Protein Docking Using a Genetic Algorithm

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A genetic algorithm (GA) for protein-protein docking is described, in which the proteins are represented by dot surfaces calculated using the Connolly program. The GA is used to move the surface of one protein relative to the other to locate the area of greatest surface complementarity between the two. Surface dots are deemed complementary if their normals are opposed, their Connolly shape type is complementary, and their hydrogen bonding or hydrophobic potential is fulfilled. Overlap of the protein interiors is penalized. The GA is tested on 34 large protein-protein complexes where one or both proteins has been crystallized separately. Parameters are established for which 30 of the complexes have at least one near-native solution ranked in the top 100. We have also successfully reassembled a 1,400-residue heptamer based on the top-ranking GA solution obtained when docking two bound subunits. Proteins 2001;44:44-56. © 2001 Wiley-Liss, Inc.

Key words: shape complementarity; macromolecular docking; protein-protein interaction; molecular recognition; proteinprotein docking; genetic algorithm

INTRODUCTION

Protein-protein recognition represents a fundamental aspect of biological function. However, although protein structures are now routinely determined by methods such as X-ray crystallography, it is much more difficult to ascertain the structure of protein complexes, and only about 100 of these are currently deposited in the Protein Data Bank (PDB). Protein docking studies are therefore important as an aid to our understanding of the ways in which proteins associate.2 Methods for protein ligand docking, such as DOCK,3 FLOG,4 FLEXX,5 and GOLD,6 are widely used in drug-discovery programs. However, because of the complexity of the problem, protein-protein docking is still largely at the theoretical stage. Many solutions have been proposed but, although very promising results have been obtained in some cases, there is still considerable scope for the development of methodology and exploration of alternative or ancillary approaches.

Protein docking methods are generally based on the idea of complementarity between the interacting molecules. This complementarity may be geometric or electrostatic, or both. Recently there have been two investigations into the

validity of the complementary shape hypothesis. Betts and Sternberg⁸investigated the conformational changes that occurred on complex formation for a total of 30 complexes. These investigators concluded that, for the enzymeinhibitor complexes that comprised most of their data, recognition could be "treated as lock and key to a first approximation." In a study of specific interprotein interactions (e.g., nonpolar buried surface area, polar buried surface area, number of hydrogen bonds), Norel et al.9 found no correlation between any of these and the likelihood that a putative docking was correct. Instead, their finding confirmed the "long held notion of the importance of molecular shape complementarity in the binding and hence in docking." Both proteins are usually treated as rigid bodies, since to allow flexibility may be computationally intractable. Many shape-based docking algorithms have been proposed. 10-15 Some include other information (e.g., hydrophobicity, electrostatics) either in conjunction with shape matching 16 or as a subsequent filter. 17 Several geometric docking programs use the Connolly molecular surface representation.¹⁸ Three are of particular interest, as they have some similarity to the method we describe below.

Connolly¹⁹ described a method for selecting "critical" points of the Connolly surface. The idea of the critical points is to preserve the important features (local maxima and minima) of the protein surface, while reducing the computational intractability associated with processing very large numbers of surface points. These critical points (termed "knobs" and "holes") represent points that would be expected to match (knobs on one protein with holes on another and vice versa) in a successful docking. Connolly required four pairs of critical points to match in order to define a rigid body translation and this proved too restrictive in one of the two complexes he attempted to dock. However, Norel et al.²⁰ showed that pairs of two critical points plus the normals to the surface at these points are sufficient to dock the example at which Connolly's algorithm failed. In further work, the same group docked 26

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"large" protein-protein complexes from the PDB using the whole of the surface of both proteins and without using any chemical information such as hydrogen bonding potential.21 The dockings usually took only a few minutes of CPU time and generated a manageable number of solutions with the correct solution ranked high (in 22 cases, ranked 1). In further work, they applied the same algorithm to 19 complexes using data taken from the native protein structures.9 Recently Hou et al.22 used a genetic algorithm in combination with a tabu search to match dots of the Connolly surface in the initial global search stage of their docking. They also required the surface normals to match; the fitness score was then calculated according to the amount of buried surface area, weighted by a penalty for steric clash, proportional to the number of overlapping atoms. This is similar in form to our fitness function (detailed under Materials and Methods), except that we take account of matching dots rather than buried surface area and calculate overlap in a different manner. They followed this by performing local energy calculations for the top ranked solutions. Most of the computation in the global search is done by the tabu search element of their hybrid algorithm. The genetic element is used to diversify the search. The local search is then also performed by a GA; it attempts to minimize the interaction energy (van der Waals energy, electrostatic energy, and hydrogenbond energy) between the participating molecules. They report good results on a test set of seven complexes (five bound and two native).

Most early attempts at protein–protein docking involved only reassembling complexes using coordinates taken from the complex. More recently there have been several studies using native proteins. ^{9,16,23–25} There have also been two protein–protein docking challenges. ^{7,26}.

Most docking studies concentrate on enzyme—inhibitor complexes (most commonly serine protease—inhibitor complexes) and antibody—antigen complexes. A recent comparison of the protein—protein interactions in these two different types of complex concluded that, in general, a protease—inhibitor interface was more static and hence more easily predicted than an antibody—antigen interface. This result is generally borne out by docking studies which have used unbound proteins. ²³

In our previous work on docking, we used techniques from graph theory to predict maximum sets of possible hydrogen bonds and used these to superpose the proteins to form a complex.²⁸ While this method was able to reassemble complexes, it proved less successful when docking native proteins, and here we have considered the use of a genetic algorithm (GA) for this purpose.

GAs have been shown to be of use in many areas of bioinformatics. A GA is a search algorithm based on accepted theories of biological evolution and natural selection. It operates on a population of solutions, applying the principle of "survival of the fittest." After a number of generations, a good, although not necessarily optimal, solution is obtained. Applications of GAs to structural biology include investigation of protein folding, ²⁹ ligand binding to receptor sites, ³⁰ protein structure and sequence comparison, ^{31,32} protein secondary structure prediction, ³⁰

protein docking,³³ nuclear magnetic resonance (NMR), and X-ray crystallographic data analysis.34 At Sheffield, we have used GAs successfully for many different applications, including database searching,35 protein folding,36 protein ligand docking and database screening,37 identifying features common to sets of ligands,38 selection of compounds for combinatorial libraries, 39 and protein surface comparison, 40 inter alia. In this article, we present a genetic algorithm for protein docking based on the surface comparison method of Poirrette et al.,40 but which we have modified in order to capture the regions of greatest complementarity between the two proteins that are being docked. We demonstrate that, for a large number and variety of complexes, using mainly native data, our GA is able to produce highly ranked putative complexes that resemble the crystallographically determined complex.

MATERIALS AND METHODS

The basic method is based on that of Poirrette et al.,⁴⁰ who used a GA for surface comparison. A GA was used to generate rotations of the smaller (query) protein relative to the larger (target) protein surface, which was held static. Both proteins were treated as rigid bodies. We provide brief details, paying particular attention to the modifications made for protein docking.

We first generated the proteins' Connolly dot surfaces using the program MS, 18,41 with a probe radius of 1.5 Å and a dot density of 1 dot/Å2. In addition to threedimensional (3D) coordinates for each dot, this program calculates the direction of the normal to the surface and also the type of surface (1 = convex, 2 = saddle, 3 = concave). We modified the program slightly so that each dot was also labeled with the hydrogen bonding potential of the nearest atom. The classification we adopted was as follows: -H-donor, H-acceptor, H-donor/acceptor, and non-H-bonding. All oxygen atoms were labeled as H-acceptor with the exception of the OH of tyrosine, the OG of serine and the OG1 of threonine, all of which were labeled as H-donor/acceptors. For simplicity, all nitrogen atoms were labeled as H-donors, including the histidine nitrogens ND1 and NE2 whose individual protonation states are difficult to assign. All other atoms were classified as non-H-bonding.40

Both proteins were translated so that their centers of gravity were positioned at the origin of space. This origin was also the center of a 3D grid placed around the target protein; it was sufficiently large that any query dot could contact any target dot, and the entire query molecule still remain within the grid. Each grid box was a 2-Å cube. Dots contained within the same grid box were given the same grid coordinate, which was that of the corner of the grid box nearest to the origin. This "coarsening" of the surface representation allowed for some tolerance in the matching of the protein surfaces, which was necessary to accommodate movements of the proteins from the native to the bound conformation, and also it enabled the implementation of a very fast routine for dot matching, thus increasing both the effectiveness and the efficiency of the program.

Each chromosome, corresponding to a potential docking, consisted of six integer elements, corresponding to the six

degrees of freedom necessary to define the movement of one rigid body relative to another. The first three elements corresponded to rotations of $0-359^{\circ}$ about the x, y, and z axes, respectively, and the remaining three to translations (measured in tenths of an Ångstrom) along the original x, y, and z axes. An initial population of chromosomes was generated at random, each was applied to the query protein dots (the target remained fixed), and the fitness of the resulting complex was calculated (as described below).

