# Binding between (Ethylene Oxide)<sub>13</sub>—(Propylene Oxide)<sub>30</sub>—(Ethylene Oxide)<sub>13</sub> and Sodium Decanoate. Volume, Enthalpy, and Heat Capacity Studies

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Volume, enthalpy, and heat capacity of transfer ( $\Delta Y_t$ ) of (ethylene oxide)<sub>13</sub>—(propylene oxide)<sub>30</sub>—(ethylene oxide)<sub>13</sub> (L64), at some concentrations, from water to the aqueous sodium decanoate (NaDec) solutions as functions of the surfactant concentration ( $m_S$ ) were determined at 298 K. The copolymer was studied in both the unassociated and associated forms. For a given L64 concentration ( $m_C$ ), the  $\Delta Y_t$  vs  $m_S$  profiles for the volume and the enthalpy are equal but different from that of the heat capacity because the latter contains also the relaxation terms. The experimental data were analyzed by assuming the distribution of L64 between the aqueous and the micellar phases and the shift of micellization equilibrium induced by the copolymer. A very good fit was obtained at  $m_C = 35$  mmol kg<sup>-1</sup>, which provided the L64–micelles binding constant ( $K_b$ ), the volume of transfer of L64 from water to micelles ( $\Delta V_{t,M}$ ) and the Setchenov constant. By using  $K_b$ ,  $\Delta V_{t,M}$ , and the L64-free surfactant interaction parameter (obtained from the study in the pre-micellar region),  $\Delta V_t$  as a function of  $m_S$  at lower  $m_C$  was calculated. The simulations resulted unsatisfactory since neither the shape of the  $\Delta V_t$  vs  $m_S$  trend was reproduced. Nevertheless, by adjusting  $K_b$  and  $\Delta V_{t,M}$ , the maximum in the  $\Delta V_t$  vs  $m_S$  curve was generated but the agreement with the experimental points was only qualitative. The data at  $m_C$  < 35 mmol kg<sup>-1</sup> below the cmc of NaDec were interpreted in terms of a premicellar association between n mol of NaDec and 1 mol of L64.

#### Introduction

In the last years, a growing scientific interest to the behavior of the poly(ethylene oxide)-*block*-poly(propylene oxide)-*block*-poly(ethylene oxide) copolymers (commercially available as Pluronics or Poloxamers) in solution has been addressed. The effect of the presence of polar additives, 1–7 organic compounds, 4,5,8,9 inorganic salts, 10,11 surfactants, 11–22 etc. has been analyzed. The importance of these studies is the ability to design microstructures with different functional properties useful in the applications.

A number of papers on the Pluronic-surfactant-water systems<sup>11–22</sup> has been reported but the information provided is very far to be exhaustive, as the surfactant-copolymer mechanism of interaction is quite complex. The sodium dodecyl sulfate (NaDS)/(ethylene oxide)<sub>97</sub>—(propylene oxide)<sub>69</sub>—(ethylene oxide)<sub>97</sub> (F127) system, studied by different points of view, is an example.<sup>13–16,21</sup> Earl experiments of Hecht et al.<sup>13,15,21</sup> indicated that the surfactant destroys the F127 micelles because of the surfactant-copolymer aggregation complex formation. Recent thermodynamic and structural studies<sup>14,15</sup> evidenced two specific modes of binding: (1) the interactions between monomeric F127 and NaDS micelles and (2) the interactions between NaDS and micellar F127 followed by the breakdown of the NaDS/F127 mixed micelles into smaller aggregates upon the addition of NaDS. Further detailed studies<sup>16</sup> showed that at temperatures just below the critical micellar temperature of pure F127, small amounts of NaDS cause the formation of F127 micelles that are broken-down by a further addition of NaDS. A similar mechanism of interaction was invoked for the F127/

To shed some light to the thermodynamics of the copolymersurfactant mixtures, we studied the water—sodium decanoate— L64 system as functions of both the copolymer and the surfactant concentrations at 298 K. The simultaneous determination of several thermodynamic properties can provide straightforward information on the interactions controlling these systems and, for this reason, we measured the volume, the enthalpy, and the heat capacity.

# **Experimental Section**

**Materials.** Sodium decanoate (Sigma) was recrystallized from absolute ethanol and dried in a vacuum oven at 313 K for at least 4 days. Its aqueous solutions gave pH=9. The standard partial molar volume of the surfactant, evaluated from density measurements, agrees with the value reported elsewhere.<sup>23</sup>

Sodium chloride (Aldrich, 99.999%) was dried in an oven at 573 K for 2 days. (Ethylene oxide)<sub>13</sub>—(propylene oxide)<sub>30</sub>— (ethylene oxide)<sub>13</sub> (Pluronic L64, nominal MW = 2900 g mol<sup>-1</sup>) was provided by Fluka. It was used as received because no difference in the apparent molar volumes of purified and not purified L64 in water was observed.<sup>3</sup>

All solutions were prepared by mass using degassed conductivity water and their concentrations were expressed as molalities.

tetradecyltrimethylammonium bromide system.<sup>17</sup> A different behavior<sup>18</sup> was exhibited by hexaethylene glycol mono-*n*-dodecyl ether, which forms mixed micelles with F127. This feature seems to be specific of nonionic surfactants as *N*,*N*-dimethyloctylamine-*N*-oxide forms mixed micelles with L64 and (ethylene oxide)<sub>75</sub>—(propylene oxide)<sub>30</sub>—(ethylene oxide)<sub>75</sub> (F68).<sup>19</sup>

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**Equipment.** *Density.* The solutions densities were measured at 298 K by using a vibrating tube flow densimeter (Model 03D, Sodev Inc.) sensitive to 3 ppm. The temperature was maintained constant within 0.001 K by using a closed loop temperature controller (Model CT-L, Sodev Inc.). The calibration of the densimeter was made with water ( $d = 0.997~047~\rm g~cm^{-3}$ )<sup>24</sup> and aqueous sodium chloride solutions the densities of which are reported in the literature.<sup>25</sup>

