Index of programming contest code library

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Arithmetic:
  bigint:
    Big (signed) integer arithmetic
  bignumber.java:
    Java template for using large integer arithmetic (BigInteger)
  binomial:
    Computes binomial coefficients
  cra:
    Chinese remainder theorem
  diophantine_sys:
    Linear system of diophantine equations (works for single equation too!)
  euclid:
    Euclidean algorithm
  eulerphi:
    Computes the Euler phi (totient) function: given a positive n, return
    the number of integers between 1 and n relatively prime to n.
  exteuclid:
    Extended Euclidean algorithm
  exp:
    Fast exponentiation
  expmod:
    Fast exponentiation mod m
  factor:
    Integer prime factorization
  factor_large:
    Integer prime factorization for larger integers (>= 2^40)
  fflinsolve:
    Fraction-free solution of linear systems of equations (for systems
    with integer coefficients)
  fib:
    Computes n-th Fibonacci number with O(log n) complexity
  frac2dec:
    Obtain the decimal representation of a fraction.
  fraction:
    A rational number class.
  infix:
    Parses and evaluates infix arithmetic expressions.
  int_mult:
    Multiply integer factors on the numerator, divide by the integer
    factors in the denominator without overflow.
  linsolve:
    Solves linear systems of equations with LU decomposition.
  mult:
    Multiply factors on the numerator, divide by the factors in the
    denominator without overflow.
  ratlinsolve:
    Rational solution of linear systems of equations (can be solved by
    fflinsolve as well).
  roman_numerals
    Converts between Arabic and Roman numerals.

Geometric (mostly 2-D):
  areapoly:
    Computes the signed area of a simple (no self-intersection) polygon.
  ccw:
    Determines the orientation of 3 points (counterclockwise, clockwise,
    undefined).
  circle_3pts:
    Computes the center and radius of a circle given 3 points.
  convex_hull:
    Computes the convex hull of a list of points.
  dist3D:
    Computes the distance between two points, a point and a line segment,
    two line segments, or a point and a triangle in 3D. There are also
    corresponding versions for infinite lines and infinite planes.

  dist_line:
    Computes the distance of a point to a line.
  greatcircle:
    Computes the distance between two points on a sphere along the surface.
    Also has routines to convert between Cartesian coordinates and
    spherical coordinates.
  heron:
    Computes the area of a triangle given the lengths of 3 sides.
  intersect_circle_circle:
    Computes the intersection of two circles.
  intersectTF:
    Given two line segments, return whether they intersect or not (but
    doesn't return the point of intersection)
  intersect_line:
    Given two 2-D line segments, return whether they intersect or not, and
    return the point of intersection if there is a unique one.
  intersect_iline:
    Given two 2-D lines (infinite), return whether they intersect or not,
    and return the point of intersection if there is a unique one.
  intersect_iline_circle:
    Given an infinite 2-D line and a circle, return whether they intersect
    and also the point(s) of intersection.
  pointpoly:
    Given a polygon and a point, determines whether the point is in the
    polygon. The behaviour when the point is on the boundary is left to
    the user.
  polygon_inter:
    Given two convex polygons, compute their intersection as another
    polygon.

Graph:
  bellmanford:
    Computes the shortest distance from one vertex to all other
    vertices. Also computes the paths. It is slow (O(n^3)) but
    handles negative weights. Can also be used to detect negative
    cycles.
  bfs_path:
    Computes the shortest distance from one vertex to all other
    vertices. Also computes the paths. The edges in the graph must
    have equal cost.
  bicomp:
    Finds the biconnected components and articulation points of a graph.
  dijkstra:
    Computes the shortest distance from one vertex to all other
    vertices. Also computes the paths.
  dijkstra_sparse:
    Same as dijkstra but for sparse graphs. Complexity O((n+m) log(n+m)).
  eulertour:
    Determines if there is an Eulerian tour in the graph. If so,
    find one.
  floyd:
    Computes the shortest distance between any two vertices.
  floyd_path:
    Like floyd, but also stores the paths.
  hungarian:
    Maximum/minimum weight bipartite matching. O(N^3).
  matching:
    Compute unweighted matching of bipartite graphs. (Matthew)
  mst:
    Compute the minimum spanning tree.
  mincostmaxflowdense:
    Compute the minimum cost maximum flow in a network. Good for
    dense graphs when maximum flow is small. Complexity is O(n^2 * flow).
  mincostmaxflowsparse:
    Compute the minimum cost maximum flow in a network. Good for
    sparse graphs when maximum flow is small. Complexity is
    O(m log(m) * flow).
  networkflow:
    Compute the maximum flow in a network. Uses Ford-Fulkerson

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```
      with complexity O(fm) where f is the value of the maximum flow
      and m is the number of edges.  Good for sparse graphs where
      the maximum flow is small.
    networkflow2:
      Compute the maximum flow in a network.  Uses relabel-to-front
      with complexity O(n^3).  Good for dense (but small) graphs
      where the maximum flow is large.
    scc:
      Compute the strongly connected components (and possibly the
      compressed graph) of a directed graph.
    top_sort:
      Topological sort on directed acyclic graph (or detect if a
      cycle exists). O(n+m)

Data Structures:
    fenwicktree:
      A data structure that supports the maintainence of cumulative sums
      in an array dynamically.  Most operations can be done in O(log N)
      time where N is the number of elements.

    suffixarray:
      An O(n) algorithm to construct a suffix array (and longest
      common prefix information) from a string.

Miscellaneous:
    asc_subseq:
      Longest (strictly) ascending/decreasing subsequence.
    binsearch:
      Binary search that also returns the position to insert an
      element if it is not found.
    common_subseq:
      Find the longest common subsequence of the two sequences.
    date:
      A class for dealing with dates in the Gregorian calendar.
    dow:
      Computing the day of the week.
    josephus:
      Finding the last survivor and killing order of the Josephus problem.
    kmp:
      Linear time string searching routines.
    int_prog:
      Integer programming.
    simplex:
      Linear programming by simplex algorithm.
    str_rotation_period:
      Computes the lexicographically least rotation of a string, as well
      as its period.
    unionfind:
      Union-find implementation to compute equivalence classes.
    vecsum:
      Find the contiguous subvector that gives the largest sum.
    zero_one:
      Zero-one programming.
```

```cpp
// 2SAT solver: returns T/F whether it is satisfiable -- O(n+m)
//   - use NOT() to negate a variable (works on negated ones too!)
//   - ALWAYS use VAR() to talk about the non-negated version of the var i
//   - use add_clause to add a clause
//   - one possible satisfying assignment is returned in val[], if
//     it exists
//   - To FORCE i to be true:  add_clause(G,VAR(i),VAR(i));
//   - To implement XOR -- say (i XOR j) :
//     add_clause(G,VAR(i),VAR(j)); add_clause(G,NOT(VAR(i)),NOT(VAR(j)));
//     NOTE: val[] is indexed by i for var i, not by VAR(i)!!!

#include <iostream>
#include <algorithm>
#include <stack>
#include <cassert>
#include <vector>
using namespace std;

const int MAX_VARS = 100;          // maximum number of variables
const int MAX_NODES = 2*MAX_VARS;

struct Graph{
  int numNodes;
  vector<int> adj[MAX_NODES];
  void clear(){
    numNodes = 0;
    for(int i=0;i<MAX_NODES;i++)
      adj[i].clear();
  }
  void add_edge(int u,int v){
    if(find(adj[u].begin(),adj[u].end(),v) == adj[u].end())
      adj[u].push_back(v);
  }
};

int po[MAX_NODES],comp[MAX_NODES];
int num_scc;

void DFS(int v, const Graph& G, int& C, stack<int>& P,stack<int>& S){
  po[v] = C++;

  S.push(v);  P.push(v);
  for(unsigned int i=0;i<G.adj[v].size();i++){
    int w = G.adj[v][i];
    if(po[w] == -1){
      DFS(w,G,C,P,S);
    } else if(comp[w] == -1){
      while(!P.empty() && (po[P.top()] > po[w]))
        P.pop();
    }
  }
  if(!P.empty() && P.top() == v){
    while(!S.empty()){
      int t = S.top();
      S.pop();
      comp[t] = num_scc;
      if(t == v)
        break;
    }
    P.pop();
    num_scc++;
  }
}

int SCC(const Graph& G){
  num_scc = 0;
  int C = 1;
  stack<int> P,S;
  fill(po,po+G.numNodes,-1);
```

```cpp
  fill(comp,comp+G.numNodes,-1);
  for(int i=0;i<G.numNodes;i++)
    if(po[i] == -1)
      DFS(i,G,C,P,S);

  return num_scc;
}


int VAR(int i) { return 2*i; }
int NOT(int i) { return i ^ 1; }

void add_clause(Graph &G, int v, int w) { // adds (v || w)
  if (v == NOT(w)) return;
  G.add_edge(NOT(v), w);
  G.add_edge(NOT(w), v);
}

bool twoSAT(const Graph &G, bool val[]) {   // assumes graph is built
  SCC(G);
  for (int i = 0; i < G.numNodes; i += 2) {
    if (comp[i] == comp[i+1]) return false;
    val[i/2] = (comp[i] < comp[i+1]);
  }
  return true;
}


// Declare this as a global variable if MAX_NODES is large to
//   avoid Runtime Error.
Graph G;

int main(){
  int m,n;
  while(cin >> n >> m && (n || m)){
    G.clear();
    G.numNodes = 2*n;

    for (int i = 0; i < m; i++) {
      cout << "Enter two variables for clause (1 - " << n
           << "), negative means negated: ";
      int x, y;
      cin >> x >> y;

      int var1 = VAR(abs(x)-1), var2 = VAR(abs(y)-1);
      if (x < 0) var1 = NOT(var1);
      if (y < 0) var2 = NOT(var2);
      add_clause(G, var1, var2);
    }

    bool val[MAX_VARS];
    if (twoSAT(G, val)) {
      for (int i = 0; i < n; i++) {
        cout << val[i] << ' ';
      }
      cout << endl;
    } else {
      cout << "Impossible" << endl;
    }
  }
  return 0;
}
```

```cpp
/*
 * Area of a polygon
 *
 * Author: Howard Cheng
 * Reference:
 *   http://www.exaflop.org/docs/cgafaq/cga2.html
 *
 * This routine returns the SIGNED area of a polygon represented as an
 * array of n points (n >= 1).  The result is positive if the orientation is
 * counterclockwise, and negative otherwise.
 *
 */

#include <iostream>
#include <iomanip>
#include <cmath>
#include <cassert>

using namespace std;

struct Point {
  double x, y;
};

double area_polygon(Point polygon[], int n)
{
  double sum = 0.0;

  for (int i = 0; i < n-1; i++) {
    sum += polygon[i].x * polygon[i+1].y - polygon[i].y * polygon[i+1].x;
  }
  sum += polygon[n-1].x * polygon[0].y - polygon[n-1].y * polygon[0].x;
  return sum/2.0;
}

int main(void)
{
  Point *polygon;
  int n;

  while (cin >> n && n > 0) {
    polygon = new Point[n];
    assert(polygon);
    for (int i = 0; i < n; i++) {
      cin >> polygon[i].x >> polygon[i].y;
    }
    cout << "Area = " << fixed << setprecision(2)
         << area_polygon(polygon, n) << endl;
    delete[] polygon;
  }
  return 0;
}
```

```
/*
 * Longest Ascending Subsequence
 *
 * Author: Howard Cheng
 * Reference:
 *   Gries, D.  The Science of Programming
 *
 * Given an array of size n, asc_seq returns the length of the longest
 * ascending subsequence, as well as one of the subsequences in S.
 * sasc_seq returns the length of the longest strictly ascending
 * subsequence.  It runs in O(n log n) time.
 *
 * Also included are simplified versions when only the length is needed.
 *
 * Note: If we want to find do the same things with descending
 * subsequences, just reverse the array before calling the routines.
 *
 */


#include <iostream>
#include <algorithm>
#include <vector>
#include <cassert>

using namespace std;

int asc_seq(int A[], int n, int S[])
{
  vector<int> last(n+1), pos(n+1), pred(n);
  if (n == 0) {
    return 0;
  }

  int len = 1;
  last[1] = A[pos[1] = 0];

  for (int i = 1; i < n; i++) {
    int j = upper_bound(last.begin()+1, last.begin()+len+1, A[i]) -
      last.begin();
    pred[i] = (j-1 > 0) ? pos[j-1] : -1;
    last[j] = A[pos[j] = i];
    len = max(len, j);
  }

  int start = pos[len];
  for (int i = len-1; i >= 0; i--) {
    S[i] = A[start];
    assert(i == 0 || pred[start] < start);
    start = pred[start];
  }

  return len;
}

int asc_seq(int A[], int n)
{
  vector<int> last(n+1);
  if (n == 0) {
    return 0;
  }

  int len = 1;
  last[1] = A[0];

  for (int i = 1; i < n; i++) {
    int j = upper_bound(last.begin()+1, last.begin()+len+1, A[i]) -
      last.begin();
    last[j] = A[i];
```

```
    len = max(len, j);
  }

  return len;
}

int sasc_seq(int A[], int n, int S[])
{
  vector<int> last(n+1), pos(n+1), pred(n);
  if (n == 0) {
    return 0;
  }

  int len = 1;
  last[1] = A[pos[1] = 0];

  for (int i = 1; i < n; i++) {
    int j = lower_bound(last.begin()+1, last.begin()+len+1, A[i]) -
      last.begin();
    pred[i] = (j-1 > 0) ? pos[j-1] : -1;
    last[j] = A[pos[j] = i];
    len = max(len, j);
  }

  int start = pos[len];
  for (int i = len-1; i >= 0; i--) {
    S[i] = A[start];
    start = pred[start];
  }

  return len;
}

int sasc_seq(int A[], int n)
{
  vector<int> last(n+1);
  if (n == 0) {
    return 0;
  }

  int len = 1;
  last[1] = A[0];

  for (int i = 1; i < n; i++) {
    int j = lower_bound(last.begin()+1, last.begin()+len+1, A[i]) -
      last.begin();
    last[j] = A[i];
    len = max(len, j);
  }

  return len;
}

int main(void)
{
  int *A, *S, n, i, k;

  while (cin >> n && n > 0) {
    A = new int[n];
    S = new int[n];
    for (i = 0; i < n; i++) {
      cin >> A[i];
    }
    k = asc_seq(A, n, S);
    cout << "length = " << k << endl;
    for (i = 0; i < k; i++) {
      cout << S[i] << " ";
    }
    cout << endl;
```

```
      k = sasc_seq(A, n, S);
      cout << "length = " << k << endl;
      for (i = 0; i < k; i++) {
        cout << S[i] << " ";
      }
      cout << endl;
      delete[] A;
      delete[] S;
  }
  return 0;
}
```

```
/*
 * Bellman-Ford Shortest Path Algorithm
 *
 * Author: Howard Cheng
 *
 * Given a weight matrix representing a graph and a source vertex, this
 * algorithm computes the shortest distance, as well as path, to each
 * of the other vertices.  The paths are represented by an inverted list,
 * such that if v preceeds immediately before w in a path from the
 * source to vertex w, then the path P[w] is v.  The distances from
 * the source to v is given in D[v] (DISCONNECT if not connected).
 *
 * Call get_path to recover the path.
 *
 * Note: the Bellman-Ford algorithm has complexity O(n^3), but it works even
 *       when edges have negative weights.  As long as there are no negative
 *       cycles the computed results are correct.
 *
 *       We can make this O(n*m) if we use an adjacency list representation.
 *
 *       This works for directed graphs too.
 *
 *       You can use this to detect negative cycles too.  See code.
 *
 */

#include <iostream>
#include <climits>
#include <cassert>

using namespace std;

const int MAX_NODES = 20;
const int DISCONNECT = INT_MAX;

/* assume that D and P have been allocated */
void bellmanford(int graph[MAX_NODES][MAX_NODES], int n, int src,
                 int D[], int P[])
{
  int v, w, k;

  for (v = 0; v < n; v++) {
    D[v] = INT_MAX;
    P[v] = -1;
  }
  D[src] = 0;

  for (k = 0; k < n-1; k++) {
    for (v = 0; v < n; v++) {
      for (w = 0; w < n; w++) {
        if (graph[v][w] != DISCONNECT && D[v] != INT_MAX) {
          if (D[w] == INT_MAX || D[w] > D[v] + graph[v][w]) {
            D[w] = D[v] + graph[v][w];
            P[w] = v;
          } else if (D[w] == D[v] + graph[v][w]) {
            /* do some tie-breaking here */
          }
        }
      }
    }
  }

  /* the following loop is used only to detect negative cycles, not */
  /* needed if you don't care about this                           */
  for (v = 0; v < n; v++) {
    for (w = 0; w < n; w++) {
      if (graph[v][w] != DISCONNECT && D[v] != INT_MAX) {
        if (D[w] == INT_MAX || D[w] > D[v] + graph[v][w]) {
          /* if we get here then there is a negative cycle somewhere */
```

```
            /* on the path from src to                              */
          }
        }
      }
    }
  }
}

int get_path(int v, int P[], int path[])
{
  int A[MAX_NODES];
  int i, k;

  k = 0;
  A[k++] = v;
  while (P[v] != -1) {
    v = P[v];
    A[k++] = v;
  }
  for (i = k-1; i >= 0; i--) {
    path[k-1-i] = A[i];
  }
  return k;
}

int main(void)
{
  int m, w, num;
  int i, j;
  int graph[MAX_NODES][MAX_NODES];
  int P[MAX_NODES][MAX_NODES], D[MAX_NODES][MAX_NODES];
  int path[MAX_NODES];

  /* clear graph */
  for (i = 0; i < MAX_NODES; i++) {
    for (j = 0; j < MAX_NODES; j++) {
      graph[i][j] = DISCONNECT;
    }
  }

  /* read graph */
  cin >> i >> j >> w;
  while (!(i == -1 && j == -1)) {
    assert(0 <= i && i < MAX_NODES && 0 <= j && j < MAX_NODES);
    graph[i][j] = graph[j][i] = w;
    cin >> i >> j >> w;
  }

  for (i = 0; i < MAX_NODES; i++) {
    bellmanford(graph, MAX_NODES, i, D[i], P[i]);
  }

  /* do queries */
  cin >> i >> j;
  while (!(i == -1 && j == -1)) {
    assert(0 <= i && i < MAX_NODES && 0 <= j && j < MAX_NODES);
    cout << i << " " << j << ":" << D[i][j] << endl;
    for (m = j; m != -1; m = P[i][m]) {
      cout << " " << m;
    }
    cout << endl;
    num = get_path(j, P[i], path);
    for (m = 0; m < num; m++) {
      cout << " " << path[m];
    }
    cout << endl;
    cin >> i >> j;
  }
```

```
    return 0;
}
```

```cpp
/*
 * Shortest Path with BFS
 *
 * Author: Howard Cheng
 *
 * Given a graph represented by an adjacency list, this algorithm uses
 * BFS to find the shortest path from a source vertex to each of the
 * other vertices.  The distances from the source to v is given in D[v], and
 * D[v] is set to -1 if the source vertex is not connected to w.  Also,
 * the shortest path tree is stored in the array P.
 *
 * Call get_path to recover the path.
 *
 * Note: All edges must have the same cost for this to work.
 *       This algorithm has complexity O(n+m).
 *
 */

#include <iostream>
#include <cassert>
#include <algorithm>
#include <queue>

using namespace std;

const int MAX_NODES = 100;

struct Node {
  int deg;              /* number of outgoing edges */
  int adj[MAX_NODES];

  /* the following is not necessary, but useful in many situations */
  int cost[MAX_NODES];
};

void BFS_shortest_path(Node graph[], int n, int src, int D[], int P[])
{
  char used[MAX_NODES];
  queue<int> q;
  int i, v, w;

  fill(used, used+MAX_NODES, 0);
  q.push(src);
  used[src] = 1;

  for (i = 0; i < MAX_NODES; i++) {
    D[i] = -1;
    P[i] = -1;
  }
  D[src] = 0;

  while (!q.empty()) {
    v = q.front();
    q.pop();
    for (i = 0; i < graph[v].deg; i++) {
      w = graph[v].adj[i];
      if (!used[w]) {
        D[w] = D[v] + 1;
        P[w] = v;
        q.push(w);
        used[w] = 1;
      } else if (D[v] + 1 == D[w]) {
        /* put tie-breaker here */
        /* eg. find largest path in lexicographic order, when the path */
        /*     is considered in REVERSE!                               */
        P[w] = max(P[w], v);
      }
    }
  }
```

```cpp
}

void clear(Node graph[], int n)
{
  int i;
  for (i = 0; i < n; i++) {
    graph[i].deg = 0;
  }
}

void add_edge(Node graph[], int v, int w, int cost)
{
  int i;

  /* make sure that we have no duplicate edges */
  for (i = 0; i < graph[v].deg; i++) {
    if (graph[v].adj[i] == w) {
      assert(0);
    }
  }

  graph[v].cost[graph[v].deg] = cost;
  graph[v].adj[graph[v].deg] = w;
  graph[v].deg++;
}

int get_path(int v, int P[], int path[])
{
  int A[MAX_NODES];
  int i, k;

  k = 0;
  A[k++] = v;
  while (P[v] != -1) {
    v = P[v];
    A[k++] = v;
  }
  for (i = k-1; i >= 0; i--) {
    path[k-1-i] = A[i];
  }
  return k;
}

int main(void)
{
  int v, w, num;
  int i;
  Node graph[MAX_NODES];
  int P[MAX_NODES][MAX_NODES], D[MAX_NODES][MAX_NODES];
  int path[MAX_NODES];

  clear(graph, MAX_NODES);
  while (cin >> v >> w && v >= 0 && w >= 0) {
    add_edge(graph, v, w, 1);
  }

  for (i = 0; i < MAX_NODES; i++) {
    BFS_shortest_path(graph, MAX_NODES, i, D[i], P[i]);
  }

  while (cin >> v >> w && v >= 0 && w >= 0) {
    cout << v << " " << w << ":" << D[v][w] << endl;
    num = get_path(w, P[v], path);
    assert(D[v][w] == -1 || num == D[v][w]+1);
    for (i = 0; i < num; i++) {
      cout << " " << path[i];
    }
    cout << endl;
  }
```

```
    return 0;

}
```

```cc
/*
 * Biconnected Components
 *
 * Author: Howard Cheng
 * Date: Oct 15, 2004
 *
 * The routine bicomp() uses DFS to find the biconnected components in
 * a graph.  The graph is stored as an adjacency list.  Use clear_graph()
 * and add_edge() to build the graph.
 *
 * Note: This works only on connected graphs.  See comment below in code.
 *
 * The code simply prints the biconnected components and the articulation
 * points.  Replace the printing code to do whatever is appropriate.
 *
 * NOTE: some articulation points may be printed multiple times.
 *
 *
 */

#include <iostream>
#include <stack>
#include <algorithm>
#include <cassert>

using namespace std;

/* maximum number of nodes, maximum degree, and maximum number of edges */
const int MAX_N = 1000;
const int MAX_DEG = 4;

struct Node {
  int deg;
  int nbrs[MAX_DEG];
  int dfs, back;
};

int dfn;

void clear_graph(Node G[], int n)
{
  int i;
  for (i = 0; i < n; i++) {
    G[i].deg = 0;
  }
}

void add_edge(Node G[], int u, int v)
{
  G[u].nbrs[G[u].deg++] = v;
  G[v].nbrs[G[v].deg++] = u;
}

void do_dfs(Node G[], int v, int pred, stack<int> &v_stack,
            stack<int> &w_stack)
{
  int i, w, child = 0;

  G[v].dfs = G[v].back = ++dfn;
  for (i = 0; i < G[v].deg; i++) {
    w = G[v].nbrs[i];
    if (G[w].dfs < G[v].dfs && w != pred) {
      /* back edge or unexamined forward edge */
      v_stack.push(v);
      w_stack.push(w);
    }
    if (!G[w].dfs) {
      do_dfs(G, w, v, v_stack, w_stack);
      child++;
```

```cc
      /* back up from recursion */
      if (G[w].back >= G[v].dfs) {
        /* new bicomponent */
        cout << "edges in new biconnected component:" << endl;
        while (v_stack.top() != v || w_stack.top() != w) {
          cout << v_stack.top() << " " << w_stack.top() << endl;
          v_stack.pop();
          w_stack.pop();
        }
        cout << v_stack.top() << " " << w_stack.top() << endl;
        v_stack.pop();
        w_stack.pop();

        if (pred != -1) {
          cout << "articulation point: " << v << endl;
        }
      } else {
        G[v].back = min(G[v].back, G[w].back);
      }
    } else {
      /* w has been examined already */
      G[v].back = min(G[v].back, G[w].dfs);
    }
  }
  if (pred == -1 && child > 1) {
    cout << "articulation point: " << v << endl;
  }
}

void bicomp(Node G[], int n)
{
  int i;
  stack<int> v_stack, w_stack;

  dfn = 0;
  for (i = 0; i < n; i++) {
    G[i].dfs = 0;
  }
  do_dfs(G, 0, -1, v_stack, w_stack);

  // NOTE: if you wish to process all connected components, you can simply
  // run the following code instead of the line above:
  //
  // for (int i = 0; i < n; i++) {
  //   if (G[i].dfs == 0) {
  //     do_dfs(G, i, -1, v_stack, w_stack);
  //   }
  // }
}

int main(void)
{
  Node G[MAX_N];
  int n, m, i, u, v;

  cin >> n;
  clear_graph(G, n);
  cin >> m;
  for (i = 0; i < m; i++) {
    cin >> u >> v;
    add_edge(G, u-1, v-1);
  }
  bicomp(G, n);
  return 0;
}
```

```
/*
 * Big integer implementation
 *
 * Author: Howard Cheng
 *
 * Each digit in our representation represents LOG_BASE decimal digits
 *
 */

#include <vector>
#include <string>
#include <cstdio>
#include <cctype>
#include <iostream>
#include <algorithm>
#include <utility>
#include <cassert>

using namespace std;
using namespace std::rel_ops;

typedef long long Digit;
#define BASE 1000000000
#define LOG_BASE 9
#define FMT_STR "%lld"
#define FMT_STR0 "%09lld"

class BigInteger {
private:

  int sign;              // +1 = positive, 0 = zero, -1 = negative
  vector<Digit> mag;     // magnitude

  void normalize();

public:
  BigInteger(Digit n = 0);
  BigInteger(const string &s);    // no error checking

  long long toLongLong() const;   // convert to long long (assumes no overflow)
  string toString() const;        // convert to string

  void clear();  // set to zero

  // comparison
  bool operator<(const BigInteger &a) const;
  bool operator==(const BigInteger &a) const;
  bool isZero() const;

  // arithmetic
  BigInteger &operator+=(const BigInteger &a);
  BigInteger &operator-=(const BigInteger &a);
  BigInteger &operator*=(const BigInteger &a);
  BigInteger &operator*=(Digit a);
  BigInteger &operator<<=(Digit a);
  BigInteger &operator/=(const BigInteger &a);
  BigInteger &operator/=(Digit a);
  BigInteger &operator%=(const BigInteger &a);
  friend Digit operator%(const BigInteger &a, Digit b);

  // we have *this = b * q + r
  // r is such that 0 <= r < |b|
  void divide(const BigInteger &b, BigInteger &q, BigInteger &r) const;
  void divide(Digit b, BigInteger &q, Digit &r) const;

  // root = floor(sqrt(a)).  Returns 1 if a is a perfect square, 0 otherwise.
  // assume >= 0
  int sqrt(BigInteger &root) const;
};
```

```
BigInteger operator+(const BigInteger &a, const BigInteger &b);
BigInteger operator-(const BigInteger &a, const BigInteger &b);
BigInteger operator*(const BigInteger &a, const BigInteger &b);
BigInteger operator*(const BigInteger &a, Digit b);
BigInteger operator<<(const BigInteger &a, Digit b);
BigInteger operator/(const BigInteger &a, const BigInteger &b);
BigInteger operator/(const BigInteger &a, Digit b);
BigInteger operator%(const BigInteger &a, const BigInteger &b);
Digit operator%(const BigInteger &a, Digit b);

BigInteger power(BigInteger x, Digit y);
istream &operator>>(istream &is, BigInteger &a);
ostream &operator<<(ostream &os, const BigInteger &a);

void BigInteger::normalize()
{
  if (mag.size() == 0) {
    return;
  }
  vector<Digit>::iterator p = mag.end();
  do {
    if (*(--p) != 0) break;
  } while (p != mag.begin());
  if (p == mag.begin() && *p == 0) {
    clear();
    sign = 0;
  } else {
    mag.erase(++p, mag.end());
  }
}


BigInteger::BigInteger(Digit n)
{
  if (n == 0) {
    sign = 0;
    return;
  }
  if (n < 0) {
    sign = -1;
    n = -n;
  } else {
    sign = 1;
  }

  while (n > 0) {
    mag.push_back(n % BASE);
    n /= BASE;
  }
}


BigInteger::BigInteger(const string &s)
{
  int l = 0;
  bool zero = true;
  bool neg = false;

  clear();

  sign = 1;
  if (s[l] == '-') {
    neg = true;
    l++;
  }

  for (; l < s.length(); l++) {
    *this *= 10;
    *this += s[l] - '0';
    zero &= s[l] == '0';
```

```
  }
  if (zero) {
    clear();
  }
  if (neg) {
    sign = -1;
  }
}

long long BigInteger::toLongLong() const
{
  long long a = 0;
  for (int i = mag.size()-1; i >= 0; i--) {
    a *= BASE;
    a += mag[i];
  }
  return sign * a;
}

string BigInteger::toString() const
{
  char buffer[LOG_BASE+1];
  string s;

  if (isZero()) {
    return "0";
  } else {
    if (sign < 0) {
      s += "-";
    }
    for (int i = mag.size()-1; i >= 0; i--) {
      if (i == (int)(mag.size()-1)) {
        sprintf(buffer, FMT_STR, mag[i]);
      } else {
        sprintf(buffer, FMT_STR0, mag[i]);
      }
      s += buffer;
    }
    return s;
  }
}

void BigInteger::clear()
{
  sign = 0;
  mag.clear();
}

bool BigInteger::operator<(const BigInteger &a) const
{
  if (sign != a.sign) {
    return sign < a.sign;
  } else if (sign == 0) {
    return false;
  } else if (mag.size() < a.mag.size()) {
    return sign > 0;
  } else if (mag.size() > a.mag.size()) {
    return sign < 0;
  } else {
    for (int i = mag.size()-1; i >= 0; i--) {
      if (mag[i] < a.mag[i]) {
        return sign > 0;
      } else if (mag[i] > a.mag[i]) {
        return sign < 0;
      }
    }
    return false;
  }
}
```

```
}

bool BigInteger::operator==(const BigInteger &a) const
{
  return sign == a.sign && mag == a.mag;
}

bool BigInteger::isZero() const
{
  return sign == 0;
}

BigInteger &BigInteger::operator+=(const BigInteger &a)
{
  if (a.sign == 0) {
    return *this;
  } else if (sign == 0) {
    sign = a.sign;
    mag = a.mag;
    return *this;
  } else if (sign < 0 && a.sign > 0) {
    BigInteger b(a);
    sign = 1;
    b -= *this;
    return *this = b;
  } else if (sign > 0 && a.sign < 0) {
    BigInteger b(a);
    b.sign = 1;
    return (*this) -= b;
  } else {
    Digit carry = 0;
    unsigned int limit = max(mag.size(), a.mag.size());
    for (unsigned int i = 0; i < limit; i++) {
      Digit s1 = (i < mag.size()) ? mag[i] : 0;
      Digit s2 = (i < a.mag.size()) ? a.mag[i] : 0;
      Digit sum = s1 + s2 + carry;
      Digit result = (sum < BASE) ? sum : sum - BASE;
      carry = (sum >= BASE);
      if (i < mag.size()) {
        mag[i] = result;
      } else {
        mag.push_back(result);
      }
    }
    if (carry) {
      mag.push_back(carry);
    }
    return *this;
  }
}

