

# COMP3203 Final Exam Summary

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# 1 Units

- unit chart

prefix	base 10	base 2
pico	$10^{-12}$	$2^{-40}$
nano	$10^{-9}$	$2^{-30}$
micro	$10^{-6}$	$2^{-20}$
milli	$10^{-3}$	$2^{-10}$
—	$10^0$	$2^0$
kilo	$10^3$	$2^{10}$
mega	$10^6$	$2^{20}$
giga	$10^9$	$2^{30}$
tera	$10^{12}$	$2^{40}$
peta	$10^{15}$	$2^{50}$

- $Hz \implies$  cycles per second
  - $GHz \implies 10^9$  cycles per second
  - etc.

## 2 Formulas

### 2.1 Frequency

$$f = \frac{1}{T}$$

### 2.2 Period

$$T = \frac{1}{f}$$

### 2.3 Wavelength

$$\lambda = vT$$

$$\lambda = \frac{v}{f}$$

### 2.4 Bandwidth

$$B = vT$$

### 2.5 Delay

$$D = D_P + D_T + D_Q$$

#### 2.5.1 Propagation

$$D_P = \frac{\text{distance}}{\text{speed of light}}$$

### 2.5.2 Transmit

$$D_T = \frac{\text{packet size}}{\text{bandwidth}}$$

### 2.5.3 Queue

$$D_Q = \sum_{\text{nodes}} (\text{buffering} + \text{switching})$$

### 2.5.4 Round Trip Time

$$RTT = 2D$$

- how long does it take a packet to go **there and back**

## 2.6 Overhead

$$T_O = \frac{h}{p} \quad \text{where } h = \text{overhead bits, } p = \text{message bits}$$

- **extra over what we want**

## 3 Error Checking

- VRC
- LRC
- **CRC**
  - this guy is usually used
  - use in tandem with ARQ
- checksum

## 4 ARQ

- automatic repeat request
- handle errors by requesting they be resent
- use in tandem with error detection
  - **CRC**
  - checksum
- main parts
  - **ACKS**
  - **NAKS**
  - **timers**

### 4.1 Sliding Window

- number frames sequentially
- window of either fixed or variable size
  - see TCP section

#### 4.1.1 Go Back N

- go back to the beginning of the window and resend everything
- $w - i = N$

#### 4.1.2 Selective Reject

- **only** resend the **damaged frame**
- need **sorting logic**
  - frames may be out of order

### 4.2 Stop and Wait

- like sliding window with a **window size** = 1

## 5 Multiaccess

- problem of **shared channels**
  - who gets a turn?
  - how do we make sure things get to the right place?
- point-to-point is easy (by contrast)

### 5.1 LANs

- local area network
- shared channel

#### 5.1.1 Switched LANs

- *interconnection by transmission*
- **complex**
  - routing tables
  - hierarchical addressing

#### 5.1.2 Broadcast LANs

- information *received by all*
- **simple**
  - no routing
  - flat addressing scheme
- MAC (medium access control)
- **used more often**

### 5.2 Uncoordinated Access Control

- sucks
- $P(\text{exactly one talks}) = np(1 - p)^{n-1}$

### 5.3 MAC Protocol

- Medium Access Control
- **dynamic**
- on demand
- must **minimize** collisions
- two classes

- random access
- scheduling

### MAC vs Static

MAC  $\implies$  dynamic, on demand

Static  $\implies$  separate dedicated channels

#### 5.3.1 Centralized

- *one* **master node**
  - makes decisions for slaves nodes
- *dependent* on **master**
  - what if it fails?
  - less efficient

#### 5.3.2 Distributed

- all nodes **equivalent**
- make a decision together
  - *distributed* fashion

### 5.4 How Does MAC Work?

- measure** prop time
- coordinate** access
- select** a winner

#### 5.4.1 Measure

- ping
- $T_{prop} = \frac{d}{v}$

#### 5.4.2 Coordinate

```

1 def coordinateTwoHosts(A,B):
2   A.listen(channel)
3
4   if channel not busy:
5     A.transmit(m)
6     while no message from B:
7       A.listen(channel)
8       if time > Tprop:
9         break
10    else:
11      A.retransmit(m)
12
13  repeat for B