Heat Capacity Measurements. The relative differences in the heat capacities per unit volume ( $\Delta\sigma/\sigma o$ ) were determined with a Picker flow microcalorimeter (Setaram) at 298.426  $\pm$  0.001 K. Using a flow rate of about 0.01 cm³ s $^{-1}$  and a basic power of 19.7 mW, the temperature increment was approximately 0.5 K. The reproducibility of the specific heat capacity measurement is  $1\times 10^{-4}~J~K^{-1}~g^{-1}.$ 

The specific heat capacity ( $C_p$ ) of a solution of density d is related to  $\Delta\sigma/\sigma_0$  through the equation

$$C_{\rm p} = C_{\rm p,o} \{1 + \Delta \sigma / \sigma_{\rm o}\} d_{\rm o} / d \tag{1}$$

where  $C_{\rm p,o}$  and  $d_{\rm o}$  correspond to the specific heat capacity and density of pure water the values of which were taken from the literature.<sup>25</sup>

Enthalpy. Enthalpies of mixing experiments were carried out at  $298.00 \pm 0.01$  K by means of a flow LKB 2107 microcalorimeter. The injection of the solutions into the apparatus was made by means of a Gilson peristaltic pump (Minipuls 2).

The experimental enthalpy ( $\Delta H^{\rm exp}$ ) was obtained from the difference between the thermal effect due to the mixing process of the copolymer solution with the surfactant solution and that due to the dilution process of the same surfactant solution with water.

The flows of the solutions were determined by weight.

The final concentration of the surfactant  $(f_S m_S)$  and the copolymer  $(f_C m_C)$  solutions, upon the mixing process, were calculated by using the dilution factors

$$f_{\rm S} = \Phi_{\rm S} / (\Phi_{\rm S} + \Phi_{\rm C}) \tag{2}$$

$$f_{\rm C} = \Phi_{\rm C} / (\Phi_{\rm S} + \Phi_{\rm C}) \tag{3}$$

where  $\Phi_C$  and  $\Phi_S$  are the flows of water in the copolymer and the surfactant solutions, respectively.

Conductivity. The specific conductivity measurements were carried out at  $298.0 \pm 0.1$  K (digital conductimeter Analytical Control 120) to evaluate the critical micellar concentration of sodium decanoate and the degree of ionization of the micelles  $(\beta)$  in water and in the water+copolymer mixtures. The former was evaluated as the intersection point of the straight lines (in the pre- and postmicellar regions) of the plot of specific conductivity vs surfactant concentration whereas  $\beta$  is given by the ratio of the slopes of these straight lines. The calculated values are collected in Table 1.

**Apparent Molar Property Calculations.** The apparent molar volumes ( $V_{\Phi,C}$ ) and heat capacities ( $C_{\Phi,C}$ ) of L64 in the water—surfactant mixture were calculated by means of the following equations

$$V_{\Phi,C} = \frac{M}{d} - \frac{10^3 (d - d_o)}{m_C dd_o}$$
 (4)

$$C_{\Phi,C} = MC_{\rm p} + \frac{10^3 (C_{\rm p} - C_{\rm p,o})}{m_{\rm C}}$$
 (5)

TABLE 1: Critical Micellar Concentration and Degree of Ionization of Micelles for Sodium Decanoate in Water + L64 Mixtures<sup>a</sup>

$m_{\rm C}$	cmc <sub>w+L64</sub>	β	
	T = 298  K		
0	108	0.52	
5.16	96	0.71	
15.43	80	0.71	
25.54	62	0.78	
30.04	59	0.82	
34.70	56	0.77	
90.01	15	0.95	
	T = 318  K		
2.50	72	0.72	

<sup>&</sup>lt;sup>a</sup> Units:  $m_{\rm C}$  and cmc<sub>w+L64</sub>, mmol kg<sup>-1</sup>.

where  $m_{\rm C}$  and M are the molality and the molecular weight of the copolymer, d and  $C_{\rm p}$  are the densities and the specific heat capacities of the water + surfactant + copolymer ternary system, respectively, and  $d_{\rm o}$  and  $C_{\rm p,o}$  are the corresponding properties of the water + surfactant mixed solvent.

The volume and the heat capacity of transfer of L64 from water to the aqueous sodium decanoate solution ( $\Delta Y_t$ ) were calculated as difference between  $Y_{\Phi,C}$  and the apparent molar property of the copolymer in water.

The enthalpy of transfer ( $\Delta H_t$ ) was evaluated as difference between  $\Delta H^{\rm exp}$  and the enthalpy of dilution of the copolymer with water ( $-3.08 \text{ kJ mol}^{-1}$ ).<sup>19</sup>

**Thermodynamic Measurements.** The volume and the heat capacity measurements were performed by choosing L64 concentrations, which fall in the pre- ( $m_C = 15$ , 25 and 35 mmol kg<sup>-1</sup>) and postmicellar (90 mmol kg<sup>-1</sup>) regions. Remember that the cmc<sup>11</sup> of L64 in water is 65 mmol kg<sup>-1</sup> at 298 K. For each copolymer concentration, the experiments were carried out in a wide interval of the surfactant concentration.

It was not possible to perform heat capacity measurements of water + L64 mixtures at compositions larger than 90 mmol kg<sup>-1</sup> because the baseline was noised due to the solutions viscosity. The  $C_{\Phi,C}$  value in water at 90 mmol kg<sup>-1</sup> (18.4 kJ  $K^{-1}$  mol<sup>-1</sup>) is higher than that at infinite dilution (10.0 kJ  $K^{-1}$ mol<sup>-1</sup>), which is in very good agreement with the literature value.<sup>27</sup> This result is not surprising although negative heat capacity of micellization is expected. In fact, in the  $C_{\Phi,C}$  vs  $m_C$ curve the pseudo phase transition model predicts<sup>28</sup> for the relaxation term of the micellization equilibrium a hump of 72 kJ K<sup>-1</sup> mol<sup>-1</sup> at the cmc and a value of 52 kJ K<sup>-1</sup> mol<sup>-1</sup> at  $m_{\rm C}$ = 90 mmol kg<sup>-1</sup>, as calculated by using eq 18 in ref 28 and the value of 230 kJ mol<sup>-1</sup> for the enthalpy of micellization.<sup>29</sup> Therefore, the relaxation contribution is expected to be minimized at high  $m_{\rm C}$  and, consequently, the  $C_{\Phi,\rm C}$  value at 90 mmol kg<sup>-1</sup> does not correspond to the property of L64 in the micellar

Experimental difficulties did allow determining the enthalpy of transfer to 5 mmol kg<sup>-1</sup>.