BigInteger &BigInteger::operator-=(const BigInteger &a)
{
  if (a.sign == 0) {
    return *this;
  } else if (sign == 0) {
    sign = -a.sign;
    mag = a.mag;
    return *this;
  } else if (sign != a.sign) {
    BigInteger b(a);
    b.sign *= -1;
    return *this += b;
  } else if (sign < 0) {
    BigInteger b(a);
    b.sign *= -1;
    sign *= -1;
    b -= *this;
    return *this = b;
```

```
  } else {
    if (*this == a) {
      clear();
      return *this;
    } else if (*this < a) {
      BigInteger b(a);
      b -= *this;
      b.sign *= -1;
      return *this = b;
    } else {
      // we know that *this > a
      unsigned int limit = mag.size();
      Digit borrow = 0;
      for (unsigned int i = 0; i < limit; i++) {
        Digit s1 = mag[i];
        Digit s2 = (i < a.mag.size()) ? a.mag[i] : 0;
        Digit diff = s1 - s2 - borrow;
        mag[i] = (diff >= 0) ? diff : diff + BASE;
        borrow = (diff < 0);
      }
      normalize();
      return *this;
    }
  }
}

BigInteger &BigInteger::operator*=(const BigInteger &a)
{
  BigInteger temp(*this);
  BigInteger c;

  if (this == &a) {
    c = a;              // make a copy to prevent clobbering it
  }

  const BigInteger &b = (this == &a) ? c : a;

  clear();
  if (b.sign) {
    for (unsigned int i = 0; i < b.mag.size(); i++) {
      if (b.mag[i] != 0) {
        *this += (temp * b.mag[i]);
      }
      temp <<= 1;
    }
    sign *= b.sign;
  }
  return *this;
}

BigInteger &BigInteger::operator*=(Digit a)
{
  if (a <= -BASE || a >= BASE) {
    BigInteger b(a);
    return (*this *= b);
  }

  if (isZero()) {
    return *this;
  } else if (a == 0) {
    clear();
    return *this;
  } else if (a < 0) {
    sign *= -1;
    a = -a;
  }

  Digit carry = 0;
  for (unsigned int i = 0; i < mag.size(); i++) {
```

```
    Digit prod = a * mag[i];
    mag[i] = (carry + prod) % BASE;
    carry = (carry + prod) / BASE;
  }
  if (carry) {
    mag.push_back(carry);
  }
  return *this;
}

BigInteger &BigInteger::operator<<=(Digit a)
{
  assert(a >= 0);
  if (sign) {
    while (a-- > 0) {
      mag.insert(mag.begin(), 0);
    }
  }
  return *this;
}

BigInteger &BigInteger::operator/=(const BigInteger &a)
{
  BigInteger temp(*this), r;
  temp.divide(a, *this, r);
  return *this;
}

BigInteger &BigInteger::operator/=(Digit a)
{
  BigInteger temp(*this);
  Digit r;
  temp.divide(a, *this, r);
  return *this;
}

BigInteger &BigInteger::operator%=(const BigInteger &a)
{
  BigInteger temp(*this), q;
  temp.divide(a, q, *this);
  return *this;
}

void BigInteger::divide(const BigInteger &b, BigInteger &q,
                        BigInteger &r) const
{
  // reference Knuth v.2 Algorithm D

  assert(!b.isZero());

  if (b.mag.size() == 1) {
    Digit r2;
    divide(b.sign*b.mag[0], q, r2);
    r = r2;
    return;
  }

  r = *this;
  if (r.sign < 0) {
    r.sign = 1;
  }
  q.clear();

  int n = b.mag.size();
  int m = mag.size() - n;
  if (m >= 0) {
    BigInteger v(b);
    q.mag.resize(m+1);
    q.sign = 1;
```

```cpp
  // D1: normalize
  Digit d = BASE / (v.mag[n-1] + 1);  // Book is wrong.  See errata on web
  r *= d;
  v *= d;
  while ((int)r.mag.size() < m+n+1) {
    r.mag.push_back(0);
  }


  // loop
  for (int j = m; j >= 0; j--) {
    // D3: calculate q2
    Digit t = r.mag[j+n] * BASE + r.mag[j+n-1];
    Digit q2 = t / v.mag[n-1];
    Digit r2 = t - q2 * v.mag[n-1];
    if (q2 == BASE || q2 * v.mag[n-2] > BASE * r2 + r.mag[j+n-2]) {
      q2--;
      r2 += v.mag[n-1];
      if (r2 < BASE &&
          (q2 == BASE || q2 * v.mag[n-2] > BASE * r2 + r.mag[j+n-2])) {
        q2--;
        r2 += v.mag[n-1];
      }
    }

    // D4: multiply and subtract
    Digit carry, borrow, diff;
    carry = borrow = 0;
    for (int i = 0; i <= n; i++) {
      t = q2 * ((i < n) ? v.mag[i] : 0) + carry;
      carry = t / BASE;
      t %= BASE;
      diff = r.mag[j+i] - t - borrow;
      r.mag[j+i] = (diff >= 0 || i == n) ? diff : diff + BASE;
      borrow = (diff < 0);
    }

    // D5: test remainder
    q.mag[j] = q2;
    if (r.mag[n+j] < 0) {
      // D6: add back
      q.mag[j]--;
      carry = 0;
      for (int i = 0; i < n; i++) {
        t = r.mag[j+i] + v.mag[i] + carry;
        r.mag[j+i] = (t < BASE) ? t : t - BASE;
        carry = (t >= BASE);
      }
      r.mag[j+n] += carry;
    }
  }

  q.normalize();
  r.normalize();

  // D8: unnormalize
  r /= d;
}

// normalize
if (sign < 0 && b.sign > 0) {
  q.sign *= -1;
  r *= -1;
  if (!r.isZero()) {
    r += b;
    q -= 1;
  }
} else if (sign > 0 && b.sign < 0) {
```

```cpp
    q.sign *= -1;
  } else if (sign < 0 && b.sign < 0 && !r.isZero()) {
    r += b;
    r *= -1;
    q += 1;
  }
}

void BigInteger::divide(Digit b, BigInteger &q, Digit &r) const
{
  if (b <= -BASE || b >= BASE) {
    BigInteger bb(b), rr;
    divide(bb, q, rr);
    r = rr.toLongLong();
    return;
  }

  int bsign = 1;
  if (b < 0) {
    b *= -1;
    bsign = -1;
  }
  q.clear();

  r = 0;
  for (int i = mag.size()-1; i >= 0; i--) {
    Digit t = r * BASE + mag[i];
    if (t / b > 0) {
      q.sign = 1;
    }
    q.mag.insert(q.mag.begin(), t / b);
    r = t - q.mag[0] * b;
  }

  // normalize
  q.normalize();

  if (sign < 0 && bsign > 0) {
    q.sign *= -1;
    r *= -1;
    if (r) {
      r += b;
      q -= 1;
    }
  } else if (sign > 0 && bsign < 0) {
    q.sign *= -1;
  } else if (sign < 0 && bsign < 0 && r) {
    r = b - r;
    q += 1;
  }
}

int BigInteger::sqrt(BigInteger &root) const
{
  assert(sign >= 0);
  root.clear();
  if (sign == 0) {
    return 1;
  }

  // figure out how many digits there are
  BigInteger x, r, t2;
  r.sign = 1;
  int d = mag.size();

  int root_d = (d % 2) ? (d+1)/2 : d / 2;

  if (d % 2) {
    r.mag.resize(1);
```

```
      r.mag[0] = mag[--d];
    } else {
      r.mag.resize(2);
      r.mag[1] = mag[--d];
      r.mag[0] = mag[--d];
    }

    root.sign = 1;

    // figure out one digit at a time
    for (int k = root_d - 1; k >= 0; k--) {
      // invariant: result is the sqrt (integer part) of the digits processed
      // so far

      // look for next digit in result by binary search
      x = root * 2;
      x <<= 1;
      Digit t;

      Digit lo = 0, hi = BASE;
      while (hi - lo > 1) {
        Digit mid = (lo + hi) / 2;
        x.mag[0] = t = mid;
        t2 = x * t;
        if (t2 < r || t2 == r) {
          lo = mid;
        } else {
          hi = mid;
        }
      }
      root <<= 1;
      root.mag[0] = lo;

      // form the next r
      x.mag[0] = t = lo;
      t2 = x * t;
      r -= t2;
      r <<= 1;
      r += (d > 0) ? mag[--d] : 0;
      r <<= 1;
      r += (d > 0) ? mag[--d] : 0;
    }

    return r.isZero();
}

BigInteger operator+(const BigInteger &a, const BigInteger &b)
{
    BigInteger r(a);
    r += b;
    return r;
}

BigInteger operator-(const BigInteger &a, const BigInteger &b)
{
    BigInteger r(a);
    r -= b;
    return r;
}

BigInteger operator*(const BigInteger &a, const BigInteger &b)
{
    BigInteger r(a);
    r *= b;
    return r;
}

BigInteger operator*(const BigInteger &a, Digit b)
{
```

```
    BigInteger r(a);
    r *= b;
    return r;
}

BigInteger operator<<(const BigInteger &a, Digit b)
{
    BigInteger r(a);
    r <<= b;
    return r;
}

BigInteger operator/(const BigInteger &a, const BigInteger &b)
{
    BigInteger r(a);
    r /= b;
    return r;
}

BigInteger operator/(const BigInteger &a, Digit b)
{
    BigInteger r(a);
    r /= b;
    return r;
}

BigInteger operator%(const BigInteger &a, const BigInteger &b)
{
    BigInteger r(a);
    r %= b;
    return r;
}

Digit operator%(const BigInteger &a, Digit b)
{
    Digit r;
    if (b > 0 && b < BASE) {
        r = 0;
        for (int i = a.mag.size()-1; i >= 0; i--) {
            r = ((r * BASE) + a.mag[i]) % b;
        }
        if (a.sign < 0) {
            r = (b - r) % b;
        }
        return r;
    }

    BigInteger q;

    a.divide(b, q, r);
    return r;
}

BigInteger power(BigInteger x, Digit y)
{
    BigInteger result(1), sx(x);

    assert(y >= 0);
    while (y > 0) {
        if (y & 0x01) {
            y--;
            result *= sx;
        } else {
            sx *= sx;
            y >>= 1;
        }
    }
    return result;
}
```

```
istream &operator>>(istream &is, BigInteger &a)
{
  string s;
  char c = ' ';

  is.get(c);

  while (!is.eof() && isspace(c)) {
    is.get(c);
  }
  if (is.eof()) {
    if (isdigit(c)) {
      a = (int)(c - '0');
      is.clear();
    }
    return is;
  }

  if (c == '-') {
    s = "-";
  } else {
    is.unget();
    if (!isdigit(c)) {
      return is;
    }
  }

  is.get(c);
  while (!is.eof() && isdigit(c)) {
    s += c;
    is.get(c);
  }
  if (!is.eof()) {
    is.unget();
  }
  a = s;
  is.clear();
  return is;
}

ostream &operator<<(ostream &os, const BigInteger &a)
{
  return (os << a.toString());
}


int main()
{
  BigInteger a, b;

  while (cin >> a >> b && (!(a == 0) || !(b == 0))) {
    cout << "a = " << a << endl;
    cout << "b = " << b << endl;
    if (!(a < 0)) {
      if (a.sqrt(b)) {
        cout << "perfect square" << endl;
      }
      cout << "sqrt(a) = " << b << endl;
    }
  }
  return 0;
}
```

```java
// Java template for using BigInteger class.
//
// Note that there is also a similar BigDecimal class which may be useful.
//
// Name of the file must be NAME.java where NAME is the class name.
//
// To compile:
//
// javac NAME.java
//
// To run:
//
// java NAME
//
//
// Note: in Java, all non-native types (including arrays) need to be
// allocated by new.  Multidimensional arrays can be allocated in one
// call.  See below.
//

// for importing IO routines
import java.io.*;
import java.util.Scanner;
import java.math.BigInteger;

class bignumber {

  // this is main
  public static void main(String argv[])
  {
    // A scanner can be used to read many different types
    Scanner sc = new Scanner(System.in);

    // checking whether there is a next token can be done before
    // actually reading it and fail (vs. I/O model in C++)
    while (sc.hasNextInt()) {
      int N = sc.nextInt();
      int K = sc.nextInt();

      // here is how to allocate two dimensional arrays
      BigInteger binom[][] = new BigInteger[N+1][N+1];
      for (int n = 0; n <= N; n++) {
        // here is how you construct from an integer.
        binom[n][0] = binom[n][n] = BigInteger.valueOf(1);
        for (int k = 1; k < n; k++) {
          binom[n][k] = binom[n-1][k-1].add(binom[n-1][k]);
        }
      }


      // to print something, use System.out.println().
      // Arguments are strings (in double quotes), and most data types
      // can be converted to strings and concatenated.
      //
      // Call it with no argument to produce a blank line, or use print()
      // to print without a trailing end-of-line
      System.out.println("C(" + N + "," + K + ")=" + binom[N][K]);
    }

    /*

    Here are a bunch of other things you can do with BigIntegers.
    Assuming a, b, c, d are BigIntegers, n is an int

    a = BigInteger.ZERO;             a = 0
    a = BigInteger.ONE;              a = 1
    a = new BigInteger("FF", 16);    a = 255
    a = sc.nextBigInteger();         cin >> a
    s = a.toString();                convert to string representation
```

```java
    s = a.toString(base);            convert to string representation in
                                     given base

    x = a.intValue();                convert to smaller types, but may
    x = a.longValue();               lose precision
    x = a.floatValue();
    x = a.doubleValue();

    a = b.abs();                     a = |b|
    n = a.signum();                  n = 0, +1, -1 depending on sign of a

    a = b.negate();                  a = -b;
    a = b.add(c);                    a = b+c
    a = b.subtract(c);               a = b-c
    a = b.multiply(c);               a = b*c
    a = b.divide(c);                 a = b/c
    a = b.remainder(c);              a = b%c
    a = b.mod(c);                    a = b%c, but c must be positive
                                             and a >= 0

    if (a.compareTo(b))              -1 if a < b
                                     0 if a == b
                                     1 if a > b
    if (a.equals(b))                 true iff a == b

    a = b.min(c);                    a = min(b, c)
    a = b.max(c);                    a = max(b, c)

    a = b.pow(n);                    a = pow(b, n)
    a = b.modpow(n, c);              a = pow(b, n) mod c, c > 0

    a = b.gcd(c);                    a = gcd(|b|, |c|)
    a = b.modInverse(c);             a = b^(-1) mod c

    n = a.bitLength();               number of bits in 2's complement
                                     representation, minus the sign bit

    if (a.isProbablePrime(n))        whether a is prime, with error
                                     of (1/2)^n

    */


    System.exit(0);
  }
}
```

```cpp
// Binomial Coefficients
//
// Two ways to compute binomial coefficients:
//
//   - one way computes all binomial coefficients with n <= MAX_N O(MAX_N^2)
//   - one way computes a single binomial coefficient O(k)
//
// Author: Howard Cheng and Cody Barnson
//

#include <iostream>

using namespace std;

typedef long long ll;

// computes all binomial coefficients up to MAX_N.  Read them off the table
// after calling precomp().  O(MAX_N^2)
const int MAX_N = 10;
ll binom[MAX_N+1][MAX_N+1];
void precomp()
{
  for (int n = 0; n <= MAX_N; n++) {
    binom[n][0] = binom[n][n] = 1;
    for (int k = 1; k < n; k++) {
      binom[n][k] = binom[n-1][k] + binom[n-1][k-1];
    }
  }
}

// computes single binomial coefficient C(n, k)   O(k)
ll binom(int n, int k)
{
  if (k == 0 || k == n) return 1;
  k = min(k, n - k);
  ll ans = 1;
  for (ll i = 1; i <= k; i++) {
    ans *= (n - k + i);
    ans /= i;
  }
  return ans;
}
```

```cpp
/*
 * Binary Search
 *
 * Author: Howard Cheng
 *
 * Note: you may wish to use the STL functions lower_bound and upper_bound
 * instead.
 *
 * Given a sorted array A of size n, it tries to find an item x in the
 * the array using binary search.  The function returns non-zero if
 * x is found, and zero otherwise.  Furthermore, if it is found, then
 * A[index] = x.  If it is not found, then index is the place x should
 * be inserted into A.
 *
 * ie.  A[i] <= x          for 0 <= i < index
 *           x < A[i]       for index <= i < n
 *
 * This routine is written for integer arrays, but can be adapted to
 * other types by changing the comparison operator.
 *
 * There is also an insert routine here that will insert the element into
 * the right place after the array has been reallocated (if necessary) to
 * store n+1 elements.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

bool bin_search(const int A[], int n, int x, int &index)
{
    int l, u, m;

    if (n <= 0 || x < A[0]) {  // check the first element, but only if it exists
        index = 0;
        return false;
    }
    if (A[n-1] < x) {
        index = n;
        return false;
    }
    if (x == A[n-1]) {
        index = n-1;
        return true;
    }
    l = 0;
    u = n-1;
    while (l+1 < u) {
        assert(A[l] <= x && x < A[u]);
        m = (l+u)/2;
        if (A[m] <= x) {
            l = m;
        } else {
            u = m;
        }
    }
    if (A[l] == x) {
        index = l;
        return true;
    } else {
        index = u;
        return false;
    }
}

void insert(int A[], int n, int x, int index)
{
```

```cpp
    int i;
    for (i = n-1; i >= index+1; i--) {
        A[i] = A[i-1];
    }
    A[index] = x;
}


int main(void)
{
    int A[10000];
    int n, i, x, index;

    // implements binary insertion sort, but only keeps the unique elements
    n = 0;
    while (cin >> x && n < 10000) {
        if (!bin_search(A, n, x, index)) {
            n++;
            insert(A, n, x, index);
        }
        cout << "List:";
        for (i = 0; i < n; i++) {
            cout << " " << A[i];
            if (i == index) {
                cout << "*";            // show which one is just inserted
            }
        }
        cout << endl;
    }
    return 0;
}
```

```cpp
/*
 * Orientation analysis
 *
 * Author: Howard Cheng
 * Reference:
 *   http://wilma.cs.brown.edu/courses/cs016/packet/node18.html
 *
 * Given three points a, b, c, it returns whether the path from a to b to c
 * is counterclockwise, clockwise, or undefined.
 *
 * Undefined is returned if the 3 points are colinear, and c is between
 * a and b.
 */

#include <iostream>
#include <cmath>

using namespace std;

/* how close to call equal */
const double EPSILON = 1E-8;

struct Point {
  double x, y;
};

/* counterclockwise, clockwise, or undefined */
enum Orientation {CCW, CW, CNEITHER};

Orientation ccw(Point a, Point b, Point c)
{
  double dx1 = b.x - a.x;
  double dx2 = c.x - b.x;
  double dy1 = b.y - a.y;
  double dy2 = c.y - b.y;
  double t1 = dy2 * dx1;
  double t2 = dy1 * dx2;

  if (fabs(t1 - t2) < EPSILON) {
    if (dx1 * dx2 < 0 || dy1 * dy2 < 0) {
      if (dx1*dx1 + dy1*dy1 >= dx2*dx2 + dy2*dy2 - EPSILON) {
        return CNEITHER;
      } else {
        return CW;
      }
    } else {
      return CCW;
    }
  } else if (t1 > t2) {
    return CCW;
  } else {
    return CW;
  }
}

int main(void)
{
  Point a, b, c;
  Orientation res;

  while (cin >> a.x >> a.y >> b.x >> b.y >> c.x >> c.y) {
    res = ccw(a,b,c);
    if (res == CW) {
      cout << "CW" << endl;
    } else if (res == CCW) {
      cout << "CCW" << endl;
    } else if (res == CNEITHER) {
      cout << "CNEITHER" << endl;
    } else {
```

```cpp
      printf("Help, I am in trouble!\n");
      exit(1);
    }
  }
  return 0;
}
```

```cpp
/*
 * Parameters of circle from 3 points
 *
 * Author: Howard Cheng
 * Reference:
 *   http://www.exaflop.org/docs/cgafaq/
 *
 * This routine computes the parameters of a circle (center and radius)
 * from 3 points.  Returns non-zero if successful, zero if the three
 * points are colinear.
 *
 */

#include <iostream>
#include <iomanip>
#include <cmath>
#include <cassert>

using namespace std;

/* how close to call equal */
const double EPSILON = 1E-8;

struct Point {
  double x, y;
};

int circle(Point p1, Point p2, Point p3, Point &center, double &r)
{
  double a,b,c,d,e,f,g;

  a = p2.x - p1.x;
  b = p2.y - p1.y;
  c = p3.x - p1.x;
  d = p3.y - p1.y;
  e = a*(p1.x + p2.x) + b*(p1.y + p2.y);
  f = c*(p1.x + p3.x) + d*(p1.y + p3.y);
  g = 2.0*(a*(p3.y - p2.y) - b*(p3.x - p2.x));
  if (fabs(g) < EPSILON) {
    return 0;
  }
  center.x = (d*e - b*f) / g;
  center.y = (a*f - c*e) / g;
  r = sqrt((p1.x-center.x)*(p1.x-center.x) + (p1.y-center.y)*(p1.y-center.y));
  return 1;
}

int main(void)
{
  Point a, b, c, center;
  double r;

  while (cin >> a.x >> a.y >> b.x >> b.y >> c.x >> c.y) {
    if (circle(a, b, c, center, r)) {
      cout << fixed << setprecision(3);
      cout << "center=(" << center.x << "," << center.y << ")" << endl;
      cout << "radius = " << r << endl;
    } else {
      cout << "colinear" << endl;
    }
  }
  return 0;
}
```

```
/*
 * Longest common subsequence
 *
 * Author: Howard Cheng
 * Reference:
 *    http://www.ics.uci.edu/~eppstein/161/960229.html
 *
 * Given two arrays A and B with sizes n and m respectively, compute the
 * length of the longest common subsequence.  It also returns in s a longest
 * common subsequence (it may not be unique).  One can specify which one
 * to choose when multiple longest common subsequences exist.
 *
 * Running time and space requirement is O(mn).
 *
 */

#include <iostream>
#include <algorithm>
#include <cassert>

using namespace std;

const int MAX_LEN = 20;

int LCS(int A[], int n, int B[], int m, int s[])
{
  int L[MAX_LEN+1][MAX_LEN+1];
  int i, j, k;

  for (i = n; i >= 0; i--) {
    for (j = m; j >= 0; j--) {
      if (i == n || j == m) {
        L[i][j] = 0;
      } else if (A[i] == B[j]) {
        L[i][j] = 1 + L[i+1][j+1];
      } else {
        L[i][j] = max(L[i+1][j], L[i][j+1]);
      }
    }
  }

  /* the following is not needed if you are not interested in the sequence */
  k = 0;
  i = j = 0;
  while (i < n && j < m) {
    if (A[i] == B[j]) {
      s[k++] = A[i];
      i++;
      j++;
    } else if (L[i+1][j] > L[i][j+1]) {
      i++;
    } else if (L[i+1][j] < L[i][j+1]) {
      j++;
    } else {
      /* put tie-breaking conditions here */

      /* eg. pick the one that starts at the first one the earliest */
      j++;
    }
  }
  return L[0][0];
}

int main(void)
{
  int A[MAX_LEN], B[MAX_LEN], s[MAX_LEN];
  int m, n, i, l;

  while (cin >> n >> m && 1 <= n && 1 <= m &&
```

```
         n <= MAX_LEN && m <= MAX_LEN) {
    for (i = 0; i < n; i++) {
      cin >> A[i];
    }
    for (i = 0; i < m; i++) {
      cin >> B[i];
    }
    l = LCS(A, n, B, m, s);
    for (i = 0; i < l; i++) {
      cout << s[i] << " ";
    }
    cout << endl << "Len = " << l << endl;
  }
  return 0;
}
```

```
/*
 * Convex hull
 *
 * Author: Howard Cheng
 * Reference:
 *    http://wilma.cs.brown.edu/courses/cs016/packet/node25.html
 *
 * Given a list of n (n >= 1) points in an array, it returns the vertices of
 * the convex hull in counterclockwise order.  Also returns the number of
 * vertices in the convex hull.  Assumes that the hull array has been
 * allocated to store the right number of elements (n elements is safe).
 * The points in the original polygon will be re-ordered.
 *
 * Note: The hull contains a maximum number of points.  ie. all colinear
 *       points and non-distinct points are included in the hull.
 *
 */

#include <iostream>
#include <iomanip>
#include <cmath>
#include <algorithm>
#include <cassert>

using namespace std;

/* how close to call equal */
const double EPSILON = 1E-8;

struct Point {
  double x, y;

  bool operator<(const Point &p) const {
    return y < p.y || (y == p.y && x < p.x);
  }

};

/* counterclockwise, clockwise, or undefined */
enum Orientation {CCW, CW, CNEITHER};

/* Global point for computing convex hull */
Point start_p, max_p;

bool colinear(Point a, Point b, Point c)
{
  double dx1 = b.x - a.x;
  double dx2 = c.x - b.x;
  double dy1 = b.y - a.y;
  double dy2 = c.y - b.y;
  double t1 = dy2 * dx1;
  double t2 = dy1 * dx2;
  return fabs(t1 - t2) < EPSILON;
}

Orientation ccw(Point a, Point b, Point c)
{
  double dx1 = b.x - a.x;
  double dx2 = c.x - b.x;
  double dy1 = b.y - a.y;
  double dy2 = c.y - b.y;
  double t1 = dy2 * dx1;
  double t2 = dy1 * dx2;

  if (fabs(t1 - t2) < EPSILON) {
    if (dx1 * dx2 < 0 || dy1 * dy2 < 0) {
      if (dx1*dx1 + dy1*dy1 >= dx2*dx2 + dy2*dy2 - EPSILON) {
        return CNEITHER;
      } else {
```

```
        return CW;
      }
    } else {
      return CCW;
    }
  } else if (t1 > t2) {
    return CCW;
  } else {
    return CW;
  }
}

bool ccw_cmp(const Point &a, const Point &b)
{
  return ccw(start_p, a, b) == CCW;
}

bool sort_cmp(const Point &a, const Point &b)
{
  if (colinear(start_p, a, max_p) && colinear(start_p, b, max_p)) {
    double dx1 = abs(start_p.x - a.x);
    double dx2 = abs(start_p.x - b.x);
    double dy1 = abs(start_p.y - a.y);
    double dy2 = abs(start_p.y - b.y);
    return dx1 > dx2 || (dx1 == dx2 && dy1 > dy2);
  } else {
    return ccw(start_p, a, b) == CCW;
  }
}

int convex_hull(Point polygon[], int n, Point hull[]) {
  int count, best_i, i;

  sort(polygon, polygon+n);
  for (int i = n-1; i >= 1; i--) {
    if (fabs(polygon[i].x - polygon[i-1].x) < EPSILON &&
        fabs(polygon[i].y - polygon[i-1].y) < EPSILON) {
      for (int j = i; j < n-1; j++) {
        polygon[j] = polygon[j+1];
      }
      n--;
    }
  }

  assert(n > 0);

  if (n == 1) {
    hull[0] = polygon[0];
    return 1;
  }

  /* find the first point: min y, and then min x */
  best_i = min_element(polygon, polygon+n) - polygon;
  swap(polygon[0], polygon[best_i]);
  start_p = polygon[0];

  /* find the maximum angle wrt start_p and positive x-axis */
  best_i = 1;
  for (i = 2; i < n; i++) {
    if (ccw_cmp(polygon[best_i], polygon[i])) {
      best_i = i;
    }
  }
  max_p = polygon[best_i];

  /* get simple closed polygon */
  sort(polygon+1, polygon+n, sort_cmp);

  /* do convex hull */
```

```
   count = 0;
   hull[count] = polygon[count]; count++;
   hull[count] = polygon[count]; count++;
   for (i = 2; i < n; i++) {
      while (count > 1 &&
             ccw(hull[count-2], hull[count-1], polygon[i]) == CW) {
         /* pop point */
         count--;
      }
      hull[count++] = polygon[i];
   }
   return count;
}

int main(void)
{
   Point *polygon, *hull;
   int n, hull_size;
   int i;

   while (cin >> n && n > 0) {
      polygon = new Point[n];
      hull = new Point[n];
      assert(polygon && hull);
      for (i = 0; i < n; i++) {
         cin >> polygon[i].x >> polygon[i].y;
      }
      hull_size = convex_hull(polygon, n, hull);
      cout << "Sorted:" << endl;
      for (i = 0; i < n; i++) {
         cout << fixed << setprecision(2);
         cout << "(" << polygon[i].x << "," << polygon[i].y << ")" << endl;
      }
      cout << endl;
      cout << "Hull size = " << hull_size << endl;
      for (i = 0; i < hull_size; i++) {
         cout << "(" << hull[i].x << "," << hull[i].y << ")" << endl;
      }
      cout << endl;
      delete[] polygon;
      delete[] hull;
   }
   return 0;
}
```

```
/*
 * Chinese Remainder Theorem
 *
 * Author: Howard Cheng
 * Reference:
 *   Geddes, K.O., Czapor, S.R., and Labahn, G.  Algorithms for Computer
 *   Algebra, Kluwer Academic Publishers, 1992, p. 180
 *
 * Given n relatively prime modular in m[0], ..., m[n-1], and right-hand
 * sides a[0], ..., a[n-1], the routine solves for the unique solution
 * in the range 0 <= x < m[0]*m[1]*...*m[n-1] such that x = a[i] mod m[i]
 * for all 0 <= i < n.  The algorithm used is Garner's algorithm, which
 * is not the same as the one usually used in number theory textbooks.
 *
 * It is assumed that m[i] are positive and pairwise relatively prime.
 * a[i] can be any integer.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

int gcd(int a, int b, int &s, int &t)
{
  int r, r1, r2, a1, a2, b1, b2, q;
  int A = a;
  int B = b;

  a1 = b2 = 1;
  a2 = b1 = 0;

  while (b) {
    assert(a1*A + a2*B == a);
    q = a / b;
    r = a % b;
    r1 = a1 - q*b1;
    r2 = a2 - q*b2;
    a = b;
    a1 = b1;
    a2 = b2;
    b = r;
    b1 = r1;
    b2 = r2;
  }

  s = a1;
  t = a2;
  assert(a >= 0);
  return a;
}

int cra(int n, int m[], int a[])
{
  int x, i, k, prod, temp;
  int *gamma, *v;

  gamma = new int[n];
  v = new int[n];
  assert(gamma && v);

  /* compute inverses */
  for (k = 1; k < n; k++) {
    prod = m[0] % m[k];
    for (i = 1; i < k; i++) {
      prod = (prod * m[i]) % m[k];
    }
    gcd(prod, m[k], gamma[k], temp);
```

```
    gamma[k] %= m[k];
    if (gamma[k] < 0) {
      gamma[k] += m[k];
    }
  }

  /* compute coefficients */
  v[0] = a[0];
  for (k = 1; k < n; k++) {
    temp = v[k-1];
    for (i = k-2; i >= 0; i--) {
      temp = (temp * m[i] + v[i]) % m[k];
      if (temp < 0) {
        temp += m[k];
      }
    }
    v[k] = ((a[k] - temp) * gamma[k]) % m[k];
    if (v[k] < 0) {
      v[k] += m[k];
    }
  }

  /* convert from mixed-radix representation */
  x = v[n-1];
  for (k = n-2; k >= 0; k--) {
    x = x * m[k] + v[k];
  }

  delete[] gamma;
  delete[] v;

  return x;
}


int main(void)
{
  int n, *m, *a, i, x;

  while (cin >> n && n > 0) {
    m = new int[n];
    a = new int[n];
    assert(m && a);
    cout << "Enter moduli:" << endl;
    for (i = 0; i < n; i++) {
      cin >> m[i];
    }
    cout << "Enter right-hand side:" << endl;
    for (i = 0; i < n; i++) {
      cin >> a[i];
    }
    x = cra(n, m, a);
    cout << "x = " << x << endl;

    for (i = 0; i < n; i++) {
      assert((x-a[i]) % m[i] == 0);
    }

    delete[] m;
    delete[] a;
  }
  return 0;
}
```

```cpp
//
// Date class
//
// This is an implementation of some common functionalities for dates.
// It can represent dates from Jan 1, 1753 to after (dates before that
// time are complicated...).
//

