Recursive Implementation of the Hanoi Towers in RISC-V

Practice 1

enrique.rios@iteso.mx / Ex: 750259, yael.morales@iteso.mx / Ex: 751669

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1 Introduction

1.1 History Context

The Hanoi Towers are a famous puzzle of mathematical origin, invented in 1883 by the French mathematician Edouard Lucas. This puzzle consists of a base with three rods or sticks called A, B and C, and a set of n disks of different sizes. Initially, the disks are stacked on rod A in decreasing order of size, with the largest disk at the bottom and the smallest at the top. The goal of the puzzle is to move all the disks from rod A to rod C, following two main rules: only one disk can be moved at a time, and at no time can a larger disk be placed on top of a smaller one.

1.2 Practice

During practice, this assembly language puzzle was implemented using the RARS simulator, which supports the RISC-V architecture. This practice allows visualizing the moves necessary to solve the problem recursively, observing how the disks are progressively moved until the final configuration is reached on the C-rod. The process requires planning and understanding of the recursive structure of the solution, which is fundamental in low-level programming and computer architecture.

1.3 Github repository

[Click here] https://github.com/Hoverpi/Hanoi_asm

2 Hanoi Risc-V Development

2.1 C code Hanoi Algorithm

```
#include <stdio.h>

// C recursive function to solve tower of hanoi puzzle

void TowerOfHanoi(int n, char from_rod, char to_rod, char aux_rod) {
    if (n == 0) return;
    TowerOfHanoi(n-1, from_rod, aux_rod, to_rod);
    printf("Move disk %d from rod %c to rod %c\n", n, from_rod, to_rod);
    TowerOfHanoi(n-1, aux_rod, to_rod, from_rod);
}

int main() {
    int N = 3; // Number of disks
    TowerOfHanoi(N, 'A', 'C', 'B'); // A, B and C are names of rods
    return 0;
}
```

2.2 Risc-V Assembly Code

1

¹Hanoi Algorithm base code

```
add s2, s2, t0
        add s3, s3, t0
        addi s10, zero, 0 # Counter initiatized to 3
addi s11, zero, 0x20 # Offset value for moving between towers
addi t1. s0, -1 # n = N - 1 (one less than the total disks)
        for:
            beq s0, t0, hanoi
            addi t1, t0, 1
            j for
end_for:
           jal ra, hanoi
hanoi:
          addi t0, zero, 1
        bne s0, t0, else
        addi sp, sp, -4  # Reserve space in the stack sw ra, 0x0(sp)  # Save ra addi sp, sp, -4
else:
        addi s0, s0, −1
        add t1, s2, zero # AUX \rightarrow TEMP add s2, s3, zero # AUX \rightarrow DST
        add s3, t1, zero # DST -> AUX/TEMP
        jal ra, hanoi
```

```
add t1, s2, zero
              add s2, s3, zero
              addi sp, sp, 4
              lw ra, 0x0(sp)
              addi sp, sp, 4

      sw
      zero, 0x0(s1)
      # Remove disk from SRC

      add
      s1, s1, s11
      # Move SRC -> SRC + OFFSET

      sub
      s3, s3, s11
      # Move DST -> DST - OFFSET

      sw
      s0, 0x0(s3)
      # Place disk in DST

              addi s10, s10, 1
              addi sp, sp, -4
              sw ra, 0x0(sp)
addi sp, sp, -4
sw s0, 0x0(sp)
              addi s0, s0, -1
              add t1, s1, zero # TEMP -> AUX
add s1, s2, zero # AUX -> DST
add s2, t1, zero # DST -> TEMP
ial ra hanoi # hanoi(n-1 A
              jal ra, hanoi
              add t1, s1, zero # TEMP \rightarrow SRC add s1, s2, zero # SRC \rightarrow AUX
              addi sp, sp, 4
exit:
                               exit
```

2.3 Registers Description

Register	Description
s0	Contains the total number of disks (N) used for operations in the Towers of Hanoi.
s1	Base address for Tower A in memory.
s2	Base address for Tower B in memory.
s3	Base address for Tower C in memory.
s10	Move counter tracking the number of moves made during the solution of the Towers of Hanoi.
s11	Constant offset (0x20) used to calculate the memory displacement between disk positions during tower manipulation.
sp	Stack pointer, used to manage the stack during recursive calls and temporarily store important registers like ra and s0.
t0, t1	Temporary registers used for calculations and value comparisons in the algorithm's loops and conditions.
t2, t4	Used to calculate and manage memory addresses where the disks are stored in the towers.
t5	Offset counter in the initial loop, incremented by 0x20 to organize the disks.
ra	Return address register, used to store the return address during recursive calls.

