# Characterizing the Conformational Ensemble of Monomeric Polyglutamine

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**ABSTRACT** Studies of synthetic polyglutamine peptides in vitro have established that polyglutamine peptides aggregate via a classic nucleation and growth mechanism. Chen and colleagues [Proc Natl Acad Sci U S A 2002;99:11884-11889] have found that monomeric polyglutamine, which is a disordered statistical coil in solution, is the critical nucleus for aggregation. Therefore, nucleation of β-sheet-rich aggregates requires an initial disorder to order transition, which is a highly unfavorable thermodynamic reaction. The questions of interest to us are as follows: What are the statistical fluctuations that drive β-sheet formation in monomeric polyglutamine? How do these fluctuations vary with chain length? And why is this process thermodynamically unfavorable, that is, why is monomeric polyglutamine disordered? To answer these questions we use multiple molecular dynamics simulations to provide quantitative characterization of conformational ensembles for two short polyglutamine peptides. We find that the ensemble for polyglutamine is indeed disordered. However, the disorder is inherently different from that of denatured proteins and the average compactness and magnitude of conformational fluctuations increase with chain length. Most importantly, the effective concentration of sidechain primary amides around backbone units is inherently high and peptide units are solvated either by hydrogen bonds to sidechains or surrounding water molecules. Due to the multiplicity of backbone solvation modes the probability associated with any specific backbone conformation is small, resulting in a conformational entropy bottleneck which makes  $\beta$ -sheet formation in monomeric polyglutamine thermodynamically unfavorable. Proteins 2006;63:297-311. © 2005 Wiley-Liss, Inc.

Key words: polyglutamine; disorder; nucleation; aggregation; β-sheet; order parameter

#### INTRODUCTION

Huntington's disease is a genetic disorder that is linked to mutations that lead to polyglutamine expansions in the N-terminal region of the protein huntingtin.<sup>2</sup> There is a strong correlation between the age of onset in Huntington's disease and the length of polyglutamine expansions coded for by exon 1 of huntingtin.<sup>3,4</sup> Disease penetrance is especially aggressive when the number of consecutive

glutamine residues crosses the 35- to 40-residue threshold.<sup>2</sup> Polyglutamine expansions in proteins other than huntingtin are associated with eight other disorders including spinal and bulbar muscular atrophy, dentatorubral–pallidoluysian atrophy, and six spinocerebellar ataxias. <sup>5,6</sup>

Neuropathology studies have shown that expanded polyglutamine tracts self-associate to form ordered protein aggregates. Paggregates appear to be rich in  $\beta$ -sheets and low-resolution structural studies indicate the cross- $\beta$  architecture that is associated with amyloid superstructures. Postmortem examinations of Huntington's disease patients show that aggregates are deposited as intranuclear inclusions within neurons. Puptake of polyglutamine aggregates into the nucleus has been linked to cell death in cell culture studies.

Why are expanded polyglutamine tracts prone to aggregation? The biophysical principles that underlie protein aggregation have been the subject of intense studies over the past 5 years. <sup>14–26</sup> Dobson and coworkers have shown that the propensity to aggregate is a generic attribute of polypeptide chains, especially of main-chain atoms that are common to all protein sequences. <sup>21,23</sup> It is reasonable to assume that the strong tendency of polyglutamine tracts to aggregate may be attributed to the duplication of backbone-like polar moities in the sidechains. <sup>2,10,41</sup>

Dobson and coworkers have also shown that aggregation propensities of polypeptides can be closely related to the hydrophobicity of amino acid sequences. <sup>27,28</sup> The more hydrophobic a sequence, the more readily it aggregates. Polyglutamine is a polar molecule and its propensity to aggregate is an interesting outlier in that it does not appear to come under the purview of recent predictive models. <sup>27,28</sup>

The process of aggregation has also been the subject of considerably scrutiny. There is growing evidence that intermediates accessible along pathways to amyloid are just as toxic — if not more toxic — than amyloids.  $^{29-34}$  In

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most systems, amyloid formation appears to be a consequence of the self-association of either denatured proteins or natively unfolded polypeptides. Every Ev

In vitro studies of recombinant proteins<sup>37–40</sup> with polyglutamine expansions and synthetic polyglutamine peptides<sup>1,26,41–44</sup> of varying lengths recapitulate many of the aggregation related phenotypes associated with proteins linked to disease. These include the sharp length-dependent propensity to form aggregates,<sup>1,26,37,38,43</sup> the ability to recruit short polyglutamine peptides into growing aggregates,<sup>43</sup> the formation of aggregates with amyloid-like superstructure,<sup>12</sup> and the formation of spherical and annular oligomers.<sup>40</sup>

Wetzel and coworkers have studied length-dependent aggregation of synthetic polyglutamine peptides.  $^{26}$  Aggregation requires high peptide concentrations (ca. 10  $\mu M$ ) and kinetic data are consistent with classic nucleation-growth behavior.  $^{1,12,26,43,44}$  Lag times and critical concentrations decrease with increasing chain length.  $^{1,12,43}$  Analysis of kinetic data for aggregation of peptides of different lengths leads to the conclusion that the monomer — a single polyglutamine chain — is the critical nucleus for aggregation.  $^{1,26}$  Following upon this observation, Wetzel and coworkers proposed a model where the nucleus is assumed to be in a rapid pre-equilibrium with the bulk phase monomer.  $^{1}$ 

Irrespective of peptide length, monomeric polyglutamine is unfolded in aqueous buffers. This fact is established by data from CD spectroscopy. 1,12,39,41,42,45 Therefore, nucleation which is a disorder to order transition is akin to highly unfavorable folding (thermodynamic) reaction. The proposed pre-equilibrium between bulk phase monomer and the nucleus for aggregation is written as:

 $\mathbf{M}_b \overset{\mathbf{k}_1}{\hookrightarrow} \mathbf{M}_N^*$ , where  $\mathbf{M}_b$  denotes bulk phase monomer,  $\mathbf{M}_N^{k_1}$  denotes the nucleus, and the pre-equilibrium constant  $K_{N^*} = \frac{k_1}{k_{-1}}$  is defined as the ratio of the rates for the forward and reverse reactions,  $k_1$  and  $k_{-1}$ , respectively. By definition the nucleus is populated with very low probability and  $K_{N^*}$  is expected to be very small for short and long chains. The length-dependent increase in aggregation is associated with a length-dependent increase in  $K_{N^*}$ , although this parameter will overwhelmingly favor the bulk phase monomer.  $^1$ 

Why is  $K_{N^*}$  small? In other words, why does polyglutamine prefer to be disordered in solution? And what is the mechanism by which polyglutamine peptides transiently populate intramolecular  $\beta$ -sheets that can elongate to form amyloid fibers? To answer these questions, we have

begun a series of studies to characterize the conformational ensembles of polyglutamine peptides of different chain lengths.