#include <iostream>
#include <string>
#include <utility>
#include <iomanip>
#include <cctype>

using namespace std;
using namespace std::rel_ops;

struct Date {

  int yyyy;
  int mm;
  int dd;

  // no dates before 1753
  static int const BASE_YEAR = 1753;

  // Enumerated type for names of the days of the week
  enum dayName {SUN,MON,TUE,WED,THU,FRI,SAT};

  // Is a date valid
  static bool validDate(int yr, int mon, int day)
  {
    return yr >= BASE_YEAR && mon >= 1 && mon <= 12 &&
      day > 0 && day <= daysIn(mon, yr);
  }

  bool isValid() const
  {
    return validDate(yyyy, mm, dd);
  }

  // Constructor to create a specific date.  If the date is invalid,
  // the behaviour is undefined
  Date(int yr = 1970, int mon = 1, int day = 1)
  {
    yyyy = yr;
    mm = mon;
    dd = day;
  }

  // Returns the day of the week for this
  dayName dayOfWeek() const
  {
    int a = (14 - mm) / 12;
    int y = yyyy - a;
    int m = mm + 12 * a - 2;
    return (dayName)((dd + y + y/4 - y/100 + y/400 + 31 * m / 12) % 7);
  }

  // comparison operators
  bool operator==(const Date &d) const
  {
    return dd == d.dd && mm == d.mm && yyyy == d.yyyy;
  }

  bool operator<(const Date &d) const
  {
    return yyyy < d.yyyy || (yyyy == d.yyyy && mm < d.mm) ||
      (yyyy == d.yyyy && mm == d.mm && dd < d.dd);
```

```cpp
}

// Returns true if yr is a leap year
static bool leapYear(int y)
{
  return (y % 400 ==0 || (y % 4 == 0 && y % 100 != 0));
}

// number of days in this month
static int daysIn(int m, int y)
{
  switch (m) {
  case 4  :
  case 6  :
  case 9  :
  case 11 :
    return 30;
  case 2  :
    if (leapYear(y)) {
      return 29;
    }
    else {
      return 28;
    }
  default :
    return 31;
  }
}

// increment by day, month, or year
//
// Use negative argument to decrement
//
// If adding a month/year results in a date before BASE_YEAR, the result
// is undefined.
//
// If adding a month/year results in an invalid date (Feb 29 on a non-leap
// year, Feb 31, Jun 31, etc.), the results are automatically "rounded down"
// to the last valid date

// add n days to the date: complexity is about n/30 iterations
void addDay(int n = 1)
{
  dd += n;
  while (dd > daysIn(mm,yyyy)) {
    dd -= daysIn(mm,yyyy);
    if (++mm > 12) {
      mm = 1;
      yyyy++;
    }
  }

  while (dd < 1) {
    if (--mm < 1) {
      mm = 12;
      yyyy--;
    }
    dd += daysIn(mm,yyyy);
  }
}

// add n months to the date: complexity is about n/12 iterations
void addMonth(int n = 1)
{
  mm += n;
  while (mm > 12) {
    mm -= 12;
    yyyy++;
  }
```

```
      while (mm < 1)  {
        mm += 12;
        yyyy--;
      }

      if (dd > daysIn(mm,yyyy)) {
        dd = daysIn(mm,yyyy);
      }
    }

    // add n years to the date
    void addYear(int n = 1)
    {
      yyyy += n;
      if (!leapYear(yyyy) && mm == 2 && dd == 29) {
        dd = 28;
      }
    }

    // number of days since 1753/01/01, including the current date
    int daysFromStart() const
    {
      int c = 0;
      Date d(BASE_YEAR, 1, 1);
      Date d2(d);

      d2.addYear(1);
      while (d2 < *this) {
        c += leapYear(d.yyyy) ? 366 : 365;
        d = d2;
        d2.addYear(1);
      }

      d2 = d;
      d2.addMonth(1);
      while (d2 < *this) {
        c += daysIn(d.mm, d.yyyy);
        d = d2;
        d2.addMonth(1);
      }
      while (d <= *this) {
        d.addDay();
        c++;
      }
      return c;
    }
};

// Reads a date in yyyy/mm/dd format, assumes date is valid and in the
// right format
istream& operator>>(istream &is, Date &d)
{
  char c;
  return is >> d.yyyy >> c >> d.mm >> c >> d.dd;
}

// print date in yyyy/mm/dd format
ostream& operator<< (ostream &os, const Date &d) {
  char t = os.fill('0');
  os << d.yyyy << '/' << setw(2) << d.mm << '/' << setw(2) << d.dd;
  os.fill(t);
  return os;
}
```

```
/*
 * Dijkstra's Algorithm
 *
 * Author: Howard Cheng
 * Reference:
 *   Ian Parberry's "Problems on Algorithms", page 102.
 *
 * Given a weight matrix representing a graph and a source vertex, this
 * algorithm computes the shortest distance, as well as path, to each
 * of the other vertices.  The paths are represented by an inverted list,
 * such that if v preceeds immediately before w in a path from the
 * source to vertex w, then the path P[w] is v.  The distances from
 * the source to v is given in D[v] (DISCONNECT if not connected).
 *
 * Call get_path to recover the path.
 *
 * Note: Dijkstra's algorithm only works if all weight edges are
 *       non-negative.
 *
 */

#include <iostream>
#include <algorithm>
#include <cassert>

using namespace std;

const int MAX_NODES = 10;
const int DISCONNECT = -1;

/* assume that D and P have been allocated */
void dijkstra(int graph[MAX_NODES][MAX_NODES], int n, int src, int D[],
              int P[])
{
  char used[MAX_NODES];
  int fringe[MAX_NODES];
  int f_size;
  int v, w, j, wj;
  int best, best_init;

  f_size = 0;
  for (v = 0; v < n; v++) {
    if (graph[src][v] != DISCONNECT && src != v) {
      D[v] = graph[src][v];
      P[v] = src;
      fringe[f_size++] = v;
      used[v] = 1;
    } else {
      D[v] = DISCONNECT;
      P[v] = -1;
      used[v] = 0;
    }
  }
  D[src] = 0;
  P[src] = -1;
  used[src] = 1;

  best_init = 1;
  while (best_init) {
    /* find unused vertex with smallest D */
    best_init = 0;
    for (j = 0; j < f_size; j++) {
      v = fringe[j];
      assert(D[v] != DISCONNECT);
      if (!best_init || D[v] < best) {
        best = D[v];
        w = v;
        wj = j;
        best_init = 1;
```

```
      }
    }

    if (best_init) {
      assert(D[w] != DISCONNECT);
      assert(fringe[wj] == w);

      /* get rid of w from fringe */
      f_size--;
      for (j = wj; j < f_size; j++) {
        fringe[j] = fringe[j+1];
      }

      /* update distances and add new vertices to fringe */
      for (v = 0; v < n; v++) {
        if (v != src && graph[w][v] != DISCONNECT) {
          if (D[v] == DISCONNECT || D[w] + graph[w][v] < D[v]) {
            D[v] = D[w] + graph[w][v];
            P[v] = w;
          } else if (D[w] + graph[w][v] == D[v]) {
            /* put tie-breaker here */
          }
          if (!used[v]) {
            used[v] = 1;
            fringe[f_size++] = v;
          }
        }
      }
    }
  }
  D[src] = 0;
}

int get_path(int v, int P[], int path[])
{
  int A[MAX_NODES];
  int i, k;

  k = 0;
  A[k++] = v;
  while (P[v] != -1) {
    v = P[v];
    A[k++] = v;
  }
  for (i = k-1; i >= 0; i--) {
    path[k-1-i] = A[i];
  }
  return k;
}

int main(void)
{
  int m, w, num;
  int i, j;
  int graph[MAX_NODES][MAX_NODES];
  int P[MAX_NODES][MAX_NODES], D[MAX_NODES][MAX_NODES];
  int path[MAX_NODES];

  /* clear graph */
  for (i = 0; i < MAX_NODES; i++) {
    for (j = 0; j < MAX_NODES; j++) {
      graph[i][j] = DISCONNECT;
    }
  }

  /* read graph */
  cin >> i >> j >> w;
  while (!(i == -1 && j == -1)) {
    assert(0 <= i && i < MAX_NODES && 0 <= j && j < MAX_NODES);
```

```
      graph[i][j] = graph[j][i] = w;
      cin >> i >> j >> w;
   }

   for (i = 0; i < MAX_NODES; i++) {
      dijkstra(graph, MAX_NODES, i, D[i], P[i]);
   }

   /* do queries */
   cin >> i >> j;
   while (!(i == -1 && j == -1)) {
      assert(0 <= i && i < MAX_NODES && 0 <= j && j < MAX_NODES);
      cout << i << " " << j << ":" << D[i][j] << endl;
      for (m = j; m != -1; m = P[i][m]) {
         cout << " " << m;
      }
      cout << endl;
      num = get_path(j, P[i], path);
      for (m = 0; m < num; m++) {
         cout << " " << path[m];
      }
      cout << endl;
      cin >> i >> j;
   }

   return 0;
}
```

```cpp
/*
 * Dijkstra's Algorithm for sparse graphs
 *
 * Author: Howard Cheng
 *
 * Given a weight matrix representing a graph and a source vertex, this
 * algorithm computes the shortest distance, as well as path, to each
 * of the other vertices.  The paths are represented by an inverted list,
 * such that if v preceeds immediately before w in a path from the
 * source to vertex w, then the path P[w] is v.  The distances from
 * the source to v is given in D[v] (-1 if not connected).
 *
 * Call get_path to recover the path.
 *
 * Note: Dijkstra's algorithm only works if all weight edges are
 *       non-negative.
 *
 * This version works well if the graph is not dense.  The complexity
 * is O((n + m) log (n + m)) where n is the number of vertices and
 * m is the number of edges.
 *
 */

#include <iostream>
#include <algorithm>
#include <vector>
#include <cassert>
#include <queue>

using namespace std;


struct Edge {
  int to;
  int weight;          // can be double or other numeric type
  Edge(int t, int w)
    : to(t), weight(w) { }
};

typedef vector<Edge>::iterator EdgeIter;

struct Graph {
  vector<Edge> *nbr;
  int num_nodes;
  Graph(int n)
    : num_nodes(n)
  {
    nbr = new vector<Edge>[num_nodes];
  }

  ~Graph()
  {
    delete[] nbr;
  }

  // note: There is no check on duplicate edge, so it is possible to
  // add multiple edges between two vertices
  //
  // If this is an undirected graph, be sure to add an edge both
  // ways
  void add_edge(int u, int v, int weight)
  {
    nbr[u].push_back(Edge(v, weight));
  }
};

/* assume that D and P have been allocated */
void dijkstra(const Graph &G, int src, vector<int> &D, vector<int> &P)
{
```

```cpp
  typedef pair<int,int> pii;

  int n = G.num_nodes;
  vector<bool> used(n, false);
  priority_queue<pii, vector<pii>,  greater<pii> > fringe;

  D.resize(n);
  P.resize(n);
  fill(D.begin(), D.end(), -1);
  fill(P.begin(), P.end(), -1);

  D[src] = 0;
  fringe.push(make_pair(D[src], src));

  while (!fringe.empty()) {
    pii next = fringe.top();
    fringe.pop();
    int u = next.second;
    if (used[u]) continue;
    used[u] = true;

    for (EdgeIter it = G.nbr[u].begin(); it != G.nbr[u].end(); ++it) {
      int v = it->to;
      int weight = it->weight + next.first;
      if (used[v]) continue;
      if (D[v] == -1 || weight < D[v]) {
        D[v] = weight;
        P[v] = u;
        fringe.push(make_pair(D[v], v));
      }
    }
  }
}

int get_path(int v, const vector<int> &P, vector<int> &path)
{
  path.clear();
  path.push_back(v);
  while (P[v] != -1) {
    v = P[v];
    path.push_back(v);
  }
  reverse(path.begin(), path.end());
  return path.size();
}

int main(void)
{
  int n;
  while (cin >> n && n > 0) {
    Graph G(n);
    int u, v, w;

    while (cin >> u >> v >> w && !(u == -1 && v == -1 && w == -1)) {
      G.add_edge(u, v, w);
    }

    while (cin >> u >> v && !(u == -1 && v == -1)) {
      vector<int> D, P, path;
      dijkstra(G, u, D, P);
      get_path(v, P, path);

      cout << "distance = " << D[v] << endl;
      cout << "path = ";
      for (unsigned int i = 0; i < path.size(); i++) {
        cout << path[i] << ' ';
      }
      cout << endl;
    }
```

```
  }
  return 0;
}
```

```c
/*
 * Solution of system of linear diophantine equations
 *
 * Author: Howard Cheng
 * Date:   Nov 25, 2000
 * Reference:
 *
 * http://scicomp.ewha.ac.kr/netlib/tomspdf/
 *
 * Look at Algorithms 287 (sort of) and 288.
 *
 * Given a system of m linear diophantine equations in n unknowns,
 * this algorithm finds a particular solution as well as a basis for
 * the solution space of the homogeneous system, if they exist.  The
 * system is represented in matrix form as Ax = b where all entries
 * are integers.
 *
 * Function: diophantine_linsolve
 *
 * Input:
 *
 * A: an m x n matrix specifying the coefficients of each equation in
 *    each row (it is okay to have zero rows, or even have A = 0)
 * b: an m-dimensional vector specifying the right-hand side of the system
 * m: number of equations in the system
 * n: number of unknowns in the system
 *
 * Output:
 *
 * The function returns the dimension of the solution space of the
 * homogeneous system Ax = 0 (hom_dim) if it has a solution.
 * Otherwise, it returns -1.
 *
 * Other results returned in the parameters are:
 *
 * xp: an n-dimensional vector giving a particular solution
 * hom_basis: an n x n matrix whose first hom_dim columns form a basis
 *            of the solution space of the homogeneous system Ax = 0
 *
 * All solutions to Ax = b can be obtained by adding integer multiples
 * of the first hom_dim columns of hom_basis to xp.
 *
 * Note:
 *
 * The contents of A and b are not changed by this function.
 *
 */

#include <stdio.h>
#include <stdlib.h>

#define MAX_N 50
#define MAX_M 50

int triangulate(int A[MAX_N+1][MAX_M+MAX_N+1], int m, int n, int cols)
{
  int ri, ci, i, j, k, pi, t;
  div_t d;

  ri = ci = 0;
  while (ri < m && ci < cols) {

    /* find smallest non-zero pivot */
    pi = -1;
    for (i = ri; i < m; i++) {
      if (A[i][ci] && (pi == -1 || abs(A[i][ci]) < abs(A[pi][ci]))) {
        pi = i;
      }
    }
```

```c
    if (pi == -1) {
      /* the entire column is 0, skip it */
      ci++;
    } else {
      k = 0;
      for (i = ri; i < m; i++) {
        if (i != pi) {
          d = div(A[i][ci], A[pi][ci]);
          if (d.quot) {
            k++;
            for (j = ci; j < n; j++) {
              A[i][j] -= d.quot*A[pi][j];
            }
          }
        }
      }
      if (!k) {
        /* swap the row to make it triangular...Alg 287 also switches the */
        /* sign, probably to preserve the sign of the minors.  I don't     */
        /* think this is necessary for our purpose.                        */
        for (i = ci; i < n && ri != pi; i++) {
          t = A[ri][i];
          A[ri][i] = A[pi][i];
          A[pi][i] = t;
        }
        ri++;
        ci++;
      }
    }
  }
  return ri;
}

int diophantine_linsolve(int A[MAX_M][MAX_N], int b[MAX_M], int m, int n,
                         int xp[MAX_N], int hom_basis[MAX_N][MAX_N])
{
  int mat[MAX_N+1][MAX_M+MAX_N+1];
  int i, j, rank, d;

  /* form the work matrix */
  for (i = 0; i < m; i++) {
    mat[0][i] = -b[i];
  }
  for (i = 0; i < m; i++) {
    for (j = 0; j < n; j++) {
      mat[j+1][i] = A[i][j];
    }
  }
  for (i = 0; i < n+1; i++) {
    for (j = 0; j < n+1; j++) {
      mat[i][j+m] = (i == j);
    }
  }

  /* triangluate the first n+1 x m+1 submatrix */
  rank = triangulate(mat, n+1, m+n+1, m+1);
  d = mat[rank-1][m];

  /* check for no solutions */
  if (d != 1 && d != -1) {
    /* no integer solutions */
    return -1;
  }
  /* check for inconsistent system */
  for (i = 0; i < m; i++) {
    if (mat[rank-1][i]) {
      return -1;
    }
  }
```

```c
    /* there is a solution, copy it to the result */
    for (i = 0; i < n; i++) {
      xp[i] = d*mat[rank-1][m+1+i];
      for (j = 0; j < n+1-rank; j++) {
        hom_basis[i][j] = mat[rank+j][m+1+i];
      }
    }

  return n+1-rank;
}

int main(void)
{
  int A[MAX_M][MAX_N], b[MAX_M], m, n, xp[MAX_N], hom_basis[MAX_N][MAX_N];
  int i, j, hom_dim;

  while (scanf("%d %d", &m, &n) == 2 && m > 0 && n > 0) {
    for (i = 0; i < m; i++) {
      printf("Enter equation %d:\n", i+1);
      for (j = 0; j < n; j++) {
        scanf("%d", &A[i][j]);
      }
      scanf("%d", &b[i]);
    }

    if ((hom_dim = diophantine_linsolve(A, b, m, n, xp, hom_basis)) >= 0) {
      printf("Particular solution:\n");
      for (i = 0; i < n; i++) {
        printf("%d ", xp[i]);
      }
      printf("\n");
      printf("hom_dim = %d\n", hom_dim);
      printf("Basis for Ax = 0:\n");
      for (j = 0; j < hom_dim; j++) {
        for (i = 0; i < n; i++) {
          printf("%d ", hom_basis[i][j]);
        }
        printf("\n");
      }
    } else {
      printf("No solution.\n");
    }

  }

  return 0;
}
```

```cpp
//
// 3-D distances between point to point, point to line segment,
// line segment to line segment, and point to triangle.
//
// There are corresponding versions of the same code for distances
// between point to infinite lines, infinite line to infinite line,
// and point to infinite plane.
//
// It is assumed that segments/lines/triangles/plane are defined by
// distinct points (so the objects are not degenerate).
//
// They can be used for 2-D objects as well by setting the z coordinates
// to 0.
//
// Author: Howard Cheng
//

#include <iostream>
#include <iomanip>
#include <cmath>
#include <algorithm>
#include <cassert>

using namespace std;

const double PI = acos(-1.0);

struct Vector {
  double x, y, z;

  Vector(double xx = 0, double yy = 0, double zz = 0)
    : x(xx), y(yy), z(zz) { }

  Vector(const Vector &p1, const Vector &p2)
    : x(p2.x - p1.x), y(p2.y - p1.y), z(p2.z - p1.z) { }

  Vector(const Vector &p1, const Vector &p2, double t)
    : x(p1.x + t*p2.x), y(p1.y + t*p2.y), z(p1.z + t*p2.z) { }

  double norm() const {
    return sqrt(x*x + y*y + z*z);
  }

};

istream &operator>>(istream &is, Vector &p)
{
  return is >> p.x >> p.y >> p.z;
}

ostream &operator<<(ostream &os, const Vector &p)
{
  return os << "(" << p.x << "," << p.y << "," << p.z << ")";
}

double dot(const Vector &p1, const Vector &p2)
{
  return p1.x * p2.x + p1.y * p2.y + p1.z * p2.z;
}

Vector cross(const Vector &p1, const Vector &p2)
{
  Vector v(p1.y*p2.z - p2.y*p1.z,
           p2.x*p1.z - p1.x*p2.z,
           p1.x*p2.y - p2.x*p1.y);
  return v;
}

// distance between two points
```

```cpp
double dist_point_to_point(const Vector &p1, const Vector &p2)
{
  Vector p(p1, p2);
  return p.norm();
}


// angle between two vectors (in radians)
double angle(const Vector &p1, const Vector &p2)
{
  return acos(dot(p1, p2)/p1.norm()/p2.norm());
}

// distance from p to the line segment from a to b
double dist_point_to_segment(const Vector &p, const Vector &a,
                             const Vector &b)
{
  Vector u(a, p), v(a, b);
  double s = dot(u,v) / dot(v,v);

  if (s < 0 || s > 1) {
    return min(dist_point_to_point(p, a), dist_point_to_point(p, b));
  }

  Vector proj(a, v, s);
  return dist_point_to_point(proj, p);
}

// distance from p to the infinite line defined by a and b
double dist_point_to_line(const Vector &p, const Vector &a,
                          const Vector &b)
{
  Vector u(a, p), v(a, b);
  double s = dot(u,v) / dot(v,v);
  Vector proj(a, v, s);
  return dist_point_to_point(proj, p);
}

// distance from p to the triangle defined by a, b, c
double dist_point_to_triangle(const Vector &p, const Vector &a,
                              const Vector &b, const Vector &c)
{
  Vector u(a, p), v1(a, b), v2(a, c);
  Vector normal = cross(v1, v2);
  double s = dot(u, normal) / (normal.norm() * normal.norm());
  Vector proj(p, normal, -s);

  // check projection: inside if sum of angles is 2*pi
  Vector wa(proj, a), wb(proj, b), wc(proj, c);
  double a1 = angle(wa, wb);
  double a2 = angle(wa, wc);
  double a3 = angle(wb, wc);
  if (fabs(a1 + a2 + a3 - 2*PI) < 1e-8) {
    return dist_point_to_point(proj, p);
  } else {
    return min(dist_point_to_segment(p, a, b),
               min(dist_point_to_segment(p, a, c),
                   dist_point_to_segment(p, b, c)));
  }
}

// distance from p to the infinite plane defined by a, b, c
double dist_point_to_plane(const Vector &p, const Vector &a,
                           const Vector &b, const Vector &c)
{
  Vector u(a, p), v1(a, b), v2(a, c);
  Vector normal = cross(v1, v2);
  double s = dot(u, normal) / (normal.norm() * normal.norm());
  Vector proj(p, normal, -s);
  return dist_point_to_point(proj, p);
```

```cpp
}

// distance from segment p1->q1 to p2->q2
double dist_segment_to_segment(const Vector &p1, const Vector &q1,
                               const Vector &p2, const Vector &q2)
{
  //
  // the points on the 1st line are p1 + t * v1
  // the points on the 2nd line are p2 + s * v2
  //
  //                              0 <= s, t <= 1
  //
  // squared distance is
  //
  // S = (p1.x - p2.x + t * v1.x - s * v2.x)^2 +
  //     (p1.y - p2.y + t * v1.y - s * v2.y)^2 +
  //     (p1.z - p2.z + t * v1.z - s * v2.z)^2
  //
  // deriviative wrt t and s are:
  //
  // 1/2 dS/dt = norm(v1)^2 * t - dot(v1, v2) * s + dot(v1, p1) - dot(v1, p2)
  // 1/2 dS/ds = -dot(v1, v2) * t + norm(v2)^2 * s - dot(v2, p1) + dot(v2, p2)
  //
  // solving for s and t with both derivatives = 0:
  //

  Vector v1(p1, q1), v2(p2, q2);
  Vector rhs(dot(v1, p2) - dot(v1, p1), dot(v2, p1) - dot(v2, p2));
  double det = v1.norm()*v1.norm()*v2.norm()*v2.norm() -
    dot(v1, v2)*dot(v1, v2);

  if (det < 1e-8) {
    // parallel lines (if v1 and v2 != 0)
    goto degenerate;
  } else {
    double t = (rhs.x*v2.norm()*v2.norm() + rhs.y * dot(v1, v2)) / det;
    double s = (v1.norm()*v1.norm()*rhs.y + dot(v1, v2) * rhs.x) / det;
    if (0 <= s && s <= 1 && 0 <= t && t <= 1) {
      Vector pp1(p1, v1, t), pp2(p2, v2, s);
      return dist_point_to_point(pp1, pp2);
    }
  }

 degenerate:
  return min(min(dist_point_to_segment(p1, p2, q2),
                 dist_point_to_segment(q1, p2, q2)),
             min(dist_point_to_segment(p2, p1, q1),
                 dist_point_to_segment(q2, p1, q1)));
}

// distance from infinite lines defined by p1->q1 and p2->q2
double dist_line_to_line(const Vector &p1, const Vector &q1,
                         const Vector &p2, const Vector &q2)
{
  //
  // the points on the 1st line are p1 + t * v1
  // the points on the 2nd line are p2 + s * v2
  //
  //                              0 <= s, t <= 1
  //
  // squared distance is
  //
  // S = (p1.x - p2.x + t * v1.x - s * v2.x)^2 +
  //     (p1.y - p2.y + t * v1.y - s * v2.y)^2 +
  //     (p1.z - p2.z + t * v1.z - s * v2.z)^2
  //
  // deriviative wrt t and s are:
  //
  // 1/2 dS/dt = norm(v1)^2 * t - dot(v1, v2) * s + dot(v1, p1) - dot(v1, p2)
```

```cpp
  // 1/2 dS/ds = -dot(v1, v2) * t + norm(v2)^2 * s - dot(v2, p1) + dot(v2, p2)
  //
  // solving for s and t with both derivatives = 0:
  //

  Vector v1(p1, q1), v2(p2, q2);
  Vector rhs(dot(v1, p2) - dot(v1, p1), dot(v2, p1) - dot(v2, p2));
  double det = v1.norm()*v1.norm()*v2.norm()*v2.norm() -
    dot(v1, v2)*dot(v1, v2);

  if (det < 1e-8) {
    // parallel lines (if v1 and v2 != 0)
    return dist_point_to_line(p1, p2, q2);
  } else {
    double t = (rhs.x*v2.norm()*v2.norm() + rhs.y * dot(v1, v2)) / det;
    double s = (v1.norm()*v1.norm()*rhs.y + dot(v1, v2) * rhs.x) / det;
    Vector pp1(p1, v1, t), pp2(p2, v2, s);
    return dist_point_to_point(pp1, pp2);
  }
}

////////////////////////////////////////////////////////////////////////
//
// This is the solution to 11836 (Star War)
//
////////////////////////////////////////////////////////////////////////

void do_case()
{
  Vector t1[4], t2[4];
  for (int i = 0; i < 4; i++) {
    cin >> t1[i];
  }
  for (int i = 0; i < 4; i++) {
    cin >> t2[i];
  }

  double best = dist_point_to_point(t1[0], t2[0]);

  // vertex-face distance
  for (int i1 = 0; i1 < 4; i1++) {
    for (int j1 = 0; j1 < 4; j1++) {
      best = min(best, dist_point_to_triangle(t1[i1], t2[j1], t2[(j1+1)%4],
                                              t2[(j1+2)%4]));
      best = min(best, dist_point_to_triangle(t2[i1], t1[j1], t1[(j1+1)%4],
                                              t1[(j1+2)%4]));
    }
  }

  // edge-edge distance
  for (int i1 = 0; i1 < 4; i1++) {
    for (int i2 = i1+1; i2 < 4; i2++) {
      for (int j1 = 0; j1 < 4; j1++) {
        for (int j2 = j1+1; j2 < 4; j2++) {
          best = min(best, dist_segment_to_segment(t1[i1], t1[i2],
                                                    t2[j1], t2[j2]));
        }
      }
    }
  }

  cout << setprecision(2) << fixed << best << endl;
}

int main(void)
{
  int T;
  cin >> T;
  while (T-- > 0) {
```

```
        do_case();
    }
    return 0;
}
```

```cpp
/*
 * Distance from a point to an (infinite) line.
 *
 * Author: Howard Cheng
 * Reference:
 *   http://www.exaflop.org/docs/cgafaq/cga1.html
 *
 * This routine computes the shortest distance from a point to a line.
 * ie. distance from point to its orthogonal projection onto the line.
 * Works even if the projection is not on the line (i.e. treat the line
 * as infinite line).
 *
 */

#include <iostream>
#include <iomanip>
#include <cmath>
#include <cassert>

using namespace std;

struct Point {
  double x, y;
};

/* computes the distance from "c" to the line defined by "a" and "b" */
double dist_line(Point a, Point b, Point c)
{
  double L2, s;

  L2 = (b.x-a.x)*(b.x-a.x)+(b.y-a.y)*(b.y-a.y);
  assert(L2 > 0);
  s = ((a.y-c.y)*(b.x-a.x)-(a.x-c.x)*(b.y-a.y)) / L2;

  return fabs(s*sqrt(L2));
}

int main(void)
{
  Point a, b, c;

  while (cin >> a.x >> a.y >> b.x >> b.y >> c.x >> c.y) {
    cout << "distance = " << fixed << setprecision(2) << dist_line(a, b, c)
         << endl;
  }
  return 0;
}
```

```c
/*
 * Computing the Day of the Week
 *
 * Author: Howard Cheng
 *
 * This routine computes the day of the week (Sunday = 0, Saturday = 6)
 * from the year, month, and day.
 *
 */

unsigned DOW(unsigned y, unsigned m, unsigned d)
{
      if (m < 3)
      {
            m += 13;
            y--;
      }
      else m++;
      return (d + 26 * m / 10 + y + y / 4 - y / 100 + y / 400 + 6) % 7;
}

#include <stdio.h>
#include <stdlib.h>

int main(int argc, char *argv[])
{
      int Day;
      void usage(void);
      unsigned d, m, y, days[] = {31, 29, 31, 30, 31, 30,
                                  31, 31, 30, 31, 30, 31};

      char *day[2][7] = {
            {"Mon", "Tue", "Wed", "Thu", "Fri", "Sat", "Sun"},
            {"Sun", "Mon", "Tue", "Wed", "Thu", "Fri", "Sat"}
      };
      char *month[]  = {"Jan", "Feb", "Mar", "Apr", "May", "Jun",
                        "Jul", "Aug", "Sep", "Oct", "Nov", "Dec",};


      if (4 > argc)
            usage();
      y = atoi(argv[1]);
      m = atoi(argv[2]);
      d = atoi(argv[3]);
      if (!m || m > 12)
            usage();
      if (!d || d > days[m - 1])
            usage();
      if (y < 100)
            y += 1900;
      Day = DOW(y, m, d);
      printf("DOW returned %d, so %d %s %d is a %s\n",
             Day, d, month[m - 1], y, day[6 - 5][Day]);
      return 0;
}

void usage(void)
{
      puts("Usage: DOW yy[yy] mm dd");
      exit(-1);
}
```

```cpp
/*
 * Euclidean Algorithm
 *
 * Author: Howard Cheng
 *
 * Given two integers, return their gcd.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

int gcd(int a, int b)
{
  int r;