2.4 Breakdown

```
.text
main:

addi s0, zero, 3  # N = 3

lui s1, 0x10010
addi s1, s1, 0  # Torre A = 0x10010000
addi s2, s1, 4  # Torre B = 0x10010004
addi s3, s2, 4  # Torre C = 0x10010008

# Move B and C pointer to the start of stack
slli t0, s0, 5  # start = N << 5
add s2, s2, t0  # Direccion en memoria de B
add s3, s3, t0  # Direccion en memoria de C

# Desplazamiento inicial en bytes
addi t2, zero, 0x00  # Desplazamiento inicial)
```

```
addi s10, zero, 0 # Counter
addi s11, zero, 0×20
addi t1, s0, -1 # n = N - 1
```

First, the number of disks (N) is set to 3, storing this value in register s0. Then, a base memory address for Tower A (s1) is defined at 0x10010000, with addresses for Tower B (s2) and Tower C (s3) assigned at 0x10010004 and 0x10010008, respectively. Next, pointers for Towers B and C are adjusted in memory using the stack by calculating an offset (start) based on the number of disks N, which is left-shifted by 5 positions and stored in t0. This offset is then applied to the addresses of Towers B and C (s2 and s3), effectively adjusting their starting positions in memory.

Afterward, an initial offset and counters are initialized, with t2 set to 0 for the initial byte offset, a counter in s10 initialized to 0 for keeping track of movements, and s11 set to a constant value of 0x20, representing an offset for moving and manipulating the disk positions in memory. Finally, the value n is calculated as N - 1 and stored in t1 for future use in operations, particularly in the recursive logic of the algorithm.

```
for: beq s0, t0, hanoi  # Si i == N, salir

    addi t1, t0, 1  # a = i + 1
    # Calcular la dirección personalizada para almacenar el dato
    add t2, zero, s1  # t3 = dirección de almacenamiento
    add t4, t2, t5

    sw t1, 0(t4)  # Guardar t1 en la dirección calculada

    addi t5, t5, 0x20  # count += 0x20
    addi t0, t0, 1  # Incrementar i
    j for  # Volver al inicio del bucle

end_for: jal ra, hanoi
    j exit
```

This section of the code iterates over the disks, storing each one in memory with a calculated address. The loop, starting at for, runs until i (t0) equals N (s0). In each iteration, it calculates the memory address using Tower A's base address (s1) plus an offset (t5). The disk number (t1 = i + 1) is then saved at this address.

The offset (t5) is updated by 0x20 for the next disk, and i is incremented. Once the loop finishes, the program jumps to the hanoi procedure for solving the Towers of Hanoi, and then moves to exit to end this segment.

```
hanoi:
                     addi t0, zero, 1
             bne s0, t0, else # If s0 != 1, jump to '
sw zero, 0x0(s1) # Remove disk from SRC
add s1, s1, s11 # Move SRC -> SRC + OFFSET
sub s3, s3, s11 # Move DST -> DST - OFFSET
sw s0, 0(s3) # Place disk in DST
addi s10, s10, 1 # Increment counter
jalr ra # Pa+um f
if:
              jalr ra
                   addi sp, sp, -4 # Reserve space in the stack ra, 0x0(sp) # Save ra
else:
                      ra, <mark>0</mark>x0(sp)
              addi sp, sp, -4

sw s0, 0x0(sp) # Save s0

      add
      t1, s2, zero
      # AUX -> TEMP

      add
      s2, s3, zero
      # AUX -> DST

      add
      s3, t1, zero
      # DST -> AUX/*

              add t1, s2, zero # AUX \rightarrow TEMP
              add s2, s3, zero
              add s3, t1, zero
              lw s0, 0x0(sp)
addi sp, sp, 4
              addi sp, sp, 4

      sw
      zero, 0x0(s1)
      # Remove disk from SRC

      add
      s1, s1, s11
      # Move SRC -> SRC + OFFSET

      sub
      s3, s3, s11
      # Move DST -> DST - OFFSET

      sw
      s0, 0x0(s3)
      # Place disk in DST

              addi s10, s10, 1 # Increment counter
              addi sp, sp, -4
             sw ra, 0x0(sp) # Save ra
addi sp, sp, -4
sw s0, 0x0(sp) # Save s0
              addi s0, s0, -1
              add t1, s1, zero
```

```
jal ra, hanoi  # hanoi(n-1, AUX, DST, SRC)

# Restore auxiliary variables and clear the stack after the second call
add t1, s1, zero  # TEMP -> SRC
add s1, s2, zero  # SRC -> AUX
add s2, t1, zero  # AUX -> TEMP

lw s0, 0x0(sp)  # Recover s0
addi sp, sp, 4
lw ra, 0x0(sp)  # Recover ra
addi sp, sp, 4

jalr ra  # Return
```

