Data Analysis in R

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LOAD PACKAGES

```
# Load packages
library(tidyverse) # Loads the `tidyverse` collection
library(readxl) # Reads CSV and Excel files
```

LOAD DATA

```
# Also convert several adjacent variables to factors
df <- read_csv("../data/state_trends.csv") |>
  select(region:psy_reg) |>
  mutate(across(c(psych_region, psy_reg), as_factor)) |>
 print()
## Rows: 48 Columns: 34
## -- Column specification -----
## Delimiter: ","
## chr (11): state, state_code, region, psych_region, psy_reg, has_nba, has_nfl...
## dbl (23): population, sq_miles, pop_density, extraversion, agreeableness, co...
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
## # A tibble: 48 x 3
##
     region
               psych_region
                                             psy_reg
##
      <chr>
               <fct>
                                             <fct>
## 1 South
              Friendly and Conventional
                                             Friendly
## 2 West
               Relaxed and Creative
                                             Creative
## 3 South
               Friendly and Conventional
                                             Friendly
## 4 West
               Relaxed and Creative
                                             Creative
## 5 West
               Friendly and Conventional
                                             Friendly
## 6 Northeast Temperamental and Uninhibited Uninhibited
## 7 South
            Temperamental and Uninhibited Uninhibited
## 8 South
               Friendly and Conventional
                                             Friendly
## 9 South
               Friendly and Conventional
                                             Friendly
## 10 West
               Relaxed and Creative
                                             Creative
## # ... with 38 more rows
```

SUMMARIZE DATAFRAME

```
## region psych_region psy_reg
## Length:48 Friendly and Conventional :24 Friendly :24
## Class :character Relaxed and Creative :10 Creative :10
## Mode :character Temperamental and Uninhibited:14 Uninhibited:14
```

SUMMARIZE CATEGORICAL VARIABLE

```
# "region" is a character variable
# summary() not very useful
df |>
  select(region) |>
 summary()
##
      region
## Length:48
## Class :character
## Mode :character
# table() works better
 select(region) |>
table()
## region
## Midwest Northeast
                         South
                                    West
         12 9
                            16
                                      11
```

SUMMARIZE FACTOR

```
# Using table()
df |>
 select(psych_region) |>
 table()
## psych_region
                                         Relaxed and Creative
      Friendly and Conventional
## Temperamental and Uninhibited
# Convert region to a factor
df <- df |>
 mutate(region = as_factor(region)) |>
 print()
## # A tibble: 48 x 3
##
     region psych_region
                                             psy_reg
##
     <fct>
               <fct>
                                             <fct>
## 1 South
             Friendly and Conventional
                                             Friendly
             Relaxed and Creative
## 2 West
                                             Creative
## 3 South
            Friendly and Conventional
                                             Friendly
## 4 West
             Relaxed and Creative
                                             Creative
## 5 West
               Friendly and Conventional
                                             Friendly
## 6 Northeast Temperamental and Uninhibited Uninhibited
## 7 South
               Temperamental and Uninhibited Uninhibited
## 8 South
               Friendly and Conventional
                                             Friendly
## 9 South
               Friendly and Conventional
                                             Friendly
## 10 West
               Relaxed and Creative
                                             Creative
## # ... with 38 more rows
# Summarize multiple factors
summary(df)
##
         region
                                         psych_region
                                                            psy_reg
## South
            :16
                  Friendly and Conventional
                                            :24
                                                      Friendly
## West
                  Relaxed and Creative
            :11
                                               :10
                                                      Creative
                                                                :10
## Northeast: 9
                  Temperamental and Uninhibited:14
                                                      Uninhibited:14
## Midwest :12
```

DESCRIPTIVES

```
# Also convert several adjacent variables to factors

df_des <- read_csv("../data/state_trends.csv") |>
   mutate(across(c(
    region, psych_region, psy_reg, has_nba:has_any
    ),
    as_factor)
   ) |>
   print()
```

```
## Rows: 48 Columns: 34
## -- Column specification --------
## Delimiter: ","
## chr (11): state, state_code, region, psych_region, psy_reg, has_nba, has_nfl...
## dbl (23): population, sq_miles, pop_density, extraversion, agreeableness, co...
##
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
## # A tibble: 48 x 34
##
     state state~1 popul~2 sq_mi~3 pop_d~4 region psych~5 psy_reg extra~6 agree~7
##
     <chr> <chr>
                      <dbl>
                              <dbl>
                                     <dbl> <fct> <fct>
                                                          <fct>
                                                                    <dbl>
                                                                           <dbl>
## 1 Alaba~ AL
                     5.02e6
                              52420
                                        96 South Friend~ Friend~
                                                                     55.5
                                                                            52.7
## 2 Arizo~ AZ
                     7.15e6 113990
                                        63 West
                                                  Relaxe~ Creati~
                                                                    50.6
                                                                            46.6
                                        57 South Friend~ Friend~
## 3 Arkan~ AR
                     3.01e6
                            53179
                                                                    49.9
                                                                            52.7
## 4 Calif~ CA
                     3.95e7 163695
                                       242 West
                                                  Relaxe~ Creati~
                                                                     51.4
                                                                            49
## 5 Color~ CO
                     5.77e6 104094
                                        55 West
                                                  Friend~ Friend~
                                                                    45.3
                                                                            47.5
## 6 Conne~ CT
                             5543
                                       650 North~ Temper~ Uninhi~
                                                                    57.6
                     3.61e6
                                                                            38.6
## 7 Delaw~ DE
                                                                            38.8
                     9.90e5
                             2489
                                       398 South Temper~ Uninhi~
                                                                     47
## 8 Flori~ FL
                              65758
                                       328 South Friend~ Friend~
                                                                     60.9
                                                                            50.7
                     2.15e7
                                       180 South Friend~ Friend~
## 9 Georg~ GA
                             59425
                                                                     63.2
                     1.07e7
                                                                            60
## 10 Idaho ID
                     1.84e6
                             83569
                                        22 West
                                                  Relaxe~ Creati~
                                                                     40.7
                                                                            52.9
## # ... with 38 more rows, 24 more variables: conscientiousness <dbl>,
      neuroticism <dbl>, openness <dbl>, data_science <dbl>,
      artificial_intelligence <dbl>, machine_learning <dbl>, data_analysis <dbl>,
## #
## #
      business_intelligence <dbl>, spreadsheet <dbl>, statistics <dbl>,
## #
      art <dbl>, dance <dbl>, museum <dbl>, basketball <dbl>, football <dbl>,
## #
      baseball <dbl>, soccer <dbl>, hockey <dbl>, has_nba <fct>, has_nfl <fct>,
      has_mlb <fct>, has_mls <fct>, has_nhl <fct>, has_any <fct>, and ...
## #
```

