

# Lithium Exchange Processes in the Conduction Network of the Nasicon $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$ Series ( $0 \leq x \leq 2$ )

K. Arbi, M. A. París, and J. Sanz\*

*Instituto de Ciencia de Materiales de Madrid (ICMM), Consejo Superior de Investigaciones Científicas (CSIC) Cantoblanco, 28049 Madrid, Spain*

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Structural sites occupied by lithium in the rhombohedral  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series ( $0 \leq x \leq 2$ ) have been investigated by  $^7\text{Li}$  NMR spectroscopy. At room temperature, the XRD patterns of the end-members of the series display rhombohedral  $R\bar{3}c$  symmetry in  $\text{LiTi}_2(\text{PO}_4)_3$  and triclinic  $C\bar{1}$  in  $\text{LiZr}_2(\text{PO}_4)_3$ . In the first compound, Li ions occupy  $M_1$  sites; however, in the second one Li occupy intermediate  $M_{1/2}$  sites. As the temperature increases, a first-order displacive transformation is detected in the triclinic phase, but a second-order/disorder transition is detected in the rhombohedral phase. From the temperature dependence of the  $^7\text{Li}$  NMR quadrupole constant ( $C_Q$ ) of the two compounds, the evolution of  $M_1$  and  $M_{1/2}$  sites occupancy in the Nasicon conduction network has been deduced. At high temperatures, analyzed phases tend toward a disordered rhombohedral phase, in which both  $M_1$  and  $M_{1/2}$  sites are equally populated and in which lithium mobility is favored by the existence of vacant  $M_1$  sites. According to this study, this phase can also be obtained by substituting Ti by Zr in the  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series.

## Introduction

Interest in lithium ion conducting solids has considerably increased because of their potential application as electrolytes in rechargeable lithium batteries.  $\text{LiM}^{\text{IV}}_2(\text{PO}_4)_3$  compounds with NASICON<sup>1</sup> structure (acronym for Na SuperIonic Conductors) have been extensively studied for their good ionic conductivity.<sup>2–6</sup> In these compounds, structure is formed by  $\text{M}_2(\text{PO}_4)_3$  units in which each  $\text{MO}_6$  octahedron shares corners with six  $\text{PO}_4$  tetrahedra and each tetrahedron shares oxygens with four octahedra (Figure 1a). The ideal framework displays the rhombohedral symmetry (space group  $R\bar{3}c$ ), but in some particular cases a triclinic distortion (space group  $C\bar{1}$ ) has been detected.<sup>7–9</sup> In the rhombohedral  $\text{LiM}^{\text{IV}}_2(\text{PO}_4)_3$  phases ( $\text{M}^{\text{IV}} = \text{Ge}$  and  $\text{Ti}$ ), Li ions occupy  $M_1$  sites at trigonal  $c$ -axes, with a six-fold oxygen coordination. However, in triclinic phases ( $\text{M}^{\text{IV}} = \text{Sn}$ ,  $\text{Hf}$ ,  $\text{Zr}$ ) Li ions are four-fold coordinated at intermediate  $M_{1/2}$  positions between  $M_1$  and  $M_2$  sites (Figure 1a). Triclinic  $\text{LiM}^{\text{IV}}_2(\text{PO}_4)_3$  compounds exhibit a triclinic-rhombohedral transition that has been analyzed by neutron diffraction.<sup>7–10</sup>

In general, Li conductivity is higher and activation energy lower in rhombohedral phases. In these samples, activation energies for lithium motion decreases when the size of tetravalent M cations increases.<sup>6</sup> In the present work,  $^7\text{Li}$  NMR spectroscopy has been used to analyze occupation of structural sites and mobility of lithium in the fast ion conductor series  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  ( $0 \leq x \leq 2$ ). In these compounds, the substitution of Ti by Zr expands the rhombohedral unit cell (see Table 1); however, information concerning the Li-sites occupation is not available.