  /* unnecessary if a, b >= 0 */
  if (a < 0) {
    a = -a;
  }
  if (b < 0) {
    b = -b;
  }

  while (b) {
    r = a % b;
    a = b;
    b = r;
  }
  assert(a >= 0);
  return a;
}

int main(void)
{
  int a, b;

  while (cin >> a >> b) {
    cout << gcd(a, b) << endl;
  }
  return 0;
}
```

```
/*
 * Euler's Phi function:
 *
 * Author: Ethan Kim
 * Complexity: O(sqrt(n))
 *
 * Computes Euler's Phi(Totient) function; Given a positive n, computes
 * the number of positive integers that are <= n and relatively prime to n.
 *
 * For prime n, it is easy to see that phi(n)=n-1.
 * For powers of prime, phi(p^k)=p^(k-1) * (p-1).
 * Also, phi is multiplicative, so phi(pq)=phi(p)*phi(q), if p and q are
 * relatively prime.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

int fast_exp(int b, int n)
{
  int res = 1;
  int x = b;

  while (n > 0) {
    if (n & 0x01) {
      n--;
      res *= x;
    } else {
      n >>= 1;
      x *= x;
    }
  }

  return res;
}

int phi(int n) {
  int k, res;
  long long p;

  assert(n > 0);

  res=1;
  for(k = 0; n % 2 == 0; k++) {
    n /= 2;
  }
  if (k)
    res *= fast_exp(2, k-1);

  for (p = 3; p*p <= n; p += 2) {
    for (k = 0; n % p == 0; k++) {
      n /= p;
    }
    if (k) {
      res *= fast_exp(p, k-1) * (p-1);
    }
  }
  if (n > 1) {
    res *= n-1;
  }
  return res;
}

int main(void) {
  int p;
  while(cin >> p && p) {
```

```
    cout << phi(p) << endl;
  }
  return 0;
}
```

```cpp
/*
 * Finding an Eulerian Tour
 *
 * Author: Howard Cheng
 *
 * The routine eulerian() determines if a graph has an Eulerian tour.
 * That is, it checks that it is connected and all vertices have even
 * degree.  We assume that the graph is represented as an adjacency matrix
 * and the an auxillary array called "deg" gives the degree of the vertex.
 *
 * The routine eulerian_tour() returns one (arbitrary) Eulerian tour.
 * The tour is stored in an array of the vertices visited in the tour,
 * and the first and last vertex is the same.
 *
 * WARNING: eulerian_tour() destroys the graph as it uses edges.  If
 *          you need the graph back then you should save a copy.
 *
 * NOTE: converting this code for directed graphs should not be that much
 *          work.  You should also be able to convert this code for Eulerian
 *          paths.
 *
 */

#include <iostream>
#include <algorithm>
#include <cassert>

using namespace std;

const int NUM_VERTICES = 50;
const int NUM_EDGES = 1000;        /* maximum number of edges in graph */

int graph[NUM_VERTICES+1][NUM_VERTICES+1];
int deg[NUM_VERTICES+1];

void clear_graph(void)
{
  fill(deg, deg+NUM_VERTICES+1, 0);
  for (int i = 1; i <= NUM_VERTICES; i++) {
    fill(graph[i], graph[i]+NUM_VERTICES+1, 0);
  }
}

void visit(int v, char visited[])
{
  int w;

  visited[v] = 1;
  for (w = 1; w <= NUM_VERTICES; w++) {
    if (!visited[w] && graph[v][w] > 0) {
      visit(w, visited);
    }
  }
}

int connected(void)
{
  char visited[NUM_VERTICES+1];
  int i;

  fill(visited, visited+NUM_VERTICES+1, 0);
  for (i = 1; i <= NUM_VERTICES; i++) {
    if (deg[i] > 0) {
      visit(i, visited);
      break;
    }
  }
  for (i = 1; i <= NUM_VERTICES; i++) {
    if (deg[i] > 0 && !visited[i]) {
```

```cpp
      return 0;
    }
  }
  return 1;
}

int eulerian(void)
{
  int i;
  for (i = 1; i <= NUM_VERTICES; i++) {
    if (deg[i] % 2 == 1) {
      return 0;
    }
  }
  return connected();
}

int find_tour(int start, int temp[])
{
  int len = 0;
  int next;

  temp[len++] = start;
  while (deg[start] > 0) {
    for (next = 1; next <= NUM_VERTICES; next++) {
      if (graph[start][next] > 0) {
        break;
      }
    }
    temp[len++] = next;
    graph[start][next]--; deg[start]--;
    graph[next][start]--; deg[next]--;
    start = next;
  }
  return len;
}

int graft_tour(int old[], int old_len, int tour[], int tour_len)
{
  int pos[NUM_VERTICES+1];
  int i, j, p1, p2;

  fill(pos, pos+NUM_VERTICES+1, -1);
  for (i = 0; i < old_len; i++) {
    pos[old[i]] = i;
  }
  for (i = 0; i < tour_len; i++) {
    if (pos[tour[i]] >= 0) {
      break;
    }
  }
  assert(i < tour_len);
  p1 = pos[tour[i]];
  p2 = i;
  for (i = old_len-1; i > p1; i--) {
    old[i+tour_len-1] = old[i];
  }
  for (i = p2+1, j = 0; i < tour_len-1; i++, j++) {
    old[p1+j+1] = tour[i];
  }
  for (i = 0; i <= p2; i++) {
    old[p1+j+1] = tour[i];
  }

  return old_len+tour_len-1;
}

int eulerian_tour(int tour[])
{
```

```cc
  int temp[NUM_EDGES+1];
  int tour_len, temp_len, first_time;
  int i, found;

  tour_len = temp_len = 0;
  first_time = 1;

  while (1) {
    found = 0;
    if (first_time) {
      for (i = 1; i <= NUM_VERTICES; i++) {
        if (deg[i] > 0) {
          found = 1;
          break;
        }
      }
    } else {
      /* this ensures that we can graft next tour on to existing one */
      for (i = 0; i < tour_len; i++) {
        if (deg[tour[i]] > 0) {
          found = 1;
          break;
        }
      }
      i = tour[i];
    }
    if (!found) {
      break;
    }

    if (first_time) {
      tour_len = find_tour(i, tour);
    } else {
      temp_len = find_tour(i, temp);
      tour_len = graft_tour(tour, tour_len, temp, temp_len);
    }
    first_time = 0;
  }
  return tour_len;
}

int main(void)
{
  int T, N, i, j, k;
  int u, v;
  int tour[NUM_EDGES+1], tour_len;

  cin >> T;
  for (i = 1; i <= T; i++) {
    clear_graph();
    if (i > 1) {
      cout << endl;
    }
    cout << "Case #" << i << endl;
    cin >> N;
    for (j = 0; j < N; j++) {
      cin >> u >> v;
      graph[u][v]++;
      graph[v][u]++;
      deg[u]++;
      deg[v]++;
    }

    if (eulerian()) {
      tour_len = eulerian_tour(tour);
      for (k = 0; k < tour_len-1; k++) {
        cout << tour[k] << " " << tour[k+1] << endl;
      }
    } else {
```

```cc
      cout << "some beads may be lost" << endl;
    }
  }
  return 0;
}
```

```cpp
/*
 * Fast Exponentiation
 *
 * Author: Howard Cheng
 *
 * Given b and n, computes b^n quickly.
 *
 */

#include <iostream>

using namespace std;

int fast_exp(int b, int n)
{
  int res = 1;
  int x = b;

  while (n > 0) {
    if (n & 0x01) {
      n--;
      res *= x;
    } else {
      n >>= 1;
      x *= x;
    }
  }

  return res;
}

int main(void)
{
  int b, n;

  while (cin >> b >> n) {
    cout << b << "^" << n << " = " << fast_exp(b, n) << endl;
  }
  return 0;

}
```

```cpp
/*
 * Fast Exponentiation mod m
 *
 * Author: Howard Cheng
 *
 * Given b, n, and m, computes b^n mod m quickly.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

int fast_exp(int b, int n, int m)
{
  int res = 1;
  long long x = b;

  while (n > 0) {
    if (n & 0x01) {
      n--;
      res = (res * x) % m;
    } else {
      n >>= 1;
      x = (x * x) % m;
    }
  }

  return res;
}

int main(void)
{
  int b, n, m;

  while (cin >> b >> n >> m) {
    cout << b << "^" << n << " mod " << m << " = " << fast_exp(b, n, m)
         << endl;
  }
  return 0;

}
```

```cpp
/*
 * Extended Euclidean Algorithm
 *
 * Author: Howard Cheng
 *
 * Given two integers, return their gcd and the cofactors to form the
 * gcd as a linear combination.
 *
 * a*s + b*t = gcd(a,b)
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

int gcd(int a, int b, int &s, int &t)
{
  int r, r1, r2, a1, a2, b1, b2, q;
  int A = a;
  int B = b;

  /* unnecessary if a, b >= 0 */
  if (a < 0) {
    r = gcd(-a, b, s, t);
    s *= -1;
    return r;
  }
  if (b < 0) {
    r = gcd(a, -b, s, t);
    t *= -1;
    return r;
  }

  a1 = b2 = 1;
  a2 = b1 = 0;

  while (b) {
    assert(a1*A + a2*B == a);
    q = a / b;
    r = a % b;
    r1 = a1 - q*b1;
    r2 = a2 - q*b2;
    a = b;
    a1 = b1;
    a2 = b2;
    b = r;
    b1 = r1;
    b2 = r2;
  }

  s = a1;
  t = a2;
  assert(a >= 0);
  return a;
}

int main(void)
{
  int a, b, s, t, res;

  while (cin >> a >> b) {
    res = gcd(a, b, s, t);
    cout << res << "=" << a << "*" << s << "+"
         << b << "*" << t << endl;
  }
  return 0;
}
```

```cpp
/*
 * Prime Factorization
 *
 * Author: Ethan Kim
 * Complexity: O(sqrt(n))
 *
 * Takes an integer and writes out the prime factorization in
 * ascending order. Prints -1 first, when given a negative integer.
 *
 * Note: you can change this code to store the factors in an array or process
 * the factors in other ways.
 *
 * Also, this code works for all integers even on INT_MIN (note that negating
 * INT_MIN does nothing, but it still works because INT_MIN is a power of 2).
 *
 */

#include <iostream>

using namespace std;

void factor(int n) {
  int printed = 0;
  long long p;

  if (n == 0 || n == 1) {
    cout << n << endl;
    return;
  }
  if (n < 0) {
    n *= -1;
    cout << "-1" << endl;
    printed = 1;
  }

  while (n % 2 == 0) {
    n/=2;
    cout << "2" << endl;
    printed = 1;
  }

  for (p = 3; p*p <= n; p += 2) {
    while (n % p == 0) {
      n /= p;
      cout << p << endl;
      printed = 1;
    }
  }

  if(n>1 || !printed)
    cout << n << endl;
}

int main(void) {
  int p;
  while(cin >> p && p != 0) {
    factor(p);
  }
  return 0;
}
```

```cpp
// Gives the prime factorization of natural numbers (Uses probability)
//
// Author: Darcy Best
// Date  : January 7, 2010
//
// This should be used for factoring large integers. If you're
//   dealing with are small integers (N < 2^31), this is going
//   overboard. -- The normal sieve of Sieve of Eratosthenes is
//   usually good even for values up to 2^40.
//
// This implementation should only be used if you have numbers
//   larger than 2^40 (10^12) to factor.
//
// Notes:
//     - You need to handle N < 2 separately.
//     - Uses Miller-Rabin Primality Test
//          - This is a probabilistic test, there is a (1/4)^K
//                probability that a composite will return prime.
//                (K = 10 or 15 should be reasonably reliable).
//     - Uses Pollard's Rho algorithm to factor composites.
//          - I have also added Brent's improvement
//     - This program writes a number as a product of its primes,
//          with normal exponents (ie. "60 = 2^2 * 3 * 5")

#include <iostream>
#include <algorithm>
#include <set>
#include <map>
#include <cmath>
#include <ctime>
#include <cstdlib>
#include <vector>
using namespace std;

typedef long long int ll;

const ll MAX_NUM = 1e16;
const ll CB_RT = ll(pow(1.0*MAX_NUM,1.0/3)) + 2;
vector<ll> primes;
ll numPrimes;
ll c = 2;
const ll K = 10;

set<ll> lgPrimes;
map<ll,ll> semiPrimes;

ll gcd(ll a,ll b){
  ll r;
  while (b) {
    r = a % b;
    a = b;
    b = r;
  }
  return a;
}

ll mult_mod(ll x,ll y,ll n){
  ll res = 0;
  while(y){
    if(y % 2){
      y--;
      res += x;
      if(res >= n)
        res -= n;
    } else {
      x <<= 1;
      y >>= 1;
      if(x >= n)
        x -= n;
```

```cpp
    }
  }
  return res;
}

ll fast_exp_mod(ll b, ll n,ll m){
  ll res = 1;
  ll x = b;

  while (n) {
    if (n % 2) {
      n--;
      res = mult_mod(res,x,m);
    } else {
      n >>= 1;
      x = mult_mod(x,x,m);
    }
  }

  return res;
}

void genSmallPrimes(){
  bool isPrime[CB_RT+7];
  for(int i=3;i<CB_RT;i+=2)
    isPrime[i] = true;

  primes.clear();
  primes.push_back(2);

  int i;
  for(i=3;i*i<CB_RT;i+=2)
    if(isPrime[i]){
      primes.push_back(i);
      for(int j=i*i;j<CB_RT;j+=(2*i))
        isPrime[j] = false;
    }

  for(;i<CB_RT;i+=2)
    if(isPrime[i])
      primes.push_back(i);
  numPrimes = primes.size();
}

ll F(ll x,ll n){
  x = mult_mod(x,x,n);
  x -= c;
  return (x < 0 ? x + n : x);
}

ll pollardRho(ll n){
  ll b,g,x,y,z;
 newC:
  c++;
  g = b = x = 1;
  while(g == 1){
    z = 1;
    y = x;
    for(ll i=0;i<b;i++){
      x = F(x,n);
      z = mult_mod(z,abs(x-y),n);
    }
    g = gcd(z,n);
    b <<= 1;
  }
  if(g == n || g == 0)
    goto newC;

  c = 2;
```

```cpp
  return g;
}

bool miller(ll n){
  if (n == 2) return true;
  ll d = n-1;
  ll s = 0,a,x;
  while(d % 2 == 0){
    d >>= 1;
    s++;
  }
  for(int i=0;i<K;i++){
    a = (rand() % (n-2)) + 2; // [2,n-1];
    x = fast_exp_mod(a,d,n);
    if(x == 1 || x == n-1)
      continue;
    for(ll r=1;r<s;r++){
      x = mult_mod(x,x,n);
      if(x == 1)
        return false;
      if(x == n-1)
        goto nextK;
    }
    return false;
  nextK:;
  }
  return true;
}

void printEntry(bool& printed,ll prime,int ex){
  if(!printed)
    printed = true;
  else
    cout << "*";
  cout << prime;
  if(ex > 1)
    cout << "^" << ex;
}

void factor(ll x){
  cout << x << "=";
  bool printed = false;

  for(int i=0;i<numPrimes;i++)
    if(x % primes[i] == 0){
      int ex = 0; // Exponent
      do{
        x /= primes[i];
        ex++;
      } while(x % primes[i] == 0);
      printEntry(printed,primes[i],ex);
    }
  if(x == 1){
    cout << endl;
    return;
  }

  // lgPrimes and semiPrimes are useful if there
  //   is a lot repetition of large primes/semi-primes
  //   in the test data
  if(lgPrimes.find(x) != lgPrimes.end()){
    printEntry(printed,x,1);
    cout << endl;
    return;
  }

  if(semiPrimes.find(x) != semiPrimes.end()){
    ll lgFac = semiPrimes[x];
    printEntry(printed,x/lgFac,1);
```

```cpp
    printEntry(printed,lgFac,1);
    cout << endl;
    return;
  }

  if(miller(x)){ // if x is prime
    printEntry(printed,x,1);
    cout << endl;
    lgPrimes.insert(x);
    return;
  }

  // Pollard's Rho does not work well with squares,
  //   so we'll check for it manually.
  ll sqrtX = ll(sqrt(x) + 0.1);
  if(sqrtX*sqrtX == x){
    printEntry(printed,sqrtX,2);
    cout << endl;
    return;
  }

  ll smFac = pollardRho(x);
  ll lgFac = x/smFac;
  if(lgFac < smFac)
    swap(smFac,lgFac);
  printEntry(printed,smFac,1);
  printEntry(printed,lgFac,1);
  cout << endl;
  semiPrimes[x] = lgFac;
}

int main(){
  genSmallPrimes();
  srand((unsigned int) time(NULL));
  ll T,N;
  cin >> T;
  while(T--){
    cin >> N;
    factor(N);
  }
  return 0;
}
```

```
/*
 * Fenwick Tree
 *
 * Author: Howard Cheng
 * Reference:
 *
 *   Fenwick, P.M. "A New Data Structure for Cumulative Frequency Tables."
 *   Software---Practice and Experience, 24(3), 327-336 (March 1994).
 *
 * This code has been tested on UVa 11525 and 11610.
 *
 * Fenwick trees are data structures that allows the maintainence of
 * cumulative sum tables dynamically.  The following operations
 * are supported:
 *
 * - Initialize the tree from a list of N integers:               O(N log N)
 *
 * - Read the cumulative sum at index 0 <= k < N:                 O(log k)
 *
 * - Read the entry at index 0 <= k < N:                          O(log N)
 *
 * - Increment/decrement an entry at index 0 <= k < N in the list:  O(log N)
 *
 * - Given a value, find an index such that the cumulative sum at
 *   that position is the value:                                  O(log N)
 *
 * The space usage is at most 2*N for N input entries.
 *
 * NOTE: it is assumed that all entries are non-negative (even after a
 *       decrement operation).
 *
 */

#include <vector>
#include <cassert>

using namespace std;

class FenwickTree
{
public:
  FenwickTree(int n = 0)
    : N(n), tree(n)
  {
    iBM = 1;
    while (iBM < N) {
      iBM *= 2;
    }
    tree.resize(iBM+1);
    fill(tree.begin(), tree.end(), 0);
  }

  // initialize the tree with the given array of values
  FenwickTree(int val[], int n)
    : N(n)
  {
    iBM = 1;
    while (iBM < N) {
      iBM *= 2;
    }

    tree.resize(iBM+1);
    fill(tree.begin(), tree.end(), 0);
    for (int i = 0; i < n; i++) {
      assert(val[i] >= 0);
      incEntry(i, val[i]);
    }
  }
```

```
  // increment the entry at position idx by val (use negative val for
  // decrement).  All affected cumulative sums are updated.
  void incEntry(int idx, int val)
  {
    assert(0 <= idx && idx < N);
    if (idx == 0) {
      tree[idx] += val;
    } else {
      do {
        tree[idx] += val;
        idx += idx & (-idx);
      } while (idx < (int)tree.size());
    }
  }

  // return the cumulative sum val[0] + val[1] + ... + val[idx]
  int cumulativeSum(int idx) const
  {
    assert(0 <= idx && idx < (int)tree.size());
    int sum = tree[0];
    while (idx > 0) {
      sum += tree[idx];
      idx &= idx-1;
    }
    return sum;
  }

  // return the entry indexed by idx
  int getEntry(int idx) const
  {
    assert(0 <= idx && idx < N);
    int val, parent;
    val = tree[idx];
    if (idx > 0) {
      parent = idx & (idx-1);
      idx--;
      while (parent != idx) {
        val -= tree[idx];
        idx &= idx-1;
      }
    }
    return val;
  }

  // return the largest index such that the cumulative frequency is
  // what is given, or -1 if it is not found
  //
  int getIndex(int sum) const
  {
    int orig = sum;
    if (sum < tree[0]) return -1;
    sum -= tree[0];

    int idx = 0;
    int bitmask = iBM;

    while (bitmask != 0 && idx < (int)tree.size()-1) {
      int tIdx = idx + bitmask;
      if (sum >= tree[tIdx]) {
        idx = tIdx;
        sum -= tree[tIdx];
      }
      bitmask >>= 1;
    }

    if (sum != 0) {
      return -1;
    }
```

```
      idx = min(N-1, idx);
      return (cumulativeSum(idx) == orig) ? idx : -1;
  }

private:
  int N, iBM;
  vector<int> tree;
};
```

```
/*
 * Solution of systems of linear equations over the integers
 *
 * Author: Howard Cheng
 * Reference:
 *   K.O. Geddes, S.R. Czapor, G. Labahn.   "Algorithms for Computer Algebra."
 *   Kluwer Academic Publishers, 1992, pages 393-399.   ISBN 0-7923-9259-0
 *
 * The routine fflinsolve solves the system Ax = b where A is an n x n matrix
 * of integers and b is an n-dimensional vector of integers.
 *
 * The inputs to fflinsolve are the matrix A, the dimension n, and an
 * output array to store the solution x_star = det(A)*x.   The function
 * also returns the det(A).   In the case that det(A) = 0, the solution
 * vector is undefined.
 *
 * Note that the matrix A and b may be modified.
 *
 */

#include <iostream>

using namespace std;

const int MAX_N = 10;

int fflinsolve(int A[MAX_N][MAX_N], int b[], int x_star[], int n)
{
  int sign, d, i, j, k, k_c, k_r, pivot, t;

  sign = d = 1;

  for (k_c = k_r = 0; k_c < n; k_c++) {
    /* eliminate column k_c */

    /* find nonzero pivot */
    for (pivot = k_r; pivot < n && !A[pivot][k_r]; pivot++)
      ;

    if (pivot < n) {
      /* swap rows pivot and k_r */
      if (pivot != k_r) {
        for (j = k_c; j < n; j++) {
          t = A[pivot][j];
          A[pivot][j] = A[k_r][j];
          A[k_r][j] = t;
        }
        t = b[pivot];
        b[pivot] = b[k_r];
        b[k_r] = t;

        sign *= -1;
      }

      /* do elimination */
      for (i = k_r+1; i < n; i++) {
        for (j = k_c+1; j < n; j++) {
          A[i][j] = (A[k_r][k_c]*A[i][j]-A[i][k_c]*A[k_r][j])/d;
        }
        b[i] = (A[k_r][k_c]*b[i]-A[i][k_c]*b[k_r])/d;
        A[i][k_c] = 0;
      }
      if (d) {
        d = A[k_r][k_c];
      }
      k_r++;
    } else {
      /* entire column is 0, det(A) = 0 */
      d = 0;
```

```
    }
  }

  if (!d) {
    for (k = k_r; k < n; k++) {
      if (b[k]) {
        /* inconsistent system */
        cout << "Inconsistent system." << endl;
        return 0;
      }
    }
    /* multiple solutions */
    cout << "More than one solution." << endl;
    return 0;
  }

  /* now backsolve */
  for (k = n-1; k >= 0; k--) {
    x_star[k] = sign*d*b[k];
    for (j = k+1; j < n; j++) {
      x_star[k] -= A[k][j]*x_star[j];
    }
    x_star[k] /= A[k][k];
  }

  return sign*d;
}

int main(void)
{
  int A[MAX_N][MAX_N], x_star[MAX_N], b[MAX_N];
  int n, i, j;
  int det;

  while (cin >> n && 0 < n && n <= MAX_N) {
    cout << "Enter A:" << endl;
    for (i = 0; i < n; i++) {
      for (j = 0; j < n; j++) {
        cin >> A[i][j];
      }
    }
    cout << "Enter b:" << endl;
    for (i = 0; i < n; i++) {
      cin >> b[i];
    }
    if (det = fflinsolve(A, b, x_star, n)) {
      cout << "det = " << det << endl;
      cout << "x_star = ";
      for (i = 0; i < n; i++) {
        cout << x_star[i] << " ";
      }
      cout << endl;
    } else {
      cout << "A is singular." << endl;
    }
  }
  return 0;
}
```

```cpp
// Compute nth Fibonacci number with matrix exponentiation
//
// Time complexity: O(log(n))
//
// Author: Cody Barnson
//
// Warning: 46th Fibonacci number (i.e. fib(46)) is largest
// that will fit into signed 32-bit integer; use long long if need
// longer.  Or perhaps the problem asks for Fibonacci number mod m

int f[1000];
int fib(int n) {
  if (n < 2) return n;
  if (f[n]) return f[n];

  int k = (n + 1) / 2;
  f[n] = (n & 1) ? fib(k) * fib(k) + fib(k - 1) * fib(k - 1)
                 : (2 * fib(k - 1) + fib(k)) * fib(k);
  return f[n];
}
```

```
/*
 * Floyd's Algorithm
 *
 * Author: Howard Cheng
 *
 * The following code takes a graph stored in an adjacency matrix "graph",
 * and returns the shortest distance from node i to node j in dist[i][j].
 * We assume that the weights of the edges is not DISCONNECT, and the
 * DISCONNECT constant is used to indicate the absence of an edge.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

const int MAX_NODES = 26;
const int DISCONNECT = -1;

int graph[MAX_NODES][MAX_NODES];
int dist[MAX_NODES][MAX_NODES];

void floyd(void)
{
  int i, j, k;

  for (i = 0; i < MAX_NODES; i++) {
    for (j = 0; j < MAX_NODES; j++) {
      dist[i][j] = graph[i][j];
    }
  }

  for (k = 0; k < MAX_NODES; k++) {
    for (i = 0; i < MAX_NODES; i++) {
      for (j = 0; j < MAX_NODES; j++) {
        if (dist[i][k] != DISCONNECT && dist[k][j] != DISCONNECT) {
          int temp = dist[i][k] + dist[k][j];
          if (dist[i][j] == DISCONNECT || dist[i][j] > temp) {
            dist[i][j] = temp;
          }
        }
      }
    }
  }

  for (i = 0; i < MAX_NODES; i++) {
    dist[i][i] = 0;
  }
}

int main(void)
{
  int w;
  int i, j;

  /* clear graph */
  for (i = 0; i < MAX_NODES; i++) {
    for (j = 0; j < MAX_NODES; j++) {
      graph[i][j] = DISCONNECT;
    }
  }

  /* read graph */
  cin >> i >> j >> w;
  while (!(i == -1 && j == -1)) {
    assert(0 <= i && i < MAX_NODES && 0 <= j && j < MAX_NODES);
    graph[i][j] = graph[j][i] = w;
    cin >> i >> j >> w;
```

```
  }

  floyd();

  /* do queries */
  cin >> i >> j;
  while (!(i == -1 && j == -1)) {
    assert(0 <= i && i < MAX_NODES && 0 <= j && j < MAX_NODES);
    cout << i << " " << j << ":" << dist[i][j] << endl;
    cin >> i >> j;
  }

  return 0;
}
```

```
/*
 * Floyd's Algorithm
 *
 * Author: Howard Cheng
 *
 * The following code takes a graph stored in an adjacency matrix "graph",
 * and returns the shortest distance from node i to node j in dist[i][j].
 * We assume that the weights of the edges is not DISCONNECT, and the
 * DISCONNECT constant is used to indicate the absence of an edge.
 *
 * Call extract_path to return the path, as well as its length (in terms
 * of vertices).  The length is -1 if no such path exists.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

const int MAX_NODES = 26;
const int DISCONNECT = -1;

int graph[MAX_NODES][MAX_NODES];
int dist[MAX_NODES][MAX_NODES];
int succ[MAX_NODES][MAX_NODES];

void floyd(void)
{
  int i, j, k;

  for (i = 0; i < MAX_NODES; i++) {
    for (j = 0; j < MAX_NODES; j++) {
      dist[i][j] = graph[i][j];
      if (i == j || graph[i][j] == DISCONNECT) {
        succ[i][j] = -1;
      } else {
        succ[i][j] = j;
      }
    }
  }

  for (k = 0; k < MAX_NODES; k++) {
    for (i = 0; i < MAX_NODES; i++) {
      for (j = 0; j < MAX_NODES; j++) {
        if (i != k && dist[i][k] != DISCONNECT && dist[k][j] != DISCONNECT) {
          int temp = dist[i][k] + dist[k][j];
          if (dist[i][j] == DISCONNECT || dist[i][j] > temp) {
            dist[i][j] = temp;
            succ[i][j] = succ[i][k];
          } else if (dist[i][j] == temp && succ[i][k] < succ[i][j]) {
            /* put tie-breaking on paths here */

            /* e.g. the test above chooses lexicographically smallest */
            /*      paths, but ignores the number of vertices in the  */
            /*      path.  To really do lexicographically sorting     */
            /*      properly, you also need to have len[i][j] which   */
            /*      can be computed easily as well.                   */
            succ[i][j] = succ[i][k];
          }
        }
      }
    }
  }

  for (i = 0; i < MAX_NODES; i++) {
    dist[i][i] = 0;
  }
}
```

```
int extract_path(int u, int v, int path[])
{
  int len = 0;

  if (dist[u][v] == DISCONNECT) {
    return -1;
  }

  path[len++] = u;
  while (u != v) {
    u = succ[u][v];
    path[len++] = u;
  }

  return len;
}

int main(void)
{
  int m, w, i, j;
  int path[MAX_NODES], len;

  /* clear graph */
  for (i = 0; i < MAX_NODES; i++) {
    for (j = 0; j < MAX_NODES; j++) {
      graph[i][j] = DISCONNECT;
    }
  }

  /* read graph */
  cin >> i >> j >> w;
  while (!(i == -1 && j == -1)) {
    assert(0 <= i && i < MAX_NODES && 0 <= j && j < MAX_NODES);
    graph[i][j] = /*graph[j][i] =*/ w;
    cin >> i >> j >> w;
  }

  floyd();

  /* do queries */
  cin >> i >> j;
  while (!(i == -1 && j == -1)) {
    assert(0 <= i && i < MAX_NODES && 0 <= j && j < MAX_NODES);
    cout << i << " " << j << ":" << dist[i][j] << endl;
    len = extract_path(i, j, path);
    for (m = 0; m < len; m++) {
      if (m) {
        cout << " ";
      }
      cout << path[m];
    }
    cout << endl;
    cin >> i >> j;
  }

  return 0;
}
```

```cpp
// Converts a fraction (with integral numerator and denominator)
//   to its decimal expansion.
//
// Author: Darcy Best
// Date  : August 22, 2010
//
// Since we are dealing with rational numbers, one of two cases
//   occur:
//       1. The number will terminate
//       2. The number will repeat
//
// The algorithm is O(D) where D is the absolute value of the
//   denominator.

