

Tree*

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July 3, 2020

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1 Problems

- 1. 编写算法:输入树的边(双亲-孩子有序对)建立对应树 的孩子-兄弟链表存储结构;
- 2. 编写算法:求树的深度;
- 3. 编写算法:输出从树根到所有叶子结点的路径;
- 4. 编写算法:统计树中叶子结点的个数。

2 Code

2.1 Tree.h

^{*}This article was typeset by Mark Taylor using the LATEX document processing system.

```
1 // tree header
2 #ifndef TREE_H
3 #define TREE_H
4 #include "SeqStack.h"
5 #include <memory>
6 #include <cassert>
7 #include <iostream>
9 template<typename T>
10 struct TreeNode {
           T _data;
11
12
           std::shared_ptr<TreeNode<T>> _first_child, _next_sibling;
13
           TreeNode(const T value = {}, std::shared_ptr<TreeNode<T>> fc = nullptr,

    std::shared_ptr<TreeNode<T>> ns = nullptr)

14
                    : _data(value), _first_child(fc), _next_sibling(ns) {}
15
           "TreeNode() { std::cout << "Destructing tree node with value " << _data << '\n'; }
16 };
17
18 template<typename T>
19 class Tree {
20 public:
21
           Tree() { _root = nullptr; }
22
           std::shared_ptr<TreeNode<T>> create_tree(std::shared_ptr<TreeNode<T>> t);
23
           std::shared_ptr<TreeNode<T>> get_root()const { return _root; }
24
25
           bool empty()const { return _root == nullptr; }
26
           size_t depth(std::shared_ptr<TreeNode<T>> t)const;
27
           size_t count_node(std::shared_ptr<TreeNode<T>> t)const;
28
           size_t count_leaves(std::shared_ptr<TreeNode<T>> t)const;
29
30
           // We do NOT set traverses as const member functions
31
           // given that we may need to modify those nodes.
           // see also <a href="https://isocpp.org/wiki/faq/pointers-to-members">https://isocpp.org/wiki/faq/pointers-to-members</a>
32
33
           void preorder(std::shared_ptr<TreeNode<T>>) = visit);
34
           void postorder(std::shared_ptr<TreeNode<T>> t, void (*visit)(std::shared_ptr<TreeNode<T>>) = visit);
35
36
           // print paths from root node to leaves
37
           void print_path(std::shared_ptr<TreeNode<T>> t)const;
38
39
  private:
40
           std::shared_ptr<TreeNode<T>> _root;
           static void visit(std::shared_ptr<TreeNode<T>> t);
41
42 };
43
44 //create tree by level
45 template<>
                    // specialization for char type
46 std::shared_ptr<TreeNode<char>> Tree<char>::create_tree(std::shared_ptr<TreeNode<char>> t)
47 {
48
           // to be added..
           return std::make_shared<TreeNode<char>>();
49
50 }
51
52 template<typename T>
53 std::shared_ptr<TreeNode<T>> Tree<T>::create_tree(std::shared_ptr<TreeNode<T>> t)
54 {
55
           return std::make_shared<TreeNode<T>>();
56 }
57
58 template<typename T>
59 size_t Tree<T>::depth(std::shared_ptr<TreeNode<T>> t) const
60 {
```

```
if (t == nullptr) return 0;
 61
 62
            size_t fc_depth = depth(t->_first_child) + 1;
 63
            size_t ns_depth = depth(t->_next_sibling);
 64
 65
            return fc_depth > ns_depth ? fc_depth : ns_depth;
 66 }
 67
 68 template<typename T>
 69 size_t Tree<T>::count_node(std::shared_ptr<TreeNode<T>> t) const
 70 €
            if (t == nullptr) return 0;
 71
 72
            size_t count = 1;
            count += count_node(t->_first_child);
 73
 74
            count += count_node(t->_next_sibling);
 75
 76
            return count;
 77 }
 78
 79
   template<typename T>
 80 size_t Tree<T>::count_leaves(std::shared_ptr<TreeNode<T>> t) const
 81 {
 82
            static size_t count = 0;
 83
            if (t != nullptr) {
 84
                    if (t->_first_child == nullptr)
 85
                            ++count:
 86
                    else
                            count_leaves(t->_first_child);
 87
 88
 89
                    count_leaves(t->_next_sibling);
 90
 91
            return count;
 92
 93
    template<typename T>
 95
    void Tree<T>::preorder(std::shared_ptr<TreeNode<T>>))
 96
 97
            if (t != nullptr) {
 98
                    visit(t);
 99
                    preorder(t->_first_child, visit);
100
                    preorder(t->_next_sibling, visit);
            }
101
   }
102
103
104 template<typename T>
105 void Tree<T>::postorder(std::shared_ptr<TreeNode<T>>) t, void(*visit)(std::shared_ptr<TreeNode<T>>))
106 {
107
            if (t != nullptr) {
108
                    postorder(t->_first_child, visit);
109
                    visit(t);
                    postorder(t->_next_sibling, visit);
110
            }
111
112 }
114 template<typename T>
void Tree<T>::print_path(std::shared_ptr<TreeNode<T>> t) const
116 {
117
            static SeqStack<T> s;
118
            while (t != nullptr) {
119
                    s.push(t->_data);
                    if (t->_first_child == nullptr) {
120
                            s.bottom_up_traverse();
121
```

```
122
                             std::cout << '\n';
                     }
123
124
                     else
125
                             print_path(t->_first_child);
126
                     s.pop();
127
                     t = t->_next_sibling;
            }
128
129
130
131 // operation for node p
132 template<typename T>
133 inline void Tree<T>::visit(std::shared_ptr<TreeNode<T>> p)
134 {
135
            assert(p != nullptr);
            std::cout << p->_data;
136
137 }
138
139 #endif // !TREE_H
```