The standard (infinite dilution) partial molar properties were evaluated as an intercept of the property of L64 against its concentration plot, at a given surfactant concentration. As well, heat capacity data at  $m_{\rm C}=2.5$  and 5 mmol kg<sup>-1</sup> were interpolated.

## **Results and Discussion**

Qualitative Analysis of the Properties of Transfer. (a) Unassociated L64. Figure 1 illustrates the plots of the volume of transfer ( $\Delta V_t$ ) of L64 from water to the aqueous NaDec solutions as a function of  $m_S$  at the copolymer concentrations



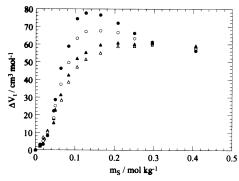


Figure 1. Volume of transfer of L64 from water to the aqueous sodium decanoate solutions as a function of the surfactant concentration: (•)  $m_{\rm C} = 0$ ; (O)  $m_{\rm C} = 15 \text{ mmol kg}^{-1}$ ; ( $\triangle$ )  $m_{\rm C} = 25 \text{ mmol kg}^{-1}$ ; ( $\Delta$ )  $m_{\rm C} =$  $35 \text{ mmol kg}^{-1}$ .

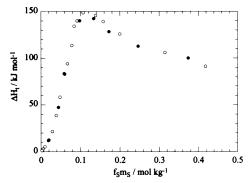


Figure 2. Enthalpy of transfer of L64 from water to the aqueous sodium decanoate solutions as a function of the surfactant concentration: (O)  $f_{\rm C}m_{\rm C} = 2.5 \text{ mmol kg}^{-1}$ ; ( $\bullet$ )  $f_{\rm C}m_{\rm C} = 5 \text{ mmol kg}^{-1}$ .

studied. The standard partial molar volume of transfer vs  $m_S$ trend is also reported, and it exhibits a sigmoid shaped curve to 0.11 mol kg<sup>-1</sup>; thereafter it decreases, tending to a constant value. A similar trend with a smoother maximum is observed at  $m_{\rm C}=15~{\rm mmol~kg^{-1}}$ . When  $m_{\rm C}$  is increased, the maximum tends to disappear and the  $\Delta V_{\rm t}$  vs  $m_{\rm S}$  curves are S-shaped in the range of  $m_S$  analyzed. Regardless of the copolymer concentration, the  $\Delta V_{\rm t}$  vs  $m_{\rm S}$  trends tend to the same value at high  $m_{\rm S}$ .

Figure 2 shows the plot of the enthalpy of transfer ( $\Delta H_t$ ) of L64 5 mmol kg<sup>-1</sup> as a function of the surfactant concentration  $(f_{\rm S}m_{\rm S})$ . The data<sup>19</sup> at 2.5 mmol kg<sup>-1</sup> are also plotted. The experimental points are independent of the copolymer concentration and define a single  $\Delta H_t$  vs  $f_S m_S$  curve showing the same shape as the volume. The region below the maximum of the  $\Delta H_{\rm t}$  vs  $f_{\rm S}m_{\rm S}$  trend at  $f_{\rm C}m_{\rm C}=2.5~{\rm mmol~kg^{-1}}$  was consistent<sup>19</sup> with the premicellar aggregation involving n mol of surfactant and 1 mol of copolymer, leading to the formation of the surfactant-copolymer aggregation complex. Contrary to classic nonionic polymers, L64 possesses hydrophilic and hydrophobic blocks, which are responsible for the copolymer micellization. Upon the NaDec addition, the PPO block as well as the surfactant chain may undergo the dehydration process and interact with each other, forming the NaDec-L64 aggregation complex, a schematic representation of which is shown in Figure 3. Such complexes are likely precursors of mixed micelles, the composition of which is expected being dependent on the copolymer concentration.

The profiles of the  $\Delta H_t$  and  $\Delta V_t$  vs surfactant concentration curves are reminiscent of those dealing with the hydrophobic solutes in the aqueous surfactant solutions, which were interpreted in terms of the shift of the micellization equilibrium induced by the solute and the distribution of the solute between

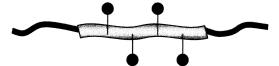


Figure 3. Schematic representation of a surfactant-copolymer aggregation complex formed by 4 surfactant molecules and 1 copolymer

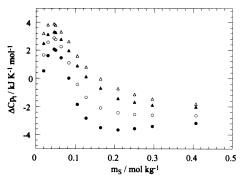


Figure 4. Heat capacity of transfer of L64 from water to the aqueous sodium decanoate solutions as a function of the surfactant concentration: (**•**)  $m_C = 0$ ; (**O**)  $m_C = 15 \text{ mmol kg}^{-1}$ ; (**A**)  $m_C = 25 \text{ mmol kg}^{-1}$ ; ( $\triangle$ )  $m_{\rm C} = 35 \text{ mmol kg}^{-1}$ .

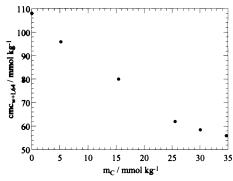
the aqueous and the micellar phases.31-34 Based on these findings, both the mass action model for the mixed micelles formation and the copolymer-surfactant aggregation complex formation could explain our results.