#include <iostream>
#include <string>
#include <algorithm>
#include <cstdlib>
#include <cassert>
using namespace std;

const int MAX_DENOM = 1001;

string itoa(int x){
  string ans;
  while(x){
    ans += (x % 10) + '0';
    x /= 10;
  }
  reverse(ans.begin(),ans.end());
  return (ans.length() ? ans : "0");
}

int firstSeen[MAX_DENOM];

void frac2dec(int numer,int denom,string& decimal,int& numRepDigs){
  assert(denom != 0);

  // Determine if it is a plus or a minus
  decimal = "";
  if(numer < 0 && denom >= 0 || numer >= 0 && denom < 0){
    decimal += "-";
  } else {
    decimal += "+";
  }
  numer = abs(numer);
  denom = abs(denom);

  // Left of the decimal point
  decimal += itoa(numer / denom);
  numer %= denom;
  if(!numer){
    numRepDigs = 0;
    return;
  }

  // Add the decimal point
  decimal += '.';

  // Right of the decimal point
  fill(firstSeen,firstSeen+denom,-1);
  int rem = numer;
  while(rem != 0 && firstSeen[rem] == -1){
    firstSeen[rem] = decimal.length();
    rem *= 10;

    decimal += itoa(rem / denom);
    rem %= denom;
  }
```

```cpp
  numRepDigs = (rem ? decimal.length() - firstSeen[rem] : 0);
}

int main(){
  int numerator,denominator,repDigs;
  string decimal;
  while(cin >> numerator >> slash >> denominator){
    frac2dec(numerator,denominator,decimal,repDigs);
    cout << numerator << "/" << denominator << "=" << decimal << endl;
    if(repDigs == 0)
      cout << "This expansion terminates." << endl;
    else
      cout << "The last " << repDigs << " digits repeat forever." << endl;
    cout << endl;
  }
  return 0;
}
```

```cpp
//
// Fraction implementation
//
// Author: Darcy Best
//
// Does NOT ever check for division by 0.
// Division by 0 will only cause a runtime error if you use the
//   toDouble() function.
//

#include <iostream>
#include <cstdlib>
using namespace std;

// Change this to whatever integer data type will prevent overflow
//    - BigInteger works with this class
typedef long long int dataType;

class Fraction{
public:
  Fraction(dataType num=0,dataType denom=1);

  double toDouble() const;

  void reduce();

  // Changes the fraction itself.
  void selfReciprocal();

  // Returns a new fraction, leaving the original.
  Fraction reciprocal() const;

  Fraction& operator+=(const Fraction& x);
  Fraction& operator-=(const Fraction& x);
  Fraction& operator*=(const Fraction& x);
  Fraction& operator/=(const Fraction& x);

  bool operator<(const Fraction& x) const;
  bool operator==(const Fraction& x) const;

  dataType num,denom;
};

Fraction operator+(const Fraction& x,const Fraction& y);
Fraction operator-(const Fraction& x,const Fraction& y);
Fraction operator*(const Fraction& x,const Fraction& y);
Fraction operator/(const Fraction& x,const Fraction& y);

istream& operator>>(istream& is,Fraction& x);
ostream& operator<<(ostream& os,const Fraction& x);

Fraction::Fraction(dataType n,dataType d){
  if(d < 0){
    num = -n;
    denom = -d;
  } else {
    num = n;
    denom = d;
  }
  reduce();
}

double Fraction::toDouble() const{
  return 1.0*num/denom;
}

// Howard's GCD function with no checks
dataType gcd(dataType a, dataType b)
{
```

```cpp
  dataType r;
  while (b) {
    r = a % b;
    a = b;
    b = r;
  }
  return a;
}

void Fraction::reduce(){
  dataType g = gcd(abs(num),denom);
  num /= g;
  denom /= g;
}

void Fraction::selfReciprocal(){
  swap(num,denom);
  if (denom < 0) {
    num = -num;
    denom = -denom;
  }
}

Fraction Fraction::reciprocal() const{
  return Fraction(denom,num);
}

// Overflow potential in the denominator.
// I've tried to factor out as much as possible before,
//   But be careful.
//
//    (w)/(a*g) + (z)/(b*g)
// = (w*b)/(a*g*b) + (a*z)/(a*g*b)
// = (w*b + a*z)/(a*g*b)
Fraction& Fraction::operator+=(const Fraction& x){
  dataType g = gcd(denom,x.denom);

  dataType a = denom / g;
  dataType b = x.denom / g;

  num = num * b + x.num * a;
  denom *= b;

  reduce();

  return (*this);
}

Fraction& Fraction::operator-=(const Fraction& x){
  dataType g = gcd(denom,x.denom);
  dataType a = denom / g;
  dataType b = x.denom / g;

  num = num * b - x.num * a;
  denom *= b;

  reduce();
  return (*this);
}

Fraction& Fraction::operator*=(const Fraction& x){
  num *= x.num;
  denom *= x.denom;
  reduce();
  return (*this);
}

Fraction& Fraction::operator/=(const Fraction& x){
  num *= x.denom;
```

```cpp
  denom *= x.num;

  if(denom < 0){
    num = -num;
    denom = -denom;
  }
  reduce();
  return (*this);
}

// Careful with overflow. If it is an issue, you can compare the
// double values, but you SHOULD check for equality BEFORE converting
bool Fraction::operator<(const Fraction& x) const{
  return (num*x.denom) < (x.num*denom);
}

bool Fraction::operator==(const Fraction& x) const{
  return (num == x.num) && (denom == x.denom);
}

Fraction operator+(const Fraction& x,const Fraction& y){
  Fraction a(x);
  a += y;
  return a;
}

Fraction operator-(const Fraction& x,const Fraction& y){
  Fraction a(x);
  a -= y;
  return a;
}

Fraction operator*(const Fraction& x,const Fraction& y){
  Fraction a(x);
  a *= y;
  return a;
}

Fraction operator/(const Fraction& x,const Fraction& y){
  Fraction a(x);
  a /= y;
  return a;
}

// Note that you can read in Fractions of two forms:
// a/b (With any number of space between a,/,b) - The input "points" to
//      the NEXT character after the denom (White space or not)
// c    (Just an integer - The input "points" to the next NON-WHITE SPACE
//      character. Careful when mixing this with getline.)
istream& operator>>(istream& is,Fraction& x){
  is >> x.num;

  char ch;
  is >> ch;
  if(ch != '/'){
    is.putback(ch);
    x.denom = 1;
  } else {
    is >> x.denom;
    if(x.denom < 0){
      x.num = -x.num;
      x.denom = -x.denom;
    }
    x.reduce();
  }

  return is;
}
```

```cpp
// Will output 5 for 5/1 and 0 for 0/1. If you want always
//     fractions, get rid of the if statement
ostream& operator<<(ostream& os,const Fraction& x){
  os << x.num;
  if(x.num != 0 && x.denom != 1)
    os << '/' << x.denom;
  return os;
}

int main(){
  Fraction x,y;
  while(cin >> x >> y){
    cout << "x:" << x << endl;
    cout << "y:" << y << endl;
    cout << "x+y= " << x+y << endl;
    cout << "x-y= " << x-y << endl;
    cout << "x*y= " << x*y << endl;
    cout << "x/y= " << x/y << endl;
    cout << endl;
  }
  return 0;
}
```

```
// Great Circle distance between two points using Heaverside formula
//
// Author: Howard Cheng
// Reference: http://mathforum.org/library/drmath/view/51879.html
//
// Given two points specified by their latitudes and longitudes, as well
// as the radius of the sphere, return the shortest distance between the
// two points along the surface of the sphere.
//
// latitude should be between -90 to 90 degrees (inclusive), and
// longitude should be between -180 to 180 degrees (inclusive)
//
// There are also routines that will convert between cartesian coordinates
// (x,y,z) and spherical coordinates (latitude, longitude, radius).
//

#include <iostream>
#include <iomanip>
#include <cmath>

using namespace std;

const double PI = acos(-1.0);

double greatcircle(double lat1, double long1, double lat2, double long2,
                   double radius)
{
  lat1 *= PI/180.0;
  lat2 *= PI/180.0;
  long1 *= PI/180.0;
  long2 *= PI/180.0;

  double dlong = long2 - long1;
  double dlat = lat2 - lat1;
  double a = sin(dlat/2)*sin(dlat/2) +
    cos(lat1)*cos(lat2)*sin(dlong/2)*sin(dlong/2);
  return radius * 2 * atan2(sqrt(a), sqrt(1-a));
}

void longlat2cart(double lat, double lon, double radius,
                  double &x, double &y, double &z)
{
  lat *= PI/180.0;
  lon *= PI/180.0;
  x = radius * cos(lat) * cos(lon);
  y = radius * cos(lat) * sin(lon);
  z = radius * sin(lat);
}

void cart2longlat(double x, double y, double z,
                  double &lat, double &lon, double &radius)
{
  radius = sqrt(x*x + y*y + z*z);
  lat = (PI/2 - acos(z / radius)) * 180.0 / PI;
  lon = atan2(y, x) * 180.0 / PI;
}

int main(void)
{
  int T;
  cin >> T;
  while (T-- > 0) {
    const double radius = 6371009;
    double lat1, long1, lat2, long2;

    cin >> lat1 >> long1 >> lat2 >> long2;

    double x1, y1, z1, x2, y2, z2;
```

```
    longlat2cart(lat1, long1, radius, x1, y1, z1);
    longlat2cart(lat2, long2, radius, x2, y2, z2);

    double d1 = sqrt((x1-x2)*(x1-x2) + (y1-y2)*(y1-y2) + (z1-z2)*(z1-z2));
    double d2 = greatcircle(lat1, long1, lat2, long2, radius);

    cout << fixed << setprecision(0) << d2 - d1 << endl;

    double radius1;
    cart2longlat(x1, y1, z1, lat1, long1, radius1);
    cout << lat1 << ' ' << long1 << ' ' << radius1 << endl;
  }
  return 0;
}
```

```cpp
// Heron's formula
//
// Computes the area of a triangle given the lengths of the three sides.
//
// Author: Howard Cheng
//

#include <iostream>
#include <iomanip>
#include <utility>
#include <cmath>

using namespace std;

// the lengths of the three sides are a, b, and c.  The routine returns
// the area of the triangle, or -1 if the three lengths do not make a
// triangle.
double area_heron(double a, double b, double c)
{
  if (a < b) swap(a, b);
  if (a < c) swap(a, c);
  if (b < c) swap(b, c);
  if (c < a - b) return -1;
  return sqrt((a+b+c)*(c-a+b)*(c+a-b)*(a+b-c))/4.0;
}

int main(void)
{
  double a, b, c;

  while (cin >> a >> b >> c) {
    cout << fixed << setprecision(4) << area_heron(a, b, c) << endl;
  }

  return 0;
}
```

```cpp
/*
 * Maximum/minimum weight bipartite matching
 *
 * Author: Howard Cheng
 * Reference:
 *   http://www.topcoder.com/tc?module=Static&d1=tutorials&d2=hungarianAlgorithm
 *
 * This file contains routines for computing the maximum/minimum weight
 * bipartite matching.
 *
 * It is assumed that each half of the graph has exactly N vertices, labelled
 * 0 to N-1.  The weight between vertex i on the left and vertex j on the
 * right is stored in G[i][j].  The cost of the optimal matching is returned,
 * and matching[i] is the vertex on the right that is matched to vertex i
 * on the left.
 *
 * If an edge is absent, the corresponding edge weight should be:
 *
 *    INT_MIN   if maximum weight matching is desired
 *    INT_MAX   if minimum weight matching is desired
 *
 * This is an implementation of the Hungarian algorithm.  The complexity
 * is O(N^3).
 *
 */

#include <iostream>
#include <algorithm>
#include <queue>
#include <cassert>
#include <climits>

using namespace std;

const int MAX_N = 3;

void update_labels(int lx[MAX_N], int ly[MAX_N], bool S[MAX_N], bool T[MAX_N],
                   int slack[MAX_N], int N)
{
  int delta;
  bool delta_init = false;

  for (int y = 0; y < N; y++) {
    if (T[y]) continue;
    delta = delta_init ? min(delta, slack[y]) : slack[y];
    delta_init = true;
  }
  for (int x = 0; x < N; x++) {
    if (S[x]) lx[x] -= delta;
  }
  for (int y = 0; y < N; y++) {
    if (T[y]) {
      ly[y] += delta;
    } else {
      slack[y] -= delta;
    }
  }
}

void add_to_tree(int x, int prevx, int G[MAX_N][MAX_N], bool S[MAX_N],
                 int prev[MAX_N], int lx[MAX_N], int ly[MAX_N],
                 int slack[MAX_N], int slackx[MAX_N], int N)
{
  S[x] = true;
  prev[x] = prevx;
  for (int y = 0; y < N; y++) {
    int temp = (G[x][y] == INT_MIN) ? INT_MAX : lx[x] + ly[y] - G[x][y];
    if (temp < slack[y]) {
      slack[y] = temp;
```

```cpp
      slackx[y] = x;
    }
  }
}

int max_weight_matching(int G[MAX_N][MAX_N], int N, int matching[MAX_N])
{
  int revmatch[MAX_N];          // match from right to left
  int max_match = 0;            // number of vertices in current matching

  fill(matching, matching+N, -1);
  fill(revmatch, revmatch+N, -1);

  // find an initial feasible labelling
  int lx[MAX_N], ly[MAX_N];
  fill(ly, ly+N, 0);
  for (int x = 0; x < N; x++) {
    lx[x] = *max_element(G[x], G[x]+N);
  }

  // now repeatedly find alternating tree, augment, and relabel
  while (max_match < N) {
    queue<int> q;
    bool S[MAX_N], T[MAX_N];
    int prev[MAX_N];
    fill(S, S+N, false);
    fill(T, T+N, false);
    fill(prev, prev+N, -1);

    // find root of alternating tree
    int root = find(matching, matching+N, -1) - matching;
    q.push(root);
    prev[root] = -2;
    S[root] = true;

    int slack[MAX_N], slackx[MAX_N];
    for (int y = 0; y < N; y++) {
      slack[y] = (G[root][y] == INT_MIN) ? INT_MAX :
        lx[root] + ly[y] - G[root][y];
      slackx[y] = root;
    }

    bool path_found = false;
    int x, y;
    while (!path_found) {

      // build alternating tree with BFS
      while (!path_found && !q.empty()) {
        x = q.front();
        q.pop();
        for (y = 0; y < N; y++) {
          // go through edges in equality graph
          if (G[x][y] == lx[x] + ly[y] && !T[y]) {
            if (revmatch[y] == -1) {
              path_found = true;
              break;
            }
            T[y] = true;
            q.push(revmatch[y]);
            add_to_tree(revmatch[y], x, G, S, prev, lx, ly, slack, slackx, N);
          }
        }
      }
      if (path_found) break;

      // no augmenting path, update the labels
      update_labels(lx, ly, S, T, slack, N);
      while (!q.empty()) {
        q.pop();
```

```
      }
      for (y = 0; y < N; y++) {
        if (!T[y] && slack[y] == 0) {
          if (revmatch[y] == -1) {
            x = slackx[y];
            path_found = true;
            break;
          } else {
            T[y] = true;
            if (!S[revmatch[y]]) {
              q.push(revmatch[y]);
              add_to_tree(revmatch[y], slackx[y], G, S, prev, lx, ly, slack,
                          slackx, N);
            }
          }
        }
      }
    }

    assert(path_found);
    max_match++;

    // augment along the path
    for (int cx = x, cy = y, ty; cx != -2; cx = prev[cx], cy = ty) {
      ty = matching[cx];
      revmatch[cy] = cx;
      matching[cx] = cy;
    }
  }

  // return the final answer
  int weight = 0;
  for (int x = 0; x < N; x++) {
    weight += G[x][matching[x]];
  }
  return weight;
}

int min_weight_matching(int G[MAX_N][MAX_N], int N, int matching[MAX_N])
{
  int M = INT_MIN;

  for (int i = 0; i < N; i++) {
    for (int j = 0; j < N; j++) {
      if (G[i][j] != INT_MAX) {
        M = max(M, G[i][j]);
      }
    }
  }

  int newG[MAX_N][MAX_N];
  for (int i = 0; i < N; i++) {
    for (int j = 0; j < N; j++) {
      newG[i][j] = (G[i][j] == INT_MAX) ? INT_MIN : M - G[i][j];
    }
  }
  int weight = max_weight_matching(newG, N, matching);
  return N*M - weight;
}

int main(void)
{
  int G[3][3] = { {INT_MAX,4,5}, {5,7,6}, {5,8,8} };
  int matching[3];

  int w = min_weight_matching(G, 3, matching);
  cout << "weight = " << w << endl;
  for (int i = 0; i < 3; i++) {
    cout << i << " is matched to " << matching[i] << endl;
```

```
  }
  return 0;
}
```

```
/*
 * Infix expressions evaluation
 *
 * Author: Howard Cheng
 *
 * The evaluate() routine takes a string containing an infix arithmetic
 * expression, and return the numeric result after evaluation.  The
 * parameter error indicates whether an error has occurred (syntax
 * error, illegal operation, etc.).  If there is an error the result
 * returned is meaningless.
 *
 * The routine assumes that the operands in the input are integers
 * with no leading signs.  It supports the standard +, -, *, / and
 * parentheses.  If you need to support more operators, operand types,
 * etc., you will need to modify the code.  See comments below.
 *
 */

#include <iostream>
#include <string>
#include <stack>
#include <cctype>
#include <cstdlib>

using namespace std;

// What is a token?  Modify if needed (e.g. to support variables, extra
// operators, etc.)
struct Token
{
  enum Type {NUMBER, PLUS, MINUS, TIMES, DIVIDE, LEFT_PAREN, RIGHT_PAREN};

  // priority of the operators: bigger number means higher priority
  // e.g. */ has priority 2, +- has priority 1, ( has priority 0
  int priority[7];

  // is the operator left associative?  It's assumed that all operators
  // of the same priority level has the same left/right associative property
  bool left_assoc[7];

  Type type;
  long val;

  Token()
  {
    priority[1] = priority[2] = 1;
    priority[3] = priority[4] = 2;
    priority[5] = 0;
    left_assoc[1] = left_assoc[2] = left_assoc[3] = left_assoc[4] = true;
  }

  int get_priority() {
    return priority[type];
  }

  bool is_left_assoc() {
    return left_assoc[type];
  }

  // returns true if there is a next token
  bool next_token(string &expr, int &start, bool &error)
  {
    int len = expr.length();

    error = false;
    while (start < len && isspace(expr[start])) {
      start++;
    }
    if (start >= len) {
```

```
      return false;
    }

    switch (expr[start]) {
    case '(':
      type = LEFT_PAREN;
      break;
    case ')':
      type = RIGHT_PAREN;
      break;
    case '*':
      type = TIMES;
      break;
    case '/':
      type = DIVIDE;
      break;
    case '+':
      type = PLUS;
      break;
    case '-':
      type = MINUS;
      break;
    default:
      // check for number
      const char *s = expr.c_str() + start;
      char *p;
      val = strtol(s, &p, 10);
      if (s == p) {
        error = true;
        return false;
      }
      type = NUMBER;
      start += (p - s);
    }
    if (type != NUMBER) {
      start++;
    }
    return true;
  }
};

// Modify this if you need to support more operators or change their
// meanings.
//
// returns true if operation is successful
bool apply_op(stack<long> &operands, Token token)
{
  long a, b;

  if (operands.size() < 2) {
    return false;
  }
  if (token.type == Token::PLUS) {
    b = operands.top(); operands.pop();
    a = operands.top(); operands.pop();
    operands.push(a+b);
  } else if (token.type == Token::MINUS) {
    b = operands.top(); operands.pop();
    a = operands.top(); operands.pop();
    operands.push(a-b);
  } else if (token.type == Token::TIMES) {
    b = operands.top(); operands.pop();
    a = operands.top(); operands.pop();
    operands.push(a*b);
  } else if (token.type == Token::DIVIDE) {
    b = operands.top(); operands.pop();
    a = operands.top(); operands.pop();
    if (b == 0) {
      return false;
```

```
    }
    operands.push(a/b);
  } else {
    return false;
  }
  return true;
}

long evaluate(string expr, bool &error)
{
  stack<Token> s;
  stack<long> operands;
  int i;
  Token token;

  error = false;
  i = 0;
  while (token.next_token(expr, i, error) && !error) {
    switch (token.type) {
    case Token::NUMBER:
      operands.push(token.val);
      break;
    case Token::LEFT_PAREN:
      s.push(token);
      break;
    case Token::RIGHT_PAREN:
      while (!(error = s.empty()) && s.top().type != Token::LEFT_PAREN) {
        if ((error = !apply_op(operands, s.top()))) {
          break;
        }
        s.pop();
      }
      if (!error) {
        s.pop();
      }
      break;
    default:        // arithmetic operators
      while (!error && !s.empty() &&
             (token.get_priority() < s.top().get_priority() ||
              token.get_priority() == s.top().get_priority() &&
              token.is_left_assoc())) {
        error = !apply_op(operands, s.top());
        s.pop();
      }
      if (!error) {
        s.push(token);
      }
    }
    if (error) {
      break;
    }
  }
  while (!error && !s.empty()) {
    error = !apply_op(operands, s.top());
    s.pop();
  }
  error |= (operands.size() != 1);
  if (error) {
    return 0;
  }
  return operands.top();
}

int main(void)
{
  int result;
  string expr;
  bool error;
```

```
  getline(cin, expr);
  while (!cin.eof()) {
    result = evaluate(expr, error);
    if (error) {
      cout << "Invalid expression" << endl;
    } else {
      cout << " = " << result << endl;
    }
    getline(cin, expr);
  }
  return 0;

}
```

```cpp
// Determines the point(s) of intersection if a circle and a circle
//
// Author: Darcy Best
// Date  : October 1, 2010
// Source: http://local.wasp.uwa.edu.au/~pbourke/geometry/2circle/
//
// Note: A circle of radius 0 must be considered independently.
// See comments in the implementation.

#include <iostream>
#include <iomanip>
#include <cmath>
#include <algorithm>
using namespace std;

#define SQR(X) ((X) * (X))

// How close to call equal
const double EPS = 1e-4;

bool dEqual(double x,double y){
  return fabs(x-y) < EPS;
}

struct Point{
  double x,y;
  bool operator<(const Point& a) const{
    if(dEqual(x,a.x))
      return y < a.y;
    return x < a.x;
  }
};

// Prints out the ordered pair. This also accounts for the negative 0.
void print(const Point& a){
  cout << "(";
  if(fabs(a.x) < 1e-4)
    cout << "0.000";
  else
    cout << a.x;
  cout << ",";
  if(fabs(a.y) < 1e-4)
    cout << "0.000";
  else
    cout << a.y;
  cout << ")";
}

struct Circle{
  double r,x,y;
};

// Input:
//   Two circles to intersect
//
// Output:
//   Number of points of intersection points
//   If 1 (or 2), then ans1 (and ans2) contain those points.
//   If 3, then there are infinitely many. (They're the same circle)
int intersect_circle_circle(Circle c1,Circle c2,Point& ans1,Point& ans2){

  // If we have two singular points
  if(fabs(c1.r) < EPS && fabs(c2.r) < EPS){
    if(dEqual(c1.x,c2.x) && dEqual(c1.y,c2.y)){
      ans1.x = c1.x;
      ans1.y = c1.y;
      // Here, you need to know what the intersection of two exact points is:
      //   "return 1;" - If the points intersect at only 1 point
      //   "return 3;" - If the circles are the same
```

```cpp
      // Note that both are true -- It all depends on the problem
      return 1;
    } else {
      return 0;
    }
  }

  double d = hypot(c1.x-c2.x,c1.y-c2.y);

  // Check if the circles are exactly the same.
  if(dEqual(c1.x,c2.x) && dEqual(c1.y,c2.y) && dEqual(c1.r,c2.r))
    return 3;

  // The circles are disjoint
  if(d > c1.r + c2.r + EPS)
    return 0;

  // One circle is contained inside the other -- No intersection
  if(d < abs(c1.r-c2.r) - EPS)
    return 0;

  double a = (SQR(c1.r) - SQR(c2.r) + SQR(d)) / (2*d);
  double h = sqrt(abs(SQR(c1.r) - SQR(a)));

  Point P;
  P.x = c1.x + a / d * (c2.x - c1.x);
  P.y = c1.y + a / d * (c2.y - c1.y);

  ans1.x = P.x + h / d * (c2.y - c1.y);
  ans1.y = P.y - h / d * (c2.x - c1.x);

  if(fabs(h) < EPS)
    return 1;

  ans2.x = P.x - h / d * (c2.y - c1.y);
  ans2.y = P.y + h / d * (c2.x - c1.x);

  return 2;
}

int main(){
  cout << fixed << setprecision(3);
  Circle C1,C2;
  Point a1,a2;

  while(cin >> C1.x >> C1.y >> C1.r >> C2.x >> C2.y >> C2.r){
    int num = intersect_circle_circle(C1,C2,a1,a2);
    switch(num){
    case 0:
      cout << "NO INTERSECTION" << endl;
      break;
    case 1:
      print(a1); cout << endl;
      break;
    case 2:
      if(a2 < a1)
        swap(a1,a2);
      print(a1);print(a2);cout << endl;
      break;
    case 3:
      cout << "THE CIRCLES ARE THE SAME" << endl;
      break;
    }
  }
  return 0;
}
```

```
/*
 * 2-D Line Intersection
 *
 * Author: Howard Cheng
 * Reference:
 *   http://www.exaflop.org/docs/cgafaq/cga1.html
 *
 * This routine takes two infinite lines specified by two points, and
 * determines whether they intersect at one point, infinitely points,
 * or no points.  In the first case, the point of intersection is also
 * returned.  The points of a line must be different (otherwise,
 * the line is not defined).
 *
 */

#include <iostream>
#include <cmath>
#include <cassert>

using namespace std;

/* how close to call equal */
const double EPSILON = 1E-8;

struct Point {
  double x, y;
};

/* returns 1 if intersect at a point, 0 if not, -1 if the lines coincide */
int intersect_iline(Point a, Point b, Point c, Point d, Point &p)
{
  double r;
  double denom, num1, num2;

  assert((a.x != b.x || a.y != b.y) && (c.x != d.x || c.y != d.y));

  num1 = (a.y - c.y)*(d.x - c.x) - (a.x - c.x)*(d.y - c.y);
  num2 = (a.y - c.y)*(b.x - a.x) - (a.x - c.x)*(b.y - a.y);
  denom = (b.x - a.x)*(d.y - c.y) - (b.y - a.y)*(d.x - c.x);

  if (fabs(denom) >= EPSILON) {
    r = num1 / denom;
    p.x = a.x + r*(b.x - a.x);
    p.y = a.y + r*(b.y - a.y);
    return 1;
  } else {
    if (fabs(num1) >= EPSILON) {
      return 0;
    } else {
      return -1;
    }
  }
}

int main(void)
{
  Point a, b, c, d, p;
  int res;

  while (cin >> a.x >> a.y >> b.x >> b.y >> c.x >> c.y >> d.x >> d.y) {
    res = intersect_iline(a, b, c, d, p);
    if (res == 1) {
      cout << "Intersect at (" << p.x << "," << p.y << ")" << endl;
    } else if (res == 0) {
      cout << "Don't intersect" << endl;
    } else {
      cout << "Infinite number of intersections" << endl;
    }
  }
```

```
  return 0;
}
```

```cpp
// Determines the point(s) of intersection if a circle and a line
//
// Author: Darcy Best
// Date  : May 1, 2010
// Source: http://mathworld.wolfram.com/Circle-LineIntersection.html

#include <iostream>
#include <cmath>
using namespace std;

#define SQR(X) ((X) * (X))

// How close to call equal
const double EPS = 1e-7;

bool dEqual(double x,double y){
  return fabs(x-y) < EPS;
}

struct Point{
  double x,y;
};

struct Line{
  Point p1,p2;
};

struct Circle{
  Point centre;
  double radius;
};

// Input of:
//  - 2 distinct points on the line
//  - The centre of the circle
//  - The radius of the circle
// Output:
//   Number of points of intersection points
//   If 1 or 2, then ans1 and ans2 contain those points.
int intersect_iline_circle(Line l,Circle c,Point& ans1,Point& ans2){
  Point p1 = l.p1;
  Point p2 = l.p2;

  Point circCentre = c.centre;
  double rad = c.radius;

  p1.x -= circCentre.x;
  p2.x -= circCentre.x;
  p1.y -= circCentre.y;
  p2.y -= circCentre.y;

  double dx = p2.x - p1.x;
  double dy = p2.y - p1.y;
  double dr = SQR(dx) + SQR(dy);
  double D  = p1.x*p2.y - p2.x*p1.y;

  double desc = SQR(rad)*dr - SQR(D);

  if(dEqual(desc,0)){
    ans1.x = circCentre.x + (D*dy) / dr;
    ans1.y = circCentre.y + (-D*dx) / dr;
    return 1;
  } else if(desc < 0){
    return 0;
  }

  double sgn = (dy < -EPS ? -1 : 1);

  ans1.x = circCentre.x + (D*dy + sgn*dx*sqrt(desc)) / dr;
```

```cpp
  ans1.y = circCentre.y + (-D*dx + abs(dy)*sqrt(desc)) / dr;

  ans2.x = circCentre.x + (D*dy - sgn*dx*sqrt(desc)) / dr;
  ans2.y = circCentre.y + (-D*dx - abs(dy)*sqrt(desc)) / dr;

  return 2;
}

int main(){
  Line L;
  Circle C;
  Point a1,a2;

  cin >> L.p1.x >> L.p1.y >> L.p2.x >> L.p2.y;
  cin >> C.centre.x >> C.centre.y >> C.radius;

  int num = intersect_iline_circle(L,C,a1,a2);
  if(num == 0)
    cout << "NO INTERSECTION." << endl;
  else if(num == 1)
    cout << "ONE INTERSECTION: (" << a1.x << "," << a1.y << ")" << endl;
  else if(num == 2)
    cout << "TWO INTERSECTIONS:(" << a1.x << "," << a1.y << ")"
         << "(" << a2.x << "," << a2.y << ")" << endl;

  return 0;
}
```

```cpp
/*
 * 2-D Line Intersection
 *
 * Author: Howard Cheng
 * Reference:
 *    http://www.exaflop.org/docs/cgafaq/cga1.html
 *
 * This routine takes two line segments specified by endpoints, and
 * determines whether they intersect at one point, infinitely points,
 * or no points.  In the first case, the point of intersection is also
 * returned.  The endpoints of a line must be different (otherwise,
 * the line is not defined).
 *
 */

#include <iostream>
#include <cmath>
#include <cassert>

using namespace std;

/* how close to call equal */
const double EPSILON = 1E-8;

struct Point {
  double x, y;
};

/* returns 1 if intersect at a point, 0 if not, -1 if the lines coincide */
int intersect_line(Point a, Point b, Point c, Point d, Point &p)
{
  Point t;
  double r, s;
  double denom, num1, num2;

  assert((a.x != b.x || a.y != b.y) && (c.x != d.x || c.y != d.y));

  num1 = (a.y - c.y)*(d.x - c.x) - (a.x - c.x)*(d.y - c.y);
  num2 = (a.y - c.y)*(b.x - a.x) - (a.x - c.x)*(b.y - a.y);
  denom = (b.x - a.x)*(d.y - c.y) - (b.y - a.y)*(d.x - c.x);

  if (fabs(denom) >= EPSILON) {
    r = num1 / denom;
    s = num2 / denom;
    if (0-EPSILON <= r && r <= 1+EPSILON &&
        0-EPSILON <= s && s <= 1+EPSILON) {
      /* always do this part if we are interested in lines instead */
      /* of line segments                                          */
      p.x = a.x + r*(b.x - a.x);
      p.y = a.y + r*(b.y - a.y);
      return 1;
    } else {
      return 0;
    }
  } else {
    if (fabs(num1) >= EPSILON) {
      return 0;
    } else {
      /* I am not using "fuzzy comparisons" here, because the comparisons */
      /* are based on the input, not some derived quantities.  You may    */
      /* want to change that if the input points are computed somehow.    */

      /* two lines are the "same".  See if they overlap */
      if (a.x > b.x || (a.x == b.x && a.y > b.y)) {
        t = a;
        a = b;
        b = t;
      }
      if (c.x > d.x || (c.x == d.x && c.y > d.y)) {
```

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        t = c;
        c = d;
        d = t;
      }
      if (a.x == b.x) {
        /* vertical lines */
        if (b.y == c.y) {
          p = b;
          return 1;
        } else if (a.y == d.y) {
          p = a;
          return 1;
        } else if (b.y < c.y || d.y < a.y) {
          return 0;
        } else {
          return -1;
        }
      } else {
        if (b.x == c.x) {
          p = b;
          return 1;
        } else if (a.x == d.x) {
          p = a;
          return 1;
        } else if (b.x < c.x || d.x < a.x) {
          return 0;
        } else {
          return -1;
        }
      }

      return -1;
    }
  }
}

int main(void)
{
  Point a, b, c, d, p;
  int res;

  while (cin >> a.x >> a.y >> b.x >> b.y >> c.x >> c.y >> d.x >> d.y) {
    res = intersect_line(a, b, c, d, p);
    if (res == 1) {
      cout << "Intersect at (" << p.x << "," << p.y << ")" << endl;
    } else if (res == 0) {
      cout << "Don't intersect" << endl;
    } else {
      cout << "Infinite number of intersections" << endl;
    }
  }

  return 0;
}
```

```cpp
/*
 * Line Intersection
 *
 * Author: Howard Cheng
 * Reference:
 *   CLRS, "Introduction to Algorithms", 2nd edition, pages 936-939.
 *
 * Given two lines specified by their endpoints (a1, a2) and (b1, b2),
 * returns true if they intersect, and false otherwise.  The intersection
 * point is not known.
 *
 */

#include <iostream>
#include <cmath>

using namespace std;

/* how close to call equal */
const double EPSILON = 1E-8;

struct Point {
  double x, y;
};

double direction(Point p1, Point p2, Point p3)
{
  double x1 = p3.x - p1.x;
  double y1 = p3.y - p1.y;
  double x2 = p2.x - p1.x;
  double y2 = p2.y - p1.y;
  return x1*y2 - x2*y1;
}

int on_segment(Point p1, Point p2, Point p3)
{
  return ((p1.x <= p3.x && p3.x <= p2.x) || (p2.x <= p3.x && p3.x <= p1.x)) &&
    ((p1.y <= p3.y && p3.y <= p2.y) || (p2.y <= p3.y && p3.y <= p1.y));
}

int intersect(Point a1, Point a2, Point b1, Point b2)
{
  double d1 = direction(b1, b2, a1);
  double d2 = direction(b1, b2, a2);
  double d3 = direction(a1, a2, b1);
  double d4 = direction(a1, a2, b2);

  if (((d1 > EPSILON && d2 < -EPSILON) || (d1 < -EPSILON && d2 > EPSILON)) &&
      ((d3 > EPSILON && d4 < -EPSILON) || (d3 < -EPSILON && d4 > EPSILON))) {
    return 1;
  } else {
    return (fabs(d1) < EPSILON && on_segment(b1, b2, a1)) ||
      (fabs(d2) < EPSILON && on_segment(b1, b2, a2)) ||
      (fabs(d3) < EPSILON && on_segment(a1, a2, b1)) ||
      (fabs(d4) < EPSILON && on_segment(a1, a2, b2));
  }
}

int main(void)
{
  Point a, b, c, d;
  int a1, a2, a3, a4, a5, a6, a7, a8;

  while (cin >> a1 >> a2 >> a3 >> a4 >> a5  >> a6 >> a7 >> a8) {
    a.x = a1; a.y = a2;
    b.x = a3; b.y = a4;
    c.x = a5; c.y = a6;
    d.x = a7; d.y = a8;
    if (intersect(a, b, c, d)) {
```