The GA was of a type known as steady-state-with-noduplicates, meaning that a fixed proportion (in our case 5%) of the chromosome population was replaced after each generation and that duplicate chromosomes were not allowed. 42,43 The chromosomes replaced were those that were least fit in the population. New chromosomes were generated by applying the genetic operators mutation and/or crossover to parents chosen by roulette wheel selection. Mutation took one parent chromosome and produced one child. In standard mutation, a position was chosen at random along the parent and randomly mutated to another value (keeping within the range 0-359 if a rotation was being mutated). Small-creep mutation operated in the same way except that the replacement value was close to the original (within 5° for a rotation and within 2 Å for a translation). When mutation was the chosen genetic operator, standard or small-creep mutations were chosen at random (with equal likelihood). Crossover took two parents and produced two children, in one of two ways. In single-point crossover a position along the chromosome was chosen at random and all elements subsequent to the chosen point were then swapped over between the two chromosomes. In exchange-crossover, a point was again chosen at random and just that element was swapped between the two chromosomes. When crossover was the chosen genetic operator, single-point or exchange-crossover were again chosen at random (with equal likelihood). After a predetermined number of generations (1,000 for all the tests reported here) the GA was presumed to have converged and the fittest population member was saved as a solution.

We have also applied a technique called niche restriction, ⁴⁴ which we use to force the GA to explore different regions of solution space. After the first run through, an area (niche) around the fittest solution was removed from the solution space. The area removed was a sphere of radius 2 Å centered on the center of gravity of the fittest solution. The GA was then restarted as before, except that no chromosomes were allowed to place the center of gravity of the query protein within the restricted niche. After the second runthrough, a second niche was defined and so on. In our case, we obtained 5 niches per GA run, each niche corresponding to a potential solution.

Fitness Function

The GA thus described is similar to the surface matching algorithm of Poirrette et al.⁴⁰ The critical difference in the new method lies in the fitness function since for protein docking we are looking for complementary rather than similar surfaces, with minimal overlap of the protein interiors. However, during initial testing we found that too

stringent a complementarity requirement was unsuccessful in that "fit" solutions did not correspond to correct orientations of the query protein. Thus we have adopted a principle of "not similar" matching where necessary. So, for a pair of target and query dots, a match was declared if (1) their grid coordinates were the same (thus, they occupy the same region of space); (2) their surface normals were nearly opposite (the angle between them should be close to 180°—the actual value was a parameter); (3) their Connolly shape type was not the same, unless they were type 2. (i.e., 1 matched 2 or 3, 3 matched 1, or 2 and 2 matched anything); or (4) their hydrogen bonding potential was satisfied, i.e., H-donor matched H-acceptor or H-donor/ acceptor, H-acceptor matched H-donor or H-donor/acceptor, H-donor/acceptor matched H-donor, H-acceptor or H-donor/acceptor, non-H-bonding matched non-H-bonding.

We also wished to apply a penalty for overlap of the protein interiors whilst allowing for slight surface clashes. We did this by defining a set of "interior" points of the target protein. These were grid points that were near to a target protein atom and that were further than a user defined "thickness" parameter from any surface dot. In all the tests described in this report, a thickness of 2 Å was used. The coordinates of the interior points were hashed to integer values and stored in a sorted list. As their creation took 5-30 min on a Silicon Graphics 270-MHz O2 workstation with R12000 processor (depending on the size of the target), a set of interior points for a particular thickness was only created once and was stored on file for subsequent GA runs. For a possible orientation of the query with respect to the target, we counted the number of matching dots and the number of clashes between query dots and target interior points. The penalty was then given by

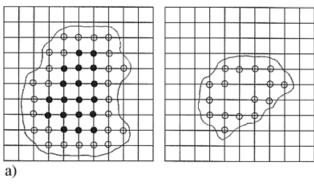
 $\mbox{Penalty} = \begin{array}{cc} \mbox{\it J* number of clashes} & \mbox{if any dots matched} \\ 100,000 & \mbox{if no dots matched} \end{array}$

where J, the penalty multiplier, was an input parameter. The fitness of the chromosome was then given by

Fitness = number of matches - penalty

We recognize that this is not an even-handed approach. For example, a long side-chain may protrude from the target. A single side-chain is "thin" (i.e., by our definition, it has no interior points) and thus, if it penetrates the query, this will not be penalized. However, for the query protein, such a side-chain's penetration of the target would attract a penalty, as it would clash with the target interior points. We have taken this pragmatic approach to minimize computation (and hence time) required for docking. Calculating the new positions of the query points is one of the most time-consuming parts of the GA. If interior points were to be defined for the query, their position would also have to be recalculated for each alteration of each chromosome, which would be a further time burden. Some results of this "lopsidedness" is discussed later.

The GA may be used with entire protein surfaces or one or both proteins may be just a site. If a site was used, surface dots were generated for only that part of the protein surface. However, if that protein was the larger of



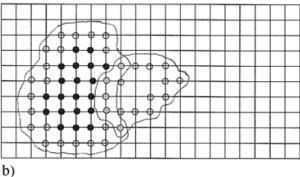


Fig. 1. a: Target and query proteins have their surfaces represented by grid point dots (○). The target also has interior points (●). b: Surface grid dots are matched (gray filled) to produce a putative complex. (N.B.: The proteins are positioned too closely together.)

the two, it could still be considered as the target. In that case, interior points were generated for the entire protein, not for the site alone. Figure 1 illustrates surface representation and matching.

During preliminary tests, we observed that, irrespective of whether a predictive complex resembled a crystallized complex, the GA tended to position the two proteins infeasibly closely. This is due in part to the protein representation we use. As surface points are mapped to grid points that are slightly nearer the origin, when grid points from two proteins are superposed, this causes the proteins to be positioned too closely together (Fig. 1). We therefore developed a separation program that we applied to each fit solution proposed by the GA. This program used a least squares superposition to find the best alignment of the pairs of normals which belong to a set of matching dots. We then moved the query protein 2 Å away from the target in the direction of this alignment.

Based on extensive testing we have determined that the parameters settings given in Table I caused the GA to converge and, as demonstrated below, appeared to be appropriate for this application domain.

RESULTS AND DISCUSSION Docking Bound Complexes

Our aim in docking is correctly to predict the structure of the complex formed when two native proteins bind. First, however, we tested the method and determined which new parameter values were successful, using the well-known (and often docked) complexes chymotrypsin—inhibitor com-

TABLE I. Parameter Settings Used by the GA

| Parameter | Value |
|--|-------|
| Population size | 400 |
| No. of runs | 1,000 |
| Percentage of population replaced each iteration (%) | 5 |
| Mutation/crossover rate (%) | 50 |
| Selection pressure | 1.1 |
| Niche sphere diameter (Å) | 2 |
| No. of niches | 5 |

plex (PDB code 1cho), subtilisin–inhibitor complex (PDB code 2sni), and the antibody Fab–antigen complex HyHel-5–lysozyme (PDB code 3hfl). We separated each complex into two PDB files and randomly reoriented the smaller protein and moved it away from the larger one. For the antibody–antigen docking, we used only those residues of the Fab within 8 Å of the known antibody-binding site. The parameter settings we wished to establish were the angle between the surface normals and the penalty multiplier. We varied the normal angle between 180° \pm 10° and 180° \pm 30° in 5° steps, and the penalty multiplier J between 0.5 and 3.5 in steps of 0.5. For each parameter combination we obtained 100 possible solution chromosomes by running the GA 20 times, each run yielding 5 niches. These were then ranked in decreasing order of fitness.