For a given  $m_{\rm C}$ , the heat capacity of transfer  $(\Delta C_{\rm p,t})$  as a function of  $m_S$  shows a maximum around at ca. 0.05 mol kg<sup>-1</sup>; thereafter it decreases, tending to a constant value at high  $m_S$ (Figure 4). An inflection point is displayed by the standard property around at ca. 0.2 mol kg<sup>-1</sup>. As well, the  $\Delta C_{\rm p,t}$  vs  $m_{\rm S}$ curve is shifted toward larger values upon the copolymer

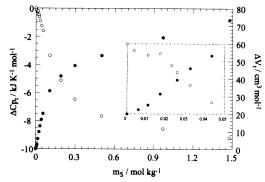
The distinctive characteristics of the heat capacity can be due to the fact that volume and enthalpy are first derivatives of Gibbs free energy whereas heat capacity is a second derivative. Consequently, the latter contains the relaxation contributions and, only when they are negligible, all the thermodynamic properties are expected to show the same features.

The L64 concentration effect is not clear. One may assume that still at high  $m_{\rm C}$  values, the adsorption of the surfactant onto the copolymer occurs or, alternatively, that L64 and NaDec form mixed micelles. The latter hypothesis is supported by the evidence of mixed micelles formation between Pluronics and surfactants. 11,18,20 To shed some light on this aspect, cmc of NaDec in the water + L64 mixtures (cmc<sub>w+L64</sub>) were determined (Table 1). When  $m_C$  is increased,  $cmc_{w+L64}$  decreases in a nonlinear manner, indicating that L64 behaves like an hydrophobic compound (Figure 5). This result apparently disagrees with the volume data: if the maximum of the property of transfer against  $m_S$  curve evidences the cmc<sub>w+L64</sub>, then it should be located at lower surfactant concentration by increasing  $m_{\rm C}$ . Indeed, because the L64 concentration smoothes the maximum and does not essentially influence the property at high  $m_S$  values, it may occur that cmcw+L64 is buried.

By combining the enthalpy of transfer at  $f_{\rm C}m_{\rm C}=2.5$  mol  $kg^{-1}$  with the corresponding heat capacity,  $\Delta H_t$  as a function of temperature was calculated. The  $\Delta H_t$  vs  $m_S$  plots (not shown) display maxima that are located at lower  $m_S$  by increasing temperature. For instance, at 318 K the maximum is present at 0.08 mol kg<sup>-1</sup>, which is close to cmc<sub>w+L64</sub> determined by conductivity (Table 1).



**Figure 5.** Dependence of the critical micellar concentration of sodium decanoate from the L64 concentration.



**Figure 6.** Volume (●) and heat capacity (○) of transfer of micellar L64 ca. 0.09 mol kg<sup>-1</sup> from water to the aqueous sodium decanoate solutions as a function of the surfactant concentration.

(b) Micellized L64. The trends of the volume and the heat capacity of transfer of L64 0.09 mol kg<sup>-1</sup> as functions of ms are illustrated in Figure 6. The aqueous L64 solution 0.09 mol kg<sup>-1</sup> exists as an equilibrium mixture of micelles with large amounts of monomers because its cmc is 0.065 mol kg<sup>-1</sup>.<sup>11</sup>  $\Delta V_t$  and  $\Delta C_{p,t}$  increase and decrease, respectively, in the whole range of  $m_S$  showing a change in the slope around at ca. 0.015 mol kg<sup>-1</sup> (see insert in Figure 6). Literature  $V_{\Phi,C}$ data at 301 K in the presence of NaDec 0.015 mol kg<sup>-1</sup> and sodium decyl sulfate (NaDeS) at several concentrations<sup>11</sup> agree with the present  $\Delta V_t$ . For a given L64 micellar solution, the shape of the  $\Delta V_t$  vs NaDeS concentration curve is monotonic. For  $0 \le m_S \le 0.015$  mol kg<sup>-1</sup>, NaDec likely solubilizes in the preexistent L64 aggregates. Because of the synergic interactions between the surfactant and L64, experienced by the decrease of the NaDec cmc with  $m_{\rm C}$ , the surfactant does aggregate at  $m_S = 0.015 \text{ mol kg}^{-1}$  (Table 1) and the NaDec-L64 mixed micelles become richer in the NaDec content with increasing  $m_{\rm S}$ .

**Surfactant**—**Copolymer Mixed Micelles Formation Model.** As stated previously, the profiles of the properties of transfer seem to be classic of systems where the hydrophobic solute distributes between the aqueous and the micellar phases.<sup>31–34</sup> The following equation, independently proposed by De Lisi et al.<sup>35</sup> and Desnoyers et al.,<sup>32,36</sup> was used to treat quantitatively the volume of transfer

$$\Delta V_{\rm t} = 2v_{\rm CS}[{\rm m}]N_{\rm f} + (1 - N_{\rm f})\Delta V_{\rm t,M} + \Delta V_{\rm m} \{[{\rm m}_{\rm o}] - [{\rm m}]\}/m_{\rm C}$$
(6)

where  $\Delta V_{\rm t,M}$  is the volume of transfer of the copolymer from water to the micellar phase. On the basis of the pseudo phase transition model for micellization and a mass action model for the solute distribution between the aqueous and the micellar phases,<sup>37</sup> the fraction of the copolymer in the aqueous phase

TABLE 2: Thermodynamic Properties for the Binding between L64 and Sodium Decanoate at 298  $K^a$ 

$m_{\rm C}$	0	2.5	5.0	15	25	35
$v_{\rm CS}$	81 ± 33					$154 \pm 16$
n	$3.1^b$ ; $3.9^c$					
$10^3 K_{\rm cpx}$	$3.6 \pm 0.4;^{b}$					
	$44 \pm 10^{c}$					
$\Delta H_{\rm cpx}$	$183 \pm 6^{b}$	$191 \pm 2$	$199 \pm 5$			
$\Delta V_{ m cpx}$	$81 \pm 3$			$95 \pm 4$	$100 \pm 5$	
$\Delta C_{ m p,cpx}$	$-20.0 \pm 0.9$	$-21.3 \pm 0.7$	$-19.7 \pm 0.9$			
$h_{\text{CS}}$	$227 \pm 36^{b}$					
$K_{\rm b}$						$43 \pm 9$
$K_{\rm S}$						$-36 \pm 13$
$\Delta V_{\rm t,M}$						$64 \pm 1$

<sup>a</sup> Units:  $m_{\rm C}$ , mmol kg<sup>-1</sup>;  $v_{\rm CS}$ , cm<sup>3</sup> kg mol<sup>-2</sup>;  $K_{\rm cpx}$ , kg<sup>n</sup> mol<sup>-n</sup>;  $\Delta H_{\rm cpx}$ , kJ mol<sup>-1</sup>;  $\Delta V_{\rm cpx}$  and  $\Delta V_{\rm t,M}$ , cm<sup>3</sup> mol<sup>-1</sup>;  $\Delta C_{\rm p,cpx}$ , kJ K<sup>-1</sup> mol<sup>-1</sup>;  $h_{\rm CS}$ , kJ kg mol<sup>-2</sup>;  $K_{\rm b}$  and  $K_{\rm S}$ , kg mol<sup>-1</sup>. <sup>b</sup> From ref 19. <sup>c</sup> From volume.

