

# Histogram 수정을 사용한 영상 개선

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# 학습 내용

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- Histogram
- Histogram modifications

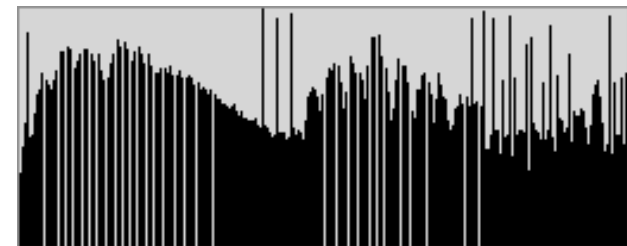
# Histogram

- A simple datum that gives **the number of pixels that a given value** in an image
- Ex) a 8bit gray-scale image

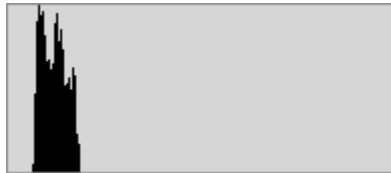
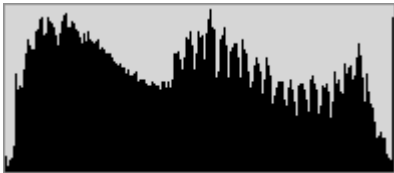


| Bin | Counts | Prob. |
|-----|--------|-------|
| 0   | 163    | 0.005 |
| 1   | 77     | 0.003 |
| ... |        |       |
| 255 | 1561   | 0.051 |