Aggregation in vitro requires concentrations in the

micromolar range. Why then is it important to study the ensemble of monomeric polyglutamine? The monomeric ensemble contributes to nucleation of aggregation in three ways: (1) through the stability of the nucleus quantified by  $K_{N^*}$ ; (2) through the thermodynamic driving force<sup>47</sup> for aggregation  $\Delta\mu$  which is written as  $\Delta\mu = \frac{G_A - G_m}{n}$ , where  $G_A$  and  $G_M$  are free energies for the aggregate and monomer and n is the number of polyglutamine molecules; and (3) through the work for nucleating a cluster<sup>47</sup> written as  $W = -\Delta\mu + G_{\rm ex}$ . Here,  $G_{\rm ex}$  is the so-called cluster excess free energy and corresponds to the free energy penalty associated with creating a phase boundary.

Molecular simulations provide detailed atomistic information regarding conformational ensembles. Such information is inaccessible to conventional spectroscopic probes, which are used to probe disordered ensembles. Decreasing CPU costs combined with major improvements in sampling algorithms <sup>48–52</sup> have spurred the use of molecular simulations for a range of mechanistic studies of protein folding <sup>51–56</sup> and aggregation phenomena. <sup>57–61</sup> Especially important are insights drawn from simulations regarding the unfolded states of proteins and peptides. <sup>62–68</sup>

Here, we use multiple molecular dynamics simulations to provide quantitative characterization of the conformational ensembles for two polyglutamine peptides with 5 and 15 residues, respectively. Our data provide a plausible explanation for the source of disorder in monomeric polyglutamine. This in turn leads to a reasonable hypothesis for why  $\beta$ -sheet formation is unfavorable for polyglutamine. We first discuss the methodology used in our calculations. This is followed by a presentation of the results and a discussion of implications for the questions of interest.

#### **METHODS**

We report results from our analysis of multiple molecular dynamics simulations for two polyglutamine peptides. The peptides studied are: N-acetyl- $(Gln)_5$ -N'-methylamide and N-acetyl- $(Gln)_{15}$ -N'-methylamide. The N- and C-termini in both peptides are capped with blocking groups to avoid complications due to charged termini. To be concise we refer to the peptide with 5 glutamine residues as Q5 and the peptide with 15 glutamine residues as Q15.

#### **Force Field**

Parameters from the all atom OPLS-AA force field<sup>69,70</sup> were used for the peptides. The four-site TIP4P model<sup>71</sup> was used to model water molecules. The TIP4P model is one of several water models in the TIPxP series.<sup>71</sup> It is an improvement over the popular three-site TIP3P model, especially in its ability to reproduce structural and thermodynamic properties of bulk water. One advantage of using the OPLS-AA force field is that it allows flexibility in the choice of water models. This option is unavailable in simulations with other nonpolarizable force fields.

#### The Simulation Engine

All molecular dynamics simulations were performed using the GROMACS package. The isothermalisobaric (NPT) ensemble was used in all equilibration and production runs. The equilibrium temperature and pressure for all molecular dynamics simulations was  $T=298~\mathrm{K}$  and  $P=1~\mathrm{bar}$ , respectively. Temperature and pressure were controlled using the weak-coupling algorithms of Berendsen and coworkers. The control parameters are  $\tau=0.2~\mathrm{ps}$  for the thermostat and  $\kappa=4.5~\mathrm{\times}10^{-5}\mathrm{bar}^{-1}$  for the compressibility. A 2.0 fs time step was used in all of our simulations. All bond lengths were constrained using the LINCS algorithm. Seighbor lists for nonbonded interactions were updated every 10 time steps.

In each of the molecular dynamics simulations, a starting conformation (see below) for the peptide of interest (Q5 or Q15) was chosen with the peptide placed at the center of a dodecahedral box of pre-equilibrated water molecules. Dimensions of the central box are different for the two peptides. For Q5 and Q15, the central simulation box is such that the shortest distance between opposing faces of the polyhedron are 40 Å and 45 Å with 1400 and 1900 water molecules, respectively. The box sizes are chosen to ensure that when peptides adopt realistic extended conformations — as determined by the distribution of conformations generated in the excluded volume limit (see below) — at least eight layers of water molecules separate the molecules in the central cell from their images.

Periodic boundary conditions with the minimum image convention were applied to ensure the absence of macroscopic interfaces. At the beginning of each simulation, a short 0.4 ps simulation of the peptide + water system in the NVT (isothermal–isochoric) ensemble was used to relieve any steric overlaps between peptide atoms and between the peptide and surrounding water molecules. Additional 50 ps (for Q5) and 100 ps simulations (for Q15) in the NPT ensemble were used as initial equilibration runs. The end points of these simulations were the starting points for 15 ns production runs.

Conformational ensembles were constructed by analyzing 60 independent 15 ns simulations for the Q5 peptide and 90 independent 15 ns simulations for the Q15 peptide. The cumulative simulation times are 0.9  $\mu$ s and 1.35  $\mu$ s for Q5 and Q15, respectively. In each simulation, snapshots of peptide conformations are written out in 0.8 ps intervals for Q5 and 2 ps intervals for Q15.

#### **Long-Range Interactions**

A 10 Å spherical cutoff with truncation was used for the van der Waals and Coulomb interactions. The choice of spherical cutoffs requires some justification because it is well known that long-range interactions have a significant influence on simulation results. <sup>76,77</sup> We have previously quantified the effects of long-range interactions in molecular dynamics simulations using two different methods for evaluating Coulomb interactions — spherical cutoffs and Ewald sums. <sup>78</sup> Free energy surfaces for peptides that are net electro-neutral are not sensitive to the algorithm used

to handle long-range electrostatics so long as the cutoff distance is not too short (Pappu, unpublished data). In simulations of peptides that do not have a net charge, the solute can be viewed as a concatenation of electro-neutral groups. Similarly, water molecules are also electroneutral. Over large separations electrostatic interactions reduce to dipole—dipole interactions which are convergent and decay more rapidly than charge—charge interactions. The main conclusion is as follows: For the particular problem of capped polyglutamine peptides in water, spherical cutoffs can be used instead of Ewald sums without introducing significant errors. Similar conclusions have been reported in the literature for other electro-neutral peptides and polymers in water and aqueous mixtures.<sup>79</sup>

## Quantifying Conformational Ensembles Using Probability Distribution Functions

Our goal is to quantify the equilibrium ensemble for monomeric polyglutamine as a function of chain length. This is accomplished by constructing probability distribution functions (PDFs), one each for Q5 and Q15. We denote a PDF as  $\rho(a,b)$ ,  $0 \le \rho \le 1$ ,where a and b are two conformation-specific, preferably independent, order parameters.

