

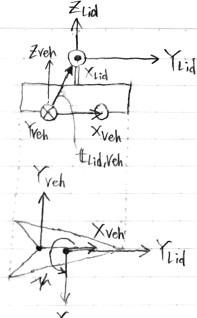
LIDAR-Data Accumulation Strategy

1. INTRODUCTION

- +-- Camera based: Dense information / Needs multiple rides
- +-- LIDAR based
 - +-- Features: Can't provide stable information / Needs multiple rides
 - +-- Intensity: Less affected by environment changes / Single ride is sufficient

2. ONE MAP FRAME GENERATION

Transition from Lidar coordinate \rightarrow to Vehicle coordinate

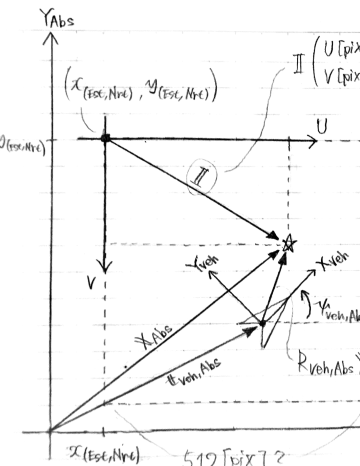


$$\mathbf{X}_{Veh} = \mathbf{R}_{Lid,Veh} \mathbf{X}_{Lid} + \mathbf{t}_{Lid,Veh}$$

$$= \begin{bmatrix} \cos(-\gamma_{Lid,Veh}) & \sin(-\gamma_{Lid,Veh}) & 0 \\ -\sin(-\gamma_{Lid,Veh}) & \cos(-\gamma_{Lid,Veh}) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} \cos \gamma_{Lid,Veh} & -\sin \gamma_{Lid,Veh} & 0 \\ \sin \gamma_{Lid,Veh} & \cos \gamma_{Lid,Veh} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{matrix} \uparrow \\ \uparrow \\ \uparrow \end{matrix} \begin{matrix} \theta = 0 \\ \phi = 0 \\ \phi = 0 \end{matrix}$$

Transition from Vehicle coordinate \rightarrow to Absolute (World) coordinate



$$\mathbf{X}_{Abs} = \mathbf{R}_{Veh,Abs} \mathbf{X}_{Veh} + \mathbf{t}_{Veh,Abs}$$

$$= \begin{bmatrix} \cos(-\gamma_{Veh,Abs}) & \sin(-\gamma_{Veh,Abs}) & 0 \\ -\sin(-\gamma_{Veh,Abs}) & \cos(-\gamma_{Veh,Abs}) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \gamma_{Veh,Abs} & -\sin \gamma_{Veh,Abs} & 0 \\ \sin \gamma_{Veh,Abs} & \cos \gamma_{Veh,Abs} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