The best results for these three complexes are summarized in Table II. The root-mean-square deviations (RMSD) quoted for these bound complexes were calculated by superposing the enzymes of the predicted and crystallized complexes and then comparing the positions of the $C\alpha$ atoms of the respective inhibitors (after the 2-Å separation described under Materials and Methods). Encouragingly, for several different combinations of parameter settings, the fittest (top ranked) solution was within 3 Å of the crystallographic solution and, in all cases but two, there were several correct hits ranked in the top 10. The parameter combinations shown in columns 2 and 3 were the most consistent in yielding good hits; these were the values chosen for subsequent docking of native proteins. Of these four, the parameter combination of normal angle $\pm 15^{\circ}$ and J = 1.0 does seem to give slightly better results than the others, with the top-ranked hit resembling the crystallized complex in all three cases. However, when docking using native coordinates, we expected that looser constraints might be necessary in order for surface dots to match and therefore we decided to retain all four parameter combinations to increase the chance of obtaining correct dockings. The results for the antibody-antigen complex were not as good as those of the enzyme-inhibitor complexes. This is in agreement with the prediction of Jackson.²⁷

Docking Native Complexes

Each of the above are separated crystallized complexes. We then turned our attention to predicting the structure of complexes when starting from native component proteins. A recent study of protein–protein complexes gave a list of 31 complexes (18 enzyme–inhibitor, 7 antibody–antigen and 6 "other" complexes) whose structures have been

| TABLE II | . Docking | Bound | Comp | lexes* |
|----------|-----------|-------|------|--------|
|----------|-----------|-------|------|--------|

| Complex (PDB Code) | Normal angle ^a | $J^{ m b}$ | Top rank ^c | Top 10 hits ^d | Total hits ^e | $\mathrm{RMSD^f}$ | Best RMSD ^g |
|--------------------|---------------------------|------------|-----------------------|--------------------------|-------------------------|-------------------|------------------------|
| 1cho | ±30° | 3.0 | 6 | 2 | 4 | 1.47 | 1.47 |
| | $\pm 20^{\circ}$ | 1.5 | 4 | 1 | 5 | 0.77 | 0.77 |
| | $\pm 20^{\circ}$ | 3.0 | 2 | 4 | 5 | 1.05 | 0.93 |
| | $\pm 15^{\circ}$ | 1.0 | 1 | 7 | 9 | 1.69 | 0.70 |
| 2sni | ±30° | 3.0 | 5 | 1 | 1 | 1.63 | 1.63 |
| | $\pm 20^{\circ}$ | 1.5 | 1 | 5 | 8 | 1.60 | 1.32 |
| | $\pm 20^{\circ}$ | 3.0 | 2 | 3 | 6 | 2.99 | 0.76 |
| | $\pm 15^{\circ}$ | 1.0 | 1 | 7 | 10 | 1.40 | 1.36 |
| 3hfl | ±30° | 3.0 | 0 | | | | |
| | $\pm 20^{\circ}$ | 1.5 | 25 | 0 | 2 | 1.63 | 1.63 |
| | $\pm 20^{\circ}$ | 3.0 | 34 | 0 | 4 | 0.94 | 0.94 |
| | $\pm 15^{\circ}$ | 1.0 | 1 | 3 | 5 | 2.00 | 2.00 |

^{*}Each row corresponds to 20 runs of the GA, each producing 5 niches giving 100 solutions per row.

solved by X-ray crystallography to a resolution of ≥ 2.8 Å, and each of which has at least one of its component proteins crystallized separately to a similarly high resolution. In order to test the GA on a wide variety of complexes, we have attempted to dock each of these complexes using whatever native data was available. We also included the well-known barnase–barstar complex (PDB code 1brs), another antibody–antigen complex (PDB code 3hfm) and the β -lactamase–inhibitor complex, which was the subject of a recent docking challenge. To our knowledge, this is the largest docking study of native proteins to date. Table IIIA–C contains details of these 34 test complexes.

For our first attempt at these native dockings, we used the entire surfaces of both proteins for the enzyme—inhibitor complexes. For the antibody—antigen complexes, we used sites of the target antibody as these proteins are very large and the binding sites of Fabs are well known to be in the complementarity determining regions (CDR). As in the bound test, for the antibody—antigen dockings we used only those residues of the target antibody protein which were within 8 Å of the known antigen-binding site. This gave target sites that were still big enough to give the GA plenty of scope for finding incorrect orientations. We also take the view that protein docking should be a pragmatic exercise—all available biochemical information can be used if necessary.

For the "other" complexes, we first attempted to dock using the whole of both proteins. Given the mixed results of this strategy (see below), we later chose the active site for the larger protein of each complex and repeated the GA runs with these sites. These sites were chosen by looking at the known structure of the crystallized complex and selecting any residue of the target protein, which had an atom within 8 Å of a query protein atom. The exceptions

were 3hhr (human growth hormone–receptor complex) and 2btf (β -actin–profilin complex), in which all residues within 6 Å of a query atom were chosen (the shape of these targets indicating that most target atoms are within 8 Å of a query atom). Clearly, this procedure would be impossible when predictively docking two proteins, the structure of whose complex was unknown. However, when two proteins are known to associate, there is frequently some biochemical evidence (e.g., from mutagenesis studies or prediction studies) to indicate the likely position of a binding site residue, so it is reasonable to assume some knowledge of the general region in which binding occurs.

The results of these native dockings are given in Table IVA-D. As suggested by Gabb et al., 16 we have assessed the quality of these dockings by calculating the RMSD of the $C\alpha$ interface atoms after the $C\alpha$ atoms of both proteins of the predicted complex are superposed on those of the crystal complex. 16 (Any atom within 10 Å of the opposite protein is considered an interface atom.) This value is a good measure of the correctness of the predicted complex as it removes the distorting effect that small errors at the interface may have on the position of atoms distant from that interface. For each complex, we also created a "reference structure" by separately superposing the $C\alpha$ atoms of the unbound proteins onto their bound counterparts. We then calculated the RMSD between the $C\alpha$ interface atoms of the reference structure and the crystallized complex. This base RMSD value is a good approximation to the best that could be expected of a rigid-body docking process. We consider a "correct" docking to be one in which the $C\alpha$ interface RMSD minus base RMSD is <4 Å, and dockings are included in Table IV only if this criterion was satisfied. All timings are in CPU minutes for a Silicon Graphics 270-MHz O2 workstation with R12000 processor.

^a180° normal angle is the angle allowed between the surface normals for a permitted match.

^bPenalty multiplier.

^cRank (by fitness score, of 100) of the highest ranked solution which resembled the complex.

^dNumber of complex-resembling hits in the 10 top ranked solutions.

^eNumber of complex-resembling hits (of 100).

^fRoot-mean-square deviation of the inhibitor $C\alpha$ atoms of the most highly ranked predicted complex when its enzyme is superposed on the Protein Data Bank (PDB) complex enzyme.

^gPredicted complex closest to the actual complex. Predicted complexes were deemed to resemble the complex if their RMSD was $\leq 3 \text{ Å}$.