 $(N_{\rm f})$  and the shift of micellization equilibrium term, are given by  $^{35,37}$ 

$$N_{\rm f} = 1/\{1 + K_{\rm b}(m_{\rm S} - [\rm m])\} \tag{7}$$

$$\Delta V_{\rm m} \{ [\rm m_o] - [\rm m] \} / m_{\rm C} = \{ \Delta V_{\rm m} [\rm m] / 2 \} \{ 2.3 K_{\rm S} N_{\rm f} + (1 + \beta) K_{\rm b} / [1 + K_{\rm b} (m_{\rm S} - [\rm m]) + K_{\rm b} m_{\rm C}] \}$$
 (8)

where [m] and [m<sub>o</sub>] stand for the cmc in the presence and the absence of the copolymer;  $K_{\rm S}$  and  $K_{\rm b}$  represent the Setchenov constant and the copolymer—micelle binding constant, respectively, whereas  $\Delta V_{\rm m}$  is the NaDec volume of micellization (9.6 cm<sup>3</sup> mol<sup>-1</sup>).<sup>28</sup>  $v_{\rm CS}$  is the parameter for the copolymer-surfactant interaction in the aqueous phase.

Equations 6–8 fitted very well the experimental data at  $m_{\rm C}$  = 35 mmol kg<sup>-1</sup> providing  $K_{\rm b}$ ,  $\Delta V_{\rm t,M}$ , and  $K_{\rm S}$ . Also, from data in the premicellar region the  $v_{\rm CS}$  parameter was obtained. The results are collected in Table 2.

The corresponding equation for the heat capacity is available,<sup>38</sup> but the lack of the enthalpy data prevented its use at  $m_{\rm C}$  = 35 mmol kg<sup>-1</sup>.

Equation 6, combined with eqs 7 and 8, predicts a break at the cmc of a given thermodynamic property of transfer, which is mostly appropriate for surfactants having low cmc's. Therefore, eqs 7 and 8 are not valid to explain the extrema in the properties of transfer ( $\Delta Y_t$ ) in the cmc region usually exhibited by short-chain surfactants.<sup>31–34</sup> The Desnoyers et al.<sup>32,36</sup> approach, based on a mass action model for the micellization and the pseudo phase transition model for the distribution of the solute between the aqueous and the micellar phases, is able to fit the  $\Delta Y_t$  vs  $m_S$  trend, showing a maximum or a minimum in the cmc region. Such peculiarity was ascribed to the shift of micellization equilibrium induced by the solute that becomes more important by decreasing  $m_{\rm C}$ . The behavior of our volume data seem to be consistent with this effect. For this reason, we assumed the Desnoyers et al. model in using eq 6. The surfactant monomer concentration in the absence of the solute, [m<sub>o</sub>], was calculated at each ms value by using the data of the water-NaDec binary system.<sup>33</sup> For fixed  $m_S$ ,  $m_C$ , and  $K_b$  values, the surfactant monomer concentration in the presence of the solute, [m], and  $N_{\rm f}$  were evaluated by means of an iterative method.

First, the simulation was done for the system at  $m_C = 35$  mmol kg<sup>-1</sup> being known  $K_b$ ,  $\Delta V_{t,M}$ , and  $v_{CS}$  (Table 2). A very good agreement between the calculated and the experimental points was found (Figure 7). The above data were also used to simulate  $\Delta V_t$  at lower  $m_C$ , but the results were unsatisfactory. The example in Figure 7, referring to the standard volume of transfer, shows that neither the shape of the  $\Delta V_t$  vs  $m_S$  trend was reproduced. Nevertheless, by adjusting  $K_b$  and  $\Delta V_{t,M}$ , the

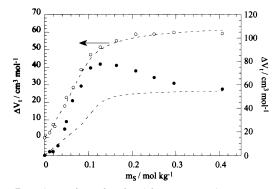


Figure 7. Volume of transfer of L64 from water to the aqueous sodium decanoate solutions as a function of the surfactant concentration: (O)  $m_{\rm C} = 35 \text{ mmol kg}^{-1}$ ; ( $\bullet$ )  $m_{\rm C} = 0$ . Lines, simulations according to eq 6 and the Desnoyers et al. model.

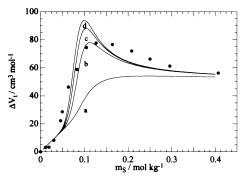


Figure 8. Standard volume of transfer of L64 from water to the aqueous sodium decanoate solutions as a function of the surfactant concentration. Lines, simulations according to eq 6 and the Desnoyers et al. model: (a)  $K_b = 50 \text{ kg mol}^{-1}$ ; (b)  $K_b = 500 \text{ kg mol}^{-1}$ ; (c)  $K_b = 500 \text{ kg mol}^{-1}$ ; 1000 kg mol<sup>-1</sup>; (d)  $K_b = 1500$  kg mol<sup>-1</sup>.

maximum in the  $\Delta V_t$  vs  $m_S$  curve was generated but the agreement with the experimental points was only qualitative. This can be seen in Figure 8, which illustrates the simulations of the standard volume of transfer at  $\Delta V_{\rm t,M} = 50 \text{ cm}^3 \text{ mol}^{-1}$ and various  $K_b$  values. It is surprising that by decreasing  $m_C$ , the  $K_{\rm b}$  value must be changed several times in magnitude to explain only qualitatively the experimental data. Desnoyers suggested that one of the assumptions in the model could not be valid, namely, the constancy of the aggregation number of the mixed micelles. In fact, it is probable that the number of sodium decanoate molecules surrounding the L64 molecule is significantly larger than in a normal micelles.