```

#### 5.4.3 Select a Winner

- let  $T_A$  = time for a collision detected by A
- let  $T_B$  = time for a collision detected by B
- A wins  $\iff T_A < T_B$

- loser is quiet until winner completes
- winner is quiet after transmission for RTT

## 5.5 MAC Efficiency

$$E = \frac{1}{1 + 2\frac{T_{prop}}{L}}$$

## 6 Ethernet

- **broadcast network**
  - every node can hear every other
- when collision occurs
  - stop sending
  - wait to retransmit

### 6.1 Limitations

- very large packet size as bandwidth increases
- MAC is technology dependent
  - are measurements accurate?
  - measurements may differ between hosts
- but it is **realistic**
  - uptime is important

### 6.2 Backoff Protocols

- **queue** of nodes **waiting to transmit**
- keep track of number of attempts
- define  $P(x)$ 
  - probability you transmit on attempt  $x$
  - decreasing in  $x$

#### 6.2.1 Implementation

- station  $i$  has  $bck_i$
- set it to 0
- if queue not empty
  - attempt transmission with  $p(bck_i)$ 
    - fails  $\implies bck_i++$
    - succeeds  $\implies bck_i := 0$
- if queue was empty, don't change  $bck_i$

### 6.3 Collision-Free Protocols

#### 6.3.1 Bitmap

- **contention period** = 8 slots
- station  $i$  inserts one bit into  $i$ th slot
- after  $N$  slots, each station knows who wants to transmit
- transmit **in order**
- a station  $i$  is out of luck if it becomes ready **just after** slot  $i$  passes



### 6.3.2 Tree Splitting

- nodes are leaves
- recursive
- keep taking left **subtree** until **one node** in **contention**
  - that node wins
  - take right subtree if applicable
  - walk back up to root

### 6.3.3 Binary Countdown

- assume **all addresses** are **same length**
- node writes its bit from **highest to lowest order**
  - if I have a 0 and somebody else has a 1
    - I drop out
  - otherwise
    - I stay in
- last man standing wins

## 7 Wireless

### 7.1 Cellular

- organized into **cells**
  - hexagons
- **neighboring cells**  $\implies$  **different frequency bands**

### 7.2 Ad Hoc

- temporary connection
- **decentralized**
- model with a **Unit Disk Graph**
  - **points** and **circles** for range
  - $G = (V, E)$  where
    - vertices are nodes
    - edges are nodes that can each other
    - asymmetric ranges  $\implies$  directed graph

#### 7.2.1 Traversal

- **compass routing**
  - draw line  $\vec{st}$
  - pick smallest angle edge  $sv$
  - draw new line  $\vec{vt}$
  - **doesn't always complete**
- **face routing**
  - draw line  $\vec{st}$
  - **LHR** or **RHR**
  - pick a face which crosses the line
  - walk it until you are **about to cross**, then **flip face** to next

## 7.3 Bluetooth

### 7.3.1 Formation

- **master nodes**
- **slave nodes**
  - bridge nodes (a special slave)

#### Rules

1. **master** only next to **slaves** (and **bridges**)
2. **slaves** only next to a **master**
3. each master's **piconet** can have **max 7 slaves**
4. bridge between **TWO** masters **ONLY**

### 7.3.2 Joining Two Piconets

- **roles** of master and slave can **switch**
  - done by *changing frequencies*
- a slave will act as a **bridge**

## 8 GPS

### 8.1 Three Techniques

### 8.2 Satellites

## 9 Routing

### 9.1 Distance Vector

### 9.2 Link State Protocol

### 9.3 MST

- two standard algorithms
  - Prim
  - Kruskal

#### 9.3.1 Kruskal

- start with nodes separated
  - keep adding smallest edge that doesn't create a cycle
  - we are done when all vertices are in the tree
- time complexity
  - # of times we change group label is at most  $\log n$
  - limited by how fast we can sort the edges
    - $\boxed{(|E| \log |E|)}$

#### 9.3.2 Prim

- **(p)rim's = (p)ick** a node
  - pick smallest edge from that vertex that reaches an unvisited vertex
  - add that edge, now imagine the two vertices as one meta-vertex
  - repeat until we have reached the last vertex

