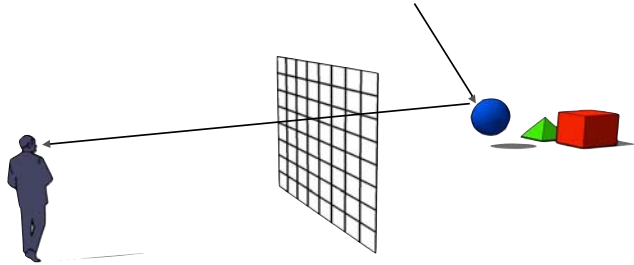
often called "scanline rendering"

examples: Pixar's PRMan, Maya's default renderer, most commercial renderers, 99.99% of hardware renderers

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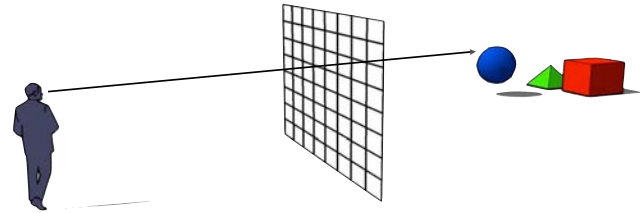
ray tracing



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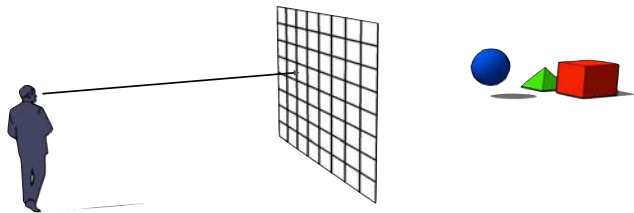
ray tracing



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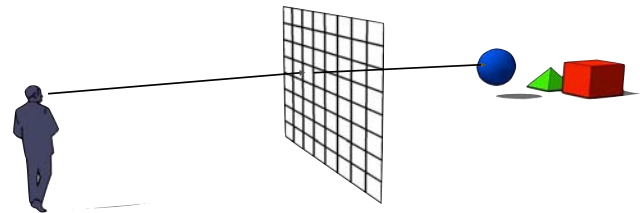
ray tracing



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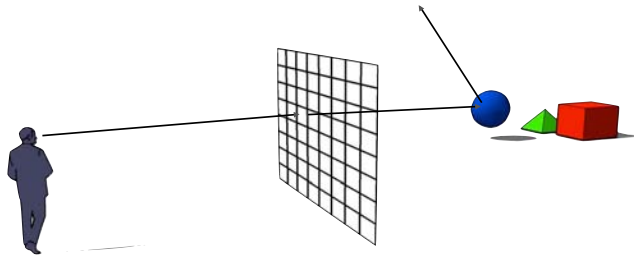
ray tracing



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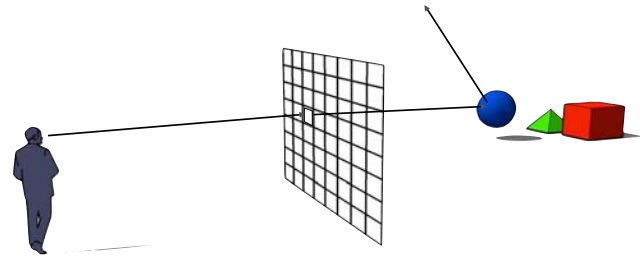
ray tracing



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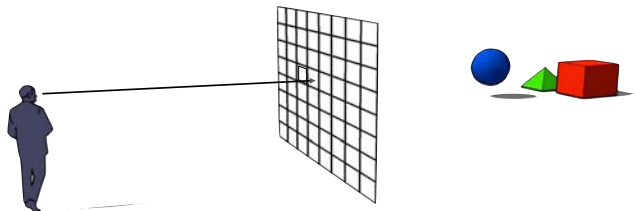
ray tracing



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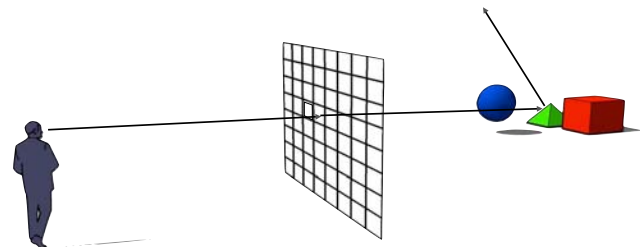
ray tracing



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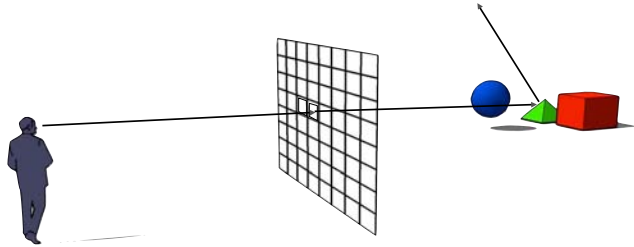
ray tracing



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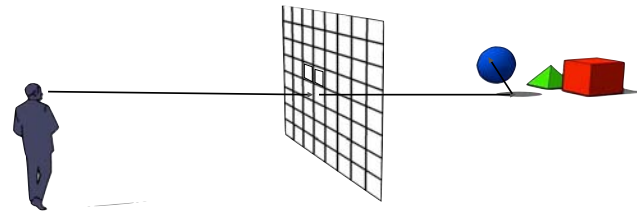
ray tracing



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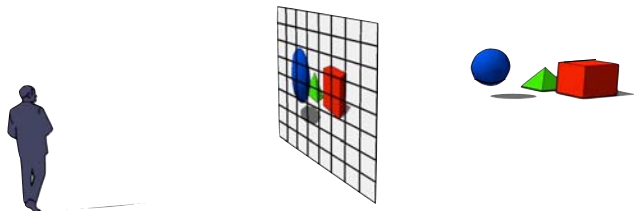
ray tracing



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ray tracing



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ray tracing

operations:

- ray-object intersection
- shading: lighting & materials calculation
- geometric transformations

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ray tracing

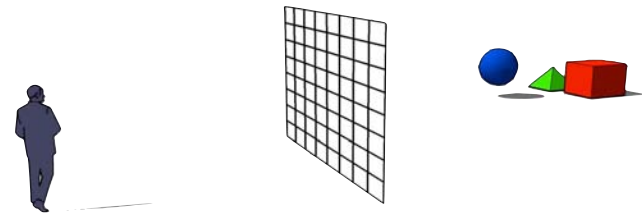
“image-order rendering”

```
for i = 1 to image_width {  
  for j = 1 to image_height {  
  
    generate “ray” from focal point through pixel (i,j)  
    which_obj = first object ray intersects in scene  
    calculate the shading on which_obj at intersection  
    pixel (i,j) = result of shading calculation  
  
  }  
}
```

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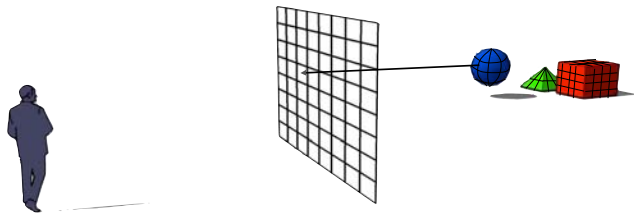
pipeline rendering



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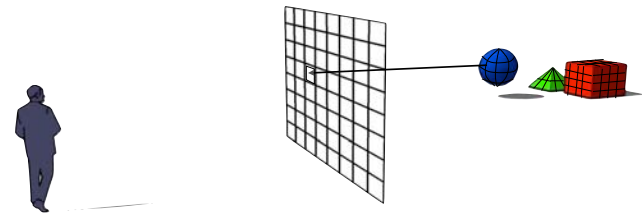
pipeline rendering



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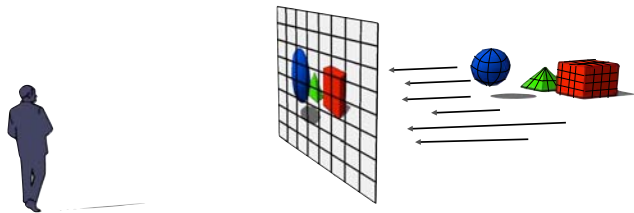
pipeline rendering



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pipeline rendering



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pipeline rendering

geometric operations:

"dicing" i.e. tessellation

shading: lighting & materials calculation

geometric transformations

perspective projections

optimized sorting for handling occlusion

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pipeline rendering

"object-order rendering"

```
for i = 1 to num_objects {  
    split object(i) into fragments  
    calculate the shading on each fragment  
    project fragments to pixels  
    pixel keeps color of closest fragment  
}
```

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ray tracing vs. pipeline rendering

raytracing has an intuitive geometric analogy that extends to many phenomena (shadows, reflections, transparency, etc.)

pipeline methods are often much faster

each has extensions for more realistic rendering: radiosity and global illumination

for interactive rendering, pipeline methods dominate, while for physically-based simulation of light transport, ray tracers dominate.