Model for the Surfactant-Copolymer Aggregation Complex Formation. Another hypothesis for the interpretation of the mixtures at  $m_{\rm C}$  < 35 mmol kg<sup>-1</sup> assumes that the large increase of the properties of transfer in the premicellar region reflects the association between a fixed number of surfactant molecules and 1 L64 molecule and, whenever the cmc is reached, mixed micellar aggregates are forming.

(i) Volume and Enthalpy. According to the one-step association model based on the formation of aggregation complexes constituted by n mol of surfactant and 1 mol of polymer, the following equation was derived for the property (first derivative of Gibbs free energy) of transfer<sup>30</sup>

$$\Delta Y_{\rm t} = \chi_{\rm cpx} \Delta Y_{\rm cpx} + 2y_{\rm CS} (m_{\rm S} - nm_{\rm cpx}) (1 - \chi_{\rm cpx}) \qquad (9)$$

Here  $\chi_{\rm cpx}$  is the fraction of the complexed polymer and  $\Delta Y_{\rm cpx}$ is the property change for the aggregation complex formation;  $m_{\rm cpx}$  is the molality of the aggregation complex, and  $y_{\rm CS}$  assumes the same meaning as above.

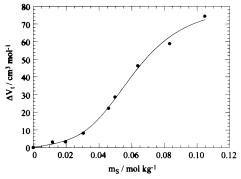


Figure 9. Best fit according to eqs 9 and 10 of the standard partial volume of transfer of L64 from water to the aqueous sodium decanoate

If the polymer is in the standard state or approaches it,  $\Delta Y_{\rm cpx}$ corresponds to the standard property and  $\chi_{cpx}$  may be written in terms of the equilibrium constant  $(K_{cpx})$  for the copolymer surfactant aggregation complex formation as

$$\chi_{\rm cpx} = K_{\rm cpx} m_{\rm S}^{\ n} / [1 + K_{\rm cpx} m_{\rm S}^{\ n}] \tag{10}$$

Equations 9 and 10 were applied to the standard volume of transfer. In the fitting procedure, the value of n was changed to minimize the standard deviation of the  $\Delta V_t$  vs  $m_S$  plot. The best fit of the experimental data is shown in Figure 9 whereas the parameters are reported in Table 2. Note that  $v_{CS}$ , within errors, is very close to that obtained from the data at  $m_C = 35$  mmol  $kg^{-1}$  although it is expected to be the same value.

The shape of the  $\Delta V_{\rm t}$  vs  $m_{\rm S}$  trend at  $m_{\rm C}=15~{\rm mmol~kg^{-1}}$  is consistent with the surfactant-copolymer aggregation complex, which is not straightforwardly evidenced at higher  $m_{\rm C}$  values. To a first approximation, we assume that the different shape of the  $\Delta V_{\rm t}$  vs  $m_{\rm S}$  curves is due to  $\chi_{\rm cpx}$ , which is expected to be dependent on  $m_{\rm C}$ . With this in mind, we calculated  $\chi_{\rm cpx}$  at some  $m_{\rm C}$  values, by using  $K_{\rm cpx}$  and n in Table 2 and solving the mass equilibrium equation by the iterative method. The profile of  $\chi_{cpx}$ vs  $m_S$  (not shown) depends on the copolymer concentration; for a fixed  $m_S$ ,  $\chi_{cpx}$  decreases with  $m_C$ . These results may explain the smoother  $\Delta V_{\rm t}$  dependence on  $m_{\rm S}$  with increasing  $m_{\rm C}$ .

The linearity predicted by eq 9 for the plot of  $\Delta V_t$ , corrected for the interaction contribution, against  $\chi_{cpx}$  was observed to ca. 0.08 mol kg<sup>-1</sup> for  $m_C = 15$  and 25 mmol kg<sup>-1</sup>, which is nearly close to the cmcw+L64 values obtained from conductivity (Table 1). The evaluated  $\Delta V_{\rm cpx}$  are collected in Table 2.

As concerns the enthalpy, the negligible effect of the copolymer concentration on the  $\Delta H_t$  values does not imply that the energetics of the copolymer-surfactant aggregation complex formation is not affected. The  $K_{\text{cpx}}$ , n, and  $\Delta H_{\text{cpx}}$  values reported elsewhere 19 were obtained by applying eqs 9 and 10 to the enthalpy data at  $f_{\rm C}m_{\rm C}=2.5~{\rm mmol~kg^{-1}}$ , and they can be assumed by referring to the standard state, as  $m_C$  does not influence  $\Delta H_t$ . For each  $m_C$  value,  $\Delta H_t$  was corrected for the second term at the right-hand side of eq 9 (calculated by using the data in Table 2) and plotted against  $\chi_{cpx}$ . The obtained  $\Delta H_{cpx}$ values are collected in Table 2.

(ii) Heat Capacity. To fit the heat capacity data, eq 9 was applied to the enthalpy and derived with respect to temperature

$$\begin{split} \Delta C_{\rm p,t} &= \chi_{\rm cpx} \Delta C_{\rm p,cpx} + 2 C_{\rm p,CS} (m_{\rm S} - n m_{\rm cpx}) (1 - \chi_{\rm cpx}) + \\ & (\delta \chi_{\rm cpx} / \delta {\rm T}) \Delta H_{\rm cpx} + 2 h_{\rm CS} (\delta \chi_{\rm cpx} / \delta {\rm T}) [n m_{\rm C} (2 X_{\rm cpx} - 1) - m_{\rm S}] \end{split} \tag{11}$$

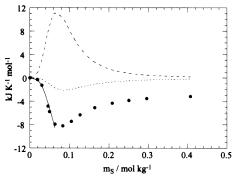


Figure 10. Standard heat capacity of transfer ( $\bullet$ ) corrected for the relaxation terms of the cooperative binding (-) and the interaction contribution ( $\cdots$ ) as a function of the surfactant concentration. Best fit (-) according to eqs 10 and 11.