SUMMARY

```
# Summary for entire dataset
df_des |> summary()
```

```
##
                       state_code
      state
                                          population
                                                             sq_miles
## Length:48
                     Length:48
                                        Min. : 576851
                                                          Min. : 1545
                                        1st Qu.: 2078518
                                                          1st Qu.: 39411
## Class :character
                      Class :character
## Mode :character Mode :character
                                        Median : 4841018
                                                          Median: 57094
##
                                              : 6845231
                                                          Mean : 65008
                                        Mean
##
                                        3rd Qu.: 7936809
                                                          3rd Qu.: 83901
##
                                               :39538223
                                                          Max.
                                                                :268596
##
    pop_density
                         region
                                                        psych_region
## Min.
         :
              6.0
                    South
                            :16
                                  Friendly and Conventional
                                                              :24
                                  Relaxed and Creative
##
  1st Qu.: 52.0
                    West
                             :11
## Median: 93.0
                                  Temperamental and Uninhibited:14
                    Northeast: 9
         : 178.4
## Mean
                    Midwest :12
## 3rd Qu.: 206.8
## Max.
          :1065.0
          psy_reg
                    extraversion
                                   agreeableness
                                                  conscientiousness
                                          :29.80
## Friendly :24
                   Min.
                          :26.50
                                   Min.
                                                  Min. :24.00
```

```
Creative :10
                    1st Qu.:44.35
                                   1st Qu.:45.77
                                                   1st Qu.:43.05
                    Median :51.15
                                   Median :52.05
                                                  Median :51.35
   Uninhibited:14
##
                    Mean :49.70
                                   Mean :50.59
                                                   Mean :50.12
##
                    3rd Qu.:56.05
                                   3rd Qu.:56.62
                                                   3rd Qu.:56.12
##
                    Max. :69.80
                                   Max. :69.40
                                                   Max. :69.60
##
                      openness
                                   data science
                                                  artificial intelligence
    neuroticism
   Min. :30.40
                   Min. :21.80
                                  Min. :17.00
                                                  Min. :18.00
                                  1st Qu.:22.00
   1st Qu.:43.85
                   1st Qu.:42.70
                                                  1st Qu.:23.00
##
##
   Median :49.00
                   Median :49.85
                                  Median :27.00
                                                  Median :26.00
##
   Mean :50.19
                   Mean :49.43
                                  Mean :31.62
                                                  Mean :27.94
   3rd Qu.:56.92
                   3rd Qu.:56.67
                                  3rd Qu.:37.00
                                                  3rd Qu.:30.00
   Max. :79.20
                   Max. :65.00
                                  Max. :74.00
##
                                                  Max.
                                                        :56.00
   machine_learning data_analysis
                                  business_intelligence spreadsheet
##
   Min. : 19.0
                    Min. :27.0
                                  Min. : 24.00
                                                       Min. :49.00
   1st Qu.: 22.0
                    1st Qu.:31.0
                                  1st Qu.: 44.50
                                                        1st Qu.:63.00
##
   Median: 32.0
                    Median:35.0
                                  Median : 52.50
                                                       Median :68.50
##
   Mean : 36.4
                    Mean :37.4
                                  Mean : 52.21
                                                       Mean :69.42
   3rd Qu.: 42.0
                    3rd Qu.:40.0
                                  3rd Qu.: 59.75
                                                        3rd Qu.:76.25
##
   Max. :100.0
                    Max. :64.0
                                  Max. :100.00
                                                       Max. :88.00
##
     statistics
                       art
                                       dance
                                                       museum
                   Min. : 65.00
##
   Min.
         :41.00
                                   Min. : 59.00
                                                   Min. :14.00
   1st Qu.:53.00
                   1st Qu.: 72.00
                                   1st Qu.: 66.75
                                                   1st Qu.:23.00
   Median :55.00
                   Median : 75.00
                                   Median : 70.00
##
                                                   Median :26.00
   Mean :56.23
                   Mean : 76.75
                                   Mean : 70.83
                                                    Mean :26.29
##
##
   3rd Qu.:62.00
                   3rd Qu.: 80.00
                                   3rd Qu.: 74.00
                                                    3rd Qu.:29.00
   Max. :73.00
                   Max. :100.00
                                   Max. :100.00
                                                    Max. :41.00
##
     basketball
                      football
                                       baseball
                                                       soccer
  Min. : 21.00
                    Min. : 19.00
                                    Min. : 27.00
                                                    Min. : 41.00
##
  1st Qu.: 33.00
                    1st Qu.: 29.75
                                    1st Qu.: 32.75
                                                     1st Qu.: 60.75
  Median : 39.50
                    Median : 40.00
                                    Median : 38.00
                                                     Median : 67.00
   Mean : 44.31
                    Mean : 42.81
##
                                    Mean : 41.38
                                                     Mean : 67.33
##
   3rd Qu.: 51.50
                    3rd Qu.: 51.25
                                    3rd Qu.: 43.75
                                                     3rd Qu.: 76.00
   Max. :100.00
                                    Max. :100.00
##
                    Max. :100.00
                                                     Max. :100.00
##
       hockey
                    has_nba has_nfl has_mlb has_mls has_nhl has_any
   Min. : 4.00
##
                    No :27
                            No :26
                                     No :31
                                              No :31
                                                      No :30
                                                               No :21
   1st Qu.: 8.00
                    Yes:21
                            Yes:22
                                     Yes:17
                                             Yes:17
                                                      Yes:18
                                                               Yes:27
## Median : 13.50
## Mean : 20.29
   3rd Qu.: 22.75
##
## Max. :100.00
# Summary for one variable
df des |>
 select(statistics) |>
 summary()
##
     statistics
## Min. :41.00
```