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mathematical preliminaries

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mathematical preliminaries

points

vectors

coordinate systems

equation forms

linear interpolation

barycentric combinations

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points

denotes a location in 1D, 2D, 3D, or n D

$$\mathbf{a} = [1 \ -2] \quad \mathbf{b} = [2 \ -1 \ 3]$$

this location is with respect to a particular **coordinate system** (to be defined later)

individual components referred to as \mathbf{a}_x , \mathbf{a}_y , \mathbf{a}_z (or generally, \mathbf{p}_x , \mathbf{p}_y , \mathbf{p}_z)

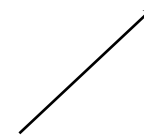
the number of components is referred to as the **dimension**

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vectors

vectors describes both an orientation and a magnitude (i.e. “direction” and length)



in graphics, vectors are used to denote:

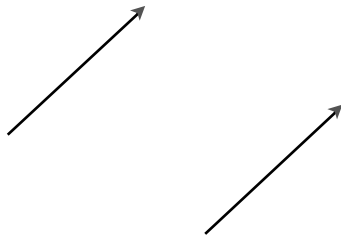
- geometric properties (like surface orientations)
- the direction that light follows as it illuminates a scene
- reflectance properties of materials
- and many other phenomena

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vectors

two vectors are **equivalent** if they have the same orientation and magnitude (like these):

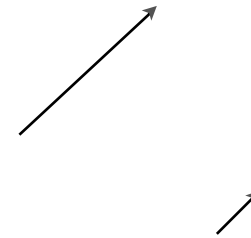


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vectors

these two vectors have the same orientation, but different magnitudes, and so are **not** equivalent

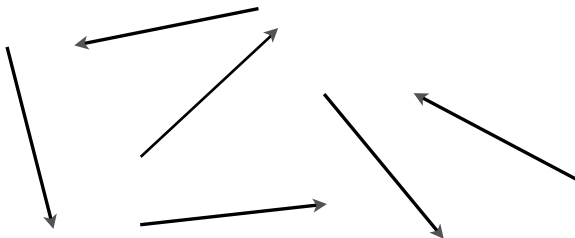


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vectors

these vectors have the same magnitude, but different orientations, and so are **not** equivalent:



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vectors

vectors are represented by ordered tuples of values, e.g.:

in 2D: $[3 \ 5]$

in 3D: $[2 \ 4 \ 9]$

as with points, the number of values specifies the **dimension** of the vector

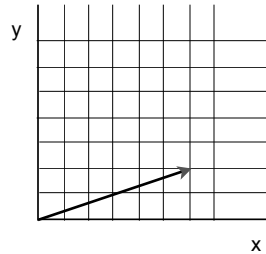
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vectors

vectors should be visualized by imagining them in the canonical coordinate system ("Real Space"), aligned with the origin:

the vector $[6 \ 2]$:



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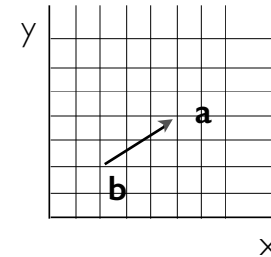
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vectors

vectors may be constructed by the difference between two points:

$$\mathbf{v} = \mathbf{a} - \mathbf{b}$$

$$\begin{bmatrix} 3 \\ 2 \end{bmatrix} = \begin{bmatrix} 5 \\ 4 \end{bmatrix} - \begin{bmatrix} 2 \\ 2 \end{bmatrix}$$



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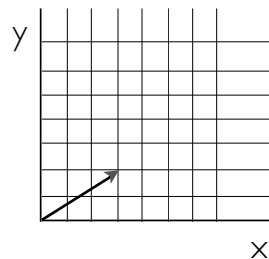
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vectors

therefore, the vector $[3 \ 2]$ is the same as the vector formed by subtracting the points:

$$\begin{bmatrix} 3 \\ 2 \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \end{bmatrix} - \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 3 \\ 2 \end{bmatrix} = \begin{bmatrix} 5 \\ 4 \end{bmatrix} - \begin{bmatrix} 2 \\ 2 \end{bmatrix}$$



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vectors

vectors may be developed this way in any number of dimensions

$$\mathbf{v} = \mathbf{a} - \mathbf{b}$$

$$\text{2D:} \quad \begin{bmatrix} 3 \\ 3 \end{bmatrix} = \begin{bmatrix} 5 \\ 4 \end{bmatrix} - \begin{bmatrix} 2 \\ 1 \end{bmatrix}$$

$$\text{3D:} \quad \begin{bmatrix} 2 \\ 2 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} - \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$$

etc.

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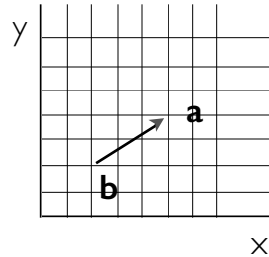
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point + vector

vectors may be added to points - you can visualize this as a displacement:

$$\mathbf{a} = \mathbf{b} + \mathbf{v}$$

$$\begin{bmatrix} 5 \\ 4 \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \end{bmatrix} + \begin{bmatrix} 2 \\ 2 \end{bmatrix}$$



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vector magnitude

the magnitude (or “length”) of a vector \mathbf{v} is given by:

$$\|\mathbf{v}\| = \sqrt{v_1^2 + v_2^2 + \dots + v_n^2}$$

where:

$$\mathbf{v} = \begin{bmatrix} v_1 \\ v_2 \\ \dots \\ v_n \end{bmatrix}$$

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unit vectors

a vector of length 1, i.e.

$$\|\mathbf{v}\| = 1$$

is called a unit vector, and is commonly used in shading calculations

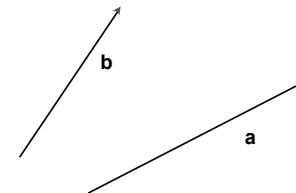
any nonzero vector may be **normalized** to unit length by:

$$\bar{\mathbf{v}} = \frac{\mathbf{v}}{\|\mathbf{v}\|}$$

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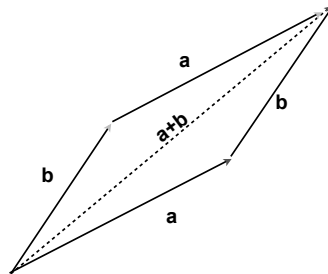
vector addition



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vector addition

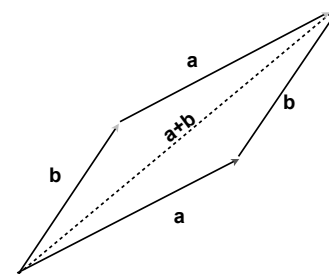


n.b.: $a+b = b+a$

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vector addition



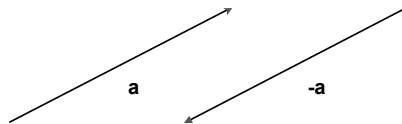
$$\mathbf{a} = [a_1 \ a_2 \ \dots \ a_n], \ \mathbf{b} = [b_1 \ b_2 \ \dots \ b_n]$$

$$\mathbf{a} + \mathbf{b} = [a_1 + b_1 \ a_2 + b_2 \ \dots \ a_n + b_n]$$

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vector negation



$-\mathbf{a}$ has the same magnitude, but opposite orientation, to \mathbf{a}

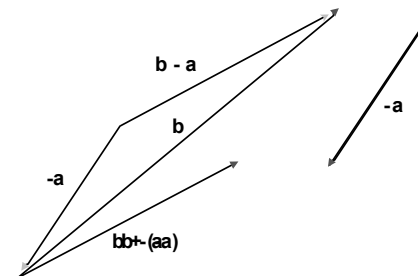
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vector subtraction

now that we have negation, we can define subtraction as:

$$\mathbf{b} - \mathbf{a} = \mathbf{b} + (-\mathbf{a})$$



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vector multiplication: scalar product

