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1 Basic

1.1 Default Code

```
#pragma GCC optimize("03,unroll-loops")
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")
//#pragma GCC optimize("trapv")
#include <bits/stdc++.h>
using namespace std;

int main()
{
   ios_base::sync_with_stdio(0);
   cin.tie(0);
   return 0;
}
```

1.2 Functions

```
__builtin_popcount(n) // 表示將n表示成2進位有幾個 1
__builtin_popcountll(n) // 表示將n表示成2進位有幾 個1
__builtin_ctz(n) // 回傳n的二進位下最低為1後面有 幾個0
__builtin_ctzll(n) // 回傳n的二進位下最低為1後面 有幾個0
int __builtin_clz (unsigned int n) // 回傳n的二進 位下最高為1前面有幾個0 (n不可為0)
int __builtin_clzll (unsigned long long n)
cout << fixed << setprecision(2) << 12.375019483 << "\n"; // 12.38

1.3 Pragma
```

```
#pragma GCC optimize("03,unroll-loops")
#pragma GCC target("avx2,bmi,bmi2,lzcnt,popcnt")
#pragma GCC optimize("trapv") // make overflow RE
    , slow
```

1.4 Random Value Generator

```
mt19937 rng(chrono::steady_clock::now().
    time_since_epoch().count());
shuffle(a.begin(), a.end(), rng);
uniform_int_distribution<long long>(l, r)(rng);
    // [l, r]
```

1.5 set map pq

```
struct edge
{
    int a, b, w;
    friend istream& operator>>(istream &in, edge
        &x)
    {     in >> x.a >> x.b >> x.w; }
    friend ostream& operator<<(ostream &out,
        const edge &x)
    {       out << "(" << x.a << "," << x.b << ","
        << x.w << ")"; return out; }
};</pre>
```

```
struct cmp
{ bool operator()(const edge &x, const edge &y) const { return x.w < y.w; } };

set <edge, cmp > st; //遞增
map <edge, long long, cmp > mp; //遞增
priority_queue <edge, vector <edge >, cmp > pq; //遞
減
```

2 Python

2.1 int(str)

```
import sys
sys.set_int_max_str_digits(1000000)
int('1'*999999) # ok
int('1'*1000000) # error
# int(str) time complexity = O(n^2 / 64)
```

2.2 有理數 (可以直接做四則運算)

```
from fractions import Fraction
Fraction(16, -10) # Fraction(-8, 5)
Fraction(123) # Fraction(123, 1)
Fraction() # Fraction(0, 1)
Fraction('3/7') # Fraction(3, 7)
Fraction(' -3/7 ') # Fraction(-3, 7)
Fraction('1.414213 \t\n') # Fraction(1414213,
   1000000)
Fraction('-.125') # Fraction(-1, 8)
Fraction('7e-6') # Fraction(7, 1000000)
Fraction(2.25) # Fraction(9, 4)
Fraction(1.1) # Fraction(2476979795053773,
   2251799813685248) (直接傳小數會失真,應改成傳
   字串)
# method
Fraction(1,2).numerator # 1 (分子)
Fraction(1,2).denominator # 2 (分母)
Fraction(__import__(math).pi).limit_denominator
   (1000) # Fraction(355, 113) (113 < 1000)
Fraction( import (math).pi).limit denominator
   (1000000) # Fraction(3126535, 995207) (995207
    < 1000000)
```

3 Data Structure

3.1 BIT

3.2 Distinct Value with BIT

```
#include <bits/stdc++.h>
using namespace std;
using pii = pair<int, int>;
using pti = pair<int, pii>;
int n, q, val[200005];
pti ques[200005];
pii ans[200005];
struct BIT
  int bit[200005];
  map<int, int> mp;
  //color, index
  void add(int idx, int dif)
    while(idx <= n)</pre>
      bit[idx] += dif, idx += idx&-idx;
  void update(int idx, int color)
    if(mp.find(color) == mp.end())
    {
      add(idx, 1);
      mp.insert({color, idx});
    }
    else
      add(mp[color], -1);
      add(idx, 1);
      mp[color] = idx;
  }
  int query(int 1, int r)
    if(1 != 1)
      return query(1, r) - query(1, 1-1);
    int ret = 0;
    while(1 <= r)</pre>
      ret += bit[r], r -= r&-r;
    return ret;
}a;
bool cmp(const pti &x, const pti &y)
  if(x.second.second != y.second.second)
    return x.second.second < y.second.second;</pre>
  return x.second.first < y.second.first;</pre>
```

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long long s = query(y);

```
int main()
                                                                if(x) {
                                                                    s -= query(x - 1);
  ios_base::sync_with_stdio(0);
                                                                return s;
  cin.tie(0);
  cin >> n >> q;
                                                           long long k_th(int k) {
  for(int i=1; i<=n; i++)</pre>
                                                                int now = 0;
    cin >> val[i];
                                                                for(int i = bit_num - 1; i >= 0; i--) {
                                                                    if(d[now + (1 << i)] < k) {</pre>
  for(int i=0; i<q; i++)</pre>
                                                                        k -= d[now + (1 << i)];
    cin >> ques[i].second.first >> ques[i].second
                                                                        now += 1 << i;
        .second;
                                                                    }
    ques[i].first = i;
 }
                                                                return now + 1;
                                                           }
 sort(ques, ques+q, cmp);
                                                       };
                                                       // 二維
 int far = 0;
 for(int i=0; i<q; i++)</pre>
                                                       struct BIT
                                                       {
    while(far < ques[i].second.second)</pre>
                                                           int n;
      a.update(far+1, val[far+1]), far++;
                                                           int bit_num;
    ans[i] = {ques[i].first, a.query(ques[i].
                                                           vector<vector<int>> d;
        second.first, ques[i].second.second)};
                                                           void init(int size) {
                                                                n = size;
 }
                                                                bit_num = __lg(size) + 1;
 sort(ans, ans+q);
                                                                d.resize(1 << bit_num);</pre>
                                                                int ln = d.size();
 for(int i=0; i<q; i++)</pre>
    cout << ans[i].second << "\n";</pre>
                                                                for(int i = 0; i < ln; i++) {</pre>
                                                                    for(int j = 0; j < ln; j++) {</pre>
                                                                         d[i].push_back(0);
                                                                }
3.3 BIT (Howard)
                                                                // memset(d.data() + 1, 0, sizeof(long
                                                                    long) * (1 << bit_num));</pre>
// 一維
struct BIT
                                                           BIT(int size) {
                                                                init(size);
    // 1~n
    int n;
                                                           void ins(int x, int y, long long v) {
    int bit_num;
                                                                for(; x <= n; x += x \& -x) {
    vector<long long> d;
                                                                    for(int j = y; j <= n; j += j & -j) {</pre>
    void init(int size) {
                                                                        d[x][j] += v;
        n = size;
        bit_num = __lg(size) + 1;
                                                                }
        d.resize(1 << bit_num);</pre>
        memset(d.data() + 1, 0, sizeof(long long)
                                                           long long query(int x, int y) {
             * (1 << bit_num));
                                                                long long s = 0;
                                                                for(; x > 0; x -= x & -x) {
                                                                    for(int j = y; j > 0; j -= j & -j){
    BIT(int size) {
        init(size);
                                                                        s += d[x][j];
                                                                    }
    void ins(int x, long long v) {
                                                                }
        for(; x \le n; x += x \& -x) {
                                                                return s;
            d[x] += v;
                                                           long long query_range(int x1, int y1, int x2,
                                                                int y2) {
    long long query(int x) {
                                                                return query(x2, y2) - query(x2, y1 - 1)
        if(x \leftarrow 0) {
                                                                    - query(x1 - 1, y2) + query(x1 - 1,
            return 0;
                                                                    y1 - 1);
                                                           }
        long long s = 0;
                                                       };
        for(; x > 0; x -= x \& -x) {
            s += d[x];
        }
                                                       3.4 Segment Tree
        return s;
    long long query_range(int x, int y) {
                                                       struct segtree
        if(x > y) {
            return 0;
                                                           int n, seg[1<<19];</pre>
```

void init(int x)

```
n = 1 << (__lg(x) + 1);
        for(int i=1; i<2*n; i++)</pre>
            seg[i] = inf;
    }
    void update(int x, int val)
        x += n;
        seg[x] = val, x /= 2;
        while(x)
             seg[x] = min(seg[2*x], seg[2*x+1]), x
                  /= 2;
    }
    int query(int 1, int r)
    {
        1 += n, r += n;
        int ret = inf;
        while(l < r)
             if(1 & 1)
                 ret = min(ret, seg[l++]);
             if(r & 1)
                 ret = min(ret, seg[--r]);
             1 /= 2, r /= 2;
        return ret;
}bm;
```

