

1 Exponential

Definition 1.1. *Let \mathcal{C} a category. For any $B, C \in \mathcal{C}$, (C^B, ev) forms an exponential where $C^B \in \mathcal{C}$ and $ev : C^B \times B \rightarrow C$, if for any object $A \in \mathcal{C}$ and $f : A \times B \rightarrow C$, there is a unique $u : A \rightarrow C^B$ such that $f = ev \circ (u \times 1_B)$. In other words, the follow diagram commutes.*

$$\begin{array}{ccc} A \times B & & \\ \downarrow u \times 1_B & \searrow f & \\ C^B \times B & \xrightarrow{ev} & C \end{array}$$