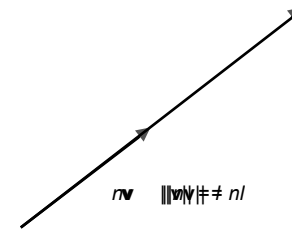
$$v = \begin{bmatrix} v_1 \\ v_2 \\ \dots \\ v_n \end{bmatrix}, \text{ with } \|v\| = l$$

$$n \cdot v = \begin{bmatrix} n \cdot v_1 \\ n \cdot v_2 \\ \dots \\ n \cdot v_n \end{bmatrix}, \text{ with } \|n \cdot v\| = nl$$

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vector multiplication: scalar product



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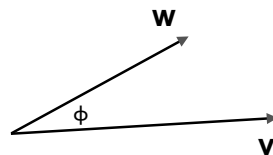
vector multiplication: dot product

for:

$$\mathbf{v} = [v_1 \ v_2 \ \dots \ v_n] \quad \text{and} \quad \mathbf{w} = [w_1 \ w_2 \ \dots \ w_n]$$

$$\mathbf{v} \cdot \mathbf{w} = v_1 w_1 + v_2 w_2 + \dots + v_n w_n \quad \text{also:}$$

$$\mathbf{v} \cdot \mathbf{w} = \|\mathbf{v}\| \|\mathbf{w}\| \cos \phi$$

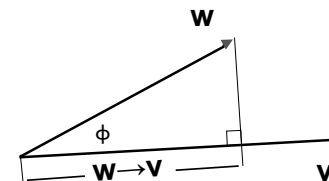


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vector multiplication: dot product

useful geometric technique: projection of one vector onto another:

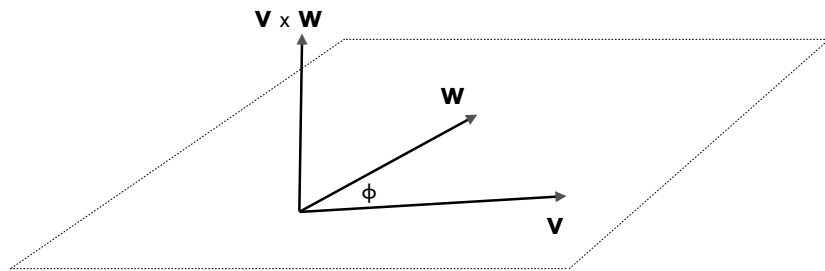


$$w \rightarrow v = \|w\| \cos \phi = \frac{w \cdot v}{\|v\|}$$

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vector multiplication: cross product



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vector multiplication: cross product

$$v \times w = \begin{bmatrix} v_2 w_3 - v_3 w_2 \\ v_3 w_1 - v_1 w_3 \\ v_1 w_2 - v_2 w_1 \end{bmatrix}$$

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vector multiplication: cross product

the cross product $\mathbf{v} \times \mathbf{w}$ is **perpendicular** to the constituent vectors \mathbf{v} , \mathbf{w}

its **magnitude** is given by:

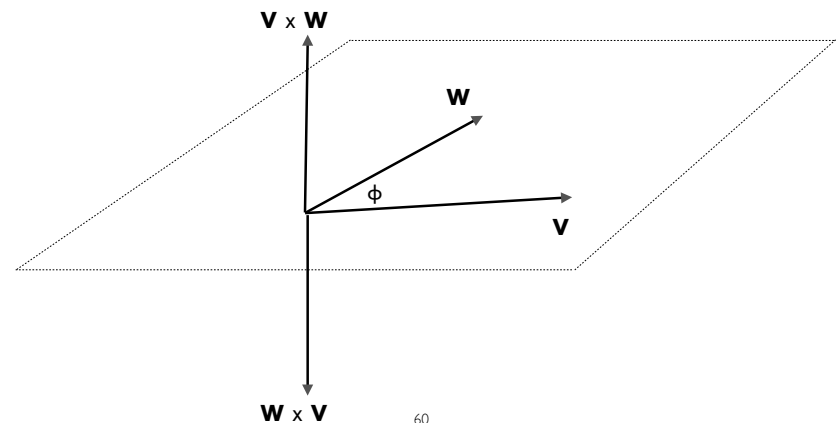
$$\|\mathbf{v} \times \mathbf{w}\| = \|\mathbf{v}\| \|\mathbf{w}\| \sin \phi$$

its **direction** is given by the **right-hand rule**, i.e. considering a counterclockwise rotation from \mathbf{v} to \mathbf{w} , $\mathbf{v} \times \mathbf{w}$ points “out” of the clock face

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vector multiplication: cross product



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uses of dot and cross products

both the dot product and the cross product can be used to get the angle between two vectors:

$$\mathbf{v} \cdot \mathbf{w} = \|\mathbf{v}\| \|\mathbf{w}\| \cos \phi$$

$$\|\mathbf{v} \times \mathbf{w}\| = \|\mathbf{v}\| \|\mathbf{w}\| \sin \phi$$

the dot product is useful for finding the projection of one vector on another

the cross product is useful for making 3-dimensional **coordinate systems** from two vectors

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vector bases

any 2D vector can be written as a combination of 2 non-zero 2D vectors that are linearly independent (in this case, that means not parallel).



$$\mathbf{c} = 1.7\mathbf{b} + 1.1\mathbf{a}$$

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vector bases

these 2 vectors form a **basis**



a 2D **basis**, in combination with an origin point forms a 2D coordinate system

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vector bases

any n -dimensional vector can be written as a combination of n non-zero n -dimensional vectors that are linearly independent (i.e. none can be composed of scaled sums of the others).

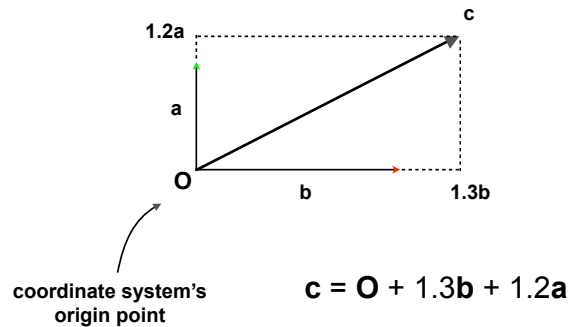
these vectors form an n -dimensional **basis**

with an origin, they form a coordinate system in n dimensions

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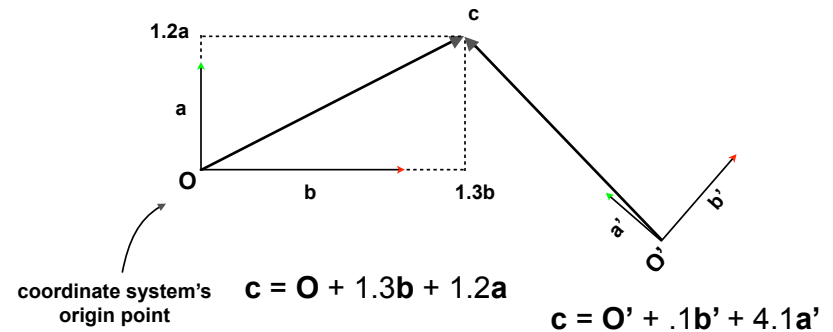
intro to coordinate systems



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intro to coordinate systems



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intro to coordinate systems

points in space have different coordinates depending on the coordinate system used

choice of coordinate system is arbitrary

a specific coordinate system is often chosen to:

- help simplify the mathematics
- simplify a problem conceptually

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choosing coordinate systems

example: car dashboard



in a moving car, the dashboard's location with respect to the earth is constantly changing

(here, the earth provides the coordinate system)