3.5 Segment Tree(Howard)

```
using TYPE = int;
const int SIZE = 1 << 19;</pre>
// 15:32678 16:65536 17:131072 18:2624144
   19:524288 20:1048576
struct segment_tree
{
    // start from 1
    TYPE node[SIZE];
    TYPE merge(TYPE a, TYPE b) {
        return min(a, b);
    void pull(int idx) {
        node[idx] = merge(node[idx * 2], node[idx
             * 2 + 1]);
    void init(int L, int R, int idx, vector<TYPE>
        &input) {
        if(L == R) {
            node[idx] = input[L];
            return;
        int now = (L + R) / 2;
        init(L, now, idx * 2, input);
        init(now + 1, R, idx * 2 + 1, input);
        pull(idx);
    TYPE query(int L, int R, int idx, int l, int
       r) {
        if(L >= 1 && R <= r) return node[idx];</pre>
        int now = (L + R) / 2;
        if(r <= now) return query(L, now, idx *</pre>
            2, 1, r);
        if(1 > now) return query(now + 1, R, idx
            * 2 + 1, 1, r);
        return merge(query(L, now, idx * 2, 1, r)
            , query(now + 1, R, idx * 2 + 1, l, r
            ));
```

3.6 Lazy Propagation Segment Tree

```
struct segtree
{
    int n;
    long long tg[2][1<<19], seg[1<<19];</pre>
    //0: add, 1: set;
    void init(int x)
    {
        n = 1 << (__lg(x) + 1);
    void set(bool tp, int idx, long long val)
        if(tp == 0)
        {
            (tg[1][idx])? (tg[1][idx] += val): (
                tg[0][idx] += val);
            seg[idx] += val;
        }
        else
        {
            tg[0][idx] = 0, tg[1][idx] = val, seg
                [idx] = val;
        }
    }
    void push(int idx)
        for(int i=__lg(idx); i>0; i--)
            int now = idx>>i;
            if(tg[0][now])
              set(0, 2*now, tg[0][now]/2);
              set(0, 2*now+1, tg[0][now]/2);
              tg[0][now] = 0;
            if(tg[1][now])
              set(1, 2*now, tg[1][now]/2);
              set(1, 2*now+1, tg[1][now]/2);
              tg[1][now] = 0;
        }
    }
    void pull(int idx)
    {
        idx >>= 1;
        while(idx)
```

```
if(tg[1][idx])
            seg[idx] = tg[1][idx];
          else
            seg[idx] = tg[0][idx] + seg[2*idx] +
                seg[2*idx+1];
          idx /= 2;
    }
    void update(bool tp, int 1, int r, long long
        val)
    {
        1 += n, r += n;
        int tl = 1, tr = r-1, len = 1;
        push(1), push(r-1);
        while(1 < r)
        {
            if(1 & 1)
                set(tp, l++, val*len);
            if(r & 1)
                set(tp, --r, val*len);
            1 /= 2, r /= 2, len *= 2;
        pull(t1), pull(tr);
    }
    long long query(int 1, int r)
        1 += n, r += n;
        push(1), push(r-1);
        long long ret = 0;
        while(1 < r)
            if(1 & 1)
                ret += seg[1++];
            if(r & 1)
                ret += seg[--r];
            1 /= 2, r /= 2;
        return ret;
    }
};
```

3.7 Binary Search on Segment Tree

```
struct SEG
{
    int n;
    int seg[1<<19];</pre>
    void init(int x)
        n = 1 << (__lg(x) + 1);
    }
    void update(int x, int dif)
        x += n;
        seg[x] += dif, x /= 2;
             seg[x] = max(seg[2*x], seg[2*x+1]), x
                  /= 2;
    }
    int query(int g)
    {
        if(seg[1] < g)
             return -1;
        int id = 1;
```

```
while(id < n)
{
    if(seg[2*id] >= g)
        id = 2*id;
    else
        id = 2*id+1;
}

return id - n;
}
}bm;
```

3.8 Merging on Segment Tree

```
struct segtree
{
    struct node
        long long sum, pre;
        node()
        {
             sum = pre = 0;
        }
    };
    node mer(node x, node y)
    {
        node ret;
        ret.sum = x.sum + y.sum;
        ret.pre = max(x.pre, x.sum + y.pre);
        return ret;
    }
    int n;
    node seg[1<<19];
    void init(int x)
    {
        n = 1 << (__lg(x) + 1);
    }
    void print()
    {
        for(int i=1, j=1; i<=__lg(n)+1; i++)</pre>
             for(; j<(1<<i); j++)</pre>
                 cout << seg[j].sum << " ";</pre>
             cout << "\n";
        cout << "\n";
    }
    void update(int x, long long val)
        x += n;
        seg[x].sum = val, seg[x].pre = max(0LL,
            val);
        x /= 2;
        while(x)
             seg[x] = mer(seg[2*x], seg[2*x+1]), x
                  /= 2;
    }
    long long query(int 1, int r)
        1 += n, r += n;
        node retl, retr;
        while(1 < r)
```

{

```
if(1 & 1)
                retl = mer(retl, seg[1++]);
            if(r & 1)
                retr = mer(seg[--r], retr);
            1 /= 2, r /= 2;
        return mer(retl, retr).pre;
    }
}bm;
```

Segment Tree(Chung)

```
struct seg{
    int L,R;
    int data;
    int lson, rson;
    int chg;
    int real(){
        return data + chg;
};
template<typename T>
struct segtree{
    //declare
    const int maxn;
    int stptr = 1;
    vector<seg> ST;
    // constructor
    segtree(const int &sz): maxn(sz) { ST.resize
        (2*sz);  }
    //operation
    void merge(seg &par, seg &lson, seg &rson){
    }
    seg merge(seg a, seg b){
        seg ret;
        return ret;
    void push(int idx, int lson, int rson){
        ST[idx].data = ST[idx].real();
        ST[lson].chg += ST[idx].chg;
        ST[rson].chg += ST[idx].chg;
        ST[idx].chg = 0;
    }
    // functions
    void build(int L,int R,int idx,vector<T>& v){ |}
        ST[idx].L = L, ST[idx].R = R;
        if(L + 1 == R){
            ST[idx].data = v[L];
            return;
        }
        int mid = (L+R) / 2;
        int lson = ST[idx].lson = stptr++;
        int rson = ST[idx].rson = stptr++;
        build(L,mid,lson,v);
        build(mid,R,rson,v);
        merge(ST[idx], ST[lson], ST[rson]);
    void single_modify(int pos,int x,int idx){
        if(ST[idx].L + 1 == ST[idx].R){
            ST[idx].data = x;
            return;
        int mid = (ST[idx].L+ST[idx].R) / 2;
        int lson = ST[idx].lson, rson = ST[idx].
            rson;
```

```
if(pos < mid) single_modify(pos,x,lson);</pre>
        else single_modify(pos,x,rson);
        merge(ST[idx], ST[lson], ST[rson]);
    void range_modify(int L,int R,int x,int idx){
        if(ST[idx].L == L && ST[idx].R == R){
            ST[idx].chg += x;
            return;
        int mid = (ST[idx].L + ST[idx].R) / 2;
        int lson = ST[idx].lson, rson = ST[idx].
            rson;
        push(idx, lson, rson);
        if(R <= mid) range_modify(L,R,x,lson);</pre>
        else if(L >= mid) range_modify(L,R,x,rson
            );
        else range_modify(L,mid,x,lson),
            range_modify(mid,R,x,rson);
        merge(ST[idx], ST[lson], ST[rson]);
    }
    seg range_query(int L,int R,int idx){
        if(ST[idx].L == L && ST[idx].R == R){
            return ST[idx];
        }
        int mid = (ST[idx].L+ST[idx].R) / 2;
        int lson = ST[idx].lson, rson = ST[idx].
            rson;
        push(idx, lson, rson);
        if(R <= mid) return range_query(L,R,lson)</pre>
        if(L >= mid) return range_query(L,R,rson)
        return merge(range_query(L,mid,lson),
            range_query(mid,R,rson));
    }
};
int main(){
    const int maxn = 2e5+5;
    int n; cin>>n;
    vector<int> v(n);
    segtree<int> ST(maxn);
    ST.build(0,n,0,v); // [0, n)
    ST.single_modify(3,10,0); // 在 3 的位置 +10
        (0-based)
    ST.range_modify(4,8,5,0); // 在 [4, 8) 的位置
         +10 (0-based)
    cout<<ST.range_query(0,n,0).real()<<"\n"; //</pre>
        查詢 [0, n)
    return 0;
```