1st Qu.:53.00 ## Median :55.00 ## Mean :56.23 ## 3rd Qu.:62.00 ## Max. :73.00

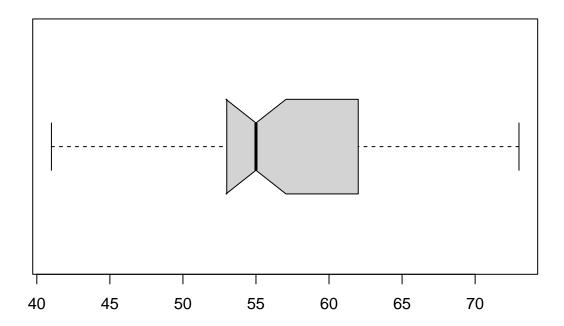
QUARTILES

```
# Tukey's five-number summary: minimum, lower-hinge,
# median, upper-hinge, maximum. No labels.
fivenum(df_des$statistics)
```

[1] 41 53 55 62 73

```
# Boxplot stats: hinges, n, CI for median, and outliers
boxplot(df_des$statistics, notch = T, horizontal = T)
```

```
## Warning in (function (z, notch = FALSE, width = NULL, varwidth = FALSE, : some
## notches went outside hinges ('box'): maybe set notch=FALSE
```



boxplot.stats(df_des\$statistics)

```
## $stats
## [1] 41 53 55 62 73
##
## $n
## [1] 48
##
```

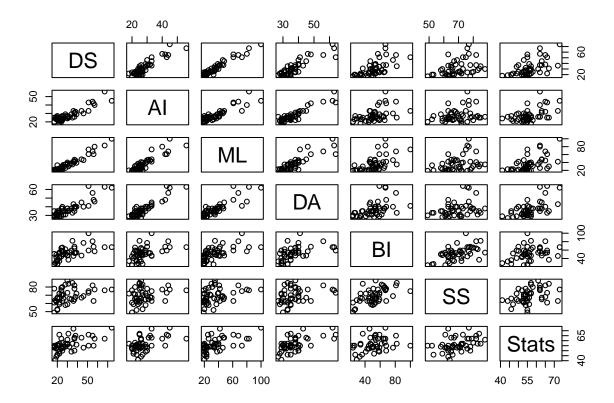
```
## $conf
## [1] 52.94752 57.05248
##
## $out
## numeric(0)
```

CORRELATIONS

```
# Load data and convert several adjacent variables to factors
df cor <- read csv("../data/state trends.csv") |>
 select( # Rename variables with `select`
   DS = data science, # New = old
   AI = artificial_intelligence,
   ML = machine_learning,
   DA = data_analysis,
   BI = business_intelligence,
   SS = spreadsheet,
   Stats = statistics) |>
 print()
## Rows: 48 Columns: 34
## -- Column specification -----
## Delimiter: ","
## chr (11): state, state_code, region, psych_region, psy_reg, has_nba, has_nfl...
## dbl (23): population, sq_miles, pop_density, extraversion, agreeableness, co...
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
## # A tibble: 48 x 7
##
                                ΒI
                                      SS Stats
        DS
              ΑI
                    ML
                          DA
##
      <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
##
        20
              23
                    23
                          35
                                36
                                      66
                                            46
  1
## 2
        26
              26
                    34
                          35
                                50
                                      66
                                            53
## 3
        25
              23
                    22
                          40
                                58
                                      63
                                            50
## 4
        57
              40
                    80
                          46
                                57
                                      77
                                            62
                          35
                                      82
## 5
        37
              26
                    41
                                64
                                            62
        38
              32
                    45
                          40
                                53
                                      68
                                            65
##
  6
## 7
              33
                    42
                                46 63
                                            72
        36
                          43
        28
                          35
                                50
                                      58
##
  8
              29
                    26
                                            54
              29
                    38
                          38
                                59
                                      65
                                            49
## 9
        34
## 10
        22
              25
                    25
                          33
                                54
                                      61
                                            66
## # ... with 38 more rows
```

CORRELATION MATRIX

```
# Scatterplot matrix
df_cor |> plot()
```



Correlation matrix

df_cor |> cor()

```
##
                DS
                          ΑI
                                    ML
                                              DA
                                                        ΒI
                                                                  SS
## DS
         1.0000000 0.9074983 0.9687222 0.8836444 0.6460126 0.3781570 0.5710977
        0.9074983\ 1.0000000\ 0.8973295\ 0.9182502\ 0.4998677\ 0.2492768\ 0.5088401
## AI
        0.9687222 0.8973295 1.0000000 0.8655480 0.6084254 0.3481992 0.5738845
## ML
        0.8836444 0.9182502 0.8655480 1.0000000 0.5024155 0.3025197 0.6008586
## DA
         0.6460126 0.4998677 0.6084254 0.5024155 1.0000000 0.5657397 0.3100625
## SS
         0.3781570 0.2492768 0.3481992 0.3025197 0.5657397 1.0000000 0.3825016
## Stats 0.5710977 0.5088401 0.5738845 0.6008586 0.3100625 0.3825016 1.0000000
```

Rounded to 2 decimals

df_cor |> cor() |>
 round(2)

```
SS Stats
##
          DS
               ΑI
                    ML
                         DA
                              BI
## DS
        1.00 0.91 0.97 0.88 0.65 0.38 0.57
## AI
        0.91 1.00 0.90 0.92 0.50 0.25 0.51
        0.97 0.90 1.00 0.87 0.61 0.35 0.57
## ML
        0.88 0.92 0.87 1.00 0.50 0.30 0.60
## DA
        0.65 0.50 0.61 0.50 1.00 0.57 0.31
## BI
## SS
        0.38 0.25 0.35 0.30 0.57 1.00 0.38
## Stats 0.57 0.51 0.57 0.60 0.31 0.38 1.00
```

