3007 Final Exam Review

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1 Definitions

Define the following terms and provide examples or sample code as appropriate.

1.1 Imperative vs Declarative

1.1.1 Imperative

- Series of instructions
- Iterative functions
- Command driven, statement oriented
- Procedural
 - C
 - Pascal
 - Assembly
- · Object oriented
 - C++
 - Java

1.1.2 Declarative

- No side effects
- Focus on relations
- "What to get" instead of "How to get"
- \bullet Order of statements shouldn't matter
- Examples:
 - SQL
 - Prolog
 - Regex

1.2 Scope vs Visibility

1.2.1 Scope

- The set of expressions for which the variable exists
- In lexical scoping
 - variables in the scope we were defined in
 - and local variables
 - who uses this?
 - * C-family languages
 - * Scheme
 - * Algol
- In dynamic scoping
 - variables in the scope we were *called* in
 - and local variables
 - who uses this?
 - * early LISP
 - * APL
 - * BASH

1.2.2 Visibility

- The set of expressions for which the variable can be reached
- If we declare a local variable with the same name as a variable in enclosing scope
 - that enclosing scope variable is now hidden
 - all references to *name* are to our locally scoped variable instead

1.3 Lexical Scope vs Dynamic Scope

1.3.1 Lexical

- Function scope is enclosed in the scope which defined us
 - if you can't find a binding, recursively search in the function that defined you

1.3.2 Dynamic

- Function scope is enclosed in the scope which called us
 - if you can't find a binding, recursively search in the function that called you

1.4 Free Variables

- Used locally but bound in an enclosing scope
- In the following example:

```
(define (f x y)
  (define z 2)
  (define (g)
     (* x y z)
  )
)
```

- x,y,z are free variables in (g)
- (g) looks them up in its enclosing scope, (f)

1.5 Applicative Order Evaluation vs Normal Order Evaluation

1.5.1 Applicative Order Evaluation

- Strict evaluation
- Evaluate an expression before it is passed in as an argument
 - go as deep as you can until you hit primitives, then evaluate and go back
 - $-\,$ as deep into the nest as possible and work backwards
 - e.g.,

```
(double (* (+ 1 3) 4))
(double (* 4 4))
(double 16)
(* 16 2)
32
```

1.5.2 Normal Order Evaluation

- Lazy evaluation
- Evaluate an expression only when its value is needed
 - first expand, then reduce

```
- e.g.,

(double (* (+ 1 3) 4))

(* (* (+ 1 3) 4) 2)

(* (* 4 4) 2)

(* 16 2)

32
```

1.6 Special Forms

- Exceptions to the usual evaluation order
 - they have their own evaluation rules
 - e.g., take the first argument without evaluating right away, evaluate the second symbol right away
- Use constructs like (delay foo), (force foo) behind the scenes

1.7 Tail Recursion

- Linear iterative processes in Scheme
- No deferred operations
 - recusrive call is the last operation of the procedure
- In Scheme, recursion is tail optimized
 - this means that it will run in constant space
 - number of steps will **grow linearly**, but memory will **remain constant**
- Even though the *program* is still recursive, the *process* is linear iterative because of tail-recursion optimization
- E.g., to compute a factorial using tail recursion, we do the following:

```
(define (factorial x)
  (define (iter prod i)
    (if (> i x)
        prod
        (iter (* i prod) (+ i 1))
    )
    )
    (iter 1 1)
)
```

• To compute a factorial using normal recursion, we would do the following instead:

1.8 First Class and Higher Order Procedures

1.8.1 First Class Procedures

- When procedures (functions) behave like variables
 - procedures can be passed as arguments into other procedures
 - or they can be *returned* from another procedure
- E.g.,

```
(define (f g)
    (g 2)
)
(define (h x)
    (+ x 3)
)
(f h) ; this would yield (+ 2 3), which evaluates to 5
```

- This is how *closures* work
 - more on this in a following subsection

1.8.2 Higher Order Procedures

- A procedure which accepts one or more procedure(s) as argument(s)
- In other words, a procedure which uses the first class procedures property of a language
- $\bullet\,$ In the above code block, (f g) is an example of a higher order procedure