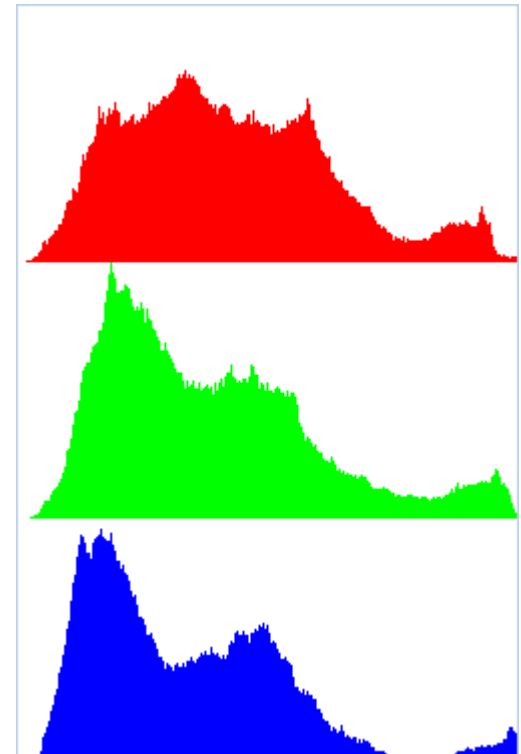
number  
of  
pixels



gray level

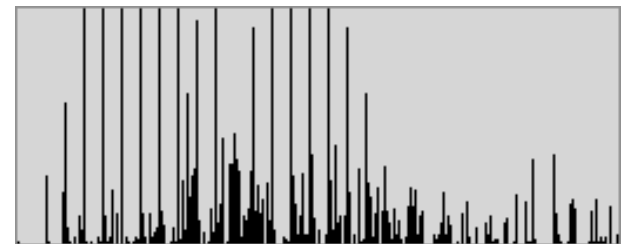


in color images





Color Quantization



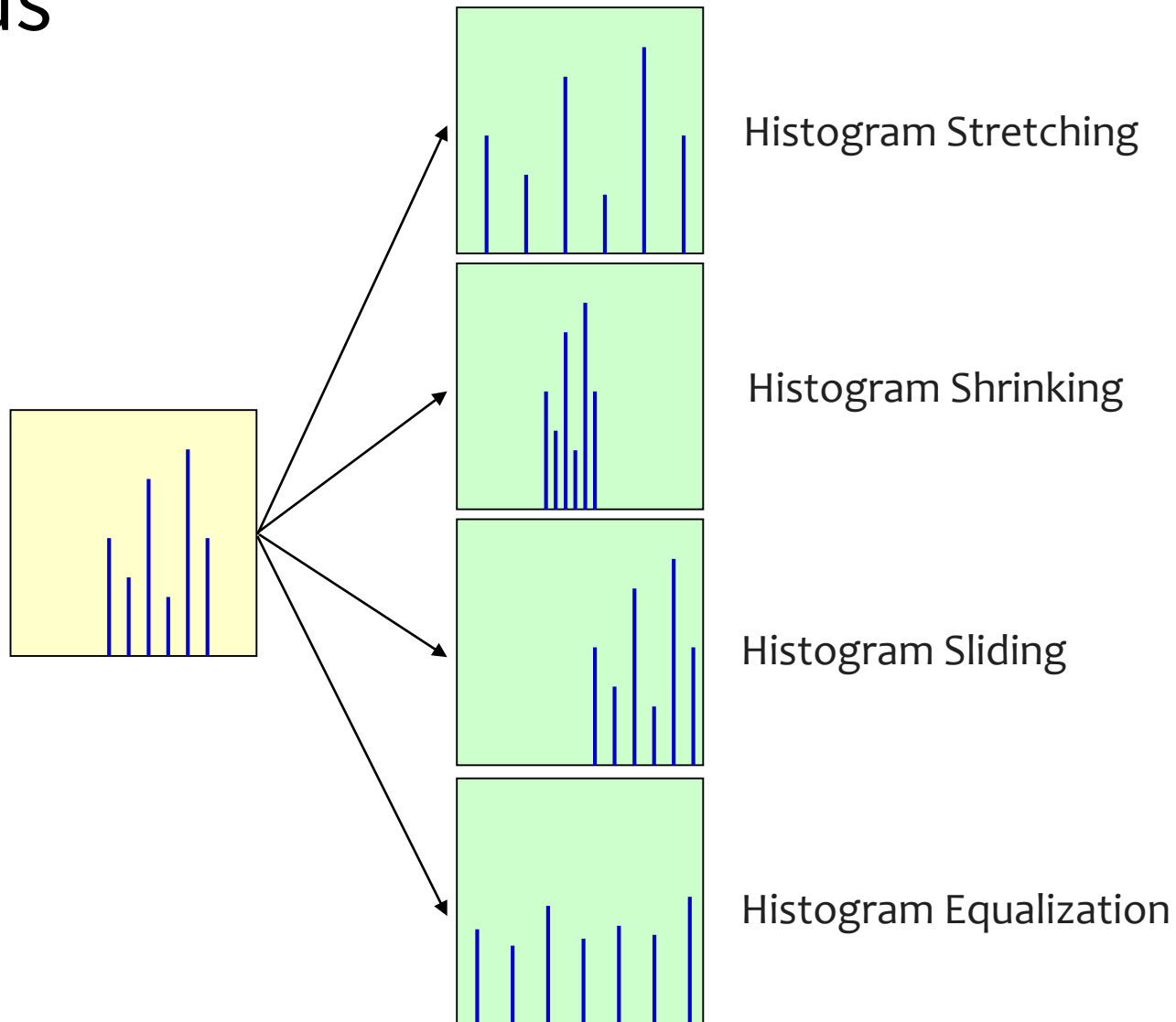
# Histogram modifications

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Improving image contrast and brightness based on **histogram**

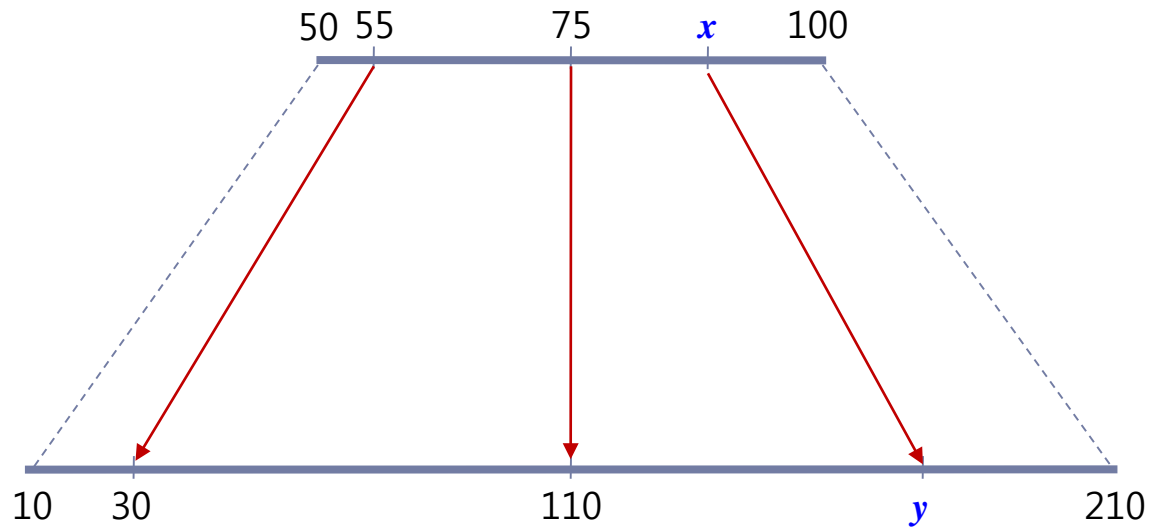
Focus on the histogram shape and range

# fields





# Stretching



$$(100 - 50) : (x - 50) = (210 - 10) : (y - 10)$$

$$(y - 10) * (100 - 50) = (x - 50) * (210 - 10)$$

$$y = \frac{(x - 50) * (210 - 10)}{(100 - 50)} + 10 = \frac{(210 - 10)}{(100 - 50)} (x - 50) + 10$$

$$I'(x, y) = \frac{(S_{\max} - S_{\min})}{(I_{\max} - I_{\min})} (I(x, y) - I_{\min}) + S_{\min}$$

$$I'(x, y) = \left[ \frac{S_{MAX} - S_{MIN}}{I_{MAX} - I_{MIN}} \right] [I(x, y) - I_{MIN}] + S_{MIN}$$