TEST AND CI FOR A SINGLE CORRELATION

```
# Can test one pair of variables at a time.
# Gives r, hypothesis test, and confidence interval
cor.test(df_cor$DS, df_cor$DA)

##
## Pearson's product-moment correlation
##
## data: df_cor$DS and df_cor$DA
## t = 12.802, df = 46, p-value < 2.2e-16
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.8004926 0.9334212
## sample estimates:
## cor
## 0.8836444</pre>
```

PACKAGES TO GET P-VALUES FOR MATRIX

```
# The `Hmisc` package can get p-values for matrix
#browseURL("https://cran.r-project.org/web/packages/Hmisc/")

# The `rstatix` package is another option (with graphs)
#browseURL("https://cran.r-project.org/web/packages/rstatix/")
```

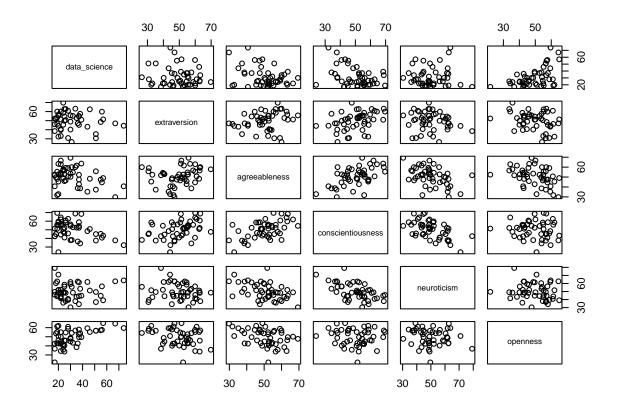
REGRESSION

LOAD DATA

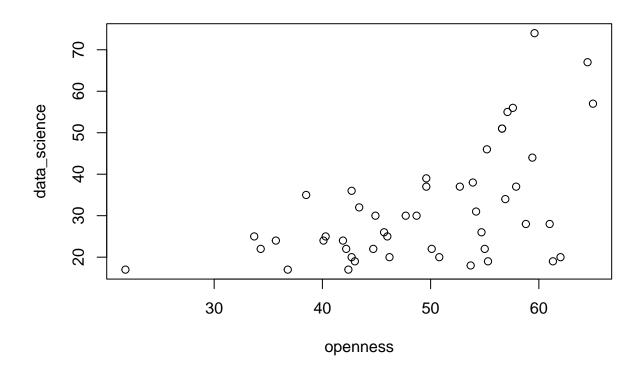
```
<dbl>
                       <dbl>
                               <dbl>
                                        <dbl>
                                                <dbl>
                                                         <dbl>
                                                                 <dbl>
                                                                          <dbl>
                                                                                  <dbl>
##
                                                 42.7
##
   1
              55.5
                        52.7
                                55.5
                                         48.7
                                                            20
                                                                    23
                                                                             23
                                                                                     35
    2
              50.6
                        46.6
                                58.4
                                         38.1
                                                 54.7
                                                            26
                                                                    26
                                                                             34
                                                                                     35
##
##
    3
              49.9
                        52.7
                                41
                                         56.2
                                                 40.3
                                                            25
                                                                    23
                                                                             22
                                                                                     40
                                43.2
##
    4
              51.4
                        49
                                         39.1
                                                 65
                                                            57
                                                                    40
                                                                             80
                                                                                     46
##
    5
              45.3
                        47.5
                                58.8
                                         34.3
                                                 57.9
                                                            37
                                                                    26
                                                                             41
                                                                                     35
##
    6
              57.6
                        38.6
                                34.2
                                         53.4
                                                 53.9
                                                            38
                                                                    32
                                                                             45
                                                                                     40
                                         62.4
                                                                             42
                                                                                     43
    7
              47
                        38.8
                                36.5
                                                 42.7
                                                            36
                                                                    33
##
##
              60.9
                        50.7
                                62.7
                                         40.8
                                                 61
                                                            28
                                                                    29
                                                                             26
                                                                                     35
##
   9
              63.2
                        60
                                 68.8
                                         38
                                                 56.9
                                                            34
                                                                    29
                                                                             38
                                                                                     38
## 10
              40.7
                        52.9
                                44.5
                                         44.2
                                                 44.7
                                                            22
                                                                    25
                                                                             25
                                                                                     33
## # ... with 38 more rows, 11 more variables: business_intelligence <dbl>,
       spreadsheet <dbl>, statistics <dbl>, art <dbl>, dance <dbl>, museum <dbl>,
## #
       basketball <dbl>, football <dbl>, baseball <dbl>, soccer <dbl>,
## #
       hockey <dbl>, and abbreviated variable names 1: agreeableness,
## #
       2: conscientiousness, 3: neuroticism, 4: openness, 5: data_science,
## #
       6: artificial_intelligence, 7: machine_learning, 8: data_analysis
```

SCATTERPLOTS

```
# Scatterplot of "data_science" and personality variables
df_reg |>
   select(data_science, extraversion:openness) |>
   plot()
```



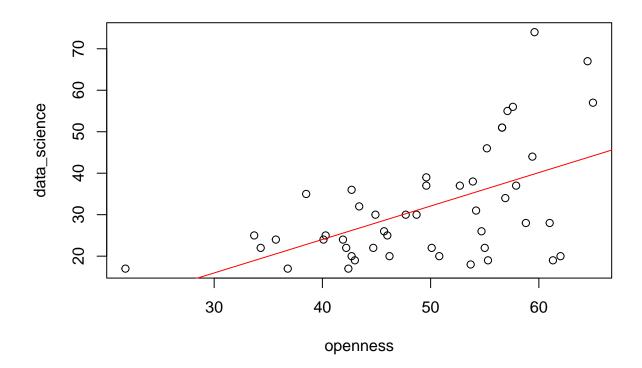
```
# Quick graphical check on bivariate association
df_reg |>
    select(openness, data_science) |>
    plot()
```



```
# Add regression line with lm(); usage: y ~ X
# Note different variable order (vs plot)

df_reg |>
    select(openness, data_science) |>
    plot()

lm(df_reg$data_science ~ df_reg$openness) |> abline(col = "red")
```