Listing 1: Tree header

2.2 Tree_test.cpp

```
1 #include "Tree.h"
   #include <iostream>
 4
   using namespace std;
6
   void tree_operations()
7
   {
8
           Tree<char> tree;
           auto root{ tree.get_root() };
9
                                            // to be added
10
           //tree.create_tree(root);
11
           /*
12
                       Α
                     / | \
13
                    B C D
14
15
                    1
                       /\
16
                    Ε
                       F G
           */
17
18
           cout <<
                                A\n"
                              / | \\
                                         n"
21
                             B C D
                                         \n''
22
                                / \\
                                         \n''
23
                             E F G
                                         \n";
24
25
           root = make_shared<TreeNode<char>>('A');
26
           root->_first_child = make_shared<TreeNode<char>>('B');
27
           root->_first_child->_first_child = make_shared<TreeNode<char>>('E');;
           root->_first_child->_next_sibling = make_shared<TreeNode<char>>('C');
28
29
           root->_first_child->_next_sibling->_next_sibling = make_shared<TreeNode<char>>('D');
30
31
           root->_first_child->_next_sibling->_next_sibling
32
                   ->_first_child = make_shared<TreeNode<char>>('F');
33
34
           root->_first_child->_next_sibling->_next_sibling
```

```
35
                     ->_first_child->_next_sibling = make_shared<TreeNode<char>>('G');
36
37
            cout << "All paths from root to leaves are as follows:\n";</pre>
38
            tree.print_path(root);
            cout << "number of tree nodes: " << tree.count_node(root) << '\n';</pre>
39
            cout << "number of tree leaves: " << tree.count_leaves(root) << '\n';</pre>
40
            cout << "depth: " << tree.depth(root) << '\n';</pre>
41
42
            cout << "preorder: "; tree.preorder(root); cout << '\n';</pre>
            cout << "postorder: "; tree.postorder(root); cout << '\n';</pre>
43
44 }
45
46 int main()
47 {
48
            tree_operations();
49
            cout << "\n\nPress any key to leave...\n";</pre>
51
            char wait;
52
            cin >> noskipws >> wait;
53
54
           return 0;
55 }
```