3.10 PBDS

```
#include <bits/extc++.h>
using namespace __gnu_pbds;
gp_hash_table<int, int> mp; // map
cc_hash_bable<int, int> mp2;
tree<int, null_type, less<int>, rb_tree_tag,
   tree_order_statistics_node_update> s; // set
int main(){
    // Insert some entries into s.
    s.insert(12); s.insert(505);
    // The order of the keys should be: 12, 505.
    assert(*s.find_by_order(0) == 12);
    assert(*s.find_by_order(3) == 505);
```

```
// The order of the keys should be: 12, 505.
    assert(s.order_of_key(12) == 0);
    assert(s.order_of_key(505) == 1);
    // Erase an entry.
    s.erase(12);
    // The order of the keys should be: 505.
    assert(*s.find_by_order(0) == 505);
    // The order of the keys should be: 505.
    assert(s.order_of_key(505) == 0);
    cout << s.size() << endl;</pre>
// 一種變形寫法
tree<pair<int, int>,null_type,less<pair<int, int</pre>
    >>,rb_tree_tag,
    tree_order_statistics_node_update> s;
void solve()
{
    s.insert({x, i});
    s.erase(s.lower_bound({x, 0}));
    cout << s.order_of_key({x, 0}) + 1 << '\n';
    cout << s.find_by_order(x - 1) -> first << '\ | }</pre>
        n';
    cout << prev(s.lower_bound(\{x, 0\})) -> first
        << '\n';
    cout \langle\langle s.lower_bound(\{x + 1, 0\}) -> first \langle\langle
          '\n';
}
```

3.11 Sweep Line

```
const int MAXN = 1e6 + 10;
int X[MAXN << 1];</pre>
struct scanline {
    int x, down, up, mark;
    bool operator<(const scanline& other) const {</pre>
        return x < other.x;</pre>
    }
};
vector<scanline> v;
int node[MAXN << 2], lazy[MAXN << 2]; // for</pre>
   segtree
void Push(int idx, int 1, int r) {
    if(lazy[idx]) node[idx] = r - l + 1;
    else if(r != 1) node[idx] = node[idx * 2] +
        node[idx * 2 + 1];
    else node[idx] = 0;
}
void Update(int idx, long long L, long long R,
   int ul, int ur, int d) { // d -> mark
    if(ul <= L && R <= ur) {
        lazy[idx] += d;
        Push(idx, L, R);
        return;
    int mid = (L + R) / 2;
    if(ul <= mid) Update(idx * 2, L, mid, ul, ur,</pre>
    if(mid < ur) Update(idx * 2 + 1, mid + 1, R,
        ul, ur, d);
    Push(idx, L, R);
// 給定很多個四邊形,要你求總面積
void solve()
{
    int n;
```

```
cin >> n;
for(int i = 0; i < n; i++) {</pre>
    int 1, r, d, u;
    cin >> 1 >> r >> d >> u;
    v.push_back({1, d + 1, u, 1});
    v.push_back({r, d + 1, u, -1});
}
sort(v.begin(), v.end());
long long ans = 0;
int last = 0;
for(int i = 0; i < 2 * n; i++) {</pre>
    if(v[i].x != last) {
        ans += (long long)1 * (v[i].x - last)
             * node[1];
        last = v[i].x;
    Update(1, 1, 1000000, v[i].down, v[i].up,
         v[i].mark);
cout << ans << ' \setminus n';
return;
```

3.12 LinkedList

```
struct Node{
    Node *next = nullptr, *prev = nullptr;
    int data;
    Node(int x=0): data(x) {}
};
struct LinkedList{
    Node *head, *tail;
    int n = 0;
    LinkedList(){
        // 初始化頭尾偽指標
        head = new Node;
        tail = new Node;
        head -> prev = tail -> next = nullptr;
        head -> next = tail;
        tail -> prev = head;
    Node *insert(Node *node, int data){
        // insert data after node a <-> c ==> a
             <-> b <-> c
        Node *a = node;
        Node *b = new Node(data);
        Node *c = node -> next;
        a -> next = c -> prev = b;
        b \rightarrow prev = a;
        b \rightarrow next = c;
        n++;
        return b;
    Node* del(Node *node){
        // 刪除 node 並且回傳前一個指標 a <-> b
            <-> c ==> a <-> c
        Node *a = node -> prev;
        Node *b = node;
        Node *c = node -> next;
        a \rightarrow next = c;
        c \rightarrow prev = a;
        n - - ;
        return a;
    Node *front(){
        return head -> next;
```

```
}
Node *back(){
    return tail -> prev;
}
unsigned size(){
    return n;
}
}lst;
```

3.13 Sparse Table

```
int n, q, a[200005], lg_table[200005],
    sparse_table[19][200005];
void init_lg()
{
    for(int i=0, lg=0; i<=n; i++)</pre>
    {
         if(i>=(2<<lg))
             lg++;
         lg_table[i] = lg;
    }
}
void init_sparse()
{
    for(int i=0; i<n; i++)</pre>
         sparse_table[0][i] = a[i];
    for(int k=1; k<=lg_table[n]; k++)</pre>
         for(int i=0; i+(1<<k)<=n; i++)</pre>
             sparse_table[k][i] = min(sparse_table
                 [k-1][i], sparse_table[k-1][i
                 +(1<<(k-1))]);
}
int query_sparse(int 1, int r)
{
    int k = lg table[r-1];
    return min(sparse_table[k][1], sparse_table[k
        ][r-(1<<k)]);
}
int main()
    cin >> n >> q;
    for(int i=0; i<n; i++)</pre>
         cin >> a[i];
    init_lg(), init_sparse();
    while(q--)
         int x, y;
         cin >> x >> y;
        x--, y--;
         cout << query_sparse(x, y+1) << "\n";</pre>
}
```

3.14 Treap

```
// string reverse
/*
input
7 2
AYBABTU
3 4
4 7
output
```

```
AYAUTBB
*/
mt19937 gen(chrono::steady_clock::now().
    time_since_epoch().count()); // C++
    randomizer
struct Treap
{
     char key;
     int pri, sz, tag;
     Treap *1, *r;
    Treap(char _key) {
   key = _key;
          pri = gen();
          sz = 1;
         tag = 0;
          1 = nullptr;
          r = nullptr;
     }
};
Treap *root = nullptr;
string s;
int Size(Treap *x)
     return x ? x -> sz : 0;
}
void push(Treap *x)
     if(x \rightarrow tag) {
          swap(x \rightarrow 1, x \rightarrow r);
          if(x \rightarrow 1) x \rightarrow 1 \rightarrow tag ^= 1;
          if(x -> r) x -> r -> tag ^= 1;
          x \rightarrow tag = 0;
     }
}
void pull(Treap *x)
     x \rightarrow sz = Size(x \rightarrow 1) + Size(x \rightarrow r) + 1;
Treap *merge(Treap *a, Treap *b)
     if(!a || !b) return a ? a : b;
     if(a -> pri > b -> pri) {
         push(a);
          a \rightarrow r = merge(a \rightarrow r, b);
          pull(a);
          return a;
     }
     else {
          push(b);
          b \rightarrow 1 = merge(a, b \rightarrow 1);
          pull(b);
          return b;
     }
}
void build(int n) // string size
{
     for(int i = 0; i < n; i++) {</pre>
          root = merge(root, new Treap(s[i]));
     }
void splitbykth(Treap *x, int k, Treap *&a, Treap
```