BIVARIATE REGRESSION

```
# Compute and save bivariate regression
fit1 <- lm(df_reg$data_science ~ df_reg$openness)</pre>
# Show model
fit1
##
## Call:
## lm(formula = df_reg$data_science ~ df_reg$openness)
##
## Coefficients:
##
       (Intercept)
                    df_reg$openness
##
           -8.2243
                              0.8062
\# Summarize regression model
summary(fit1)
##
## Call:
## lm(formula = df_reg$data_science ~ df_reg$openness)
```

```
##
## Residuals:
      Min
                1Q Median
## -22.197 -7.822 -0.636
                             6.350
                                   34.173
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
                                9.2229 -0.892
## (Intercept)
                    -8.2243
## df_reg$openness
                     0.8062
                                0.1835
                                         4.394 6.49e-05 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 11.66 on 46 degrees of freedom
## Multiple R-squared: 0.2957, Adjusted R-squared: 0.2804
## F-statistic: 19.31 on 1 and 46 DF, p-value: 6.488e-05
# Confidence intervals for coefficients
confint(fit1)
                         2.5 %
                                  97.5 %
##
## (Intercept)
                   -26.7890606 10.340520
## df reg$openness
                    0.4369258 1.175521
# Predict values of "data science"
predict(fit1)
                                                                       7
                     2
                               3
                                                   5
                                                             6
## 26.201468 35.876149 24.266532 44.180250 38.456064 35.231170 26.201468 40.955356
                    10
                              11
                                        12
                                                  13
                                                            14
## 37.649840 27.813915 36.279260 27.975160 18.945458 24.105287 26.443335 35.069925
                    18
                              19
                                        20
                                                  21
                                                            22
                                                                      23
## 32.731878 37.407973 39.826643 26.765824 22.815330 29.023250 28.620138 36.118016
                    26
                              27
                                        28
                                                            30
                                                  29
## 19.429192 41.197223 31.038808 38.214197 41.761579 43.777138 31.764409
                                                                          9.351399
          33
                    34
                              35
                                        36
                                                  37
                                                            38
                                                                      39
## 28.862005 25.798356 39.181665 31.764409 39.665399 36.359883 25.556489 32.167521
                    42
                              43
                                        44
                                                  45
                                                            46
## 34.263702 30.232585 35.473037 37.811085 37.407973 21.444750 20.557904 25.959601
# Prediction intervals for values of "data_science"
predict(fit1, interval = "prediction")
## Warning in predict.lm(fit1, interval = "prediction"): predictions on current data refer to _future_ :
##
            fit
                        lwr
                                 upr
## 1 26.201468
                  2.3662348 50.03670
## 2 35.876149 12.0908906 59.66141
                 0.3226886 48.21038
## 3 24.266532
## 4 44.180250 19.7871953 68.57330
## 5 38.456064 14.5450318 62.36710
## 6 35.231170 11.4682748 58.99407
## 7 26.201468 2.3662348 50.03670
```

```
## 8 40.955356 16.8677571 65.04295
## 9 37.649840 13.7843267 61.51535
                 4.0443105 51.58352
## 10 27.813915
## 11 36.279260 12.4781738 60.08035
## 12 27.975160
                 4.2108654 51.73945
## 13 18.945458
                -5.4610823 43.35200
## 14 24.105287
                 0.1509350 48.05964
## 15 26.443335
                 2.6193943 50.26728
## 16 35.069925 11.3120501 58.82780
## 17 32.731878
                9.0210428 56.44271
## 18 37.407973
                13.5550171 61.26093
## 19 39.826643
                15.8253845 63.82790
## 20 26.765824
                 2.9561468 50.57550
                -1.2310968 46.86176
## 21 22.815330
## 22 29.023250
                 5.2878987 52.75860
## 23 28.620138
                 4.8747996 52.36548
## 24 36.118016 12.3234312 59.91260
## 25 19.429192
                -4.9255705 43.78395
## 26 41.197223
               17.0897203 65.30473
## 27 31.038808
                 7.3318744 54.74574
## 28 38.214197 14.3174104 62.11098
## 29 41.761579 17.6057220 65.91744
## 30 43.777138
               19.4269563 68.12732
## 31 31.764409
                 8.0589101 55.46991
## 32 9.351399 -16.4563515 35.15915
## 33 28.862005
                 5.1228309 52.60118
                 1.9431707 49.65354
## 34 25.798356
## 35 39.181665
               15.2248726 63.13846
## 36 31.764409
                 8.0589101 55.46991
## 37 39.665399 15.6755899 63.65521
## 38 36.359883 12.5554599 60.16431
## 39 25.556489
                1.6886545 49.42432
## 40 32.167521
                 8.4608053 55.87424
## 41 34.263702 10.5274948 57.99991
## 42 30.232585
                 6.5185930 53.94658
## 43 35.473037 11.7021836 59.24389
## 44 37.811085 13.9369178 61.68525
## 45 37.407973 13.5550171 61.26093
## 46 21.444750
                -2.7149603 45.60446
## 47 20.557904 -3.6834905 44.79930
## 48 25.959601
                 2.1125659 49.80664
```