TABLE III. Enzyme-Inhibitor, Antibody-Antigen, and Other Complexes

| .1 .3 .5 .9 | Description A. Enzyme–In Trypsin/pancreatic trypsin inhibitor α-Chymotrypsinogen/pancreatic trypsin inhibitor | PDB code hibitor Comple 1bra 1chg | | No. of residues | PDB code | Res ^a (Å) | No. of residues |
|---|--|---|--|---|---|--|---|
| .1 .3 .5 .9 | A. Enzyme–In Trypsin/pancreatic trypsin inhibitor α-Chymotrypsinogen/pancreatic trypsin inhibitor | hibitor Compl 1bra | exes | residues | code | (\mathbf{A}) | residues |
| .3 .5 .9 .8 | Trypsin/pancreatic trypsin inhibitor α-Chymotrypsinogen/pancreatic trypsin inhibitor | 1bra | | | | | |
| .3 .5 .9 .8 | α -Chymotrypsinogen/pancreatic trypsin inhibitor | | 0.0 | | | | |
| .5 .9 .8 | inhibitor | 1chg | 2.2 | 223 | 1bpi | 1.1 | 51 |
| .9 .8 | TZ 11:1 . A / | - 6 | 2.5 | 245 | 1hpt | 2.3 | 56 |
| .8 | Kallikrein A/pancreatic trypsin inhibitor | 2pka | 2.1 | 232 | 1bpi | 1.1 | 57 |
| | β-Trypsin/pancreatic trypsin inhibitor | 3ptn | 1.7 | 223 | 4pti | 1.5 | 58 |
| | Subtilisin/streptomyces inhibitor | 1sup | 1.6 | 275 | 2ssi | 2.6 | 107 |
| .1 | Subtilisin/chymotrypsin inhibitor | 2sbt | 2.8 | 275 | 2ci2 | 2.0 | 64 |
| .0 | α-Chymotrypsin/Eglin C | 4cha | 1.7 | 245 | $1 \mathrm{acb^b}$ | | 63 |
| .5 | Trypsin/APPI | 1bra | 2.2 | 223 | $1 \mathrm{brc^b}$ | | 56 |
| .8 | α-Chymotrypsin/Ovomucoid | 4cha | 1.7 | 245 | $1 \mathrm{cho^b}$ | | 53 |
| .2 | Subtilisin Carlsberg/Egin C | 1scd | 2.3 | 274 | $1 \mathrm{cse^b}$ | | 63 |
| .0 | Trypsin/CMT-I | 3ptn | 1.7 | 223 | $1 \mathrm{ppe^b}$ | | 29 |
| .1 | Subtilisin Novo/Eglin C | 1sup | 1.6 | 275 | $1 \mathrm{sbn^b}$ | | 63 |
| .4 | Papain/Stefin B | 1ppn | 1.6 | 212 | $1\mathrm{stf}^\mathrm{b}$ | | 98 |
| .3 | Trypsin/BBI | 3ptn | 1.7 | 223 | $1 \mathrm{tab^b}$ | | 36 |
| .8 | Trypsinogen/pancreatic trypsin inhibitor | 1tgt | 1.5 | 225 | $1 \mathrm{tgs^b}$ | | 56 |
| .0 | Thermitase/Eglin C | 1thm | 1.4 | 279 | $2\mathrm{tec^b}$ | | 63 |
| .3 | α-Thrombin/Hirudin | 2hnt | 2.5 | 290 | $4 \mathrm{htc^b}$ | | 61 |
| .7 | Uracil-DNA glycosylase/inhibitor | 1udh | 1.8 | 227 | $1\mathrm{udi}^\mathrm{b}$ | | 83 |
| .0 | Barnase/Barstar | 1a2p | 1.5 | 107 | 1a19 | 2.8 | 89 |
| | B. Antibody–A | Antigen Compl | exes | | | | |
| .1 | Fab D44.1 (a.b-chains)/lysozyme | 1mlb | 2.1 | 432 | 1lza | 1.6 | 129 |
| .8 | | | | | | | 129 |
| .5 | | | 1.0 | | | | 389 |
| .5 | | | | | | | 389 |
| .6 | | | | | | | 58 |
| .8 | | liel ^b | | | | | 85 |
| .7 | | 3hflp | | | | | 129 |
| .0 | Fab HyHel-10(1,h-chains)/lysozyme | 3hfm ^b | | 429 | 1lza | 1.6 | 129 |
| | C. Othe | r Complexes | | | | | |
| .8 | Actin/deoxyribonuclease I | 1atn ^b | | 258 | 3dni | 2.0 | 373 |
| .6 | | | | | | | 161 |
| .0 | | | 16 | | | | 71 |
| .6 | | 2htf ^b | 1.0 | | | 2.0 | 160 |
| .8 | | | | | | | 185 |
| .5 .5 | | | | | | | 103 |
| .7 | β-Lactamase/β-lactamase inhibitory | TEM1 ^c | 1.7 | 288 | BLIP ^c | 2.0 | 165 |
| 8. 8. 9. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. | 3 5 5 6 7 7 9 8 8 8 8 8 8 8 8 8 8 8 9 9 9 9 9 9 | Fab D44.1 (a,b-chains)/lysozyme Fv D1.3 (a,b-chains)/lysozyme Fab NC41 (1,h-chains)/Neuraminidase Fab NC10 (1,h-chains)/Neuraminidase Fab (1,h-chains)/Streptomyces protein G Fab JE142 (1,h-chains)/HPR Fab HyHel-5(1,h-chains)/lysozyme Fab HyHel-10(1,h-chains)/lysozyme C. Othe Actin/deoxyribonuclease I Glycerol kinase/GSF III Subtilisin/subtilisin prosegment β-Actin/profilin Human growth hormone/receptor Methylamine dehydrogenase/Amicyanin β-Lactamase/β-lactamase inhibitory | Fab D44.1 (a,b-chains)/lysozyme 1mlb Fv D1.3 (a,b-chains)/lysozyme 1vfa Fab NC41 (1,h-chains)/Neuraminidase 1nca ^b Fab NC10 (1,h-chains)/Neuraminidase 1nmb ^b Fab (1,h-chains)/Streptomyces protein G 1igc ^b Fab JE142 (1,h-chains)/HPR 1jel ^b Fab HyHel-5(1,h-chains)/lysozyme 3hfl ^b Fab HyHel-10(1,h-chains)/lysozyme 3hfm ^b C. Other Complexes Actin/deoxyribonuclease I 1atn ^b Glycerol kinase/GSF III 1gla ^b Subtilisin/subtilisin prosegment 1sup β -Actin/profilin 2btf ^b Human growth hormone/receptor 3hhr ^b Methylamine dehydrogenase/Amicyanin 2bbk | Fv D1.3 (a,b-chains)/lysozyme 1vfa 1.8 Fab NC41 (1,h-chains)/Neuraminidase 1nca ^b Fab NC10 (1,h-chains)/Neuraminidase 1nmb ^b Fab (1,h-chains)/Streptomyces protein G 1igc ^b Fab JE142 (1,h-chains)/HPR 1jel ^b Fab HyHel-5(1,h-chains)/lysozyme 3hfl ^b Fab HyHel-10(1,h-chains)/lysozyme 3hfm ^b C. Other Complexes Actin/deoxyribonuclease I 1atn ^b Glycerol kinase/GSF III 1gla ^b Subtilisin/subtilisin prosegment 1sup 1.6 β -Actin/profilin 2btf ^b Human growth hormone/receptor 3hhr ^b Methylamine dehydrogenase/Amicyanin 2bbk β -Lactamase/ β -lactamase inhibitory TEM1 ^c 1.7 | Fab D44.1 (a,b-chains)/lysozyme 1mlb 2.1 432 Fv D1.3 (a,b-chains)/lysozyme 1vfa 1.8 223 Fab NC41 (1,h-chains)/Neuraminidase 1ncab 435 Fab NC10 (1,h-chains)/Neuraminidase 1nmbb 388 Fab (1,h-chains)/Streptomyces protein G 1igcb 435 Fab JE142 (1,h-chains)/HPR 1jelb 432 Fab HyHel-5(1,h-chains)/lysozyme 3hflb 427 Fab HyHel-10(1,h-chains)/lysozyme 3hfmb 429 C. Other Complexes Actin/deoxyribonuclease I 1atnb 489 Subtilisin/subtilisin prosegment 1sup 1.6 264 β-Actin/profilin 2btfb 375 Human growth hormone/receptor 3hhrb 393 Methylamine dehydrogenase/Amicyanin 2bbk 489 β-Lactamase/β-lactamase inhibitory TEM1c 1.7 288 | Fab D44.1 (a,b-chains)/lysozyme 1mlb 2.1 432 1lza Fv D1.3 (a,b-chains)/lysozyme 1vfa 1.8 223 1lza Fab NC41 (1,h-chains)/Neuraminidase 1nca ^b 435 7nn9 Fab NC10 (1,h-chains)/Neuraminidase 1nmb ^b 388 7nn9 Fab (1,h-chains)/Streptomyces protein G 1igc ^b 435 1igd Fab JE142 (1,h-chains)/HPR 1jel ^b 432 1poh Fab HyHel-5(1,h-chains)/lysozyme 3hfl ^b 427 1lza Fab HyHel-10(1,h-chains)/lysozyme 3hfm ^b 429 1lza C. Other Complexes C. Other Complexes Actin/deoxyribonuclease I 1atn ^b 258 3dni Glycerol kinase/GSF III 1gla ^b 489 1f3g Subtilisin/subtilisin prosegment 1sup 1.6 264 1spb ^b β-Actin/profilin 2btf ^b 375 1pne Human growth hormone/receptor 3hhr ^b 393 1hgu Methylamine dehydrogenase/Amicyanin 2bbk 489 1aan β-Lactamase/β-lactamase inhibitory TEM1 ^c 1.7 288 BLIP ^c | Fab D44.1 (a,b-chains)/lysozyme 1mlb 2.1 432 1lza 1.6 Fv D1.3 (a,b-chains)/lysozyme 1vfa 1.8 223 1lza 1.6 Fab NC41 (1,h-chains)/Neuraminidase 1ncab 435 7nn9 2.0 Fab NC10 (1,h-chains)/Neuraminidase 1nmbb 388 7nn9 2.0 Fab (1,h-chains)/Streptomyces protein G 1igcb 435 1igd 1.1 Fab JE142 (1,h-chains)/HPR 1jelb 432 1poh 2.0 Fab HyHel-5(1,h-chains)/lysozyme 3hflb 427 1lza 1.6 Fab HyHel-10(1,h-chains)/lysozyme 3hfmb 429 1lza 1.6 C. Other Complexes C. Other Complexes Actin/deoxyribonuclease I 1atnb 489 1f3g 2.1 Subtilisin/subtilisin prosegment 1sup 1.6 264 1spbb 375 1pne 2.0 G-Actin/profilin 2btfb 375 1pne 2.0 Human growth hormone/receptor 3hhrb 393 1hgu 2.5 Methylamine dehydrogenase/Amicyanin 2bbk 489 1aan 2.0 G-Lactamase/β-lactamase inhibitory TEM1c 1.7 288 BLIPc |

^aRes is the resolution in Ångstroms of the crystallized structure.