Listing 2: Tree test

2.3 SeqStack.h

```
1 // sequential stack header
 2 #pragma once
3 #ifndef SEQSTACK_H
4 #define SEQSTACK_H
6 #include "Stack.h"
7 #include <iostream>
8 #include <cassert>
10 const int defaultStackSize = 30;
11 const int stackIncreament = 20;
                                                  // let it double its capacity
12
13 template<typename T>
14 class SeqStack : public Stack<T> {
15 public:
           SeqStack(int sz = defaultStackSize);
           SeqStack(const SeqStack<T>& stack);
17
           SeqStack<T>& operator=(const SeqStack<T>& stack);
19
           ~SeqStack() { delete[] elem; }
20
           void push(const T& x);
21
           void pop();
22
           void pop(T& x);
23
           T& top()const;
           void clear() { _top = -1; }
24
25
           inline bool isEmpty()const { return _top == -1; }
           bool isFull()const { return _top == maxSize - 1; }
26
27
           int max_size()const { return maxSize; }
28
           inline int size()const { return _top + 1; }
29
           void bottom_up_traverse()const;
30
31 private:
```

```
// pointer to stack array
32
           T* elem;
33
           int _top;
                                                              // index of stack top: [0, size), when stack's
            \hookrightarrow empty, _top=-1
34
           int maxSize;
                                                         // maximum volume of the stack
35
           void overflowProcess();
36 };
37
38 template<typename T>
39 SeqStack<T>::SeqStack(int sz) {
                                          // construct an empty stack with a size of sz
           _{top} = -1;
40
           maxSize = sz;
41
42
           elem = new T[maxSize];
43
           assert(elem != nullptr);
44 }
45
46 template<typename T>
47 SeqStack<T>::SeqStack(const SeqStack<T>& stack) { // copy constructor
           _top = stack._top;
49
           maxSize = stack.maxSize;
50
          elem = new T[maxSize];
51
           assert(elem != nullptr);
52
           for (int i = 0; i <= _top; ++i) elem[i] = stack.elem[i];</pre>
53 }
54
55 template<typename T>
56 SeqStack<T>& SeqStack<T>::operator=(const SeqStack<T>& stack) { // copy assignment
           if (&stack == this)
57
                                     return *this;
58
           delete[] elem;
59
           _top = stack._top;
60
           maxSize = stack.maxSize;
61
           elem = new T[maxSize];
62
           assert(elem != nullptr);
63
           for (int i = 0; i <= _top; ++i) elem[i] = stack.elem[i];</pre>
64
           return *this;
65 }
66
67 template<typename T>
68 void SeqStack<T>::push(const T& x){ // add a new element at the top of the stack
69
           if (isFull()) overflowProcess();
70
           elem[++_top] = x;
71 }
72
73 template<typename T>
74 void SeqStack<T>::pop() { // pop out the top element of the stack
75
           assert(!isEmpty());
           --_top;
76
77 }
78
79 template<typename T>
80 void SeqStack<T>::pop(T& x) { // pop out the top element of the stack and assign it to x
          assert(!isEmpty());
82
           x = elem[_top--];
83 }
84
85 template<typename T>
86 T& SeqStack<T>::top() const { // get the top element
87
          assert(!isEmpty());
88
           return elem[_top];
89 }
90
91 template<typename T>
```

```
92 void SeqStack<T>::bottom_up_traverse() const
93
94
            for (int i = 0; i <= _top; ++i) {</pre>
                    std::cout << elem[i] << '\t';
95
96
97
   }
98
99 template<typename T>
100 void SeqStack<T>::overflowProcess() { // private member function, expanding the stack's size
            T* newArray = new T[maxSize += stackIncreament];
101
            assert(newArray != nullptr);
102
103
            for (int i = 0; i <= _top; ++i) newArray[i] = elem[i];</pre>
104
            delete elem;
105
            elem = newArray;
106 }
107
108 #endif // !SEQSTACK_H
```

Listing 3: Sequential stack header

2.4 Stack.h

```
1 // stack header, abstract base class for interfaces
2 #pragma once
3 #ifndef STACK_H
4 #define STACK_H
6 template<typename T>
7 class Stack {
8 public:
          virtual void push(const T& x) = 0;
9
          virtual void pop() = 0;
10
          virtual void pop(T& x) = 0;
11
          virtual T& top()const = 0;
12
          virtual void clear() = 0;
13
          virtual bool isEmpty()const = 0;
14
15
          virtual int size()const = 0;
16 };
17
18 #endif // !STACK_H
```

Listing 4: Stack header

3 Output

```
Microsoft Visual Studio Debug Console
                                                                                                                                                                       D
                        G
All paths from root to leaves are as follows:
            В
                       Ε
number of tree nodes: 7
number of tree leaves: 4
depth: 3
preorder: ABECDFG
postorder: EBCFGDA
Destructing tree node with value A
Destructing tree node with value B
Destructing tree node with value C
Destructing tree node with value D
Destructing tree node with value D
Destructing tree node with value G
Destructing tree node with value G
Press any key to leave...
D:\src\VS files\VC\DataStructures\Tree\Debug\Tree.exe (process 15476) exited with code 0.
Press any key to close this window . . .
```

Figure 1: Tree test in Win10

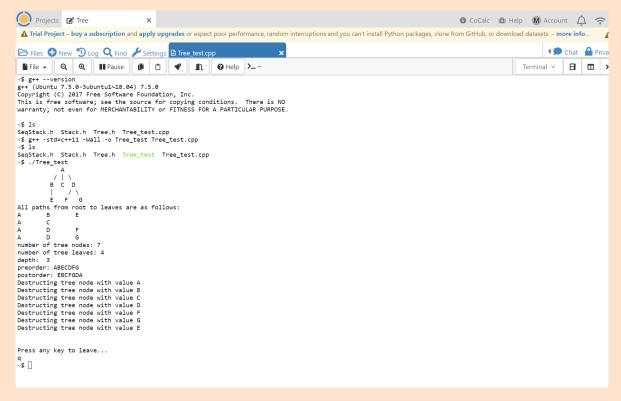


Figure 2: Tree test in Ubuntu

4 Appendix



Hello from the Beatles.