if(!x) {

```
s[x] += s[y], s[y] = 0;
         a = b = nullptr;
         return;
                                                                   h[y] = x;
                                                                   return 1;
    push(x);
                                                              }
                                                          }bm;
    if(Size(x \rightarrow 1) + 1 \leftarrow k) {
         a = x;
         splitbykth(a \rightarrow r, k - Size(x \rightarrow l) - 1,
                                                          4.2 LCA
             a \rightarrow r, b);
         pull(a);
    }
                                                          vector<int> a[N];
    else {
                                                          int dep[N], lif[N][20];
         splitbykth(b \rightarrow 1, k, a, b \rightarrow 1);
                                                          void dfs(int x, int p)
         pull(b);
    }
                                                              dep[x] = dep[p] + 1;
}
                                                              for(int i: a[x])
                                                                   if(i != p)
void reverse_update(int a, int b)
                                                                       dfs(i, x);
                                                          }
    Treap *1, *m, *r;
    splitbykth(root, b, l, r);
                                                          void init(int n)
    splitbykth(l, a - 1, l, m);
    m \rightarrow tag = 1;
                                                              dfs(1, 0);
    root = merge(merge(1, m), r);
                                                              for(int i=1; (1<<i)<n; i++)</pre>
}
                                                                   for(int j=1; j<=n; j++)</pre>
                                                                        lif[j][i] = lif[lif[j][i-1]][i-1];
void output(Treap *x)
                                                          }
{
    if(!x) return;
                                                          int up(int x, int k)
    push(x);
                                                          {
    output(x -> 1);
                                                              int j = 0;
    cout \langle\langle x \rangle key;
                                                              while(k)
    output(x -> r);
}
                                                                   if(k & 1)
                                                                       x = lif[x][j];
void solve()
                                                                   k /= 2, j++;
{
                                                              }
    int n, m;
                                                              return x;
    cin >> n >> m;
                                                          }
    cin >> s;
    build(n);
                                                          int lca(int x, int y, int n)
    for(int i = 0; i < m; i++) {</pre>
         int 1, r;
                                                              if(dep[x] > dep[y])
         cin >> 1 >> r;
                                                                   swap(x, y);
         reverse_update(1, r);
                                                              y = up(y, dep[y] - dep[x]);
                                                              if(x == y)
    output(root);
                                                                   return x;
    cout << '\n';
                                                              for(int i=__lg(n); i>=0; i--)
    return;
}
                                                                   if(lif[x][i] != lif[y][i])
                                                                       x = lif[x][i], y = lif[y][i];
    Graph
                                                              return lif(x)[0];
4.1 DSU
                                                          }
```

4.3 HLD

```
ret = max(ret, segmax.query(1, n, 1, dfn[
        sz[x] += sz[i];
        if(sz[son[x]] < sz[i])
                                   son[x] = i;
                                                                 v], dfn[u]));
    }
}
                                                         return ret;
int top[N]; // 維護每個節點所在的鏈的頂端節點
                                                     }
int dfn[N], rnk[N]; // dfn -> node to seg, rnk ->
    tree to node
                                                     int getLca(int u, int v) {
int cnt = 1; // index start from 1
                                                         while(top[u] != top[v]){
void dfs_hld(int x, int f){
                                                              if(dep[top[u]] > dep[top[v]])
    top[x] = (son[fa[x]] == x ? top[fa[x]] : x);
                                                                  u = fa[top[u]];
    rnk[cnt] = x;
                                                              else
                                                                  v = fa[top[v]];
    dfn[x] = cnt++;
    if(son[x])
                  dfs_hld(son[x], x);
    for(int i : ed[x]){
                                                         return dep[u] > dep[v] ? v : u;
        if(i == f || i == son[x])
                                      continue;
                                                     }
        dfs_hld(i, x);
                                                     void solve()
    }
}
                                                          cin >> n;
int getSum(int u, int v) {
                                                         for(int i = 0; i < n - 1; i++) {</pre>
    int ret = 0;
                                                              int a, b;
    while(top[u] != top[v]){
                                                              cin >> a >> b;
                                                              ed[a].push_back(b);
        if(dep[top[u]] > dep[top[v]]) {
            int a = dfn[top[u]], b = dfn[u];
                                                              ed[b].push_back(a);
            if(a > b) swap(a, b);
                                                         }
            ret += segsum.query(1, n, 1, a, b);
                                                         dfs_sz(1, 1, 0);
            u = fa[top[u]];
                                                         dfs_hld(1, 1);
        }
                                                         vector<int> w(n + 1, 0);
        else {
                                                         for(int i = 1; i <= n; i++) {</pre>
            int a = dfn[top[v]], b = dfn[v];
                                                              cin >> w[dfn[i]];
            if(a > b) swap(a, b);
                                                         segmax.init(1, n, 1, w);
            ret += segsum.query(1, n, 1, a, b);
            v = fa[top[v]];
                                                         segsum.init(1, n, 1, w);
        }
                                                         int q;
                                                         cin >> q;
    if(dfn[u] < dfn[v]) {
                                                         while(q--) {
        ret += segsum.query(1, n, 1, dfn[u], dfn[
                                                              string op;
            v]);
                                                              cin >> op;
                                                              if(op == "QMAX") {
    else {
                                                                  int a, b;
        ret += segsum.query(1, n, 1, dfn[v], dfn[
                                                                  cin >> a >> b;
            u]);
                                                                  cout << getMax(a, b) << '\n';</pre>
                                                              else if(op == "QSUM") {
    return ret;
                                                                  int a, b;
}
                                                                  cin >> a >> b;
                                                                  cout << getSum(a, b) << '\n';</pre>
int getMax(int u, int v) {
                                                              }
                                                              else {
    int ret = -1e15;
    while(top[u] != top[v]){
                                                                  int a, t;
        if(dep[top[u]] > dep[top[v]]) {
                                                                  cin >> a >> t;
            int a = dfn[top[u]], b = dfn[u];
                                                                  segmax.update(1, n, 1, dfn[a], t);
            if(a > b) swap(a, b);
                                                                  segsum.update(1, n, 1, dfn[a], t);
            ret = max(ret, segmax.query(1, n, 1,
                                                              }
                                                         }
                a, b));
            u = fa[top[u]];
                                                         return;
        }
                                                     }
        else {
            int a = dfn[top[v]], b = dfn[v];
            if(a > b) swap(a, b);
                                                     4.4 Negative Cycle
            ret = max(ret, segmax.query(1, n, 1,
                a, b));
                                                     struct EDGE
            v = fa[top[v]];
        }
                                                       int first, second;
    if(dfn[u] < dfn[v]) {</pre>
                                                       long long val;
        ret = max(ret, segmax.query(1, n, 1, dfn[
            u], dfn[v]));
                                                     vector<EDGE> e;
    else {
```

```
long long dis[N];
int pre[N];
int bellman()
  int ret = 0;
  for(EDGE i: e)
    if(dis[i.second] > dis[i.first] + i.val)
      dis[i.second] = dis[i.first] + i.val;
      pre[i.second] = i.first;
      ret = i.second;
  }
  return ret;
bool vis[N];
void f_neg(int x)
  vector<int> ret;
  while(!vis[x])
    vis[x] = 1;
    ret.push_back(x);
    x = pre[x];
  ret.push_back(x);
  reverse(ret.begin(), ret.end());
  while(ret.back() != x)
    ret.pop_back();
  cout << "YES\n";</pre>
  for(int i: ret)
    cout << i << " ";
  cout << ' \ n';
}
int main()
  for(int i=1; i<=n-1; i++)</pre>
    bellman();
  int fin = bellman();
  if(fin)
   f_neg(fin);
  else
    cout << "NO\n";
}
```

4.5 Euler Tour

```
continue;
         vis[j] = 1;
         dfs(i);
         seq.push_back(i);
    }
}
void no()
{
    cout << "IMPOSSIBLE\n";</pre>
    exit(0);
}
int main()
    seq.reserve(m + 1);
    dfs(1);
    seq.push_back(1);
  for(int i=1; i<=n; i++)</pre>
    if(a[i].size() % 2)
      no();
  for(int i=0; i<m; i++)</pre>
    if(!vis[i])
      no();
  if(seq.front() != 1)
    no();
  reverse(seq.begin(), seq.end());
  for(int i: seq)
    cout << i << " ";
  cout << "\n";
}
```