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choosing coordinate systems

example: car dashboard



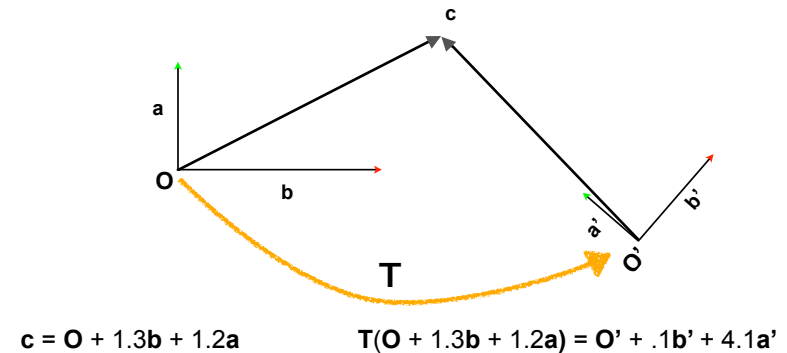
however, with respect to a fixed part of the car itself (e.g. the driver), the dashboard is at a fixed location

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intro to coordinate systems

points represented in one coordinate system may be easily represented in another by using **geometric transformations**



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coordinate systems

coordinate systems allow us to uniquely define:

- points
- vectors

geometric transformations allow us to define:

- translation
- rotation
- scaling
- shearing
- etc.

...as transformations between coordinate systems

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operations on vectors

vectors may be added, subtracted, rotated & otherwise transformed:

$$\mathbf{v} = \alpha_1 \mathbf{v}_1 + \alpha_2 \mathbf{v}_2 + \alpha_3 \mathbf{v}_3 + \dots + \alpha_n \mathbf{v}_n$$

reminder: vectors invariant under translation.

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operations on points

translation, rotation, & other geometric transformations:

$$\mathbf{p}' = \mathbf{p} + \mathbf{v}$$

subtraction, but NO arbitrary addition!

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linear combinations for points

while vectors may be combined in arbitrary linear combination, points may not!

$$\mathbf{x} = \alpha\mathbf{p} + \beta\mathbf{q} \quad \text{true only if } \alpha + \beta = 1$$

why? because translating \mathbf{x} , \mathbf{p} , \mathbf{q} by \mathbf{v} will not result in a valid equality if $\alpha + \beta \neq 1$

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equations: explicit

form: $y = f(x)$

examples:

$$y = mx + c$$

$$y = x^2$$

$$y = \sin(x)$$

problems: axis-dependent, ill-defined slopes, difficult to represent bounded surfaces

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equations: implicit

form: $0 = f(x, y)$

examples:

$$x^2 + y^2 - r^2 = 0$$

$$ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$$

problems: difficult to generate points directly

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equations: parametric

form:

$$\begin{aligned}x &= x(u) = f_1(u) \\ y &= y(u) = f_2(u) \\ z &= z(u) = f_3(u)\end{aligned}$$

examples:

$$x(t) = \cos(t), y(t) = \sin(t) \quad \text{circle}$$

$$\begin{aligned}x(t) &= x_1 + t(x_2 - x_1) \\ y(t) &= y_1 + t(y_2 - y_1)\end{aligned} \quad \begin{array}{l} \text{line through} \\ (x_1, y_1) \text{ and } (x_2, y_2) \end{array}$$

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interpolation

the process of computing a curve/surface that includes a given set of points

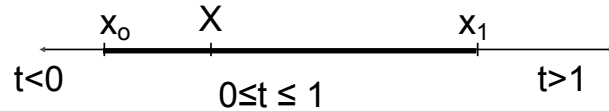
[vs. approximation: computing a curve that remains "near" a set of points]

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linear interpolation

$$X(t) = (1-t) \cdot x_0 + t \cdot x_1$$



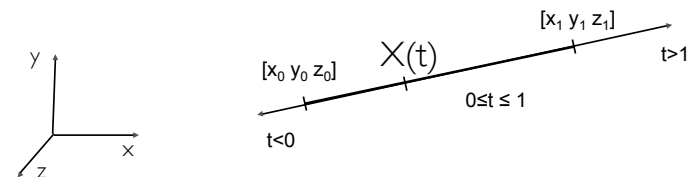
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linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

$$X(t) = \begin{bmatrix} x(t) \\ y(t) \\ z(t) \end{bmatrix} = (1-t) \begin{bmatrix} x_0 \\ y_0 \\ z_0 \end{bmatrix} + t \begin{bmatrix} x_1 \\ y_1 \\ z_1 \end{bmatrix}$$

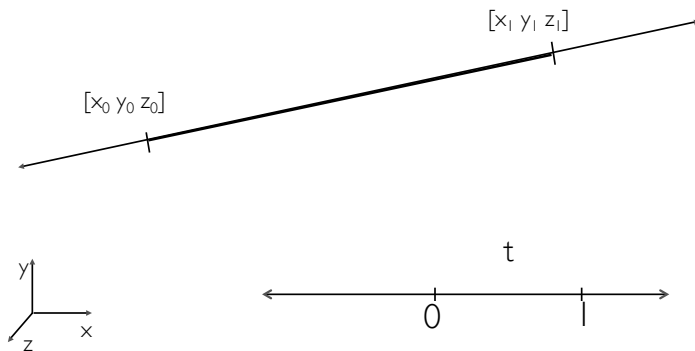


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linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

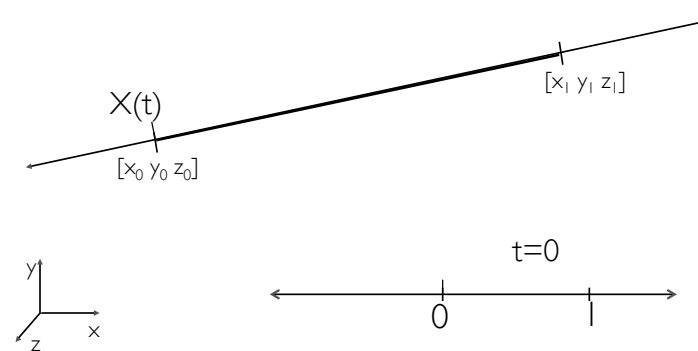


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linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

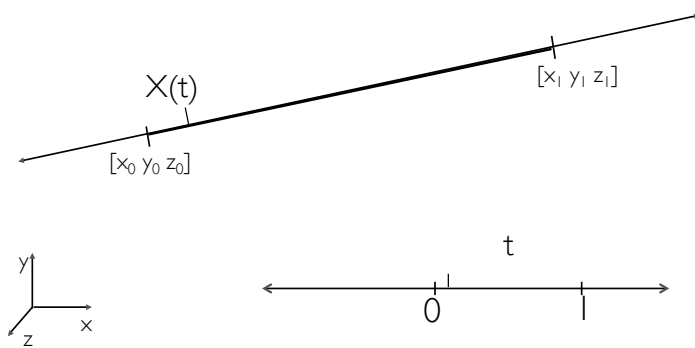


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linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