Enzyme-Inhibitor Complexes

Table IVA shows that the GA performed extremely well on these complexes. In every case, for at least one parameter combination, a complex that was close to the PDB complex was found. This means that, although there are literally millions of ways in which one protein may be oriented with respect to the other, the GA produced a list of 400 such orientations, which always contained at least one (and in most cases many) approximately correct prediction. For 13 of the 19 complexes, correct hits were found for every parameter combination. For 11 of the complexes, at least one good hit was found ranked in the top 5 for at least

one set of parameters. Figure 2a shows the $C\alpha$ trace of the best predicted docking of the Kallikrein A (PDB code 2pka)–pancreatic trypsin inhibitor (PDB code 1bpi) superposed onto the actual complex (PDB code 2kai). The predicted complex is shown in lime green (enzyme) and red (inhibitor) and the actual complex in blue (enzyme) and turquoise (inhibitor).

The two complexes, 1cho and 2sni, which gave similarly high-ranking hits when docked using bound coordinates gave quite different results when docked using native coordinates. The worst top rank for the native 1cho docking was 5, whilst for 2sni the best native docking rank

^bData taken from complex.

The coordinates of TEM-1, BLIP, and the temblip complex were obtained from Professor M.N.G. James.

TABLE IV. Results of Enzyme-Inhibitor, Antibody-Antigen, Other Complex, and Other Complex (Site)

| | | | | Norma | l angle ±2 | 20° J 1.5 | Norma | l angle ± | 5° J 1.0 | Norma | ıl angle ±2 | 20° J 3.0 | Norma | l angle ±3 | 30° J 3.0 | Total |
|----------------------|---------------|--------------|-------------------|----------------|-------------|-----------|--------------|------------|---------------|--------------|--------------|-----------|-------------------|----------------|----------------|-------------|
| Complex ^a | $Tdots^{b}$ | $Qdots^c$ | Base ^d | Ranke | $RMSD^f$ | Nhitsg | Ranke | $RMSD^f$ | Nhitsg | Ranke | $RMSD^f$ | Nhitsg | Rank ^e | $RMSD^f$ | Nhitsg | timeh |
| | | | | | | A | . Enzym | e/Inhibito | Results | | | | | | | |
| 1brb | 8008 | 2768 | 0.38 | 4 | 1.40 | 5 | 13 | 3.52 | 7 | 3 | 2.76 | 9 | 5 | 4.08 | 11 | 380 |
| 1cgi | 8941 | 2705 | 1.48 | 83 | 5.14 | 2 | None | | | 7 | 4.24 | 4 | 34 | 5.04 | 8 | 360 |
| 2kai | 9095 | 2768 | 1.00 | 6 | 1.23 | 13 | 9 | 3.78 | 7 | 48 | 4.26 | 5 | 4 | 4.39 | 8 | 380 |
| 2ptc | 8184 | 2670 | 0.74 | 13 | 3.15 | 4 | 17 | 4.70 | 4 | 2 | 3.63 | 3 | 1 | 4.38 | 6 | 360 |
| 2sic | 8348 | 4547 | 0.38 | 70 | 4.00 | 1 | 62 | 2.87 | 1 | 2 | 2.65 | 9 | 25 | 3.91 | 5 | 560 |
| 2sni | 8694 | 2976 | 0.85 | 50 | 2.91 | 3 | 25 | 3.89 | 2 | 14 | 4.08 | 5 | 51 | 2.05 | 2 | 400 |
| 1acb | 8995 | 2855 | 0.59 | None | 0.41 | 10 | None | 0.41 | 20 | None | 0.41 | - 4 | 2 | 2.32 | 1 | 380 |
| 1brc | 8008 | 2287 | 0.39 | 1 | 2.41 | 13 | 1 | 2.41 | 20 | 1 | 2.41 | 14 | 28 | 2.63 | 5 | 280 |
| 1cho | 8995 | 2573 | 0.33 | 1 | 1.87 | 13 | 2 | 2.06 | 7 | 5 | 2.60 | 2 | 1 | 1.79 | 9 | 300 |
| 1cse | 8961 | 2912 | 0.29 | 37 | 2.28 | 2 | 25 | 3.89 | $\frac{2}{7}$ | 11 | 2.04 | 5 | $\frac{36}{2}$ | 2.40 | 8 | 360 |
| 1ppe | 8184 | 1581 2903 | 0.69 0.29 | 1 | 0.97 | 13 12 | 36 1 | 0.77 | 9 | 1 1 | 1.00 3.80 | 13 16 | 4 | $0.96 \\ 2.49$ | 12 14 | 200 380 |
| 1sbn 1stf | 8348 8083 | 4592 | 0.29 0.27 | $\frac{4}{56}$ | 3.58 2.01 | 2 | None | 4.25 | 9 | 18 | 2.80 | 3 | 4 37 | 3.00 | 14 | 600 |
| 1tab | 8184 | 2043 | 0.27 | 13 | 4.36 | 1 | None | | | None | 2.00 | Э | None | 5.00 | 1 | 260 |
| 1tgs | 8547 | 2729 | 0.67 | None | 4.00 | 1 | 56 | 1.89 | 1 | 31 | 1.97 | 1 | None | | | 360 |
| 2tec | 8403 | 2965 | 0.19 | None | | | 12 | 0.79 | 1 | 38 | 1.58 | 2 | 18 | 1.27 | 4 | 360 |
| 4htc | 11179 | 2916 | 0.16 | 33 | 2.82 | 1 | 7 | 2.55 | 2 | 15 | 3.13 | 2 | 2 | 1.91 | 2 | 380 |
| 1udi | 9649 | 3715 | 0.37 | 6 | 3.12 | 3 | 29 | 1.68 | 1 | 9 | 2.98 | 2 | 13 | 2.23 | 3 | 460 |
| 1brs | 4681 | 4061 | 0.47 | 36 | 3.94 | 2 | 16 | 3.25 | 1 | 28 | 3.05 | 1 | 1 | 3.14 | $^{\circ}_{2}$ | 520 |
| | | | | | | В | Antibod | ly–Antige | n Roculte | | | | | | | |
| | 2222 | * 000 | | | 0.40 | | | iy—Minge | Tresuits | | 0.40 | _ | | 0.4= | | |
| 1mlc | 3382 | 5032 | 0.88 | 74 | 3.19 | 1 | None | | | 18 | 3.42 | 1 | 55 | 3.17 | 2 | 660 |
| 1vfb | 3974 | 5032 | 1.12 | None | | | None | | | None | | | None | 1 10 | 1 | 660 |
| 1nca | 4829 | 14207 | 0.38 0.22 | None | | | None | | | None | | | 74 | 1.19 | 1 | 2000 |
| 1nmb | 4443 6110 | 14207 2887 | 0.22 0.74 | None 19 | 4.28 | 4 | None 44 | 3.45 | 1 | None 31 | 2.98 | 1 | None 20 | 4.60 | 4 | 1920 400 |
| 1igc 1jel | 4193 | 3609 | 0.74 0.27 | None | 4.20 | 4 | None | 5.40 | 1 | None | 2.90 | 1 | 100 | 3.58 | 1 | 500 |
| 3hfl | 3172 | 5032 | 0.42 | 76 | 2.64 | 2 | None | | | 70 | 2.76 | 2 | 83 | 2.50 | 1 | 660 |
| 3hfm | 3917 | 5032 | 0.44 | 67 | 3.63 | 1 | None | | | None | 2.10 | | 50 | 3.38 | 1 | 660 |
| | | | | | | | | her Comp | lov Rocul | | | | | | _ | |
| | | | | | | 0.1 | | ner Comp | iex ræsui | | | | | | | |
| 1atn | 14931 | 9620 | 0.33 | None | | | None | | | None | | | None | | | 1340 |
| 1gla | 17669 | 5527 | 0.49 | None | | | None | | | None | | | None | | _ | 600 |
| 1spb | 8348 | 3495 | 0.35 | None | | | None | | | None | | | 43 | 3.00 | 1 | 420 |
| 2btf | 15173 | 5450 | 0.29 | None | | | None | | | None | | | None | 0.50 | | 800 |
| 3hhr | 16045 | 10170 | 2.92 | None | | | None | | | None | | | 91 | 6.78 | 1 | 1800 |
| 1mda | 20445 9803 | 4127 6630 | 2.69 0.88 | None 66 | 3.10 | 1 | None None | | | None None | | | None None | | | 640 780 |
| temblip | 9803 | 0030 | 0.88 | 66 | 3.10 | 1 | | | | | | | None | | | 180 |
| | | | | | | D. (| Other Co | mplex (Si | te) Result | S | | | | | | |
| 1atn | 3747 | 9620 | 0.33 | 50 | 3.97 | 1 | 66 | 2.06 | 2 | 48 | 1.35 | 4 | 90 | 3.98 | 1 | 1340 |
| 1gla | 1672 | 5527 | 0.49 | None | | | None | | | None | | | 40 | 4.35 | 2 | 600 |
| 1spb | 3495 | 3913 | 0.35 | None | | | None | | | 40 | 1.12 | 1 | 73 | 1.42 | 1 | 440 |
| 2btf | 3446 | 5450 | 0.29 | 20 | 4.26 | 1 | 33 | 2.85 | 2 | None | | | 16 | 1.90 | 2 | 580 |
| 3hhr | 6687 | 10170 | 2.92 | None | | | 35 | 5.80 | 1 | None | | | 56 | 0.90 | 1 | 1800 |
| 1mda | 5796 | 4127 | 2.69 | 12 | 5.00 | 6 | 21 | 6.44 | 4 | 10 | 4.95 | 6 | 1 | 5.05 | 18 | 640 |
| temblip | 6630 | 6469 | 0.88 | 10 | 2.16 | 3 | 53 | 3.08 | 1 | 8 | 3.51 | 6 | 8 | 2.81 | 4 | 780 |