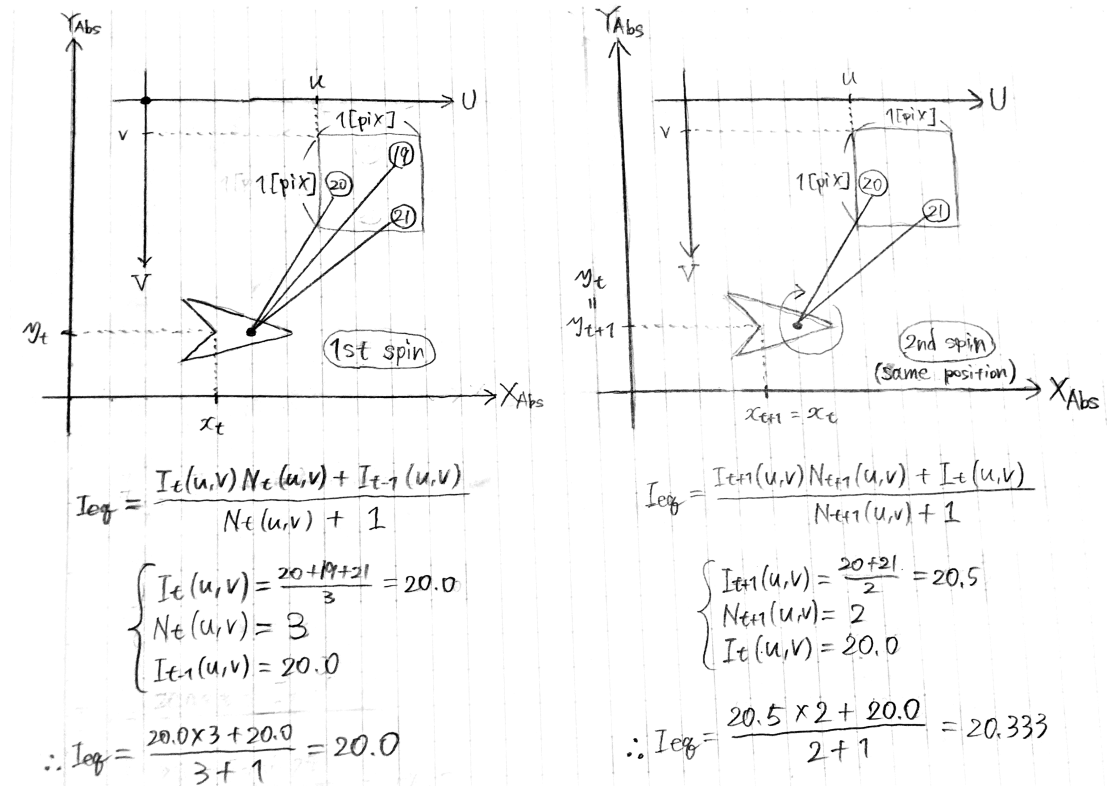
$$\Pi \left(\begin{matrix} U [pix] \\ V [pix] \end{matrix} \right) = \begin{pmatrix} \text{round} \left(\frac{x_{Abs} - x_{(Est, Nire)} [m]}{\text{Resolution} [m/pix]} \right) \\ \text{round} \left(\frac{y_{(Est, Nire)} - y_{Abs} [m]}{\text{Resolution} [m/pix]} \right) \end{pmatrix}$$

512 [pix] ?

Q: Is the max value of the Image domain (U and V) 512[pix]?

The equation of each pixel's intensity level $I_{eq}(u, v)$ in same position is;

$$I_{eq}(u, v) = \frac{I_{new}(u, v) * N(u, v) + I_{old}(u, v)}{N(u, v) + 1}$$



It weights every new value $I_{new}(u, v)$ by the number of irradiations $N(u, v)$, which means considering new value $I_{new}(u, v)$ is more trustful than old value $I_{old}(u, v)$. If the equation took the average of the intensity levels, the final value $I_{eq}(u, v)$ would be 20.2 (not 20.333).

Q: What does “the defference between the pixel values” mean? > “An intuitive solution is to calculate the averaged intensity value based on the number of irradiations $N(u, v)$. This solution doesn't take into account *the difference between the pixel values.*”