Regression diagnostics

lm.influence(fit1)

```
## $hat
                       2
                                   3
                                              4
                                                         5
## 0.03204490 0.02772167 0.04147177 0.08091649 0.03861935 0.02579005 0.03204490
            8
                       9
                                  10
                                             11
                                                        12
                                                                    13
## 0.05401502 0.03466878 0.02636937 0.02908997 0.02591083 0.08211198 0.04238617
                      16
                                  17
                                             18
                                                                    20
           15
                                                        19
## 0.03106722 0.02535670 0.02130032 0.03358023 0.04647249 0.02983302 0.05041491
                      23
                                  24
                                             25
                                                        26
## 0.02341341 0.02427486 0.02852779 0.07752552 0.05575763 0.02096431 0.03738215
```

```
29
                       30
                                              32
                                                          33
                                                                     34
                                   31
## 0.05999714 0.07712024 0.02084074 0.20992957 0.02374313 0.03377347 0.04259852
                       37
                                   38
                                              39
                                                          40
                                                                     41
                                                                                 42
  0.02084074 0.04547427 0.02937850 0.03487007 0.02094552 0.02348722 0.02157232
##
           43
                       44
                                   45
                                              46
                                                          47
  0.02647725 0.03541925 0.03358023 0.06033532 0.06751747 0.03306718
##
## $coefficients
##
       (Intercept) df_reg$openness
## 1
      -0.661243471
                       0.0106777299
  2
       0.444262476
                      -0.0132696890
## 3
       0.101465339
                      -0.0017302988
##
  4
      -2.369351364
                       0.0538154992
## 5
       0.125590014
                      -0.0031792941
## 6
      -0.096461644
                       0.0031495416
## 7
       1.044787321
                      -0.0168711787
## 8
       1.655507634
                      -0.0392663702
## 9
       0.267222337
                      -0.0070000389
## 10 -0.470060791
                       0.0069932736
## 11 -0.499188974
                       0.0143195190
                      -0.0023314355
## 12
       0.158542334
       1.407753236
                      -0.0257011543
## 14 -0.014848249
                       0.0002540647
## 15 -0.764638068
                       0.0122320902
## 16
       0.551530983
                      -0.0185405734
## 17 -0.052312107
                      -0.0044248647
## 18 -0.942349197
                       0.0249934967
## 19 -3.717906815
                       0.0903259877
## 20
       0.510585247
                      -0.0080560436
## 21
       1.984291426
                      -0.0347373723
## 22 -0.557615112
                       0.0073871213
## 23 -0.178502804
                       0.0024795829
## 24
       0.688990775
                      -0.0200649761
## 25
       0.574295673
                      -0.0104443967
## 26
       2.928080007
                      -0.0691489198
## 27 -0.031552372
                       0.0001911322
## 28 -1.464232864
                       0.0374118744
## 29
       3.082003742
                      -0.0721124239
## 30 -4.120333190
                       0.0939681638
## 31
       0.138302747
                       0.0003165704
       3.476819223
   32
                      -0.0662619232
## 33 -0.248431728
                       0.0033588162
   34 -0.429800977
                       0.0070387030
##
  35
       1.097177894
                      -0.0271206404
   36
      0.100074286
                       0.0002290667
## 37 -0.459970218
                       0.0112200949
## 38
       0.913648305
                      -0.0260233701
## 39 -0.182248441
                       0.0030074605
## 40 -0.130779946
                      -0.0017313399
## 41 -0.053927444
                       0.0022721303
## 42 -0.009979763
                       0.0001017136
## 43 0.172822854
                      -0.0054331671
## 44 -1.303105522
                       0.0338753022
## 45 -0.942349197
                       0.0249934967
```

```
## 46 -0.829945259
                    0.0147975669
## 47 0.697397610 -0.0125537453
## 48 -0.990384870
                    0.0161317059
##
## $sigma
                   2
                            3
                                     4
                                               5
                                                        6
         1
## 11.74726 11.68981 11.78425 11.61496 11.78270 11.77736 11.69089 11.61629
         9
                  10
                           11
                                     12
                                              13
                                                       14
                                                                 15
## 11.77176 11.75200 11.69266 11.78081 11.74707 11.78477 11.73075 11.49945
         17
                  18
                           19
                                     20
                                              21
                                                       22
                                                                 23
  11.62757 11.60315 10.56715 11.75813 11.63644 11.70591 11.77815 11.58972
         25
                  26
                           27
                                     28
                                              29
                                                       30
                                                                 31
## 11.77802 11.28208 11.78374 11.47076 11.29981 11.22030 11.73426 11.71476
         33
                  34
                           35
                                     36
                                              37
                                                       38
## 11.77037 11.77069 11.66100 11.75836 11.76621 11.48831 11.78241 11.68480
         41
                  42
                           43
                                     44
                                              45
                                                       46
                                                                 47
## 11.77755 11.78473 11.76539 11.49235 11.60315 11.76494 11.77280 11.70625
## $wt.res
##
             1
                                      3
                                                  4
                                                               5
                                                                           6
##
    -6.2014681
               -9.8761487
                             0.7334680 12.8197504
                                                     -1.4560636
                                                                   2.7688300
             7
                         8
                                      9
                                                 10
                                                              11
                                                      9.7207396
                                                                   2.0248405
##
     9.7985319 -12.9553561
                            -3.6498402
                                        -5.8139149
##
            13
                        14
                                     15
                                                 16
                                                              17
                                                                  13.5920268
##
     6.0545424
               -0.1052873
                            -7.4433351 -17.0699253 -12.7318775
            19
                        20
                                     21
                                                 22
                                                              23
##
    34.1733567
                 5.2341755
                            12.1846701
                                        -9.0232500
                                                     -2.6201383 -14.1180157
                        26
##
            25
                                     27
                                                 28
                                                              29
##
     2.5708083 -22.1972231
                            -1.0388084
                                         17.7858035 -21.7615794
                                                                  23.2228621
            31
                        32
                                     33
                                                 34
                                                              35
##
     7.2355905
                 7.6486007
                             -3.8620053
                                         -3.7983564 -11.1816646
                                                                   5.2355905
##
            37
                        38
                                     39
                                                 40
                                                              41
                                                                          42
##
     4.3346014 -17.3598828
                             -1.5564894
                                        -10.1675212
                                                      2.7362980
                                                                  -0.2325850
                                                              47
##
            43
                        44
                                     45
                                                 46
                                                                          48
    -4.4730370 17.1889151 13.5920268 -4.4447501
                                                      3.4420956
                                                                  -8.9596011
```