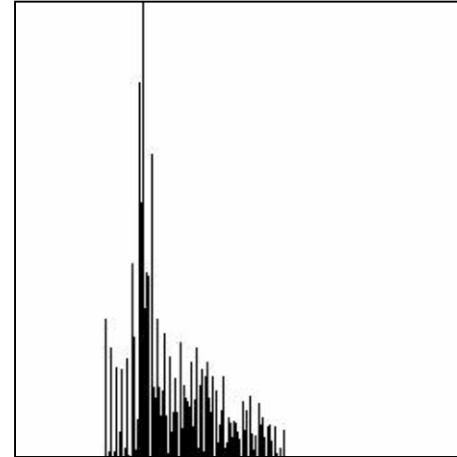
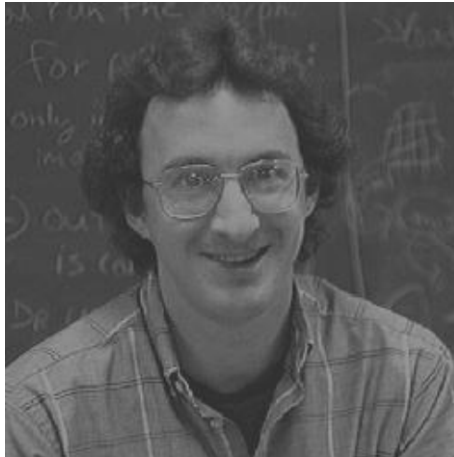
$I_{MAX}$  : largest gray-level value in the image  $I(x, y)$

$I_{MIN}$  : smallest gray-level value in  $I(x, y)$

$S_{MAX}$  : maximum gray-level values possible  
(for an 8-bit image this is 255)

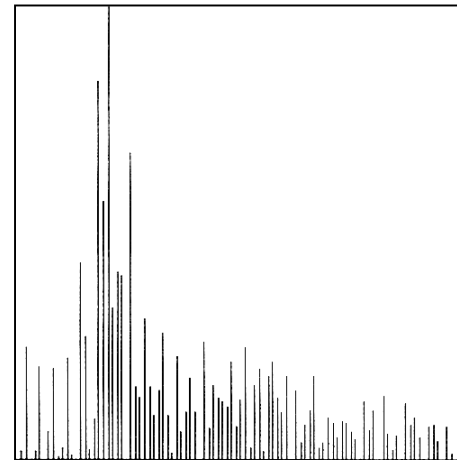
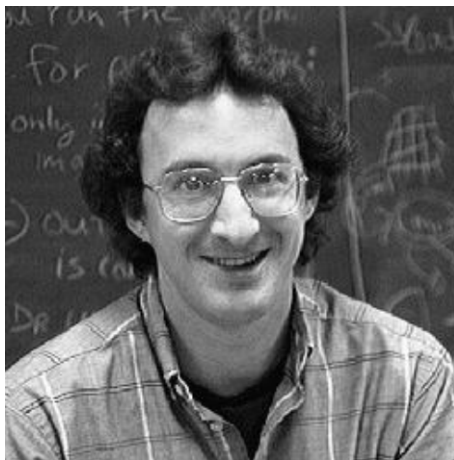
$S_{MIN}$  : minimum gray-level values possible  
(for an 8-bit image this is 0)

Low-contrast  
image



Histogram of  
low-contrast  
image

Image after  
histogram  
stretching



Histogram of  
image after  
stretching

# Shrinking

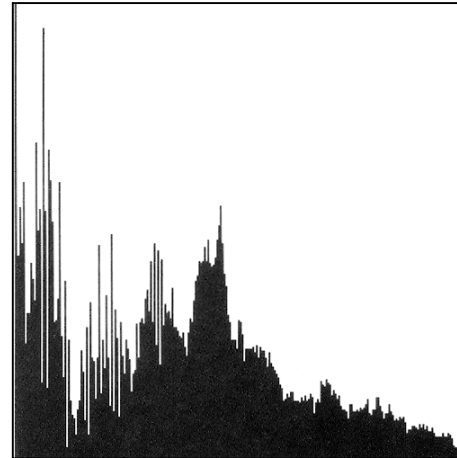
$$I'(x, y) = \left[ \frac{S_{MAX} - S_{MIN}}{I_{MAX} - I_{MIN}} \right] [I(x, y) - I_{MIN}] + S_{MIN}$$

$I_{MAX}$  : largest gray-level value in the image  $I(x, y)$

$I_{MIN}$  : smallest gray-level value in  $I(x, y)$

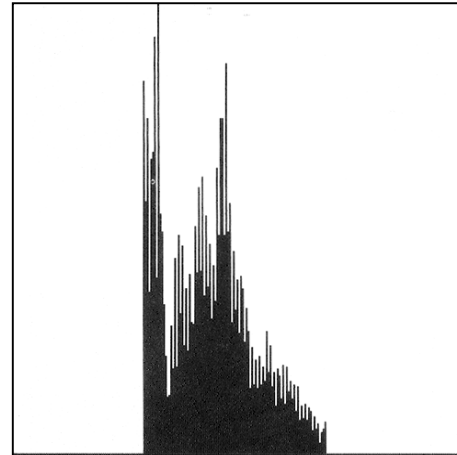
$S_{MAX}$  : maximum desired in the compressed histogram