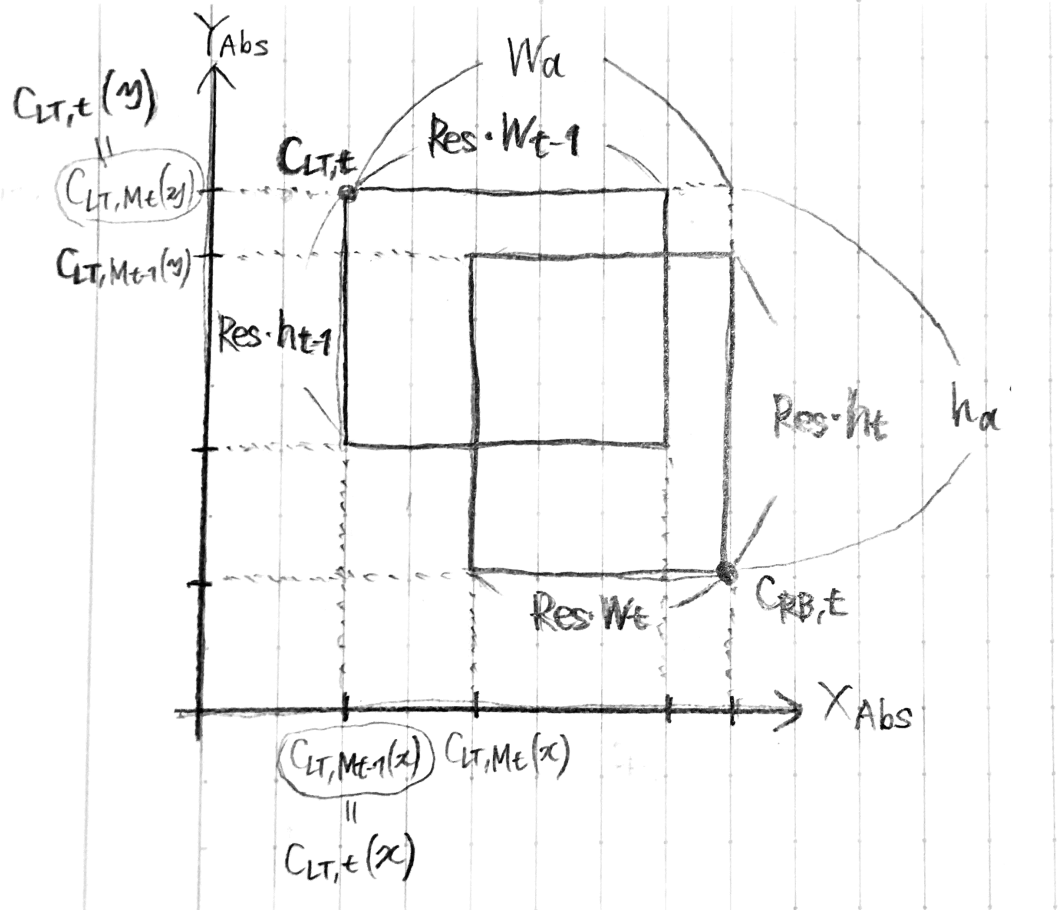
Q: What does $_{eq}$ mean in $I_{eq}(u, v)$? $_{equal}$?

3. MULTIPLE FRAMES ACCUMULATION

For all map images and the accumulated map, the top-left corner is considered as a reference.

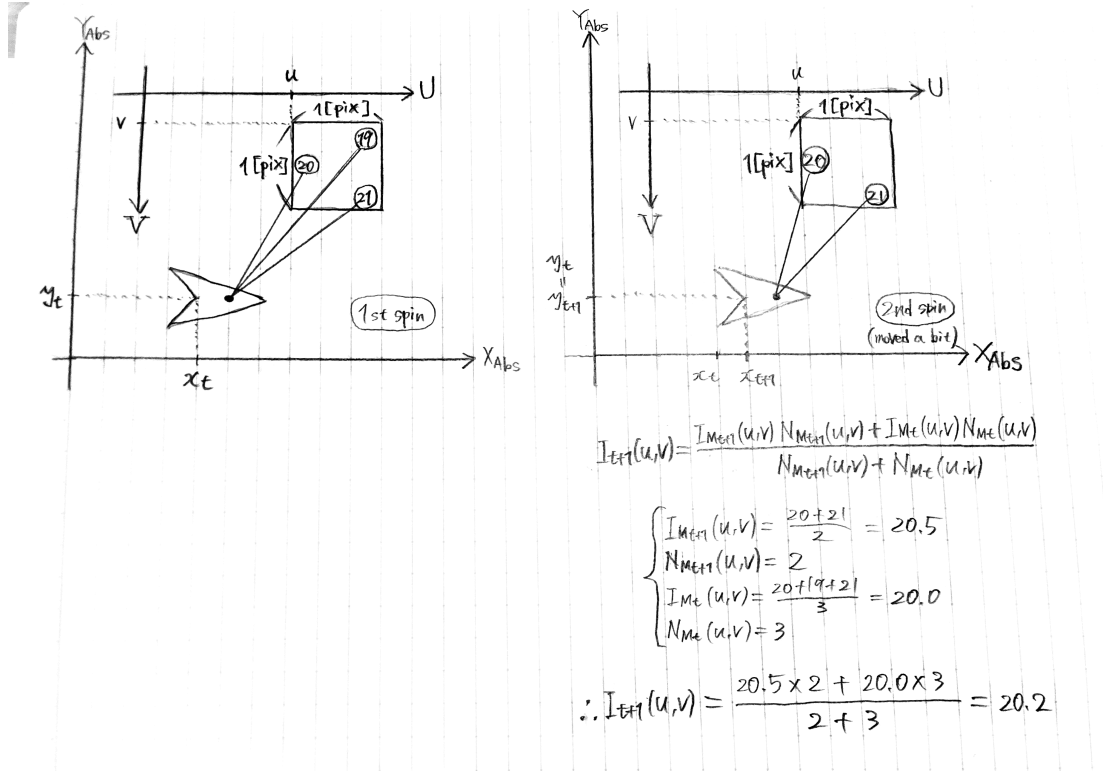
$$C_{LT,t}(x) = \min(C_{LT,M_{t-1}}(x), C_{LT,M_t}(x))$$