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      cout << "Yes" << endl;
    } else {
      cout << "No" << endl;
    }
  }
  return 0;
}
```

```
/*
 * Integer multiplication/division without overflow
 *
 * Author: Howard Cheng
 *
 * Given a list of factors in the numerator (num, size n) and a list
 * of factors in the denominator (dem, size m), it returns the product
 * of the numerator divided by the denominator.  It is assumed that
 * the numerator is divisible by the denominator (ie. the result
 * is an integer).  Overflow will not occur as long as the final result
 * is representable.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

int gcd(int a, int b)
{
    int r;

    while (b) {
        r = a % b;
        a = b;
        b = r;
    }
    assert(a >= 0);
    return a;
}

int mult(int A[], int n, int B[], int m)
{
    int i, j, prod, d;
    int count = 0;

    /* unnecessary if the two lists are positive */
    for (i = 0; i < n; i++) {
        if (A[i] < 0) {
            A[i] *= -1;
            count++;
        }
    }
    for (i = 0; i < m; i++) {
        if (B[i] < 0) {
            B[i] *= -1;
            count++;
        }
    }

    for (i = 0; i < n; i++) {
        for (j = 0; j < m; j++) {
            d = gcd(A[i], B[j]);
            A[i] /= d;
            B[j] /= d;
        }
    }
    prod = 1;
    for (i = 0; i < n; i++) {
        prod *= A[i];
    }
    for (j = 0; j < m; j++) {
        assert(B[j] == 1);
    }
    return (count % 2 == 0) ? prod : -prod;
}

int main(void)
```

```
{
    int A[1000], B[1000], n, m, i;

    while (cin >> n >> m && n > 0 && m > 0) {
        for (i = 0; i < n; i++) {
            cin >> A[i];
        }
        for (i = 0; i < m; i++) {
            cin >> B[i];
        }
        cout << "prod = " << mult(A,n,B,m) << endl;
    }

    return 0;
}
```

```c
/*
 * All-integer programming
 *
 * Author: Howard Cheng
 * Reference:
 *   http://www.cs.sunysb.edu/~algorith/implement/syslo/distrib/processed/
 *
 * This algorithm is based on GOMORY cutting plane method.
 *
 * This algorithm solves the following INTEGER LP problem:
 *
 * minimize      SUM  (A[0][j] * x[j])          [cost function]
 *             (j=0 to n-1)
 *
 *    s.t.        SUM  (A[i][j]*x[j])  <=  A[i][n]   1 <= i <= m
 *             (j=0 to n-1)
 *
 *    and         x[j] >= 0        0 <= j <= n-1
 *
 * n = number of variables
 * m = number of constraints
 *
 * Input : An input array A with m+n+1 rows and n+1 columns.
 *         Store the cost function in row 0, and the constraints in rows
 *         1 to m.  Set A[0][n] = 0.
 *         A vector x allocated for n values to store returned value.
 *
 * Output: Returns 1 if a solution is found, 0 if no solution exists.
 *         The minimum value of the cost function is returned in
 *          value.
 *         The variable assignment to x[j] that gives the minimum is given
 *          in x[j], where 0 <= j <= n-1.
 *
 * Important Notes:
 *
 * 1. If we want to have constraints that are >=, just multiply all the
 *    coefficients by -1.
 * 2. If we want to have constraints that are ==, do both >= and <=.
 * 3. The contents of A is destroyed after this routine.
 * 4. The coefficients in the cost function must be positive.  If not,
 *    make a change of variable x'[i] = m[i]-x[i] where m[i] is the
 *    maximum value for variable[i] and adjust all constraints as well
 *    as the returned optimal value.  This is especially useful if you
 *    wish to maximize the cost function.
 *
 *    Usually there is some maximum for each variable if you wish to
 *    maximize the function (or the value could be infinity.
 *
 *    NOTE: if any coefficient in the objective function is negative or
 *          0, the routine will crash.
 *
 * 5. If one only wishes to know if there is any variable assignment
 *    satisfying the constraints, just put 1 in each coefficient
 *    of the objective function.
 */

#include <stdio.h>
#include <assert.h>


#define MAX_VARS  50
#define MAX_CONS  50
#define MAX_ROWS  MAX_VARS+MAX_CONS+1
#define MAX_COLS  MAX_VARS+1

int euclid(int u, int v)
{
  int w = u / v;
  if (w*v > u) {
```

```c
    w--;
  }
  if ((w+1)*v <= u) {
    w++;
  }
  return w;
}

int int_prog(int A[MAX_ROWS][MAX_COLS], int n, int m, int *value, int *x)
{
  int iter, nosol;
  int b, c, i, j, k, l, r, r1, s, t, denom, num;

  for (j = 0; j < n; j++) {
    if (A[0][j] <= 0) {
      // BAD objective function coefficient: make sure it is positive
      assert(false);
    }
  }

  /* set constraints that x[j] >= 0, and clear output */
  for (i = 0; i < n; i++) {
    for (j = 0; j < n+1; j++) {
      A[m+1+i][j] = 0;
    }
    A[m+1+i][i] = -1;
  }
  A[0][n] = 0;

  nosol = 0;
  do {
    r = 0;
    do {
      iter = (A[++r][n] < 0);
    } while (!iter && r != n+m);
    if (iter) {
      for (k = iter = 0; k < n && !iter; k++) {
        iter = (A[r][k] < 0);
      }
      nosol = !iter;
      if (iter) {
        l = k-1;
        for (j = k; j < n; j++) {
          if (A[r][j] < 0) {
            for (i = 0; !(s = A[i][j] - A[i][l]); i++)
              ;
            if (s < 0) {
              l = j;
            }
          }
        }
        for (s = 0; !A[s][l]; s++)
          ;
        num = -A[r][l];
        denom = 1;
        for (j = 0; j < n; j++) {
          if (A[r][j] < 0 && j != l) {
            for (i = s-1, b = 1; b && i >= 0; i--) {
              b = (A[i][j] == 0);
            }
            if (b) {
              i = A[s][j];
              r1 = A[s][l];
              t = euclid(i, r1);
              if (t*r1 == i && t > 1) {
                for (i = s+1; !(r1 = t*A[i][l] - A[i][j]); i++)
                  ;
                if (r1 > 0) {
                  t--;
```

```
                    }
                }
                c = -A[r][j];
                if (c*denom > t*num) {
                  num = c;
                  denom = t;
                }
              }
            }
          }
          for (j = 0; j <= n; j++) {
            if (j != l) {
              c = euclid(A[r][j]*denom, num);
              if (c) {
                for (i = 0; i <= n+m; i++) {
                  A[i][j] += c*A[i][l];
                }
              }
            }
          }
        }
      }
    }
  } while (iter && !nosol);

  *value = -A[0][n];
  for (j = 0; j < n; j++) {
    x[j] = A[m+1+j][n];
  }

  return !nosol;
}

int main(void)
{
  int A[MAX_ROWS][MAX_COLS];
  int x[MAX_VARS];
  int val, t;
  int m, n, i, j;

  while (scanf("%d %d", &n, &m) == 2 && n > 0 && m > 0) {
    /* read cost function */
    printf("Input cost function to minimize:\n");
    for (i = 0; i < n; i++) {
      scanf("%d", &A[0][i]);
    }

    /* read constraints */
    for (i = 1; i <= m; i++) {
      printf("Input constraint #%d:\n", i);
      for (j = 0; j < n+1; j++) {
        scanf("%d", &A[i][j]);
      }
    }

    t = int_prog(A, n, m, &val, x);
    if (t) {
      printf("Minimum cost = %d\n", val);
      for (i = 0; i < n; i++) {
        printf("x[%2d] = %2d\n", i, x[i]);
      }
    } else {
      printf("No solution exists.\n");
    }
  }