This segment implements the recursive solution for the Towers of Hanoi. The base case (if) handles moving a single disk directly between source (SRC) and destination (DST). It removes the disk from SRC, adjusts the addresses using offsets, and places the disk in DST. If there are more than one disk (else), it recursively moves n-1 disks to an auxiliary tower (AUX), makes the move to the target tower, and then moves the n-1 disks from AUX to the destination.

During the recursion, registers ra (return address) and s0 (disk count) are saved on the stack. Offsets are adjusted to ensure that the disks are moved correctly, taking into account each recursive call's impact on the towers' state. The program finishes the recursion with a jalr instruction that returns to the previous recursive level or ends the function when all operations are complete.

3 Tests

3.1 Video Test

[Click here] Hanoi Test with 4 Disks

3.2 8 Disks Stadistics

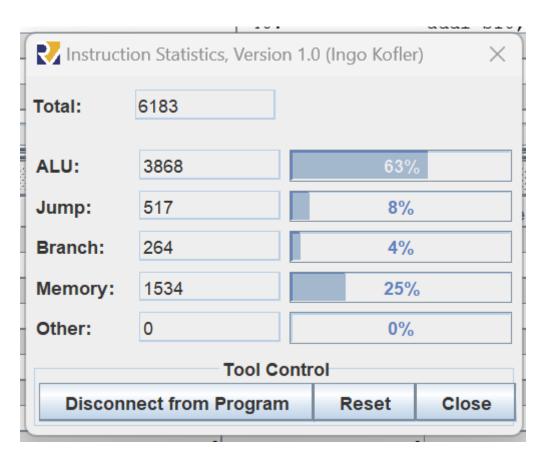


Figure 3.1: 8 Disks Stadistics

3.3 4 <= N <= 15 Graphic

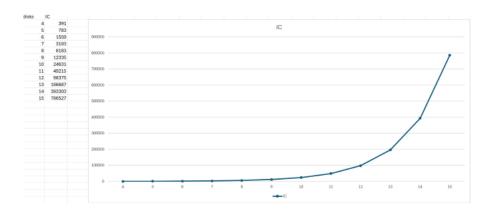


Figure 3.2: Instruction Count Graphic

4 Conclusions

Yael Salvador Morales Renteria: By means of this practice we saw that to implement the towers of hanoi is something complicated in assembly language since in a language like C, pyhton, etc. it is easier since everything is integrated but in this language we saw that we use more than 100 lines of code to be able to make this exercise but thanks to this we can save memory inside the device that we are using and even in didactic terms as the machine solves this algorithm that we did.

José Enrique Rios Gómez: Implementing the Hanoi algorithm in assembly was an incredibly challenging experience, especially when recursion was introduced; it added an extra layer of complexity that made the task feel daunting. Despite the difficulties, I can't fault the language itself because assembly offers significant control over the operations being performed, which is undeniably valuable. However, for larger program development, I find it hard to envision myself using assembly. This is precisely why higher-level languages and their compilers exist. Nonetheless, from a learning standpoint, working with assembly proved to be an enriching experience, greatly enhancing my understanding of low-level operations and system mechanics.