## Experimental Section

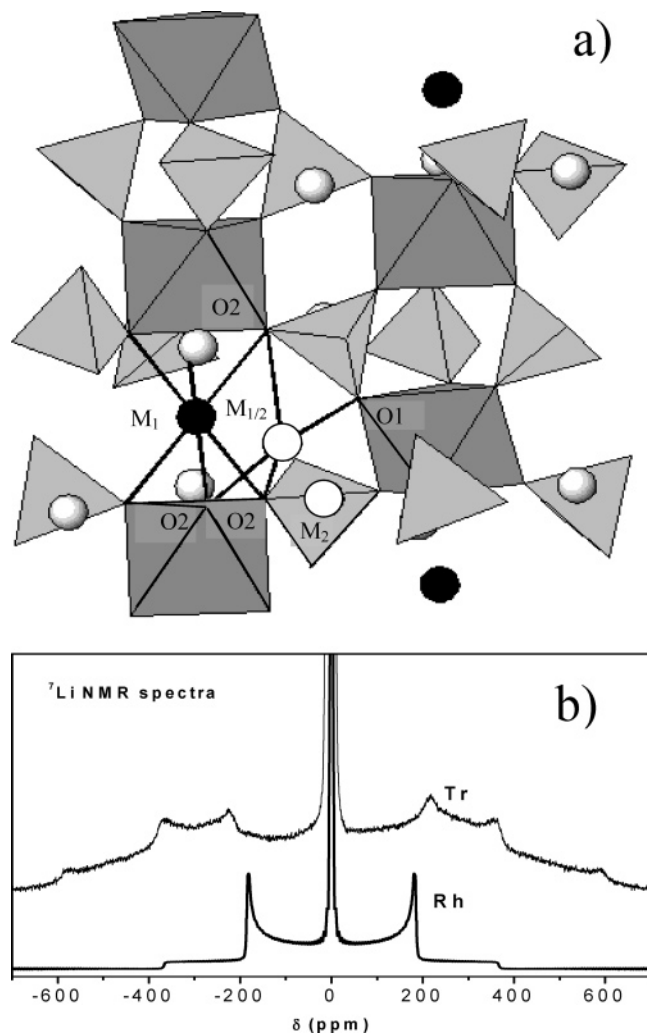
$\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  compounds ( $0 \leq x \leq 2$ ) have been prepared following the method described elsewhere.<sup>11,12</sup> X-ray diffraction (XRD) was used to assess purity of prepared compositions. XRD patterns were recorded with the Cu  $K\alpha$  radiation ( $\lambda = 1.5405981 \text{ \AA}$ ) in the temperature range 25–500 °C, using a high-temperature AP HTK10 camera adapted to a PW 1050/25 Phillips diffractometer. Powder XRD patterns were collected in the 10–70°  $2\theta$  range with a step size of 0.02° and a counting time of 0.1 s/step. The Fullprof program was used to determine unit cell parameters of prepared samples.

$^7\text{Li}$  MAS NMR spectra were recorded in a MSL-400 Bruker spectrometer (9.4 T) at 155.50 MHz. Spectra were obtained after  $\pi/2$  pulse irradiation ( $\approx 4 \mu\text{s}$ ) with a recycling time of 10 s. The number of scans was 400. In the temperature range 100–450 K, quadrupole interactions remain small ( $C_Q < 180 \text{ kHz}$ ), making the irradiation of the central and satellite transitions non selective.  $^7\text{Li}$  NMR chemical shifts were given relative to a 1 M LiCl aqueous solution. The fitting of the NMR spectra was carried out with the Bruker WINFIT software package.<sup>13</sup> This program allows the position, line width and intensity of components to be determined; however, quadrupole  $C_Q$  and  $\eta$  values have to be deduced with a trial and error procedure.

## Results and Discussion

XRD patterns of the  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  ( $0 \leq x \leq 2$ ) series are given in Figure 2. In this figure, a progressive shift of diffraction peaks to lower  $2\theta$  values is observed that corresponds to the unit cell expansion induced by Zr for Ti substitution. The progressive increase of the  $c/a$  ratio produces the splitting

\* To whom correspondence should be addressed. E-mail: jsanz@icmm.csic.es.