^aComplex is the Protein Data Bank (PDB) code of the complex.

was 14. However, this could be explained by the fact that the inhibitor for the native 1cho docking was taken from the complex, whereas for 2sni, both proteins were native. The majority of the incorrect orientations predicted by the GA, and certainly most of the high-ranking incorrect predictions, did position the inhibitor in the active site of

the enzyme, with the error being in the orientation of the inhibitor within the site. This reflects the more deeply concave nature of the enzyme active sites compared with the remainder of the enzyme surface.

The run times given are the total times for 20 runs of the GA, producing 100 solutions. The time needed to generate

 $^{{}^{\}rm b}Number$ of surface dots generated for the target protein.

 $^{^{\}mathrm{c}}$ Number of surface dots generated for the query protein.

^dRoot-mean-square deviation (in Å) obtained by superposing the $C\alpha$ atoms of each unbound component onto the corresponding bound protein and then calculating the RMSD between interface atoms of this reference structure and the crystallized complex.

eRank (by fitness score, of 100) of the highest ranked solution that resembled the complex.

^fRoot-mean-square deviation of interface $C\alpha$ atoms.

gTotal number (out of 100) of complex-resembling hits found.

^hTotal time (CPU mins) is the time taken for 20 runs giving 100 solutions.

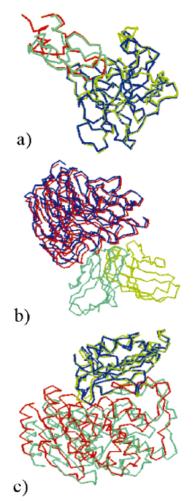


Fig. 2. Docking native complexes. The $C\alpha$ traces of the predicted complex with the lowest RMSD is shown superposed onto the crystallized complex. a: 2kai. The predicted enzyme and inhibitor are shown in lime green and red with the crystallized enzyme and inhibitor in blue and turquoise respectively. b:1nca. Only part of the Fab is shown, with lime green for the light chain and turquoise for the heavy chain. This is the same for both crystallized and predicted complex as the docked Fab is shown in red and the actual in blue. c: temblip. The predicted enzyme and inhibitor are shown in lime green and red, with the crystallized enzyme and inhibitor in blue and turquoise, respectively.

400 solutions varied between approximately 17 h (for the smallest complex, 1tab) and 40 h (for 1stf, the largest complex). However, as the fitness score produced by the GA was also a ranking of the solution, no subsequent ranking or screening was necessary. The run times increased, particularly with the size of the query protein. This was to be expected, as this was the protein upon which most computation was carried out. Thus docking the barnase—barstar complex (1brs) required a similar time to that required by papain—stefin B (1stf) because the query proteins had a similar number of surface dots, although papain had nearly twice as many dots as barnase.

Antibody-Antigen Complexes

For each of these complexes, the query protein was docked against a site within the CDR of the antibody

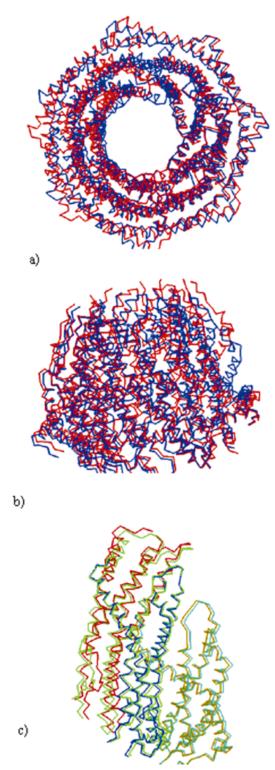


Fig. 3. Reassembling a heptamer. Protein Data Bank complex 1avo reassembled by repeatedly adding a docked subunit. **a:** End-on view of the $C\alpha$ chains of the helical assembly, actual complex in blue with predicted superposed in red. **b:** Side-on view of a. **c:** Small errors in docking the first pair of subunits mean that subsequent subunits become further out of step. This is just the first three subunits; the yellow chain is the first target, the blue is the second, and the red would be the target for the fourth subunit (not shown). The actual complex is in turquoise.

(selected as described above). Even so, the dockings still generally involved more surface dots than for the enzyme—inhibitor cases described above and thus provided a more severe test, the results of which are given in Table IVB. The bound docking tests suggested that the GA did not perform quite as well on antibody—antigen complexes, and the native test confirmed this. Nevertheless, in 6 of 8 cases, the GA did find at least one hit in the top 400, the two exceptions being the Fab—lysozyme complex 1vfb and the Fab—neuraminidase complex 1nmb. In fact, in the case of 1nmb, which (with 1nca) has the largest query protein of any complex considered (neuraminidase has 389 residues), hits were found that somewhat resembled the crystallized complex but whose RMSD (of the order of 7 Å) were too great too allow them to be considered correct.

The complexity of the docking was also reflected in the longer run times. The run time is generally dependent on the size of the query protein. Hence, all the runs with lysozyme (which has 129 residues) as the query took about half an h for one run and thus to obtain 400 solutions took about 40 h. Neuraminidase is a very large query protein (389 residues) and the two neuraminidase complexes took about 120 h for 400 solutions. Figure 2b shows the $C\alpha$ trace of the predicted Fab-neuraminidase (PDB codes 1nca, 7nn9) complex, with the lowest RMSD, superposed on the actual 1nca complex. For clarity, only the part of the Fab that contacts the neuraminidase is shown, with its light chain in lime green and its heavy chain in turquoise. This is the same for the predicted and actual complexes, since the Fab coordinates used in docking were taken from the complex. The predicted neuraminidase is shown in red and the complexed in blue.

Other Complexes

These complexes provided a very stiff test indeed for the GA. To the best of our knowledge, most have not previously been used in theoretical docking studies. Exceptions are the TEM-1/BLIP complex, which was the subject of a docking challenge,7 and the human growth hormonegrowth hormone receptor complex (3hhr), which has recently been studied. 45 Although human growth hormone is itself a complex, consisting of two chains that are identical in sequence, but different in conformation, we have followed Betts and Sternberg⁸ in treating the hormone as a single preassembled unit; this we have attempted to dock with its receptor. All the complexes are very large, and the dockings involved many surface dots. Another particular problem was that, in some cases, the conformation of the native protein had some significant differences to that of the complex. For example, the RMSD between native methylamine dehydrogenase (2bbk) and that in the 1mda complex with amicyanin is 6 Å—considering just those residues 4 Å from the interface gives an RMSD of 2.8 Å. This clearly poses a problem for a rigid body docking procedure.

In view of these difficulties, the GA performed better than might have been expected, even when docking entire proteins (Table IVC). For three of the complexes—3hhr, 1spb (subtilisin—subtilisin prosegment complex), and TEM1-BLIP—it found a correct docking, although in each

case it was only 1 from 400 possible solutions. However, when attention was restricted to docking a site of one protein against the whole of the other protein, its performance was, as was hoped, much improved (Table IVD). The GA found at least one hit for each complex. For four of the complexes-1atn, 1gla, 1mda, and TEM1-BLIP-it found several hits for most of the parameter combinations, while for two complexes-1gla and 1spb-only one hit was found. It was pleasing to find that the GA was able to find solutions ranked in the top 10 for the TEM-1/BLIP complex, as our previous attempts (using clique-detection methods) had completely failed for this complex.²⁸ Figure 2c shows the predicted TEM-1/BLI P complex with the lowest RMSD, superposed on the actual complex. A direct comparison with the docking challenge result is difficult as we are docking with the benefit of hindsight, whereas the challenge participants did not know the answer. However, although all the participants ranked near-native complexes top in their submissions, some did use their judgment to "overrule" the ranking of their scoring procedure, 25 so the fact that our best hit was ranked 8 by the GA does not mean that we would have failed the docking challenge. However, in this example, it is notable that the group of Abagyan and Totrov and that of Sternberg and Jackson scored the correct solution top in their respective ranking systems.7

Performance of the GA

The GA was run with four combinations of the normal angle/penalty multiplier parameters. Although there was no consistently best performer for the enzyme-inhibitor complexes, overall it did seem that the 180°± 30° with penalty multiplier J = 3.0 combination was the most satisfactory. Table V, which summarizes the results for all complexes for this parameter combination, shows that for 30 of the 34 complexes, the GA found at least one solution ranked in the top 100, when these parameters were applied. For 21 of these cases, more than one good solution was found, and for 15 cases, a good solution was found ranked in the top 20. In 6 cases, this parameter combination produced a docking that resembled the complex which was ranked one or two. However, using all four parameter combinations, at least one good solution among 400 was found for all but two of the test complexes, although this was at the expense of having more false hits.