The choice of order parameters is not trivial and this topic has received considerable attention in formulations of molecular simulations  $^{51,80-82}$  and energy landscape theories.  $^{83}$  The first order parameter is invariably the radius of gyration  $(R_{\rm g})$  which quantifies the size of a polypeptide. The second parameter helps quantify the shape, conformation, or topology of the molecule. When the native conformation is known, several options exist for the second order parameter which quantifies overall shape or conformation.  $^{82,83}$  The choice is governed by whether one is interested in extracting information regarding transition states (kinetics) or conformational equilibria (thermodynamics).

For polyglutamine in water, we have no a priori knowledge of the preferred shape or conformation. Therefore, we adapt ideas from polymer physics to select two order parameters. We use  $R_{\rm g}$  to quantify the sizes of peptides and asphericity  $(\delta)^{84}$  to quantify overall shape. Both  $R_{\rm g}$  and  $\delta$  are measurable using scattering experiments.  $^{84,86}$  If the value of  $R_{\rm g}$  is small, the conformation is compact and if  $R_{\rm g}$  is large the conformation is swollen or expanded.

Asphericity is a dimensionless quantity and for a given conformation it is defined as:  $\delta=1-3$   $L_1^2L_2^2+L_2^2L_3^2+L_3^2L_1^2$  and  $0\leq\delta\leq 1.$  Li=1,2,3) are the eigenvalues of the radius of gyration tensor.  $^{85}$   $\delta\approx 1$  for a rodlike polymer and  $\delta\approx 0$  for a perfect sphere. Oblate spheroids, prolate spheroids, and ellipsoids have asphericity values that are greater than 0.2 and less than 0.7.  $^{84}$  If  $\delta$  is small, the chain assumes a roughly spherical shape and is globular. For intermediate values,  $0.3\leq\delta\leq0.5$ , the chain is a loosely packed globule.  $^{84}$ 

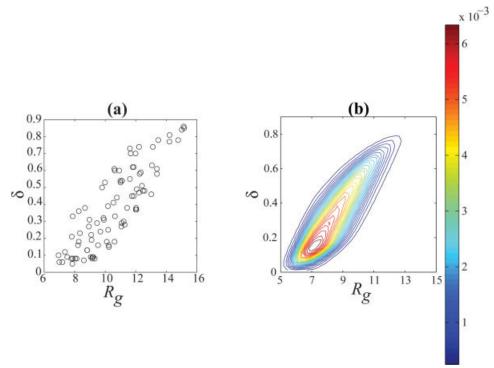


Figure 1.

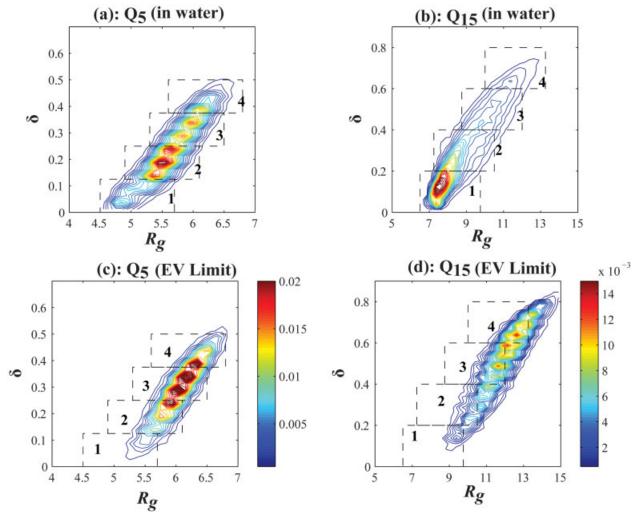


Figure 3.

#### Algorithm to Construct the PDF $\rho(\delta, R_g)$

We use a bootstrapping method<sup>91</sup> to stitch together information from multiple, unbiased trajectories in order to construct an estimate for  $\rho(\delta, R_{\wp})$ .

1. Setting up initial conformations: We used a Metropolis Monte Carlo (MMC) algorithm<sup>87</sup> to sample conformational space for each peptide. Details regarding the MMC simulations are described elsewhere.<sup>68</sup> The potential functions we use are such that conformations in the ensemble generated using the MMC simulations are self-avoiding and uniformly adopt all realizable values in  $(\delta, R_{\rm g})$  space. Representative conformations corresponding to different values of  $\delta$  and  $R_{\rm g}$  are randomly drawn from the initial ensemble. These conformations represent the starting geometries for independent molecular dynamics simulations. Figure 1(a) shows the order parameters of the initial conformations for the 90 molecular dynamics simulations of Q15.

To emphasize that these initial  $(\delta,R_g)$  values span all of conceivable space, Figure 1(b) shows the PDF  $\rho_{\rm id}(\delta,R_g)$  for an ideal Q15 peptide. <sup>88</sup> To generate  $\rho_{\rm id}(\delta,R_g)$ , we freeze all bond lengths and bond angles at equilibrium values <sup>89</sup> and constrain the peptide units to be planar and trans. We then turn off all other interatomic interactions and generate an ensemble of conformations via a Monte Carlo procedure that randomly varies the backbone  $(\phi,\psi)$  and sidechain  $\chi$ -angles. Figure 1(b) illustrates that constraints of chain connectivity naturally give rise to an oblong shape for the two-dimensional PDFs. Comparison of Figures 1(a,b) establishes that  $(\delta,R_g)$  values of initial conformations for the different dynamics simulations uniformly cover the realizable order parameter space.

- 2. Collecting data for construction of  $\rho(\delta, R_{\rm g})$ : In each of the 60 simulations for Q5 and 90 simulations for Q15 we discard the first 3 ns of data. This was based on the observation that in a typical molecular dynamics simulation, for both Q5 and Q15, the characteristic decay time for the autocorrelation function  $^{90}$  of  $R_{\rm g}$  was approximately 3 ns. Pruned data were used in subsequent analysis.
- 3. Bootstrap procedure for constructing  $\rho(\delta, R_g)$ :

Fig. 1. (a):  $(\delta,R_{\rm g})$  values of initial conformations for the 90 molecular dynamics simulations of Q15. (b): Illustration of calculated  $\rho_{\rm id}(\delta,R_{\rm g})$  for an ideal 15-mer of polyglutamine. This illustrates the generality of the oblong shape of the two-dimensional PDFs for polypeptide chains.