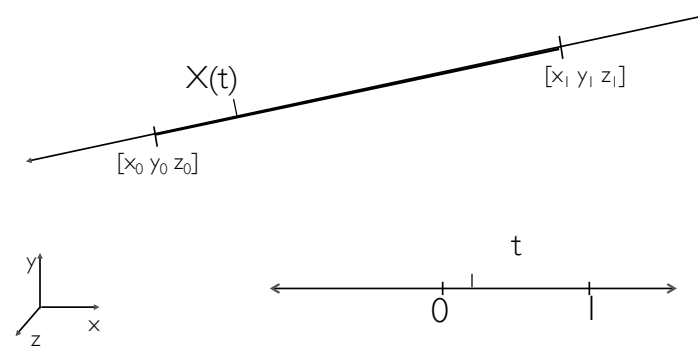


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83

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

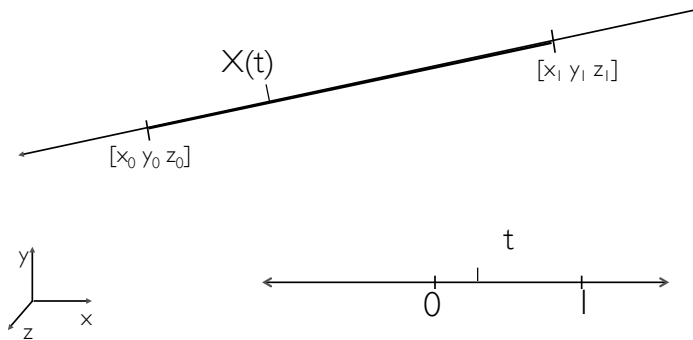


84

84

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

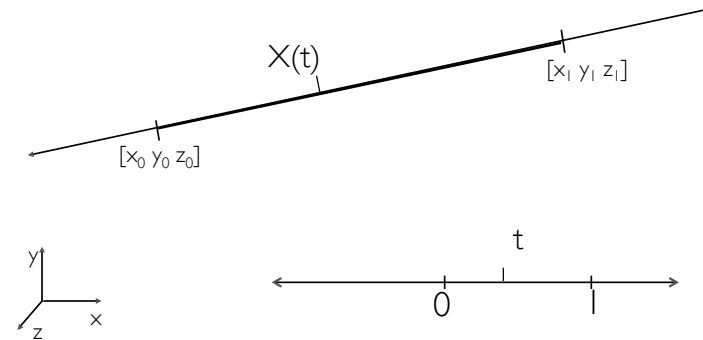


85

85

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

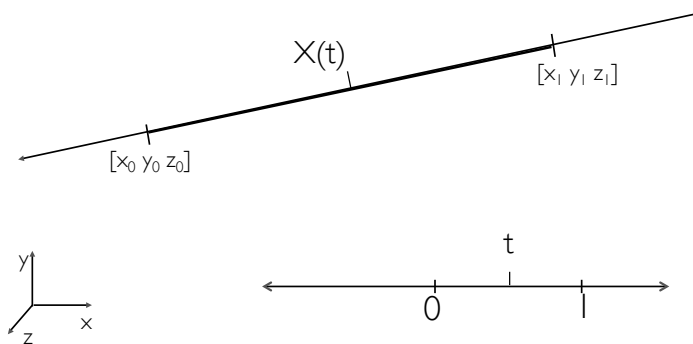


86

86

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

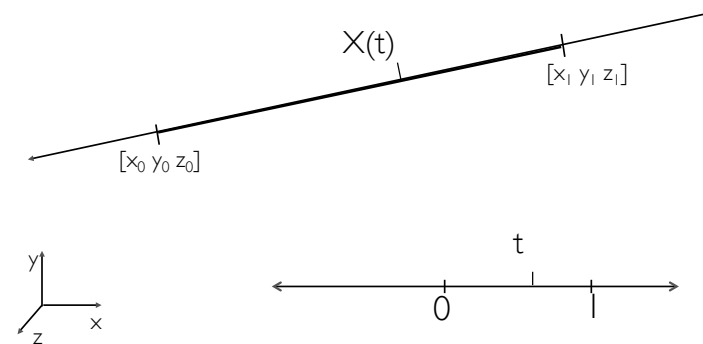


87

87

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

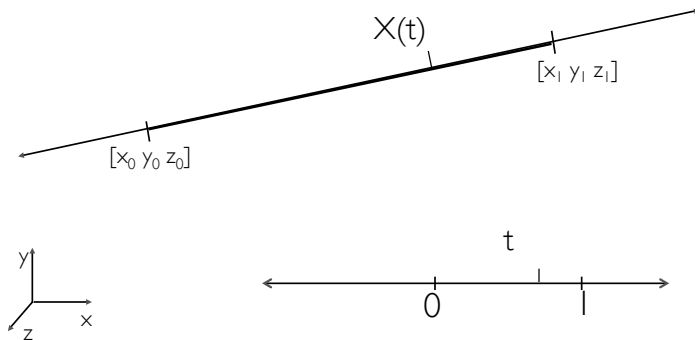


88

88

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

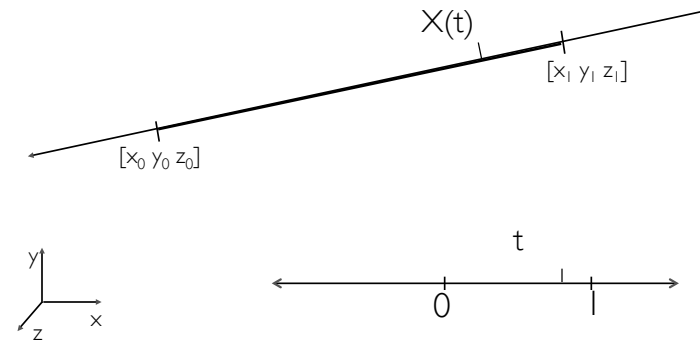


89

89

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

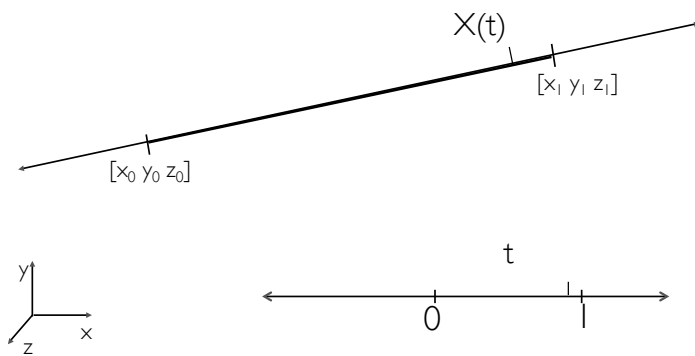


90

90

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

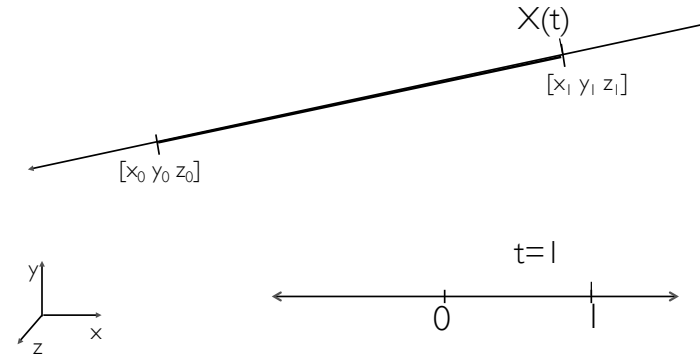


91

91

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

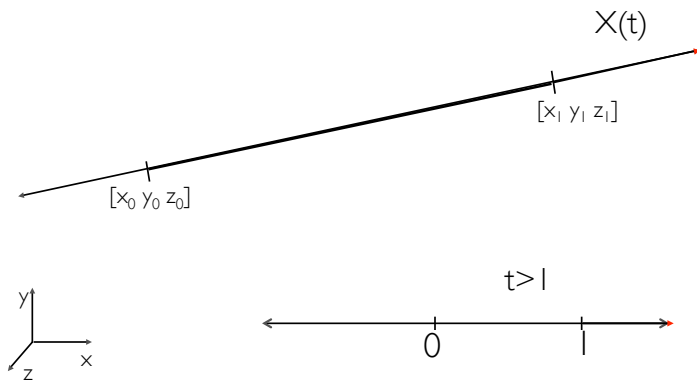


92

92

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

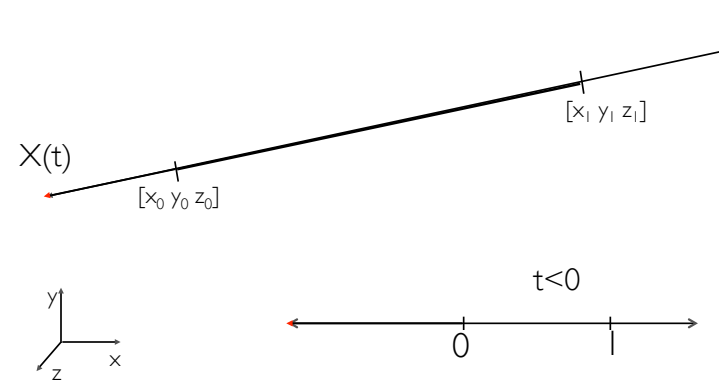


93

93

linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$

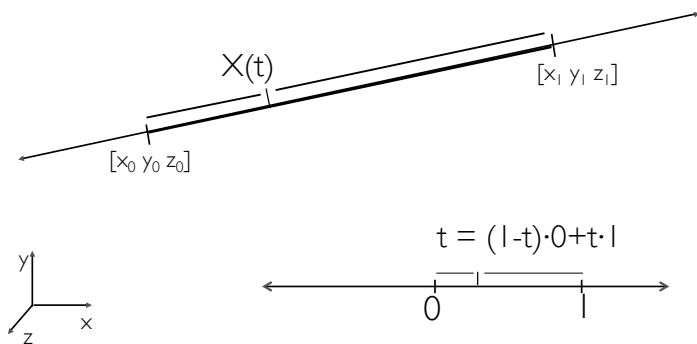


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linear interpolation

$$X(t) = (1-t)x_0 + tx_1$$



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some notes on light & vision