1.9 Closures

- When a nested function is returned by its enclosing scope
- In practice, the returned function is typically a lambda (anonymous procedure)
- E.g.,

```
(define (multBy x)
    (lambda (y)(* x y)) ; lambda captures the free variable x
)

((multBy 12) 3) ; 36

(define (double) (multBy 2))
(define (triple) (multBy 3))

(double 2) ; 4
(triple 2) ; 6
```

1.10 Abstraction Barriers

- Hide implementation within complex procedures
 - user does not need to know how they work
 - they need only be guaranteed that they will work
- Prevents pollution of the global namespace

• Prevents excess free variables

1.11 Referential Transparency

- The idea that references can be substituted for their values without changing result of an expression
- Purely functional languages are referentially transparent
- Imperative languages are by definition **not** referentially transparent

1.12 Clause (Prolog)

- Facts and rules about the domain
- They specify truths and relations between symbols/entries in the domain
 - facts:
 * cold(ottawa).
 * rainy(ottawa).
 rules:
 * icy(X):- cold(X),rainy(X).
- Read from a file or asserted in the REPL with assert()
- Removed with retract()

1.13 Unification

- Prolog attempts to unify variables, atoms, and predicates
 - predicates unify with predicates with the same number of functors and if the functors can be unified
 - variables unify with variables and atoms
 - an atom will always unify with itself
- ullet The query succeeds if all $can\ be\ unified$
 - fails otherwise

1.14 Resolution

- Algorithm to resolve queries
- The algorithm:

```
Resolve:
Input: A query Q and program P
Output: True if Q can be inferred by P, false otherwise

Algorithm:
Start with a goal G, initially set to Q
Attempt to unify the first subgoal G1 from G

If no unification possible, then backtrack
If no backtrack possible, FAIL
Else, extend the goal G to G' with the following:
If unified with a rule, substitute G1 with the body of that rule
If unified with a fact, remove G1 from F

If G' is empty, SUCCESS
Else, Resolve G'
```

- If a clause unifies with a goal, it satisfies the goal
 - a **fact** satisfies the goal immediately
 - a **rule** substitutes subgoals for the original goal
- Backtracking here means the following:
 - attempt another clause to satisfy the subgoal
 - if we are out of clauses to try, undo a previously satisfied subgoal and attempt to satisfy it another way
 - * if we are out of subgoals, we can fail

2 Scheme Comprehension

Output: ((2 c) (a b c))

What is the output of the following expressions/programs?

```
1. (+ (* 3 4)(- 5 2 1)(/ 8 2))
   Output: 18
2. (and (> (+ (* 3 4)(- 5 2 1)(/ 8 2)) 0)(or (= (- 4 5)(+ 3 6 (* 10 -1)))(>= (* (/ 16
   4)(+ 1 (* 3 2)(- 31 29)))(+ (* 3 4)(- 5 2 1)(* 8 2)))))
   Output: #t
3. (let ((1 (+ 2 1))(e (/ 16(* 4 4)))(t (length '(5 7)))) (if (< 1 e) t 0))
   Output: 0
4. ((lambda (x y) (+ 3 x (* 2 y))) (+ 3 3)(* 2 2))
   Output: 17
5. (let ((a (lambda (b c)(* b c)))(b 10)(c 5))(+ (a 3 2) b c))
   Output: 21
6. (define (x \ y \ z)((lambda \ (y \ z)(-y \ z)) \ z \ y)) \ (x \ 3 \ 5)
   Output: 2
7. (define (foo y) ((lambda (x) y) ((lambda (y)(* y y)) y))) (foo 3)
   Output: 3
8. (((lambda(x)(lambda(y)(+ x y))) 12) ((lambda(z)(* 3 z)) 3))
   Output: 21
9. ((lambda (a b c)(list '(a b c) (list a b c) a 'b c)) 1 2 3)
   Output: ((a b c) (1 2 3) 1 b 3)
10. (((lambda (a)(lambda (b) '(lambda (c) '(a b c)))) 1) 2)
   Output: (lambda (c) '(a b c))
11. (eval '(let ((a (lambda(x y)(list x y)))(b 2)(c 3))(list (a b 'c) '(a b c)))
   (interaction-environment))
```