  return 0;
}
```

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```cpp
//
// Josephus Problem
//
// Author: Darcy Best
// Date  : September 4, 2010
//
// The Josephus problem:
//    A group of n people are in a circle, and you start by killing
//      person f. Then, you kill every kth person until only one person
//      is left.
//
// Two implementations are given here (Note that neither depend on k):
//    1. Determine the survivor              -- O(n)
//    2. Determine the full killing order -- O(n^2)
//
// If there are 17 people, with every 5th person killed (killing the
//    1st person first), the kill order is:
//      1,6,11,16,5,12,2,9,17,10,4,15,14,3,8,13,7 (survivor = 7)
//
// NOTE: This is 1-based, not 0-based.

#include <iostream>
using namespace std;

const int MAX_N = 100;

int survivor(int n,int f,int k){
  return (n==1 ? 1 : (survivor(n-1,k,k) + (f-1)) % n + 1);
}

void killOrder(int n,int f,int k,int A[]){
  if(n == 0) return;
  A[0] = 0;
  killOrder(n-1,k,k,A+1);
  for(int i=0;i<n;i++)
    A[i] = (A[i] + (f-1)) % n + 1;
}

int main(){
  int n,f,k,kOrder[MAX_N];
  while(cin >> n >> f >> k && (n || f || k)){
    killOrder(n,f,k,kOrder);
    for(int i=0;i<n;i++)
      cout << kOrder[i] << endl;

    cout << "Survivor: " << survivor(n,f,k) << endl;
  }
  return 0;
}
```

```cc
/*
 * KMP String Matching
 *
 * Author: Howard Cheng
 *
 * The prepare_pattern routine takes in the pattern you wish to search
 * for, and perform some processing to give a "failure array" to be used
 * by the actual search.  The complexity is linear in the length of the
 * pattern.
 *
 * The find_pattern routine takes in a string s, a pattern pat, and a
 * vector T computed by prepare_pattern.  It returns the index of the
 * first occurrence of pat in s, or -1 if it does not occur in s.
 * The complexity is linear in the length of the string s.
 *
 */

#include <iostream>
#include <string>
#include <vector>
#include <algorithm>

using namespace std;

void prepare_pattern(const string &pat, vector<int> &T)
{
  int n = pat.length();
  T.resize(n+1);
  fill(T.begin(), T.end(), -1);
  for (int i = 1; i <= n; i++) {
    int pos = T[i-1];
    while (pos != -1 && pat[pos] != pat[i-1]) {
      pos = T[pos];
    }
    T[i] = pos + 1;
  }
}

int find_pattern(const string &s, const string &pat, const vector<int> &T)
{
  int sp = 0, kp = 0;
  int slen = s.length(), plen = pat.length();
  while (sp < slen) {
    while (kp != -1 && (kp == plen || pat[kp] != s[sp])) {
      kp = T[kp];
    }
    kp++;    sp++;
    if (kp == plen) {
      // a match is found
      return sp - plen;

      // if you want more than one match (i.e. all matches), do not return
      // in the above but rather record the location of the match.  Continue
      // the loop with:
      //
      // kp = T[kp];
    }
  }
  return -1;
}

int main(void)
{
  string str, pat;

  while (cin >> str >> pat) {
    vector<int> T;
    prepare_pattern(pat, T);
    cout << "index = " << find_pattern(str, pat, T) << endl;
```

```cc
  }
  return 0;
}
```

```
/*
 * Solution of systems of linear equations
 *
 * Author: Howard Cheng
 * Reference:
 *   K.E. Atkinson. "An Introduction to Numerical Analysis."  2nd Ed., John
 *   Wiley & Sons, 1988, pages 520-521.  ISBN 0-471-62489-6
 *
 * To solve the system Ax = b where A is an n x n matrix, first call
 * LU_decomp on A to obtain its LU decomposition.  Once the LU
 * decomposition is obtained, it can be used to solve linear systems with
 * the same coefficient matrix A but different vectors of b using the
 * LU_solve routine.  This routine is numerically stable (provided that
 * the original coefficient matrix has a small condition number).
 *
 * The inputs to LU_decomp are the matrix A, the dimension n, an
 * output array pivot of n-1 elements such that pivot[i] = j means
 * that rows i and j were swapped during the i-th step, and an output
 * parameter to return the determinant of the matrix.  The function
 * returns 1 if successful, and 0 if the matrix is singular.  The
 * matrix A is overwritten by its LU decomposition on return.  If the
 * matrix is singular, the content of A should not be used (it represents
 * intermediate results during the decomposition).
 *
 * The inputs to LU_solve are the LU decomposition of A, the dimension
 * n, the pivot array from LU_decomp, and n-dimensional vectors b and
 * x.  This function should be called only if the original matrix A
 * has a small condition number.  You can check this by checking that
 * the determinant returned by LU_decomp is not too close to 0.  This is
 * only a crude check: you should really be computing the condition number
 * of the matrix.
 *
 */

#include <iostream>
#include <cmath>

using namespace std;

const int MAX_N = 10;

int LU_decomp(double A[MAX_N][MAX_N], int n, int pivot[], double &det)
{
  double s[MAX_N];              /* factors used in implicit scaling */
  double c, t;
  int i, j, k;

  det = 1.0;

  /* compute s[i] */
  for (i = 0; i < n; i++) {
    s[i] = 0.0;
    for (j = 0; j < n; j++) {
      if ((t = fabs(A[i][j])) > s[i]) {
        s[i] = t;
      }
    }
    if (s[i] == 0.0) {
      /* a row of zeroes: singular */
      det = 0.0;
      return 0;
    }
  }

  /* do the row reductions */
  for (k = 0; k < n-1; k++) {
    c = fabs(A[k][k]/s[k]);
    pivot[k] = k;
    for (i = k+1; i < n; i++) {
```

```
      t = fabs(A[i][k]/s[i]);
      if (t > c) {
        c = t;
        pivot[k] = i;
      }
    }

    if (c == 0) {
      /* pivot == 0: singular */
      det = 0.0;
      return 0;
    }

    /* do row exchange */
    if (k != pivot[k]) {
      det *= -1.0;
      for (j = k; j < n; j++) {
        t = A[k][j];
        A[k][j] = A[pivot[k]][j];
        A[pivot[k]][j] = t;
      }
      t = s[k];
      s[k] = s[pivot[k]];
      s[pivot[k]] = t;
    }

    /* do the row reduction */
    for (i = k+1; i < n; i++) {
      A[i][k] /= A[k][k];
      for (j = k+1; j < n; j++) {
        A[i][j] -= A[i][k] * A[k][j];
      }
    }

    det *= A[k][k];
  }

  /* note that the algorithm as state in the book is incorrect.  The */
  /* following is need to ensure that the last row is not all 0's.   */
  /* (maybe the book is correct, depending on what you think it's     */
  /* supposed to do.)                                                 */
  if (A[n-1][n-1] == 0.0) {
    det = 0.0;
    return 0;
  } else {
    det *= A[n-1][n-1];
    return 1;
  }
}

void LU_solve(double A[MAX_N][MAX_N], int n, int pivot[], double b[],
              double x[])
{
  double t;
  int i, j, k;

  for (i = 0; i < n; i++) {
    x[i] = b[i];
  }
  for (k = 0; k < n-1; k++) {
    /* swap if necessary */
    if (k != pivot[k]) {
      t = x[k];
      x[k] = x[pivot[k]];
      x[pivot[k]] = t;
    }

    for (i = k+1; i < n; i++) {
      x[i] -= A[i][k] * x[k];
```

```
    }
  }

  x[n-1] /= A[n-1][n-1];

  for (i = n-2; i >= 0; i--) {
    for (j = i+1; j< n; j++) {
      x[i] -= A[i][j] * x[j];
    }
    x[i] /= A[i][i];
  }
}

int main(void)
{
  double A[MAX_N][MAX_N], x[MAX_N], b[MAX_N];
  int pivot[MAX_N];                    /* only n-1 is needed, but what the heck */
  int n, i, j;
  double det;

  while (cin >> n && 0 < n && n <= MAX_N) {
    cout << "Enter A:" << endl;
    for (i = 0; i < n; i++) {
      for (j = 0; j < n; j++) {
        cin >> A[i][j];
      }
    }
    cout << "Enter b:";
    for (i = 0; i < n; i++) {
      cin >> b[i];
    }
    if (LU_decomp(A, n, pivot, det)) {
      LU_solve(A, n, pivot, b, x);
      cout << "LU decomposition of A:" << endl;
      for (i = 0; i < n; i++) {
        for (j = 0; j < n; j++) {
          cout << A[i][j] << " ";
        }
        cout << endl;
      }
      cout << "det = " << det << endl;
      cout << "x = ";
      for (i = 0; i < n; i++) {
        cout << x[i] << " ";
      }
      cout << endl;
    } else {
      cout << "A is singular" << endl;
    }
  }
  return 0;
}
```

```c
/* unweighted matching in a bipartite graph.
 * author: Matthew McNaughton, Jan 16, 1999.
 * mcnaught@cs.ualberta.ca
 *
 * The bipartite graph G is split into two sets, U and V,
 * of user-defined maximum size MAXU and MAXV.
 * the input graph is in bipgraph[MAXU][MAXV].
 * there is an edge between node u \in U and node v \in V
 * iff bipgraph[u][v] != 0.
 *
 * The output is in matching[MAXU].
 * node u \in U and node v \in V are matched iff matching[u] == v.
 *
 * parameters match(int u, int v) mean: u is the number of vertices
 * in U, v the  number in V. They are assumed to be numbered 0 .. u-1
 * and 0 .. v-1, respectively.
 *
 * Technique: given a non-maximum matching M on G, find an "alternating path"
 * u_1 v_1 ... u_n v_n so that u_1 and v_n are not matched in M, but
 * v_k and u_k+1 are matched with each other. Then "flip" the edges so
 * that edges on this path which were not in the matching are, and edges
 * which were are not. This increases the size of the matching by one.
 * It is a fact that if no such path exists, then M is maximum.
 *
 * This algorithm finds several alternating paths at once by performing
 * bfs starting at all unmatched nodes u \in U. Paths which do not
 * have intersecting nodes can be alternated in the same bfs run.
 * bfs is performed repeated until the matching cannot be expanded.
 */

#include <stdio.h>
#include <string.h>
#include <assert.h>

FILE *in, *out;

/* change these as necessary */
#define MAXU 100
#define MAXV 100

#define U(i) (i)
#define V(i) ((i) + MAXU)
#define isU(i) ((i) < MAXU)
#define isV(i) ((i) >= MAXU)

#define isMatched(i) (isU(i) ? flagUmatched[(i)] : flagVmatched[(i)-MAXU])
#define isUsed(i) (isU(i) ? flagUused[(i)] : flagVused[(i)-MAXU])
#define isVisited(i) (isU(i) ? flagUvisited[(i)] : flagVvisited[(i)-MAXU])

#define setMatched(i) (isU(i)?(flagUmatched[(i)]=1):(flagVmatched[(i)-MAXU]=1))
#define setUsed(i) (isU(i)?(flagUused[(i)]=1):(flagVused[(i)-MAXU]=1))
#define setVisited(i) (isU(i)?(flagUvisited[(i)]=1):(flagVvisited[(i)-MAXU]=1))

char bipgraph[MAXU][MAXV];
int matching[MAXU]; /* matching[u] == v, _not_ plus MAXU */
char flagUmatched[MAXU], flagVmatched[MAXV];
char flagUvisited[MAXU], flagVvisited[MAXV];
char flagUused[MAXU],    flagVused[MAXV];
int predecessor[MAXU+MAXV], queue[MAXU+MAXV];

/* u and v are the number of vertices in sets U, and V, respectively,
 * filling up bipgraph[0..u-1][0..v-1].
 * result:
 *   matching[u0]==v0 iff u0 and v0 are in the matching,
 * otherwise matching[u0] = -1 */
void
match(int u, int v) {
  int i,j, head,tail, bad, last, increased;
```

```c
  for( i = 0; i < u; i++ ) {
    matching[i] = -1;
    flagUmatched[i] = 0;
  }
  for( i = 0; i < v; i++ ) flagVmatched[i] = 0;

  do { /* find alternating paths by repeated bfs. */
    for( i = 0; i < MAXU+MAXV; i++ ) predecessor[i] = -1;
    for( i = 0; i < MAXU; i++ ) flagUused[i] = flagUvisited[i] = 0;
    for( i = 0; i < MAXV; i++ ) flagVused[i] = flagVvisited[i] = 0;

    head = tail = 0;

    /* put all the unmatched u's on the queue. They start the
     * alternating path. */
    for( i = 0; i < u; i++ ) {
      if( ! isMatched(U(i))) {
        queue[tail++] = U(i);
        predecessor[i] = -1; /* redundant statement */
        setVisited(U(i));
      }
    }

    /* flag that at least one path was found by the bfs.
     * when the bfs does not find an alternating path we are done. */
    increased = 0;

    while( head != tail ) {
      i = queue[head++];

      /* this node appeared on some previously found alternating path. */
      if( isUsed(i) ) continue;

      if( isV(i) && !isMatched(i) ) {
        /* we got to the end of an alternating path. see if
         * it is disjoint with other paths found so far. only
         * then can we mess it up a bit. */
        bad = 0;
        for( j = i; j != -1; j = predecessor[j]) {
          if( isUsed(j)) {
            bad = 1;
            break;
          }
        }

        if( ! bad ) {
          /* this path is pristine. switch "polarity" of edges
           * in the matching on this path. */

          /* flag and instrumentation - whether (not) to quit,
           * and how many paths we found this bfs. */
          increased++;
          for( j = i; j != -1; last = j, j = predecessor[j] ) {
            if( isV(j) && !isMatched(j)) {
              /* the only unmatched v - actually this means we
               * are on the first iteration of this loop. */
              setMatched(j);

            } else if( isU(j) ) {
              if( isMatched(j) ) {
                /* the node we saw in the previous iteration of
                 * this loop must be a V. We will match with it
                 * instead of the one we used to match with, which
                 * must be the next node visited in this loop. */
                assert(isV(last));
                matching[j] = last - MAXU;
              } else {
                /* we are the very first u, one of the ones the
                 * bfs queue was "seeded" with. We should have ...*/
```

```c
                    assert(predecessor[j] == -1);
                    setMatched(j);
                    assert(isV(last));
                    matching[j] = last - MAXU;
                }
            }
            setUsed(j); /* this node cannot be used for other
                         * paths we might run across in the future
                         * on this bfs. */
        } /* for */
    } /* if ! bad */
} /* isV and !isMatched */

else if( isV(i) ) {
    /* this must be a matched V - find the matching U and put it on
     * the queue if it is not visited or used. */

    bad = 1;

    for( j = 0; j < u; j++ ) {
        if( isMatched(U(j)) && matching[j] == i - MAXU ) {
            /* this is the one. */
            if( ! isVisited(U(j)) && !isUsed(U(j))) {
                setVisited(U(j));
                queue[tail++] = U(j);
                predecessor[U(j)] = i;
            }
            bad = 0;
            break;
        }
    }
    assert(!bad);
} /* isV */
else if( isU(i) ) {
    /* we are at U. whether it is unmatched (a "seed"),
     * or matched, we do the same thing - put on the queue
     * all V's which it is connected to in the graph but
     * which it is _not_ paired to in the current matching. */

    for( j = 0; j < v; j++ ) {
        if( bipgraph[i][j] &&
            !isVisited(V(j)) &&
            !isUsed(V(j)) &&
            matching[i] != j ) {
            /* we can put this one on the queue. */
            queue[tail++] = V(j);
            predecessor[V(j)] = i;
            setVisited(V(j));
        }
    }
} else {
    assert(0); /* should be no other cases. */
}
/* this is the end of the bfs. */
}
} while( increased );

return;
}


int
main() {
    int i,j,u,v,setnum;

    in = stdin; out = stdout; setnum = 0;

    while( fscanf(in, "%d %d", &u, &v) == 2 ) {
```

```c
    for( i = 0; i < u; i++ ) for( j = 0; j < v; j++ ) bipgraph[i][j] = 0;

    while( fscanf(in, "%d %d", &i, &j) == 2 && i != -1 && j != -1 ) {
        bipgraph[i][j] = 1;
    }

    match(u,v);

    fprintf(out, "Problem #%d:\n", ++setnum);
    for( i = 0; i < u; i ++ ) {
        if( matching[i] != -1 )
            fprintf(out, "match %d to %d\n", i, matching[i]);
    }
}
return 0;
}
```

```
/*
 * Min Cost Max Flow for Dense graphs
 *
 * Authors: Frank Chu, Igor Naverniouk
 * http://shygypsy.com/tools/mcmf3.cpp
 *
 * Min cost max flow * (Edmonds-Karp relabelling + Dijkstra)
 *
 * This implementation takes a directed graph where each edge has a
 * capacity ('cap') and a cost per unit of flow ('cost') and returns a
 * maximum flow network of minimal cost ('fcost') from s to t.
 *
 * PARAMETERS:
 *      - cap (global): adjacency matrix where cap[u][v] is the capacity
 *          of the edge u->v. cap[u][v] is 0 for non-existent edges.
 *      - cost (global): a matrix where cost[u][v] is the cost per unit
 *          of flow along the edge u->v. If cap[u][v] == 0, cost[u][v] is
 *          ignored. ALL COSTS MUST BE NON-NEGATIVE!
 *      - n: the number of vertices ([0, n-1] are considered as vertices).
 *      - s: source vertex.
 *      - t: sink.
 * RETURNS:
 *      - the flow
 *      - the total cost through 'fcost'
 *      - fnet contains the flow network. Careful: both fnet[u][v] and
 *          fnet[v][u] could be positive. Take the difference.
 * COMPLEXITY:
 *      - Worst case: O(n^2*flow  <?  n^3*fcost)
 * REFERENCE:
 *      Edmonds, J., Karp, R.  "Theoretical Improvements in Algorithmic
 *          Efficieincy for Network Flow Problems".
 *      This is a slight improvement of Frank Chu's implementation.
 **/

#include <iostream>
#include <algorithm>
#include <climits>
using namespace std;

// the maximum number of vertices + 1
const int NN = 1024;

// adjacency matrix (fill this up)
int cap[NN][NN];

// cost per unit of flow matrix (fill this up)
int cost[NN][NN];

// flow network and adjacency list
int fnet[NN][NN], adj[NN][NN], deg[NN];

// Dijkstra's successor and depth
int par[NN], d[NN];         // par[source] = source;

// Labelling function
int pi[NN];

const int Inf = INT_MAX/2;

// Dijkstra's using non-negative edge weights (cost + potential)
#define Pot(u,v) (d[u] + pi[u] - pi[v])

bool dijkstra(int n, int s, int t)
{
  for (int i = 0; i < n; i++) {
    d[i] = Inf;
    par[i] = -1;
  }
```

```
  d[s] = 0;
  par[s] = -n - 1;

  while (1) {
    // find u with smallest d[u]
    int u = -1, bestD = Inf;
    for (int i = 0; i < n; i++) {
      if (par[i] < 0 && d[i] < bestD) {
        bestD = d[u = i];
      }
    }
    if (bestD == Inf) break;

    // relax edge (u,i) or (i,u) for all i;
    par[u] = -par[u] - 1;
    for (int i = 0; i < deg[u]; i++) {
      // try undoing edge v->u
      int v = adj[u][i];
      if (par[v] >= 0) continue;
      if (fnet[v][u] && d[v] > Pot(u,v) - cost[v][u]) {
        d[v] = Pot( u, v ) - cost[v][u];
        par[v] = -u-1;
      }

      // try edge u->v
      if (fnet[u][v] < cap[u][v] && d[v] > Pot(u,v) + cost[u][v]) {
        d[v] = Pot(u,v) + cost[u][v];
        par[v] = -u - 1;
      }
    }
  }

  for (int i = 0; i < n; i++) {
    if (pi[i] < Inf) {
      pi[i] += d[i];
    }
  }

  return par[t] >= 0;
}

#undef Pot

int mcmf( int n, int s, int t, int &fcost )
{
  // build the adjacency list
  fill(deg, deg+NN, 0);
  for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
      if (cap[i][j] || cap[j][i]) {
        adj[i][deg[i]++] = j;
      }
    }
  }

  for (int i = 0; i < NN; i++) {
    fill(fnet[i], fnet[i]+NN, 0);
  }
  fill(pi, pi+NN, 0);
  int flow = fcost = 0;

  // repeatedly, find a cheapest path from s to t
  while (dijkstra(n, s, t)) {
    // get the bottleneck capacity
    int bot = INT_MAX;
    for (int v = t, u = par[v]; v != s; u = par[v = u]) {
      bot = min(bot, fnet[v][u] ? fnet[v][u] : (cap[u][v] - fnet[u][v]));
    }
```

```
    // update the flow network
    for (int v = t, u = par[v]; v != s; u = par[v = u]) {
      if (fnet[v][u]) {
        fnet[v][u] -= bot;
        fcost -= bot * cost[v][u];
      } else {
        fnet[u][v] += bot;
        fcost += bot * cost[u][v];
      }
    }

    flow += bot;
  }

  return flow;
}

//---------------- EXAMPLE USAGE -----------------
#include <iostream>
using namespace std;

int main()
{
  int numV;
  cin >> numV;
  for (int i = 0; i < NN; i++) {
    fill(cap[i], cap[i]+NN, 0);
  }

  int m, a, b, c, cp;
  int s, t;
  cin >> m;
  cin >> s >> t;

  // fill up cap with existing capacities.
  // if the edge u->v has capacity 6, set cap[u][v] = 6.
  // for each cap[u][v] > 0, set cost[u][v] to  the
  // cost per unit of flow along the edge i->v
  for (int i=0; i<m; i++) {
    cin >> a >> b >> cp >> c;
    cost[a][b] = c; // cost[b][a] = c;
    cap[a][b] = cp; // cap[b][a] = cp;
  }

  int fcost;
  int flow = mcmf( numV, s, t, fcost );
  cout << "flow:" << flow << endl;
  cout << "cost:" << fcost << endl;

  return 0;
}
```

```
/**
 *    //////////////////////
 *    // MIN COST MAX FLOW //
 *    //////////////////////
 *
 *    Authors: Frank Chu, Igor Naverniouk
 **/


/*********************
 * Min cost max flow * (Edmonds-Karp relabelling + fast heap Dijkstra)
 *********************
 * Takes a directed graph where each edge has a capacity ('cap') and a
 * cost per unit of flow ('cost') and returns a maximum flow network
 * of minimal cost ('fcost') from s to t. USE mcmf3.cpp FOR DENSE GRAPHS!
 *
 * PARAMETERS:
 *      - cap (global): adjacency matrix where cap[u][v] is the capacity
 *          of the edge u->v. cap[u][v] is 0 for non-existent edges.
 *      - cost (global): a matrix where cost[u][v] is the cost per unit
 *          of flow along the edge u->v. If cap[u][v] == 0, cost[u][v] is
 *          ignored. ALL COSTS MUST BE NON-NEGATIVE!
 *      - n: the number of vertices ([0, n-1] are considered as vertices).
 *      - s: source vertex.
 *      - t: sink.
 * RETURNS:
 *      - the flow
 *      - the total cost through 'fcost'
 *      - fnet contains the flow network. Careful: both fnet[u][v] and
 *          fnet[v][u] could be positive. Take the difference.
 * COMPLEXITY:
 *      - Worst case: O(m*log(m)*flow  <?  n*m*log(m)*fcost)
 * FIELD TESTING:
 *      - Valladolid 10594: Data Flow
 * REFERENCE:
 *      Edmonds, J., Karp, R.  "Theoretical Improvements in Algorithmic
 *          Efficieincy for Network Flow Problems".
 *      This is a slight improvement of Frank Chu's implementation.
 **/

#include <iostream>
#include <algorithm>
#include <climits>
using namespace std;

// the maximum number of vertices + 1
#define NN 1024

// adjacency matrix (fill this up)
int cap[NN][NN];

// cost per unit of flow matrix (fill this up)
int cost[NN][NN];

// flow network and adjacency list
int fnet[NN][NN], adj[NN][NN], deg[NN];

// Dijkstra's predecessor, depth and priority queue
int par[NN], d[NN], q[NN], inq[NN], qs;

// Labelling function
int pi[NN];

#define Inf (INT_MAX/2)
#define BUBL { \
t = q[i]; q[i] = q[j]; q[j] = t; \
t = inq[q[i]]; inq[q[i]] = inq[q[j]]; inq[q[j]] = t; }

// Dijkstra's using non-negative edge weights (cost + potential)
#define Pot(u,v) (d[u] + pi[u] - pi[v])
```

```
bool dijkstra( int n, int s, int t )
{
  fill(d, d+NN, Inf);
  fill(par, par+NN, -1);
  fill(inq, inq+NN, -1);

  d[s] = qs = 0;
  inq[q[qs++] = s] = 0;
  par[s] = n;

  while (qs) {
    // get the minimum from q and bubble down
    int u = q[0];
    inq[u] = -1;
    q[0] = q[--qs];
    if( qs ) inq[q[0]] = 0;
    for (int i = 0, j = 2*i + 1, t; j < qs; i = j, j = 2*i + 1) {
      if (j + 1 < qs && d[q[j + 1]] < d[q[j]]) j++;
      if (d[q[j]] >= d[q[i]]) break;
      BUBL;
    }

    // relax edge (u,i) or (i,u) for all i;
    for (int k = 0, v = adj[u][k]; k < deg[u]; v = adj[u][++k]) {
      // try undoing edge v->u
      if (fnet[v][u] && d[v] > Pot(u,v) - cost[v][u])
        d[v] = Pot(u,v) - cost[v][par[v] = u];

      // try using edge u->v
      if (fnet[u][v] < cap[u][v] && d[v] > Pot(u,v) + cost[u][v])
        d[v] = Pot(u,v) + cost[par[v] = u][v];

      if (par[v] == u) {
        // bubble up or decrease key
        if( inq[v] < 0 ) { inq[q[qs] = v] = qs; qs++; }
        for( int i = inq[v], j = ( i - 1 )/2, t;
            d[q[i]] < d[q[j]]; i = j, j = ( i - 1 )/2 )
          BUBL;
      }
    }
  }

  for( int i = 0; i < n; i++ ) if( pi[i] < Inf ) pi[i] += d[i];

  return par[t] >= 0;
}

int mcmf( int n, int s, int t, int &fcost )
{
  // build the adjacency list
  fill(deg, deg+NN, 0);
  for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++)
      if (cap[i][j] || cap[j][i]) adj[i][deg[i]++] = j;
  }
  for (int i = 0; i < NN; i++) {
    fill(fnet[i], fnet[i]+NN, 0);
  }
  fill(pi, pi+NN, 0);

  int flow = fcost = 0;

  // repeatedly, find a cheapest path from s to t
  while (dijkstra(n, s, t)) {
    // get the bottleneck capacity
    int bot = INT_MAX;
    for (int v = t, u = par[v]; v != s; u = par[v = u]) {
      bot = min(bot, fnet[v][u] ? fnet[v][u] : ( cap[u][v] - fnet[u][v] ));
    }
```

```
    // update the flow network
    for (int v = t, u = par[v]; v != s; u = par[v = u])
      if (fnet[v][u]) { fnet[v][u] -= bot; fcost -= bot * cost[v][u]; }
      else { fnet[u][v] += bot; fcost += bot * cost[u][v]; }

    flow += bot;
  }

  return flow;
}

int main()
{
  int numV;
  int m, a, b, c, cp;
  int s, t;

  cin >> numV;
  cin >> m;
  cin >> s >> t;

  // fill up cap with existing capacities.
  // if the edge u->v has capacity 6, set cap[u][v] = 6.
  // for each cap[u][v] > 0, set cost[u][v] to  the
  // cost per unit of flow along the edge u->v
  for (int i=0; i<m; i++) {
    cin >> a >> b >> cp >> c;
    cost[a][b] = c; // cost[b][a] = c;
    cap[a][b] = cp; // cap[b][a] = cp;
  }

  int fcost;
  int flow = mcmf( numV, s, t, fcost );
  cout << "flow:" << flow << endl;
  cout << "cost:" << fcost << endl;

  return 0;
}
```

```
/*
 * Implementation of Kruskal's Minimum Spanning Tree Algorithm
 *
 * Author: Howard Cheng
 *
 * This is a routine to find the minimum spanning tree.  It takes as
 * input:
 *
 *      n: number of vertices
 *      m: number of edges
 *  elist: an array of edges (if (u,v) is in the list, there is no need
 *         for (v,u) to be in, but it wouldn't hurt, as long as the weights
 *         are the same).
 *
 * The following are returned:
 *
 *  index: an array of indices that shows which edges from elist are in
 *         the minimum spanning tree.  It is assumed that its size is at
 *         least n-1.
 *   size: the number of edges selected in "index".  If this is not
 *         n-1, the graph is not connected and we have a "minimum
 *         spanning forest."
 *
 * The weight of the MST is returned as the function return value.
 *
 * The run time of the algorithm is O(m log m).
 *
 * Note: the elements of elist may be reordered.
 *
 * Modified by Rex Forsyth using C++  Aug 28, 2003
 * This version defines the unionfind and edge as classes and  provides
 * constructors. The edge class overloads the < operator. So the sort does
 * not use a  * cmp function. It uses dynamic arrays.
 */

#include <cmath>
#include <iostream>
#include <iomanip>
#include <cstdlib>
#include <cassert>
#include <algorithm>
using namespace std;

class UnionFind
{
    struct UF { int p; int rank; };

  public:
    UnionFind(int n) {              // constructor
        howMany = n;
        uf = new UF[howMany];
        for (int i = 0; i < howMany; i++) {
            uf[i].p = i;
            uf[i].rank = 0;
        }
    }

    ~UnionFind() {
        delete[] uf;
    }

    int find(int x) { return find(uf,x); }       // for client use

    bool merge(int x, int y) {
        int res1, res2;
        res1 = find(uf, x);
        res2 = find(uf, y);
        if (res1 != res2) {
            if (uf[res1].rank > uf[res2].rank) {
```

```
                uf[res2].p = res1;
            }
            else {
                uf[res1].p = res2;
                if (uf[res1].rank == uf[res2].rank) {
                    uf[res2].rank++;
                }
            }
            return true;
        }
        return false;
    }

  private:
    int howMany;
    UF* uf;

    int find(UF uf[], int x) {                // for internal use
        if (uf[x].p != x) {
            uf[x].p = find(uf, uf[x].p);
        }
        return uf[x].p;
    }
};

class Edge {

  public:
    Edge(int i=-1, int j=-1, double weight=0) {
        v1 = i;
        v2 = j;
        w = weight;
    }
    bool operator<(const Edge& e) const { return w < e.w; }

    int v1, v2;          /* two endpoints of edge              */
    double w;            /* weight, can be double instead of int */
};


double mst(int n, int m, Edge elist[], int index[], int& size)
{
    UnionFind uf(n);

    sort(elist, elist+m);

    double w = 0.0;
    size = 0;
    for (int i = 0; i < m && size < n-1; i++) {
        int c1 = uf.find(elist[i].v1);
        int c2 = uf.find(elist[i].v2);
        if (c1 != c2) {
            index[size++] = i;
            w += elist[i].w;
            uf.merge(c1, c2);
        }
    }

    return w;
}

int main(void)
{
    cout << fixed << setprecision(2);

    int n;
    cin >> n;
    double* x = new double[n];
    double* y = new double[n];
```

```
    int* index = new int[n];

    for (int i = 0; i < n; i++)  cin >> x[i] >> y[i];

    Edge* elist = new Edge[n*n];
    int k = 0;
    for (int i = 0; i < n; i++)
        for (int j = i+1; j < n; j++)
            elist[k++] = Edge(i,j,hypot(x[i]-x[j], y[i]-y[j]) );

    int t;  // number of edges in the mst
    cout << mst(n, k, elist, index, t) << endl;
    return 0;
}
```

```cpp
/*
 * Multiplication/division without overflow
 *
 * Author: Howard Cheng
 *
 * Given a list of factors in the numerator (num, size n) and a list
 * of factors in the denominator (dem, size m), it returns the product
 * of the numerator divided by the denominator, while reducing the
 * result as soon as it is larger than some BOUND.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

const int BOUND = (1 << 16);

double mult(double num[], int n, double dem[], int m)
{
   int i, j;
   double prod = 1.0;
   i = j = 0;
   while (i < n || j < m) {
      if (prod >= BOUND && j < m) {
         prod /= dem[j++];
      } else if (i < n) {
         prod *= num[i++];
      } else {
         assert(j < m);
         prod /= dem[j++];
      }
   }
   return prod;
}

int main(void)
{
  double A[1000], B[1000];
  int n, m, i;

  while (cin >> n >> m && n > 0 && m > 0) {
    for (i = 0; i < n; i++) {
      cin >> A[i];
    }
    for (i = 0; i < m; i++) {
      cin >> B[i];
    }
    cout << "prod = " << mult(A, n, B, m) << endl;
  }

  return 0;
}
```

```
/*
 * Network Flow (Relabel-to-front)
 *
 * Author: Howard Cheng
 *
 * The routine network_flow() finds the maximum flow that can be
 * pushed from the source (s) to the sink (t) in a flow network
 * (i.e. directed graph with capacities on the edges).  The maximum
 * flow is returned.  The flow is given in the flow array (look for
 * positive flow).
 *
 * The complexity of this algorithm is O(n^3), which is good if the
 * graph is small but the maximum flow can be large.  Since the
 * algorithm is O(n^3) we are going to use the adjacency matrix
 * representation.
 *
 */

#include <iostream>
#include <list>
#include <cassert>

using namespace std;

const int MAX_NODE = 102;

void clear_graph(int graph[MAX_NODE][MAX_NODE], int n)
{
  for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
      graph[i][j] = 0;
    }
  }
}

void push(int graph[MAX_NODE][MAX_NODE], int flow[MAX_NODE][MAX_NODE],
          int e[], int u, int v)
{
  int cf = graph[u][v] - flow[u][v];
  int d = (e[u] < cf) ? e[u] : cf;
  flow[u][v] += d;
  flow[v][u] = -flow[u][v];
  e[u] -= d;
  e[v] += d;
}

void relabel(int graph[MAX_NODE][MAX_NODE], int flow[MAX_NODE][MAX_NODE],
             int n, int h[], int u)
{
  h[u] = -1;
  for (int v = 0; v < n; v++) {
    if (graph[u][v] - flow[u][v] > 0 &&
        (h[u] == -1 || 1 + h[v] < h[u])) {
      h[u] = 1 + h[v];
    }
  }
  assert(h[u] >= 0);
}

void discharge(int graph[MAX_NODE][MAX_NODE], int flow[MAX_NODE][MAX_NODE],
               int n, int e[], int h[], list<int>& NU,
               list<int>::iterator &current, int u)
{
  while (e[u] > 0) {
    if (current == NU.end()) {
      relabel(graph, flow, n, h, u);
      current = NU.begin();
    } else {
      int v = *current;
```

```
      if (graph[u][v] - flow[u][v] > 0 && h[u] == h[v] + 1) {
        push(graph, flow, e, u, v);
      } else {
        ++current;
      }
    }
  }
}

int network_flow(int graph[MAX_NODE][MAX_NODE], int flow[MAX_NODE][MAX_NODE],
                 int n, int s, int t)
{
  int e[MAX_NODE], h[MAX_NODE];
  int u, v, oh;
  list<int> N[MAX_NODE], L;
  list<int>::iterator current[MAX_NODE], p;

  for (u = 0; u < n; u++) {
    h[u] = e[u] = 0;
  }
  for (u = 0; u < n; u++) {
    for (v = 0; v < n; v++) {
      flow[u][v] = 0;
      if (graph[u][v] > 0 || graph[v][u] > 0) {
        N[u].push_front(v);
      }
    }
  }
  h[s] = n;
  for (u = 0; u < n; u++) {
    if (graph[s][u] > 0) {
      e[u] = flow[s][u] = graph[s][u];
      e[s] += flow[u][s] = -graph[s][u];
    }
    if (u != s && u != t) {
      L.push_front(u);
    }
    current[u] = N[u].begin();
  }

  p = L.begin();
  while (p != L.end()) {
    u = *p;
    oh = h[u];
    discharge(graph, flow, n, e, h, N[u], current[u], u);
    if (h[u] > oh) {
      L.erase(p);
      L.push_front(u);
      p = L.begin();
    }
    ++p;
  }

  int maxflow = 0;
  for (u = 0; u < n; u++) {
    if (flow[s][u] > 0) {
      maxflow += flow[s][u];
    }
  }
  return maxflow;
}

void print_flow(int flow[MAX_NODE][MAX_NODE], int n)
{
  for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
      if (flow[i][j] > 0) {
        cout << i << "->" << j << ":" << flow[i][j] << endl;
      }
```

```
      }
    }
}

int main(void)
{
  int graph[MAX_NODE][MAX_NODE];
  int s, t;
  int n, m, u, v, c;
  int flow[MAX_NODE][MAX_NODE];
  int maxflow;

  while (cin >> n && n > 0) {
    clear_graph(graph, n);
    cin >> m >> s >> t;
    while (m-- > 0) {
      cin >> u >> v >> c;
      graph[u][v] = c;
    }
    maxflow = network_flow(graph, flow, n, s, t);
    cout << "flow = " << maxflow << endl;
    print_flow(flow, n);
  }

  return 0;
}
```

```cpp
/*
 * Network Flow
 *
 * Author: Howard Cheng
 *
 * The routine network_flow() finds the maximum flow that can be
 * pushed from the source (s) to the sink (t) in a flow network
 * (i.e. directed graph with capacities on the edges).  The maximum
 * flow is returned.  Note that the graph is modified.  If you wish to
 * recover the flow on an edge, it is in the "flow" field, as long as
 * is_real is set to true.
 *
 * Note: if you have an undirected network. simply call add_edge twice
 * with an edge in both directions (same capacity).  Note that 4 edges
 * will be added (2 real edges and 2 residual edges).  To discover the
 * actual flow between two vertices u and v, add up the flow of all
 * real edges from u to v and subtract all the flow of real edges from
 * v to u.  (In fact, for a residual edge the flow is always 0 in this
 * implementation.)
 *
 * This code can also be used for bipartite matching by setting up an
 * appropriate flow network.
 *
 * The code here assumes an adjacency list representation since most
 * problems requiring network flow have sparse graphs.
 *
 * This is the basic augmenting path algorithm and it is not the most
 * efficient.  But it should be good enough for most programming contest
 * problems.  The complexity is O(f m) where f is the size of the flow
 * and m is the number of edges.  This is good if you know that f
 * is small, but can be exponential if f is large.
 *
 */

#include <iostream>
#include <algorithm>
#include <vector>
#include <list>
#include <cassert>

using namespace std;

struct Edge;
typedef list<Edge>::iterator EdgeIter;

struct Edge {
  int to;
  int cap;
  int flow;
  bool is_real;
  EdgeIter partner;

  Edge(int t, int c, bool real = true)
    : to(t), cap(c), flow(0), is_real(real)
  {};

  int residual() const
  {
    return cap - flow;
  }
};

struct Graph {
  list<Edge> *nbr;
  int num_nodes;
  Graph(int n)
    : num_nodes(n)
  {
    nbr = new list<Edge>[num_nodes];
```

```cpp
  }

  ~Graph()
  {
    delete[] nbr;
  }

  // note: this routine adds an edge to the graph with the specified capacity,
  // as well as a residual edge.  There is no check on duplicate edge, so it
  // is possible to add multiple edges (and residual edges) between two
  // vertices
  void add_edge(int u, int v, int cap)
  {
    nbr[u].push_front(Edge(v, cap));
    nbr[v].push_front(Edge(u, 0, false));
    nbr[v].begin()->partner = nbr[u].begin();
    nbr[u].begin()->partner = nbr[v].begin();
  }
};

void push_path(Graph &G, int s, int t, const vector<EdgeIter> &path, int flow)
{
  for (int i = 0; s != t; i++) {
    if (path[i]->is_real) {
      path[i]->flow += flow;
      path[i]->partner->cap += flow;
    } else {
      path[i]->cap -= flow;
      path[i]->partner->flow -= flow;
    }
    s = path[i]->to;
  }
}

// the path is stored in a peculiar way for efficiency: path[i] is the
// i-th edge taken in the path.
int augmenting_path(const Graph &G, int s, int t, vector<EdgeIter> &path,
                    vector<bool> &visited, int step = 0)
{
  if (s == t) {
    return -1;
  }
  for (EdgeIter it = G.nbr[s].begin(); it != G.nbr[s].end(); ++it) {
    int v = it->to;
    if (it->residual() > 0 && !visited[v]) {
      path[step] = it;
      visited[v] = true;
      int flow = augmenting_path(G, v, t, path, visited, step+1);
      if (flow == -1) {
        return it->residual();
      } else if (flow > 0) {
        return min(flow, it->residual());
      }
    }
  }
  return 0;
}

// note that the graph is modified
int network_flow(Graph &G, int s, int t)
{
  vector<bool> visited(G.num_nodes);
  vector<EdgeIter> path(G.num_nodes);
  int flow = 0, f;

  do {
    fill(visited.begin(), visited.end(), false);
    if ((f = augmenting_path(G, s, t, path, visited)) > 0) {
      push_path(G, s, t, path, f);
```

```
      flow += f;
    }
  } while (f > 0);

  return flow;
}

int main(void)
{
  Graph G(100);
  int s, t, u, v, cap, flow;

  cin >> s >> t;
  while (cin >> u >> v >> cap) {
    G.add_edge(u, v, cap);
  }

  flow = network_flow(G, s, t);
  cout << "maximum flow = " << flow << endl;

  return 0;
}
```

```cpp
/*
 * Point-in-polygon test
 *
 * Author: Howard Cheng
 * Reference:
 *    http://www.exaflop.org/docs/cgafaq/cga2.html
 *
 * Given a polygon as a list of n vertices, and a point, it returns
 * whether the point is in the polygon or not.
 *
 * One has the option to define the behavior on the boundary.
 *
 */


#include <iostream>
#include <cmath>
#include <cassert>

using namespace std;

/* how close to call equal */
const double EPSILON = 1E-8;

/* what should be returned on the boundary? */
const bool BOUNDARY = true;

struct Point {
  double x, y;
};

/* counterclockwise, clockwise, or undefined */
enum Orientation {CCW, CW, CNEITHER};

Orientation ccw(Point a, Point b, Point c)
{
  double dx1 = b.x - a.x;
  double dx2 = c.x - b.x;
  double dy1 = b.y - a.y;
  double dy2 = c.y - b.y;
  double t1 = dy2 * dx1;
  double t2 = dy1 * dx2;

  if (fabs(t1 - t2) < EPSILON) {
    if (dx1 * dx2 < 0 || dy1 * dy2 < 0) {
      if (dx1*dx1 + dy1*dy1 >= dx2*dx2 + dy2*dy2 - EPSILON) {
        return CNEITHER;
      } else {
        return CW;
      }
    } else {
      return CCW;
    }
  } else if (t1 > t2) {
    return CCW;
  } else {
    return CW;
  }
}

bool point_in_poly(Point poly[], int n, Point p)
{
  int i, j, c = 0;

  /* first check to see if point is one of the vertices */
  for (i = 0; i < n; i++) {
    if (fabs(p.x - poly[i].x) < EPSILON && fabs(p.y - poly[i].y) < EPSILON) {
      return BOUNDARY;
    }
  }
```

```cpp
  /* now check if it's on the boundary */
  for (i = 0; i < n-1; i++) {
    if (ccw(poly[i], poly[i+1], p) == CNEITHER) {
      return BOUNDARY;
    }
  }
  if (ccw(poly[n-1], poly[0], p) == CNEITHER) {
    return BOUNDARY;
  }

  /* finally check if it's inside */
  for (i = 0, j = n-1; i < n; j = i++) {
    if (((poly[i].y <= p.y && p.y < poly[j].y ||
         (poly[j].y <= p.y && p.y < poly[i].y)) &&
        (p.x < (poly[j].x - poly[i].x) * (p.y - poly[i].y)
         / (poly[j].y - poly[i].y) + poly[i].x))
      c = !c;
  }
  return c;
}

int main(void)
{
  Point *polygon, p;
  int n;
  int i;

  while (cin >> n && n > 0) {
    polygon = new Point[n];
    assert(polygon);
    for (i = 0; i < n; i++) {
      cin >> polygon[i].x >> polygon[i].y;
    }
    while (cin >> p.x >> p.y) {
      if (point_in_poly(polygon, n, p)) {
        cout << "yes";
      } else {
        cout << "no";
      }
      cout << endl;
    }
    delete[] polygon;
  }
  return 0;
}
```

```cpp
/*
 * Convex Polygon Intersection
 *
 * Author: Howard Cheng
 *
 * This routine takes two convex polygon, and returns the intersection
 * which is also convex.  If the intersection contains less than
 * 3 points, it is considered empty.
 *
 */

#include <iostream>
#include <iomanip>
#include <cmath>
#include <algorithm>
#include <cassert>

using namespace std;

/* how close to call equal */
const double EPSILON = 1E-8;

struct Point {
  double x, y;
};

const bool BOUNDARY = true;

/* counterclockwise, clockwise, or undefined */
enum Orientation {CCW, CW, CNEITHER};

/* Global point for computing convex hull */
Point start_p;

Orientation ccw(Point a, Point b, Point c)
{
  double dx1 = b.x - a.x;
  double dx2 = c.x - b.x;
  double dy1 = b.y - a.y;
  double dy2 = c.y - b.y;
  double t1 = dy2 * dx1;
  double t2 = dy1 * dx2;

  if (fabs(t1 - t2) < EPSILON) {
    if (dx1 * dx2 < 0 || dy1 * dy2 < 0) {
      if (dx1*dx1 + dy1*dy1 >= dx2*dx2 + dy2*dy2 - EPSILON) {
        return CNEITHER;
      } else {
        return CW;
      }
    } else {
      return CCW;
    }
  } else if (t1 > t2) {
    return CCW;
  } else {
    return CW;
  }
}

bool ccw_cmp(const Point &a, const Point &b)
{
  return ccw(start_p, a, b) == CCW;
}

int convex_hull(Point polygon[], int n, Point hull[]) {
  int count, best_i, i;

  if (n == 1) {
```

```cpp
    hull[0] = polygon[0];
    return 1;
  }

  /* find the first point: min y, and then min x */
  start_p = polygon[0];
  best_i = 0;
  for (i = 1; i < n; i++) {
    if ((polygon[i].y < start_p.y) ||
        (polygon[i].y == start_p.y && polygon[i].x < start_p.x)) {
      start_p = polygon[i];
      best_i = i;
    }
  }
  polygon[best_i] = polygon[0];
  polygon[0] = start_p;

  /* get simple closed polygon */
  sort(polygon+1, polygon+n, ccw_cmp);

  /* do convex hull */
  count = 0;
  hull[count] = polygon[count]; count++;
  hull[count] = polygon[count]; count++;
  for (i = 2; i < n; i++) {
    while (count > 1 &&
           ccw(hull[count-2], hull[count-1], polygon[i]) == CW) {
      /* pop point */
      count--;
    }
    hull[count++] = polygon[i];
  }
  return count;
}

bool point_in_poly(Point poly[], int n, Point p)
{
  int i, j, c = 0;

  /* first check to see if point is one of the vertices */
  for (i = 0; i < n; i++) {
    if (fabs(p.x - poly[i].x) < EPSILON && fabs(p.y - poly[i].y) < EPSILON) {
      return BOUNDARY;
    }
  }

  /* now check if it's on the boundary */
  for (i = 0; i < n-1; i++) {
    if (ccw(poly[i], poly[i+1], p) == CNEITHER) {
      return BOUNDARY;
    }
  }
  if (ccw(poly[n-1], poly[0], p) == CNEITHER) {
    return BOUNDARY;
  }

  /* finally check if it's inside */
  for (i = 0, j = n-1; i < n; j = i++) {
    if ((((poly[i].y <= p.y && p.y < poly[j].y) ||
         (poly[j].y <= p.y && p.y < poly[i].y)) &&
        (p.x < (poly[j].x - poly[i].x) * (p.y - poly[i].y)
         / (poly[j].y - poly[i].y) + poly[i].x))
      c = !c;
  }
  return c;
}

/* returns 1 if intersect at a point, 0 if not, -1 if the lines coincide */
int intersect_line(Point a, Point b, Point c, Point d, Point &p)
```

```
{
  double r, s;
  double denom, num1, num2;

  num1 = (a.y - c.y)*(d.x - c.x) - (a.x - c.x)*(d.y - c.y);
  num2 = (a.y - c.y)*(b.x - a.x) - (a.x - c.x)*(b.y - a.y);
  denom = (b.x - a.x)*(d.y - c.y) - (b.y - a.y)*(d.x - c.x);

  if (fabs(denom) >= EPSILON) {
    r = num1 / denom;
    s = num2 / denom;
    if (-EPSILON <= r && r <= 1+EPSILON && -EPSILON <= s && s <= 1+EPSILON) {
      p.x = a.x + r*(b.x - a.x);
      p.y = a.y + r*(b.y - a.y);
      return 1;
    } else {
      return 0;
    }
  } else {
    if (fabs(num1) >= EPSILON) {
      return 0;
    } else {
      return -1;
    }
  }
}

int intersect_polygon(Point poly1[], int n1, Point poly2[], int n2,
                      Point *&out)
{
  Point *newpoly, p;
  char *used;
  int new_n = n1 + n2 + n1*n2;
  int count, i, i2, j, j2, new_count;
  int n;

  newpoly = new Point[new_n];
  out = new Point[new_n];
  used = new char[new_n];
  assert(newpoly && out && used);
  count = 0;
  fill(used, used+new_n, 0);

  for (i = 0; i < n1; i++) {
    if (point_in_poly(poly2, n2, poly1[i])) {
      newpoly[count++] = poly1[i];
    }
  }
  for (i = 0; i < n2; i++) {
    if (point_in_poly(poly1, n1, poly2[i])) {
      newpoly[count++] = poly2[i];
    }
  }

  for (i = 0; i < n1; i++) {
    i2 = (i+1 == n1) ? 0 : i+1;
    for (j = 0; j < n2; j++) {
      j2 = (j+1 == n2) ? 0 : j+1;
      if (intersect_line(poly1[i], poly1[i2], poly2[j], poly2[j2], p) == 1) {
        newpoly[count++] = p;
      }
    }
  }

  if (count >= 3) {
    n = convex_hull(newpoly, count, out);
    if (n < 3) {
      delete[] out;
      n = 0;
```

```
    }
  } else {
    delete[] out;
    n = 0;
  }

  /* eliminate duplicates */
  for (i = 0; i < n-1; i++) {
    for (j = i+1; j < n; j++) {
      if (out[i].x == out[j].x && out[i].y == out[j].y) {
        used[j] = 1;
      }
    }
  }
  j = 0;
  new_count = 0;
  for (i = 0; i < n; i++) {
    if (!used[i]) {
      out[new_count++] = out[i];
    }
  }
  n = new_count;

  delete[] newpoly;
  delete[] used;
  return n;
}

int read_poly(Point *&poly)
{
  int n, i;

  cin >> n;
  if (n == 0) {
    return 0;
  }
  poly = new Point[n];
  assert(poly);
  for (i = 0; i < n; i++) {
    cin >> poly[i].x >> poly[i].y;
  }
  return n;

}

int main(void)
{
  Point *poly1, *poly2, *intersection;
  int n1, n2, n3, i;

  while ((n1 = read_poly(poly1))) {
    n2 = read_poly(poly2);
    n3 = intersect_polygon(poly1, n1, poly2, n2, intersection);
    delete[] poly1;
    delete[] poly2;
    if (n3 >= 3) {
      for (i = 0; i < n3; i++) {
        cout << fixed << setprecision(2);
        cout << "(" << intersection[i].x << "," << intersection[i].y
             << ")";
      }
      cout << endl;
      delete[] intersection;
    } else {
      cout << "Empty Intersection" << endl;
    }
  }

  return 0;
```

```
}
```

```cpp
// Performs guassian elimination over the rationals.
//
// Author: Darcy Best
// Date  : September 22, 2010
//
// pair<int,int> means first = numerator, second = denominator

#include <iostream>
#include <iomanip>
#include <cstdlib>
using namespace std;

#define pii pair<int,int>
const int MAX_N = 100;

pii *r_m,m_m;

void print(pii x){
  if(x.second == 1)
    cout << x.first;
  else
    cout << x.first <<  "/" << x.second;
}

void print(pii A[MAX_N][MAX_N],int m,int n){
  for(int i=0;i<m;i++){
    for(int j=0;j<n;j++){
      cout << setw(5);
      print(A[i][j]);
    }
    cout << endl;
  }
  cout << endl;
}

void read(pii& x){
  cin >> x.first;
  char ch;
  if(cin.peek() == '/')
    cin >> ch >> x.second;
  else
    x.second = 1;
}

int gcd(int a,int b){
  while (b) {
    int r = a % b;
    a = b;
    b = r;
  }
  return a;
}

pii reduce(pii a){
  if(a.first == 0){
    a.second = 1;
  } else {
    if(a.second < 0){
      a.first *= -1;
      a.second *= -1;
    }
    int g = gcd(abs(a.first),a.second);
    a.first /= g;
    a.second /= g;
  }
  return a;
}

pii operator*(pii a,pii b){
```

```cpp
  return reduce(pii(a.first*b.first,a.second*b.second));
}

pii operator+(pii a,pii b){
  return reduce(pii(a.first*b.second+b.first*a.second,a.second*b.second));
}

void multRow(pii& x){
  x = x * m_m;
}

void addMultRow(pii& x){
  x = x + (m_m * (*r_m++));
}

int rowReduction(pii A[MAX_N][MAX_N],int rows,int cols){
  int rank = 0;
  for(int c=0;c<cols;c++){
    for(int r=rank;r<rows;r++){
      if(A[r][c].first){
        if(r != rank) // Swap rows
          swap_ranges(A[rank],A[rank]+cols,A[r]);
        if(c == cols-1) // Inconsistent
          return -1;

        // Make first entry 1
        m_m = pii(A[rank][c].second,A[rank][c].first);
        for_each(A[rank]+c+1,A[rank]+cols,multRow);
        A[rank][c] = pii(1,0);

        for(int i=(arb?rank+1:0);i<rows;i++)
          if(A[i][c].first && i != rank){
            // Make the other rows 0
            m_m = pii(-A[i][c].first,A[i][c].second);
            r_m = A[rank]+c+1;
            for_each(A[i]+c+1,A[i]+cols,addMultRow);
            A[i][c] = pii(0,1);
          }
        rank++;
        break;
      }
    }
  }
  return rank;
}

int main(){
  int C=0;
  int T,m,n,rank;
  pii A[MAX_N][MAX_N];
  while(cin >> T && T){
    if(C++)
      cout << endl;
    cout << "Solution for Matrix System # " << T << endl;
    cin >> n >> m;
    for(int i=0;i<m;i++)
      for(int j=0;j<=n;j++)
        read(A[i][j]);

    if((rank = rowReduction(A,m,n+1)) < 0){
      cout << "No Solution." << endl;
    } else {
      if(rank != n){
        cout << "Infinitely many solutions containing " << n-rank << " arbitrary constants." << endl
;
      } else {
        for(int i=0;i<n;i++){
          cout << "x[" << i+1 << "]=";print(A[i][n]); cout << endl;
        }
```

```
        }
      }
    }
  return 0;
}
```