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dual nature of light

“wave-particle duality”: light can behave as:

a wave - as evidenced by the double-slit experiment

a particle - as evidenced by the photoelectric effect

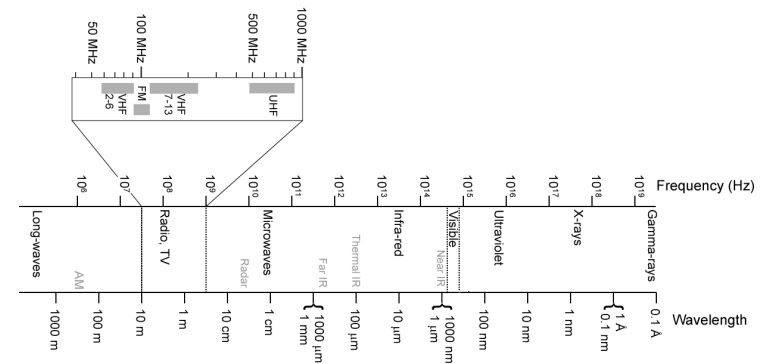
in this class, we will almost always be discussing light in terms of geometric optics, which models light as a particle (i.e. photons).

but to discuss color we must use the wave properties.

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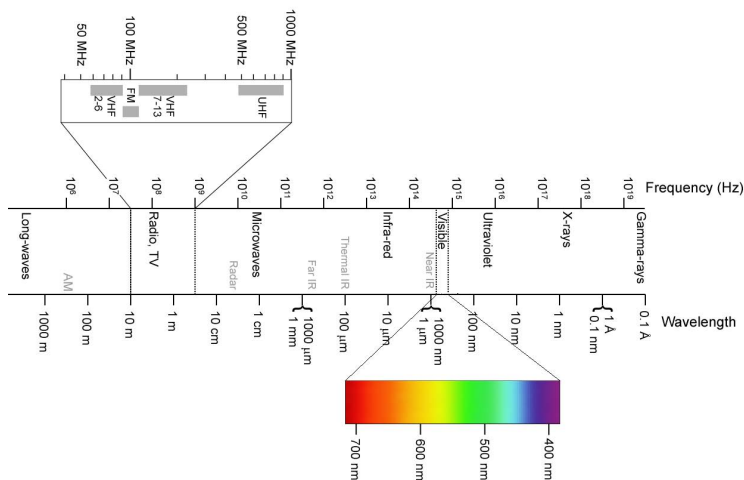
the electromagnetic spectrum



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the visible spectrum

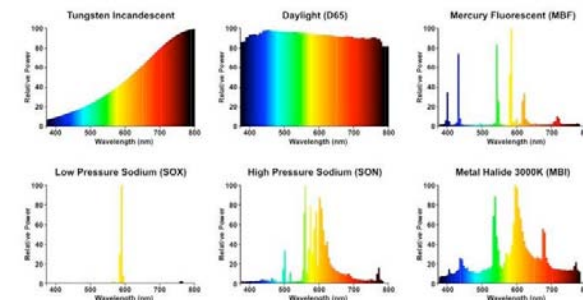


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spectral power distribution (SPD)

energy emitters (and reflectors) can be characterized by their SPD: a graph of “intensity” vs. frequency



note: “intensity” is really a vague term - here we mean radiant exitance (radiant flux per area).

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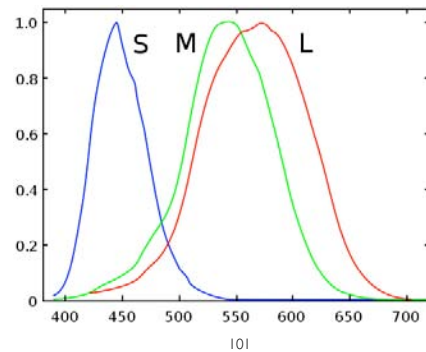
100

tristimulus theory of color vision

the human eye has 3 types of color receptors (*cones*)

incident light is reduced to a function of 3 signals by the eye

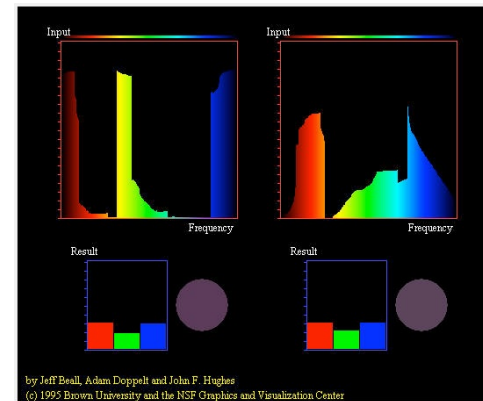
the response is a function of wavelength for each type of receptor



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metamers

metamers are two emitters (or reflectors) with different SPDs, but which appear the same (i.e. perceptually).



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Q: how many component colors do we use?

for monitors, 3: RGB space (for manufacturing simplicity)

more general devices may have higher dimensions (e.g. CMYK space)

all are approximations to the CIE XYZ color space (which defines the range of human color perception)

[note: a *color spaces* describes the entire range of wavelengths possible with a specific representation]

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so what 3 colors do we use?

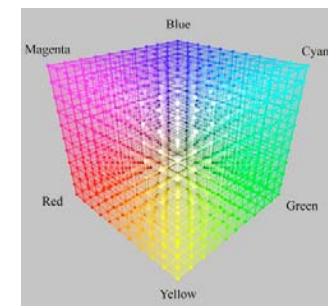
RGB uses additive color mixing of red, green & blue:

red + green = yellow

green + blue = cyan

blue + red = magenta

red + green + blue = white



if we also allow intensity of each component to be controlled, we can go from black to white, and the corresponding shades of colors as well.

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encoding RGB

colors are encoded as triples: $[r\ g\ b]$

we often illustrate colors though normalized encoding: each element is in $[0\ 1]$

e.g.

black = $[0\ 0\ 0]$

yellow = $[1\ 1\ 0]$

white = $[1\ 1\ 1]$

magenta = $[1\ 0\ 1]$

red = $[1\ 0\ 0]$

cyan = $[0\ 1\ 1]$

green = $[0\ 1\ 0]$

gray = $[a\ a\ a]$ (for any a on $[0\ 1]$)

blue = $[0\ 0\ 1]$

blue = $[0\ 0\ 1]$

in implementation, each channel will use the entire range of values of its data type

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images

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what is an image?

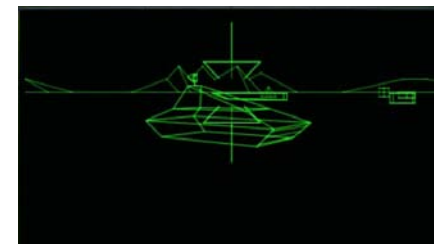
an image is a 2D representation of energy (usually light, sometimes sound)

for modern devices - raster devices - an image is a rectangular set of samples of a continuous 2D function

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before raster devices: vector devices!



advantages: extremely high resolution

disadvantages: slow, unreliable, hard to do color

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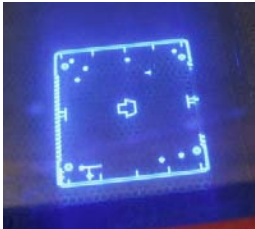
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(we still have some vector devices around)

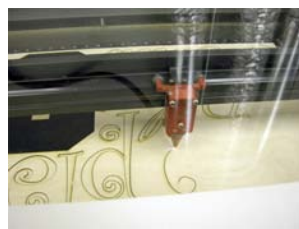
pen plotters

laser cutters

rapid prototyping machines



rapid prototyping machine drawing a part



laser cutters cutting metal (top) and engraving wood

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raster devices

raster devices use arrays of pixels or sensors to display or acquire colors

n.b. raster devices are resolution-dependent, measured in one of:

dots-per-inch (dpi) - usually for print processes

pixels-per-inch (ppi) - usually for monitors

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raster hardcopy devices

system where a digital image is converted into a series of dots or pixels. This system would allow us to use a commercial supplier.