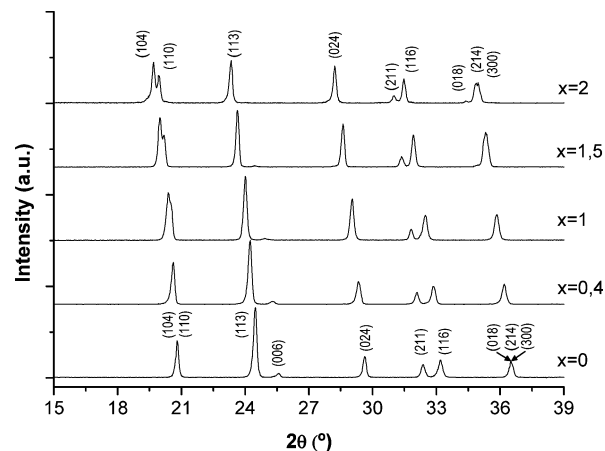
**Figure 1.** (a) Rhombohedral structure of Nasicon compounds showing structural  $M_1$ ,  $M_{1/2}$ , and  $M_2$  sites. (b) Static  $^7\text{Li}$  NMR spectra of triclinic and rhombohedral  $\text{LiZr}_2(\text{PO}_4)_3$  phases.

**TABLE 1: Quadrupole Constant,  $C_Q$  (kHz), Asymmetry Parameter,  $\eta$ , and Hexagonal Unit Cell Parameters of the Rhombohedral  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  Series**

$x_{\text{Zr}}$	$C_Q$ (kHz)	$\eta$ (dimensionless)	$a$ (Å)	$c$ (Å)
0	44	0	8.511	20.843
0.4	50	0	8.566	21.071
0.63	65	0	8.605	21.212
1	73,3	0	8.672	21.462
1.5	88	0	8.764	21.779
2	100,5	0	8.847	22.241

of (104) and (110) peaks near  $20^\circ$ , and that of the (214) and (300) peaks near  $36.5^\circ$ . Unit cell parameters deduced from these patterns are given in Table 1. In the case of the sample  $x = 2$ , only the XRD pattern of the rhombohedral phase, recorded at  $70^\circ\text{C}$ , has been considered.

$^7\text{Li}$  NMR ( $I = 3/2$ ) spectra of the  $\text{LiZr}_2(\text{PO}_4)_3$  samples are formed by a central ( $-1/2, 1/2$ ) and two satellite ( $-3/2, -1/2$  and  $1/2, 3/2$ ) transitions.<sup>14</sup> In previous works, quadrupole constants ( $C_Q$  and  $\eta$  parameters) of lithium located at  $M_1$  and  $M_{1/2}$  sites were deduced in  $\text{LiM}^{\text{IV}}_2(\text{PO}_4)_3$  compounds.<sup>15,16</sup> In  $\text{LiZr}_2(\text{PO}_4)_3$  samples, satellite lines of the triclinic phase are split over a larger region than in the rhombohedral phase (see Figure 1b). From analysis of  $^7\text{Li}$  NMR spectra, quadrupole  $C_Q$  and  $\eta$  constants of the  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series have been deduced (see Table 1).



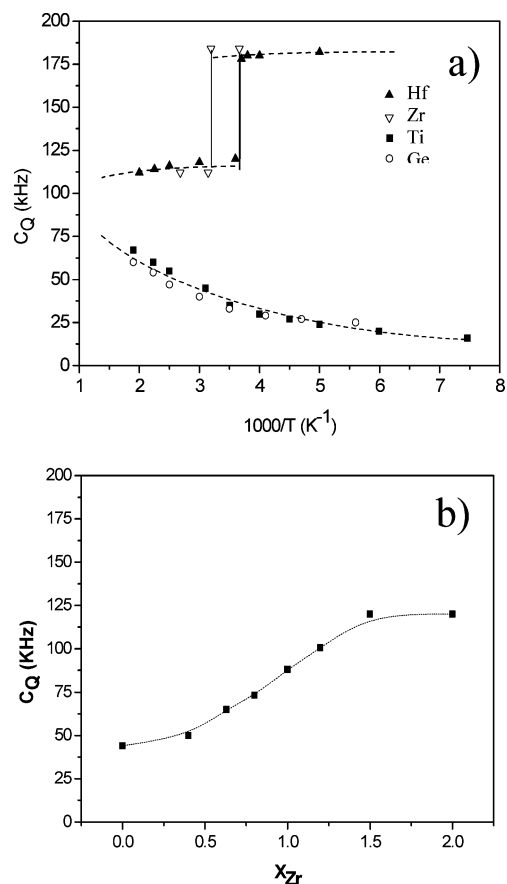
**Figure 2.** XRD patterns of the series  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  recorded at room temperature. The XRD pattern of the sample with  $x = 2$  corresponds to that of the rhombohedral phase recorded at  $70^\circ\text{C}$ .