4.6 Hamiltonian Routes

```
long long dp[1<<20][20];</pre>
vector<int> a[25];
int main()
{
    dp[1][0] = 1;
    for(int i=0; i<(1<<n); i++)</pre>
         for(int j=0; j<n; j++)</pre>
              if(!dp[i][j])
                  continue;
              for(int k: a[j])
              {
                  if((i>>k) & 1)
                       continue;
                  dp[i | (1 << k)][k] += dp[i][j];
                  dp[i | (1 << k)][k] %= mod;
              }
         }
    }
}
```

4.7 Dijkstra

```
{
                                                            }
        if(x.second != y.second)
             return x.second > y.second;
        return x.first > y.first;
    }
};
long long dis[N];
                                                       }
priority_queue<pii, vector<pii>, cmp> pq;
int main()
                                                       4.9 SCC kosaraju
{
    memset(dis, 0x3f, sizeof(dis));
    for(int i=1; i<=n; i++)</pre>
        sort(a[i].begin(), a[i].end(), [](pii x,
                                                       bitset<N> vis;
            pii y){return x.second < y.second;});</pre>
                                                       int SCC cnt;
                                                       int n, m;
    dis[1] = 0;
    for(pii i: a[1])
                                                       void dfs(int x)
        if(dis[i.first] <= i.second)</pre>
             continue;
                                                            vis[x] = 1;
        pq.push(i);
        dis[i.first] = i.second;
    }
                                                                dfs(i);
    while(!pq.empty())
                                                       }
        pii now = pq.top();
        pq.pop();
                                                       void dfs2(int x)
        if(dis[now.first] != now.second)
             continue;
                                                            vis[x] = 1;
        for(pii i: a[now.first])
        {
             long long dis now = i.second + now.
                                                                dfs2(i);
                 second;
                                                            }
             if(dis[i.first] <= dis_now)</pre>
                                                       }
                 continue;
             dis[i.first] = dis_now;
                                                       void kosaraju()
             pq.push({i.first, dis[i.first]});
        }
                                                                    dfs(i);
    for(int i=1; i<=n; i++)</pre>
                                                                }
        cout << dis[i] << " ";
    cout << "\n";
                                                            SCC cnt = 0;
}
                                                           vis = 0;
```

Floyd-Warshall

```
const int N = 505;
const long long INF = 0x3f3f3f3f3f3f3f3f3f;
long long dis[N][N];
int main()
{
    memset(dis, 0x3f, sizeof(dis));
    int n, m, q;
    cin >> n >> m >> q;
    for(int i=1; i<=n; i++)</pre>
        dis[i][i] = 0LL;
    for(int i=0, x, y, z; i<m; i++)</pre>
    {
        cin >> x >> y >> z;
        dis[x][y] = min(dis[x][y], 1LL * z);
        dis[y][x] = min(dis[y][x], 1LL * z);
```

```
for(int k=1; k<=n; k++)</pre>
    for(int i=1; i<=n; i++)</pre>
         for(int j=1; j<=n; j++)</pre>
              dis[i][j] = min(dis[i][j], dis[i
                  ][k] + dis[k][j]);
```

```
const int N = 1e5 + 10;
vector<int> ed[N], ed_b[N]; // 反邊
vector<int> SCC(N); // 最後SCC的分組
vector<int> pre; // 後序遍歷
    for(int i : ed[x]) {
        if(vis[i]) continue;
    pre.push_back(x);
    SCC[x] = SCC\_cnt;
    for(int i : ed_b[x]) {
        if(vis[i]) continue;
    for(int i = 1; i <= n; i++) {</pre>
        if(!vis[i]) {
    for(int i = n - 1; i >= 0; i--) {
        if(!vis[pre[i]]) {
            SCC_cnt++;
            dfs2(pre[i]);
        }
    }
}
```

Flow

5.1 Max Flow Dinic

```
const int N = 1100; // vertex
struct Dinic{
    struct Edge {
        int v, f, re;
    int n,s,t,level[N];
    vector<Edge> ed[N];
    void init(int _n, int _s, int _t){
```

```
s = _s;
        t = _t;
        for (int i = 0; i < n; i ++) ed[i].clear</pre>
    void add_edge(int u, int v, int f){
        ed[u].push_back({v, f, (int)ed[v].size()
        ed[v].push_back({u, 0, (int)ed[u].size()
            - 1});
    bool BFS(){
        for (int i = 0; i < n; i++) level[i] =</pre>
            -1;
        queue<int> que;
        que.push(s);
        level[s] = 0;
        while (!que.empty()){
            int u = que.front(); que.pop();
            for (auto it : ed[u]){
                 if (it.f > 0 && level[it.v] ==
                     level[it.v] = level[u]+1;
                     que.push(it.v);
                }
            }
        }
        return level[t] != -1;
    int DFS(int u, int nf){
        if (u == t) return nf;
        int res = 0;
        for (auto &it : ed[u]){
            if (it.f > 0 && level[it.v] == level[
                u]+1){
                 int tf = DFS(it.v, min(nf, it.f))
                res += tf;
                nf -= tf;
                it.f -= tf;
                ed[it.v][it.re].f += tf;
                if (nf == 0) return res;
        if (!res) level[u] = -1;
        return res;
    int flow(int res=0){
        while (BFS())
        res += DFS(s,2147483647);
        return res;
} flow;
```

5.2 Min Cost Max Flow

```
// 在最大流量的前題下最小花費
struct MinCostMaxFlow{
    typedef int Tcost;
    static const int MAXV = 5e3 + 10;
    static const int INFf = 1000000;
    const int INFc = 1e9;
    struct Edge{
        int v, cap;
        Tcost w;
        int rev;
        Edge(){}
        Edge(int t2, int t3, Tcost t4, int t5)
        : v(t2), cap(t3), w(t4), rev(t5) {}
```

```
int V, s, t;
    vector<Edge> g[MAXV];
    void init(int n, int _s, int _t){
        V = n; s = _s; t = _t;
        for(int i = 0; i <= V; i++) g[i].clear();</pre>
    void addEdge(int a, int b, int cap, Tcost w){
        g[a].push_back(Edge(b, cap, w, (int)g[b].
            size()));
        g[b].push_back(Edge(a, 0, -w, (int)g[a].
            size()-1));
    Tcost d[MAXV];
    int id[MAXV], mom[MAXV];
    bool inqu[MAXV];
    queue<int> q;
    pair<int, Tcost> solve(){ // Max Flow : Min
        int mxf = 0; Tcost mnc = 0;
        while(1){
             fill(d, d+1+V, INFc);
            fill(inqu, inqu+1+V, 0);
            fill(mom, mom+1+V, -1);
             mom[s] = s;
            d[s] = 0;
             q.push(s); inqu[s] = 1;
             while(q.size()){
                 int u = q.front(); q.pop();
                 inqu[u] = 0;
                 for(int i = 0; i < (int) g[u].</pre>
                     size(); i++){
                     Edge &e = g[u][i];
                     int v = e.v;
                     if(e.cap > 0 \&\& d[v] > d[u]+e
                         .w){
                         d[v] = d[u] + e.w;
                         mom[v] = u;
                         id[v] = i;
                         if(!inqu[v]) q.push(v),
                             inqu[v] = 1;
                     }
                 }
             if(mom[t] == -1) break;
             int df = INFf;
             for(int u = t; u != s; u = mom[u])
                 df = min(df, g[mom[u]][id[u]].cap
                    );
             for(int u = t; u != s; u = mom[u]){
                 Edge &e = g[mom[u]][id[u]];
                 g[e.v][e.rev].cap += df;
            mxf += df;
            mnc += df*d[t];
        return {mxf,mnc};
    }
}flow;
```