The first two terms are formally equal to those in eq 9. The third and fourth terms represent the relaxation contributions of the surfactant—copolymer aggregation complex process and the interaction equilibrium, respectively. Their presence can explain the peculiar profile of  $\Delta C_{\rm p,t}$  vs  $m_{\rm S}$ . The relaxation contribution for  $0 \le m_{\rm C} \le 5$  mmol kg<sup>-1</sup> can be evaluated by using the data in Table 2. Note that in calculating the dependence of  $\chi_{\rm cpx}$  on temperature,  $\Delta H_{\rm cpx}$  was assumed to be constant.

Figure 10 illustrates the dependence on  $m_{\rm S}$  of the two relaxation terms and the standard heat capacity of transfer corrected for them. The large relaxation contribution of the equilibrium aggregation complex formation is responsible for the  $\Delta C_{\rm p,t}$  positive values and the maximum present at ca. 0.05 mol kg<sup>-1</sup> in the  $\Delta C_{\rm p,t}$  vs  $m_{\rm S}$  trend. The other contribution is relatively small. The shape of the obtained trend is equal to that observed for the enthalpy and the volume, as it is a sigmoid curve up to ca. 0.08 mol kg<sup>-1</sup>; thereafter it increases, tending to a constant value. It seems that the heat capacity with respect to other properties detects a lower cmc.

Equation 11, applied to the data in the premicellar region, provided  $\Delta C_{\rm p,cpx}$  being used the  $K_{\rm cpx}$  and n values obtained from the enthalpy. The  $C_{\rm p,CS}$  parameter resulted negligible. The best fit is shown in Figure 10. The large value of  $\Delta C_{\rm p,cpx}$  (Table 2) may question the calculated dependence of  $\chi_{\rm cpx}$  on temperature because  $\Delta H_{\rm cpx}$  was assumed to be temperature independent. Nevertheless, the uncertainties on  $\Delta H_{\rm cpx}$  and  $K_{\rm cpx}$  make reliable the calculations done. The  $\Delta C_{\rm p,cpx}$  values were also obtained at  $m_{\rm C}=2.5$  and 5 mmol kg $^{-1}$  (Table 2).

Thermodynamics of Interaction between Sodium Decanoate and L64. The parameter reflecting the unspecific interactions between the free surfactant and free L64 is positive for the enthalpy and the volume and null for the heat capacity. Also, the interaction parameter for the free energy (calculated<sup>39</sup> as  $RTK_S/4$ ) indicates that the surfactant—copolymer interactions are favorable. The L64/*N*,*N*-dimethyloctylamine *N*-oxide system displayed a similar behavior.<sup>19</sup>

The  $K_{\rm cpx}$  and n values provided by the analysis of the volume and the enthalpy data give comparable  $\chi_{\rm cpx}$  values. As well, the standard heat capacity data indirectly confirm these results. The  $\Delta V_{\rm cpx}$  and  $\Delta H_{\rm cpx}$  values are positive as the properties of L64 micellization (143.2 cm³ mol⁻¹ and 230 kJ mol⁻¹ for the volume¹¹ and the enthalpy,²9 respectively). To the best of our knowledge, no heat capacity of L64 micellization ( $\Delta C_{\rm p,m}$ ) is known. Notwithstanding, from the specific heat capacity of some Pluronics⁴0 in water one expects that  $\Delta C_{\rm p,m}$  is negative like  $\Delta C_{\rm p,cpx}$ .

As concerns the copolymer concentration effect,  $\Delta V_{\rm cpx}$  increases with  $m_{\rm C}$  (Table 2) tending to the L64  $\Delta V_{\rm m}$  value. The

 $\Delta C_{\rm p,cpx}$  and  $\Delta H_{\rm cpx}$  values, within the errors, are independent of  $m_{\rm C}$  in the range 0–5 mmol kg<sup>-1</sup>. Dai and Tam<sup>12</sup> showed that for the NaDS/(propylene oxide)<sub>19</sub>—(ethylene oxide)<sub>33</sub>—(propylene oxide)<sub>19</sub> system, the enthalpy for the polymer—surfactant aggregation complex formation at the critical aggregation concentration increases with the copolymer concentration in the interval 0.15–1.3 mmol kg<sup>-1</sup>.

By increasing  $m_{\rm C}$ , larger proportions of L64 segments may dehydrate and interact with NaDec clusters bound to the polymer. Consequently, the L64–NaDec aggregation complex likely tends to assume a character more and more similar to the L64 aggregates.

The solubilization of L64 35 mmol kg<sup>-1</sup> in the NaDec micelles involves a change in the volume comparable to the  $\Delta V_{\rm t}$  value (ca. 70 cm<sup>3</sup> mol<sup>-1</sup>) at  $m_{\rm C} = 90$  mmol kg<sup>-1</sup>, taken at very high  $m_{\rm S}$ , which may be a measure of the volume of transfer of micellar L64 from water to the NaDeS micellar phase. These volume variations together with the degree of ionization of micelles ( $\beta$ ) are consistent with highly charged NaDec–L64 mixed aggregates, due to the screening of the copolymer segments. The L64–NaDeS mixed micelles<sup>11</sup> at 301 K behave similarly although  $\beta$  is more strongly affected.

#### **Conclusions**

The present study is a part of a project aimed to characterize the water-surfactant-copolymer ternary systems through thermodynamic experiments and modelization of the data. To this purpose, volume, enthalpy, and heat capacity of transfer of L64, at some concentrations, from water to the aqueous sodium decanoate solutions as functions of the surfactant concentration were determined. The mechanism of interaction is not easily understandable as the models used to quantitatively treat the experimental results do not straightforwardly define all the systems under study. Nevertheless, the information drawn is an important basis for the improvement of the models. On the other hand, as far as we know, no quantitative approaches to the thermodynamics of interaction between surfactants and copolymers are known. For instance, Li et al. 14 reported only a quite detailed qualitative description of the interactions in the NaDS-F127-water mixture, which is one of the most investigated systems.