In previous works, quadrupole  $C_Q$  and  $\eta_Q$  constants were calculated with expressions<sup>15,16</sup>

$$C_Q = \frac{e^2 Q V_{zz}}{h} \quad \eta_Q = \frac{V_{xx} - V_{yy}}{V_{zz}} \quad (1)$$

where  $Q$  is the quadrupole moment of nuclei and  $V_{xx}$ ,  $V_{yy}$ ,  $V_{zz}$  are the principal values of the electric field gradient (EFG) tensor at structural sites occupied by lithium. In the triclinic  $\text{LiZr}_2(\text{PO}_4)_3$  phase, quadrupole constants calculated for  $M_{1/2}$  sites,  $C_Q = 180$  kHz and  $\eta_Q = 0.6$ , are similar to those deduced from NMR spectra recorded at 300 K.<sup>11</sup> At these sites, lithium exhibits an almost planar four-fold coordination with Li–O distances between 1.9 and 2.26 Å.<sup>9</sup> In the rhombohedral  $\text{LiTi}_2(\text{PO}_4)_3$  phase, the experimental  $C_Q = 35$  kHz deduced from NMR spectra at 300 K corresponds to that calculated for lithium at  $M_1$  sites, with Li–O distances near 2.1 Å.<sup>12,17</sup> In the rhombohedral  $\text{LiZr}_2(\text{PO}_4)_3$  sample, mean Li–O distances should increase above 2.40 Å in  $M_1$  sites; however, Li ions move to six positions related by  $-3$  symmetry axes in order to reduce Li–O distances to 2.3 Å in  $M_1$  cavities.<sup>10</sup> In this phase, the analysis of quadrupole constants was difficult because of the Li hopping between equivalent sites.

The mobility of lithium produces the partial average at the NMR time scale ( $t \sim 10^{-8}$  s) of quadrupole  $C_Q$  constants of occupied sites. From this fact, the temperature dependence of the quadrupole  $C_Q$  constant can inform us about the relative occupation of  $M_1$  and  $M_{1/2}$  sites. The variations of  $C_Q$  values of  $\text{LiTi}_2(\text{PO}_4)_3$  and  $\text{LiZr}_2(\text{PO}_4)_3$  are given in Figure 3a. For sake of comparison,  $C_Q$  values measured in isostructural  $\text{LiGe}_2(\text{PO}_4)_3$  and  $\text{LiHf}_2(\text{PO}_4)_3$  phases are also included. In triclinic  $\text{LiZr}_2(\text{PO}_4)_3$  and  $\text{LiHf}_2(\text{PO}_4)_3$  phases,  $C_Q$  and  $\eta$  values are more important (180 kHz, 0.6), indicating that sites occupied by Li display lower symmetry. Along the triclinic–rhombohedral transformation (displacive first-order transition), significant changes were detected in geometry and disposition of  $\text{ZrO}_6$  and  $\text{PO}_4$  polyhedra, that produced the decrease on  $C_Q$  to 120 kHz and  $\eta$  to 0. In the rhombohedral  $\text{LiTi}_2(\text{PO}_4)_3$  sample,  $C_Q$  is nearly constant ( $\sim 20$  kHz) below 250 K, but increases up to 70 kHz at 500 K, indicating that occupation of Li sites changes (second-order transition). In the rhombohedral  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series, quadrupole  $C_Q$  constants measured at room temperature increase from 40 to 120 kHz as the Zr content increases (Figure 3b). In samples with  $x > 1.5$ , quadrupole constants measured at room temperature are near those measured at 340 K in the rhombohedral  $\text{LiZr}_2(\text{PO}_4)_3$  phase.<sup>11</sup>