5.3 Min Cut

```
// add dinic
// 給定兩個點 start 和 end , 中間會有很多條路,
    問你說最小要刪除幾條路才可以保證 start 不能到
    end
vector<pair<int, int>> ans;
vector<int> vis(MXN);
```

```
void dfs(int x)
{
    vis[x] = 1;
    for(auto i : flow.ed[x]) {
        if(vis[i.v] == 1) continue;
        if(vis[i.v] == 0 && i.f > 0) {
            dfs(i.v);
        }
    }
vector<pair<int, int>> G;
void solve()
    int n, m;
    cin >> n >> m;
    flow.init(n + 1, 1, n);
    while(m--) {
        int a, b;
        cin >> a >> b;
        flow.add_edge(a, b, 1);
        flow.add_edge(b, a, 1);
        G.push_back({a, b});
        // flow.add_edge(b, a, 1);
    flow.flow();
    dfs(1);
    for(pair<int, int> i : G) {
        if((vis[i.first] == 1 && vis[i.second] ==
             0) || (vis[i.first] == 0 && vis[i.
            second] == 1)) ans.push_back(i);
    cout << ans.size() << '\n';</pre>
    for(auto i : ans) {
        cout << i.first << ' ' << i.second << '\n
    }
    return;
}
```

5.4 Maximum Bipartite Matching

```
// add dinic
// 左邊有 n 個點,右邊有 m 個點,共有 e 條邊
void solve()
{
    int n, m, e;
    cin >> n >> m >> e;
    flow.init(n + m + 10, n + m + 1, n + m + 2);
    while(e--) {
        int a, b;
        cin >> a >> b;
        flow.add_edge(a, b + n, 1);
    for(int i = 1; i <= n; i++) {</pre>
        flow.add edge(n + m + 1, i, 1);
    for(int i = n + 1; i <= n + m; i++) {</pre>
        flow.add_edge(i, n + m + 2, 1);
    cout << flow.flow() << '\n';</pre>
    return;
}
```

5.5 KM

```
const int N = 210;
```

```
const int INF = 1e9 + 7;
struct KM { // max weight, for min negate the
   weights
    int n, mx[N], my[N], pa[N];
    long long g[N][N], lx[N], ly[N], sy[N];
    bool vx[N], vy[N];
    vector<pair<int, int>> match;
    void init(int _n) { // 1-based
        n = _n;
        for(int i = 1; i <= n; i++) fill(g[i], g[</pre>
            i] + n + 1, 0);
    void addEdge(int x, int y, long long w) {
        g[x][y] = w;
    }
    void augment(int y) {
        for(int x, z; y; y = z) {
            x = pa[y], z = mx[x], my[y] = x, mx[x]
                ] = y;
        }
   void bfs(int st) {
        for(int i = 1; i <= n; ++i) sy[i] = INF,</pre>
            vx[i] = vy[i] = 0;
        queue<int> q;
        q.push(st);
        for(;;) {
            while(q.size()) {
                int x=q.front();
                q.pop();
                vx[x] = 1;
                for(int y = 1; y <= n; ++y) {
                     if(!vy[y]){
                         long long t = lx[x] + ly[
                             y] - g[x][y];
                         if(t == 0) {
                             pa[y] = x;
                             if(!my[y]){augment(y)
                                 ;return;}
                             vy[y]=1, q.push(my[y]
                         else if(sy[y]>t) pa[y]=x,
                             sy[y]=t;
                     }
                }
            long long cut = INF;
            for(int y = 1; y <= n; ++y) {</pre>
                if(!vy[y] && cut > sy[y]) {
                     cut = sy[y];
            for(int j = 1; j <= n; ++j) {</pre>
                if(vx[j]) lx[j] -= cut;
                 if(vy[j]) ly[j] += cut;
                else sy[j] -= cut;
            for(int y = 1; y <= n; ++y) {
                 if(!vy[y] && sy[y] == 0) {
                     if(!my[y]) {
                         augment(y);
                         return;
                     vy[y]=1;
                     q.push(my[y]);
                }
            }
        }
    long long solve(){
```

```
fill(mx, mx + n + 1, 0);
         fill(my, my + n + 1, 0);
         fill(ly, ly + n + 1, 0);
         fill(lx, lx + n + 1, -INF);
         for(int x = 1; x <= n; ++x) {</pre>
             for(int y = 1; y <= n; ++y) {
                 lx[x] = max(lx[x], g[x][y]);
         for(int x = 1; x \leftarrow n; ++x) bfs(x);
         long long ans = 0;
         for(int y = 1; y <= n; ++y) {</pre>
             ans += g[my[y]][y];
             match.push_back({my[y], y});
         }
         return ans;
    }
} graph;
```

6 Math

6.1 Matrix

```
const int MOD = 1e9 + 7;
typedef vector<vector<ll>>> matrix;
matrix operator*(matrix A, matrix B)
{
    const int n = A.size(), m = B.size(), o = B
        [0].size();
    matrix ret(n, vector<ll>(0, 0));
    for(int i = 0; i < n; i++) {</pre>
        for(int j = 0; j < o; j++) {</pre>
             for(int k = 0; k < m; k++) {
                 ret[i][j] += A[i][k] * B[k][j];
                 ret[i][j] %= MOD;
             }
        }
    return ret;
}
matrix power(matrix A, int n)
    matrix ans(A.size(), vector<ll>(A.size(), 0))
    for(int i = 0; i < A.size(); i++) ans[i][i] =</pre>
         1;
    while(n) {
        if(n \& 1) ans = ans * A;
        A = A * A;
        n >>= 1;
    return ans;
}
```

6.2 Combination

```
int c[n + 1][n + 1];
for(int i = 0; i < n; i++) {
    c[i][i] = 1;
    c[i][0] = 1;
}
for(int i = 2; i <= n; i++) {
    for(int j = 1; j <= i - 1; j++) {
        c[i][j] = c[i - 1][j] + c[i - 1][j - 1];
        c[i][i - j] = c[i - 1][j] + c[i - 1][j - 1];
    }
}</pre>
```

```
const int N = 1e6 + 10;
const int mod = 1e9 + 7;
int fac[N], fac_inv[N];
void init()
    fac[0] = 1;
    for(int i = 1; i < N; i++) {</pre>
        fac[i] = fac[i - 1] * i % mod;
    fac_inv[N - 1] = power(fac[N - 1], mod - 2,
       mod);
    for(int i = N - 2; i >= 0; i--) {
        fac_inv[i] = fac_inv[i + 1] * (i + 1) %
            mod;
    }
}
int C(int n, int m)
    return fac[n] * fac_inv[m] % mod * fac_inv[n
        - m] % mod;
}
```

6.3 Exponentiation

```
int power(int a, int b, int m) // (a ^ b) % m
{
    a %= m;
    int ret = 1 % m;
    for(; b; b >>= 1) {
        if(b & 1) ret = ret * a % m;
        a = a * a % m;
    }
    return ret;
}
```

6.4 Unique factorization domain

```
const int N = 1e4 + 10;
vector<int> prime;
vector<int> vis(N);
vector<int> prime_count(N); // 算最後的次方
void add_integer(int n, int d)
    for(int i = 0; i < prime.size(); i++) {</pre>
        while(n % prime[i] == 0) {
             n /= prime[i];
            prime_count[i] += d;
        if(n == 1) break;
    }
}
void add_factorial(int n, int d) // n ^ d
{
    for(int i = 1; i <= n; i++) {</pre>
        add_integer(i, d);
    }
}
void solve()
{
    for(int i = 2; i <= 10000; i++) {</pre>
        if(!vis[i]) prime.push_back(i);
```

```
for(int j = i * 2; j <= 10000; j += i)</pre>
            vis[j] = 1;
                                                        return 1;
    // main code
                                                     }
    // 對於很多數字一起相乘可使用
                                                      int c;
    // add_factorial->階層
                                                      cin >> c;
    // 求解
    double ans = 1;
    for(int i = 0; i < prime.size(); i++) ans *=</pre>
                                                      else{
        pow(prime[i], prime_count[i]);
    cout << fixed << setprecision(5) << ans << '\</pre>
       n';
    return:
}
```

6.5 Quick Mul

```
11 qMul(ll a,ll b,ll mod){
    11 \text{ ans} = 0;
    while(b){
         if(b\&1) ans = (ans+a)%mod;
         a = (a+a)\% mod;
         b>>=1;
    return ans;
}
// 0(1)
11 qMul(11 x,11 y,11 mod){
    11 \text{ ret} = x * y - (11)((long double)x / mod *
        y) * mod;
    return ret<0?ret+mod:ret;</pre>
}
```