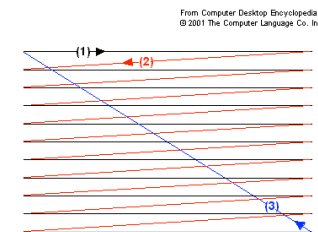
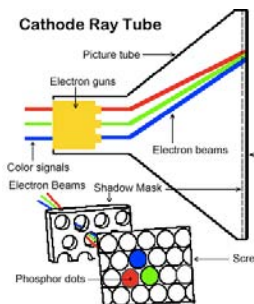


both dot matrix and inkjet printers are raster devices

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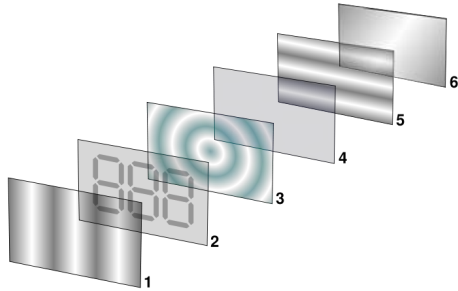
raster devices - CRT



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raster devices - LCD display

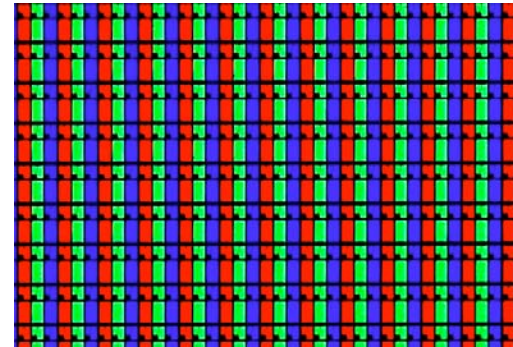


layers in an LCD display: 1,5: polarizing filters. 2, 4 electrode plates. 3: liquid crystal. 6: backlight

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LCD display - up close

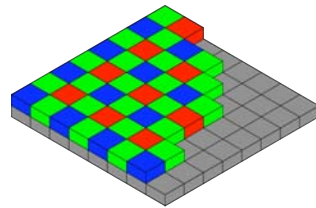
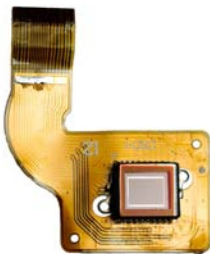


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input devices

digital cameras, film & “flatbed” scanners
(all have resolutions much higher than displays)

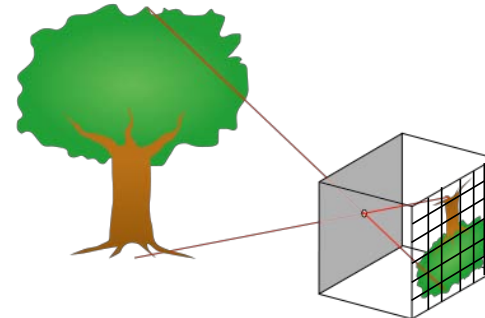


camera CCD and color filter array (image is processed using *demosaicing*)

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image formation



light on sensor as a 2D function

$$I(x, y) : \mathbb{R}^2 \rightarrow V$$

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raster image from $I(x,y)$

how do we go from continuous $I(x,y)$ to pixel value in a raster image?

camera or scanner pixel (i.e. input device):

measurement of the average “intensity” over some small area around the pixel

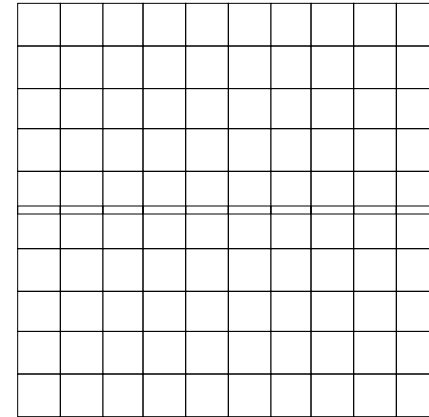
but: unless you know very specifically the device an image came from, all you can assume is:

a pixel is a point sample and image is an array of point samples

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display pixels



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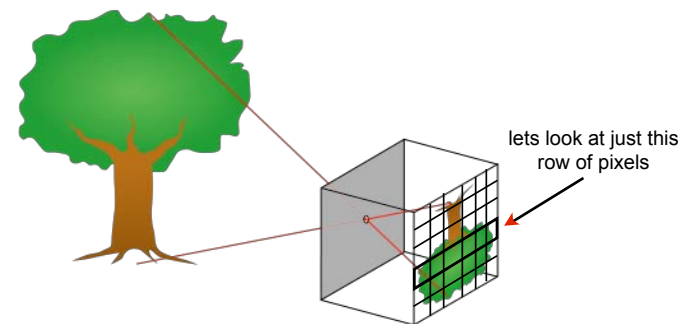
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image pixels (samples)

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image formation



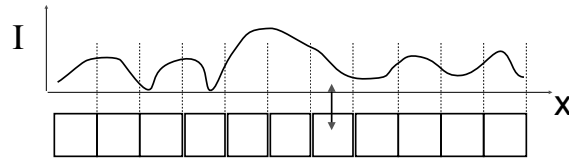
light on sensor as a 2D function

$$I(x, y) : \mathbb{R}^2 \rightarrow V$$

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1d pixel array



each pixel gets average intensity for its interval of $I(x)$

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image pixel values

data stored in pixel values:

- 1 value for grey scale, OR
- 3 values: 1 each for red, green and blue
- alpha : a separate value designating opacity

each of red/blue/green/alpha is called a **channel**

Q: what data type should each value be?

- depends on both the device and the available memory
- e.g. 10 megapixel camera, 32-bit data for each color = 115MB!

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pixel data types and applications

1 bit : (b&w) - hires text displays (e.g. digital ink)

8 bit RGB (24 bits per pixel): web & email images

12-16 bit RGB (36-42 bits per pixel): highend digital cameras

16-bit greyscale (16 bits per pixel): medical imaging

16-bit floating-point RGB (48 bits per pixel): HDR images & rendering

32-bit floating-point RGB (96 bits per pixel): HDR images & rendering

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what does color depth give us?

data type - bits & format per channel	description	# of possible colors per channel	# of possible colors overall
1	black & white	2	2
8 fixed precision	RGB (+A) "24-bit color"	256 per channel (0-255)	16 million
16 fixed precision	greyscale "16-bit greyscale"	65536 (0-65535)	65536
16 fixed precision	RGB (+A) "48-bit color"	65536 (0-65535)	281 trillion
16 floating point	HDR RGB (+A) "half precision"	65536 (6x10)	281 trillion
32 floating point	HDR RGB (+A) +Z	4.3 trillion	!!!!

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dynamic range

dynamic range specifies the maximum contrast possible, and is a major factor in image quality

$$R_d = I_{\max} / I_{\min} \quad (\text{i.e. maximum intensity divided by minimum intensity})$$



note:

natural illumination has a dynamic range of about 10⁶

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dynamic range

$$R_d = I_{\max} / I_{\min} \quad (\text{i.e. maximum intensity divided by minimum intensity})$$

typical values:

- desktop display: 20:1 to 100:1 (best)
- photograph, mono print: 30:1
- photograph, transparency: 1000:1
- high dynamic range (HDR) display: 10000:1

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dynamic range

how many levels are needed?

rule of thumb: < 2% between adjacent intensity:

- min: 0;
- value 1: I_{\min}
- value 2: $(1.02)^2 \cdot I_{\min}$
- value 3: $(1.02)^3 \cdot I_{\min}$
- value 4: $(1.02)^4 \cdot I_{\min}$
- etc.

this ends up being about 12 steps per unit of dynamic range

e.g. if we want a R_d of 20:

$$20 \cdot 12 = 240 \text{ steps}$$

(just enough in an 8-bit fixed-precision channel: 0-255)

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dynamic range - integer vs. floating point

in 48-bit integer color, the dynamic range per channel is:

$$65535 / 1 = 65535$$

in “half” precision format, the dynamic range is:

$$6.5 \times 10^4 / 6 \times 10^{-8} = 1 \times 10^{12}$$

Q: how can the ranges be different when the # of possible colors is the same?