$S_{MIN}$  : minimum desired in the compressed histogram



Histogram  
of original  
image

Image after  
shrinking  
to the range  
 $[75, 175]$



Histogram  
of shrunk  
image

# Sliding

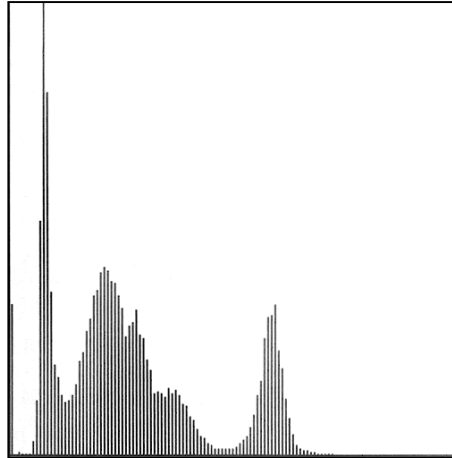
$$S(x, y) = I(x, y) + \textit{offset}$$

*offset* : amount to slide the histogram

Original  
image



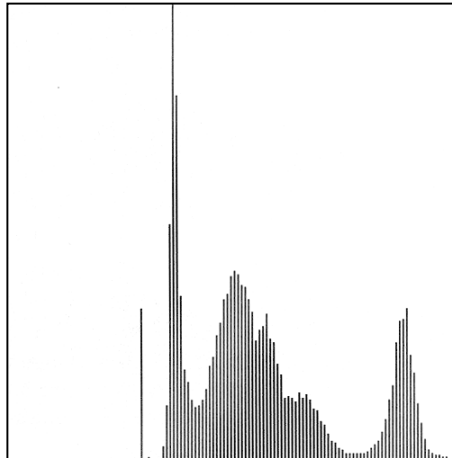
Histogram of  
original image



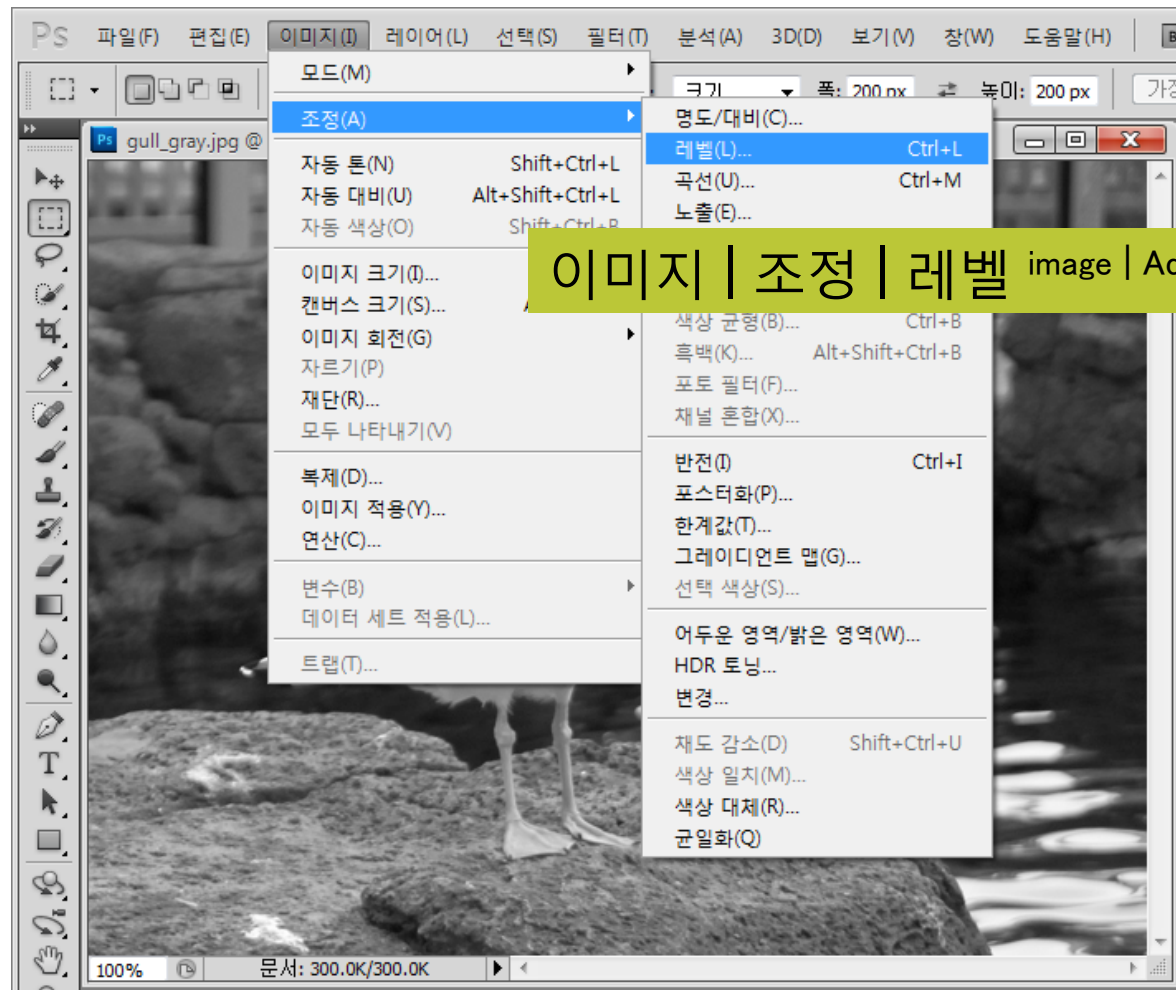
positive-  
value  
histogram  
sliding



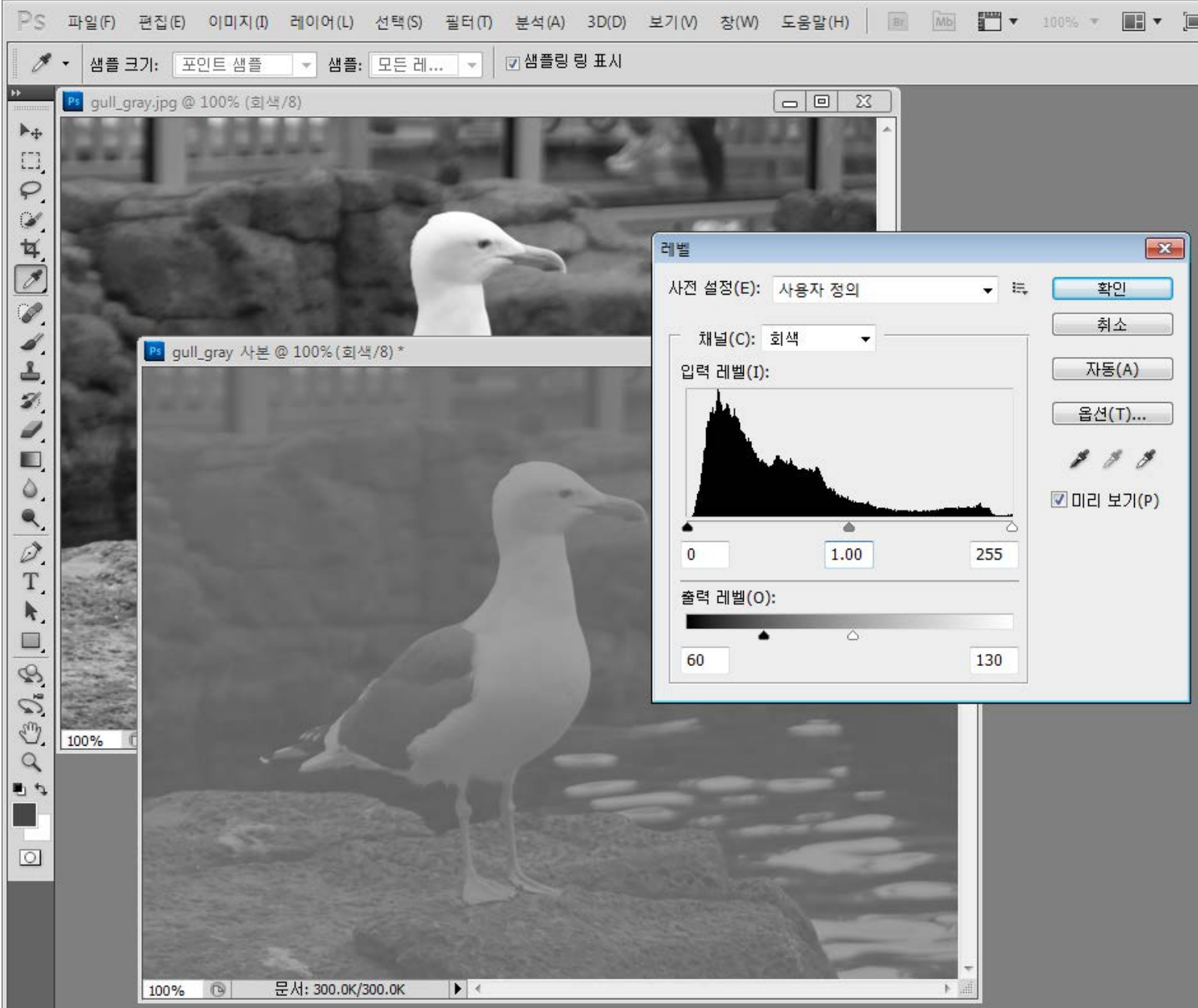
Histogram of  
image after  
sliding

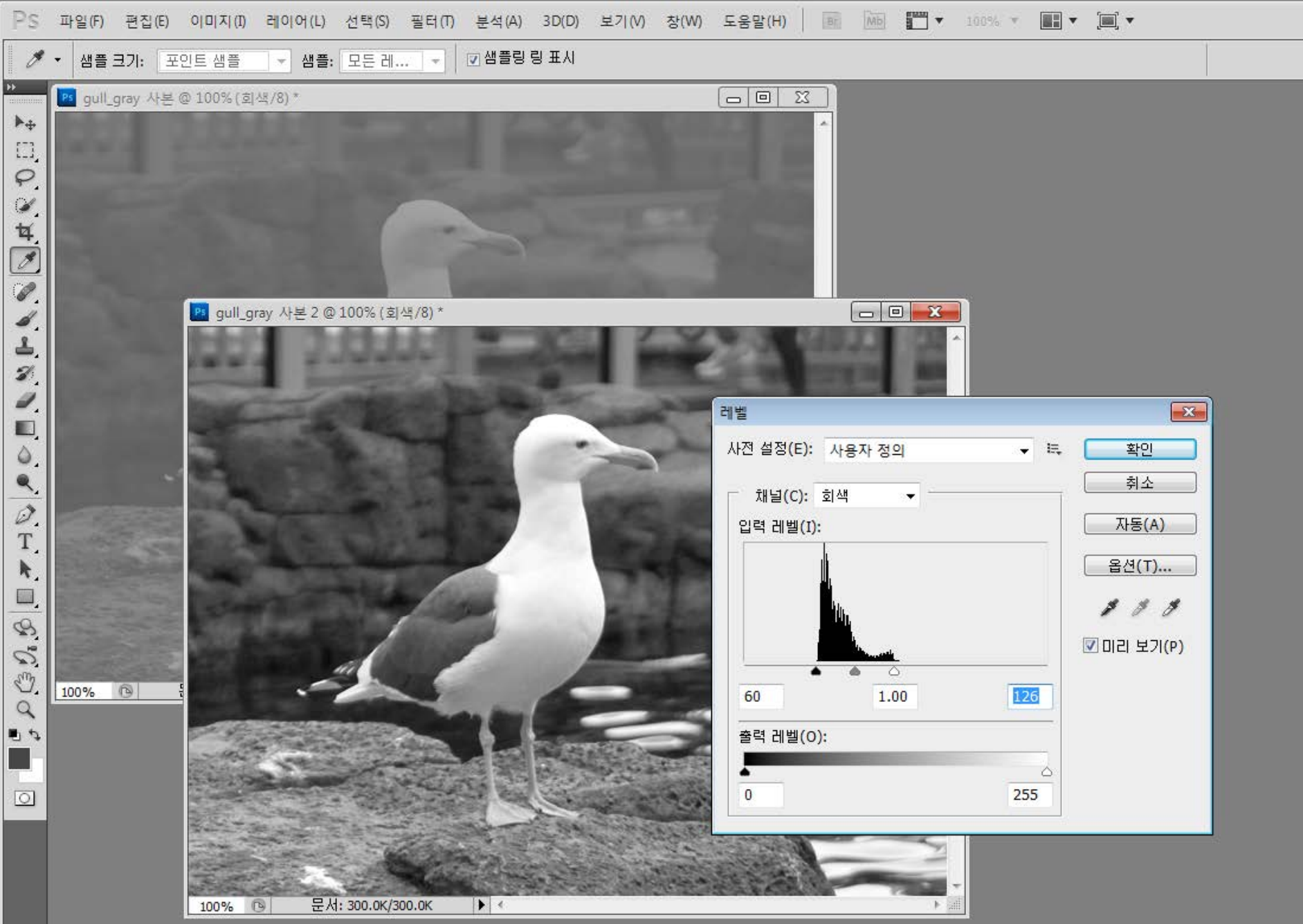


# Using Photoshop









샘플 크기: 포인트 샘플 샘플: 모든 레... ☒ 샘플링 링 표시

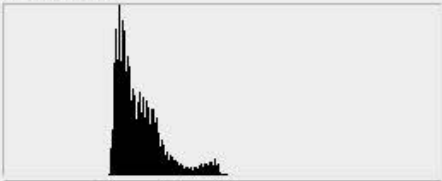
gull\_gray 사본 @ 100% (회색/8) \*


gull\_gray 사본 2 @ 100% (회색/8) \*

레벨

사전 설정(E): 사용자 정의

채널(C): 회색

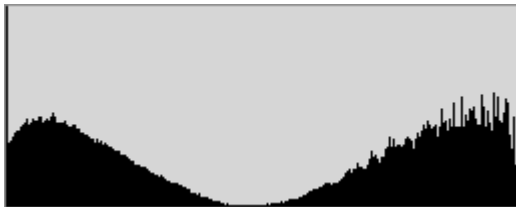
입력 레벨(I):  
  
60 1.00 130

출력 레벨(O):  
  