Fig. 3. **(a)**:  $\rho(\delta,R_g)$  from the bootstrap analysis of molecular dynamics simulations for Q5. Ad hoc rectangular envelopes are superimposed on the PDF to compute cumulative statistics. Numerical labels, 1 to 4, are assigned to each region. **(b)**:  $\rho(\delta,R_g)$  from the bootstrap analysis of molecular dynamics simulations for Q15. Numerical labels, 1 to 4, are assigned to each region superimposed on the PDF. **(c)**: Contour maps of  $\rho_{\rm EV}(\delta,R_g)$  for Q5. The boxes superposed on this PDF are identical to the ones used in Figure 3(a). **(d)**: Contour maps of  $\rho_{\rm EV}(\delta,R_g)$  for Q15. The boxes superposed on this PDF are identical to the ones used in Figure 3(b). Dimensions of ad hoc boxes and cumulative statistics for all four PDFs are shown in Table I. Figures 3(a,c) share the same color bar. This is located adjacent to Figure 3(c). The color bar for the Q15 PDFs is located to the right of Figure 3(d).

- (a) To analyze the last 12 ns of each molecular dynamics trajectory a sampling frequency  $\tau_{\rm s}$  is chosen at random from the interval 4 ps  $\leq \tau_{\rm s} \leq 40$  ps.  $N_{\rm s}$  distinct snapshots are selected from the trajectory in intervals of  $\tau_{\rm s}$  ps such that  $N_{\rm s}\tau_{\rm s}=12$  ns.
- (b) Step (a) is repeated for each independent trajectory of the peptide of interest and the data are pooled.
- (c) The pooled data are used to construct a two-dimensional histogram in the two-dimensional order parameter space. The number of points  $(N_{\rm s})$  sampled from each trajectory and the total numbers of trajectories are used to normalize the histogram.
- (d) Steps (a)–(c) are repeated 50 times. This is analogous to the technique of bootstrapping with replacement. The different normalized histograms are averaged to construct the desired PDF,  $\rho(\delta, R_{\rm g})$ . The standard deviation is an estimate of the error in our construction of  $\rho(\delta, R_{\rm g})$ .

Our strategy is similar to the ensemble dynamics methodology of Pande and coworkers. The only difference is in the use of different starting conformations for each simulation. The bootstrapping procedure for constructing  $\rho(\delta,R_{\rm g})$  is valid only if each trajectory is not confined to a small region around its starting point in  $(\delta,R_{\rm g})$ -space. The general validity of our procedure is established in Figure 2. Here, we show the typical span in order parameter space for representative 15 ns trajectories of the Q5 and Q15 peptides, respectively. It is clear that the trajectories are not confined to a specific region and that the full range of realizable space can be sampled.

#### RESULTS

#### $\rho(\delta, R_{\rm g})$ for Q5 and Q15

PDFs for the Q5 and Q15 peptides in water are shown in Figures 3(a,b). We tabulate cumulative statistics for different regions of the order parameter space by superposing ad hoc rectangular boxes on the contours shown in Figures 3(a,b). The box sizes are chosen to maximize overlap across the oblong contour map and cover a range of  $\delta$  and  $R_{\rm g}$  values within each box. Dimensions for the ad hoc boxes are different for Q5 and Q15. Table I also shows cumulative statistics for each of the four regions identified for Q5 and Q15. Cumulative statistics for a given box are computed by integration over  $\rho$  in that box.

The statistics shown in Table I lead to the following observations: If the peptides were structured one would expect the cumulative statistics for at least one of the ad hoc boxes to be dominant. We make this assertion based on the range of  $\delta$  and  $R_{\rm g}$  values for each ad hoc box. Figures 3(a,b), as well as data in Table I, emphasize that this is not the case. The ensembles of Q5 and Q15 are clearly disordered in that the peptides do not have an overwhelming preference for specific regions of the order parameter space. There is a length dependence to this disorder in that there is a marked preference for compact, globular conformations in the Q15 ensemble. The Q5 peptide is too short to realize such preferences.

Our conclusion that polyglutamine ensemble is disordered is consistent with the findings of Chen and col-

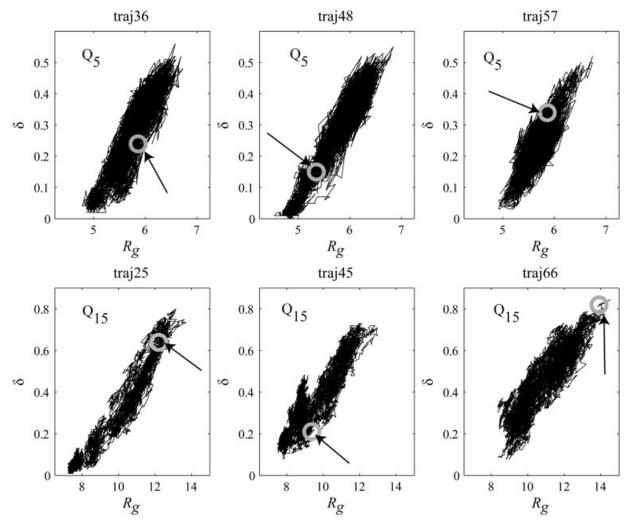


Fig. 2. Span of sample trajectories. Top row shows a mapping of  $(\delta, R_g)$  from three sample molecular dynamics trajectories for Q5. Bottom row shows similar information for Q15. Arrows point to  $(\delta, R_g)$  values of initial conformations for each trajectory. These are also marked by gray open circles.

leagues<sup>43</sup> who used UV-CD spectroscopy to characterize the ensemble for monomeric polyglutamine. Chen and colleagues found that the CD spectra for Q5, Q15, Q28, and Q40 are roughly equivalent to each other. It is also true that that the CD spectra of Chen and colleagues bear close resemblance to CD spectra for chemically denatured proteins.<sup>93</sup> The insensitivity of CD data to changes in chain length and the similarity in CD profiles to those seen for denatured proteins (especially in terms of the negative molar ellipticities in the 200 nm range) raises an interesting question.

#### Comparing Different Flavors of Disorder

Is the disorder seen in our simulations for polyglutamine in water akin to the disorder seen for denatured proteins? In other words, is a PDF in water similar to a PDF in denaturant and is there essentially only one type of statistical-coil state? To answer this question it would be useful to predict the PDF for polyglutamine in a denaturing environment and compare it to the PDFs shown in

Figures 3(a,b). We can do this using a recently developed model<sup>68</sup> that provides an accurate facsimile of the ensemble of conformations accessible to polypeptides in harshly denaturing environments such as 8M urea.<sup>94</sup> Such ensembles can be mimicked by simulating conformational ensembles in the excluded volume (EV) limit.<sup>68,86</sup> This is because denatured polypeptides behave like polymers in a so-called good solvent and the EV limit provides an ideal mimic of good solvent conditions.

We generated conformational ensembles for Q5 and Q15 in the EV limit and used these ensembles to compute  $\rho_{\rm EV}(\delta,\,R_{\rm g}).$  The results are shown in Figures 3(c,d). Additionally, in Figure 4 we plot the probability distributions  $p\bigg(\frac{R_g}{\sqrt{N}}\bigg)$  for both Q5 and Q15 versus  $\frac{R_g}{\sqrt{N}}$  because the variation of  $R_g$  with chain length N obeys well-defined scaling laws. Data are shown for the peptides in water and in the EV limit.