6.6 Miller Rabin

```
// n < 4,759,123,141
                             3: 2, 7, 61
                            4: 2, 13, 23,
// n < 1,122,004,669,633
   1662803
// n < 3,474,749,660,383
                                   6 : pirmes <=
   13
// n < 2<sup>64</sup>
// 2, 325, 9375, 28178, 450775, 9780504,
   1795265022
ll magic[] = {};
bool witness(ll a,ll n,ll u,int t){
 if(!a) return 0;
 11 x = power(a, u, n);
 for(int i = 0; i < t; i++) {</pre>
    11 nx = qMul(x, x, n);
    if(nx == 1 && x != 1 && x != n - 1) return 1;
   x = nx;
 }
 return x != 1;
bool miller_rabin(ll n) {
 int s = (magic size); // init
  // iterate s times of witness on n
 if(n < 2) return 0;</pre>
 if(!(n & 1)) return n == 2;
 11 u = n - 1; int t = 0;
 // n-1 = u*2^t
 while(!(u & 1)) u >>= 1, t++;
 while(s--){
    11 a = magic[s] % n;
```

```
if(witness(a, n, u, t)) return 0;
if(miller_rabin(c)){
    cout << "prime\n";</pre>
    cout << "not_prime\n";</pre>
```

6.7 Pollard's Rho

```
11 add(l1 x, l1 y, l1 p) {
    return (x + y) \% p;
11 f(11 x, 11 mod) { return add(qMul(x,x,mod),1,
    mod); }
ll pollard_rho(ll n) {
  if(!(n & 1)) return 2;
    while(true) {
        11 y = 2, x = rand() % (n - 1) + 1, res =
        for(int sz = 2; res == 1; sz *= 2) {
             for(int i = 0; i < sz && res <= 1; i</pre>
                ++) {
                 x = f(x, n);
                 res = \_gcd(llabs(x - y), n);
            y = x;
        if (res != 0 && res != n) return res;
    }
}
vector<ll> ret;
void fact(ll x) {
    if(miller_rabin(x)) {
        ret.push_back(x);
        return;
    ll f = pollard rho(x);
    fact(f); fact(x / f);
}
```

Sum of Powers Formulas and Expansions

```
\sum_{i=0}^{n} i^{p} = \sum_{i=0}^{n} (n-i) ((i+1)^{p} - i^{p})
p=1:
                               \sum_{i=0}^{n} i = \frac{n(n+1)}{2} = \frac{n^2 + n}{2}
    p=2:
                   \sum_{i=0}^{n} i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{2n^3 + 3n^2 + n}{6}
    p=3:
                      \sum_{i=0}^{n} i^3 = \left(\frac{n(n+1)}{2}\right)^2 = \frac{n^4 + 2n^3 + n^2}{4}
```

```
p = 4:
\sum_{i=0}^{n} i^{4} = \frac{n(n+1)(2n+1)(3n^{2}+3n-1)}{30} = \frac{6n^{5}+15n^{4}+10n^{3}-n}{30}
p = 5:
\sum_{i=0}^{n} i^{5} = \frac{n^{2}(n+1)^{2}(2n^{2}+2n-1)}{12} = \frac{2n^{6}+6n^{5}+5n^{4}-n^{2}}{12}
```

```
/* 12721 13331 14341 75577 123457 222557 556679 999983 1097774749 1076767633 100102021 999997771 1001010013 1000512343 987654361 999991231 999888733 98789101 987777733 999991921 1010101333 1010102101 1000000000039 100000000000037 2305843009213693951 4611686018427387847 9223372036854775783 18446744073709551557 */
```

6.9 ax+by=gcd(a,b)

```
pair<int,int> extgcd(int a, int b){
    if (b == 0) return {1, 0};
    int k = a / b;
    pair<int, int> p = extgcd(b, a - k * b);
    return {p.second, p.first - k * p.second};
}
```

6.10 Discrete Sqrt

```
void calcH(long long &t, long long &h, const long
    long p) {
  long long tmp=p-1;
    for(t = 0; (tmp & 1) == 0; tmp /= 2) t++;
    h = tmp;
// solve equation x^2 \mod p = a
bool solve(long long a, long long p, long long &x
   , long long &y) {
  if(p == 2) {
       x = y = 1;
        return true;
  int p2 = p / 2, tmp = power(a, p2, p);
  if (tmp == p - 1) return false;
 if ((p + 1) % 4 == 0) {
   x = power(a, (p + 1) / 4,p);
        y = p - x;
        return true;
    else {
    long long t, h, b, pb;
       calcH(t, h, p);
    if (t >= 2) {
      do {
                b = rand() \% (p - 2) + 2;
      } while (power(b, p / 2, p) != p - 1);
      pb = power(b, h, p);
        int s = power(a, h / 2, p);
    for (int step = 2; step <= t; step++) {</pre>
      int ss = (((long long)(s * s) % p) * a) % p
      for(int i = 0; i < t - step; i++) ss = qMul</pre>
          (ss, ss, p);
      if(ss + 1 == p) s = (s * pb) % p;
            pb = ((long long)pb * pb) % p;
        x = ((long long)s * a) % p;
        y = p - x;
    return true;
}
```

6.12 Gauss

```
// O(n^3)
const double EPS = 1e-9;
const int INF = 100; // it doesnt actually have
    to be infinity or a big number
// return meaning
// one solution : 1
// inf solution : INF
// no solution : 0
int gauss (vector < vector < double > > a, vector <</pre>
    double> & ans) {
    int n = (int) a.size();
    int m = (int) a[0].size() - 1;
    vector<int> where (m, -1);
    for (int col=0, row=0; col<m && row<n; ++col)</pre>
         {
         int sel = row;
         for (int i=row; i<n; ++i)</pre>
             if (abs (a[i][col]) > abs (a[sel][col
                  sel = i;
         if (abs (a[sel][col]) < EPS)</pre>
             continue;
         for (int i=col; i<=m; ++i)</pre>
             swap (a[sel][i], a[row][i]);
         where[col] = row;
         for (int i=0; i<n; ++i)</pre>
             if (i != row) {
                  double c = a[i][col] / a[row][col]
                      ];
                  for (int j=col; j<=m; ++j)</pre>
                      a[i][j] -= a[row][j] * c;
             }
         ++row;
    ans.assign (m, 0);
    for (int i=0; i<m; ++i)</pre>
         if (where[i] != -1)
             ans[i] = a[where[i]][m] / a[where[i
                 ]][i];
    for (int i=0; i<n; ++i) {</pre>
         double sum = 0;
         for (int j=0; j<m; ++j)</pre>
             sum += ans[j] * a[i][j];
         if (abs (sum - a[i][m]) > EPS)
             return 0;
    for (int i=0; i<m; ++i)</pre>
         if (where[i] == -1)
             return INF;
    return 1;
}
```

6.13 FFT

```
// 多項式乘法a*b=ans
const int MAXN = 262144;
// (must be 2^k)
// 262144, 524288, 1048576, 2097152, 4194304
// before any usage, run pre_fft() first
typedef long double ld;
typedef complex<ld> cplx; //real() ,imag()
const ld PI = acosl(-1);
const cplx I(0, 1);
cplx omega[MAXN+1];
void pre_fft(){
    for(int i=0; i<=MAXN; i++) {</pre>
        omega[i] = exp(i * 2 * PI / MAXN * I);
}
// n must be 2^k
void fft(int n, cplx a[], bool inv=false){
    int basic = MAXN / n;
    int theta = basic;
    for (int m = n; m >= 2; m >>= 1) {
        int mh = m >> 1;
        for (int i = 0; i < mh; i++) {</pre>
            cplx w = omega[inv ? MAXN - (i *
                theta % MAXN) : i * theta % MAXN
                ];
            for (int j = i; j < n; j += m) {</pre>
                 int k = j + mh;
                 cplx x = a[j] - a[k];
                 a[j] += a[k];
                 a[k] = w * x;
            }
        theta = (theta * 2) % MAXN;
    int i = 0;
    for (int j = 1; j < n - 1; j++) {</pre>
        for (int k = n >> 1; k > (i ^= k); k >>=
        if (j < i) swap(a[i], a[j]);</pre>
    if(inv) {
        for (i = 0; i < n; i++) a[i] /= n;</pre>
cplx arr[MAXN + 1];
inline void mul(int _n,long long a[],int _m,long
   long b[],long long ans[]){
    int n=1, sum = _n + _m - 1;
    while(n < sum) n <<= 1;</pre>
    for(int i = 0; i < n; i++) {</pre>
        double x = (i < _n ? a[i] : 0), y = (i < _m 
            ? b[i] : 0);
        arr[i] = complex < double > (x + y, x - y);
    fft(n, arr);
    for(int i = 0; i < n; i++) arr[i]=arr[i]*arr[</pre>
        i];
    fft(n,arr,true);
    for(int i=0;i<sum;i++) ans[i]=(long long int)</pre>
        (arr[i].real() / 4 + 0.5);
}
long long a[MAXN];
long long b[MAXN];
long long ans[MAXN];
int a_length;
int b_length;
```