3 Normal and Applicative Order

Show the substitution model using normal and applicative order for the following examples:

3.1 First Example

```
(define (f x)(+ x (* 2 x)))
(define (g y)(* 10 (f y)))
(g (+ 1 2 3))
```

3.1.1 Applicative Order

```
(g (+ 1 2 3))

(g 6)

(* 10 (f 6))

(* 10 (+ 6 (* 2 6)))

(* 10 (+ 6 12))

(* 10 18)
```

3.1.2 Normal Order

```
(g (+ 1 2 3))

(* 10 (f (+ 1 2 3)))

(* 10 (+ (+ 1 2 3) (* 2 (+ 1 2 3))))

(* 10 (+ (+ 1 2 3) (* 2 6)))

(* 10 (+ 6 12))

(* 10 18)
```

3.2 Second Example

```
(define (abs x)
(if (< x 0) (- x) x))
(define (square x) (* x x))
(define (inc x)(+ x 1))
(+ (abs (- 75 100))(square (inc (abs (* -2 3)))))</pre>
```

3.2.1 Applicative Order

```
(+ (abs -25)(square (inc (abs (* -2 3))))

(+ (- -25)(square (inc (abs (* -2 3))))

(+ 25 (square (inc (abs (* -2 3))))

(+ 25 (square (inc (abs -6))))

(+ 25 (square (inc (- -6))))

(+ 25 (square (inc 6)))

(+ 25 (square (+ 6 1)))
```

```
(+ 25 (square 7))
(+ 25 (* 7 7))
(+ 25 49)
74
```

3.2.2 Normal Order

```
(+ (abs (- 75 100))(square (inc (abs (* -2 3))))

(+ (- (- 75 100))(square (inc (abs (* -2 3)))))

(+ (- (- 75 100))(* (inc (abs (* -2 3)))(inc (abs (* -2 3)))))

(+ (- (- 75 100))(* (+ (abs (* -2 3)) 1)(+ (abs (* -2 3)) 1)))

(+ (- (- 75 100))(* (+ (- (* -2 3)) 1)(+ (- (* -2 3)) 1)))

(+ (- -25)(* (+ (- (* -2 3)) 1)(+ (- (* -2 3)) 1)))

(+ 25 (* (+ (- (* -2 3)) 1)(+ (- (* -2 3)) 1)))

(+ 25 (* (+ 6 1)(+ 6 1)))

(+ 25 (* (+ 6 1)(+ 6 1)))

(+ 25 49)
```

4 Data Abstraction

```
; make a point
(define (make-point x y)
  (list x y)
; define get x of a point
(define (x-point p)
  (car p)
; define get\ y of a point
(define (y-point p)
  (cadr p)
)
; make a line segment
(define (make-segment x1 y1 x2 y2)
  (list (make-point x1 y1) (make-point x2 y2))
; get start of segment
(define (start-segment s)
  (car s)
; get end of segment
(define (end-segment s)
  (cadr s)
; get midpoint of a segment
(define (midpoint-segment s)
```

5 Lists and Iteration (in Scheme)

a) Define procedures map, filter, and reduce.

```
(define (map f L)
 (cond
    ((null? L) L)
    (else (cons (f (car L)) (map f (cdr L))))
   )
 )
(define (filter f L)
 (cond
    ((null? L) L)
    ((f (car L))(cons (car L) (filter f (cdr L))))
    (else (filter f (cdr L)))
 )
(define (reduce f L init)
 (define (helper v L)
    (cond
      ((null? L) v)
      (else (helper (f v (car L)) (cdr L)))
 (helper init L)
```

- b) Define a procedure (last L) that returns the last element of the list L.
- 6 Streams
- 7 Contour Models
- 8 MCI
- 9 Prolog