The conformational ensemble in water, although disordered, is inherently different from the disorder one would

TABLE I. Cumulative Statistics (%) for Each of the Four Regions Identified for Q5 and Q15\*

	Box 1 (%)	Box 2 (%)	Box 3 (%)	Box 4 (%)	Total (%)
Q5 in water	$16.1 \pm 1.3$	$40.4\pm1.1$	$29.1 \pm 0.9$	$13.8\pm0.8$	$99.4 \pm 0.1$
Q5 in EV limit	$5.5\pm0.9$	$27.6 \pm 1.7$	$42.0\pm1.6$	$22.1 \pm 1.8$	$97.2 \pm 0.4$
Q15 in water	$36.1 \pm 3.4$	$33.1 \pm 2.0$	$22.1 \pm 1.8$	$6.7\pm1.0$	$98.1 \pm 0.3$
Q15 in EV limit	$3.0\pm0.5$	$8.1\pm0.9$	$23.6 \pm 1.3$	$21.3\pm0.8$	$56.1 \pm 1.5$

\*All errors are standard errors obtained from the bootstrap analysis. Column 6 shows the sum of the cumulative statistics in the four regions for each class of simulation. Sizes of ad hoc boxes in Figure 3 are as follows: 1.2 Å along  $R_{\rm g}$  and 0.125 along  $\delta$  for Q5, and 3.25 Å along  $R_{\rm g}$  and 0.2 along  $\delta$  for Q15. Definitions of the four regions for Q5 are as follows: Box 1: 4.5  $\leq$   $R_{\rm g}$  < 5.7 and 0  $\leq$   $\delta$  < 0.125; Box 2: 4.9  $\leq$   $R_{\rm g}$  < 6.1 and 0.125  $\leq$   $\delta$  < 0.25; Box 3: 5.3  $\leq$   $R_{\rm g}$  < 6.5 and 0.25  $\leq$   $\delta$  < 0.375; Box 4: 5.6  $\leq$   $R_{\rm g}$  < 6.8 and 0.375  $\leq$   $\delta$  < 0.5. Definitions of the four regions for Q15 are: Box 1: 6.5  $\leq$   $R_{\rm g}$  < 9.75 and 0  $\leq$   $\delta$  < 0.2; Box 2: 7.25  $\leq$   $R_{\rm g}$  < 10.5 and 0.2  $\leq$   $\delta$  < 0.4; Box 3: 8.75  $\leq$   $R_{\rm g}$  < 12 and 0.4  $\leq$   $\delta$  < 0.6; Box 4: 10  $\leq$   $R_{\rm g}$  < 13.25 and 0.6  $\leq$   $\delta$  < 0.8.

expect for a chain in the EV limit. In the latter case, conformations that are relatively extended with larger values of  $\delta$  are favored. These differences are tabulated in Table I which provides a summary of cumulative statistics over boxes used to analyze  $\rho(\delta,\,R_{\rm g})$  for the peptides in water. As shown in Table I, differences between  $\rho(\delta,\,R_{\rm g})$  and  $\rho_{\rm EV}(\delta,\,R_{\rm g})$  increase with increasing chain length. However, in water and in the EV limit there is an increase in conformational heterogeneity as chain length increases. This is characterized by broadening of the  $R_{\rm g}$  distribution for Q15 vis-à-vis Q5 (Fig. 4). This increase in conformational heterogeneity implies an ensemble characterized by large fluctuations — a feature that has direct bearing on the increase in likelihood of nucleating  $\beta$ -sheets with increasing chain lengths.

In the EV limit, the scaling of  $R_{\rm g}$  with chain length can be written as  $R_{\rm g}=R_{\rm o}N^{0.59}$ .  $^{86,88,95}$  Unlike denatured proteins which obey the scaling laws for chains in the EV limit,  $^{94}$  the ensemble for disordered polyglutamine in water is, on average, much more compact [Figs. 3(b,d) and 4]. To compute the requisite scaling exponent and average packing density we will need to carry out simulations for several chain lengths including very long chains. This analysis is part of ongoing work. A discussion of two possibilities for monomeric polyglutamine follows.

In accordance with the behavior of folded, globular proteins, which are akin to chains in a poor solvent, the radius of gyration for monomeric polyglutamine could scale as,  $R_g = R_0 N^{0.34}$ . If this scaling applies, then polyglutamine prefers to be collapsed or crumpled<sup>96</sup> without showing a discernible preference for a specific backbone conformation. If so, the mechanism of  $\beta$ -sheet nucleation involves a conformational transition on the manifold of compact states.<sup>95</sup> It is also possible that the disordered ensemble is such that chain-chain repulsions exactly counterbalance chain-chain attractions. For this case  $R_{\rm g} = R_{\rm o} N^{0.5}$  and polyglutamine would behave like a flexible, unperturbed chain in a so-called theta state.88 However, the ensemble average value of  $\delta$  is 0.29 for Q15, which is consistent with a spheroid rather than an ellipsoid or a rod.  $^{84}$  The Q15 peptide is a likely indicator of the average shape for longer peptides. Hence, the current data would appear to exclude the theta state as a possibility because  $\delta > 0.6$  for a chain in the theta state. 86 Therefore, it appears that polyglutamine in water is a statistical coil in a poor solvent in that it is compact with access to a heterogeneous distribution of backbone conformations.

#### **Regular Local Conformations**

We analyzed the ensembles of Q5 and Q15 in water to assess quantitative preferences for canonical local secondary structures such as α-helices, β-strands, and polyproline II  $(P_{II})$  helices. These structures come about when consecutive stretches of backbone  $(\phi, \psi)$ -angles adopt similar values. To assay for regular local structures we use the PROSS algorithm. 97 This is a method for secondary structure assignment based solely on backbone  $(\phi, \psi)$ -angles. The results are tabulated in Table II. For a given peptide, the numbers shown in Table II quantify the probability of finding a conformation with at least three consecutive residues adopting  $(\phi,\psi)$ -angles compatible with either regular  $\alpha$ -helices, regular  $\beta$ -strands, or regular  $P_{II}$ -helices. It is clear that these probabilities vary with chain length. However, for a chain of a given length, the probabilities for accessing short stretches of different canonical regular conformations are similar to each other. The conclusion is that by this low-resolution assay for structure, no single regular conformation dominates. In the parlance of energy landscape theory, 83 we propose that the landscape is like an egg-carton showing signatures of maximal frustration.98

#### **Conformational Propensities**

In Figure 5(a,b) we compare the conformational propensities of individual residues extracted from the Q5 and Q15 peptides, which are shown as Ramachandran (contour) maps.  $^{99}$  For a given residue in Q5 or Q15, contour maps are constructed by picking conformations from an ad hoc cluster [Fig. 3(a,b)] and tabulating the residue-specific probabilities for accessing distinct regions within  $(\varphi,\psi)$ -space.