- time complexity
  - $O(|E| \log |E| + |V| \log |E|)$

## 9.4 Dijkstra

- add all vertices to a min-heap of  $d(v)$   $Q$ 
  - initialize  $d(s)$  is 0
  - initialize all other  $d(v)$  to  $\infty$
- pop  $s$  and update weight of all neighbors  $v$  of  $s$  as  $d(s) + wt(s, v)$ 
  - keep track that you popped it
- pop the lowest and repeat the above step for the lowest
- continue until  $Q$  contains no more vertices
- time complexity
  - $O(|E| \log |E| + |V| \log |E|)$

## 10 IP

### 10.1 IPv4

#### 10.1.1 Classes

#### 10.1.2 Subnets

#### 10.1.3 Subnet Masks

### 10.2 IPv6

### 10.3 DHCP

### 10.4 ARP

### 10.5 RARP

## 11 TCP

### 11.1 How it Works (Sliding Window)

### 11.2 Building Statistics

### 11.3 Equilibrium Model

- **loss**  $\implies$  decrease  $w$ 
  - $w = \frac{w}{2}$
- **no loss**  $\implies$  increase  $w$ 
  - $w = w + \frac{1}{w}$

## 12 Sample Test

1

A system has an  $n$ -layer protocol hierarchy. Applications generate messages of length  $M$  Bytes. At each level of the layers, an  $h$ -Byte header is added.

## 1.1

[3 pts] What fraction of the network bandwidth is filled with headers? (Give the formula.)

$$\text{overhead} = \frac{nh}{nh + M}$$

## 1.2

[3 pts] Now assume  $M = 20h$ . What should the max number  $n$  of layers be so that the fraction in previous Question 1 does not exceed 10 % of the total?

$$\begin{aligned} \text{overhead} &= \frac{nh}{nh + M} \\ 10\% &\geq \frac{nh}{nh + 20h} \\ \frac{1}{10} &\geq \frac{n}{n + 20} \\ (n + 20)\frac{1}{10} &\geq n \\ (n + 20)\frac{1}{10} &\geq n \\ \frac{n}{10} + 2 &\geq n \\ n + 20 &\geq 10n \\ 20 &\geq 9n \\ n &\leq \frac{20}{9} \end{aligned}$$

## 1.3

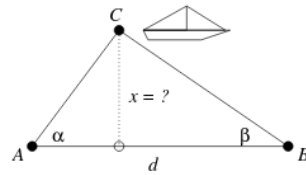
Two CDMA users are assigned the 9-bit vectors  $A = 110011011, B = 100101111$ , respectively. Are they orthogonal? (Prove or disprove!) **Hint:** Recall  $0 \rightarrow -1$  and  $1 \rightarrow +1$ .

Take inner product of vectors in mod 2.

$$\begin{aligned} \langle \vec{A}, \vec{B} \rangle \mod 2 &= 1 + 0 + 0 + 0 + 0 + 1 + 0 + 1 + 1 \mod 2 \\ &= 0 \end{aligned} \quad \Longleftrightarrow \text{orthogonal}$$

## 2

You are observing a ship from two base stations  $A, B$ . Assume that at this time of observation  $\alpha = \pi/3, \beta = \pi/4$  and  $d = 1000$  m.



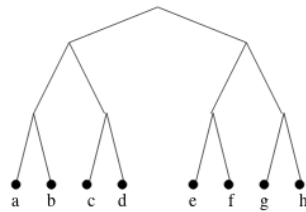
Derive a formula for the unknown distance  $x$  (You are not required to evaluate the trigonometric functions of  $\pi/3$  and  $\pi/4$ ).

$$x = d \frac{\tan \alpha \tan \beta}{\tan \alpha + \tan \beta}$$

$$x = 1000 \text{ m} \frac{\tan \frac{\pi}{3} \tan \frac{\pi}{4}}{\tan \frac{\pi}{3} + \tan \frac{\pi}{4}}$$

## 3

Ethernet stations  $a, b, c, d, e, f, g, h$  contend for a channel. Assume  $a, e, f, g, h$  become ready at once and that they use the tree resolution protocol to resolve contentions.