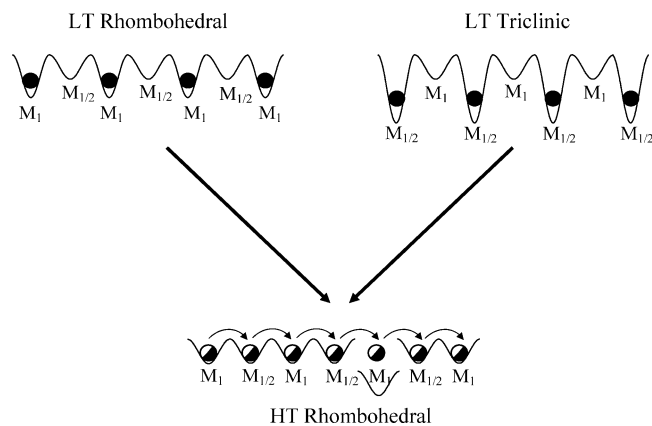
**Figure 3.** (a) Temperature dependence of quadrupole  $C_Q$  constants deduced from  $^7\text{Li}$  NMR spectra of the  $\text{LiR}_2(\text{PO}_4)_3$  series, R = Ge, Ti, Zr, and Hf. (b) Dependence of the quadrupole  $C_Q$  constant on the composition of the  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series.  $^7\text{Li}$  NMR spectra were recorded at room temperature. In the case of  $x = 2$ , the  $C_Q$  value corresponds to the sample heated at 70 °C.

To investigate factors limiting the lithium mobility, we have analyzed the geometry of triangular bottlenecks T<sub>1</sub> ( $\text{O}_2\text{O}_2\text{O}_1$ ) and T<sub>2</sub> ( $\text{O}_2\text{O}_2\text{O}_2$ ) located between M<sub>1</sub> and M<sub>2</sub> sites (see Figure 1a). In this analysis, we have determined Li–O distances necessary to pass Li ions through the windows (radius of inscribed spheres). In the triclinic  $\text{LiZr}_2(\text{PO}_4)_3$  phase, Li–O distances at T<sub>1</sub> (four sided) and T<sub>2</sub> (three sided polygons) windows are near 2.06 and 2.25 Å; however, these distances become 2.20 and 2.18 Å in the rhombohedral  $\text{LiZr}_2(\text{PO}_4)_3$  phase. In the rhombohedral  $\text{LiTi}_2(\text{PO}_4)_3$  phase, Li–O distances at T<sub>1</sub> and T<sub>2</sub> windows are near 2.05 and 1.98 Å. According to this analysis, T<sub>2</sub> windows limit Li mobility in rhombohedral  $\text{LiTi}_2(\text{PO}_4)_3$ , but T<sub>1</sub> windows limit lithium diffusion in the triclinic  $\text{LiZr}_2(\text{PO}_4)_3$  phase.

**Fast Exchange Processes.** At increasing temperatures, T<sub>1</sub> and T<sub>2</sub> windows expand favoring Li mobility in the conduction network. In this case, fast exchange processes between M<sub>1</sub> and M<sub>1/2</sub> sites should produce a signal with intermediate characteristics. According to this model, the monotonic increment of  $C_Q$  detected in  $\text{LiTi}_2(\text{PO}_4)_3$  has been interpreted by assuming that the residence time at M<sub>1/2</sub> sites (probability  $P_{1/2}$ ) increases at the expense of that at M<sub>1</sub> sites (probability  $P_1$ ).<sup>12</sup> This increment can be analyzed with the expression<sup>15,16</sup>

$$C_Q = \frac{C_Q^1 P_1 + C_Q^2 3P_{1/2}}{P_1 + 3P_{1/2}} \quad (2)$$

where,  $C_Q^1 = 15$  and  $C_Q^2 = 170$  kHz are the quadrupole



**Figure 4.** Variation of energy barriers produced during the heating of the rhombohedral and triclinic end members of the  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series.

constants and  $P_1$  and  $P_{1/2}$  are the occupation probabilities of M<sub>1</sub> and M<sub>1/2</sub> sites by lithium. The factor 3 takes into account the multiplicity of M<sub>1/2</sub> sites with respect to M<sub>1</sub> sites.