#### Results for Q5

Figure 5(a) shows  $(\phi,\psi)$ -maps for all residues of the Q5 peptide using conformations drawn from all four ad hoc regions of  $(\delta,R_{\rm g})$ -space. For conformations drawn from box 1 there is a clear preference for  $\alpha$ -helical  $(\phi,\psi)$ -angles. This implies a preference for either a single turn of  $\alpha$ -helix or for Type I helical turns. Conversely, for conformations drawn from box 4 there is a marked preference for  $P_{\rm II}$ -like

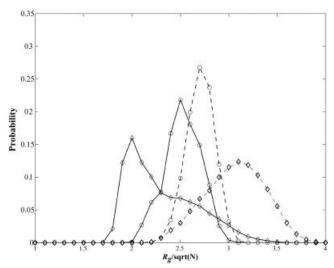


Fig. 4. Comparison of probability distributions of radii of gyration. Here N denotes chain length. Four curves are shown. These include Q5 in water (-o), Q15 in water (- $\diamond$ ),Q5 in the EV limit (—o), and Q15 in the EV limit (-- $\diamond$ ).

TABLE II. Probability (%) of Finding a Conformation with Regular Local Structure\*

	α-Helix	β-Strand	$P_{II}$ -Helix
Q5 in water	$4.24\pm0.45$	$4.19\pm0.20$	$6.32 \pm 0.36$
Q15 in water	$13.49 \pm 1.44$	$12.13\pm0.87$	$16.71\pm0.88$

<sup>\*</sup>Regular structures are assayed using PROSS algorithm.<sup>97</sup> All errors are standard errors estimated from the bootstrap analysis.

(φ,ψ)-angles. Although the intrinsic propensity of glutamine for  $P_{\rm II}$  and  $\alpha\text{-helical}$  (φ,ψ)-angles is high and consistent with experimental data  $^{100}$  this does not result in an ensemble that is a simple combination of regular  $P_{\rm II}$  and  $\alpha\text{-helices}.$  Instead, irregular conformations that are realized by combinations of the two types of (φ,ψ)-angles are the norm. This is quantified in terms of the populations associated with boxes 2 and 3 for Q5 [Fig. 3(a)] — the two regions that account for approximately 70% of the Q5 conformational ensemble (Table I). From analysis of the Q5 dihedral angle distributions we conclude that helical turns and bends derived by irregular combinations of  $\alpha\text{-helical}$  and  $P_{\rm II}$  (φ,ψ)-angles dominate the ensemble for the Q5 peptide.

#### Results for Q15

As a point of comparison, we show in Figure 5(b)  $(\phi,\psi)$ -maps for the five central amino acids of the Q15 peptide. Data in Table I indicate that for Q15 there is a greater preference for conformations that are compact and globular versus those that are extended. There is an approximately 70% chance of finding the peptide in the regions 1 and 2 shown in Figure 3(b). Conformations drawn from these regions are compact and loosely packed globules and there is an increased propensity for forming Type II turns. The latter is evidenced by the increased accessibility for positive  $\phi$ -angles, especially left-handed

 $\alpha$ -helix  $(\varphi,\psi)$ -angles, which in combination with the intrinsic propensity for the  $P_{\rm II}$  region leads to the formation of  $\beta$ -turns [Fig. 5(b)].

#### **β-Sheet Formation in Q15**

Although the probability of forming β-turns is finite and quantifiable, the overall likelihood of sampling regular  $\beta$ -sheet geometries remains small. This is because the tendency toward disorder, driven by the intrinsic propensity for different regions of  $(\phi,\psi)$ -space, promotes the sampling of diverse backbone conformations. In other words, there exists an entropic bottleneck to accessing β-sheet geometries. This bottleneck can be overcome and statistical fluctuations do lead to a small but real probability that the Q15 peptide accesses antiparallel β-sheets. We estimate this probability to be between 0.1 and 2%. In Figure 6 we show representative structures drawn from each ad hoc region of the two-dimensional order parameter space identified in Figure 3(b). It is clear that when the chain is compact there is a finite probability of adopting antiparallel β-sheet geometries. Not surprisingly, it is nearly impossible to nucleate any kind of β-sheet structure for the Q5 peptide. Even for Q15, the small likelihoods associated with  $\beta$ -sheet structures implies that interactions which promote conformational heterogeneity compete with β-sheet formation. We now proceed to identify the interactions that promote conformational heterogeneity and hence a disordered ensemble.

#### Why are the Ensembles for Q5 and Q15 Disordered?

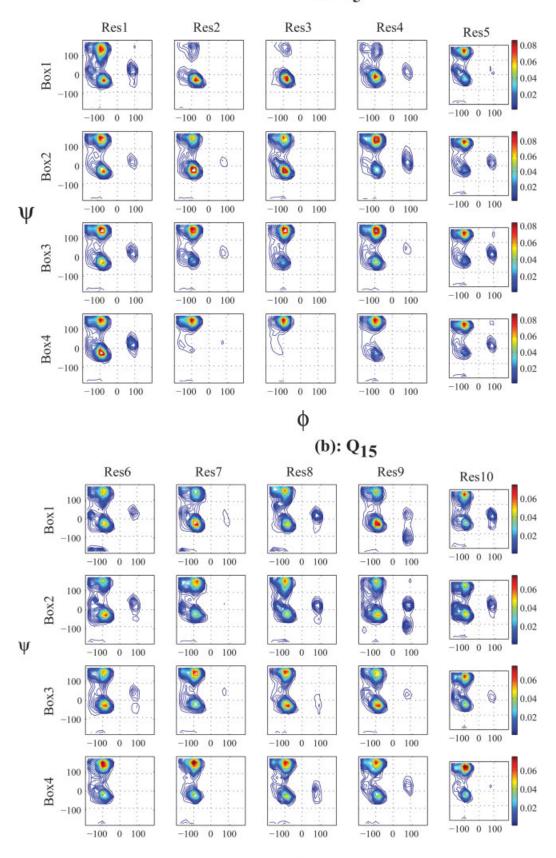
The Q5 ensemble is disordered because the peptide is too short to realize cooperative transitions into ordered, regular secondary structures. We focus our analysis on the Q15 ensemble and quantify the average number of hydrogen bonds (backbone-backbone, backbone-sidechain, and sidechain-sidechain) found in different conformations accessible in the disordered ensemble.

In general, a Q15 conformation drawn from any of the four conformational regions, shown in Figure 3(b), will have more sidechain—backbone hydrogen bonds than either of the other two types. This is shown in Figure 7, which plots the average number of hydrogen bonds per conformation realized in each region identified in Figure 3(b).