We have been quite generous in our definition of what constituted a hit as we wished to assess the utility of the GA in docking as wide a range of complexes as possible. The interface RMSD of our "hits" ranged from 0.77 Å (enzyme–inhibitor complex, 2tec) to 6.78 Å (human growth hormone–receptor complex, 3hhr), although in the case of 3hhr, the base interface RMSD was 2.92 Å. There are, however, different "grades" of nonhit. For example, the fittest docking of the enzyme–inhibitor complex 2sic with an RMSD of <4 Å is ranked 25 (Table V). In fact, 8 of the top 10 fittest solutions had RMSD values of <5 Å. Because we chose a cutoff RMSD value of 4 Å (relaxed by the base RMSD), none of these were classed as hits although they clearly resembled the crystallized complex more closely than a prediction with RMSD of 20 Å.

TABLE V. Docking All Complexes Using Normal $\pm 30^{\circ}$ and J 3.0

| Complex Rank RMSD Nhits 1brb 5 4.08 11 1cgi 34 5.04 8 2kai 4 4.39 8 2ptc 1 4.38 6 2sic 25 3.91 5 2sni 51 2.05 2 1acb 2 2.32 1 1brc 28 2.63 5 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1 1.27 4 4htc 2 1.91 2 | | | | | |
|---|----------------------|------|------|-------|--|
| 1cgi 34 5.04 8 2kai 4 4.39 8 2ptc 1 4.38 6 2sic 25 3.91 5 2sni 51 2.05 2 1acb 2 2.32 1 1brc 28 2.63 5 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 2tec 18 1.27 4 4htc 2 1.91 2 | Complex | Rank | RMSD | Nhits | |
| 2kai 4 4.39 8 2ptc 1 4.38 6 2sic 25 3.91 5 2sni 51 2.05 2 1acb 2 2.32 1 1brc 28 2.63 5 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 2tec 18 1.27 4 4htc 2 1.91 2 | 1brb | 5 | 4.08 | 11 | |
| 2ptc 1 4.38 6 2sic 25 3.91 5 2sni 51 2.05 2 1acb 2 2.32 1 1brc 28 2.63 5 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 1cgi | 34 | 5.04 | 8 | |
| 2sic 25 3.91 5 2sni 51 2.05 2 1acb 2 2.32 1 1brc 28 2.63 5 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | | 4 | 4.39 | 8 | |
| 2sic 25 3.91 5 2sni 51 2.05 2 1acb 2 2.32 1 1brc 28 2.63 5 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 2ptc | 1 | 4.38 | 6 | |
| 1acb 2 2.32 1 1brc 28 2.63 5 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | | 25 | 3.91 | 5 | |
| 1brc 28 2.63 5 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 2sni | 51 | 2.05 | 2 | |
| 1cho 1 1.79 9 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 1acb | 2 | 2.32 | 1 | |
| 1cse 36 2.40 8 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 1brc | 28 | 2.63 | 5 | |
| 1ppe 2 0.96 12 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 1cho | 1 | 1.79 | 9 | |
| 1sbn 4 2.49 14 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 1cse | 36 | 2.40 | 8 | |
| 1stf 37 3.00 1 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 1ppe | 2 | 0.96 | 12 | |
| 1tab None 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 1sbn | 4 | 2.49 | 14 | |
| 1tgs None 2tec 18 1.27 4 4htc 2 1.91 2 | 1stf | 37 | 3.00 | 1 | |
| 2tec 18 1.27 4 4htc 2 1.91 2 | 1tab | None | | | |
| 2tec 18 1.27 4 4htc 2 1.91 2 | 1tgs | None | | | |
| | | 18 | 1.27 | 4 | |
| | 4htc | 2 | 1.91 | 2 | |
| 1udi 13 2.23 3 | 1udi | 13 | 2.23 | 3 | |
| 1brs 1 3.14 2 | 1brs | 1 | 3.14 | 2 | |
| 1mlc^{a} 55 3.17 2 | 1 m l c a | 55 | 3.17 | 2 | |
| 1vfb ^a None | $1vfb^{a}$ | None | | | |
| 1nca ^a 74 1.19 1 | 1nca ^a | 74 | 1.19 | 1 | |
| 1nmb ^a None | $1 \mathrm{nmb^a}$ | None | | | |
| $1igc^{a}$ 20 4.60 4 | | 20 | 4.60 | 4 | |
| 1jel ^a 100 3.58 1 | 1jel ^a | 100 | 3.58 | 1 | |
| $3hfl^a$ 83 2.50 1 | $3\mathrm{hfl^a}$ | 83 | 2.50 | 1 | |
| 3hfm ^a 50 3.38 1 | $3 \mathrm{hfm^a}$ | 50 | 3.38 | 1 | |
| 1atn ^a 90 3.98 1 | 1atn ^a | 90 | 3.98 | 1 | |
| 1gla ^a 40 4.35 2 | 1gla ^a | 40 | 4.35 | 2 | |
| 1spb ^a 73 1.42 1 | | 73 | 1.42 | 1 | |
| 2btf ^a 16 1.90 2 | | 16 | 1.90 | 2 | |
| 3hhr 91 6.78 1 | 3hhr | 91 | 6.78 | 1 | |
| 1mda ^a 1 5.05 18 | 1 md a^{a} | 1 | 5.05 | 18 | |
| temblip ^a 8 2.81 4 | temblip ^a | 8 | | 4 | |

^aIndicates that only part of the target protein was used.

The GA performed well in comparison with two other recent large docking studies that have used unbound proteins. In their study, Ritchie and Kemp²⁴ docked 18 enzyme-inhibitor and antibody-antigen complexes and found solutions ranking in the top 100 in only 4 cases, when their dockings were constrained to search only the receptor-binding site. They required some knowledge of the ligand-binding site to generate more highly ranked solutions. However, they successfully docked the Fab fragment-antigen complex 1vfb, which the GA was unable to dock using any of our parameter combinations. Our results are also comparable to those of Norel et al., 9 who docked 19 unbound complexes. In 15 cases, they found a solution in the top 100, and 5 of these were in the top 10. However, their test cases only involved 8 different complexes—the multiple results came from using the same proteins crystallized to different resolution or in different crystal forms. Thus, although large, their test set was not as extensive as ours. In general, the GA is somewhat slower than comparable docking methods, with one hundred orientations taking 3-33 h. For example, the methods of Norel et al.,9 and Ritchie and Kemp²⁴ took only a few

minutes and about 2 h, respectively. The "correct" hits produced by the GA also tend to have slightly worse RMSD than those of these other groups.

Docking Subunits

We are also interested in docking protein subunits to form oligomers, as some proteins, such as bacterial toxins, are monomeric in solution but associate to form oligomeric pores (e.g., aerolysin, hemolysin E). The intersubunit interactions that occur when dimers (or other such complexes) form are thought to be largely driven by hydrophobic forces. 46 As our GA modeled these interactions (requiring non H-bonding atoms to match with similar), we wished to see how well it performed in this context. A difficulty with this kind of docking is that subunits are not often able to be crystallized separately from the complete protein. Thus, docking tests are usually performed using bound coordinates. If the GA were ever to be used to predict the structure of an oligomer, the minimum test it must pass is to reassemble crystallized oligomers. This problem has been studied by Cummings et al.,47 who reassembled diubiquitin from the subunits of the crystallized dimer and also by Hendrix et al., 45 who, as part of a three-protein docking of human growth hormone and its receptor (which is composed of two monomers, each of which interacts with the hormone in a different fashion), reassembled the entire complex using the bound coordinates. We successfully assembled this complex (PDB code 3hhr, Table IVC,D) by treating the receptor as a single protein (a dimer). To the best of our knowledge, the reassembly of a unit larger than a trimer has not yet been attempted.