$$C_{LT,t}(y) = \max(C_{LT,M_{t-1}}(y), C_{LT,M_t}(y))$$



The equation of each pixel's intensity level $I_t(u, v)$ between slightly different position is;

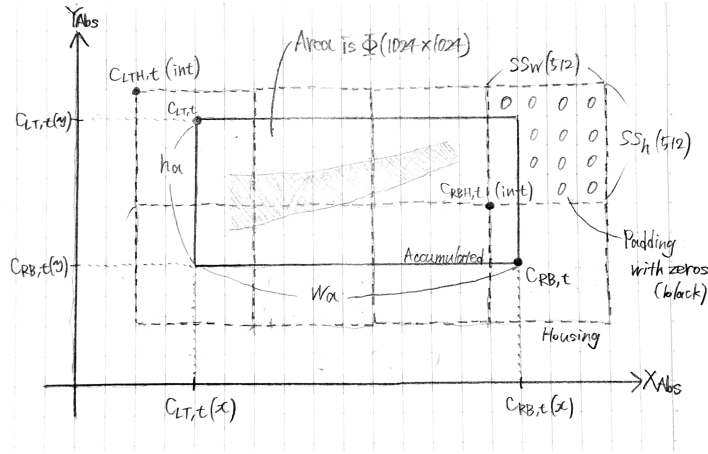
$$I_t(u, v) = \frac{I_{M_t}(u, v) * N_{M_t}(u, v) + I_{M_{t-1}}(u, v) * N_{M_{t-1}}(u, v)}{N_{M_t}(u, v) + N_{M_{t-1}}(u, v)}$$



In contrast to $I_{eq}(u, v)$, It seems that $I_t(u, v)$ just takes average of the intensity levels of each frames (I think).

4. LABELING AND SAVING

While accumulating the multiple LIDAR frames, saving procedures will be applied when the size of the accumulated frames exceeds a threshold Φ ($= 1024 \times 1024$). The accumulated map image will be padded with pixels that the value is zero (black), so that the hosing map image (= padded map image) can be cut with an integer number of sub-images whose size is $SS_w \times SS_h$ ($= 512 \times 512$).