Sidechain—backbone hydrogen bonds are realizable in a wide variety of backbone geometries, including compact globules and extended geometries. Additionally, these hydrogen bonds can be both local and nonlocal. This is illustrated in Figure 8, where we show four dissimilar backbone conformations, all of which have four sidechain—backbone hydrogen bonds. The backbone peptide units are

Fig. 5. Ramachandran plots shown as contour maps in  $(\varphi,\psi)$ -space. (a): Contour maps are shown for each of the five residues of the Q5 peptide. Each row corresponds to conformations extracted from an ad hoc cluster identified in Figure 3. (b): Ramachandran maps for the five central residues of the Q15 peptide. Each row corresponds to conformations extracted from an ad hoc cluster identified in Figure 3. In both sets of plots the color bar for each row is situated at the end of the row.

### (a): Q5



φ

Figure 5.

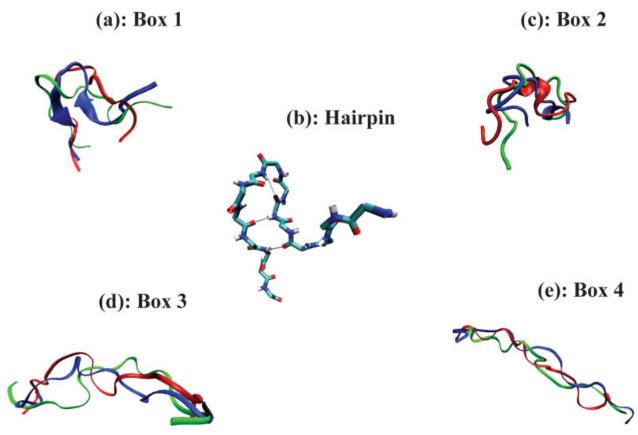


Fig. 6. Representative conformations drawn from the different regions (boxes 1–4) of the order parameter space identified in Figure 3(b). The pictures are meant purely for illustration only. No quantitative statistics are to be ascribed to these snapshots. Figure 6(b) illustrates the fact that statistical fluctuations can lead to a sampling of β-sheet geometries that are akin to a β-hairpin with antiparallel strands.

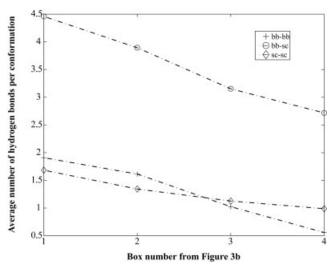


Fig. 7. Average number of hydrogen bonds per conformation extracted from the four ad hoc clusters identified for Q15. Data shown are for backbone—backbone (+), sidechain—backbone (o), and sidechain—sidechain ( $\diamondsuit$ ) hydrogen bonds. The dashed-dotted lines (-.) serve as visual aids.

predominantly solvated by way of hydrogen bonds to the polar sidechain or through surrounding water molecules and these modes of backbone solvation are not restricted to a specific backbone conformation. The conclusion is that Q15 is disordered because sidechain–backbone hydrogen bonds can form almost anywhere along the chain and in any of the conformations accessible to Q15.

Eberhardt and Raines<sup>101</sup> showed that 25.2*M*-formamide is almost as good as 55.5*M*-water in terms of its ability to form hydrogen bonds with backbone peptide units. Formamide, which is a primary amide, mimics polar moieties in the sidechains of glutamine and asparagine. In polyglutamine the effective concentration of the sidechain primary amide around the backbone peptide unit is always high because the polar moiety is covalently attached to the backbone. Hence, the glutamine sidechain can compete with water as an alternative solvent and form hydrogen bonds to the backbone. This increases the number of different modes for solvating the backbone. Consequently, the probability associated with any specific backbone conformation decreases and this in turn promotes backbone disorder.

#### What are the Implications for $\beta$ -sheet Nucleation?

In addition to providing an explanation for the observed disorder, the conformation-independent probability of realizing multiple sidechain–backbone hydrogen bonds also leads to a hypothesis for why  $\beta$ -sheet formation is postulated to be a highly unfavorable thermodynamic reaction. <sup>1</sup>

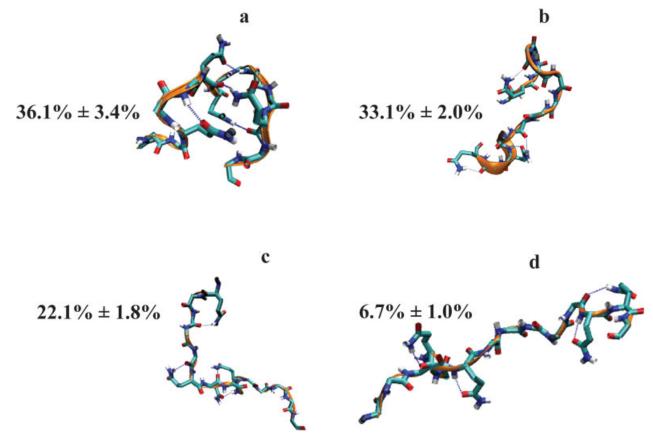


Fig. 8. Four disparate conformations each with four sidechain–backbone hydrogen bonds. Sidechain atoms are depicted only for those residues that participate in sidechain–backbone hydrogen bonds. Blue dotted lines indicate sidechain–backbone hydrogen bonds. In all pictures the gold colored ribbon identifies the backbone. Numbers (%) shown next to each conformation refer to the percentage probabilities associated with the ad hoc cluster from which the conformation is drawn.

Classic secondary structures are characterized by backbone-backbone hydrogen bonds that require a regular repeat of  $(\phi,\psi)$ -angles. <sup>102</sup> In the case of  $\beta$ -sheets there is an additional need for the appropriate registry of  $\beta$ -strands. The possibility of realizing sidechain-backbone hydrogen bonds almost anywhere along the homopolymeric chain interferes with the cooperativity of interactions required for transitioning into regular secondary structures, 103 since a large fraction of peptide units become unavailable for cooperative backbone-backbone interactions. Consequently, the probability of adopting conformations in which the backbone solvates itself via backbone-backbone hydrogen bonds is very small. For example, the probability of finding an individual glutamine in α-helical or P<sub>II</sub>-like  $(\phi,\psi)$  value is high (Fig. 5). Sidechain-backbone hydrogen bonds contribute to these high intrinsic propensities (data not shown). Intrinsic propensities facilitate the formation of bends and turns. However, it is not easy to localize these bends and turns to a specific part of the homopolymeric polyglutamine sequence. Additionally, the high intrinsic propensity for  $P_{II}$ - and  $\alpha$ -helical  $(\phi,\psi)$  values interferes with strand propagation. This in turn makes it difficult to realize the correct registry of strands required for backbone-backbone hydrogen bonding. Our model provides a plausible explanation for the strong chain length dependent aggregation of polyglutamine peptides.