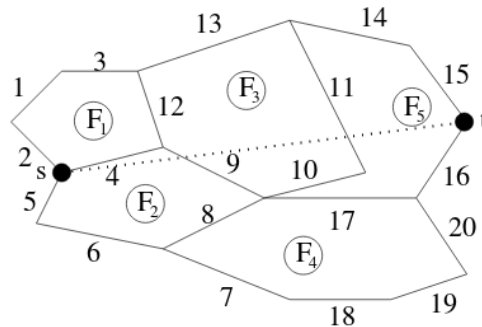


for each contention slot give in the table below the winning stations.

Slot	Station
1	a e f g h
2	a
3	e f g h
4	e f
5	e
6	f
7	g h
8	g
9	h

4

The links and faces of a planar wireless network are labeled as depicted in the Figure below. Moreover there is a source node  $s$  and a destination node  $t$ .



4.1

Apply the face routing algorithm with the left-hand rule (on a face) to give a path from  $s$  to  $t$ . In the table below name the face and the edges of that face being traversed. **Your answers must list all the links traversed and the paths formed must arise from the corresponding routing algorithm!**

Face	List of Edges Being Traversed
$F_2$	4
$F_3$	12, 13
$F_5$	14, 15

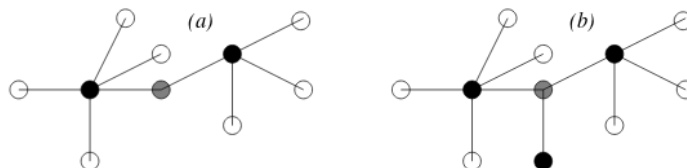
4.2

Apply the compass routing algorithm to give a path from  $s$  to  $t$ .

4, 9, 10, 11, 14, 15

5

In the networks below empty (gray, black) bullets are pure slaves, bridges, masters, respectively. According to Bluetooth formation rules, which of the two networks are bluetooth networks, which are not and why?



5.1 A

- valid
  - all piconets have slavecount  $\leq 7$
  - all piconets have slaves

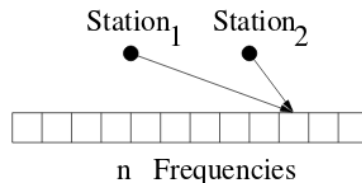
- no adjacent masters
- no adjacent slaves
- bridge connects **two** piconets by their master nodes

## 5.2 B

- **invalid**
- the good
  - all piconets have slavecount  $\leq 7$
  - no adjacent masters
  - no adjacent slaves
- the bad
  - bridge connects **three** piconets by their master nodes
  - should be **TWO**
  - one piconet has **no slaves**

## 6

There are  $n \geq 2$  possible frequencies and 2 synchronous wireless stations. Each station is using frequency-hopping to select at random (with probability  $1/n$ ) one of these frequencies. What is the probability that the stations select the same frequency? (Give explanation of your answer.)



Define event  $A$  is both stations select same frequency.

$$\begin{aligned}
 P(A) &= n \frac{1}{n} \frac{1}{n} \\
 &= \frac{1}{n}
 \end{aligned}$$

## 7

$n$  sensors all having range equal to 1, form a unit line graph arranged on a line such that the  $i$ th sensor has  $x$ -coordinate equal to  $x_i$ , for  $i = 1, 2, \dots, n$ . Further, assume  $x_i = i + (-1)^i$ , for all  $i = 1, 2, \dots, n$ .

### 7.1

Give the values  $x_1, x_2, x_3$ .

$$\begin{aligned}
 x_1 &= 1 + (-1)^1 = 1 - 1 = 0 \\
 x_2 &= 2 + (-1)^2 = 2 + 1 = 3 \\
 x_3 &= 3 + (-1)^3 = 3 - 1 = 2
 \end{aligned}$$

### 7.2

[2 pts] Is the unit line graph a connected graph? Give a precise explanation of your answer.

In order for the graph to be connected, we need some node with an x-coordinate of 1 at a bare minimum.  
Is it possible to have such an x-coordinate?

$$\begin{aligned}1 &= i + (-1)^i \\ i &= 0\end{aligned}$$

Our  $i \in \{1, 2, \dots, n\} \implies i \neq 0$ . Therefore it is not a connected graph.