150 220

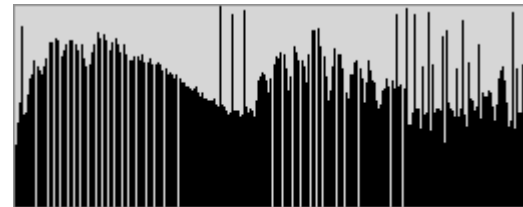
확인 취소 자동(A) 옵션(T)... 미리 보기(P)

100% 문서: 300.0K/300.0K

# Equalization

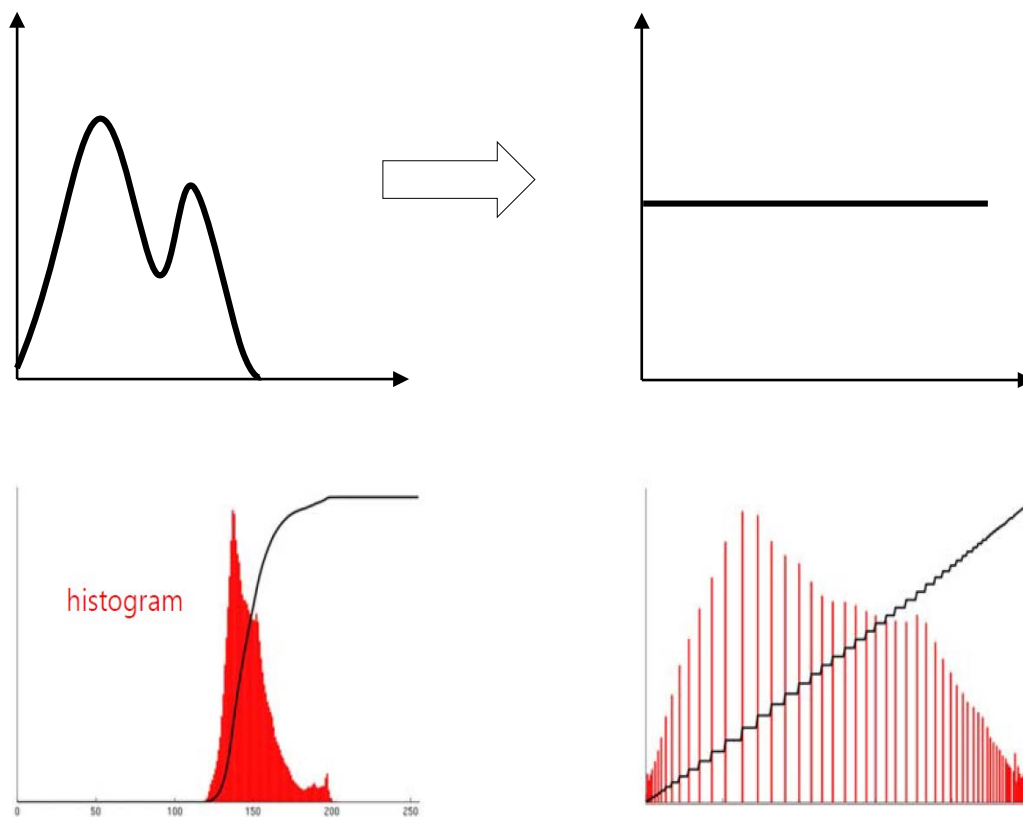


높은 contrast



좋은 contrast

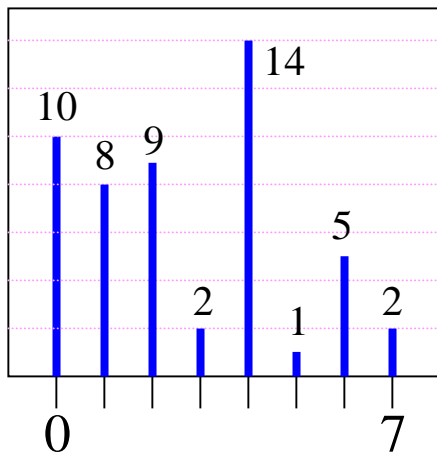
균일하지 않은 gray level의 분포를 재분배하여  
발생 빈도를 균등하게 분포하도록 만드는 과정