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**Supporting Information Available:** Table of the experimental enthalpies of transfer of L64 from water to the aqueous sodium decanoate solution. Tables of the apparent molar volume and heat capacity for L64 in the aqueous surfactant solutions. Table of specific conductivity of sodium decanoate in water + L64 mixtures. This material is available free of charge via the Internet at http://pubs.acs.org.

## **References and Notes**

- (1) Yang, L.; Alexandridis, P. Macromolecules 2000, 33, 5587.
- (2) Cheng, Y.; Jolicoeur, C. Macromolecules 1995, 28, 2665.
- (3) De Lisi, R.; Milioto, S. Langmuir 1999, 15, 6277.
- (4) Ivanova, R.; Lindman, B.; Alexandridis, P. Langmuir 2000, 16, 3660.
- (5) Alexandridis, P.; Ivanova, R.; Lindman, B. Langmuir 2000, 16, 3676.

- (6) Holmqvist, P.; Alexandridis, P.; Lindman, B. *J. Phys. Chem. B* **1998**, *102*, 1149.
- (7) Ivanova, R.; Lindman, B.; Alexandridis, P. *Langmuir* 2000, 16, 9058.
- (8) Gadelle, F.; Koros, W. J.; Schechter, R. S. *Macromolecules* **1995**, 28, 4883.
- (9) Hurter, P. N.; Alexandridis, P.; Hatton, T. A. In *Solubilization in Surfactant Aggregates*; Christian, S. D., Scamehorn, J. F., Eds.; M. Dekker: New York, 1995.
- (10) Guomin, M.; Sukuraman, S.; Beaucage, G.; Saboungi, M. L.; Thiyagarajan, P. *Macromolecules* **2001**, *34*, 552 and references therein.
  - (11) De Lisi, R.; Milioto, S. Langmuir 2000, 16, 5579.
  - (12) Dai, S.; Tam, K. C.; Li, L. Macromolecules 2001, 34, 7049.
  - (13) Hecht, E.; Hoffmann, H. Langmuir 1994, 10, 86.
- (14) Li, Y.; Xu, R.; Bloor, D. M.; Holzwarth, J. F.; Wyn-Jones, E. Langmuir 2000, 16, 10515.
  - (15) Hecht, E.; Hoffmann, H. Colloids Surf. A 1995, 96, 181.
- (16) Li, Y.; Xu, R.; Courdec, S.; Bloor, D. M.; Wyn-Jones, E.; Holzwarth, J. F. *Langmuir* **2001**, *17*, 183.
- (17) Li, Y.; Xu, R.; Courdec, S.; Bloor, D. M.; Holzwarth, J. F.; Wyn-Jones, E. *Langmuir* **2001**, *17*, 5742.
- (18) Courdec, S.; Li, Y.; Bloor, D. M.; Holzwarth, J. F.; Wyn-Jones, E. *Langmuir* **2001**, *17*, 4818.
- (19) De Lisi, R.; Milioto, S.; Muratore, N. *Macromolecules* **2002**, *35*, 6075.
- (20) Almgren, M.; van Stam, J.; Li, P.; Stilbs, P.; Bahadur, P. J. Phys. Chem. 1991, 95, 5677.
- (21) Hecht, E.; Mortensen, K.; Gradzielski, M.; Hoffmann, H. *J. Phys. Chem.* **1995**, *99*, 4866.
  - (22) Zhang, K.; Lindman, B.; Coppola, L. Langmuir 1995, 11, 538.
- (23) De Lisi, R.; Milioto, S.; Pellerito, A.; Inglese, A. Langmuir 1998, 14, 6045.

- (24) Kell, G. S. J. Chem. Eng. Data 1967, 12, 66.
- (25) Hill, P. G.; MacMillan, R. D. C.; Lee, V. J. Phys. Chem. Ref. Data 1982, 11, 1.
  - (26) Zana, R. J. Colloid Interface Sci. 1980, 78, 330.
- (27) Senkow, S.; Mehta, S. K.; Douhéret, G.; Roux, A. H.; Roux-Desgranges, G. Phys. Chem. Chem. Phys. 2002, 4, 4472.
- (28) De Lisi, R.; Perron, G.; Desnoyers, J. E. Can. J. Chem. 1980, 58, 959.
- (29) Alexandridis, P.; Holzwarth, J. F.; Hatton, T. A. Macromolecules 1994, 27, 2414.
- (30) De Lisi, R.; De Simone, D.; Milioto, S. J. Phys. Chem. B 2000, 104, 12130.
- (31) Yamashita, F.; Perron, G.; Desnoyers, J. E.; Kwak, J. C. T. In *Phenomena in Mixed Surfactant Systems*; Scamehorn, J. F., Ed.; ACS Symposium Series; American Chemical Society: Washington, DC, 1986.
- (32) Hètu, D.; Roux, A. H.; Desnoyers, J. E. J. Solution Chem. 1987, 16, 529.
- (33) Hètu, D.; Camiré, C.; Perron, G.; Desnoyers, J. E. *Langmuir* **1994**, *10*, 4039.
- (34) Milioto, S.; Romancino, D.; De Lisi, R. J. Solution Chem. 1987, 16, 943.
- (35) De Lisi, R.; Milioto, S.; Castagnolo, M.; Inglese, A. J. Solution Chem. 1987, 16, 373.
- (36) Roux, A. H.; Hètu, D.; Perron, G.; Desnoyers, J. E. J. Solution Chem. **1984**, *13*, 1.
  - (37) De Lisi, R.; Turco Liveri, V. Gazz. Chim. Ital. 1983, 113, 371.
- (38) De Lisi, R.; Milioto, S. In *Solubilization in Surfactant Aggregates*; Christian, S. D., Scamehorn, J. F., Eds.; M. Dekker: New York, 1995.
- (39) Desnoyers, J. E.; Billon, M.; Leger, S.; Perron, G.; Morel, J. P. J. Solution Chem. 1976, 5, 681.
  - (40) Meilleur, L.; Hardy, A.; Quirion, F. Langmuir 1996, 12, 4697.