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**effect of reduced bit depth
(i.e. not enough levels)**



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quantization artifact - “banding”



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“clipping” - highlights all set to max



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alpha

alpha is a fourth per-pixel channel, in addition to R, G, & B

it allows one to specify transparency, useful when images are being composited

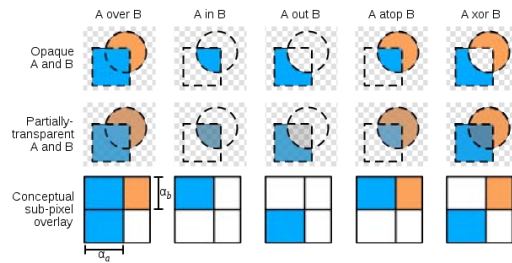
e.g. “over” operator for pixels:

$$\text{final color} = \text{fg_color} * \alpha + \text{bg_color} * (1-\alpha)$$

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alpha compositing



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The OpenEXR Image Format

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OpenEXR

open-source HDR format developed by ILM

supports 16-bit ("half") & 32-bit floating point, and 32-bit integer pixels

multiple lossless compression algorithms

scan-line and tile- based methods

portable & extensible

compatible with graphics hardware

c++-based

see: www.openexr.com

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OpenEXR example



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OpenEXR image file interface

we will be using the “simple” OpenEXR interface

we will be constrained to using the “half” pixel type

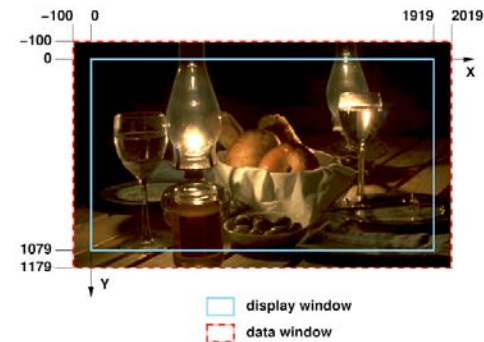
we can only read/write RGBA files

we will only be addressing scanline-based images
(though the simple interface supports tiling as well)

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OpenEXR image coordinates



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OpenEXR “half” pixels

```
struct Rgba
{
    half r; // red
    half g; // green
    half b; // blue
    half a; // alpha (opacity) (convention: 0 to 1)
};
```

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the “half” format

16-bit floating-point format for each channel (R, G, B, A, etc)

65536 possible values for each channel

minimum positive value: 6×10^{-8}

maximum positive value: 6.5×10^4

dynamic range: $6.5 \times 10^4 / 6 \times 10^{-8} = 1 \times 10^{12}$

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writing an image file

```
void
writeRgba (const char fileName[],
           const Rgba *pixels,
           int width,
           int height)
{
    //
    // Write an RGBA image using class RgbaOutputFile.
    //
    // - open the file
    // - describe the memory layout of the pixels
    // - store the pixels in the file
    //

    RgbaOutputFile file (fileName, width, height, WRITE_RGBA);
    file.setFrameBuffer (pixels, 1, width);
    file.writePixels (height);
}
```

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reading an image file

```
void
readRgba (const char fileName[],
          Array2D<Rgba> &pixels,
          int &width,
          int &height)
{
    //
    // Read an RGBA image using class RgbaInputFile:
    //
    // - open the file
    // - allocate memory for the pixels
    // - describe the memory layout of the pixels
    // - read the pixels from the file
    //

    RgbaInputFile file (fileName);
    Box2i dw = file.dataWindow();

    width = dw.max.x - dw.min.x + 1;
    height = dw.max.y - dw.min.y + 1;
    pixels.resizeErase (height, width);

    file.setFrameBuffer (&pixels[0][0] - dw.min.x - dw.min.y * width, 1, width);
    file.readPixels (dw.min.y, dw.max.y);
}
```

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example main

```
int
main (int argc, char *argv[])
{
    try
    {
        int w, h;
        Array2D<Rgba> p;

        readRgba ("myimage.exr", p, w, h);

        cout << "width height is " << w << " " << h << endl;

        // convert to a red-only image:
        for (int y = 0; y < h; ++y)
        {
            for (int x = 0; x < w; ++x)
            {
                Rgba &px = p[y][x]; // get the pixel
                px.g = 0; px.b = 0; px.a = 1; // note: px.r left alone!
            }
        }

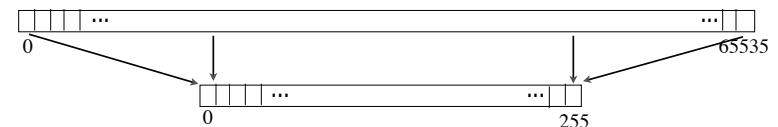
        writeRgba ("myimage_red.exr", &p[0][0], w, h);
    }
    catch (const std::exception &exc)
    {
        std::cerr << exc.what() << std::endl;
        return 1;
    }

    return 0;
}
```

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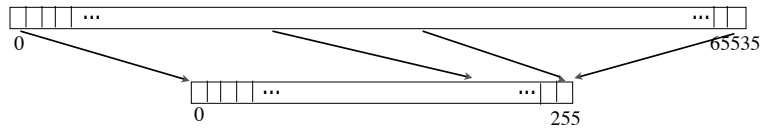
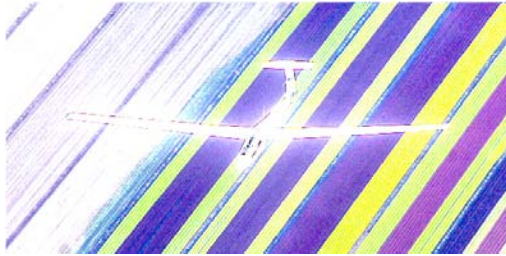
exposure & compression in EXR format: displaying “half” format on 8-bit RGB



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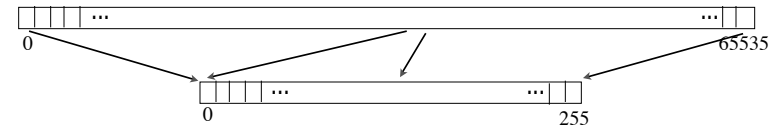
exposure & compression in EXR format: displaying “half” format on 8-bit RGB



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exposure & compression in EXR format: displaying “half” format on 8-bit RGB



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online resources

on the class resources page:

- openEXR technical intro
- reading & writing openEXR files

online:

- www.openexr.com

on CLIC machines:

- libraries, test programs, and test images

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Ray Tracing

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introduction

basic idea:

- trace the path light follows through a scene.
- model its material interactions.
- iterate. a lot.

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introduction

strength of the algorithm:

- very intuitive solution to visible surface determination
- extends to many secondary phenomena (i.e. shadows, refraction, multiple lights, etc.)
- produces very realistic images

weaknesses:

- not good for some common secondary phenomena (diffuse inter-reflection)
- slow

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ray traced example scene



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ray traced example scene



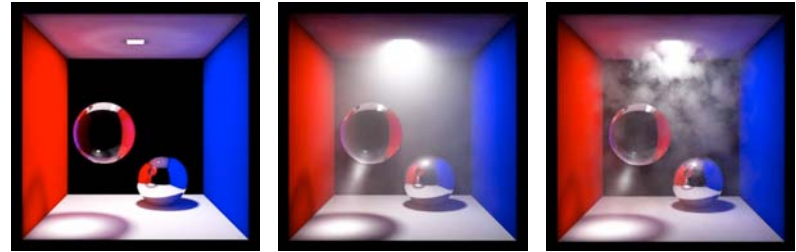
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ray traced example scene



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ray traced example scene



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