Support for these observations comes from the mutational analysis of Thakur and Wetzel<sup>44</sup> who showed that sequences of the form (Q9PG)4 and (Q10PG)4 undergo spontaneous aggregation, whereas sequences of the form (Q7PG)4 and (Q8PG)4 do not aggregate as readily. Furthermore, the sequence ( $P_{\rm D}GQ9$ ), where  $P_{\rm D}$  is D-proline enhances the aggregation rate vis-a-vis the sequences with L-proline. Ross and coworkers have arrived at similar conclusions using mutational analysis of the exon 1 fragment of huntingtin.  $^{104}$  These data are suggestive of a minimum length requirement for extended  $\beta$ -strands. Insertion of turn forming amino acids in locations that interrupt the disordering tendencies of polyglutamine appear to pre-pay some of the entropic penalty that opposes  $\beta$ -sheet nucleation.

#### DISCUSSION

#### **Summary**

We have used multiple molecular dynamics simulations to characterize the conformational ensemble of monomeric polyglutamine for two peptides, Q5 and Q15. Consistent with expectations from CD data, we have shown that the

ensembles for both peptides are disordered. However, there are quantifiable differences between the two ensembles and in particular as chain length increases there is an increased probability of sampling more compact geometries. Furthermore, fluctuations for Q15 are greater than for Q5 as evidenced by the broadening of the distribution shown in Figure 4.

We showed that a typical Q15 conformation has on average four to five sidechain–backbone hydrogen bonds (Fig. 7). This is true irrespective of whether the conformations are compact, semi-compact, or extended (Fig. 8). Sidechain–backbone hydrogen bonds can furthermore be local or non-local. Conformations in the disordered ensemble are solvated by hydrogen bonds to sidechain polar groups or surrounding water molecules. The multiplicity of alternative (non backbone–backbone) hydrogen bonding possibilities provides an insight into why  $\beta$ -sheet formation is thermodynamically unfavorable.

Nucleation of  $\beta$ -sheet, a process which requires a change in solvation state whereby the backbone solvates itself, requires that a conformational entropy bottleneck be overcome. This bottleneck is based on the nearly conformation-independent probability of realizing sidechain–backbone hydrogen bonds in polyglutamine tracts. In short, we propose that swapping so many sidechain–backbone or water–backbone hydrogen bonds for backbone–backbone hydrogen bonds is opposed by conformational entropy.

It should be noted that it is more than likely that our observations will vary if we were to use a different force field. Hence, the robustness of our conclusions can only be assayed by carrying out similar simulations using a cross-section of force fields and water models — an expensive, yet important proposition.

It is imperative to remind the reader that at the requisite concentrations (ca.  $10\mu M$ ) long polyglutamine peptides aggregate to form  $\beta$ -sheet rich aggregates.  $\beta$ -sheet aggregates are expected to be thermodynamically preferred states at high concentrations. The fact that monomeric polyglutamine is predominantly unfolded in solution leaves it susceptible to folding via aggregation. The question of interest is why is folding or  $\beta$ -sheet formation thermodynamically unfavorable for monomeric polyglutamine? The foregoing analysis provides a plausible explanation for why monomeric polyglutamine prefers to be disordered in solution.

β-helices versus antiparallel β-sheets? We find that statistical fluctuations can lead to a sampling of β-sheet geometries for Q15 (Fig. 6). Because it is relatively easy to sample bends and turns, there is a small but finite probability of accessing antiparallel β-sheets. This is important in light of two different interpretations of fiber diffraction data for a D2Q15K2 peptide. Perutz and coworkers proposed that the data were consistent with the peptide adopting a β-helical structure that gives rise to a water-filled nanotube for the amyloid fiber. Recently Sikorski and Atkins to be consistent with a once folded that the data appear to be consistent with a once folded hairpin conformation. The trends seen in our simulations [Fig. 6(b)], provide tentative and independent support for

the model of Sikorski and Atkins.  $^{106}$  However, results from coarse-grain simulations  $^{107}$  and shorter molecular dynamics simulations  $^{108}$  appear to lend support for the parallel  $\beta$ -helix model while data for aggregation kinetics are consistent with both structural models.  $^{26}$ 

Pending the availability of data of the kind shown in this work for longer polyglutamine peptides, we are forced to remain agnostic about the types of  $\beta$ -sheet structures accessible to polyglutamine peptides. This is an important issue to resolve because it is reasonable to assume that  $\beta$ -sheet structures sampled by the monomer  $^{26}$ — the nucleus for aggregation— are related to the structure of the monomer in the context of the aggregate. Alternatively, it is also conceivable that heterogeneity in monomeric  $\beta$ -sheet structures could explain the diversity of oligomeric structures observed by Muchowski and coworkers  $^{40}$  for aggregates of polyglutamine expansions.

#### **Connection to Theories and Ongoing Work**

The finding of Wetzel and coworkers that the monomer acts as the nucleus  $^1$  for aggregation is significant because there are theories for  $\beta\text{-sheet}$  nucleation that allow one to calculate the free energy for  $\beta\text{-sheet}$  formation as a function of chain length.  $^{109}$ 

Finkelstein <sup>109</sup> has estimated the minimal length  $N^*$  of an unstable intermediate to be  $N^* \approx \frac{F_t}{(-\Delta F_\beta)}$ . Here  $F_t$  is the free energy of a turn/bend/loop that connects adjacent strands of a sheet and  $\Delta F_\beta = F_\beta - F_c$  is the free energy change for a transition from coil to  $\beta$ -sheet. The length  $N^*$  is estimated by stipulating that for  $N=N^*$  the free energy gain from addition of a strand compensates the free energy lost for nucleating a turn. Interestingly, in this theory there is a chain length past which the  $\beta$ -sheet is the stable entity — a situation that does not appear to hold for monomeric polyglutamine. Finkelstein <sup>109</sup> notes that conformational heterogeneity in the coil state will profoundly influence both the sign and magnitude of  $\Delta F_\beta$ .

We propose that sidechain–backbone hydrogen bonds leads to frustration  $^{83}$  in that  $\Delta F_{\beta}$  can never be less than zero for monomeric polyglutamine irrespective of chain length although the relative values of  $\Delta F_{\beta}$  decrease with increasing chain length. To test this hypothesis we need robust estimates of  $\Delta R_i F_{\beta}$  for polyglutamine as a function of chain length. This will require quantitative knowledge of length-dependent changes in PDFs for longer polyglutamine chains and significant enhancement in sampling including the use of replica exchange  $^{49,52,59}$  and other multiplexing  $^{110}$  strategies. This work is ongoing.

#### **ACKNOWLEDGMENTS**

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$$\mathbf{T} = \frac{1}{N+1} \sum_{i=0}^{N} (\mathbf{s}_i \otimes \mathbf{s}_i). \tag{5}$$

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