6.14 Theorem

- Lucas' Theorem : For $n,m\in\mathbb{Z}^*$ and prime P, C(m,n) mod $P=\Pi(C(m_i,n_i))$ where m_i is the i-th digit of m in base P.
- Stirling approximation : $n! \approx \sqrt{2\pi n} (\frac{n}{\epsilon})^n e^{\frac{1}{12n}}$
- Stirling Numbers(permutation |P|=n with k cycles): S(n,k)= coefficient of x^k in $\Pi_{i=0}^{n-1}(x+i)$
- Stirling Numbers(Partition n elements into k nonempty set):

$$S(n,k) = \frac{1}{k!} \sum_{j=0}^{k} (-1)^{k-j} {k \choose j} j^n$$

- Pick's Theorem : A=i+b/2-1 A: Area i: grid number in the inner b: grid number on the side
- Catalan number : $C_n = \binom{2n}{n}/(n+1)$ $C_n^{n+m} C_{n+1}^{n+m} = (m+n)! \frac{n-m+1}{n+1}$ for $n \geq m$ $C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!}$ $C_0 = 1$ and $C_{n+1} = 2(\frac{2n+1}{n+2})C_n$ $C_0 = 1$ and $C_{n+1} = \sum_{i=0}^n C_i C_{n-i}$ for $n \geq 0$
- Euler Characteristic: planar graph: V-E+F-C=1 convex polyhedron: V-E+F=2 V,E,F,C: number of vertices, edges, faces(regions), and components
- Kirchhoff's theorem : $A_{ii}=deg(i), A_{ij}=(i,j)\in E$?-1:0, Deleting any one row, one column, and cal the det(A)
- Polya' theorem (c is number of color' m is the number of cycle size): $(\sum_{i=1}^m c^{gcd(i,m)})/m$
- Burnside lemma: $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
- 錯排公式: (n 個人中,每個人皆不再原來位置的組合數): dp[0] = 1; dp[1] = 0; dp[i] = (i-1)*(dp[i-1] + dp[i-2]);
- Bell 數 (有 n 個人,把他們拆組的方法總數): $B_0=1$ $B_n=\sum_{k=0}^n s(n,k)$ (second-stirling) $B_{n+1}=\sum_{k=0}^n \binom{n}{k} B_k$
- Wilson's theorem : $(p-1)! \equiv -1 (mod \ p)$
- Fermat's little theorem : $a^p \equiv a (mod \ p)$
- Euler's totient function: $A^{B^C} \bmod \ p = pow(A, pow(B, C, p-1)) \bmod \ p$
- 歐拉函數降冪公式: $A^B \mod C = A^{B \mod \phi(c) + \phi(c)} \mod C$
- 6 的倍數: $(a-1)^3 + (a+1)^3 + (-a)^3 + (-a)^3 = 6a$

7 Geometry

7.1 Structure

```
using TYPE = int;
struct Pt {
    TYPE x, y;
};
struct Line{
    Pt st, ed;
```

|}

```
};
struct Circle{
    Pt o; // center
    TYPE r; // radius
};
struct poly{
    int n; // n 邊形
    vector<Pt> pts;
};
```

7.2 Vector

```
using TYPE = int;
struct Pt {
   TYPE x, y;
    Pt(TYPE _x = 0, TYPE _y = 0):x(_x), y(_y) {}
    Pt operator+(const Pt &a){
        return Pt(x + a.x, y + a.y);
    Pt operator-(const Pt &a){
        return Pt(x - a.x, y - a.y);
    Pt operator*(const TYPE &a){
        return Pt(x * a, y * a);
    }
    Pt operator/(const TYPE &a){
        return Pt(x / a, y / a);
    TYPE operator*(const Pt &a){ //計算幾何程式碼
       中內積通常用*表示
        return x * a.x + y * a.y;
    TYPE operator^(const Pt &a){ //計算幾何程式碼
       中外積通常用^表示
        return x * a.y - y * a.x;
    bool operator<(const Pt &a) const { // 判斷兩
       點座標 先比 x 再比 y
        return x < a.x \mid \mid (x == a.x \&\& y < a.y);
    }
};
```

7.3 Collinear

```
bool collinearity(const Pt& a, const Pt& b, const
   Pt& c){
   return (b - a) ^ (c - a) == 0;
}
bool collinearity(const Pt& a, const Pt& b, const
   Pt& c){
   return (b - a) ^ (c - a) < EPS;
}</pre>
```

7.4 InLine

```
bool inLine(const Pt& p, const Line& li){
    return collinearity(li.st, li.ed, p) && (li.
        st - p) * (li.ed - p) < 0;
}
bool inLine(const Pt& p, const Line& li){
    return collinearity(li.st, li.ed, p) && (li.
        st - p) * (li.ed - p) < EPS;</pre>
```

7.5 Convex Hull

```
struct Pt {
    int x, y;
    Pt(){}
    Pt(int _x, int _y) {
        x = _x, y = _y;
    Pt operator-(const Pt &a) {
        return Pt(x - a.x, y - a.y);
    bool operator<(const Pt &a) const {</pre>
        return x < a.x || (x == a.x && y < a.y);
    }
};
int cross(Pt& o, Pt& a, Pt& b) {
    Pt 1hs = o - a, rhs = o - b;
    return lhs.x * rhs.y - lhs.y * rhs.x;
}
vector<Pt> convex_hull(vector<Pt> hull){
    sort(hull.begin(), hull.end());
    int top = 0;
    vector<Pt> stk;
    for(int i = 0; i < hull.size(); i++) {</pre>
        while(top >= 2 && cross(stk[top - 2], stk
            [top - 1], hull[i]) <= 0)
             stk.pop_back(), top--;
        stk.push_back(hull[i]);
        top++;
    for(int i = hull.size() - 2, t = top + 1; i
        >= 0; i--) {
        while(top >= t && cross(stk[top - 2], stk
            [top - 1], hull[i]) <= 0)
            stk.pop_back(), top--;
        stk.push_back(hull[i]);
        top++;
    stk.pop_back();
    return stk;
}
```

8 String

8.1 Trie

```
void build(string &s)
{
    int n = s.size();
    for(int i=0, v=0; i<n; i++)
    {
        pii &now = a[v][s[i]-'a'];
        if(now.first != -1)
            v = now.first;
    else
        v = now.first = ++idx;
    if(i == n-1)
            now.second++;
    }
}</pre>
```

8.2 Hash

8.3 Z Function

```
// 一個字串的後綴可以和字串本身匹配到多長從第i項
   開始一路到n-1
inline vector<int> z_function(string s)
    int n = s.size();
    vector<int> z(n, 0);
    for(int i = 1, l = 0, r = 0; i < n; i++) {</pre>
        if(i <= r && z[i - 1] < r - i + 1) {</pre>
           z[i] = z[i - 1];
       }
        else {
            z[i] = \max(0, r - i + 1);
           while(i + z[i] < n \&\& s[z[i]] == s[i]
               + z[i]]) z[i]++;
        if(i + z[i] - 1 > r) l = i, r = i + z[i]
           - 1;
    }
    return z;
}
```