Extended Li motions are favored by creation of vacant M<sub>1</sub> sites at the intersection of conduction channels in rhombohedral phases. From the analysis of  $C_Q$  values, it was shown that creation of vacancies at M<sub>1</sub> sites is an activated process, with an  $E_a$  near 0.07 eV.<sup>18</sup> However,  $C_Q$  values measured at 450 K showed that 2/3 of M<sub>1</sub> sites are still occupied at this temperature. From this fact, the total vacancy disordering,  $P_1 = P_2 = 0.25$  ( $C_Q \approx 100$  kHz) is not attained in  $\text{LiTi}_2(\text{PO}_4)_3$ , in the temperature range 200–500 K.

In the triclinic  $\text{LiZr}_2(\text{PO}_4)_3$  phase, Li ions occupy M<sub>1/2</sub> sites, but in the rhombohedral  $\text{LiZr}_2(\text{PO}_4)_3$  phase, T<sub>1</sub> and T<sub>2</sub> windows cannot coordinate Li ions, favoring Li mobility.<sup>10,11,19</sup> At the triclinic-rhombohedral transition, the quadrupole constant  $C_Q$  decreased from 180 to 120 kHz and  $\eta$  from 0.6 to 0. In this case, the full exchange between M<sub>1</sub> and M<sub>1/2</sub> sites,  $P_1 = P_2 = 0.25$  ( $C_Q \approx 100$  kHz), reproduces reasonably well experimental results. Fast exchange processes between M<sub>1</sub> and M<sub>1/2</sub> sites, simulates also the rhombohedral  $R\bar{3}c$  symmetry ( $\eta_Q = 0$ ). This model differs from that deduced from diffraction experiments, where occupation of intermediate M<sub>1/2</sub> sites was not analyzed in the rhombohedral  $\text{LiZr}_2(\text{PO}_4)_3$  phase.<sup>20</sup>

At this point, it is interesting to analyze Li mobility in the  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series. In the rhombohedral  $\text{LiTi}_2(\text{PO}_4)_3$  end-member, Li ions occupy M<sub>1</sub> sites and activation energy for Li motion,  $E_a$ , is 0.46 eV. In the triclinic  $\text{LiZr}_2(\text{PO}_4)_3$  phase, Li ions occupy M<sub>1/2</sub> sites and activation energy  $E_a$  is 0.6 eV. Finally, occupation of M<sub>1</sub> and M<sub>1/2</sub> sites becomes similar and activation energy for Li motion decreased to 0.3 eV in the rhombohedral  $\text{LiZr}_2(\text{PO}_4)_3$  phase (see Figure 4). A similar effect can be obtained by substitution of Ti by Zr in  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series. In these samples, unit cell expansion associated with Zr incorporation favors the progressive occupation of M<sub>1/2</sub> at the expense of M<sub>1</sub> sites. Along this series, Li mobility increases and activation energy  $E_a$  decreases from 0.46 to 0.3 eV.<sup>2</sup> The stabilization of the rhombohedral phase in Zr-doped samples eliminates problems derived from stresses produced at the triclinic-rhombohedral transition and enlarges the electrochemical window (lower reducibility of Zr) of experimental devices.

## Conclusions

Li sites and lithium mobility in  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series have been analyzed with  $^7\text{Li}$  NMR spectroscopy. From the analysis of quadrupole constants of end members of the series, the

preferential occupation of  $M_1$  sites in rhombohedral and that of  $M_{1/2}$  sites in triclinic phases were deduced.

The analysis of the temperature dependence of  $C_Q$  values showed the progressive occupation of midway  $M_{1/2}$  sites at the expense of  $M_1$  sites when the temperature increases in the rhombohedral  $\text{LiTi}_2(\text{PO}_4)_3$  sample. The opposite effect was detected in triclinic  $\text{LiZr}_2(\text{PO}_4)_3$  samples, where  $M_{1/2}$  sites are preferentially occupied at low temperatures. Above the triclinic–rhombohedral transition, a full delocalization of lithium on  $M_1$  and  $M_{1/2}$  sites was detected. In the case of  $\text{LiTi}_{2-x}\text{Zr}_x(\text{PO}_4)_3$  series, a similar effect is produced when Ti is substituted by larger Zr cations. The stabilization of the rhombohedral phase in Zr-doped samples eliminates problems derived from stresses produced at the triclinic–rhombohedral transition and enlarges the electrochemical window (lower reducibility of Zr) of experimental devices.

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