The top-left and bottom-right corners of the housing map images are calculated in;

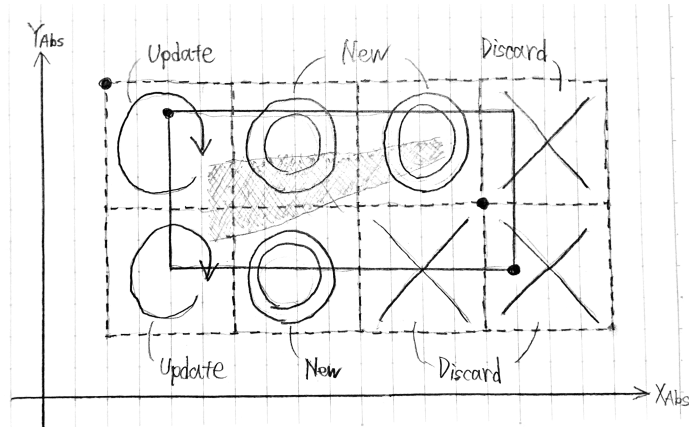
$$C_{LTH,t}(x) = \text{floor}\left(\frac{C_{LT,t}(x)}{SS_w}\right)$$

$$C_{LTH,t}(y) = \text{ceil}\left(\frac{C_{LT,t}(y)}{SS_h}\right)$$

$$C_{RBH,t}(x) = \text{floor}\left(\frac{C_{LT,t}(x) + Rse * w_a}{SS_w}\right)$$

$$C_{RBH,t}(y) = \text{ceil}\left(\frac{C_{LT,t}(y) - Rse * h_a}{SS_h}\right)$$

If the ID of the sub-images in the current housing map image is already existed, then just update the pixels. The sub-image that has no information (= all black) will be excluded from saving process to save storing size.



5. LOCALIZATION BASED ON THE GENERATED MAP

A. Map Image Creation

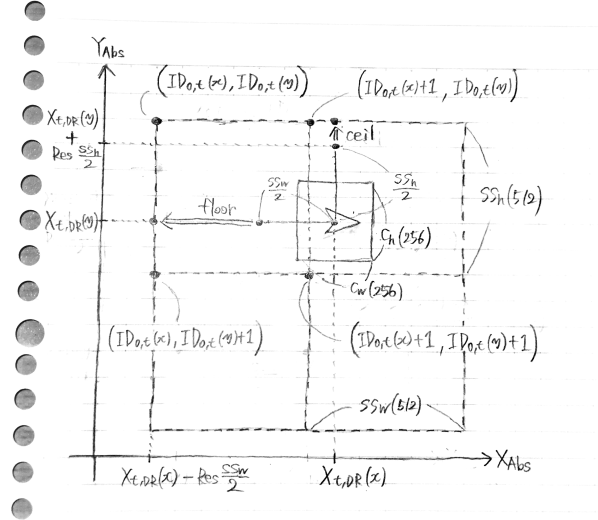
The offset between dead reckoning $X_{t,DR}$ and the actual location is estimated by calculating the cross correlation between LIDAR and map images. The map image is retrieved according to the dead reckoning measurement, and the labelling ID of the current driving area is calculated using;

$$ID_{0,t}(x) = \text{floor}\left(\frac{X_{t,DR}(x) - Rse * \frac{SS_w}{2}}{SS_w}\right)$$

$$ID_{0,t}(y) = \text{ceil}\left(\frac{X_{t,DR}(y) + Rse * \frac{SS_h}{2}}{SS_h}\right)$$

The map is created by combining four surrounding sub-images, which are;

- $(ID_{0,t}(x), ID_{0,t}(y))$
- $(ID_{0,t}(x) + 1, ID_{0,t}(y))$
- $(ID_{0,t}(x), ID_{0,t}(y) + 1)$
- $(ID_{0,t}(x) + 1, ID_{0,t}(y) + 1)$



Then, the large map images is cut equally around the vehicle position $X_{t,DR}$ to produce a small map image with size of $C_w \times C_h$.

B. LIDAR Image Creation

LIDAR frames and vehicle (irradiation frames as well) are saved and stacked during the last n frames. The current accumulated LIDAR image ($f = 1 \sim n$) can be obtained as a combination of the current LIDAR *frame* ($f = 1$) and previously *accumulated image* ($f = 2 \sim n - 1$) after removing the pixels of the last frame ($f = n$) in the stack.