Oct 04, 21 12:27	**roman_numerals.cc**	Page 1/1

```cpp
// Converts Roman Numerals to Arabic Numbers (and vice versa)
//
// Author: Darcy Best
// Date  : September 5, 2010
//
// If you are given a valid integer (0 < x < 4000), then it will give
//    the standard roman numeral representation of it. Note that if you give
//    it a number such that x >= 4000, then it will just append as many "M"s
//    as needed.
//
// If you are given a valid roman numberal, then it will give you the answer
//    as a base 10 number.

#include <iostream>
#include <string>
#include <map>
using namespace std;

const string Roman[13]  = {"M","CM","D","CD","C","XC","L","XL","X","IX","V","IV","I"};
const int Arabic[13] = {1000,900,500,400,100,90,50,40,10,9,5,4,1};

string toRoman(int x){
  string roman;
  for(int i=0;i<13;i++)
    while(x >= Arabic[i]){
      x -= Arabic[i];
      roman += Roman[i];
    }
  return roman;
}

int toInt(string s){
  int L1,L2,ind=0,ans=0;
  while(ind < 13){
    L1 = s.length();
    L2 = Roman[ind].length();
    if(s.substr(0,min(L1,L2)) == Roman[ind]){
      ans += Arabic[ind];
      s.erase(0,min(L1,L2));
    } else {
      ind++;
    }
  }
  return ans;
}

int main(){
  char c;
  int x;
  string s;

  // Checks to see if the line is Roman Numerals or Arabic Numbers,
  //   then converts to the opposite.
  while(cin >> c){
    cin.putback(c);
    if(c >= '0' && c <= '9'){
      cin >> x;
      cout << toRoman(x) << endl;
    } else {
      cin >> s;
      cout << toInt(s) << endl;
    }
  }
  return 0;
}
```

```cpp
// Compresses a directed graph into its strongly connected components
//
// Author: Darcy Best
// Date  : October 1, 2010
//
// A set of nodes is "strongly connected" if for any pair of nodes in
// the set, there is a path from u to v AND from v to u.
//
// Compressing a graph into its strongly connected components means
// converting each strongly connected component into a super-node.
//
// We then build a "compressed" graph made with the super-nodes.  We
// add an edge in the compressed graph between U and V if there is a
// vertex u in U and v in V such that there was an edge from u to v in
// the original graph. The compressed graph will be a Directed Acyclic
// Graph (DAG), and the list of components will be in REVERSE
// topological order.
//
// If you are only concerned with the number of strongly connected
// components, you do not need to build the graph. See comments below
// on how to remove the SCC graph.
//
// The complexity of this algorithm is O(|V| + |E|).
//

#include <iostream>
#include <algorithm>
#include <stack>
#include <cassert>
#include <vector>
#include <set>
using namespace std;

const int MAX_NODES = 100005;

struct Graph{
  int numNodes;
  set<int> adj[MAX_NODES];
  void clear(){
    numNodes = 0;
    for(int i=0;i<MAX_NODES;i++)
      adj[i].clear();
  }
  void add_edge(int u,int v){
    adj[u].insert(v);
  }
};

int po[MAX_NODES],comp[MAX_NODES];

void DFS(int v,const Graph& G,Graph& G_scc,int& C,
         stack<int>& P,stack<int>& S){
  po[v] = C++;

  S.push(v);  P.push(v);
  for(auto w : G.adj[v]) {
    if(po[w] == -1){
      DFS(w,G,G_scc,C,P,S);
    } else if(comp[w] == -1){
      while(!P.empty() && (po[P.top()] > po[w]))
        P.pop();
    }
  }
  if(!P.empty() && P.top() == v){
    while(!S.empty()){
      int t = S.top();
      S.pop();
      comp[t] = G_scc.numNodes;
      if(t == v)
```

```cpp
        break;
    }
    G_scc.numNodes++;
    P.pop();
  }
}

int SCC(const Graph& G,Graph& G_scc){
  G_scc.clear();
  int C=1;
  stack<int> P,S;
  fill(po,po+G.numNodes,-1);
  fill(comp,comp+G.numNodes,-1);
  for(int i=0;i<G.numNodes;i++)
    if(po[i] == -1)
      DFS(i,G,G_scc,C,P,S);

  // You do not need this if you are only interested in the number of
  //    strongly connected components.
  for(int i=0;i<G.numNodes;i++){
    for(auto w : G.adj[i]) {
      if(comp[i] != comp[w])
        G_scc.add_edge(comp[i],comp[w]);
    }
  }

  return G_scc.numNodes;
}

// Declare these as a global variable if MAX_NODES is large to
//    avoid Runtime Error.
Graph G,G_scc;

int main(){
  int u,v,m,n;
  int n_scc;
  while(cin >> n >> m && (n || m)){
    G.clear();
    G.numNodes = n;
    for(int i=0;i<m;i++){
      cin >> u >> v;
      G.add_edge(u,v);
    }
    n_scc = SCC(G,G_scc);

    cout << "# of Strongly Connected Components: " << n_scc << endl;
  }
  return 0;
}
```

```cpp
#include <algorithm>

using namespace std;

const int MAX_CONSTRAINTS = 100;
const int MAX_VARS = 100;
const int MAXM = MAX_CONSTRAINTS + 1;
const int MAXN = MAX_VARS + 1;

const double EPS = 1e-9;
const double INF = 1.0/0.0;

double A[MAXM][MAXN];
int basis[MAXM], out[MAXN];

void pivot(int m, int n, int a, int b)
{
  int i, j;
  for (i = 0; i <= m; i++)
    if (i != a)
      for (j = 0; j <= n; j++)
        if (j != b)
          A[i][j] -= A[a][j] * A[i][b] / A[a][b];
  for (j = 0; j <= n; j++)
    if (j != b) A[a][j] /= A[a][b];
  for (i = 0; i <= m; i++)
    if (i != a) A[i][b] = -A[i][b] / A[a][b];
  A[a][b] = 1 / A[a][b];
  swap(basis[a], out[b]);
}

double simplex(int m, int n, double C[][MAXN], double X[])
{
  int i, j, ii, jj;
  for (i = 1; i <= m; i++)
    copy(C[i], C[i]+n+1, A[i]);
  for (j = 0; j <= n; j++)
    A[0][j] = -C[0][j];
  for (i = 0; i <= m; i++)
    basis[i] = -i;
  for (j = 0; j <= n; j++)
    out[j] = j;
  for (;;) {
    for (i = ii = 1; i <= m; i++)
      if (A[i][n] < A[ii][n] || (A[i][n] == A[ii][n] && basis[i] < basis[ii]))
        ii = i;
    if (A[ii][n] >= -EPS) break;
    for (j = jj = 0; j < n; j++)
      if (A[ii][j] < A[ii][jj] - EPS ||
          (A[ii][j] < A[ii][jj] - EPS && out[i] < out[j]))
        jj = j;
    if (A[ii][jj] >= -EPS) return -INF;
    pivot(m, n, ii, jj);
  }
  for (;;) {
    for (j = jj = 0; j < n; j++)
      if (A[0][j] < A[0][jj] || (A[0][j] == A[0][jj] && out[j] < out[jj]))
        jj = j;
    if (A[0][jj] > -EPS) break;
    for (i=1, ii=0; i <= m; i++)
      if ((A[i][jj]>EPS) &&
          (!ii || (A[i][n]/A[i][jj] < A[ii][n]/A[ii][jj]-EPS) ||
           ((A[i][n]/A[i][jj] < A[ii][n]/A[ii][jj]+EPS) &&
            (basis[i] < basis[ii]))))
        ii = i;
    if (A[ii][jj] <= EPS) return INF;
    pivot(m, n, ii, jj);
  }
  fill(X, X+n, 0);
```

```cpp
  for (i = 1; i <= m; i++)
    if (basis[i] >= 0)
      X[basis[i]] = A[i][n];
  return A[0][n];
}


#include <iostream>
#include <iomanip>


int main(void)
{
  double C[MAXM][MAXN], X[MAX_VARS];

  C[0][0] = -1;   C[0][1] = -3;  C[0][2] = 0;  C[0][3] = 0;
  C[1][0] = -2;   C[1][1] = -3;  C[1][2] = -6; C[1][3] = 250;
  C[2][0] = -1;   C[2][1] = -5;   C[2][2] = -5;  C[2][3] = 400;
  C[3][0] = -59;   C[3][1] = -35;   C[3][2] = -160;  C[3][3] = 30;

  double val = simplex(2, 2, C, X);

  cout << fixed << setprecision(3);
  cout << "val = " << val << endl;
  cout << "X[0] = " << X[0] << endl;
  cout << "X[1] = " << X[1] << endl;
  //  cout << "X[2] = " << X[2] << endl;
  return 0;
}
```

```cpp
/*
 * Finding the lexicographically least rotation of a string, and finding
 * the smallest period of a string.
 *
 * Author: Sumudu Fernando
 *
 * Given a string, the algorithm can be used to compute two things:
 *
 *   a) the position at which the lexicographically least rotation starts.
 *      If there are ties, give the first position.
 *   b) the length of the shortest substring such that the original string
 *      is a concatenation of copies of that substring
 *
 * Complexity: O(n) where n = length of the string
 *
 * Tested on: 719         Glass Beads
 *            10298        Power Strings
 *            ACPC 2011 H  Let's call a SPaDE a SPaDE
 */

#include <iostream>
#include <string>
#include <algorithm>

using namespace std;

// pos = position of the start of the lexicographically least rotation
// period = the period
void compute(string s, int &pos, int &period)
{
  s += s;
  int len = s.length();
  int i = 0, j = 1;
  for (int k = 0; i+k < len && j+k < len; k++) {
    if (s[i+k] > s[j+k]) {
      i = max(i+k+1, j+1);
      k = -1;
    } else if (s[i+k] < s[j+k]) {
      j = max(j+k+1, i+1);
      k = -1;
    }
  }

  pos = min(i, j);
  period = (i > j) ? i - j : j - i;
}

int main(void)
{
  string s;
  while (cin >> s) {
    int pos, period;
    compute(s, pos, period);
    int n = s.length();
    s += s;
    cout << "least rotation = " << s.substr(pos, n) << endl;
    cout << "period = " << s.substr(0, period) << endl;
  }
  return 0;
}
```

```
/*
 * Suffix array
 *
 * Author: Howard Cheng
 * References:
 *   Manber, U. and Myers, G.   "Suffix Arrays: a New Method for On-line
 *   String Searches."  SIAM Journal on Computing.  22(5) p. 935-948, 1993.
 *
 *   T. Kasai, G. Lee, H. Arimura, S. Arikawa, and K. Park.  "Linear-time
 *   Longest-common-prefix Computation in Suffix Arrays and Its
 *   Applications."  Proc. 12th Annual Conference on Combinatorial
 *   Pattern Matching, LNCS 2089, p. 181-192, 2001
 *
 *   J. Kärkkäinen and P. Sanders. Simple linear work suffix array
 *   construction.  In Proc. 13th International Conference on Automata,
 *   Languages and Programming, Springer, 2003
 *
 * The build_sarray routine takes in a string str of n characters (null-
 * terminated), and construct an array sarray.  Optionally, you can also
 * construct an lcp array from the sarray computed.  The properties
 * are:
 *
 * - If p = sarray[i], then the suffix of str starting at p (i.e.
 *   str[p..n-1] is the i-th suffix when all the suffixes are sorted in
 *   lexicographical order
 *
 *   NOTE: the empty suffix is not included in this list, so sarray[0] != n.
 *
 * - lcp[i] contains the length of the longest common prefix of the suffixes
 *   pointed to by sarray[i-1] and sarray[i].  lcp[0] is defined to be 0.
 *
 * - To see whether a pattern P occurs in str, you can look for it as
 *   the prefix of a suffix.  This can be done with a binary search in
 *   O(|P| log n) time.  Call find() to return a pair <L, R> such that
 *   all occurrences of the pattern are at positions sarray[i] with
 *   L <= i < R.  If L == R then there is no match.
 *
 * The construction of the suffix array takes O(n) time.
 *
 */

#include <iostream>
#include <iomanip>
#include <string>
#include <algorithm>
#include <climits>

using namespace std;

bool leq(int a1, int a2,   int b1, int b2)
{
  return(a1 < b1 || a1 == b1 && a2 <= b2);
}

bool leq(int a1, int a2, int a3,   int b1, int b2, int b3)
{
  return(a1 < b1 || a1 == b1 && leq(a2,a3, b2,b3));
}

void radixPass(int* a, int* b, int* r, int n, int K)
{
  int* c = new int[K + 1];
  fill(c, c+K+1, 0);
  for (int i = 0;  i < n;  i++) c[r[a[i]]]++;
  for (int i = 0, sum = 0;  i <= K;  i++) {
    int t = c[i];  c[i] = sum;  sum += t;
  }
  for (int i = 0;  i < n;  i++) b[c[r[a[i]]]++] = a[i];
  delete [] c;
```

```
}

#define GetI() (SA12[t] < n0 ? SA12[t] * 3 + 1 : (SA12[t] - n0) * 3 + 2)

void sarray_int(int* s, int* SA, int n, int K) {
  int n0=(n+2)/3, n1=(n+1)/3, n2=n/3, n02=n0+n2;
  int* s12  = new int[n02 + 3];  s12[n02]= s12[n02+1]= s12[n02+2]=0;
  int* SA12 = new int[n02 + 3]; SA12[n02]=SA12[n02+1]=SA12[n02+2]=0;
  int* s0   = new int[n0];
  int* SA0  = new int[n0];

  for (int i=0, j=0;  i < n+(n0-n1);  i++) if (i%3 != 0) s12[j++] = i;

  radixPass(s12 , SA12, s+2, n02, K);
  radixPass(SA12, s12 , s+1, n02, K);
  radixPass(s12 , SA12, s  , n02, K);

  int name = 0, c0 = -1, c1 = -1, c2 = -1;
  for (int i = 0;  i < n02;  i++) {
    if (s[SA12[i]] != c0 || s[SA12[i]+1] != c1 || s[SA12[i]+2] != c2) {
      name++;  c0 = s[SA12[i]];  c1 = s[SA12[i]+1];  c2 = s[SA12[i]+2];
    }
    if (SA12[i] % 3 == 1) { s12[SA12[i]/3]      = name; }
    else                  { s12[SA12[i]/3 + n0] = name; }
  }

  if (name < n02) {
    sarray_int(s12, SA12, n02, name);
    for (int i = 0;  i < n02;  i++) s12[SA12[i]] = i + 1;
  } else
    for (int i = 0;  i < n02;  i++) SA12[s12[i] - 1] = i;

  for (int i=0, j=0;  i < n02;  i++) if (SA12[i] < n0) s0[j++] = 3*SA12[i];
  radixPass(s0, SA0, s, n0, K);

  for (int p=0,  t=n0-n1,  k=0;  k < n;  k++) {
    int i = GetI();
    int j = SA0[p];
    if (SA12[t] < n0 ?
        leq(s[i],        s12[SA12[t] + n0], s[j],        s12[j/3]) :
        leq(s[i],s[i+1],s12[SA12[t]-n0+1], s[j],s[j+1],s12[j/3+n0]))
    {
      SA[k] = i;  t++;
      if (t == n02) {
        for (k++;  p < n0;  p++, k++) SA[k] = SA0[p];
      }
    } else {
      SA[k] = j;  p++;
      if (p == n0)  {
        for (k++;  t < n02;  t++, k++) SA[k] = GetI();
      }
    }
  }
  delete [] s12; delete [] SA12; delete [] SA0; delete [] s0;
}

void build_sarray(string str, int sarray[])
{
  int n = str.length();

  if (n <= 1) {
    for (int i = 0; i < n; i++) {
      sarray[i] = i;
    }
    return;
  }

  int *s = new int[n+3];
  int *SA = new int[n+3];
```

```cpp
  for (int i = 0; i < n; i++) {
    s[i] = (int)str[i] - CHAR_MIN + 1;
  }
  s[n] = s[n+1] = s[n+2] = 0;
  sarray_int(s, SA, n, 256);
  copy(SA, SA+n, sarray);

  delete[] s;
  delete[] SA;
}


void compute_lcp(string str, int sarray[], int lcp[])
{
  int n = str.length();
  int *rank = new int[n];
  for (int i = 0; i < n; i++) {
    rank[sarray[i]] = i;
  }
  int h = 0;
  for (int i = 0; i < n; i++) {
    int k = rank[i];
    if (k == 0) {
      lcp[k] = -1;
    } else {
      int j = sarray[k-1];
      while (i + h < n && j + h < n && str[i+h] == str[j+h]) {
        h++;
      }
      lcp[k] = h;
    }
    if (h > 0) {
      h--;
    }
  }
  lcp[0] = 0;
  delete[] rank;
}


pair<int,int> find(const string &str, const int sarray[],
                   const string &pattern)
{
  int n = str.length(), p = pattern.length();
  int L, R;

  if (pattern <= str.substr(sarray[0], p)) {
    L = 0;
  } else if (pattern > str.substr(sarray[n-1], p)) {
    L = n;
  } else {
    int lo = 0, hi = n-1;
    while (hi - lo > 1) {
      int mid = lo + (hi - lo)/2;
      if (pattern <= str.substr(sarray[mid], p)) {
        hi = mid;
      } else {
        lo = mid;
      }
    }
    L = hi;
  }

  if (pattern < str.substr(sarray[0], p)) {
    R = 0;
  } else if (pattern >= str.substr(sarray[n-1], p)) {
    R = n;
  } else {
    int lo = 0, hi = n-1;
    while (hi - lo > 1) {
      int mid = lo + (hi - lo)/2;
```

```cpp
      if (pattern < str.substr(sarray[mid], p)) {
        hi = mid;
      } else {
        lo = mid;
      }
    }
    R = hi;
  }

  if (L > R) R = L;
  return make_pair(L, R);
}


int main(void)
{
  string str;
  int sarray[100], lcp[100];
  unsigned int i;

  while (cin >> str) {
    build_sarray(str, sarray);
    compute_lcp(str, sarray, lcp);
    for (i = 0; i < str.length(); i++) {
      cout << setw(3) << i << ":" << setw(2) << lcp[i] << ","
           << str.substr(sarray[i], str.length()-sarray[i]) << endl;
    }
  }
  return 0;
}
```

```cpp
/*
 * Topological sort
 *
 * Author: Howard Cheng
 *
 * Given a directed acyclic graph, the topological_sort routine
 * returns a vector of integers that gives the vertex number (0 to n-1)
 * such that if there is a path from v1 to v2, then v1 occurs earlier
 * than v2 in the order.  Note that the topological sort result is not
 * necessarily unique.
 *
 * topological_sort returns true if there is no cycle.  Otherwise it
 * returns false and the sorting is unsuccessful.
 *
 * The complexity is O(n + m).
 *
 */


#include <iostream>
#include <algorithm>
#include <vector>
#include <queue>

using namespace std;

typedef int Edge;
typedef vector<Edge>::iterator EdgeIter;

struct Graph {
  vector<Edge> *nbr;
  int num_nodes;
  Graph(int n)
    : num_nodes(n)
  {
    nbr = new vector<Edge>[num_nodes];
  }

  ~Graph()
  {
    delete[] nbr;
  }

  // note: There is no check on duplicate edge, so it is possible to
  // add multiple edges between two vertices
  void add_edge(int u, int v)
  {
    nbr[u].push_back(Edge(v));
  }
};

bool topological_sort(const Graph &G, vector<int> &order)
{
  vector<int> indeg(G.num_nodes);
  fill(indeg.begin(), indeg.end(), 0);
  for (int i = 0; i < G.num_nodes; i++) {
    for (int j = 0; j < G.nbr[i].size(); j++) {
      indeg[G.nbr[i][j]]++;
    }
  }

  // use a priority queue if you want to get a topological sort order
  // with ties broken by lexicographical ordering
  queue<int> q;
  for (int i = 0; i < G.num_nodes; i++) {
    if (indeg[i] == 0) {
      q.push(i);
    }
  }
```

```cpp
  order.clear();
  while (!q.empty()) {
    int v = q.front();
    q.pop();
    order.push_back(v);
    for (int i = 0; i < G.nbr[v].size(); i++) {
      if (--indeg[G.nbr[v][i]] == 0) {
        q.push(G.nbr[v][i]);
      }
    }
  }

  return order.size() == G.num_nodes;
}


int main(void)
{
  int n, m;

  while (cin >> n >> m && (n || m)) {
    Graph G(n);
    for (int i = 0; i < m; i++) {
      int u, v;
      cin >> u >> v;
      G.add_edge(u, v);
    }
    vector<int> order;
    if (topological_sort(G, order)) {
      for (int i = 0; i < n; i++) {
        if (i) cout << ' ';
        cout << order[i];
      }
      cout << endl;
    } else {
      cout << "there is a cycle" << endl;
    }
  }
  return 0;
}
```

```cpp
// UnionFind class -- based on Howard Cheng's C code for UnionFind
// Modified to use C++ by Rex Forsyth, Oct 22, 2003
//
// Constuctor -- builds a UnionFind object of size n and initializes it
// find -- return index of x in the UnionFind
// merge -- updates relationship between x and y in the UnionFind


class UnionFind
{
      struct UF { int p; int rank; };

   public:
      UnionFind(int n) {            // constructor
         howMany = n;
         uf = new UF[howMany];
         for (int i = 0; i < howMany; i++) {
            uf[i].p = i;
            uf[i].rank = 0;
         }
      }

      ~UnionFind() {
         delete[] uf;
      }

      int find(int x) { return find(uf,x); }        // for client use

      bool merge(int x, int y) {
         int res1, res2;
         res1 = find(uf, x);
         res2 = find(uf, y);
         if (res1 != res2) {
            if (uf[res1].rank > uf[res2].rank) {
               uf[res2].p = res1;
            }
            else {
               uf[res1].p = res2;
               if (uf[res1].rank == uf[res2].rank) {
                  uf[res2].rank++;
               }
            }
            return true;
         }
         return false;
      }

   private:
      int howMany;
      UF* uf;

      int find(UF uf[], int x) {     // recursive funcion for internal use
         if (uf[x].p != x) {
            uf[x].p = find(uf, uf[x].p);
         }
         return uf[x].p;
      }
};
```

```cpp
/*
 * Largest subvector sum
 *
 * Author: Howard Cheng
 * Reference: Programming Pearl, page 74
 *
 * Given an array of integers, we find the continguous subvector that
 * gives the maximum sum.  If all entries are negative, it returns
 * an empty vector with sum = 0.
 *
 * If we want the subvector to be nonempty, we should first scan for the
 * largest element in the vector (1-element subvector) and combine the
 * result in this routine.
 *
 * The sum is returned, as well as the start and the end position
 * (inclusive).  If start > end, then the subvector is empty.
 *
 */

#include <iostream>
#include <cassert>

using namespace std;

int vecsum(int v[], int n, int &start, int &end)
{
  int maxval = 0;
  int max_end = 0;
  int max_end_start, max_end_end;
  int i;

  start = max_end_start = 0;
  end = max_end_end = -1;
  for (i = 0; i < n; i++) {
    if (v[i] + max_end >= 0) {
      max_end = v[i] + max_end;
      max_end_end = i;
    } else {
      max_end_start = i+1;
      max_end_end = -1;
      max_end = 0;
    }

    if (maxval < max_end) {
      start = max_end_start;
      end = max_end_end;
      maxval = max_end;
    } else if (maxval == max_end) {
      /* put whatever preferences we have for a tie */
      /* eg. longest subvector, and then the one that starts the earliest */
      if (max_end_end - max_end_start > end - start ||
          (max_end_end - max_end_start == end - start &&
           max_end_start < start)) {
        start = max_end_start;
        end = max_end_end;
        maxval = max_end;
      }
    }
  }
  return maxval;
}

int main(void)
{
  int n;
  int *v;
  int i;
  int sum, start, end;
```

```cpp
  while (cin >> n && n > 0) {
    v = new int[n];
    assert(v);
    for (i = 0; i < n; i++) {
      cin >> v[i];
    }
    sum = vecsum(v, n, start, end);
    cout << "Maximum sum " << sum << " from " << start << " to " << end << "."
         << endl;
    delete[] v;
  }

  return 0;
}
```

```c
/*
 * Zero-one programming
 *
 * Author: Howard Cheng
 * Reference:
 *    http://www.cs.sunysb.edu/~algorith/implement/syslo/distrib/processed/
 *
 * This algorithm is based on BALAS branching testing.
 *
 * This algorithm solves the BINARY linear program:
 *
 *      min  cx                 [cost function]
 *      s.t.
 *           Ax <= b            [constraints]
 *           x[i] = 0 or 1.
 *
 * where A is an m x n matrix,
 *       c and x are n-dimensional vectors,
 *       b is an m-dimensional vector.
 *
 * n = number of variables
 * m = number of constraints
 *
 * It returns whether there exists a solution.
 * The optimal value of the cost function is returned in value.
 * The assignment giving the optimal cost function value is returned in x.
 *
 * Important Notes:
 *
 * 1. The matrices and arrays start their indices at 1!!!!!!
 * 2. If we want to have constraints that are >=, just multiply all the
 *    coefficients by -1.
 * 3. If we want to have constraints that are ==, do both >= and <=.
 * 4. The content of A, b, and c is preserved after this routine.
 * 5. The coefficients in the cost vector c must be positive.  If not,
 *    make a change of variable x'[i] = 1-x[i] and adjust all constraints
 *    as well as the returned optimal value.  This is especially useful
 *    if you wish to maximize the cost function.
 *
 */

#include <stdio.h>
#include <limits.h>
#include <assert.h>

#define MAX_VAR 1000
#define MAX_CONS 100
#define MAX_ROWS MAX_CONS+1
#define MAX_COLS MAX_VAR+1

int zero_one(int A[MAX_ROWS][MAX_COLS], int *b, int *c, int n, int m,
             int *val, int *x)
{
  int exist;
  int alpha, beta, gamma, i, j, mnr, nr;
  int p, r, r1, r2, s, t, z;
  int y[MAX_ROWS], w[MAX_ROWS], zr[MAX_ROWS];
  int ii[MAX_COLS], jj[MAX_COLS], xx[MAX_COLS];
  int kk[MAX_COLS+1];

  for (i = 1; i <= m; i++) {
    y[i] = b[i];
  }
  z = 1;
  for (j = 1; j <= n; j++) {
    xx[j] = 0;
    z += c[j];
  }
  *val = z+z;
```

```c
  s = t = z = exist = 0;
  kk[1] = 0;
m10:
  p = mnr = 0;
  for (i = 1; i <= m; i++) {
    if ((r = y[i]) < 0) {
      p++;
      gamma = 0;
      alpha = r;
      beta = -INT_MAX;
      for (j = 1; j <= n; j++) {
        if (xx[j] <= 0) {
          if (c[j] + z >= *val) {
            xx[j] = 2;
            kk[s+1]++;
            jj[++t] = j;
          } else {
            if ((r1 = A[i][j]) < 0) {
              alpha -= r1;
              gamma += c[j];
              if (beta < r1) {
                beta = r1;
              }
            }
          }
        }
      }
      if (alpha < 0) {
        goto m20;
      }
      if (alpha + beta < 0) {
        if (gamma + z >= *val) {
          goto m20;
        }
        for (j = 1; j <= n; j++) {
          r1 = A[i][j];
          r2 = xx[j];
          if (r1 < 0) {
            if (!r2) {
              xx[j] = -2;
              for (nr = 1; nr <= mnr; nr++) {
                zr[nr] -= A[w[nr]][j];
                if (zr[nr] < 0) {
                  goto m20;
                }
              }
            }
          } else {
            if (r2 < 0) {
              alpha -= r1;
              if (alpha < 0) {
                goto m20;
              }
              gamma += c[j];
              if (gamma + z >= *val) {
                goto m20;
              }
            }
          }
        }
        mnr++;
        w[mnr] = i;
        zr[mnr] = alpha;
      }
    }
  }

  if (!p) {
    *val = z;
```

```c
      exist = 1;
      for (j = 1; j <= n; j++) {
        x[j] = (xx[j] == 1) ? 1 : 0;
      }
      goto m20;
    }

    if (!mnr) {
      p = 0;
      gamma = -INT_MAX;
      for (j = 1; j <= n; j++) {
        if (!xx[j]) {
          beta = 0;
          for (i = 1; i <= m; i++) {
            r = y[i];
            r1 = A[i][j];
            if (r < r1) {
              beta += r - r1;
            }
          }
          r = c[j];
          if ((beta > gamma) ||
              (beta == gamma && r < alpha)) {
            alpha = r;
            gamma = beta;
            p = j;
          }
        }
      }
      if (!p) {
        goto m20;
      }
      s++;
      kk[s+1] = 0;
      jj[++t] = p;
      ii[s] = xx[p] = 1;
      z += c[p];
      for (i = 1; i <= m; i++) {
        y[i] -= A[i][p];
      }
    } else {
      s++;
      ii[s] = kk[s+1] = 0;
      for (j = 1; j <= n; j++) {
        if (xx[j] < 0) {
          jj[++t] = j;
          ii[s]--;
          z += c[j];
          xx[j] = 1;
          for (i = 1; i <= m; i++) {
            y[i] -= A[i][j];
          }
        }
      }
    }
    goto m10;

m20:
    for (j = 1; j <= n; j++) {
      if (xx[j] < 0) {
        xx[j] = 0;
      }
    }
    if (s > 0) {
      do {
        p = t;
        t -= kk[s+1];
        for (j = t+1; j <= p; j++) {
          xx[jj[j]] = 0;
```

```c
        }
        p = (ii[s] >= 0) ? ii[s] : -ii[s];
        kk[s] += p;
        for (j = t-p+1; j <= t; j++) {
          p = jj[j];
          xx[p] = 2;
          z -= c[p];
          for (i = 1; i <= m; i++) {
            y[i] += A[i][p];
          }
        }
        s--;
        if (ii[s+1] >= 0) {
          goto m10;
        }
      } while (s);
    }

    return exist;
}

int main(void)
{
  int A[MAX_ROWS][MAX_COLS];
  int c[MAX_COLS], x[MAX_COLS], b[MAX_ROWS];
  int val, t;
  int m, n, i, j;

  while (scanf("%d %d", &n, &m) == 2 && n > 0 && m > 0) {
    /* read cost function */
    printf("Input cost function to minimize:\n");
    for (i = 1; i <= n; i++) {
      scanf("%d", &c[i]);
    }

    /* read constraints */
    for (i = 1; i <= m; i++) {
      printf("Input constraint #%d:\n", i);
      for (j = 1; j <= n; j++) {
        scanf("%d", &A[i][j]);
      }
      scanf("%d", &b[i]);
    }

    t = zero_one(A, b, c, n, m, &val, x);
    if (t) {
      printf("Minimum cost = %d\n", val);
      for (i = 1; i <= n; i++) {
        printf("x[%2d] = %2d\n", i, x[i]);
      }
    } else {
      printf("No solution exists.\n");
    }
  }

  return 0;
}
```