We have tested this use of the GA on three different proteins, HIV-1 protease (PDB code 4hpv), proteasome activator reg-alpha (PDB code 1avo) and diubuquitin (PDB code 1aar). HIV-1 protease is a dimer with two identical chains, A and B, each of 99 residues. We separated the PDB file into two files and docked the two chains, using A as the target. The proteasome activator is a heptamer with 14 chains, 7 pairs that form a circular helical assembly with a central hole. Each subunit consists of two chains of 59 and 139 residues, respectively. In this case, we docked two identical copies of the A,B-chain subunit. This is a slightly more stringent test than that imposed on 4hpv, as the RMSD between the A,B-chain subunit and the adjacent C,D-chain subunit is 0.2 Å. Diubiquitin is a dimer consisting of two distinct copies of the ubiquitin monomer; the $C\alpha$ RMSD between the two chains is 1.4 Å. We docked two identical copies of the A chain which provides a more severe test than docking the A chain against the B chain.

The results, which were very encouraging, are shown in Table VI. For the 4hpv dimer, the top 15 solutions for normal angle $\pm 20^\circ$ and J=1.5 were all within 2.6 Å of the actual complex. The 1aar and 1avo results, whilst not as outstanding as 4hpv, were still very good with each parameter set providing multiple hits within the top ten ranked solutions. This time, taking all three complexes into consideration, the parameter combination of normal angle $\pm 20^\circ$ and J=1.5 did seem significantly better than the other three since a correct hit was ranked top for every

TABLE VI. Docking Bound Subunits*

| Complex (PDB code) | Normal angle ^a | $J^{ m b}$ | Top Rank ^c | Top 10 hits ^d | Total hits ^e | $\mathrm{RMSD^f}$ | ${ m Best} \ { m RMSD}^{ m g}$ |
|--------------------|---------------------------|------------|-----------------------|--------------------------|-------------------------|-------------------|--------------------------------|
| 4hpv | ±30° | 3.0 | 1 | 10 | 18 | 1.99 | 1.52 |
| r | ±20° | 1.5 | 1 | 10 | 20 | 2.00 | 0.98 |
| | $\pm 20^{\circ}$ | 3.0 | 1 | 10 | 13 | 1.86 | 1.72 |
| | $\pm 15^{\circ}$ | 1.0 | 1 | 10 | 27 | 2.79 | 1.38 |
| 1avo | ±30° | 3.0 | 4 | 4 | 7 | 2.31 | 1.27 |
| | $\pm 20^{\circ}$ | 1.5 | 1 | 4 | 6 | 1.42 | 1.42 |
| | $\pm 20^{\circ}$ | 3.0 | 2 | 2 | 3 | 3.53 | 3.53 |
| | $\pm 15^{\circ}$ | 1.0 | 4 | 2 | 6 | 1.81 | 1.81 |
| 1aar | ±30° | 3.0 | 4 | 3 | 5 | 2.66 | 2.47 |
| | $\pm 20^{\circ}$ | 1.5 | 1 | 5 | 8 | 2.33 | 2.17 |
| | $\pm 20^{\circ}$ | 3.0 | 1 | 3 | 4 | 2.32 | 2.32 |
| | $\pm 15^{\circ}$ | 1.0 | 2 | 6 | 7 | 1.92 | 1.87 |

^{*}Each row corresponds to 20 runs of the GA, each producing 5 niches giving 100 solutions per row.

complex. However, the docking was done using bound coordinates and we anticipate that native docking might again require looser angle matching constraints.

When attempting to predict the structure of an oligomer, one needs to assemble multiple copies of a subunit. We have done this for the proteasome activator reg-alpha, 1avo. Figure 3a,b shows views of a heptamer, based on the predicted 1avo dimer with the lowest RMSD to the actual dimer, superposed onto the actual heptamer. Naturally, the predicted assembly becomes slightly further out of step with the crystallized complex with each additional subunit. Figure 3c shows just the first three docked subunits. Even so the overall RMSD between all 1,400 $C\alpha$ atoms of our assembly and the crystallized complex is only 4.2 Å.

The case of 1avo illustrates the lack of even-handedness of the treatment of the query and target proteins. As both are the same, we anticipated that the GA would produce a similar number of dockings with the query bound "before" as "after" the target (Fig. 4a). In practice, however, most correct solutions (and all the correct solutions which rank highly) have the query after the target (in position 1, see Fig. 4a). The reason for this seemed to be that there was a helix (residues 1-31), which stuck out from the monomer (Fig. 4b). This helix was "thin" (had few interior points defined) in the target and so when the GA approached position 1 this did not cause a clash with query dots because the query has no interior points. However, when the GA approached position 2 and overlap of the query helix with the target interior occurred, this caused a penalized clash (Fig. 4c). This type of situation may be a reason for the failure of the GA in the unbound cases where few or no solutions were found.

The 1avo assembly also illustrates a situation in which the GA may be of immediate practical use. When a circular assembly (e.g., a trans-membrane pore) is expected to be composed of a number of subunits, a further constraint is imposed on the docking by the fact that when a number (which may be known) of the subunits are docked together, the last must also dock with the first. From a list of 100 dockings produced by the GA, only a few, if any, will satisfy this condition.

Diubiquitin is unusual, in that the structure of the monomer (ubiquitin) has also been determined alone. As a final test, we also attempted to form diubiquitin by docking two copies of ubiquitin. This was also attempted by Cummings et al.,47 who reported success when they used only part of the monomer as their docking target. They also found it necessary to delete the C-terminal residue Gly 76 and to truncate the flexible residue Arg 42 by deleting all atoms beyond the CB. They give biochemical justifications for all their modifications. Our results proved very similar to theirs. The GA gave no correct hits when the entire surface of the monomer was used for both query and target. However, when the target protein was restricted to only those residues which are within 8 Å of the other monomer (in the crystallized dimer) and the same deletion of Gly 76 and alteration of Arg 42 performed, the GA found 6 correct hits using the parameter combination of normal angle $\pm 30^{\circ}$ and J=3. The fittest correct hit (with an interface RMSD of 3.9 Å to the crystal dimer) was ranked.4

CONCLUSIONS

We have developed a GA for protein-protein docking, based on matching complementary Connolly surfaces. We have tested the GA first on three complexes using bound coordinates and then on 34 complexes (some very large) using unbound coordinates and it has performed very well.

^a180° normal angle is the angle allowed between the surface normals for a permitted match.

^bPenalty multiplier.

^cRank (by fitness score, of 100) of the highest ranked solution which resembled the complex.

^dNumber of complex-resembling hits in the 10 top ranked solutions.

^eNumber of complex-resembling hits (of 100).

 $^{^{}f}$ Root-mean-square deviation of the query $C\alpha$ atoms of the predicted complex when the target monomer is superposed upon the monomer of the crystallized dimer.

 $^{^{\}rm g}$ Predicted complex closest to the actual complex. Predicted complexes were deemed to resemble the complex if this RMSD was $<4~{\rm \AA}$.

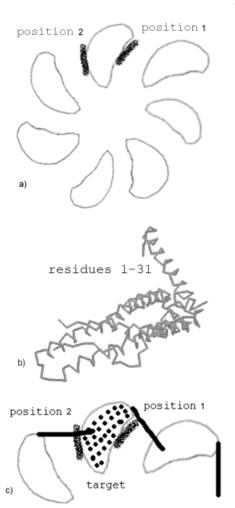


Fig. 4. The GA prefers one of two alternate binding sites for 1avo The two binding sites are shown by chalk lines at positions 1 and 2 of the target monomer. **a:** As 1avo is a heptamer, the query protein will bind in position 1 and position 2. However, almost all correct dockings found by the GA were in position 1. **b:** 1avo monomer showing residues 1–31 protruding. **c:** The target protein has interior points defined. If the query helix (black line) penetrates the target (position 2), a penalized clash with interior points occurs. If the target helix penetrates the query (position 1) no such clash occurs. Although no such clash occurs in the actual binding of the two monomers, this clash drives the GA away from the solution at position 2.

When proteins dock, many factors have an influence. We have modeled only two, the surface shape and the "chemical shape." Even so, these have been sufficient, in most cases, to find orientations near to the crystallized complex. We have established a set of parameters for which the GA found solutions ranked in the top 100 for 30 of the 34 complexes. The GA has also been used to dock subunits, including successfully reassembling a heptamer from bound components.

A great strength of the GA is that the solutions produced are already ranked which eliminates the need for a further screening/ranking step in the docking process. Whilst it is not true that the fittest solution was necessarily correct, a list of 100 putative orientations, of which at least one is probably close to the crystallographic complex, is a very good start, although there is still room for improvement.

The fitness function at present is very simple. We intend to try to enhance it by including some electrostatic elements and also by weighting some features more heavily than others. For example, in antibody–antigen interactions, tyrosine residues represent over a quarter of the total interaction energy donated by the antibody.²⁷ Therefore, we might choose to weight interactions involving tyrosines accordingly, just for antibody–antigen docking. Frequently, when docking, some feature of the binding site may be known. For example, mutagenesis studies may implicate a particular residue in binding. We intend to modify the GA so that such information may be included if available.

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