influence.measures(fit1)

```
## Influence measures of
   lm(formula = df_reg$data_science ~ df_reg$openness) :
##
     dfb.1_ dfb.df_.
                   dffit cov.r cook.d
   0.04803 -0.072119 -0.14468 1.041 1.05e-02 0.0277
     -0.25781 0.294363 0.34161 1.073 5.79e-02 0.0809
     0.01347 -0.017143 -0.02526 1.086 3.26e-04 0.0386
   -0.01035 0.016990 0.03875 1.070 7.67e-04 0.0258
    0.11294 -0.091684 0.15500 1.046 1.21e-02 0.0320
    0.18011 -0.214757 -0.27400 1.043 3.73e-02 0.0540
     0.02869 -0.037779 -0.05980 1.078 1.82e-03 0.0347
## 11 -0.05396  0.077805  0.14604  1.043  1.07e-02  0.0291
## 12 0.01701 -0.012573 0.02840 1.071 4.12e-04 0.0259
```

```
## 13 0.15145 -0.139001 0.16090 1.124 1.31e-02 0.0821
## 14 -0.00159 0.001370 -0.00192 1.091 1.89e-06 0.0424
## 15 -0.08238  0.066247 -0.11542  1.059  6.75e-03  0.0311
## 16 0.06061 -0.102433 -0.24252 0.972 2.86e-02 0.0254
## 17 -0.00569 -0.024177 -0.16329 1.012 1.33e-02 0.0213
## 18 -0.10264  0.136850  0.22212  1.016  2.44e-02  0.0336
## 19 -0.44465 0.543061 0.73113 0.708 2.20e-01 0.0465
## 20 0.05488 -0.043529 0.07925 1.067 3.20e-03 0.0298
      ## 23 -0.01915  0.013375 -0.03552 1.069 6.44e-04 0.0243
     0.07513 -0.109992 -0.21179 1.006 2.22e-02 0.0285
      0.06162 -0.056338  0.06588  1.130  2.22e-03  0.0775
     0.32800 -0.389395 -0.49201 0.930 1.13e-01 0.0558
## 28 -0.16132  0.207210  0.31143  0.974  4.70e-02  0.0374
      0.34470 -0.405446 -0.50183 0.940 1.18e-01 0.0600
## 30 -0.46410 0.532071 0.62280 0.930 1.80e-01 0.0771
## 31 0.01490 0.001714 0.09091 1.049 4.19e-03 0.0208
      0.37508 -0.359355 0.37863 1.291 7.24e-02 0.2099
## 33 -0.02667  0.018130 -0.05179  1.065  1.37e-03  0.0237
## 34 -0.04615  0.037991 -0.06138  1.076  1.92e-03  0.0338
## 35 0.11891 -0.147760 -0.20672 1.046 2.14e-02 0.0426
      0.01076  0.001238  0.06565  1.058  2.19e-03  0.0208
## 37 -0.04941 0.060583 0.08230 1.088 3.45e-03 0.0455
## 38 0.10051 -0.143913 -0.26684 0.972 3.46e-02 0.0294
## 39 -0.01955  0.016217 -0.02556 1.082 3.34e-04 0.0349
## 40 -0.01414 -0.009414 -0.12863 1.032 8.31e-03 0.0209
## 41 -0.00579 0.012257 0.03646 1.067 6.79e-04 0.0235
## 42 -0.00107 0.000548 -0.00296 1.068 4.49e-06 0.0216
      0.01856 -0.029339 -0.06355 1.066 2.06e-03 0.0265
## 44 -0.14330 0.187270 0.29182 0.980 4.14e-02 0.0354
## 45 -0.10264 0.136850 0.22212 1.016 2.44e-02 0.0336
## 46 -0.08915 0.079909 -0.09876 1.105 4.97e-03 0.0603
      0.07487 -0.067747 0.08147 1.116 3.39e-03 0.0675
## 48 -0.10692 0.087550 -0.14394 1.052 1.04e-02 0.0331
```

MULTIPLE REGRESSION

```
# Moving the outcome, y, to the front and having nothing
# else but predictor variables, X, can make things easier
df_reg <- df_reg |>
   select(data_science, extraversion:openness) |>
   print()
```

```
##
  # A tibble: 48 x 6
      data_science extraversion agreeableness conscientiousness neuroticism openn~1
##
                            <dbl>
##
              <dbl>
                                            <dbl>
                                                               <dbl>
                                                                             <dbl>
                                                                                     <dbl>
                                                                              48.7
                                                                                      42.7
##
    1
                 20
                             55.5
                                             52.7
                                                                55.5
##
    2
                                            46.6
                 26
                             50.6
                                                                58.4
                                                                              38.1
                                                                                      54.7
##
    3
                 25
                             49.9
                                            52.7
                                                                41
                                                                              56.2
                                                                                      40.3
```

```
43.2
## 4
                57
                           51.4
                                         49
                                                                        39.1
                                                                                65
## 5
                37
                           45.3
                                         47.5
                                                            58.8
                                                                        34.3
                                                                                57.9
## 6
                38
                           57.6
                                         38.6
                                                            34.2
                                                                        53.4
                                                                                53.9
## 7
                36
                           47
                                         38.8
                                                            36.5
                                                                        62.4
                                                                                42.7
## 8
                28
                           60.9
                                         50.7
                                                            62.7
                                                                        40.8
                                                                                61
## 9
                34
                           63.2
                                         60
                                                            68.8
                                                                        38
                                                                                56.9
                22
                           40.7
                                          52.9
                                                            44.5
                                                                        44.2
                                                                                44.7
## # ... with 38 more rows, and abbreviated variable name 1: openness
# Note that if you want to just move one variable to the
# front and keep everything else in the same order, you can
# do this: select(data_analysis, everything()) />
# Three ways to specify model
# Most concise
lm(df_reg)
##
## Call:
## lm(formula = df_reg)
##
## Coefficients:
##
         (Intercept)
                           extraversion
                                              agreeableness conscientiousness
              7.1013
##
                                 0.3570
                                                     0.1183
                                                                       -0.7037
##
         neuroticism
                               openness
##
             -0.1442
                                 0.8761
# Identify outcome, infer rest
lm(data_science ~ ., data = df_reg)
##
## Call:
## lm(formula = data_science ~ ., data = df_reg)
## Coefficients:
         (Intercept)
                           extraversion
                                              agreeableness conscientiousness
##
              7.1013
                                 0.3570
                                                     0.1183
                                                                       -0.7037
##
         neuroticism
                               openness
             -0.1442
                                 0.8761
##
# Identify entire model
lm(data_science ~ extraversion + agreeableness +
   conscientiousness + neuroticism + openness, data = df_reg)
##
## Call:
## lm(formula = data_science ~ extraversion + agreeableness + conscientiousness +
       neuroticism + openness, data = df_reg)
##
## Coefficients:
##
         (Intercept)
                           extraversion
                                             agreeableness conscientiousness
```

```
0.3570
##
             7.1013
                                                   0.1183
                                                                     -0.7037
##
        neuroticism
                              openness
##
            -0.1442
                                0.8761
# Save model
fit2 <- lm(df_reg)</pre>
# Show model
fit2
##
## Call:
## lm(formula = df_reg)
## Coefficients:
##
         (Intercept)
                          extraversion
                                            agreeableness conscientiousness
##
             7.1013
                                0.3570
                                                   0.1183
                                                                     -0.7037
##
        {\tt neuroticism}
                              openness
            -0.1442
                                0.8761
# Summarize regression model
summary(fit2)
##
## Call:
## lm(formula = df_reg)
## Residuals:
       Min
                 1Q Median
                                   3Q
                                           Max
## -24.1425 -5.8822 -0.8419 7.3259 25.8733
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
                     7.1013 27.7356 0.256 0.79917
## (Intercept)
## extraversion
                      0.3570
                                 0.1789
                                          1.996 0.05250 .
                                 0.2384
                                          0.496 0.62226
## agreeableness
                      0.1183
## conscientiousness -0.7037
                                 0.2161 -3.256 0.00224 **
## neuroticism
                     -0.1442
                                 0.2009 -0.718 0.47683
## openness
                      0.8761
                                 0.2033
                                          4.309 9.68e-05 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 10.67 on 42 degrees of freedom
## Multiple R-squared: 0.4612, Adjusted R-squared: 0.3971
## F-statistic: 7.19 on 5 and 42 DF, p-value: 6.125e-05
```