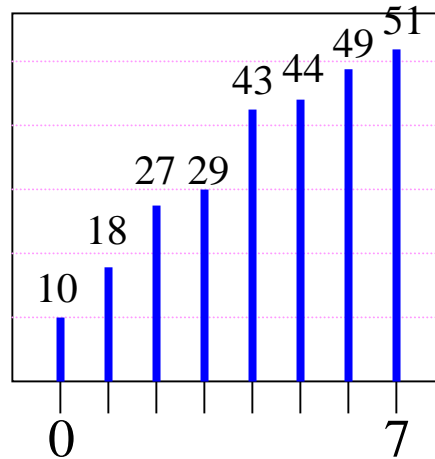


## algorithm

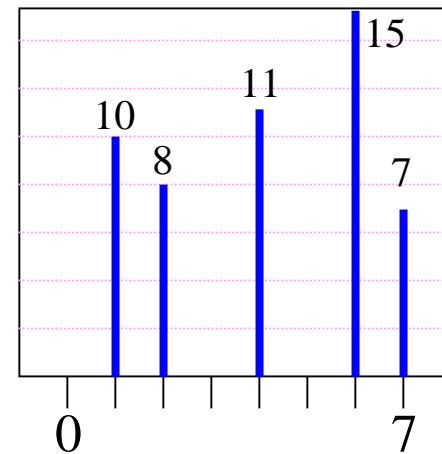
- ① 입력 영상의 히스토그램의 값을 누적시켜 히스토그램 누적 합 계산
- ② 히스토그램의 누적 합을 전체 픽셀의 개수로 나누어 값을 정규화함
- ③ 정규화된 값에 최대 gray level 값을 곱한 후 반올림을 수행
- ④ 입력 영상의 각 gray level에 대해 변환 값으로 대응시킴



히스토그램



누적값



균일화 결과

$$\frac{(10, 18, 27, 29, 43, 44, 49, 51)}{51} \times 7$$

$$\approx (1.37, 2.47, 3.71, 3.98, 5.90, 6.04, 6.73, 7.00)$$

$$\approx (1, 2, 4, 4, 6, 6, 7, 7)$$

|           | 픽셀값 | 개수 | 누적값 | 균일화  | 반올림 |
|-----------|-----|----|-----|------|-----|
| 4 5 3 6 7 | 0   | 10 | 10  | 1.37 | 1   |
| 4 2 2 4 6 | 1   | 8  | 18  | 2.47 | 2   |
| 0 2 2 5 7 | 2   | 9  | 27  | 3.71 | 4   |
| 0 0 2 3 5 | 3   | 2  | 29  | 3.98 | 4   |
| 0 1 2 4 4 | 4   | 14 | 43  | 5.90 | 6   |
|           | 5   | 1  | 44  | 6.04 | 6   |
|           | 6   | 5  | 49  | 6.73 | 7   |
|           | 7   | 2  | 51  | 7.00 | 7   |

$$\frac{10}{51} * 7 = 1.37$$

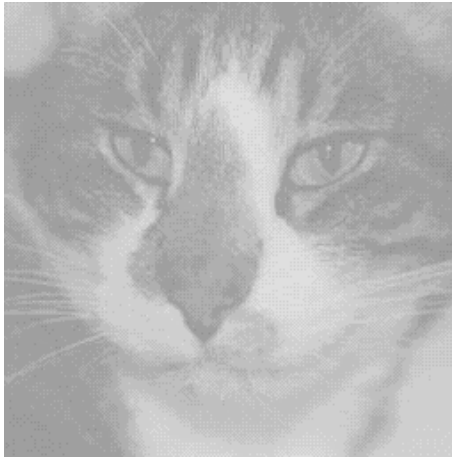
$$\frac{43}{51} * 7 = 5.90$$

## 균일화를 위한 공식

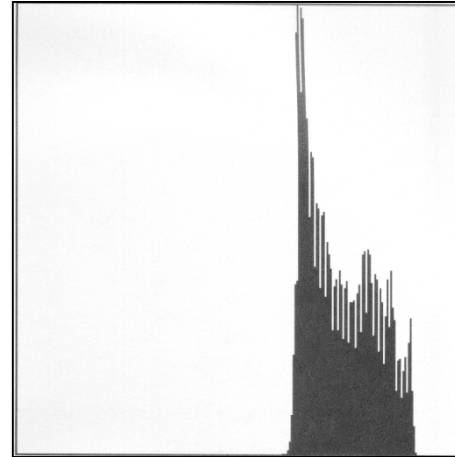
$$Normalization = \frac{\text{누적값}}{\text{전체 픽셀의 수}} \times \text{maximum\_gray\_level}$$



Original light  
image



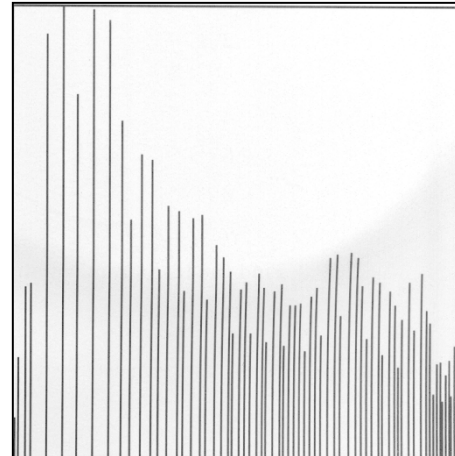
Histogram  
of original  
image



Light image  
after histogram  
equalization



Histogram  
of equalized  
image



- Histogram

- A simple datum that gives the number of pixels that a given value in an image

- Histogram modifications

- Improving image contrast and brightness by changing shape and range of histogram
- Histogram Stretching, Histogram Shrinking, Histogram Sliding, Histogram Equalization

# Reference

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- R. Gonzalez, R. Woods, **Digital Image Processing (2nd Edition)**, Prentice Hall, 2002
- Scott E Umbaugh, **Computer Imaging**, CRC Press, 2005