CONTINGENCY

LOAD DATA

```
# Also convert all variables to factors
df_cont <- read_csv("../data/state_trends.csv") |>
 select(region, psy_reg) |>
 mutate(across(everything(), as_factor)) |>
 print()
## Rows: 48 Columns: 34
## -- Column specification ---
## Delimiter: ","
## chr (11): state, state_code, region, psych_region, psy_reg, has_nba, has_nfl...
## dbl (23): population, sq_miles, pop_density, extraversion, agreeableness, co...
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
## # A tibble: 48 x 2
##
     region
             psy_reg
     <fct>
               <fct>
## 1 South
              Friendly
## 2 West
              Creative
## 3 South Friendly
## 4 West
              Creative
            Friendly
## 5 West
## 6 Northeast Uninhibited
## 7 South
              Uninhibited
## 8 South
               Friendly
## 9 South
               Friendly
## 10 West
               Creative
## # ... with 38 more rows
```

ANALYZE DATA

```
# Create contingency table
ct <- table(df_cont$region, df_cont$psy_reg)</pre>
##
##
               Friendly Creative Uninhibited
##
     South
                     10
                               2
##
     West
                      3
                                8
                                            0
    Northeast
##
                      0
                                0
                                            9
    Midwest
##
                     11
# Call also get cell, row, and column %
# With rounding to get just 2 decimal places
# Multiplied by 100 to make %
# Row percentages
ct |>
```

```
prop.table(1) |> # 1 is for row percentages
  round(2) * 100
##
##
               Friendly Creative Uninhibited
##
     South
                     62
                              12
                                          25
##
     West
                     27
                              73
                                          0
                                         100
##
     Northeast
                     0
                               0
##
    Midwest
                     92
                                           8
# Column percentages
ct |>
  prop.table(2) |> # 2 is for columns percentages
round(2) * 100
##
##
               Friendly Creative Uninhibited
##
                    42
                              20
                                          29
     South
##
     West
                     12
                              80
                                          0
                     0
                               0
##
     Northeast
                                          64
     Midwest
                     46
# Total percentages
ct |>
  prop.table() |> # No argument for total percentages
round(2) * 100
##
               Friendly Creative Uninhibited
##
##
     South
                     21
                               4
##
     West
                     6
                              17
                                           0
                      0
##
     Northeast
                               0
                                          19
##
     Midwest
                     23
                               0
                                           2
# Chi-squared test (but n is small)
tchi <- chisq.test(ct)</pre>
## Warning in chisq.test(ct): Chi-squared approximation may be incorrect
tchi
##
## Pearson's Chi-squared test
##
## data: ct
## X-squared = 50.002, df = 6, p-value = 4.697e-09
# Get p-value in one step
table(df_cont$region, df_cont$psy_reg) |> chisq.test()
```

```
## Warning in chisq.test(table(df_cont$region, df_cont$psy_reg)): Chi-squared
## approximation may be incorrect
##
##
  Pearson's Chi-squared test
## data: table(df_cont$region, df_cont$psy_reg)
## X-squared = 50.002, df = 6, p-value = 4.697e-09
# Additional tables
tchi$observed # Observed frequencies (same as ct)
##
##
               Friendly Creative Uninhibited
                     10
##
                               2
     South
                     3
                               8
                                           0
##
     West
                                           9
##
     Northeast
                     0
                               0
##
    Midwest
                     11
                               0
                                           1
tchi$expected
              # Expected frequencies
##
##
               Friendly Creative Uninhibited
##
                   8.0 3.333333
                                    4.666667
     South
##
     West
                    5.5 2.291667
                                    3.208333
                    4.5 1.875000
                                    2.625000
##
     Northeast
                    6.0 2.500000
                                    3.500000
##
     Midwest
tchi$residuals # Pearson's residual
##
##
                Friendly Creative Uninhibited
##
     South
                0.7071068 -0.7302967 -0.3086067
##
     West
               -1.0660036 3.7708009 -1.7911821
##
    Northeast -2.1213203 -1.3693064
                                       3.9347354
##
    Midwest
               2.0412415 -1.5811388 -1.3363062
tchi$stdres # Standardized residual
##
##
                Friendly Creative Uninhibited
     South
##
                1.2247449 -1.0052494 -0.4490887
##
     West
               -1.7170914 4.8270542 -2.4240449
##
     Northeast -3.3282012 -1.7073312 5.1866269
    Midwest
               3.333333 -2.0519567 -1.8333970
```